

Stability of charged sulfur vacancies in 2D and bulk MoS₂ from plane-wave density functional theory with electrostatic corrections

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(Dated: October 11, 2020)

Two-dimensional (2D) semiconducting transition metal dichalcogenides such as MoS₂ have attracted extensive research interests for potential applications in optoelectronics, spintronics, photovoltaics, and catalysis. To harness the potential of these materials for electronic devices requires a better understanding of how defects control the carrier concentration, character, and mobility. Utilizing a correction scheme developed by Freysoldt and Neugebauer to ensure the appropriate electrostatic boundary conditions for charged defects in 2D materials, we perform density functional theory calculations to compute formation energies and charge transition levels associated with sulfur vacancies in monolayer and layered bulk MoS₂. We investigate the convergence of these defect properties with respect to vacuum spacing, in-plane supercell dimensions, and different levels of theory. We also analyze the electronic structures of the defects in different charge states to gain insights into the effect of defects on bonding and magnetism. We predict that both vacancy structures undergo a Jahn-Teller distortion, which helps stabilize the sulfur vacancy in the -1 charged state.

I. INTRODUCTION

Two-dimensional (2D) semiconductor materials, such as transition metal dichalcogenides (TMDCs), monochalcogenides, group III-V compounds, and phosphorene, have attracted extensive research interests for potential applications in optoelectronics, spintronics, photovoltaics, and catalysis [1–18]. One of the most commonly used and promising 2D semiconductor materials is the prototypical TMDC material, molybdenum disulfide (MoS₂), which has demonstrated interesting electronic, optical, and mechanical properties, making it a promising candidate for optoelectronic and catalytic applications [1, 2, 19–21]. Monolayer MoS₂ can be directly grown on substrates using chemical vapor deposition [22] or exfoliated from its layered bulk counterpart via micromechanical [2, 23] or liquid-phase [24, 25] exfoliation techniques. In this work, we focus on the semiconducting trigonal prismatic 1H-MoS₂ phase and its layered bulk counterpart, 2H-MoS₂.

Just as in bulk semiconductors, 2D semiconductors contain both intrinsic defects, *e.g.*, vacancies and antisites, as well as extrinsic defects, *e.g.*, substitutional and interstitial dopants and impurities. These defects are often charged and can also interact to form pairs or complexes. The lower dimensionality of 2D materials reduces the electronic screening, and hence point defects are expected to have an even stronger impact on the electronic properties of these systems compared to in bulk semiconductors. Understanding the effect of defects, dopants, and impurities on the electronic properties is crucial for the selection of materials and the choice of suitable synthesis and processing conditions. Accurate determination of defect formation energies and charge transition levels (CTLs) enables us to predict their effect on the electronic properties and how they respond to changes in synthesis and processing, allowing

for some control over the defect concentrations, and hence to tailor the carrier concentration, character, and mobility in 2D materials [26–29].

Unfortunately, experimental data of defect concentrations are scarce due to the difficulty of measuring defects in low-dimensional systems and establishing and maintaining thermodynamic equilibrium in these systems. Exciton emission peaks associated with defect states within the bandgap have been observed in the photoluminescence spectra of MoS₂ [30–32]; however, the type and nature of the defects responsible for such peaks are not directly known and have to be inferred by comparison against computational predictions of defect levels. This highlights the importance of accurate computational studies of defect levels and formation energies to complement experimental observations to better understand the effect of defects, dopants, and impurities on the electronic properties of emerging 2D semiconductor materials.

Density functional theory (DFT) calculations of point defects in solids is a mature field with a proven record of experimentally validated predictions [33]. Similar approaches may be applied to point defects in 2D materials as well; however, additional care must be taken to ensure the appropriate electrostatic boundary conditions for charged defects in 2D materials when applying DFT methods utilizing plane-wave basis sets and periodic boundary conditions. Several previous computational studies on defects and dopants in MoS₂ considered neutral defects [34, 35], or employed the Lany-Zunger (modified Markov-Payne) correction [36–38], or a uniform scaling scheme [39–41] to treat the charged defects.

In this work, we use the 2D charge correction scheme developed recently by Freysoldt and Neugebauer [42] – which has an advantage of not requiring any extrapolation or prior knowledge of scaling laws – to compute the formation energies and CTLs associated with the single S vacancy in both monolayer and layered bulk MoS₂. The S vacancy has been observed directly by high-resolution transmission electron microscopy [43–45] and scanning tunneling microscopy [46] and has been predicted to have one of the lowest forma-

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tion energies compared to other intrinsic defects [34, 40, 41]. Since the S vacancy is one of the more well-studied defects in MoS₂, we use it here to validate and benchmark this new charge correction scheme for 2D monolayers as well as the SCAN+rVV10 functional [47].

The paper is organized as follows. Sec. II lays out the DFT computational details and benchmarks the calculated structural and electronic properties of the pristine monolayer and layered bulk MoS₂ against other computational and experimental studies. In Sec. III, we present the defect formation energies and CTls for the S vacancy defect in monolayer and layered bulk MoS₂ and demonstrate the effectiveness of the Freysoldt-Neugebauer 2D charge correction scheme when applied to these systems. We predict that the S vacancy in both systems is most stable in either the neutral or -1 charged states, in agreement with other studies in literature, validating our approach. In Sec. IV, we analyze the electronic structures of the S vacancy in the various charge states. The -1 charged S vacancy is found to undergo a Jahn-Teller distortion, which stabilizes this defect in both monolayer and layered bulk MoS₂.

II. COMPUTATIONAL DETAILS

We compute the material and defect properties using density functional theory (DFT) with the projector-augmented wave (PAW) method [48, 49] as implemented in the plane-wave code VASP [50]. The PAW potentials describe the core states of Mo and S by the electronic configurations of [Ar]4s²3d¹⁰ and [Ne], respectively. We treat the exchange-correlation using two different sets of functionals – the Perdew-Burke-Ernzerhof (PBE) [51] generalized gradient approximation (GGA) functional and the strongly constrained and appropriately normed (SCAN) [52] meta-GGA functional – and compare the results. For the calculations with SCAN, we also include long-range van der Waals interactions via the SCAN+rVV10 functional [47]. We perform spin-polarized calculations employing a plane-wave cutoff energy of 520 eV, which ensures energy convergence to within 1 meV/atom. To facilitate rapid convergence of the Brillouin zone integration, we use Methfessel-Paxton smearing [53] with a smearing energy width of 0.10 eV and a Γ -centered Monkhorst-Pack k -point meshes [54]. For the structural relaxations, we use k -point meshes corresponding to a $12 \times 12 \times 1$ k -point mesh per hexagonal unit cell for monolayer MoS₂ (≈ 400 k -points per reciprocal atom in 2D) and $12 \times 12 \times 3$ k -point mesh per hexagonal unit cell for layered bulk MoS₂ (≈ 2500 k -points per reciprocal atom in 3D). For the density of states calculations, we double the density of the k -point meshes in all directions and use Gaussian smearing with a reduced smearing width of 0.02 eV.

