

We have presented the graphical abstract image and text for your article below. This briefly summarises your work, and will be presented with your article online. It will not appear in the print edition.

DISCUSSIONS

1

Crystal structure evaluation: calculating relative stabilities and other criteria: general discussion

5
10
15
Matthew Addicoat, Claire Adjiman, Mihails Arhangel'skis, Gregory Beran, David Bowskill, Gerit Brandenburg, Doris Braun, Virginia Burger, Jason Cole, Aurora Cruz-Cabeza, Graeme Day, Volker Deringer, Rui Guo, Alan Hare, Julian Helfferich, Johannes Hoja, Luca Iuzzolino, Samuel Jobbins, Noa Marom, David McKay, John Mitchell, Sharmarke Mohamed, Marcus Neumann, Sten Nilsson Lill, Jonas Nyman, Artem R. Oganov, Pablo Piaggi, Sarah Price, Susan Reutzel-Edens, Ivo Rietveld, Michael Ruggiero, Matthew Ryder, German Sastre, Christian Schön, Christopher Taylor, Alexandre Tkatchenko, Seiji Tsuzuki, Joost van den Ende, Scott Woodley, Grahame Woollam and Qiang Zhu

20
Please check this proof carefully. Our staff will not read it in detail after you have returned it.

Proof corrections must be returned as a single set of corrections, approved by all co-authors. No further corrections can be made after you have submitted your proof corrections as we will publish your article online as soon as possible after they are received.

25
Please ensure that:

- The spelling and format of all author names and affiliations are checked carefully. Names will be indexed and cited as shown on the proof, so these must be correct.
- Any funding bodies have been acknowledged appropriately.
- All of the editor's queries are answered.
- Any necessary attachments, such as updated images or ESI files, are provided.

30
Translation errors between word-processor files and typesetting systems can occur so the whole proof needs to be read. Please pay particular attention to: tables; equations; numerical data; figures and graphics; and references.

35
Please send your corrections preferably as a copy of the proof PDF with electronic notes attached or alternatively as a list of corrections – do not change the text within the PDF file or send a revised manuscript. Corrections at this stage should be minor and not involve extensive changes.

Please return your **final** corrections, where possible within **48 hours** of receipt, by e-mail to: faraday@rsc.org. If you require more time, please notify us by email.

40

1 **Researcher information**

If any authors have ORCID or ResearcherID details that are not listed below, please provide these with your proof corrections.

5 Please check that the ORCID and ResearcherID details listed below have been assigned to the correct author. Authors should have their own unique ORCID iD and should not use another researcher's, as errors will delay publication.

Please also update your account on our online manuscript submission system to add your ORCID details, which will then be automatically included in all future submissions. See [here](#) for step-by-step instructions and more information on author identifiers.

First (given) name(s)	Last (family) name(s)	ResearcherID	ORCID
Matthew	Addicoat		
Claire	Adjiman		
Mihails	Arhangelskis		
Gregory	Beran		
David	Bowskill		
Gerit	Brandenburg		
Doris	Braun		
Virginia	Burger		
Jason	Cole		
Aurora	Cruz-Cabeza		
Graeme	Day		
Volker	Deringer		
Rui	Guo		
Alan	Hare		
Julian	Helfferich		
Johannes	Hoja		
Luca	Iuzzolino		
Samuel	Jobbins		
Noa	Marom		
David	McKay		
John	Mitchell		
Sharmarke	Mohamed		
Marcus	Neumann		
Sten	Nilsson Lill		
Jonas	Nyman		
Artem R.	Oganov		
Pablo	Piaggi		

1

5

10

15

20

25

30

35

40

45

50

Sarah	Price		
Susan	Reutzel-Edens		
Ivo	Rietveld		
Michael	Ruggiero		
Matthew	Ryder		
German	Sastre		
Christian	Schön		
Christopher	Taylor		
Alexandre	Tkatchenko		
Seiji	Tsuzuki		
Joost	van den Ende		
Scott	Woodley		
Grahame	Woollam		
Qiang	Zhu		

Queries for the attention of the authors

Journal: Faraday Discussions

Paper: C8FD90031K

Title: Crystal structure evaluation: calculating relative stabilities and other criteria: general discussion

For your information: You can cite this article before you receive notification of the page numbers by using the following format: (authors), Faraday Discuss., (year), DOI: 10.1039/C8FD90031K.

Editor's queries are marked on your proof like this **1**, **2** etc. and for your convenience line numbers are indicated like this 5, 10, 15,

Please ensure that all queries are answered when returning your proof corrections so that publication of your article is not delayed.

Query Reference	Query	Remarks
1	Please confirm that the spelling and format of your name is correct. Names will be indexed and cited as shown on the proof, so these must be correct. No late corrections can be made. FOR YOUR INFORMATION: You can cite this paper before the page numbers are assigned with: (authors), Faraday Discuss., DOI: 10.1039/c8fd90031k.	

DISCUSSIONS

Crystal structure evaluation: calculating relative stabilities and other criteria: general discussion

Matthew Addicoat, Claire Adjiman, Mihails Arhangel'skis, Gregory Beran, David Bowskill, Gerit Brandenburg, Doris Braun, Virginia Burger, Jason Cole, Aurora Cruz-Cabeza, Graeme Day, Volker Deringer, Rui Guo, Alan Hare, Julian Helfferich, Johannes Hoja, Luca Iuzzolino, Samuel Jobbins, Noa Marom, David McKay, John Mitchell, Sharmarke Mohamed, Marcus Neumann, Sten Nilsson Lill, Jonas Nyman, Artem R. Oganov, Pablo Piaggi, Sarah Price, Susan Reutzel-Edens, Ivo Rietveld, Michael Ruggiero, Matthew Ryder, German Sastre, Christian Schön, Christopher Taylor, Alexandre Tkatchenko, Seiji Tsuzuki, Joost van den Ende, Scott Woodley, Grahame Woollam and Qiang Zhu

DOI: 10.1039/C8FD90031K

(200:[200]200) **Christian Schön** opened the discussion of the paper by Gregory J. O. Beran: Concerning the multi-tier approach to improving the quality of the computations, where you did a careful analysis of different types of approximations, it is still very disconcerting that there appears to be no inherently systematic approach to gain an estimate of the errors involved in the calculations – often it seems that one does not really know where the error is hiding (*e.g.* fortuitous error cancellations). This contrasts with the analytical convergence criteria and error bounds one gets when using *e.g.* perturbation theory, and is quite bothersome (especially since many people do not even try to provide error estimates in the discussion sections of their papers). Do you see any progress in this area?

Gregory Beran replied: Quantification of uncertainty is a major challenge in electronic structure theory (and many other areas of chemical simulation). Our preferred, albeit imperfect, approach is to investigate the sensitivity of the prediction to the modeling choices. For example, one can explore how the structures, thermochemical properties, relative polymorph stabilities, or other properties of interest converge with respect to the basis set and level of theory. A few earlier studies from our group exemplify this. For aspirin forms I and II, the relative energy rankings proved quite insensitive to the electronic structure method and basis set, leading to relatively high confidence in the relative energetics.¹ The close similarities in crystal packing between the two forms allow for

1 substantial error cancellation in the relative energies. In contrast, the energy
rankings for the five polymorphs of oxalyl dihydrazide are very sensitive to the
electronic structure treatment, making the quantitative stability ranking less
certain.² In that case, the basis set superposition error (BSSE) associated with the
5 intramolecular hydrogen bonding in the alpha polymorph is harder to correct
than the BSSE for the purely intermolecular hydrogen bonding found in the other
polymorphs. Only in the limit of the large basis sets does one achieve a balanced
description of both types of interactions.

10 Perhaps the best example of sensitivity analysis/uncertainty quantification
from our work occurs in our recent study, which predicted the methanol phase
diagram.³ In that case, by examining how the predicted phase boundaries change
upon altering the relative free energies between two forms, we showed that our
calculations reproduced the experimental phase diagram to within $\sim 0.5 \text{ kJ mol}^{-1}$.
15 Furthermore, the sensitivity analysis was used to investigate which features of the
calculations were most important and where one should focus the computational
effort in order to obtain accurate predictions. The Electronic Supplementary
Information for ref. 3 goes into considerable detail on these issues.

20 1 S. Wen and G. J. O. Beran, *Cryst. Growth Des.*, 2012, **12**, 2169–2172.

2 S. Wen and G. J. O. Beran, *J. Chem. Theory Comput.*, 2012, **8**, 2698–2705.

3 C. Cervinka and G. J. O. Beran, *Chem. Sci.*, 2018, **9**, 4622–4629.

25 (201:[201]201) **Volker Deringer** said: You have nicely discussed the different
“tiers” of methodology, and how the acetaminophen example was only amenable
to the computationally more affordable tiers. How do you expect this to change
over time, when more and cheaper CPU time will become available? Do you expect
“Tier 1” methods to be routinely in reach within a time frame of a couple of years –
and what impact will that have on the field?

30 **Gregory Beran** responded: Future advances in computer power will certainly
help, but as the timings indicate, the computational cost of a Tier 1 calculation is
roughly 200 times that of a Tier 3 or Tier 4 one, and that ratio will continue
growing with increasing molecular size. For many applications, the difference
35 between Tier 1 and 3 results may not be worth the difference in computational
cost. In the longer term, we think it will likely prove more beneficial to move
beyond the quasi-harmonic approximation and find better ways to handle the
dynamics and anharmonicity in the crystal, perhaps using machine learning or
other approaches to develop accurate potentials that can be sampled more
40 cheaply. High-quality energies/forces from fragment methods could potentially
provide inputs for developing such potentials.

(202:[202]202) **Aurora Cruz-Cabeza** asked: Could you please give an estimate as
to how your Tier 1–4 calculations compare in terms of computational expense?

45 **Gregory Beran** answered: Several factors play a role in the overall computa-
tional timings. Generally speaking, MP2 scales $O(N^5)$ with system size N , while
large-scale DFT calculations typically scale $O(N^3)$ or better. However, things
become more nuanced for the calculations performed here. The fragment-based
50 hybrid many-body interaction (HMBI) energy approach decomposes the full

1 crystal calculation to a series of quantum mechanical (QM) monomer and short-
range dimer calculations, while longer-range dimers and many-body interactions
are approximated at a lower level of theory (*e.g.* with the AMOEBA polarizable
5 force field or in some cases here, periodic Hartree–Fock, HF). Evaluation of the
QM dimers forms the computational bottleneck. At long range, the model
switches to a force field or Hartree–Fock description of the dimer intermolecular
interactions.

10 Furthermore, the HMBI approach exploits space group symmetry and requires
evaluation only of the symmetrically unique dimers. Thus, the computational cost
grows $O(N^5)$ with the size of the monomer, but it grows only linearly with the
number of molecules in the asymmetric unit. The fragment-based calculations
employ atom-centered Gaussian-orbital basis sets, and the convergence of the
15 MP2 correlation energy with basis set size is slow—cubic, rather than the expo-
nential convergence DFT would have in the same basis sets.

20 For fragment-based phonon calculations like those with HMBI, it turns out
that the same QM dimer calculations are needed for either a Γ -point-only
calculation or a supercell lattice dynamics calculation.¹ The extra work associ-
ated with the supercell occurs purely at the low level of theory (*e.g.* polarizable
force field). In addition, the finite displacements are done on a smaller scale (in
individual monomers or dimers, which often have fewer atoms than the whole
unit cell), which further reduces the cost. So while MP2 frequencies are consid-
erably more expensive than DFT ones, it might prove more efficient to use the
25 fragment approach to capture phonon dispersion for sufficiently large cells.

For plane-wave DFT, the basis set grows with the size of the unit cell. This
becomes especially problematic for large supercell phonon calculations. On the
other hand, one can typically perform less k -point sampling in larger cells. DFT
codes typically also exploit the symmetry of the cell to reduce the number of k -
points.

30 Overall, one expects the cost of fragment-based MP2 calculations to grow more
rapidly than plane-wave DFT as the molecules get larger, while the plane-wave
DFT calculation cost grows more steeply with unit cell size. Acetic acid, imid-
azole and acetaminophen each have four molecules in the unit cell and one in the
asymmetric unit. Carbon dioxide and ice are not discussed here, since their small
35 molecular size and the extraordinarily high symmetry in carbon dioxide make
them anomalously fast compared to larger organic molecules of interest to the
community.

40 For acetic acid or imidazole, a single-point energy MP2/aug-cc-pVTZ +
AMOEBA calculation is more expensive than the plane-wave B86bPBE-XDM (80 Ry
plane-wave cut-off) one by a factor of ~ 1.5 .² The relative cost increases by a factor
of ~ 6 – $8\times$ for a force or frequency calculation. The DFT basis set used in those
calculations was probably larger than necessary, and for acetaminophen we
reduced the plane-wave cut-off to 60 Ry. We also reduced the k -point mesh from
45 $5\times 5\times 5$ to $1\times 3\times 3$. As a result, MP2 is $\sim 49\times$, $\sim 242\times$, and $\sim 153\times$ more expensive
than DFT for an energy, force, and frequency calculation. For comparison, if we
kept the 80 Ry plane-wave cut-off, the ratios would be $\sim 3\times$, $\sim 16\times$, and $\sim 0.2\times$.
With the very large DFT basis set, the frequency calculation is actually cheaper
with fragment MP2/augcc-pVTZ, though again, that DFT basis set would probably
50 be unnecessarily large.

Based on these test calculations, we estimated overall computational costs in CPU hours and relative costs for the Tier 1–4 calculations. This includes mapping out the energy–volume curves at 10 different geometries (assuming 100 optimization cycles per geometry optimization) and computing phonon frequencies at three volumes (for the reference frequencies and two more to compute the Grüneisen parameters). The results are summarized in Table 1. From this table, one sees that the Tier 1 calculations cost roughly 1–2 orders of magnitude more than the Tier 4 ones. On the other hand, for Tiers 3 and 4, the computational cost is dominated by the DFT geometry optimizations and phonon calculations. Single-point energy refinement at the MP2/aug-cc-pVTZ level in Tier 3 increases the computational cost only marginally—no more than ~20% here. In contrast, switching to Tier 2 starts to increase the computational cost much more dramatically, especially for acetaminophen.

Even the single-point refinement calculations in the paper, which extrapolate to the complete basis set limit, correct the known deficiencies in MP2 with MP2C, and replace AMOEBA with periodic HF, do not increase the cost of Tier 3 too much. For the smaller two crystals, this refinement incurs only 10–20% higher cost compared to the pure DFT Tier 4 calculations. For acetaminophen, it roughly doubles the cost compared to the Tier 4 calculation. When combined with the quality of the predictions discussed in the paper, Tier 3 provides a valuable compromise between accuracy and computational cost.

1 S. Hirata, *J. Chem. Phys.*, 2008, **129**, 204104.

2 All timings were performed on a 16-core node with dual 2.4 GHz Intel Xeon E5-2630 v3 processors, 64 GB of RAM, and several terabytes of local disk storage.

(807:[203]203) **David McKay** communicated: The four tiers of computational methodology are set out in decreasing order of computational cost, with Tier 1 having HMBI energies, geometries and frequencies, then DFT coming in from right to left, *i.e.* frequencies, then geometries, then energies. Would the results of methods including DFT be improved (closer to the all-HMBI Tier 1) if, rather than considering the cost of the methods, you considered the competency of the methods at each stage, perhaps giving a Tier 2' of HMBI, DFT and HMBI for energies, geometries and frequencies, respectively? Perhaps also a Tier 3' of DFT, DFT, HMBI.