We model the defective systems by constructing $3 \times 3 \times 1$, $4 \times 4 \times 1$, and $5 \times 5 \times 1$ supercells based on the hexagonal primitive unit cell, as well as $3 \times 2 \times 1$ and $4 \times 2 \times 1$ supercells based on an orthorhombic unit cell, and removing a single S atom to create a S vacancy. For monolayer MoS₂, in addition to varying the in-plane supercell size, we also vary the amount

of vacuum spacing between layers to be 10, 15, or 20 Å. We explicitly allow for symmetry breaking during the relaxation of the defect structures by turning off the symmetrization of the electronic charge density. Spin-orbit coupling was considered in a few select calculations and was found to change the defect formation energies by only 10 to 15 meV and to lead to a splitting of about 140 meV at the top of the valence band and of about 70 meV of the S vacancy defect level in monolayer MoS₂. While not insignificant, the effects are not so large as to qualitatively change our conclusions; therefore, the following results presented in this paper are reported without including spin-orbit coupling.

The formation energy $E^f[X^q]$ of a point defect X with charge q is determined from DFT calculations using a supercell approach following

$$E^f[X^q] = E_{\text{tot}}[X^q] - E_{\text{tot}}[\text{pristine}] - \sum_i n_i \mu_i + qE_F + E_{\text{corr}}, \quad (1)$$

where $E_{\text{tot}}[X^q]$ and $E_{\text{tot}}[\text{pristine}]$ are the total DFT-derived energies of the supercell containing the defect X and the pristine supercell respectively, n_i is the number of atoms of species i added/removed by the defect, μ_i is the corresponding chemical potential of the species, and E_F is the Fermi energy. In this work, we considered only the Mo-rich/S-poor limit, for which the appropriate S chemical potential $\mu_S(\text{S-poor}) = (\mu_{\text{MoS}_2} - \mu_{\text{Mo}(\text{bcc})})/2$. The final term in Eq. (1), E_{corr} , contains corrections to the formation energy due to electrostatic interactions with periodic images and compensating background charges, which are introduced in supercell calculations using plane-wave DFT approaches. In VASP specifically, a homogeneous compensating background charge delocalized throughout the entire supercell is implicitly included by setting the average electrostatic potential in the supercell to zero. Various correction schemes have been developed for charged defects in bulk 3D materials [36, 39, 55–61]. In this work, we use the approach developed by Freysoldt, Neugebauer, and Van de Walle [58, 59] to study the S vacancy in layered bulk MoS₂.

Charged defects in single-layer materials pose additional challenges that lead to the divergence of the energy with vacuum spacing. Komsa *et al.* proposed a uniform scaling scheme for charged defects at surfaces and interfaces [62] and in 2D materials [63]. In this work, we study the S vacancy in monolayer MoS₂ using the correction scheme developed recently by Freysoldt and Neugebauer [42]. The Freysoldt-Neugebauer scheme uses a surrogate model to directly correct the electrostatic energy induced by the wrong electrostatic boundary conditions. This scheme is computationally efficient as it is implemented as a post-processing step, requiring as input only the electrostatic potential of the converged DFT calculations. The correction scheme proposed by Freysoldt and Neugebauer has the advantage of not requiring any extrapolation or making assumptions about the finite-size scaling behavior, which would require the evaluation of large supercells to recover the correct asymptotic behavior [64].

Table I compares the lattice parameters, band gaps, and dielectric coefficients for monolayer and layered bulk MoS₂ computed in this work with experimental values. The PBE

TABLE I. Lattice constants, band gaps, and dielectric coefficients for monolayer and layered bulk MoS₂ calculated using different functionals, compared with experimental values. The PBE and SCAN+rVV10 values are calculated in this work, while the HSE values are taken from the literature. The in-plane lattice parameter a is well-reproduced by the PBE and SCAN functionals, with SCAN+rVV10 also reproducing the c lattice parameter (i.e., the interlayer spacing) in the layered bulk MoS₂. PBE and HSE functionals fail to reproduce this interlayer distance due to missing van der Waals interactions, therefore the c lattice parameter is fixed to the experimental value (values marked with *). As expected, both PBE and SCAN functionals significantly underestimate the band gaps by about 0.8 to 1.0 eV in the monolayer and 0.3 to 0.4 eV in the layered bulk.

	a (Å)	c (Å)	d_{S-S} (Å)	E_{gap} (eV)	$\varepsilon_{\parallel}(\varepsilon_0)$	$\varepsilon_{\perp}(\varepsilon_0)$
ML MoS₂:						
PBE	3.18	—	3.12	1.67		17.18
SCAN+rVV10	3.17	—	3.11	1.80		16.27
HSE	3.16[40]	—		2.17, 2.21[40], 2.25[65], 2.3[66]		
Expt.	3.2±0.1[46, 67]	—		2.40±0.05[67], 2.63[68], 2.7[69]		
bulk MoS₂:						
PBE@expt. c	3.18	12.30*	3.12	0.88	15.39	6.51
SCAN+rVV10	3.16	12.30	3.11	0.98	14.80	5.15
HSE@expt. c	3.16[40]	12.30*[40]		1.45, 1.47[40], 1.50 [66] 1.17[72], 1.2[73, 74], 1.23[75], 1.29[76]		
Expt.	3.15[70], 3.16[71]	12.29[71], 12.3[70]			15.2±0.2[77]	6.2±0.1[77]

and SCAN+rVV10 values are calculated in this work, while the HSE values are taken from Refs. 40, 65, and 66. All functionals well reproduce the in-plane lattice parameter a , with SCAN+rVV10 also reproducing the experimental c lattice parameter (i.e., the interlayer spacing) in the layered bulk MoS₂. PBE and HSE functionals significantly overpredict the interlayer distance in layered bulk MoS₂ due to missing van der Waals interactions; therefore the c lattice parameter is fixed to the experimental value in subsequent calculations. As expected, both PBE and SCAN functionals significantly underestimate the fundamental band gaps by about 30–40% in the monolayer [67–69] and 20–30% in the layered bulk [72–76]. Some studies report good agreement between PBE-computed band gaps and experimentally-measured *optical* band gaps; however, this is misleading as the appropriate comparison is with the *fundamental* band gap as is reported here. Despite underestimating the fundamental band gaps, it is still worth noting that PBE and SCAN do qualitatively reproduce the key features of the band structure, showing the indirect-to-direct band gap transition when going from the layered bulk to monolayer MoS₂.

The charge correction scheme requires the dielectric properties as input [42, 58, 59]. We compute the dielectric tensor components for the monolayer with DFT using supercells containing a slab of thickness d^{slab} and a vacuum region of thickness d^{vac} ($d^{\text{slab}} + d^{\text{vac}} = d^{\text{sc}}$ = supercell c lattice parameter). As a result, the computed dielectric tensor components for the supercell ε^{sc} are combinations of the dielectric tensor components for the monolayer $\varepsilon^{\text{slab}}$ and vacuum ε^{vac} (= 1). The in-plane components (subscripted \parallel) behave as capacitors in parallel, while the out-of-plane components (subscripted \perp) behave as capacitors in series, yielding the following relations [78]:

$$\varepsilon_{\parallel}^{\text{sc}} = \frac{d^{\text{vac}}}{d^{\text{sc}}} \varepsilon^{\text{vac}} + \frac{d^{\text{slab}}}{d^{\text{sc}}} \varepsilon_{\parallel}^{\text{slab}} = 1 + (\varepsilon_{\parallel}^{\text{slab}} - 1) \frac{d^{\text{slab}}}{d^{\text{sc}}} \quad (2)$$

$$\frac{1}{\varepsilon_{\perp}^{\text{sc}}} = \frac{d^{\text{vac}}}{d^{\text{sc}}} \frac{1}{\varepsilon^{\text{vac}}} + \frac{d^{\text{slab}}}{d^{\text{sc}}} \frac{1}{\varepsilon_{\perp}^{\text{slab}}} = 1 + \left(\frac{1}{\varepsilon_{\perp}^{\text{slab}}} - 1 \right) \frac{d^{\text{slab}}}{d^{\text{sc}}}. \quad (3)$$

The dielectric tensor components for the slab $\varepsilon_{\parallel}^{\text{slab}}$ and $\varepsilon_{\perp}^{\text{slab}}$ are only uniquely defined for a given choice of slab thickness d^{slab} . To solve for a unique combination of slab thickness and dielectric constants, we make the simplifying assumption that $\varepsilon_{\parallel}^{\text{slab}} = \varepsilon_{\perp}^{\text{slab}}$, i.e., that the slab is dielectrically isotropic. This gives the following expression for the slab dielectric constant [78],

$$\varepsilon^{\text{slab}} = \frac{\varepsilon_{\parallel}^{\text{sc}} - 1}{1 - (\varepsilon_{\perp}^{\text{sc}})^{-1}} \quad (4)$$

and the corresponding slab thickness,

$$d^{\text{slab}} = d^{\text{sc}} \left(\frac{1}{1 - (\varepsilon_{\perp}^{\text{sc}})^{-1}} + \frac{1}{1 - \varepsilon_{\parallel}^{\text{sc}}} \right)^{-1}. \quad (5)$$

Based on these expressions, we estimate the averaged dielectric constant and slab thickness to be 17.2 ε_0 and 5.4 Å computed with PBE and 16.3 ε_0 and 5.4 Å computed with SCAN+rVV10. These values of slab thickness are physically meaningful as they correspond approximately to the S–S distance (d_{S-S} listed in Table I) + 2× the covalent radius of S ($r_S = 1.05$ Å).

The assumption of an isotropic dielectric slab need not be valid for a monolayer; however, this simplified dielectric model correctly reproduces the asymptotic screening properties of the repeated slab system. The consistent choice of d^{slab} and $\varepsilon^{\text{slab}}$ ensures that, despite the approximation of mapping the anisotropic dielectric tensor of the slab onto an isotropic dielectric tensor, the correct asymptotic behavior of the electrostatic potential is still recovered. At distances shorter or comparable to the length scale set by d^{slab} , both the dielectric anisotropy within the layer as well as microscopic variations

due to the detailed atomic and electronic structure come into play. Since the latter is unavoidable and fundamentally limits all continuum modeling attempts, we do not expect that a more elaborate setup of the surrogate model would significantly improve its performance.

Calculating the dielectric tensor for the layered bulk MoS₂ is much more straightforward since there is no vacuum region in the cells. The dielectric tensors are evaluated with the PBE functional using density functional perturbation theory (DFPT), and with the SCAN+rVV10 functional using finite field method as DFPT is not currently implemented in VASP for meta-GGAs and hybrid functionals. The in-plane and out-of-plane static dielectric coefficients for layered bulk MoS₂ computed in this work agree well with experimentally-measured values [77]. Applying the simple dielectric model from above to the layered bulk system ($\epsilon_{\parallel}^{\text{slab}} = \epsilon_{\perp}^{\text{slab}} = \epsilon^{\text{slab}}$, $d^{\text{slab,bulk}} = 2d^{\text{slab,ML}}$, $d^{\text{sc}} = 12.3$ Å) predicts in-plane dielectric constants of 15.2 ϵ_0 (PBE) and 14.3 ϵ_0 (SCAN+rVV10), and out-of-plane dielectric constants of 5.8 ϵ_0 (PBE) and 5.5 ϵ_0 (SCAN+rVV10), within $\approx 10\%$ of the directly computed values, which further validates our use of the simple dielectric model for the monolayer.

The dielectric properties of each system are required as inputs to the charge correction schemes employed in this work. For the bulk charge correction scheme, we provide the full anisotropic dielectric tensor computed for layered bulk MoS₂. Meanwhile, the 2D charge correction scheme, as currently implemented, takes as inputs only a single averaged dielectric constant for the slab as well as a slab thickness, which defines the positions of the dielectric interfaces. We test the sensitivity of the charge correction scheme to the choice of dielectric constant – changing the dielectric constant by up to 50% changes the formation energies and CTs by around 100 meV which does not qualitatively alter our results.