Table 1 Approximate computational costs for Tiers 1–4 using either HMBI (MP2/aug-cc-pVTZ + AMOEBA) or B86bPBE-XDM. The estimates assume 10 geometry optimization/energy calculations to map out the energy volume curves, 3 phonon calculations to obtain the reference phonons and Grüneisen parameters, and 100 geometry optimization cycles per geometry optimization

Crystal	CPU hours				Relative time			
	Tier 1	Tier 2	Tier 3	Tier 4	Tier 1	Tier 2	Tier 3	Tier 4
Acetic acid ^a	37 600	30 700	5330	5270	7.1	5.8	1.0	1
Imidazole ^a	92 800	74 100	13 100	13 000	7.1	5.7	1.0	1
Acetaminophen ^b	1 290 000	745 000	8000	6600	195	113	1.2	1

^a DFT calculations employed an 80 Ry plane-wave cut-off and a 5×5×5 *k*-point mesh. ^b DFT calculations employed a 60 Ry plane-wave cut-off and a 1×3×3 *k*-point mesh.

1 **Gregory Beran** communicated in reply: Given the reality of needing to reduce
computational cost, as evidenced by the timing data presented in response to the
question, we did not investigate approaches of the sort you mention.
5 What follows is therefore speculation: in the molecular quantum chemistry
literature, there are usually not substantial differences between the quality of
harmonic vibrational frequencies for intramolecular modes predicted with DFT
versus MP2, assuming sufficiently large basis sets. The empirical factors people
10 use to scale the frequencies to improve agreement with experiment are generally
similar in magnitude (typically around 0.9–1.0, depending on the specific model
chemistry). It is less obvious how well that insight translates to the soft lattice
phonons, which contribute significantly to thermal expansion and thermal
15 contributions to the enthalpy and entropy. On the other hand, the soft lattice
modes are largely governed by the crystal packing and cell volume. So as long as
the model gets those reasonably correctly, it should perform well. Our thermal
expansion data and plot of the phonon frequencies for ice demonstrate generally
20 similar performance for either HMBI or DFT on the low-frequency modes, so one
might think there could be some freedom to mix and match the different models
along the lines you suggest. However, in the end, the practical matters of
computational effort drive us toward Tiers 3 and 4 discussed in the paper.

25 (205:[204]204) **Mihails Arhangel'skis** enquired: My question concerns model-
ling unit cell expansion with quasi-harmonic calculations. How was anisotropic
unit cell expansion accounted for? In the case of low symmetry (monoclinic and,
especially, triclinic) unit cells I would imagine that a large number of structure
30 distortions would have to be considered in order to map the temperature
expansion in each crystallographic direction. Presumably, one would have to
study expansion about each principal axis separately, while also considering the
variations in unit cell angles. I would be curious to know whether such calcula-
tions are practical for low symmetry cells, or whether there this can be done in
a more efficient way.

35 **Gregory Beran** responded: For the quasi-harmonic calculation, we perform the
expansion/compression along a one-dimensional semi-anisotropic coordinate.
Specifically, the energy *versus* volume curve is generated by optimizing the
structure under various positive and negative hydrostatic pressures. This allows
40 the volume to expand or contract by deforming the unit cell in whatever manner
minimizes the energy change. A closely related approach would optimize the cell
subject to a volume constraint for various different volumes. However, algorithms
to perform such constant volume optimizations are not currently implemented in
the software packages used in our work. Either way, the volume dependence of the
45 phonons can subsequently be determined along the same one-dimensional
coordinate. The semi-anisotropic approach used in our work is an approxima-
tion relative to a fully anisotropic expansion model which would allow all inde-
pendent degrees of freedom to vary independently, but it should provide a more
realistic description of how the unit cell varies than a simple isotropic scaling of
50 the lattice parameters. For detailed analysis of the impact of including different
degrees of anisotropy in quasi-harmonic calculations, see the recent work by
Abraham and Shirts.¹ In the examples they looked at, the difference between an
isotropic and a fully anisotropic model was up to ~ 1 kJ mol⁻¹. The differences

1 involving quasi-anisotropic approaches like ours are considerably smaller. Regarding low-symmetry cells: the computational bottleneck for the hybrid many-body interaction fragment model is the number of dimer calculations that need to be evaluated. For careful calculations of the sort employed here, we typically
5 employ conservative cut-offs that evaluate dimer interactions quantum mechanically to 9–10 Å, before smoothly switching to an MM treatment for longer-range interactions. See ref. 2 for more details. Exploiting space group symmetry typically reduces the number of dimers by a factor corresponding to the ratio between the total number of molecules in the unit cell (Z) and the number of molecules in the asymmetric unit (Z'). For example, in the orthorhombic polymorph of acetic acid ($Pna2_1$ space group, $Z = 4$, $Z' = 1$) with the 9–10 Å cut-off mentioned above, a typical single-point energy calculation on crystalline acetic acid might require
10 over 212 dimers without space group symmetry, or 53 dimers with symmetry (savings factor = 4). See ref. 3 for more details. Four-fold symmetry is common to many of the most frequently occurring space groups, and such symmetry savings factors are common. Therefore, calculations on a unit cell with $P1$ symmetry will require several-fold more computational effort than calculations on a comparable cell with four-fold symmetry.

20 One nice feature of the fragment approach, however, is that the computational effort for the expensive quantum mechanical calculations grows linearly with the number of molecules in the unit cell. The quantum mechanical dimer interactions occur within a finite radius (*e.g.* the aforementioned 9–10 Å cut-off), regardless of whether those molecules occupy the central unit cell or a periodic image cell. In contrast, the computational cost of the periodic density functional grows cubically with the basis set size, and increasing the unit cell dimensions increases the number of plane-waves which fit in the unit cell for a given plane-wave cut-off. This behavior could make a fragment approach particularly attractive for modeling a defect in a larger supercell, for example.

30 1 N. S. Abraham and M. R. Shirts, 2017, arXiv:1712.00936 [cond-mat.mtrl-sci].

2 S. Wen, K. D. Nanda, Y. Huang and G. J. O. Beran, *Phys. Chem. Chem. Phys.*, 2012, **14**, 7578–7590.

3 Y. N. Heit and G. J. O. Beran, *J. Comput. Chem.*, 2014, **35**, 2205–2214.

35 (203:[205]205) **Marcus Neumann** asked: In the calculation of the Grüneisen parameter you apply hydrostatic pressure in order to estimate the unit cell changes under thermal pressure. How well is this approximation validated? What is the expected free energy error of the approximation?

40 **Gregory Beran** answered: We have not investigated this issue in detail, though we provide some discussion regarding the isotropic *versus* the quasi-anisotropic hydrostatic approach in our answer to Mihails Arhangeliskis' previous question. Abraham and Shirts recently investigated various ways of performing the quasi-harmonic approximation that include varying degrees of anisotropy.¹ They
45 found that fully anisotropic expansion allowed the crystal to adopt structures up to 1 kJ mol⁻¹ lower in energy than isotropic expansion. Free energy differences between polymorphs were even smaller, at a fraction of a kJ mol⁻¹. Our approximation, which lies intermediate between the isotropic and fully anisotropic
50 models, seems like it should perform reasonably well.

1 N. S. Abraham and M. R. Shirts, 2017, arXiv:1712.00936 [cond-mat.mtrl-sci].

(204:[206]206) **Joost van den Ende** remarked: In Figure 4 and Figure S6 you show the dependence of the molar volume and electronic energy of CO₂ as a function of the different density functionals + dispersion correction used. Intuitively, I would think that using empirical dispersion corrections works better for larger molecules which fall “better” in the training set of the used dispersion correction. Therefore I would argue that CO₂ might not be the best test system to analyse the performance of empirical dispersion corrections. As a very experienced user of electronic structure calculations, do you think there is a size dependence of the studied molecules on the precision of empirical dispersion corrections?

Gregory Beran responded: Previous work by Gohr *et al.* suggests that the dispersion correction is quite important even for carbon dioxide.¹ For example, the lattice energy of phase I is 8.7, 22.7, and 23.5 using PBE, PBE-D2, and PBE-D3(BJ), respectively. Omitting the dispersion correction also leads to substantial overestimation of the molar volume and underestimation of the bulk modulus. Similar evidence for the reasonably good performance of various dispersion corrections for carbon dioxide, acetic acid and imidazole can be found in ref. 2.

More generally, modern dispersion corrections (Grimme’s D3, Distasio and Tkatchenko’s many-body dispersion, and Becke and Johnson’s XDM) are largely non-empirical and adapt well to a variety of systems. So I do not think this small molecules used for some of the benchmarks are a significant problem. Our paper did use the more empirical D2 for a few results, since D3 was not available in the Quantum Espresso software used, and it generally performed less well. We do not advocate general use of the D2 correction.

1 S. Gohr, S. Grimme, T. Soehnel, B. Paulus and P. Schwerdtfeger, *J. Chem. Phys.*, 2013, **139**, 174501.

2 A. Otero-de-la-Roza and E. R. Johnson, *J. Chem. Phys.*, 2012, **137**, 054103.

(206:[207]207) **Johannes Hoja** said: You have shown that the quasi-harmonic approximation at the Tier 3 level provides a good description of the thermal expansion and accurate sublimation enthalpies for small molecule crystals. Do you have an estimate of the level of molecular flexibility up to which one could obtain reliable sublimation enthalpies and entropies using the quasi-harmonic approximation?

Gregory Beran replied: This is a really important question and one we intend to investigate in the future. The quasi-harmonic calculations do appear to perform well for acetaminophen in the paper, which has slightly more flexibility than the completely rigid small molecules considered in earlier parts of the paper. Of course, many pharmaceuticals and other organic molecules of interest exhibit far more flexibility than any of the species considered in our paper. For sufficiently flexible species, it might make more sense to treat them with molecular dynamics (using a high-quality potential) or some other technique which can capture the anharmonicity in these species. On the other hand, our paper shows (*e.g.* Figure 2) that zero-point vibrational energy can contribute appreciably to the molar

1 volume. Zero-point vibrational effects are not captured in classical molecular
dynamics. One might also expect that the anharmonicity of the intramolecular
vibrational modes will play an increasingly important role in larger molecules.
5 The use of a one-dimensional Morse approximation for the anharmonicity
described in your paper (DOI: 10.1039/C8FD00066B) might help address that
problem. Future work will hopefully provide further clarity on the practical limits
of the quasi-harmonic approximation for more flexible species.

10 (207:[208]208) **Michael Ruggiero** remarked: To follow up on the previous point,
in Tier 1 the unit cell was constrained to an isotropic expansion/contraction,
while in Tiers 2–4 the cell was allowed to optimize anisotropically. Does this
have any influence on the results?

15 **Gregory Beran** responded: This is a good point. The Tier 1 results come from
an earlier publication,¹ and our computational procedures have evolved since
then. In that work, we optimized the geometries on-the-fly (instead of using the
1D energy–volume curves). While that allows the structures to relax in a fully
anisotropic fashion, the Grüneisen parameters in that work were computed from
20 volumes that were scaled isotropically. For ice and carbon dioxide, the experi-
mental expansion is quite isotropic, so this is not a significant issue. However,
acetic acid and imidazole expand somewhat more anisotropically, so there is
probably some error introduced by computing the Grüneisen parameters under
an isotropic approximation. Specifically, one would anticipate that the energy
25 changes associated with those volume changes are too large, and that the
frequency changes for the lowest-energy phonon modes will be overestimated.
Hopefully the errors introduced by this approximation are small, and indeed the
Tier 1 thermal expansion curves are fairly parallel to the experimental ones.

30 1 Y. N. Heit and G. J. O. Beran, *Acta Cryst. B*, 2016, 72, 514–529.

35 (208:[209]209) **Michael Ruggiero** said: In the poster presented, the results
using phonon dispersion are very compelling. In the cases where phonon
dispersion isn't utilized and yields good results, in your opinion do you think that
this is due to a cancellation of errors, a system dependent case where phonon
dispersion isn't actually needed, or some combination of both?

40 **Gregory Beran** replied: For the Tier 3 hybrid approach, which we advocate due
to its relatively low computational cost and good quality of results, the thermal
expansion is pretty consistently underestimated across all the examples. As Jessica
McKinley showed in her poster at the meeting (for another example, see the
Electronic Supplementary Information for ref. 1), including phonon dispersion
helps correct this. In contrast, the Tier 1 results, which do include phonon
45 dispersion, track the experimental thermal expansion quite well. It is true that
some of the calculations (most notably the Tier 4 DFT calculations, especially those
with the D2 dispersion correction) expand the crystals more significantly with
increasing temperature, even without including phonon dispersion. We suspect
that this is due to error cancellation. As shown in Figures 2, 5 and S7 from the main
50 paper (DOI: 10.1039/c8fd00048d), the expansion is suppressed somewhat once the
MP2-level single-point energies are applied on top of those energies.

1 Y. N. Heit, K. D. Nanda and G. J. O. Beran, *Chem. Sci.*, 2016, 7, 246–255.

(209:[210]210) **Michael Ruggiero** asked: You've shown the importance of phonon dispersion for accurately determining thermodynamic properties, however such simulations are often prohibitively expensive. Is there any indication or marker for how much phonon dispersion to include to best marry computational cost and accuracy, or is it highly system dependent? To follow up, when thermodynamic values are computed accurately without phonon dispersion, what happens when dispersion is ultimately included? Are the non-dispersion simulations accurate due to a cancellation of errors, or do such methods simply not require dispersion?

Gregory Beran answered: We are pursuing additional strategies for capturing phonon dispersion effectively with reasonable computational cost and hope that it will be feasible to capture these effects in much larger crystals in the future. For example, Brandenburg *et al.* reported promising results in modeling the thermal expansion of carbamazepine with a density functional tight binding model.¹ Regarding the accuracy of the thermochemical predictions without phonon dispersion, one can obtain a reasonable estimate for the impact on the sublimation enthalpies or entropies by comparing the temperature dependent curvature of the Tier 1 *versus* Tier 3/4 results in Figures 6 and 7 of the main paper (DOI: 10.1039/c8fd00048d). Visual inspection suggests that the sublimation enthalpy errors at higher temperatures that are due to neglecting phonon dispersion are somewhere around 1–2 kJ mol⁻¹ for carbon dioxide, acetic acid and imidazole, for example. The errors are considerably smaller for ice, which expands much less due to the strong three-dimensional hydrogen bond network. In other words, the magnitude of the errors will depend on the nature of the crystal packing. It is possible, of course, that fortuitous error cancellation will sometimes lead to reasonable-looking predictions of thermochemical properties despite modeling the thermal expansion poorly.

1 J. G. Brandenburg, J. Potticary, H. A. Sparkes, S. L. Price and S. R. Hall, *J. Phys. Chem. Lett.*, 2017, 8, 4319.

(210:[211]211) **Sarah Price** said: Chick Wilson's paper¹ shows the thermal ellipsoids of a methyl group libration in form I paracetamol (acetaminophen) over the range of temperatures of the structures you have been modelling. The amplitude of the librations is huge, even as extrapolated to 0 K. Do you think that this may have affected your results for predicting the thermal expansion, as would the quasi-harmonic expansion be appropriate?

1 C. C. Wilson, Zero point motion of the librating methyl group in *p*-hydroxyacetanilide, *Chemical Physics Letters*, 1997, 280, (5–6), 531–534.

Gregory Beran responded: This is an interesting question that merits future investigation. At the moment, we lack the data to answer this definitively. In other cases we have examined, neglecting phonon dispersion leads to an underestimation of the thermal expansion. It would be interesting to perform the phonon dispersion calculations and see how much of the thermal expansion the model captures. The magnitude of the residual disagreement between the predicted and

1 experimental temperature dependence of the molar volumes could point toward
the importance of effects such as the high-amplitude librations you point to.

5 (211:[212]212) **Sarah Price** remarked: Your work has been very important in
showing that even zero-point lattice modes have a significant effect in expanding
the lattice, implying that lattice energy minimisation with the perfect model
would give errors for even the lowest-temperature crystal structures. The differ-
10 ence in methyl rotational amplitudes between polymorphs, depending on how
tightly the methyl group is packed, could well affect the relative free energies. It
would be unfeasible if we needed to calculate both quantum mechanical zero-
point effects and had to do classical MD to get a full description of how the
molecules are moving to get accurate thermodynamic and spectral properties.