III. DEFECT FORMATION ENERGY

Figure 1 demonstrates that upon application of the charge correction scheme, the defect formation energies for charged S vacancies in the monolayer and the layered bulk MoS₂ become well-converged in all cases except for the +1 S vacancy in layered bulk MoS₂. On both plots, the open symbols indicate the uncorrected defect formation energies in the Mo-rich/S-poor limit, calculated with SCAN+rVV10. The uncorrected energies strongly depend on the in-plane supercell size, and for the monolayers, also on the vacuum spacing. After correction, the energies are converged to within 100 meV across all supercell and vacuum sizes in all cases except the +1 S vacancy in layered bulk MoS₂, for which the correction does not work because the defect charge turns out to be delocalized (c.f. Fig. 4). For delocalized defect states, the energy correction evaluated by the electrostatic correction scheme is not meaningful, and in this system turns out to be close to zero, leading to an overlap between the uncorrected and “corrected” (red diamond) symbols in Fig. 1(b). The dotted lines connecting the corrected energies are included as a guide to the eye, showing that when the correction scheme is applied

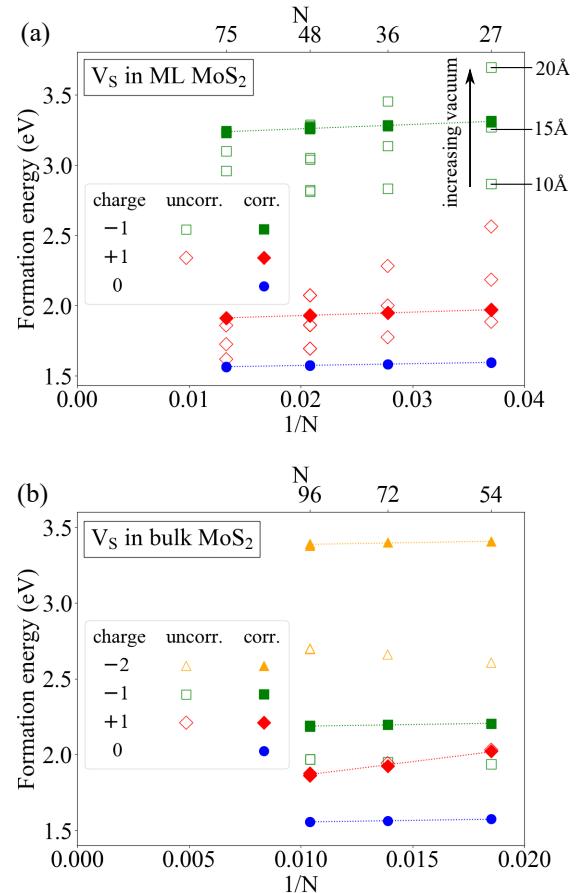


FIG. 1. Uncorrected (open symbols) and corrected (filled symbols) formation energies for S vacancies in (a) monolayer MoS₂ and (b) layered bulk MoS₂ in different charge states, calculated with SCAN+rVV10. The Fermi level is set to the valence band maximum. In the top plot for S vacancies in monolayer MoS₂, the multiple data points corresponding to each supercell size indicate the energies evaluated in supercells with different vacuum spacings of 10, 15, and 20 Å. The uncorrected energies diverge with increasing vacuum spacing and also exhibit a strong dependence on in-plane supercell size. The corrected energies are well converged across all supercell and vacuum sizes in all cases except the +1 S vacancy in layered bulk MoS₂, for which the correction does not work due to the delocalized nature of the defect state (see text).

successfully, only a small dependence on in-plane supercell size, which is comparable to that for the neutral defect remains. This small supercell size dependence reflects the elastic interactions between defects, which are not accounted for in the electrostatic charge correction scheme. The unphysical linear divergence in energy with vacuum spacing is effectively addressed by the correction scheme as evidenced by the overlapping filled symbols in the Fig. 1(a). These plots also show that the magnitudes of the correction terms range from tens to hundreds of meV depending on the system, charge state, and supercell size, and must be included when evaluating formation energies of charged point defects.

Figure 2 shows that the S vacancy is most stable in the neutral charge state in both monolayer and layered bulk MoS₂

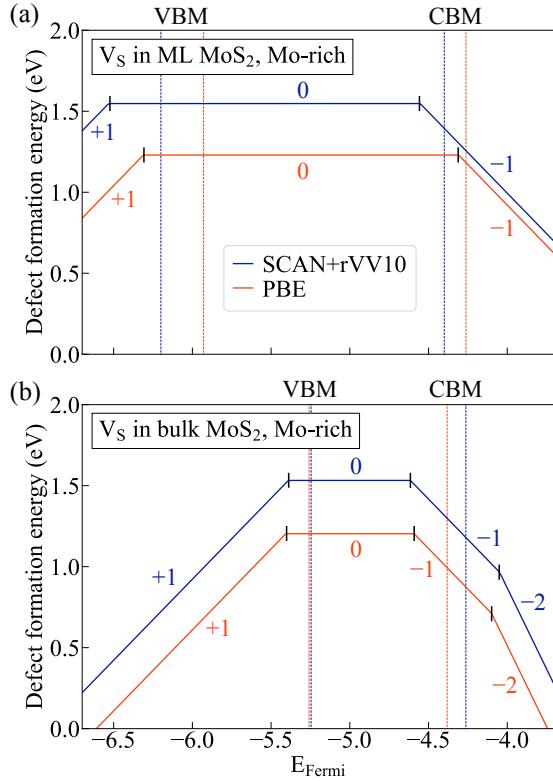


FIG. 2. Formation energy of the S vacancy in (a) monolayer MoS_2 and (b) layered bulk MoS_2 as a function of Fermi level position, calculated with PBE (orange) and SCAN+rVV10 (blue). The valence and conduction band edge positions calculated with respect to vacuum level are indicated by the vertical dashed lines. The slopes of each segment of the formation energy plots are indicated, and correspond to the most stable charge state for the defect over that range of Fermi energies. The points at which the slopes change are the charge transition levels (CTLs) and are marked by black vertical lines. In all cases, the neutral S vacancy is predicted to be most stable across most of the gap, and only the 0/-1 charge transition level is predicted to be within the band gap, close to the conduction band minimum.

for Fermi energies spanning most of the band gap, with the -1 charged S vacancy becoming more favorable close to the conduction band minimum (CBM). The formation energy of the neutral S vacancy in both monolayer and layered bulk MoS_2 under Mo-rich/S-poor conditions is computed with SCAN+rVV10 to be ≈ 1.5 eV, in good agreement with other DFT-computed values reported in literature [40, 41, 79]. PBE predicts the formation energy to be ≈ 0.3 eV lower; this is in part due to the underestimation of μ_{MoS_2} and therefore μ_S resulting from missing van der Waals interactions.