15 **Gregory Beran** replied: This raises a good point. The quasi-harmonic approx-
imation has clear limitations (*e.g.* high temperatures or highly flexible molecules).
If one can obtain a good potential, switching to a dynamical treatment would be
an appealing way to circumvent those limitations. However, classical molecular
20 dynamics simulations do not capture the zero-point vibrational effects, which
appear to contribute appreciably to molecular crystal volumes (*e.g.* Figure 2 in the
main article (DOI: 10.1039/c8fd00048d)). There have been advances in path
integral molecular dynamics techniques in recent years,¹ so perhaps it will
become feasible at some point to use those types of approaches to capture the
25 nuclear quantum effects more effectively.

1 T. E. Markland and M. Ceriotti, *Nature Rev. Chem.*, 2018, 2, 0109.

30 (212:[213]213) **Seiji Tsuzuki** remarked: I have comments on the DFT calcula-
tions of the intermolecular interaction energy. You showed that the performance
of the DFT calculations for evaluating the sublimation energy is not very good.
The calculated sublimation energy depends on the calculated depth of the
intermolecular interaction energy potential. The depth of the potential depends
35 strongly on the choice of dispersion correction method and functionals used for
the DFT calculations. I believe that the choice of PBE functionals is not so good. I
believe that the performance of the calculations of the sublimation energies will
be improved if you choose an appropriate dispersion correction method and
functionals.

40 **Gregory Beran** responded: Our paper considers multiple different density
functionals and van der Waals dispersion corrections. Our most important results
use the B86bPBE-XDM model, which Erin Johnson and co-workers have
demonstrated works well for molecular crystals and other systems where non-
covalent interactions are important.^{1,2} In addition, one of the important results
45 in the paper is that when using hybrid approaches like Tier 3 that use
wavefunction-based single-point energy refinement of DFT geometries/
refinement, the final results are relatively insensitive to the choice of density
functional/dispersion correction (see Figure 4 in the paper).

50 During the discussion I also shared two predicted values for the sublimation
enthalpy of alpha methanol, which were taken from our recent paper.³ These
numbers compared the sublimation enthalpy computed with our fragment

1 method at the CCSD(T)/CBS + periodic HF level of theory. The difference between
the two values was whether we optimized the geometries and computed the
phonons using MP2-level fragment calculations (*i.e.* Tier 1) or with plane-wave
5 PBE-D3 (Tier 3). Because the single-point energies defining the energy–volume
curve are at the CCSD(T) level, the results are not directly dependent on the PBE-
D3 energy well depth. In that case, the Tier 1 sublimation enthalpy was
45.0 kJ mol⁻¹, which is in excellent agreement with the experimentally reported
value of 45.7 ± 0.3 kJ mol⁻¹.³ The Tier 3 value of 42.8 kJ mol⁻¹ has an error that is
10 several kJ mol⁻¹ larger. This result is consistent with our other results presented
in the *Faraday Discussions* paper (DOI: 10.1039/c8fd00048d), which demonstrate
that while the hybrid wavefunction/DFT calculations perform well, they are not
quite as good as those done entirely with higher-level wavefunction methods.

15 1 S. R. Whittleton, A. Otero-de-la-Roza and E. R. Johnson, *J. Chem. Theory Comput.*, 2017, **13**,
441–450.

2 S. R. Whittleton, A. Otero-de-la-Roza and E. R. Johnson, *J. Chem. Theory Comput.*, 2017, **13**,
5332–5342.

3 C. Cervinka and G. J. O. Beran, *Chem. Sci.*, 2018, **9**, 4622–4629.

20 (213:[214]214) **Seiji Tsuzuki** enquired: You used the HF method for the analysis
of many-body interactions. The HF method overestimates the Coulombic inter-
actions (electrostatic and induction interactions). The induction interaction is
a major source of the many-body interactions in general. Therefore, the HF
method probably overestimates the many-body interactions. On the other hand,
25 DFT calculations can evaluate Coulombic interactions more accurately owing to
the consideration of electron correlation. Why did you not use DFT calculations
instead of HF calculations for the evaluation of the many-body interactions?

30 **Gregory Beran** answered: Our experience has been that when focusing on the
long-range pairwise and many-body induction interactions, HF typically performs
better than typical generalized gradient approximation (GGA) and can even be
better than hybrid density functionals. There are examples of fragment methods
that combine periodic DFT with monomer and dimer corrections computed with
35 wavefunction methods,^{1–3} However, those work best in cases where polarization
effects are relatively weak. This can be understood in terms of the delocalization
errors and problems in the many-body repulsion inherent in density functionals.
Our earlier benchmark calculations on three-body interactions demonstrate this
nicely.⁴ Additional discussion of repulsion issues can be found in a paper by
40 Gillan.⁵ In the context of our fragment approaches, it is important to emphasize
that the energies are dominated by the 1-body and shorter-range 2-body terms,
which are computed with higher levels of theory. HF is only used for the non-
pairwise additive contributions involving three or more molecules. In practice,
such contributions are typically no more than 10–20%, and often they are 5–10%.

45 1 O. Bludsky, M. Rubes and P. Soldan, *Phys. Rev. B*, 2008, **77**, 092103.

2 S. Tsuzuki, H. Orita, K. Honda and M. Mikami, *J. Phys. Chem. B*, 2010, **114**, 6799–6805.

3 C. R. Taylor, P. J. Bygrave, J. N. Hart, N. L. Allan and F. R. Manby, *Phys. Chem. Chem. Phys.*,
2012, **14**, 7739–7743.

4 J. Rezac, Y. Huang, P. Hobza and G. J. O. Beran, *J. Chem. Theory Comput.*, 2015, **11**, 3065–
3079.

50 5 M. J. Gillan, *J. Chem. Phys.*, 2014, **141**, 224106.

(803:[215]215) **Gerit Brandenburg** communicated: The authors nicely analyzed how to combine different electronic structure methods to compute different components of the free energy (relaxed geometry, lattice energy, lattice dynamics). I wondering if their ranking (good to less good) is well justified in following the hierarchy of HMBI, DFT, FF. This will most likely depend on the type of many-body methodology that is used for the clusters and the type of embedding. As a first point, the many-body method employed is mostly MP2, which is certainly appropriate for CO₂ and ice I_h. However, for unsaturated π -stacked systems, MP2 is known to have deficiencies and DFT might be even more accurate. The literature data on the studied systems is summarized in Table 2. Could the authors comment on the accuracy of the employed HMBI variants for the lattice energy? The second issue is the force field describing the embedding. While I am confident that both geometries and energies from the HMBI approach will be only slightly perturbed by the embedding, this might not hold for the low-energy frequency modes. Have the authors studied this, for instance by enlarging the region that is treated with the many-body method?

1 A. Otero-de-la-Roza and E. R. Johnson, *J. Chem. Phys.*, 2012, **137**, 054103.

2 A. M. Reilly and A. Tkatchenko, *J. Chem. Phys.*, 2013, **139**, 024705.

3 A. Zen, J. G. Brandenburg, J. Klimeš, A. Tkatchenko, D. Alfè and A. Michaelides, *Proc. Natl. Acad. Sci. USA*, 2018, **115**, 1724.

4 S. Wen and G. J. O. Beran, *J. Chem. Theory Comput.*, 2011, **7**, 3733.

5 M. J. Gillan, D. Alfè, P. J. Bygrave, C. R. Taylor and F. R. Manby, *J. Chem. Phys.*, 2013, **139**, 114101.

6 M. Cutini, B. Civalleri, M. Corno, R. Orlando, J. G. Brandenburg, L. Maschio and P. Ugliengo, *J. Chem. Theory Comput.*, 2016, **12**, 3340.

Gregory Beran communicated in reply: Lattice energies: We agree about the limitations of MP2 for describing non-covalent interactions. This issue in the context of molecular crystals is discussed in some detail in our earlier review.¹ There are multiple strategies for addressing these MP2 deficiencies, but one of our favored approaches and one we adopt in the current paper is MP2C.² This employs intermolecular perturbation theory to correct the treatment of the dispersion energy in MP2. Based on its excellent performance for non-covalent interactions and $O(N^5)$ scaling with system size N , David Sherrill and co-workers anointed MP2C the “bronze standard” for non-covalent interactions.³ We have used MP2C to study the polymorphs of oxalyl dihydrazide,⁴ and we have a new MP2D model⁵ which recasts MP2C in a framework based on Grimme’s D3

Table 2 Lattice energies of the studied crystals from MP2 and DFT compared to semi-experimental estimated and high-level results. Energies are given in kJ mol⁻¹

	Semi-exp. ^a	DMC ^b	MP2 ^c	DFT ^d
CO ₂	-28.4	-28.2	-29.1	-21.6
Ice I _h	-58.8	-59.2	-58.7	-72.8
Acetic acid	-72.8	—	-61.2	-71.8
Imidazole	-86.8	—	-88.6	-87.5

^a Experimental sublimation enthalpies with estimations of zero-point and thermal effects from DFT computations as summarized in ref. 1–3. ^b Diffusion Monte Carlo data from ref. 3. ^c MP2 data from ref. 4–6, non converged basis set for acetic acid and imidazole. ^d B86bPBE-XDM for CO₂, acetic acid, imidazole, PBE-D3 for ice I_h.

1 dispersion correction. MP2D extends the range of applicability of MP2C to also
include intramolecular interactions and facile geometry optimizations, which
could prove useful in molecular crystals.

5 To compare against the lattice energies you cite, we extracted our best Tier 3
lattice energies at the MP2/aug-cc-pVTZ + AMOEBA and MP2C/CBS + periodic HF
levels. Specifically, we evaluated the crystal energy at the minimum of the energy
versus volume curves that result from single-point energy refinement on the
10 B86bPBE-XDM geometries. As can be seen in Table 3, MP2/augcc-pVTZ +
AMOEBA performs well for carbon dioxide, reasonably for ice, and poorly for
acetic acid and imidazole. Imidazole in particular demonstrates the problem of
MP2 over-binding the van der Waals dispersion interactions involving π systems.

15 Refinement of the single-point energies by replacing MP2 with MP2C,
extrapolating to the complete basis set limit, and improving the many-body
treatment from the AMOEBA force field to periodic Hartree-Fock leads to
considerable improvement. Three of the four MP2C/CBS + periodic HF lattice
energies lie within 2 kJ mol⁻¹ of the semi-experimental value. For acetic acid, the
error is larger at 4 kcal mol⁻¹. More detailed analysis of basis set effects and post-
20 MP2 correlation contributions are found in our earlier studies.⁶⁻⁸ Aside from
acetic acid, the MP2C lattice energies are appreciably better than the results we
obtained with our own B86bPBE-XDM calculations, which are also reported in
Table 3.

25 For additional comparison, consider the sublimation enthalpy data in our
paper. For acetic acid at 50 K (the lowest temperature we have experimentally
derived values for), the predicted and experimental sublimation enthalpies are
63.4 and 66.0 kJ mol⁻¹, or an error of 2.6 kJ mol⁻¹. Looking at all four crystals, the
errors in the low-temperature sublimation enthalpies are in the range of \sim 1-3 kJ
mol⁻¹ with MP2C (Figure 6). The sublimation enthalpies computed with
30 B86bPBE-XDM in our paper exhibit errors of \sim 3-8 kJ mol⁻¹. Overall, the accuracy
of sublimation enthalpies and lattice energies appears fairly consistent, especially
given that the experimental data may well have uncertainties of a couple of kJ
mol⁻¹ or more.

35 From a pragmatic point of view, dispersion-corrected DFT has advanced
tremendously over the last decade, and it performs very well for many molecular
crystal problems.⁹⁻¹¹ In many cases its accuracy is more than sufficient to make
useful predictions. However, in cases where one is not confident in the DFT
results (*e.g.* when particularly small energy differences are obtained or when one
observes high sensitivity of the results to the specific functional or dispersion
40 correction), then the fragment approaches provide an alternative that can allow

Table 3 Lattice energies for the four small molecule crystals (kJ mol⁻¹). Errors vs. the semi-experimental values are given in parentheses

	Semi-exp.	MP2/aug-cc-pVTZ + AMOEBA	MP2C/CBS + periodic HF	B86bPBE-XDM
CO ₂	28.4	27.7 (-0.7)	26.3 (-2.1)	23.9 (-4.5)
Ice	58.8	55.4 (-3.4)	57.4 (-1.4)	67.9 (9.1)
Acetic acid	72.8	64.5 (-8.3)	68.7 (-4.1)	73.5 (0.7)
50 Imidazole	86.8	101.2 (14.4)	88.8 (2.0)	90.8 (4.0)

1 one to push toward even higher accuracy. This philosophy fits nicely with the Tier
3 approach: if DFT modeling of a given system proves inconclusive, the results can
be refined with moderate amounts of additional computational work.

5 Embedding: First let us clarify that we do not embed in the traditional sense
(*e.g.* there is no electrostatic embedding). Rather, the quantum mechanical
monomers and dimers are computed in isolation, and those terms are used to
replace the corresponding polarizable MM contributions from the super-system
calculation.⁶ That said, one parameter in our model is the distance interval
10 over which one should transition smoothly from the short-range dimers treated at
the high level (*e.g.* MP2 or MP2C) to long-range dimers modeled at the low level
(AMOEBA or periodic HF). We typically choose a conservative interval of 9–10 Å for
this transition, which ensures that the important pairwise interactions are well
15 described by the high-level method. We have examined these cut-offs in some
detail previously.¹² For the many-body contribution, which is evaluated solely at
the low level of theory, replacing AMOEBA with periodic HF provides an improved
description and insight into the approximation made using AMOEBA. In addition
to the data shown in the *Faraday Discussions* paper (DOI: 10.1039/C8FD00048D),
20 the positive impact resulting from this model improvement is also demonstrated
in our recent work on the methanol phase diagram.¹³ Switching from AMOEBA to
periodic HF for many-body treatment brings the predictions of the both the
sublimation enthalpy and the molar volume of alpha methanol into excellent
agreement with experimental results.

25 1 G. J. O. Beran, *Chem. Rev.*, 2016, **116**, 5567.

2 A. Hesselmann, *J. Chem. Phys.*, 2008, **128**, 144112.

3 L. A. Burns, M. S. Marshall and C. D. Sherrill, *J. Chem. Phys.*, 2014, **141**, 234111.

4 S. Wen and G. J. O. Beran, *J. Chem. Theory Comput.*, 2012, **8**, 2698.

5 J. Rezáč, C. Greenwell and G. J. O. Beran, *J. Chem. Theory Comput.*, 2018, submitted.

6 G. J. O. Beran and K. Nanda, *J. Phys. Chem. Lett.*, 2010, **1**, 3480.

7 S. Wen and G. J. O. Beran, *J. Chem. Theory Comput.*, 2011, **7**, 3733.

8 Y. Huang, Y. Shao and G. J. O. Beran, *J. Chem. Phys.*, 2013, **138**, 224112.

9 M. A. Neumann, F. J. J. Leusen and J. Kendrick, *Angew. Chem., Int. Ed.*, 2008, **47**, 2427.

10 S. Grimme, A. Hansen, J. G. Brandenburg and C. Bannwarth, *Chem. Rev.*, 2016, **116**, 5105.

11 J. Hoja, A. M. Reilly and A. Tkatchenko, *WIREs Comput. Mol. Sci.*, 2017, **7**, e1294.

12 S. Wen, K. Nanda, Y. Huang and G. J. O. Beran, *Phys. Chem. Chem. Phys.*, 2012, **14**, 7578.

13 C. Červinka and G. J. O. Beran, *Chem. Sci.*, 2018, **9**, 4622.

35 (214:[216]216) **Ivo Rietveld** opened the discussion of the paper by Grahame R.
Woollam: To what level do the results of the crystal structure prediction help
explain the experimental results: the observed stability behaviour of the poly-
morphs and the conditions under which those polymorphs can be obtained?

40 **Grahame Woollam** responded: The experimentally observed stability rela-
tionship is only reproduced in the crystal structure landscape when the energy
contribution of disorder is taken into account. The disordered model of Form I is
found to be lower in energy than all of the other predicted structures and there is
45 no indication of a missing thermodynamically more stable form, which repre-
sents the outcome of the experimental polymorphism screens. Experimentally
Form II is metastable to Form I, converting during competitive ripening studies.
The calculated internal energy difference for Forms II and I is 0.54 kcal mol⁻¹,
50 which compares well to the experimentally measured (by DSC) exothermic crys-
tallisation enthalpy of 0.33 kcal mol⁻¹ (following the melt of Form II). Concerning

1 the conditions to prepare Form II, it cannot be formed by a simple recrystallisation
2 procedure; we need to do something extreme to prepare the metastable
3 form. The toluene/TBME method gives it; in retrospect, we can access both
4 conformers from solution. The kinetically driven process results in a structure
5 that accommodates both conformers in the frozen-in disordered Form II structure.
6 From the crystal structure landscape, we see that the Form II disorder model
7 moves up in relative energy in between the single components of ranks 1 and 58.
8 Conversely, the Form I disorder model moves down to a lower relative energy than
9 either single component (ranks 11 and 45) by more than $kT \ln 2$.

10
11 (215:[217]217) **Graeme Day** enquired: You have shown in this paper that, by
12 properly modelling disorder in Form I, the prediction results improve and
13 disordered Form I gets resolved to below the global lattice energy minimum of the
14 landscape of ordered crystal structures. To be confident in now having the correct
15 energy ranking, wouldn't we have to look at every structure on the landscape and
16 assess whether it has disordered configurations? Have you looked at modelling
17 the disorder in some of the other predicted structures to see if they gain a similar
18 amount of stabilisation? In terms of assessing disorder as part of a workflow,
19 could you also comment on how automated the procedure could be made:
20 identifying structures with disorder, creating symmetry adapted ensembles and
21 assessing the resulting free energy? Identifying structures that could be disordered
22 seems to be the trickiest step.

23
24 **Grahame Woollam** replied: The contrast of the *ab initio* crystal structure
25 landscape featuring the single component of experimentally metastable Form II
26 as rank 1 prompted a closer look into the structures containing two molecules in
27 the asymmetric unit. If we accept that in the case of loratadine the ordered
28 structures containing two molecules in the asymmetric unit provided insight into
29 the relevance and importance of configurational variation, it is even more infor-
30 mative that only families 1 and 2 contained $Z' > 1$ (Forms II and I, respectively). As
31 such, we have explored all families that may exist in other ordered arrangements
32 with lower symmetry that were not generated by the CSP procedure.

33
34 This is a pertinent point; we are actively working in this area. A stepwise
35 approach is required; the largely automated workflow follows the order identified
36 by Graeme Day. For the moment, we are working pragmatically by benchmarking
37 using systems with experimentally determined disorder. Indeed, identifying
38 *a priori* that a molecule could feature thermodynamically favourable disorder is
39 a challenge. However, going back to the CSP of loratadine, the $Z' = 2$ structures
40 were informative; Form I conformers 1 and 2 were found 18 and 19 times,
41 respectively. Of those 18 times, conformer 1 (AAAA) coincided with a second
42 conformer 1 within a $Z' = 2$ structure just once (*i.e.* AAAA and AAAA). Whereas
43 eight out of the 38 $Z' = 2$ structures contain both Form I conformers 1 and 2 (AAAA
44 and AABA), suggesting that the low-energy structures containing both conformers
45 1 and 2 result in a thermodynamically stable product, owing to the number of
46 times they were generated *ab initio* (thermodynamically favourable). Additionally,
47 all of the AAAA and AABA structures are within $0.90 \text{ kcal mol}^{-1}$ of the lowest-
48 energy structure.

49
50 Conversely, Form II conformers 1 and 2 appear together in a $Z' = 2$ structure
51 just once (ABAA and BBAA) in rank 12, highlighting that the structure is stable at

1 only 0.61 kcal mol⁻¹ higher energy than rank 1; however, not as significant as the
Form I AAAA and AABA configuration. As such, a thorough investigation of the $Z' >$
5 1 structures may provide the necessary information to get started on the
symmetry adapted ensembles to assess the resulting free energies.

(225:[218]218) **Jason Cole** said: Graeme Day made the point that it would be
interesting to analyse the possibility of lowering the energies of all structures in
the predicted landscapes by using the same substitution of conformations. I was
10 wondering whether this had been attempted for any individual examples, other
than the experimental cases, to get an understanding of what the overall distortion
to the CSP landscape might be expected as a consequence: *i.e.* how common
is the motif in the modelled structures that gets energetically improved by
considering the disorder?

15 **Grahame Woollam** answered: There has been no disorder modelling of the
predicted structures outside of Form I (family 2, energy rank structures 11 and 45)
and Form II (family 1, energy rank structures 1 and 58). Families 3–5 and the
individual structures have not been assessed; the response to Graeme Day's
20 question on this paper applies here. For families 1 and 2 the motifs don't change
following the introduction of configurational variation; they remain as rods and
mosaics coming from the single component systems and matching the experi-
mental structures of Forms II and I, respectively.

25 (234:[219]219) **Christian Schön** remarked: The discussion about disorder
brings to my mind the issue of time scales and self-averaging. It appears to me
that frozen-in disorder is just a matter of time scales, and similarly when we
discuss dynamical disorder. It is really important to take the observational time
scales into account when deciding whether one should add a configurational
30 entropy term to the free energy. Now, in macroscopic (and often even in meso-
scopic) systems, one can never fully equilibrate all the disordered states, since we
cannot explore enough of the configuration space of the energy landscape for
such systems. However, we can hope to use the self-averaging concept: here we
would divide the macroscopic system into many subsystems that are just at the
35 size limit of being a “macroscopic” system, in the sense that we would still
recognize them as miniature representatives of the bulk system. If the equili-
bration time scales of these sub-systems are short enough that we can assume the
sub-blocks are pretty close to equilibrium on the observational time scale, then we
can approximate the full free energy by a sum over the free energies of each such
40 sub-system, where each sub-system will have a slightly different free energy (as if
they were members of a Boltzmann ensemble), but their average will be a good
approximation to the total free energy of the macroscopic system (that is where
the term “self-averaging” comes from, of course). Here, it is important to keep in
45 mind that when trying to identify systems with “controlled disorder”, such as
solid solutions (the disorder only applies to the distribution of *e.g.* two cations on
the positions of one cation in the aristotype of the solid solution structure, but not
to the underlying cation–anion–lattice structure!) during a crystal structure
prediction using global optimization techniques, we need to analyze all the
50 minimum structures found and place them into structure families – often there
are several structure families within one chemical system (*e.g.* a rocksalt family

1 and a wurtzite family in mixed alkali-halide compounds¹). This can lead to
several solid solution phases present in the same diagram with different life-
times,² *i.e.* on short observational time scales the system can be in one solid
5 solution phase or the other (without knowing that another feasible – perhaps
more stable – solid solution phase exists in the system)! Proceeding in this
fashion for molecular crystals by identifying families of local minimum structures
sounds very promising.

10 On another point, you also discussed the asymmetric unit in your study, but I
am not quite sure that this makes sense – once you insert disorder, the symmetry
of the structure is lost, and thus the asymmetric unit becomes the full set of
atoms/molecules in the cell. So how can you proceed the way you do once this
symmetry is lost?

15 1 J. C. Schön, I. V. Pentin and M. Jansen, *J. Phys. Chem. B*, 2007, **111**, 3943–3952.

2 M. Jansen, I. V. Pentin and J. C. Schön, *Angew. Chem., Int. Ed.*, 2012, **51**, 132–135.

20 **Grahame Woollam** responded: In our paper we used symmetry-adapted
ensemble theory to compute the configurational free energy of Form I. The free
energy of this form is associated with disorder that is a thermodynamic equilib-
rium property. The approach is indeed only valid if the system under consideration
has the time to equilibrate. Since neither crystal structure prediction nor symmetry-
adapted ensemble theory provide rate constants for configurational changes, we
take a pragmatic approach to decide whether the method is applicable. We first use
25 symmetry-adapted ensemble theory to compute occupancy factors for each
molecular conformation. If the calculated occupancies match the experimental
occupancies to within a few percent, we take this as a confirmation that the system
is indeed close to equilibrium and that symmetry-adapted ensemble theory applies.
If, on the other hand, the computed and experimental occupancies strongly
30 disagree, we conclude that the disorder is not an equilibrium property. Exper-
imental occupancies are determined for the atoms in the asymmetric unit. In
symmetry-adapted ensemble theory, individual configurations indeed break the
crystal symmetry, but not so the actual ensemble. By averaging over all config-
urations of the ensemble and their symmetry copies, a computed asymmetric unit
with computed occupancies is obtained that can be compared to the experimental
35 results. It is important to realise that molecular crystals can get into a state close to
thermodynamic equilibrium even if the rate constants for configurational changes
in the bulk are so slow that the disorder appears static. When crystals grow, there is
a surface layer in which molecules are significantly more mobile than in the bulk
and are subjected to intermolecular interactions that resemble the crystal field of
40 the bulk. The surface layer can hence equilibrate towards a bulk-like equilibrium
state. In such cases, the standard textbook formulas for the calculation of the
configurational free energy apply at the temperature of the crystal growth process.

45 *P1* structures are commonly used to construct or depict a supercell for
simplicity. However, the supercells of loratadine do maintain symmetry elements;
this is a key aspect of the SAE model, and the disordered components interacting
with one another.

50 (216:[219]220) **Aurora Cruz-Cabeza** queried: I would like to know whether the
disorder in loratadine Form I is static or dynamic.

1 **Grahame Woollam** answered: The ratio of Form I conformers 1 and 2 changed
with increasing temperature; conformer 1 increased from 0.51 at 10 K through to
0.55 at 273 K, with the change marginally outside of 3 times e.s.d. At 353 K (just 54
5 K below the melting point of Form I) the increase in ratio was discontinuous.

10 (217:[220]221) **Aurora Cruz-Cabeza** asked: If disorder in Form I is dynamic,
then rotation of the group would need to be considered through molecular
dynamics. This may be a limitation for your static model of disorder and poses
a challenge for the computation of entropies and free energies.

15 **Grahame Woollam** replied: Dynamic disorder is temperature dependent
disorder; could we consider that Form I is dynamic based on the information
above? Static disorder is considered random and free to orient; while the carba-
mate tail has a number of configurations available, the “forward” and “back”
positions are favoured in the crystal systems with alternating frequency. The
disorder models don’t represent the model as random and free to orient, but
instead thermodynamically favourable through alternating configurations in
microdomains. Substitutional disorder, which is largely seen in inorganic
20 chemistry, is where chemically inequivalent species replace the host molecules in
a substitutional manner, as the name suggests. If this is considered to be like
static disorder, perhaps Form I could be considered a chemically equivalent solid
solution. Definitions are taken from Disorder in crystal structures: new
approaches in finding the best model, Markus Neuburger, Basel, 2012.¹ The QM
static calculation may be regarded as a microstate of what an MD simulation
25 could provide (with improved accuracy). The static calculation may represent
a frame from the MD trajectory(?). However, we do not capture the information
over time scales and temperature using the static approach. The experimental
occupancy measured in Form I changes with temperature, although marginally.
30 As such, the difference is subtle, which may ultimately be within the error asso-
ciated with the MD force field calculations.

1 Disorder in crystal structures: new approaches in finding the best model, Markus Neu-
burger, Basel, 2012.

35 (218:[221]222) **Aurora Cruz-Cabeza** said: The disorder present in loratadine
Form II is static. The molecules are “frozen” in the conformations available
during crystallisation. I wonder if crystallisations of Form II have been carried out
at different temperatures and whether or not a change in occupancies has been
40 observed.

45 **Grahame Woollam** responded: Many crystallisations have been attempted to
prepare Form II; the conditions are specific and prescribed, and as such the form
is crystallised with an onset *ca.* 20 °C and isolated at 4 °C. No other preparations
have yielded Form II; instead Form I is prepared from the same solvent and solute
composition if isolated at higher temperatures. The best Form I crystals, for
example (and those used in the ν T-SCXRD experiments), were obtained from
toluene/TBME isolated at room temperature. The Form II single crystal structure
presented in the paper was solved at 10 K using Synchrotron radiation. A 100 K
50 structure solution was made using equipment available in-house; however the

1 quality of the data did not allow the same conclusions to be drawn for Form II as
for Form I. This relates to the size and quality of the metastable crystals formed
under severe kinetically driven conditions.

5 (219:[222]223) **Rui Guo** asked: If loratadine Form II is indeed frozen-in during
the specific crystallization setup, can we assume that the global minimum found
in the CSP is still out there, waiting to be found? Are there any temperature-varied
experiments on Form II, similar to those for Form I in Table 3?

10 **Grahame Woollam** answered: If the question relates to the rank 1 structure,
which is an ordered component of Form II, given our time frame and crystal-
lisation conditions, it is hypothesised that Form II is an accommodating structure
that is adopted due to its ability to feature the two configurations of the cyclo-
heptane head group. The structures of family 1 are less numerous on the crystal
15 landscape, and from a solution mediated process we would expect to convert to
the more stable Form I as the crystal landscape is dominated by this family of
structures; as such, many nucleation avenues lead to this dynamically favoured
form. It may be postulated that the Form II structure could anneal in the solid
20 state to a fully ordered single-component structure given sufficient time, the
correct temperature and perhaps humidity to enable relaxation. However, the
saddle point for conversion of the cycloheptane head group from the BBAA to the
ABAA conformation in this accommodating structure is increased (as calculated
from the Form II disorder model structure) to $2.5 \text{ kcal mol}^{-1}$, as compared to
25 $2.0 \text{ kcal mol}^{-1}$ in the Form I disorder model structure. Regarding vT-SCXRD, the
response to the previous question applies.

30 (222:[223]224) **Rui Guo** queried: With regard to the supercells you used to
calculate the energy gain from configuration disorder, how sensitive is this energy
to the size and shape of the supercells?

35 **Grahame Woollam** replied: When disordered sites are close enough to interact
strongly, the isolated site model is not applicable and in principle one needs to
consider all combinations of disordered configurations in a cell or supercell.
However, many of these combinations are symmetry equivalent, and by limiting
lattice energy calculations to one representative per symmetry equivalent set and
working out the correct multiplicities, the computational effort can be greatly
40 reduced. This approach is called symmetry-adapted ensemble theory. Typically
the number of molecules per cell or supercell would be the right choice to feature
in the calculation of energy gain, though with Forms I and II of loratadine an
alternative selection allowed for the conservation of computational time. In both
cases it was clear from geometrical calculations that the disordered sites interact
45 along one-dimensional rods, with little interaction between the rods. Therefore,
the energies refer to the number of molecules per rod, with two rods per supercell.
The evaluation of the energy differences was again based on the energies of the
entire supercell. As such the energy calculations are not sensitive to the size and
shape of the cell/supercell.

50 (221:[224]225) **Rui Guo** asked: Did you use the supercells of the same size and
shape for both forms of loratadine? Isn't it reasonable to assume that a more

1 balanced choice of supercells should be based on their specific ways of molecular
packing, which as you have shown clearly for the two forms are indeed rather
different?

5 **Grahame Woollam** answered: The supercells were constructed independently;
both feature doubling of the shortest axis (incidentally the *b* axis in both systems,
and as such $1 \times 2 \times 1$ supercells resulted) in order to capture the interactions
between neighbouring disordered molecules – translated and featuring the
stacking of the tricyclic ring systems.

10 (223:[226]227) **Jason Cole** enquired: Have any efforts been made to explore
incommensurate refinements or possible very large supercells with respect to the
crystallography to resolve or more accurately model the underlying statistical
disorder in the forms?

15 **Grahame Woollam** responded: No refinements were made to the experimental
structures to resolve an incommensurate structure or very large supercell.

20 (224:[225]226) **Jason Cole** asked: Were satellite peaks observed in the structural
data, as these would be indicative of a more ordered supercell?

25 **Grahame Woollam** replied: There were no interpretable additional peaks
observed for any structures.