The kinks in the formation energy plots indicate charge transition levels (CTLs). The 0/-1 CTL is predicted to be within the band gap close to the CBM, corresponding to a deep acceptor state. Our calculations estimate the 0/-1 CTL to be 1.6 to 1.7 eV above the valence band minimum (VBM) in monolayer MoS_2 and 0.6 to 0.7 eV above the VBM in layered bulk MoS_2 , again in good agreement with previous computational studies [40, 41, 79]. Our estimate of the position

of the 0/-1 CTL in monolayer MoS_2 is also consistent with the mid-gap defect states identified in electron tunneling spectroscopy measurements, which were estimated to be closer to the conduction band, approximately 0.5 – 0.1 eV below the CBM [80]. As previously noted, both PBE and SCAN functionals significantly underestimate the band gaps; therefore, some CTLs which appear outside the band gap in our calculations may fall within the band gap, leading to multiple defect levels within the gap. Indeed, calculations with HSE and GW in the literature have predicted that the +1/0 CTL in monolayer MoS_2 and the $-1/-2$ CTL in layered bulk MoS_2 may also fall within the band gap [40, 79]. The position of the +1/0 CTL in layered bulk MoS_2 is uncertain since the correction method does not work when the extra charge occupies a delocalized state. Figure 4 shows that the extra hole in the calculation of the +1 charged S vacancy in layered bulk MoS_2 has a delocalized charge distribution that corresponds to an empty state at the VBM. This indicates that the localized defect state associated with the S vacancy is located within the valence band region (see Fig. 6 in Sec. IV) and not likely to be stabilized within the band gap, hence the +1/0 CTL is not relevant.

IV. ELECTRONIC STRUCTURE

Figure 3 shows the total charge and spin density distributions around the charged S vacancy in monolayer and layered bulk MoS_2 . The charge and spin densities associated with the additional hole or electron(s) remain fairly localized around the defect site for the +1 and -1 charged S vacancy in the monolayer, as well as for the -1 and -2 charged S vacancy in the bulk. The charge and spin densities around the -1 charged S vacancy look very similar in both the monolayer and layered bulk, demonstrating a breaking of the 3-fold symmetry of the native lattice. The 3-fold symmetry around the defect site is maintained in all the other charged and neutral S vacancy configurations we studied. Each of the configurations depicted in Fig. 3 exhibits a net magnetic moment, including the -2 charged S vacancy in the bulk for which the parallel spin configuration is more stable than the anti-parallel (non-magnetic) configuration by ≈ 150 meV when evaluated with SCAN+rVV10 (≈ 40 meV when evaluated with PBE). This is also reflected in the projected density of states plots in Figs. 5 and 6.

Figure 4 illustrates the delocalization of charge in the +1 S vacancy in layered bulk MoS_2 , explaining why the charge correction scheme – which assumes a relatively localized charge – does not work in this case. Unlike in monolayer MoS_2 , in layered bulk MoS_2 the extra charge (hole) associated with the +1 S vacancy is completely delocalized, not only within the layer containing the S vacancy but also over adjacent layers. Since the correction scheme assumes a relatively localized charge, it fails in this case, as seen in Fig. 1. As a result, we are unable to accurately quantify the formation energy of this defect. However, the delocalized nature of the charge as well as the calculated density of states for this defect (Fig. 6b), which indicates that a state at the top of the valence band

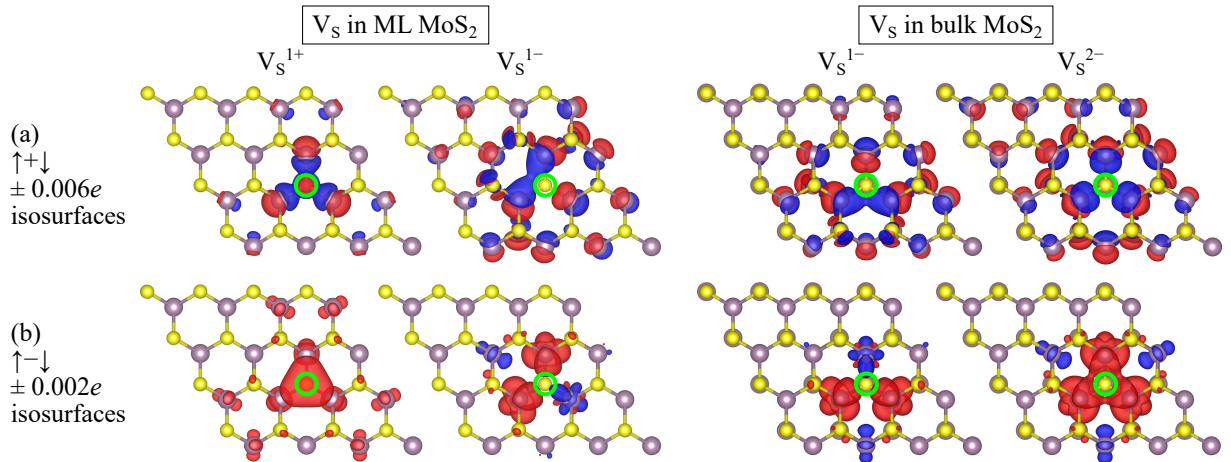


FIG. 3. (a) Total charge and (b) spin density distributions of the extra hole or electron(s) around the charged S vacancy in monolayer and layered bulk MoS₂. Mo atoms are depicted in purple and S in yellow, the position of the S vacancy within each 4 × 4 supercell is marked by the green circles, and the red (blue) indicate the positive (negative) charge and spin isosurfaces. The symmetry is broken in the -1 charge state in both the monolayer and layered bulk systems.