30 (226:[227]228) **Sten Nilsson Lill** enquired: In relation to the comment by
Aurora Cruz-Cabeza, have you investigated the barriers and dynamics involved for
interconversion of the conformers seen in the disordered parts of your crystal
structures I and II?

35 **Grahame Woollam** answered: There have not been any MD calculations to
investigate the flipping of the alternating configurations in the crystal. However,
the saddle point for conversion of the cycloheptane head group from the BBAA to
the ABAA conformer in the Form II disorder model structure was calculated to be
2.5 kcal mol⁻¹, as compared to 2.0 kcal mol⁻¹ in the Form I disorder model
structure. This encourages the idea that the alternative cycloheptane head
configuration is frozen-in. In terms of varying the ethyl carbamate tail in Form I,
Table 5 demonstrates the energy gain or penalty from having a favourable or
unfavourable assembly, with the $1 \times 2 \times 1$ supercell featuring the configuration of
conformer 2, 1, 2, 1 in the abcd configuration, *i.e.* a 50 : 50 occupancy at 0 K (see
Figure 14).

45 (227:[228]229) **Susan Reutzl-Edens** remarked: You have indicated that Form
II, the polymorph with “frozen-in” disorder, was obtained under a very specific set
of conditions, so perhaps it is unsurprising that only a limited range of disorder
was ever observed for this polymorph. As it is not unusual to find limited
conditions in which to nucleate a specific polymorph, I am curious as to whether
you have considered seeding to possibly grow Form II crystals under diverse
50 conditions to assess the accessible range of disorder experimentally. Can you
please comment?

1 **Grahame Woollam** responded: This is a valid point; perhaps the limited range
of crystallisation conditions provide a limited range of disorder observed exper-
5 imentally, because the structure accommodates those configurations available
from the solution to the interface/bulk of the crystal. On the flip side, it could be
that the accommodating structure is only formed under such conditions, whereby
10 the available solution conformers are provided at a specified rate during desu-
persaturation through both the cooling crystallisation and self-induced drown-
out concomitantly to form such a metastable structure, which is fleeting in any
other organic solvent systems, yet long-lasting in the solid state.

15 (229:[229]230) **Sharmarke Mohamed** said: This work has shown that the crystal
form landscapes generated from crystal structure prediction methods could be
used to rationalise the observed crystal disorder for conformationally flexible
20 molecules. It is promising to see that GRACE is capable of locating the two
ordered components of each disordered structure of loratadine. Could the
authors comment on the capabilities of GRACE in modelling cases of dynamic
proton disorder (*i.e.* in ionisable molecules leading to salts or cocrystals) where
25 you have covalent bond breaking and formation as a result of proton disorder?
This is not just a question that is of general academic interest (although the
problem of proton disorder clearly continues to be a challenge for crystallogra-
phers), but as was evident in the discussions, there are clear regulatory require-
ments in formulating active pharmaceutical ingredients in solid forms with well-
30 defined covalent bonding. The relative energies of the neutral or ionised forms of
molecular complexes can be significant and so it is interesting to know whether
GRACE can suggest the correct molecular complex (salt or cocrystal) as well as the
energy barrier/stability for proton migration.

35 **Grahame Woollam** replied: The prediction of proton positions and proton
disorder in molecular crystals of pharmaceutical interest is still a challenge. The
problem is not specific to GRACE, but rather related to the underlying level of
theory in the computation of the potential energy hypersurface. According to the
40 experience of one of the authors (Marcus Neumann), calculations with the PBE
functional and the Neumann-Perrin dispersion correction have a substantial
failure rate in identifying the correct proton position in cases where the proton
position is ambiguous.

45 (231:[231]231) **Doris Braun** remarked: In Table 4 of your manuscript an
enthalpy of recrystallisation of $0.33 \text{ kcal mol}^{-1}$ is given, which is also compared to
the internal energy difference obtained for Forms II and I ($0.54 \text{ kcal mol}^{-1}$). Does
50 the value really correspond to the enthalpy of recrystallization? How was it
measured/integrated?

Grahame Woollam responded: The value relates to the exothermic transition
(crystallisation) measured by DSC following the melt of Form II and prior to the
subsequent melt of Form I.

 (232:[232]232) **Doris Braun** commented: The enthalpy of fusion rule¹ is often
50 applied to derive the energy differences between polymorphs, which gives an

1 energy difference (enthalpy of transformation) of $1.74 \text{ kcal mol}^{-1}$ for the two
loratadine polymorphs.

5 1 A. Burger and R. Ramberger, On the polymorphism of pharmaceuticals and other
molecular crystals: I. Theory of thermodynamic rules, *Mikrochimica Acta*, 1979, 2, (3–4),
259–271.

10 **Grahame Woollam** replied: For the 10 K min^{-1} heating rate and conditions
applied, this value is correct and represents the difference in enthalpy of fusion
between the polymorphic pair, assuming full and complete melting, without
interference of the recrystallisation exotherm.

15 (233:[233]233) **Doris Braun** asked: By integrating the melting peak of Form II
(5.09 kJ mol^{-1}) and the recrystallisation peak of Form I ($-6.83 \text{ kJ mol}^{-1}$, if
complete recrystallisation occurred), the value should be exothermic and not
endothermic.

Grahame Woollam answered: It is indeed exothermic.

20 (235:[235]235) **Virginia Burger** enquired: I have a question about how each of
the partially occupied conformers is identified within a disordered polymorph. Is
disorder identified within the electron density map and are the individual
conformers then fitted to the map and assigned occupancies based on their
25 electron densities? Are the actual partially occupied conformers visible within the
electron density map? Or could, for example, polymorph Form I have been
assigned three (or more) partially occupied conformers instead of just two?

30 **Grahame Woollam** responded: We see two distinct conformations in the
electron density.

(236:[236]236) **Virginia Burger** asked: In the electron density for polymorph
Form I, does the crystallographer see two distinct configurations (for conformers
1 and 2), or is the data just “blurry”?

35 **Grahame Woollam** answered: We see two distinct conformations in the elec-
tron density.

40 (237:[237]237) **Michael Ruggiero** opened the discussion of the paper by Samuel
A Jobbins: What happens when the system requires some large-scale re-
orientation, perhaps occurring along a non-intuitive pathway? What limitations
are there to the *metashooting* technique? Do you limit yourself by inputting the
transition state directly? How prone is the algorithm to “missing” the right
45 mechanism?

50 **Samuel Jobbins** responded: Thanks for your questions. The transition mech-
anism is deduced by implementing “plain” transition path sampling, which is
completed prior to the *metashooting* procedure being carried out. Thus, by the
time the *metashooting* takes place, the most likely subset of the transition path
ensemble has been obtained (which is what is sampled using the *metashooting*).

1 The shooting steps that take place in the *metashooting* part of the work are to generate the correct velocity distributions for new trajectories on the biased energy surface, in order to ensure control in the variation of the collective variable.

5 Large-scale reorientations may occur in the transition path sampling runs. When one generates an initial trajectory using the geometrical–topological procedure we have followed, it is quite easy to deliberately avoid unfavourable regions of the trajectory space. If any large-scale reorientation is to occur, the path sampling algorithm should find it – however, it may take more iterations of the algorithm before the converged subset of trajectories is found.

10 Inputting the transition state directly should not itself not be a limitation – in fact, we consider it a positive of the method. The transition state for both the transition path sampling and the *metashooting* must be dynamical, as it is mandatory that it links the two basins of attraction. The initial path sampling intermediate is generated from the geometric trajectory, and the initial *meta-shooting* intermediate may be any point along a (converged) trajectory that links the two basins. From here, shooting to the two basins and filling up from the “outside-in” allows for accurate weighting of the entire underlying free energy landscape.

20 Finally, the algorithm should not “miss” the ideal trajectory. Transition path sampling, by definition, should always find the most favourable subset of transition pathways in trajectory space. It is these that are biased upon in the *meta-shooting* technique, and the trajectories that we report in the paper. Further information can be found in papers on transition path sampling.^{1–3}

25 1 C. Dellago, P. G. Bolhuis, F. S. Csajka and D. Chandler, *J. Chem. Phys.*, 1998, **108**, 1964–1977.

2 P. G. Bolhuis, D. Chandler, C. Dellago and P. L. Geissler, *Annu. Rev. Phys. Chem.*, 2002, **53**, 291–318.

30 3 C. Dellago, P. G. Bolhuis and P. L. Geissler, *Advances in Chemical Physics*, ed. I. Prigogine and S. A. Rice, John Wiley and Sons, 2002, pp. 1–78.

35 (238:[238]238) **Michael Ruggiero** asked: How do you determine which trajectories to follow? Since you start from a pre-determined intermediate, what if your initial transition state is inaccurate? Is it possible to seed the system with specific information, *e.g.* vibrational normal modes, to help “steer” the algorithm?

40 **Samuel Jobbins** replied: Thank you for your intriguing questions. The trajectories utilised in the *metashooting* component of the work are extracted from the prior transition path sampling scheme, which converged upon the most likely subset of reactive trajectories linking two basins of interest after more than two hundred iterations. For more information on the path sampling procedure and how it converges upon the most plausible subset of the transition path ensemble, I’d recommend reading the papers which illustrate the method in detail.^{1–3}

45 In our work, we generated an initial trajectory using a geometrical–topological technique involving the transformation of periodic nodal surfaces, as used in previous work by our group.^{4,5} Intermediates could then be generated by interpolation, and a structure which linked the two basins (by propagation with MD forwards and backwards in time) was selected to be the initial intermediate. One of the advantages of shooting-off from a generated intermediate in this way is that

50

1 it does not matter at all whether or not the initial transition state is a plausible
starting structure – the starting trajectory need only link the two basins of interest.
In fact, it is highly likely that none of the intermediate states in our initial
5 trajectory have any physical relevance at all. The TPS algorithm will gradually steer
the system away from this initial unfavourable regime towards a more favourable
one. Thus, the initial regime should not matter – however, generating an ener-
getically reasonable first trajectory certainly decreases the number of TPS itera-
tions required before initial trajectory decoherence, and minimises the
10 computing expenditure required to move towards more relevant regions of
trajectory space.

Another advantage of this geometrical–topological approach is that, if desired,
certain characteristics can be hard-coded into the initial trajectory. The non-
linear mapping from the two limiting configurations proceeds according to
a set of particular deformation modes that are defined within the model. As
15 a result, specific features may be deliberately encoded (or avoided!) in the initial
pathway to greatly reduce the number of path sampling iterations required.
Additionally, a direct appreciation of the favourability of a particular model can be
ascertained by monitoring the conservation or disappearance of initial transition
20 motifs whilst the path sampling procedure is being performed.

- 1 C. Dellago, P. G. Bolhuis, F. S. Csajka and D. Chandler, *J. Chem. Phys.*, 1998, **108**, 1964–1977.
- 2 P. G. Bolhuis, D. Chandler, C. Dellago and P. L. Geissler, *Annu. Rev. Phys. Chem.*, 2002, **53**, 291–318.
- 3 C. Dellago, P. G. Bolhuis and P. L. Geissler, *Advances in Chemical Physics*, ed. I. Prigogine and S. A. Rice, John Wiley and Sons, 2002, pp. 1–78.
- 4 S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, **78**, 125204.
- 5 H. G. von Schnering and R. Nesper, *Z. Phys. B: Condens. Matter*, 1991, **83**, 407–412.

(239:[239]239) **Marcus Neumann** said: You mentioned that it’s difficult to pick
30 the order parameter, but is that also true if the start point and end point of
a transformation are known? What if the start point and end point are predicted
structures in the crystal energy landscape of a flexible organic molecule? Are there
any general rules for the construction of the order parameter?

35 **Samuel Jobbins** answered: Thanks for your questions. Selecting the collective
variable(s)/order parameter(s) is often the most difficult part of the job! There are
a number of general rules for constructing suitable collective variable(s):

1) The collective variable(s) must distinguish between the initial and final
40 configurations of interest, and (if appropriate) all relevant intermediate and
transition state regions, meaning no overlap between regions of importance;

2) The collective variable(s) must be able to describe all of the events of
importance in a given transformation, particularly those that are “slow”, and
tolerate fluctuations in thermal energy;

3) The number of collective variables should not be too large – otherwise the
45 calculation will be prohibitively expensive.

It is immediately apparent, however, that points 2) and 3) can be quite
mutually exclusive, as characterising all the necessary reaction coordinates to
describe a particular system can require quite a number of collective variables! In
50 addition, omitting a relevant collective variable can lead to basin over-filling or
failure to sample relevant regions of configuration space. (Indeed, this is why we

1 have included the 3rd coordination sphere in the work as well as the 1st, as
biasing only the 1st coordination sphere proved too coarse to distinguish between
competing intermediates and produced an incorrect energy scheme.^{1,2}) In my
5 opinion, the best approach is to characterise the system using as few collective
variables as possible, but by cleverly designing them such that they are truly
“collective” and that each order parameter encapsulates as much information
about the system and the transformation of interest as possible.

10 Knowing the start and end points of a simulation can obviously help to intu-
itively deduce a relevant set of collective variables. Sometimes it is quite evident –
for example, when simulating a chemical reaction, a certain bond length might be
the only variable of interest. However, in more complex systems with many
degrees of freedom, ascertaining a fundamental set of collective variables can be
a very non-trivial task. For example, in the case of flexible organic molecules,
15 a reasonable start would be to address which particular bonds, angles, torsions,
etc. play a vital role in the transformation under scrutiny. Some combination of
these important reaction coordinates might then prove sufficient to correctly
generate a free energy profile using metadynamics or the *metashooting* procedure.

20 One final point – in the scheme described in the paper, we used TPS initiated
from a model first trajectory. As such, knowing the start and end points of the
simulation are mandatory if one wishes to utilise transition path sampling and
the *metashooting* technique in its current formulation. But, as I've said, whether or
not this helps to determine the collective variables depends highly on the nature
of the system and the event under scrutiny.

25 1 A. Laio and M. Parrinello, *Proc. Natl. Acad. Sci. USA*, 2002, **99**, 12562–12566.

2 A. Laio and F. L. Gervasio, *Rep. Prog. Phys.*, 2008, **71**, 126601.

(240:[240]240) **Julian Helfferich** remarked: We have so far discussed the
30 collective variables, but I would like to address the methods. How far does your
metashooting procedure depend on the methods you have chosen, metadynamics
and the shooter method? Could you exchange them for other, potentially cheaper,
biasing and transition path methods?

35 **Samuel Jobbins** responded: Thank you for your question. The *metashooting*
procedure is by its very nature dependent on its two component techniques –
metadynamics and transition path sampling. The TPS steps in the *metashooting*
procedure control the variation in the collective variable, ensuring that it remains
within the trajectory space corresponding to the reactive transition path
40 ensemble. The metadynamics component deposits the bias within only this
relevant region, allowing for the underlying energy surface corresponding to the
transition to be explored efficiently and in precise detail. It is conceivable that the
two core methods could be “switched out” for other biasing/transition path
methods. However, we have illustrated that the union of TPS and metadynamics
45 currently implemented can produce exquisite and accurate detail, particularly of
the intermediate and transition state regions. Whether or not changing the
methods for others would have an effect on the accuracy or the expense of the
work, or whether unifying other techniques in this manner would be as robust or
effective, remain open questions. For myself, rather than changing the methods
50 utilised, I would advocate tuning and optimising the parameters involved in the

1 two techniques of the procedure, in order to maximise the efficacy and speed of
the *metashooting* analysis.

5 (241:[241]241) **Pablo Piaggi** said: I would like to comment on the performance
of metadynamics. First of all, there is a common misconception that the meta-
dynamics algorithm becomes slower as the simulation progresses. This is only
true in the most rudimentary implementation, in which an increasing number of
10 Gaussians have to be summed in order to calculate the bias potential. In modern
implementations, a grid is used to construct the bias potential and therefore there
is no need to sum all the Gaussians.¹ As a consequence, the cost of the algorithm
is constant in time. Furthermore, other methods, such as adaptive biasing force,
are also based on collective coordinates (CVs) and typically the calculation of the
CVs is the bottleneck of these methods.

15 ¹ https://plumed.github.io/doc-v2.4/user-doc/html/_metadyn.html

Samuel Jobbins replied: I wholly concur with this contribution. Thank you for
bringing it to attention!

20 (242:[242]242) **Pablo Piaggi** remarked: It has been shown¹ that in finite size
systems the barriers can be different to those in an infinite system. In the case
under consideration the transformation will probably proceed by nucleation and
growth, and I suspect the size of the simulation box is smaller than the critical
25 cluster. Did you assess whether the size of the system affects the results?

¹ M. Salvalaglio, C. Perego, F. Giberti, M. Mazzotti and M. Parrinello, Molecular-dynamics
simulations of urea nucleation from aqueous solution, *Proc. Natl. Acad. Sci. USA*, 2015,
112, E6–E14.

30 **Samuel Jobbins** responded: Thanks for your question. We have not directly
tested whether or not the size of the system would affect the results – however, we
strongly believe that it would, as it is likely that the precise nature of the motifs
seen in the transition path sampling runs is highly dependent on the simulation
system size. Addressing this would be a useful validation of the method, and
35 indeed would help to determine whether or not the system can be suitably scaled-
down and studied by *ab initio* methods. However, based on previous work,^{1,2} we
believe that the system size utilised produced representative motifs and
nucleation/growth events, whilst keeping the number of atoms in the system
tractable for efficient MD/metadynamics simulations.

¹ S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, 78, 125204.

² D. Zahn, Y. Grin and S. Leoni, *Phys. Rev. B.*, 2005, 72, 064110.

40 (243:[243]243) **Sarah Price** enquired: It is really spectacular that you have
identified intermediate basins and transition states in this solid state trans-
formation of ZnO. Your calculations were done with the simple exp-6 interatomic
potentials that Robin Grimes derived in 1993, and were later validated for ZnO
in 2007 in your group, but this validation is unlikely to have included these local
45 basins and transition state regions of the potential energy surface. Please can you
comment on the extent to which your results could be an artefact of the potentials
50 used?

1 **Samuel Jobbins** answered: Thank you for your question and for your high
praise about the work! The structures represented by the extrema on the free
energy surface that are described in this work correspond very closely to the
5 previously reported structures. Notably, the five-coordinated tetragonal and
hexagonal forms of ZnO have been discussed at great length in the literature.
Indeed, there still remains considerable debate as to the roles of these two
intermediates – for example, one *ab initio* study suggested that the tetragonal
intermediate was vital to the WZ-RS transformation in ZnO,¹ however an experi-
10 mental study utilising high resolution angular dispersive X-ray diffraction
appeared to indicate that the hexagonal pathway was more favourable for zinc
oxide transformations.²

Subsequent work has shown that the two intermediates are in direct competi-
15 tion with one another, and that a number of external factors are relevant, such as
pressure, temperature and the arrangement of local coordination motifs.³ In
addition, the work of Zagorac *et al.* found a number of the metastable ZnO phases
using *ab initio* techniques, some of which correlate directly with the configura-
tions observed in this work.⁴ Finally, in the group's previous work, the existence
and energy rankings of intermediates found using this force field were validated
20 using density functional theory calculations.⁵

Therefore, all of these works, both theoretical and experimental, report the
same (or very similar) metastable configurations as those presented in this paper.
As a result, I believe I can say with some certainty that the chances of the inter-
25 mediate basins having little physical significance is very low – however, as always,
further study (perhaps using a different potential model or a higher level of
theory) would be a very suitable future endeavour to ensure this!

1 A. M. Saitta and F. Decrempe, *Phys. Rev. B.*, 2004, **70**, 35214.

2 H. Liu, Y. Ding, M. Somayazulu, J. Qian, J. Shu, D. Häusermann and H. Mao, *Phys. Rev. B.*,
30 2005, **71**, 212103.

3 J. Cai and N. Chen, *J. Phys.: Condens. Matter*, 2007, **19**, 266207.

4 D. Zagorac, J. C. Schön, J. Zagorac and M. Jansen, *Phys. Rev. B.*, 2014, **89**, 075201.

5 S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, **78**, 125204.

(245:[245]245) **David McKay** queried: The speaker responded to a previous
35 question on the computational expense of metadynamics by saying that particu-
lar intermediate states are targeted to avoid spending time in unwanted minima.
He also remarked that regarding accuracy, to verify these results he would like to
be able to repeat the process using the DFT potential in metadynamics and
transition path sampling. Rather than repeating the whole process with DFT, is
40 there any scope for only using DFT as a correction to key structures along the
potential energy surface?

Samuel Jobbins replied: Many thanks for your interesting question. It may be
45 conceivable to try to treat the entire transition pathway (including the key struc-
tures) using density functional theory on top of the existing results. In particular,
a few iterations of the *metashooting* procedure could be carried out using density
functional theory, in order to see if there is significant deviation from the obtained
results and how the energetics of the new trajectories compare with older ones.

50 However, both the transformation mechanism (as deduced by transition path
sampling) and the free energy surface (produced by *metashooting*) have been

1 ascertained by describing the atomic interactions using a classical Buckingham-
style empirical pair potential.¹ One would hope that the scheme and (in partic-
ular) the intermediate regions produced by the potential would correlate well with
5 any results that would be obtained using a higher level of theory. Previous work by
our group has shown that the intermediates generated by the force field can be
stabilised using density functional theory and have the correct energy rankings.²
However, to be absolutely sure about this work, the entire process could be
repeated again with a different potential model or higher level of theory.

10 1 D. J. Binks and R. W. Grimes, *J. Am. Ceram. Soc.*, 1993, **76**, 2370–2372.

2 S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, **78**, 125204.

(246:[246]246) **David McKay** asked: Another consideration when going to more
accurate methods is system size, which in this case is large for DFT. Does the
15 study at force-field level provide any pointers as to how the system size could
be reduced for DFT calculations, while retaining a reasonable model system?

Samuel Jobbins responded: It is of course very true that the mechanism
deduced by transition path sampling is dependent on the size of the system. The
20 system size of 1200 Zn–O pairs was chosen as this is small enough for compu-
tational tractability but large enough for critical nucleation and growth events to
be visualised.^{1,2} To scale down for a density functional theory-type study, it is
conceivable that one could ascertain the size of these critical nuclei and the
number of atoms required for their formation, and construct a new model system
25 with a sufficient number of atoms to produce such features (with some additional
neighbouring atomic sites, so that an interface is present when considering the
periodic boundary conditions).

However, one must be very careful when scaling down the system. Making the
system too small can completely suppress the formation of key intermediates,
30 and the system may get “locked-in” to a regime of unrealistic trajectories, both in
terms of the details which emerge and the time scales over which they occur. I
would not be surprised if 1200 Zn–O pairs actually approached the minimum size
required to generate such meaningful events, however it would be interesting to
experiment with this to properly determine the minimum system size that could
35 be studied with density functional theory.

1 S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, **78**, 125204.

2 D. Zahn, Y. Grin and S. Leoni, *Phys. Rev. B.*, 2005, **72**, 064110.

(247:[247]247) **Christian Schön** said: We have seen similar intermediates (*e.g.*
the 5-5 structure, the ionic analogue of the hexagonal BN structure) on the energy
40 landscapes of related systems,^{1–3} which were also stable minima when locally
optimized on the *ab initio* energy landscape. Thus, I would believe they also exist
in your system. On another issue, I would hesitate to make the system smaller –
you might be in danger of locking the system into a limited number of (perhaps
unrealistic) pathways between the regions you want to connect. If you recall the
water-freezing simulations by Ohmine and co-workers *ca.* 15 years ago,⁴ they
45 found that even the large “crystalline” nuclei that had formed inside the liquid
phase after about 100 ns vanished again (I think they needed about 200 ns before
the whole system crystallized). So, a smaller system size might lead to

1 unrealistically fast freezing rates. Do you ever see paths where seeds of the new
phase grow and then vanish again?

5 You also mentioned that you could measure activation energies – can you also
deduce activation entropies, or more generally measure the generalized barriers⁵
via the probability flows on the landscape of the system between metastable
configurations?^{6,7} Perhaps via effective transition rates?

1 J. C. Schön and M. Jansen, *Comp. Mater. Sci.*, 1995, **4**, 43–58.

2 J. C. Schön, *Z. Anorg. Allg. Chem.*, 2004, **630**, 2354–2366.

3 D. Zagorac, J. C. Schön and M. Jansen, *J. Phys. Chem. C*, 2012, **116**, 16726–16739.

4 M. Matsumoto, S. Saito and I. Ohmine, *Nature*, 2002, **416**, 409–413.

5 J. C. Schön, M. A. C. Wevers and M. Jansen, *J. Phys. Cond. Matt.*, 2003, **15**, 5479–5486.

6 M. A. C. Wevers, J. C. Schön and M. Jansen, *J. Phys. Cond. Matt.*, 1999, **11**, 6487–6499.

7 S. Neelamraju, J. C. Schön, K. Doll and M Jansen, *Phys. Chem. Chem. Phys.*, 2012, **14**, 1223–
1234.

15 **Samuel Jobbins** answered: Thanks for your correspondence and queries. I
appreciate the vote of confidence with respect to the existence of the intermedi-
ates and transition states found in the work! I am very confident that they are
meaningful metastable minima, as they have been seen in a great deal of previous
20 work, including your own. I also am inclined to agree with your comment
regarding system size – it would be interesting to see how small one could go
whilst still observing plausible mechanistic details, however my intuition tells me
that this limit would not be much smaller than the system size that we have used
in this work! During the initial transition path sampling scheme, there are
25 multiple examples of “failed” trajectories, in which a transformation begins, but
then “fails” and reverts back to the existing structure. Such failed trajectories were
often seen in the very early stages of transformation, particularly from rocksalt to
zincblende, around the time of the formation of the cubic seed. Another frequent
example of trajectory “failure” was when the transition became “stuck” in the
intermediate 5-coordinate basin.

30 Pairing TPS and metadynamics allows us to globally map the free energy. In
transition path sampling, the system still spends the most time around the main
basins of attraction, while *metashooting* can weight even elusive intermediates
accurately. TPS is a method that allows the generation of reactive trajectories
35 without bias, as single trajectories follow their natural dynamics without external
perturbation. Reaction rates are thus accessible by combining TPS with methods
like Umbrella Sampling. A more precise outcome is provided by Transition
Interface Sampling (TIS).¹ Additionally, the separation of enthalpic and entropic
contributions can be addressed in metadynamics by introducing an instantane-
40 ous measure of entropy, based on pair correlation functions. All of these
measures require a precise knowledge of the free energy, including possible
intermediates, which is exactly what is provided by our *metashooting*
methodology.

45 1 T. S. van Erp, D. Moroni and P. G. Bolhuis, *J. Chem. Phys.*, 2003, **118**, 7762–7774.

(248:[248]248) **Christian Schön** asked: Regarding your shooting algorithm:
since there are many competing basins in your system, how can you sit “in the
50 middle” and shoot, and still reach the two basins between which you try to
establish a transformation route? Where is the “middle”, exactly?

1 **Samuel Jobbins** responded: The shooter algorithm here corresponds directly to the original algorithm reported in the transition path sampling literature. More information about the transition path sampling method can be found in ref. 1–3.

5 When referring to the “middle”, we simply mean a dynamical mid-point of the current trajectory that links the two basins of interest. In the beginning of the transition path sampling work, the mid-point is an interpolated intermediate from the geometric trajectory that successfully links the two basins of attraction. Subsequent mid-points are dynamical intermediates from the latest reactive trajectory. In the *metashooting* component, the transformation route has already been established by transition path sampling, and so shooting from the mid-point still reaches the two basins of interest along the converged subset of trajectories. By the time *metashooting* is carried out, the transition path ensemble has been sampled and the most likely subset of trajectories has been found – it is these trajectories which are biased and evaluated by the *metashooting* procedure.

10 1 C. Dellago, P. G. Bolhuis, F. S. Csajka and D. Chandler, *J. Chem. Phys.*, 1998, **108**, 1964–1977.

2 P. G. Bolhuis, D. Chandler, C. Dellago and P. L. Geissler, *Annu. Rev. Phys. Chem.*, 2002, **53**, 291–318.

20 3 C. Dellago, P. G. Bolhuis and P. L. Geissler, *Advances in Chemical Physics*, ed. I. Prigogine and S. A. Rice, John Wiley and Sons, 2002, pp. 1–78.

(249:[249]249) **Christian Schön** enquired: Does your procedure measure the probability flows directly? Also, we should not confuse the local “entropy”/“free energy” measured as a function of the order parameter during the metadynamics phase of the simulations with the “entropic” part of the generalized barrier that is related to the probability flows and thus contributes to the rate constants of the processes being analyzed. After all, a local free energy is only defined on observational time scales that are larger than the equilibration time and shorter than the escape time from the region, so you might be able to measure local densities of states – a static quantity – but it might not be permissible to compute the free energy, which is a time dependent quantity!

35 **Samuel Jobbins** replied: I’m not sure I fully agree with this analysis. The Laio *et al.* paper on metadynamics describes in considerable detail how, at the infinite time limit, the deposited bias is approximately equal to the negative of the free energy, plus an irrelevant additive constant.¹ There are a number of ways that the error in this can be estimated, and also a number of methods which can be implemented to reduce this error. Utilising the well-tempered prescription of metadynamics also helps to overcome any potential issues here associated with over-filling (and hence over-estimating the free energy barriers). However – to reiterate – Laio *et al.* clearly show that the free energy (an equilibrium property) can be very well estimated using non-equilibrium dynamics in metadynamics. This is indeed one of the great selling points of the method, and as such both enthalpic and entropic contributions should be accounted for in the present scheme.

45 More generally, one can consider the situation in this way: large free energy barriers represent a major limitation for the exploration of reactive events – even more so if *ab initio* methods are used. In “plain” molecular dynamics, the escape time in the presence of energy barriers much larger than $k_{\text{B}}T$ is, in principle,

1 infinite. Metadynamics implements a coarse-grained representation of the true
high-dimensional potential energy surface of interest, which will contain a large
number of low-lying saddle points. In the lower dimensional coordinate space of
5 the collective variables, the free energy surface is smooth. In this regime, the
basin escape time is finite, allowing for a global mapping of the free energy, which
converges within a finite time.

1 A. Laio and F. L. Gervasio, *Rep. Prog. Phys.*, 2008, **71**, 126601.

10 (250:[250]250) **John Mitchell** asked: Systems like chemical reactions, with few
degrees of freedom, have tightly defined mechanisms corresponding to a specific
trajectory or a narrow range of trajectories across the potential energy surface.
Other energy landscapes, like those for protein folding, with very many degrees of
15 freedom, have much looser families of trajectories connecting regions. Would you
classify the phase transition you are looking at as a single mechanism, or a broad
family of region-connecting trajectories? Do you think your methodology is better
suited for tightly defined mechanisms or for broader families of trajectories?

20 **Samuel Jobbins** answered: Thanks for your intriguing question. The under-
lying energy landscape corresponding to a condensed matter phase transition can
be very coarse, owing to the many degrees of freedom in the system. This is of
course dependent on the number of atoms in the system, but for 1200 Zn–O pairs
the complexity of the (complete) energy landscape is probably intermediate
25 between the two examples you have cited here! In this particular transition, there
are a great number of transition pathways possible, each of which has a particular
probability (as determined by the energy of the transformation). The initial
transition path sampling procedure samples reactive pathways in trajectory space
and ultimately converges upon the most likely subset of reactive trajectories
30 linking the two basins (prior to the *metashooting* technique actually being uti-
lised). For more information on transition path sampling, I'd recommend taking
a look at ref. 1–3.