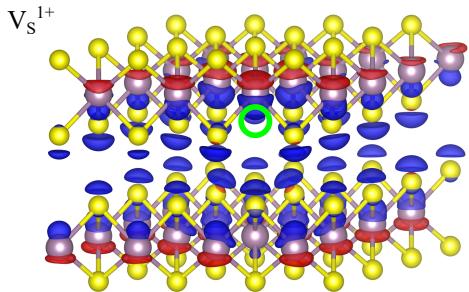


FIG. 4. Side view of the total charge density distribution of the extra hole around the positively charged S vacancy in layered bulk MoS₂. Mo atoms are depicted in purple and S in yellow, the position of the S vacancy within the 4 × 4 supercell is marked by the green circle, and the red (blue) indicate the positive (negative) 0.001e charge isosurfaces. The charge density is completely delocalized not only within the layer containing the S vacancy but also on adjacent layers.

is depleted when the +1 S vacancy is formed, are consistent with it being a state within the valence band.

The projected densities of states corresponding to the S vacancy in different charge states in monolayer MoS₂ (Fig. 5) and layered bulk MoS₂ (Fig. 6) show that a defect state with primarily Mo $d_{x^2-y^2}$ and d_{xy} orbital character is induced in the gap. The density of states is projected onto the d -orbitals of the three Mo atoms directly adjacent to the S vacancy. In defect-free MoS₂, the Mo atoms have trigonal prismatic (D_{3h}) symmetry, which gives rise to the following energetic splitting of d -orbitals: d_{z^2} (a'_1 orbital) < $d_{x^2-y^2} = d_{xy}$ (e' orbitals) < $d_{xz} = d_{yz}$ (e'' orbitals). The degeneracy of the orbitals is reflected in the overlapping d -orbital contributions in the projected density of states for the pristine monolayer for the blue $d_{x^2-y^2}$ and d_{xy} states (e') and green d_{xz} and d_{yz} (e'') peaks. When a S vacancy is created, this generates a doubly degen-

erate defect state in the band gap with primarily e' character. Another defect state with primarily e'' character also appears near the top of the valence band. In the neutral state (V_S^0), the state at the top of the valence band is filled while the states in the gap remain empty.

When adding an extra electron to the neutral S vacancy, the system undergoes a Jahn-Teller distortion, which stabilizes the -1 charged S vacancy in both monolayer and layered bulk MoS₂. In the negatively charged state (V_S^{1-}), the previously doubly degenerate defect state in the gap splits and the additional electron occupies the lowest energy state, which exhibits predominantly $d_{x^2-y^2}$ (dark blue) character. This breaking of the degeneracy among the e' orbitals is also associated with the breaking of the D_{3h} symmetry of the vacancy. In pristine monolayer (layered bulk) MoS₂, the three Mo atoms that surround a S atom form an equilateral triangle with each pair of Mo atoms 3.17 Å (3.16 Å) apart. Around a S vacancy, the Mo atoms relax slightly inward, retaining the 3-fold symmetry and forming equilateral triangles with atoms 3.07 Å (3.07 Å) apart when in the neutral state. In the -1 charged state, the three Mo atoms form an isosceles triangle around the S vacancy with two Mo-Mo pairs approximately 3.05 Å (3.05-3.06 Å) apart, and the third Mo-Mo pair 3.18 Å (3.18 Å) apart. Such simultaneous electronic and geometric symmetry-breaking is an example of a Jahn-Teller distortion, and is responsible for stabilizing the -1 charged S vacancy in both monolayer and layered bulk MoS₂. The symmetric V_S^{1-} structures without Jahn-Teller distortions are higher in energy by 116 meV (43 meV) and 120 meV (50 meV) in the monolayer and layered bulk MoS₂, respectively, when evaluated with the SCAN+rVV10 (PBE) functional. These relaxation energies due to the Jahn-Teller distortion may be sufficiently large for experimental observation as an asymmetry in the optical excitation/de-excitation energies during photoluminescence spectroscopy experiments.

Unlike in the neutral and negatively charged S vacancy, the

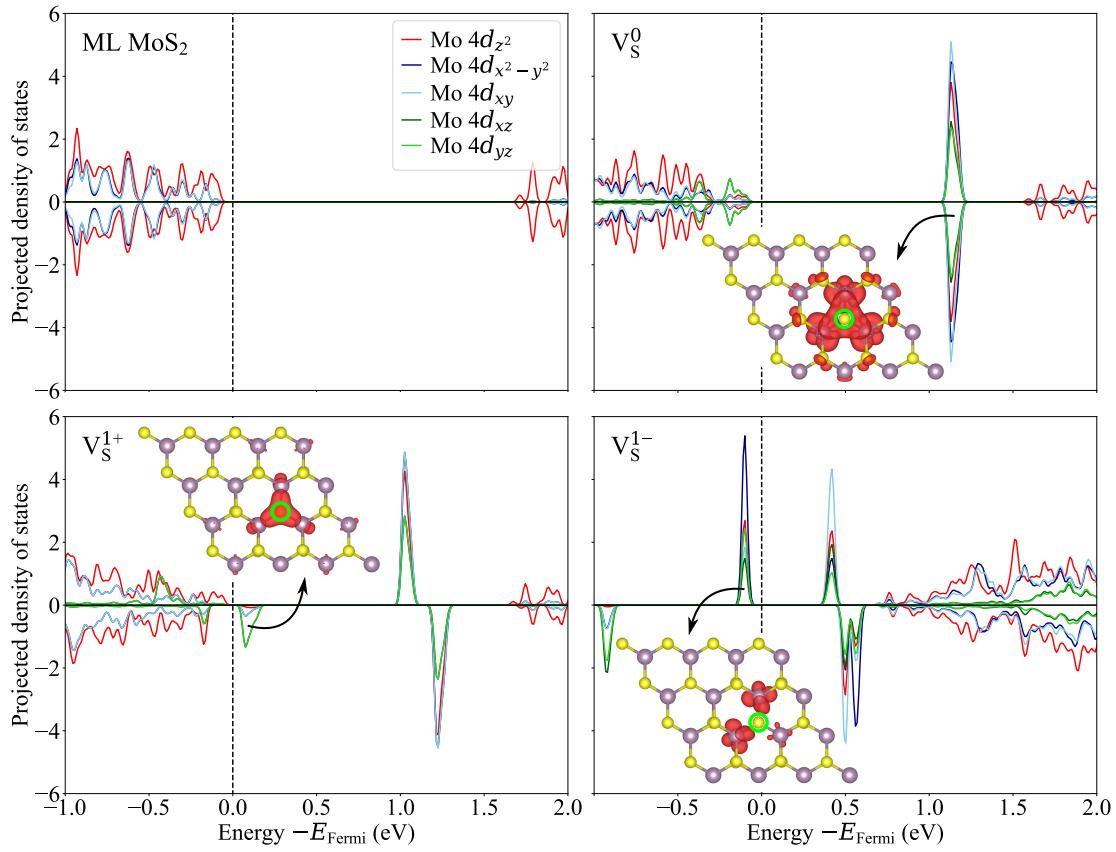


FIG. 5. Projected density of states for the pristine monolayer MoS₂ and the S vacancy in monolayer MoS₂ in the neutral (V_S^0), +1 (V_S^{1+}), and -1 (V_S^{-1}) charge states. The density of states is projected onto the *d*-orbitals of the three Mo atoms directly adjacent to the S vacancy. The defect state in the band gap has primarily $d_{x^2-y^2}$ (dark blue) and d_{xy} (light blue) character. In the -1 charge state, the degeneracy between these two orbitals is broken, with the additional electron occupying a state with dominant $d_{x^2-y^2}$ character. The insets illustrate the electronic orbitals corresponding to the defect states of interest.