These lowest energy reactive trajectories correspond to the transition mecha-
nisms reported in the paper. The *metashooting* procedure is then only applied to
35 this lowest energy subset of reactive trajectories in the coarse-grained, lower
dimensional space of the collective variables, which is why the final free energy
profile looks relatively smooth and well defined. I see no reason why the meth-
odology should not work on more simple or complex cases. Systems with fewer
degrees of freedom would be easier to characterise and define in terms of reaction
40 coordinates, and would likely converge more quickly than their larger counter-
parts. More complicated systems may be more expensive to compute, however if
an appropriate order parameter is chosen, transition path sampling should still
be able to find the corresponding favourable reactive subset in trajectory space.
These trajectories can then be biased using *metashooting* to generate the energy
45 landscape corresponding to the “path of least resistance” for a given system.

1 C. Dellago, P. G. Bolhuis, F. S. Csajka and D. Chandler, *J. Chem. Phys.*, 1998, **108**, 1964–
1977.

2 P. G. Bolhuis, D. Chandler, C. Dellago and P. L. Geissler, *Annu. Rev. Phys. Chem.*, 2002, **53**,
291–318.

3 C. Dellago, P. G. Bolhuis and P. L. Geissler, *Advances in Chemical Physics*, ed. I. Prigogine
50 and S. A. Rice, John Wiley and Sons, 2002, pp. 1–78.

1 (251:[251]251) **Marcus Neumann** said: In a periodic supercell, many paths leading from a highly symmetric start point to a highly symmetric end point are related by symmetry. Does your method somehow exploit these energy relationships?

5 **Samuel Jobbins** replied: The initial trajectory is generated using a geometrical-topological approach, in which periodic nodal surfaces are wrapped around the limiting structures and transformed according to a pre-defined set of deformation modes. In this respect, symmetry can be incorporated into the initial trajectory. Such a scheme has been used in previous work by our group.^{1,2} However, in its current implementation, the actual *metashooting* procedure does not take symmetry into account at all when sampling the trajectory space or applying the metadynamics scheme. However, this could certainly be worth looking into in the future, as it may well help to increase the efficiency of the technique.

10 1 S. E. Boulfelfel and S. Leoni, *Phys. Rev. B.*, 2008, **78**, 125204.

2 H. G. von Schnering and R. Nesper, *Z. Phys. B: Condens. Matter*, 1991, **83**, 407–412.

15 (819:[252]252) **Scott Woodley** communicated: What is the definition of your energy? You state in your paper that you use CP2K and mention the use of Buckingham potentials with parameters derived from Grimes *et al.*, but is this the Shell Model or rigid ions? If the latter, how would you expect your results to change if you added oxygen polarisation into your model?

25 **Samuel Jobbins** communicated in reply: In the molecular dynamics and transition path sampling runs, the total energy (as computed by CP2K) was used as the energy function. In the *metashooting*, the free energy is reconstructed as the negative of the deposited bias potential, as explained in the original paper on metadynamics. We indeed use the Buckingham potential of Binks and Grimes,¹ however in this work the oxygen polarisation term was not included. Initial calculations showed that just using the core charges and van der Waals interactions was sufficient to describe the relevant bulk phases of ZnO, with reasonable values for the geometric parameters and transition pressures. I personally suspect that the oxygen shells would actually make little difference to the transition mechanism – however, there may be some subtle effects, and there would be considerable differences if one, for example, wanted to calculate phonon dispersion curves. Perhaps repeating the procedure with the shells (or with another potential model) might be a good future endeavour to help validate the methodology.

30 1 D. J. Binks and R. W. Grimes, *J. Am. Ceram. Soc.*, 1993, **76**, 2370–2372.

35 (824:[253]253) **Noa Marom** communicated: You showed an example of solid state transformation from one crystal structure to another. Can *metashooting* also be used for amorphous to crystalline transformations?

40 **Samuel Jobbins** communicated in response: Thanks for your question! In principle, any system that can be described with a suitable set of collective variables/order parameters for the metadynamics and TPS stages of *metashooting* can be studied using our technique. In fact, we are currently in the process of

1 studying a phase transition between two configurations of a metal–organic
framework, which is believed to proceed *via* an amorphous intermediate. Once the
most likely subset of trajectories linking the two configurations is found, we
5 intend to apply the *metashooting* method to quantify the underlying free energy
surface. Of course, as usual, the difficult part of this is determining which reaction
coordinates are relevant to the transition! My advice for treating an amorphous
system would be to attempt to exploit any short-range order present in the
system, and to use mean coordination sequences or Steinhardt parameters to
10 attempt to globally characterise the system.

(825:[254]254) **Noa Marom** communicated: Do you envision using machine
learning to identify the best collective variables for a system?

15 **Samuel Jobbins** communicated in reply: What a fascinating idea! In principle,
the idea of using a machine learning algorithm to substantially reduce the
dimensionality of a problem to a handful of tractable collective variables is a very
enticing prospect indeed (and arguably is a textbook example of the merits of
machine learning). In practice, however, there are often so many possible variables
20 to utilise in each system that it is quite hard to envisage a machine learning
algorithm being able to successfully capture the often subtle chemical/physical
nuances in every possible system. Often, a great deal of chemical intuition (and
sometimes luck!) is required to ensure that only appropriate variables are chosen,
and that all of the important variables are considered. I, however, am only just
25 beginning to enter the machine learning world and would love to know if this
could be done. Do you have any suggestions about how this could be done in
practice? There are so many different systems (and hence collective variables) to
study – how would one train such an algorithm to ensure that it could make useful
suggestions for such a disparate selection of systems?

30 (300:[300]300) **Marcus Neumann** opened the discussion of the paper by Alexandre
Tkatchenko:† Fig. 9 and Fig. 10 seem to suggest that thermal expansion affects
the lattice free energy only weakly if phonons are treated in the harmonic
approximation, and much more strongly when the anharmonicity of phonon
35 modes is taken into account. Is this interpretation correct?

Johannes Hoja responded: This seems to be the case for this particular system.
However, for a general statement further investigations involving a variety of
40 systems would be necessary.

(302:[301]301) **John Mitchell** enquired: Thinking about the things you added to
your model, I'm not surprised that you added mode-by-mode analysis of the
vibrations. I am looking for an accuracy of 3 kJ mol⁻¹ in my applications, and
45 would also expect to require that. However, I am surprised by how much difference
the many-body dispersion makes, compared to using just pairwise dispersion.
This might be disturbing, since omission of many-body effects seems to lead
to significant increases in error. Is this widely true across drug-like molecules? Are

50 † Alexandre Tkatchenko's paper was presented by Johannes Hoja, *University of Luxembourg*.

1 there other non-obvious sources of error that we need to be aware of that are
currently missing from most models?

5 **Johannes Hoja** replied: For the five systems discussed in our paper, the mean
absolute deviation between the PBE+TS and PBE+MBD energies varies between
1.8 and 3.2 kJ mol⁻¹. Therefore, we observe significant effects for all systems but
their magnitude seems to depend on the molecular size and flexibility. Figure 2 in
10 our paper shows a correlation plot between PBE+TS and PBE+MBD. Given the
spread of the data points, even fitting the best possible pairwise model to the
MBD data would not provide sufficient correlation. Note that the differences
between PBE+TS and PBE+MBD originate from many-body dispersion interac-
tions and also from the included dielectric screening effects. Therefore,
15 Figure 3(b) illustrates purely the effect of many-body interactions. It can be seen
that contributions of up to about 5-atom interactions are necessary to converge
the relative stabilities. A discussion about many-body dispersion effects for
molecular dimers, supramolecular systems and molecular crystals can be found
in ref. 1 and 2. Non-obvious sources of error for static energy calculations could be
20 revealed by benchmarks on larger and more flexible crystals using Quantum
Monte Carlo (QMC).

1 A. M. Reilly and A. Tkatchenko, *Chem. Sci.*, 2015, 6, 3289–3301.

2 A. Ambrosetti, D. Alfè, R. A. DiStasio Jr. and A. Tkatchenko, *J. Phys. Chem. Lett.*, 2014, 5,
849–855.

25 (303:[302]302) **Graeme Day** asked: I have a question about the validation of
crystal structure prediction methods: when evaluating methods used to rank
structures, how do we know when we have the correct ranking? Target systems for
benchmarking should be chosen carefully and should be experimentally well
characterised.

30 Are the blind test molecules the best systems to revisit when assessing new
methods? It does not seem to me that the blind test molecules are selected in
a way that makes them good benchmarks. Apart from a few exceptions, such as
the polymorphic molecule XXIII, most of the blind test molecules have not been
35 experimentally studied very much at all. They are included in the blind tests
simply because their crystal structures have not been published. So, once they are
no longer blind targets, I don't think that they are valuable for validation. Should
the community agree on some better sets of molecules to use for testing?

40 **Johannes Hoja** answered: I agree that the blind test systems are not ideal
benchmarks (with the exception of system XXIII). It would be better to create a set
of experimentally well-studied systems, for which extensive polymorph screening
has been done and for which reliable experimental relative stabilities are available
(maybe at different thermodynamic conditions). Ideally, this set should cover
45 a variety of different types of molecular crystals, *i.e.* crystals with different
molecular size and flexibility, salts, co-crystals, solvates, and also disordered
systems.

50 (306:[303]303) **Susan Reutzl-Edens** said: As a follow-up to Graeme's general
question about the use of blind test molecules for benchmarking purposes, the

1 evaluation of systems from the literature that are well characterized experimen-
tally is likely to produce more meaningful results than for systems chosen simply
for being blind test targets – unless, of course, experimental validation is forth-
coming. In this work, what experimental validation data is available to assess the
5 various energy models that were used for the CCDC blind test molecules?

Johannes Hoja responded: The available experimental data for the systems of
the latest blind test¹ consists of the measured crystal structures (5 polymorphs for
system XXIII and one form for the other systems). In addition, slurring experi-
ments indicate that form A of system XXIII is the most stable polymorph at 257 K,
10 while form D is the most stable polymorph at 293 K. Furthermore, all 5 poly-
morphs of XXIII co-exist under ambient conditions. Therefore, we can assume
that these 5 polymorphs must have very similar stabilities.

15 1 A. M. Reilly *et al.*, *Acta Cryst. B*, 2016, 72, 439–459.

(304:[304]304) **German Sastre** enquired: My question concerns large molecules
(*e.g.* molecule XXVI in your Fig. 1) containing a large number of dihedral angles,
where large variations imply very similar energies. What is the balance between
20 intramolecular dispersion contributions and intermolecular dispersion contri-
butions? There are not many comments in your paper regarding the effect of
geometry (in particular dihedral angles) on energy. What degree of accuracy in the
dispersion is necessary in order to obtain correct dihedrals?

25 **Johannes Hoja** replied: In our methods, we do not distinguish between intra-
and intermolecular dispersion interactions. We evaluated the quality of our
calculated structures by comparing the cell parameters and the root-mean-square
deviation to those of the experimentally measured structures. In these metrics,
30 PBE+TS, PBE+MBD and PBE0+MBD yield structures of quite similar quality (see
Table 2). All the optimized structures are available in the Supporting Information.
We also explored what impact the structure optimization method has on the
resulting PBE0+MBD energies of the five XXIII polymorphs (see Figure 5). It can be
seen that the optimization method used has only a small impact on the
35 PBE0+MBD relative stabilities; the largest observed change in relative energy
amounts to 0.8 kJ mol⁻¹.

The similarity of the structures is illustrated in Fig. 1 for system XXVI. Fig. 1
shows an overlay of the two molecules within the optimized unit cells obtained
with PBE+TS (blue), PBE+MBD (red), and PBE0+MBD (green). To put this into
40 perspective for dihedral angles, we compared the dihedral angles defined by
atoms 1–4 in the plot. PBE+TS yields a dihedral angle of 51.3 degrees, while the
PBE+MBD and PBE0+MBD dihedral angles amount to 52.2 degrees and 51.4
degrees, respectively. For this dihedral angle all three methods agree within 1
degree.

45 (305:[305]305) **Rui Guo** remarked: I noticed that in the paper, the constructed
supercells are completely based on the unit cell parameters. I'd like to add that
this practice largely mirrors that routinely used for metals or inorganic materials
where the interacting species in the unit cell, metals or ions, have isotropic
50 interactions. For organic molecular crystals, where intermolecular interactions or

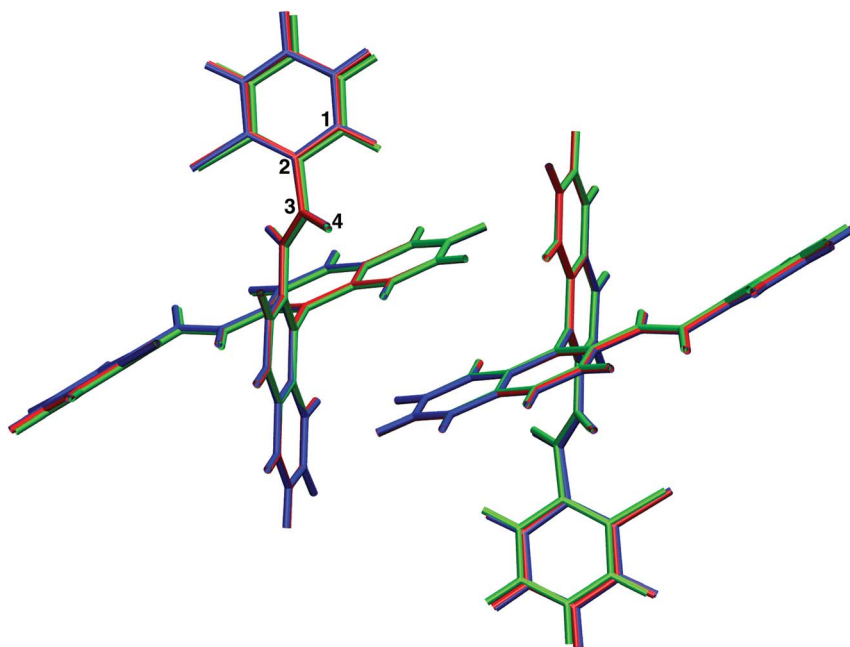


Fig. 1 System XXVI: overlay of the two molecules within the optimized unit cells obtained with PBE+TS (blue), PBE+MBD (red), and PBE0+MBD (green).

even the shapes of the molecules can be very anisotropic, a more informed approach, focusing more on molecular packing and intermolecular interactions, may lead to better computing efficiency. As an example, succinic acid form β has a molecular packing with hydrogen-bonded chains running along the $[10\bar{1}]$ direction, and weak $\text{CH}\cdots\text{O}$ contacts between the chains. I recently calculated its phonon dispersion curves, and found that due to the specific molecular packing, extending the unit cell along the c axis for a supercell converges the integrated Helmholtz free energy much faster than extending along the a or b axes. It can be rationalized that extending the c axis preserves the network of weak $\text{CH}\cdots\text{O}$ contacts in the supercell, while extending the other two axes would have no such effect. A paper on this subject is currently being prepared with Prof. Keith Refson.

Johannes Hoja answered: Utilizing a more informed approach for the generation of supercells is a great idea for reducing the computational cost. In our paper, we employed supercells with minimal lengths of 10 \AA in each direction. For a selected structure set we also evaluated the vibrational free energies using larger supercells with a minimal length of 14 \AA . Increasing the supercell size changed the relative stabilities on average by 0.3 kJ mol^{-1} , and the maximum observed change amounts to 0.9 kJ mol^{-1} . For the structure showing the largest energy change upon increasing the supercell size, we plotted the phonon dispersion curves in the Supporting Information for the unit cell and the two calculated supercells. It can be seen that supercells of appropriate size are crucial for the correct description of the acoustic modes.

1 (335:[306]306) **Luca Iuzzolino** asked: With your methodology for optimising and ranking crystal structures, how many crystal structures do you think you could tackle with a computational expense feasible for a practically useful CSP study?

5 **Johannes Hoja** replied: I believe that the lattice relaxation with PBE+TS and a subsequent PBE0+MBD energy calculation would be feasible for up to around 100 structures. Vibrational free energies within the harmonic approximation are in my opinion reasonable for tens of structures, while the quasi-harmonic and Morse free energies should be done for a few selected structures.