defect state associated with the positively charged S vacancy (V_S^{1+}) appears to have a different character in the monolayer compared to in the layered bulk. In the monolayer, the electron is removed from a localized defect state near the top of the valence band. However, in the layered bulk, Fig. 6 shows that the electron removal depletes a delocalized state at the top of the valence band rather than the localized defect state, which is located 0.6 eV below the VBM.

This difference in behavior between the monolayer and bulk for the V_S^{1+} vacancy is notable when comparing the predicted +1/0 CTLs (see Fig. 2). Indeed, the +1/0 CTL is predicted to fall below the VBM extracted from the Kohn-Sham band structures in both cases. Therefore, under appropriate electrostatic boundary conditions, one would expect the electron in both cases to be depleted from a valence-band state that is delocalized within the slab, instead of from a localized defect state. This suggests that the charge localization may be an artefact of the calculation due to the periodic boundary conditions which artificially stabilize the observed localized solution compared to the delocalized one.

To estimate the energy correction for a delocalized charge, we consider a surrogate model, similar to the Gaussian charge

model, where the excess charge is delocalized in the plane but remains localized perpendicular to the layer. We find that the uncorrected energy of the delocalized solution does indeed appear to be higher than that of the localized solution. Therefore, DFT calculations for charged simulation cells can converge to a localized solution, even though after correction, the delocalized solution might be the actual ground state. This systematic error arises because the degree of in-plane localization of the defect charge has a profound impact on the electrostatic energy, no matter how the vacuum size is chosen. Consider two extreme cases: one in which the charge is entirely delocalized over the 2D material (e.g., a band-like state) and another, where the defect charge is laterally localized. At a given vacuum separation, we can invoke the superposition principle to construct the localized case from the delocalized one. For this, we add a localized charge in the unit cell plus a compensating background delocalized over the 2D slab equivalent to the delocalized distribution. The excess electrostatic energy from this charge-neutral periodic array compared to the isolated localized case with the counter charge moved to infinity is due to the interaction between the charge and its counter charge and is therefore always attractive. This additional attractive

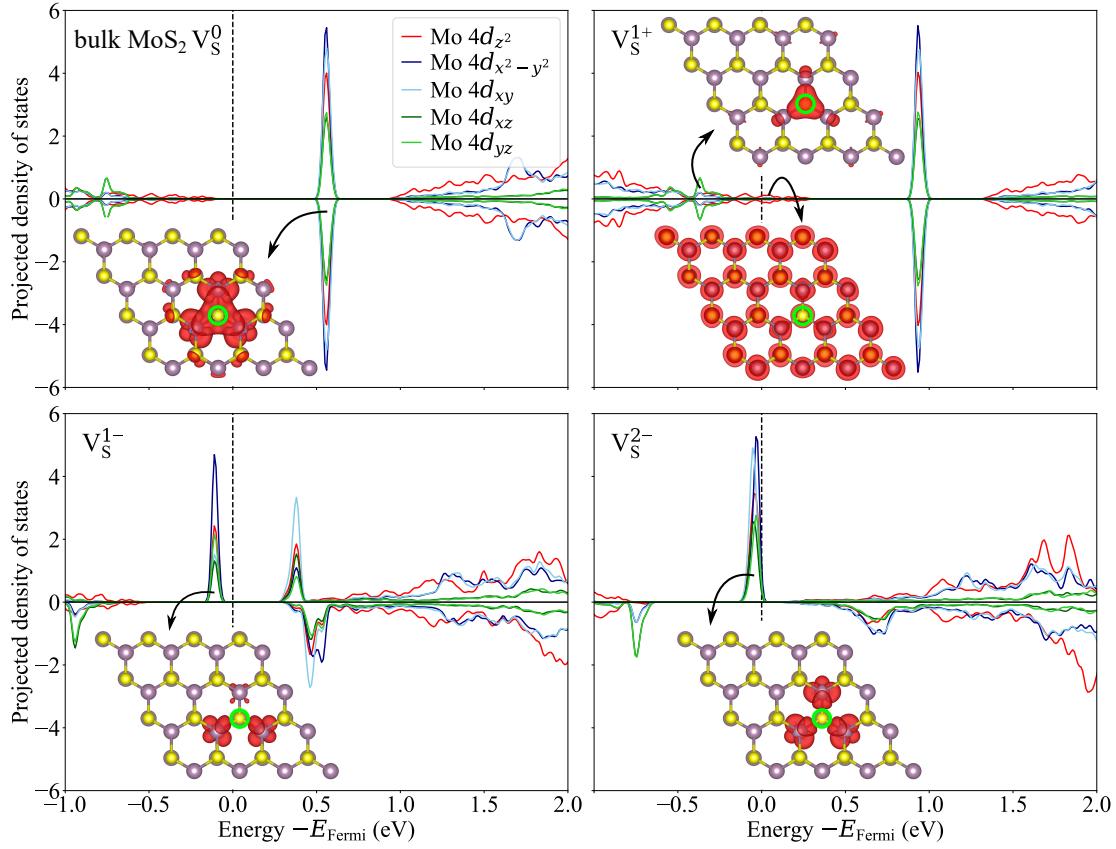


FIG. 6. Projected density of states for the S vacancy in layered bulk MoS₂ in the neutral (V_S^0), +1 (V_S^{1+}), -1 (V_S^{1-}), and -2 (V_S^{2-}) charge states. The density of states is projected onto the d -orbitals of the three Mo atoms directly adjacent to the S vacancy. Similar to the S vacancy in the monolayer, the degeneracy between $d_{x^2-y^2}$ (dark blue) and d_{xy} (light blue) orbitals is broken in the -1 charge state. The degeneracy is restored in the -2 charge state, for which the parallel spin configuration is lower in energy. The insets show the electronic orbitals corresponding to the defect states of interest.

energy contribution may lower the energy of the localized solution sufficiently to potentially stabilize the localized solution even if the delocalized one should be lower in the limit of large lateral size.

The same argument also explains the apparent discrepancy between the position of the predicted -1/2 CTL in layered bulk MoS₂ and the location of the corresponding defect states in the density of states. When a second electron is added to create the -2 charged S vacancy (V_S^{2-}) in layered bulk MoS₂, the D_{3h} symmetry is restored, and the most stable configuration is found to be when the two extra electrons have their spins aligned ($\mu_B = 2$). The density of states for V_S^{2-} in layered bulk MoS₂ – depicted in the bottom right panel of Fig. 6 – suggests that the second additional electron also occupies a localized defect state within the band gap. However, based on the defect formation energies, we predicted the -1/2 CTL in layered bulk MoS₂ to be above the CBM. Again, due to the compensating homogeneous background, the localized defect state corresponding to V_S^{2-} is artificially stabilized and therefore shows up in the gap in the density of states, which is not corrected. When the correct electrostatic boundary conditions are accounted for by including the correction term in the de-

fect formation energies, the energy of the defect state is raised by ≈ 0.7 to 0.8 eV (c.f. Fig. 1(b)), pushing it into the conduction band.

These implicit consequences of the homogeneous charge background imply that one must be careful when basing the analysis of defect states *solely* on calculations of the electronic structure – such as the density of states – which is quite often the case in the literature. In Kohn-Sham DFT, band structure and density of states are calculated based on one-electron energies, which is an approximation of the actual interacting electron system. While these calculations can provide valuable insight into the defect states and their orbital contributions, they may not be the most accurate way to estimate the positions of these defect states and CTLs. The location of the CTLs is given by the energy difference between different charge states of the defects and, as such, includes exchange and correlation contributions that are beyond the single-particle energies of the density of states. This many-body contribution can shift the energy of the CTLs. Moreover, as we argue above, there are some cases for which DFT may predict the wrong electronic ground state when a compensating homogeneous background charge is included, which can

lead to incorrect conclusions being drawn based on the density of states alone. Furthermore, different choices of functionals may also shift the CTLS and band edge positions relative to the vacuum level by up to 0.5 eV or more, which also adds to the uncertainty in predicting the energy of the CTLS relative to the band edges. *A posteriori* correction schemes for band alignment [81, 82] may be used in combination with the current charge correction scheme to obtain more accurate estimates of the positions of the defect states. Therefore, it is essential to employ and compare different approaches for investigating defect properties — as presented in this work — to obtain a more reliable and complete understanding of these defects.

Finally, we compare our electronic structure analysis with previous studies. Based on our electronic structure calculations, we identify the defect state near the top of the valence band to have a predominantly e'' character. The corresponding electronic orbital depicted in the inset of the V_S^{1+} subplot of Fig. 5 is largely localized in the region between the three Mo atoms neighboring the S vacancy site, which does suggest significant contributions from the d_{xz} and d_{yz} orbitals with lobes oriented in those directions. Our findings are in contrast to previous studies [38, 41], which identified that state as the singlet a'_1 (i.e., d_{z^2}) state instead. These same studies did identify the defect state in the gap to be the doubly degenerate e' state, in agreement with our results. Komsa and Krasheninnikov [40] briefly mention that the S vacancy in monolayer MoS₂ undergoes a Jahn-Teller distortion upon addition of an extra electron; however, they did not elaborate further on that assertion or present any analysis of the defect electronic structure. Noh et al. [41] computed the density of states for V_S^{1-} , and while they did find a shift between the up and down-spin states as we did, they did not observe the splitting of the defect state indicative of a Jahn-Teller distortion. This could be due to the authors not having allowed for symmetry breaking of the original lattice during the structural relaxation, which would preclude the Jahn-Teller distorted structure from being found. Jahn-Teller distortions have not been reported in other studies on S vacancy in MoS₂ [37, 79, 83], which only evaluated the electronic structure of the neutral S vacancy in which such distortions are not predicted to occur. To the best of our knowledge, the Jahn-Teller distorted S vacancy structure has thus far not been observed in experiments. One reason for this is that the distortion of the lattice is very small, with displacements of about 0.1 Å between neighboring Mo atoms. Such small distortions challenge even high-resolution STEM

imaging techniques. Furthermore, unless the Fermi level in the system is close to the top of the gap through n-type doping, gating, or substrate effects, the majority of S vacancies in MoS₂ is expected to be in the neutral charge state, which does not exhibit the Jahn-Teller distortion.

V. CONCLUSION

In this work, we performed density functional theory calculations to compute the formation energies and charge transition levels associated with sulfur vacancies in monolayer and layered bulk MoS₂. We utilize the correction scheme recently developed by Freysoldt and Neugebauer to ensure the appropriate electrostatic boundary conditions for charged defects in 2D materials. We demonstrate the effectiveness of the correction scheme for the convergence of the defect formation energies with respect to vacuum spacing and in-plane supercell dimensions. We benchmark the SCAN+rVV10 functional and this new charge correction scheme for 2D monolayers against other studies in literature, and find good agreement, validating our approach. By analyzing the electronic structures of the defects in different charge states, we predict that both systems undergo a Jahn-Teller distortion, which helps stabilize the sulfur vacancy in the -1 charged state.

We show that the ubiquitous finite-size errors in charged-defect calculations for 2D materials tend to favor localized solutions over delocalized ones, irrespective of the sign of the correction applied to the localized state, and independent of the chosen *a posteriori* correction scheme. As a result, the uncorrected stability region may fall within the band gap, allowing us to apply the charge correction scheme to estimate the CTLS even if they fall (after correction) outside the band gap. The results illustrate that the combination of the *a posteriori* charge correction schemes with computationally feasible functionals provides a valuable tool for predicting the properties of charged defects in 2D semiconductor materials.

ACKNOWLEDGMENTS

This work was supported by the National Science Foundation through the 2DCC-MIP under award DMR-1539916 and by the awards DMR-1748464 and OAC-1740251. Computational resources were provided by the University of Florida Research Computing Center.

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