10 (336:[307]307) **Luca Iuzzolino** said: The methods you use to calculate the relative energy differences between polymorphs are very accurate but also very computationally expensive. In this study they were applied to a few crystal structures; do you think they would be widely applicable to CSP studies where a large number of putative crystal structures need to be considered? Otherwise you will have to trust the energy ranking produced at the search stage to limit the number of crystal structures that are optimised to a feasible number, and this may lead to a loss of important forms if they are not well-ranked.

15 (337:[308]308) **Johannes Hoja** answered: Our presented approach is intended for the final stage of a crystal structure prediction procedure, assuming an already limited structure set. Therefore, one would need to trust the preceding methods not to miss important forms. However, our method could also function as reference data for the creation of tailor-made force fields or machine-learning models that can be used at the search stage.

20 (337:[308]308) **Artem R. Oganov** remarked: Last week I saw John Perdew, who was excited about his new SCAN functional. The recipe is to combine it with the rVV10 van der Waals functional when one needs to describe van der Waals systems. What is better – SCAN+rVV10 or PBE(PBE0)+MBD? Or perhaps SCAN+MBD (which I haven't seen used yet)?

25 (337:[308]308) **Johannes Hoja** responded: The performance of several density-functional approximations (including PBE, PBE0, SCAN) when paired with the MBD, VV10, and D3 van der Waals (vdW) models are discussed in ref. 1. SCAN+vdW can provide accurate interaction energies when the damping function used is optimized for the studied system. However, the effective range of the SCAN functional is much more system dependent than that of PBE or PBE0. Therefore, the PBE+vdW and PBE0+vdW methods provide a more universal description since the same range-separation parameter can be used for a variety of systems. Note that in contrast to MBD, VV10 is a pairwise method and provides therefore no description of many-body dispersion interactions.

30 1 J. Hermann and A. Tkatchenko, *J. Chem. Theory Comput.*, 2018, **14**, 1361–1369.

35 (338:[309]309) **Artem R. Oganov** enquired: In your work, you used PBE (or PBE0) as exchange–correlation functional, supplemented with many-body dispersion. Other people recommend SCAN exchange–correlation functional,

1 supplemented with rVV10 functional for the description of van der Waals
bonding. Which scheme is better? SCAN seems to be better than PBE; is this your
5 impression too? What about the comparison between many-body dispersion and
rVV10 functional?

Johannes Hoja replied: A comparison between PBE and SCAN with different
van der Waals models (MBD, VV10, D3) can be found in ref. 1 (see the previous
question).

10 1 J. Hermann and A. Tkatchenko, *J. Chem. Theory Comput.*, 2018, **14**, 1361–1369.

(341:[310]310) **Gregory Beran** said: Your results seem to show that as you refine
the energies by increasing the sophistication of your computational models, the
energy gaps between structures often decrease. We have seen similar behaviors in
15 our own work. Pessimistically, this suggests that even though the field is
increasingly able to predict the energetics accurately, that does not necessarily
translate to an increased ability to rank/discriminate between structures. It also
ties back to Sally Price's comment in the introductory lecture about how the field
has transitioned away from the search for *the* unique crystal structure, whose
20 energetic stability would ideally be well-separated from the other candidate
structures/polymorphs, to a more nuanced understanding of how complicated
crystal energy landscapes can be.

Johannes Hoja answered: I agree that we will often be faced with complicated
25 crystal energy landscapes, where several structures are in a very narrow energy
window. Such cases could lead to the identification of new crystal forms or
highlight once again the necessity of also including kinetic effects. However,
accurate first-principles calculations are a prerequisite for the understanding of
30 such complicated energy landscapes.

(342:[311]311) **Virginia Burger** queried: You mentioned that someone is trying
to crystallize the low energy polymorph (structure N70). Did you learn anything
35 from your theoretical analysis that could guide the experimental search?

Johannes Hoja responded: Structure N70 has several similarities with the
experimentally obtained Form A and both structures differ mainly by the stacking
of the sheets. At the static lattice energy level structure N70 is about 1 kJ mol^{-1}
40 more stable than Form A and is additionally significantly stabilized by vibrational
free energies, *i.e.* temperature effects. Therefore, Form A could be dynamically
favored over structure N70. We believe that, for example, extremely low melting
beginning from Form A could potentially lead to the crystallization of structure
N70.

(343:[312]312) **Virginia Burger** remarked: Regarding benchmarking: XtalPi has
45 been testing our CSP work on axitinib, which has around five polymorph crystal
structures, many more polymorphs and lots of experimental data, and we have
found it to be a more useful benchmark case because of all the experimental data.
Finally, you mentioned that simulations could provide more accurate free energy
50 results. We have run such simulations for molecule XXIII from the blind test and

1 have found that the more stable experimental structures have the lowest free
energies at room temperature, which is exciting. We are putting together a paper
about this now.

5 **Johannes Hoja** replied: Indeed, molecular dynamics simulations would
provide a better treatment of anharmonic effects than our quasi-harmonic/Morse
free energies. However, the accuracy of such an approach will also highly depend
on the quality of the underlying energy evaluation method.

10 (805:[314]314) **Gerit Brandenburg** communicated: During the discussion of the
author's excellent contribution, the importance of many-body dispersion effects
was mentioned. I would like to clarify that the statements made crucially depend
on the definition of the "body", *i.e.* a dipole excitation *vs.* an effective atomic
excitation.

15 **Alexandre Tkatchenko** communicated in reply: Indeed, the absolute magni-
tude of the many-body dispersion energy will depend on at least two critical
aspects: (1) the definition of the fragment and its polarizability (*i.e.* infinitesimal
20 volume of electron density, localized orbital, or atomic density fragment), and (2)
the definition of the coupling potential between such fragments. However, the
point we make is rather independent of such considerations. We have demon-
strated that MBD (where atomic fragments are employed) provides a quantitative
description of the relative energies of molecular crystal polymorphs when
25 combined with non-empirical hybrid exchange–correlation functionals (such as
PBE0). Independently of which atom-pairwise model is used to describe vdW
dispersion interactions, the correlation between MBD and such effective pairwise
models leads to a spread that is larger than 4 kJ mol⁻¹. This is at least 4 times
larger than the desired accuracy of 1 kJ mol⁻¹. We have also demonstrated that
30 the convergence of the many-atom expansion within the MBD method is quali-
tatively different for various polymorphs. We expect these qualitative findings to
hold independently of the method employed to describe many-body dispersion
interactions.

35 (808:[315]315) **David McKay** communicated: Section 6 and Table 4 nicely
describe the computational costs of the methods involved in the study. PBE0-
MBD is the most successful method here, but is 17 times more expensive than
PBE-TS. Could this cost increase be elaborated on? I have previously shied away
40 from hybrid-DFT functionals in the solid state, as we tend to see these as
prohibitively expensive. I assume there is a cut-off distance for the Fock exchange
calculation – is this a parameter that must be converged, and is the cost kept low
here with a short distance?

45 **Johannes Hoja** communicated in response: Hybrid density functional
approximations like PBE0 are significantly more expensive than generalized
gradient approximations like PBE because of the necessity to calculate the Har-
tree–Fock exchange. A detailed description of the periodic Hartree–Fock exchange
implementation in FHI-aims utilizing numeric atom-centered basis functions is
50 available in ref. 1. In our calculations we did not use any special settings or cut-off
distances for the evaluation of the Hartree–Fock exchange. Note that the relative

1 timings provided in our paper are for a particular molecular crystal of average
size, which has 172 atoms in the unit cell. In general, the relative cost will depend
on the calculated system and also on the HPC infrastructure used.

5 1 S. V. Levchenko, X. Ren, J. Wieferink, R. Johanni, P. Rinke, V. Blum and M. Scheffler,
Comput. Phys. Commun., 2015, **192**, 60–69.

(817:[316]316) **Volker Deringer** communicated: Towards the end of your paper
you've taken the method to the limit of what can be done (in terms of computing
10 cost), and in the conclusions you suggest that machine-learning methods might
help with this in the future. There seem to be several possibilities indeed: one
could fit potentials to MBD-corrected input data, or “learn” only the MBD
correction, or possibly even thermal properties directly. Could you elaborate on
this a bit – what do you think are the most promising directions there?

15 **Alexandre Tkatchenko** communicated in reply: Indeed, currently the cost of
explicit PBE0+MBD calculations plus vibrational free energies is quite high.
However, valuable and reliable reference data can already be produced with this
methodology for 10–100 crystalline polymorphs of a given molecule. I see two
20 possible approaches that combine machine learning with PBE0+MBD:

(1) Directly learn the forces/Hessians for different polymorphs and reconstruct
a “molecule in a crystal” force field from a finite number of polymorphs.

(2) Learn the PBE0 energy (which should be rather local for closed-shell
25 molecules) and learn the MBD Hamiltonian parameters and compute the MBD
energy explicitly.

Machine learning ZPE and thermal properties should also be rather straight-
forward. We have demonstrated that for gas-phase molecules this can be done
with quantitative accuracy.¹ Applying such models to crystals requires some non-
trivial extension, but this should doable.

30 1 W. Pronobis, A. Tkatchenko and K.-R. Müller, *J. Chem. Theory Comput.*, 2018, **14**, 2991–
3003.

(821:[317]317) **Seiji Tsuzuki** communicated: You showed that the contribu-
35 tions of the many-body dispersion interactions and vibrational energies to the
lattice energies of crystals are not negligible. Do the contributions of many-body
dispersion and vibrational energies have a significant impact on the relative
stability of polymorphs, or are the contributions of these terms to the relative
stability not significant due to cancellation?

40 **Alexandre Tkatchenko** communicated in response: As our paper shows, both
the many-body dispersion and vibrational free energies are crucial for obtaining
the correct description of free energy differences between polymorphs. The many-
body energy decomposition shows that many-body effects vary significantly for
45 different polymorphs. In the case of vibrational free energies, the low-frequency
phonons depend heavily on the crystal structure and hence lead to substan-
tially different entropy contributions for different polymorphs.

(823:[318]318) **David Bowskill** communicated: This approach determines the
50 geometry of organic crystals using the PBE functional and then applies the MBD

1 correction, followed by a proportion of exact exchange using the PBE0 functional.
 By applying these corrections, the static crystal structure and associated energy no
 longer reside at local minima. Do you have any evidence of how much this will
 5 affect the predicted crystal energies? For example, would full geometry optimisation
 using the PBE0 functional with MBD correction produce noticeably
 different results? In addition, how much does this affect the harmonic approxi-
 mation, which assumes that the molecules are positioned at minima in the crystal
 energy landscape?

10 **Johannes Hoja** communicated in reply: In our paper we studied how the
 PBE0+MBD energies depend on the optimization method used (see Figure 5). It
 can be seen that the structure optimization method has only a small effect on the
 relative PBE0+MBD stabilities, with a maximum change of 0.8 kJ mol⁻¹ in the
 15 relative stabilities. The structures used for the vibrational free energy calculations
 in the harmonic approximation were always optimized with exactly the same
 method as is used for the harmonic approximation to ensure that we are in a local
 minimum.

20 (307:[319]319) **Marcus Neumann** opened the discussion of the paper by Jan
 Gerit Brandenburg: What is the root mean square deviation between the lattice
 energy differences calculated with DFTB3-D3 and higher level methods for the
 compounds that you have studied?

25 **Gerit Brandenburg** answered: The root mean square (rms) deviation was
 calculated between the energies of the crystal structures after DFTB3-D3 and the
 final optimisations. The distributed multipoles and intramolecular energy were
 calculated with an improved charge distribution (PBE0 6-31G(d,p)). The FIT
 repulsion–dispersion potential was calculated relative to the global minimum
 30 structure in E_{latt} after the final optimisations (see Table 4). The rms values were
 calculated for all the CSP-generated crystal structures that were found to be within
 50 kJ mol⁻¹ after the final optimisations, as well as for a more limited set of crystal
 structures that matched the most important putative polymorphs found in the
 original CSP studies (see the Electronic Supplementary Information); this set
 35 included all the experimentally known forms with $Z' = 1$. The results in Table 4
 confirm the conclusion of the paper that we cannot rely on DFTB3-D3 lattice
 energies.

40 **Table 4** Root mean square (rms) deviations calculated between the energies of crystal
 structures

Molecule	$\sim\text{rms}_{\Delta E_{\text{latt}}}$ for all crystal structures/kJ mol ⁻¹	$\sim\text{rms}_{\Delta E_{\text{latt}}}$ for crystal structures matching the most important PPMs/kJ mol ⁻¹
XXVI	21	13
GSK269984B	34	21
XX	15	5
XXIII	21	10
Mebendazole	15	7
Overall	21	13

1 Related to this is a comparison with periodic DFT-D methods for selected
crystal structures from the 6th crystal structure prediction blind test (POLY59
set¹). The absolute lattice energies (X23 set) mean unsigned errors of DFTB3-D3
5 are competitive to PBE-TS, but for relative lattice energies, periodic dispersion
corrected density functional (DFT-D) profits a lot from error compensation, which
does not hold for the tight-binding Hamiltonian.

1 Brandenburg *et al.*, *Acta Cryst. B*, 2016, 72, 502–513.

10 (308:[320]320) **Christian Schön** enquired: While looking like a nice compromise
between *ab initio* calculations and empirical potentials, there is one big
problem with DFTB: up to now, not enough pairwise tight-binding parameters are
available. According to the practitioners, it takes $\frac{1}{2}$ –1 year to generate a new set of
15 parameters for your problem of interest, and you need such parameters for every
pair of atom types (n atoms $\rightarrow n(n+1)/2$ pairs). What is the story on this at the
moment? We have found some parameters for organic molecules in the literature,
but it would be incredibly helpful if there were also such parameters *e.g.* for
interactions between metals and organic molecules.

20 **Gerit Brandenburg** replied: There are different groups working on DFTB
parametrization. While we used the 3OB parameter set, a current list is available.¹
A different strategy from the group of Stefan Grimme is the development of
a tight-binding Hamiltonian that relies on element parameters only and can thus
25 be parameterized much more rapidly. Elements up to Rn are available.²

1 <http://www.dftb.org/parameters/download>

2 Grimme *et al.*, *J. Chem. Theory Comput.*, 2017, 13, 1989.

30 (309:[321]321) **Matthew Addicoat** asked: Following up on parameters, you may
have been referring to the QUASINANO parameters, which are single-element
parameters up to element 90 (Th).^{1,2} Did you try using the MIO parameters at
all? I've had significant experience in both COFs and ionic liquids where we used
the MIO parameters with Lennard-Jones dispersion – in one paper a reviewer did
35 ask us to repeat our calculations with 3OB – we did so and got poorer results.³

In your paper, you did significant work on re-parameterising the dispersion
component, but didn't add any extra hydrogen bonding or halogen corrections.
Three of your molecules do have fluorine, chlorine or both. Did you see any
problems or poor behaviour with those molecules?

40 1 M. Wahiduzzaman, A. F. Oliveira, P. Philipson, L. Zhechkov, E. van Lenthe, H. A. Witek and
T. Heine, *J. Chem. Theory Comput.*, 2013, 9, 4006–4017.

2 A. F. Oliveira, P. Philipson and T. Heine, *J. Chem. Theory Comput.*, 2015, 11, 5209–18.

3 M. A. Addicoat, R. Stefanovic, G. B. Webber, R. Atkin and A. J. Page, *J. Chem. Theory
Comput.*, 2014, 10, 4633–4643.

45 **Gerit Brandenburg** answered: The QUASINANO set mentioned is part of the
effort to generate a DFTB parametrization for the whole periodic table. However,
it is still necessary to combine them with pair-parameters and those are only
available up to Ca.¹ A more extensive full parametrization is provided by the GFN-
50 xTB variant.²

1 A systematic comparison of QUASINANO, MIO, and 3OB parameter sets for
DFTB3 combined with the D3 dispersion correction has not been published. All
our initial tests on established benchmark sets for molecular dimers and crystals
5 (S66, L7, S12L, X23 test sets) have shown that the use of 3OB parameters is better
suited to describe the noncovalent interactions of mostly organic molecules. Our
optimized damping parameter sets with corresponding statistical evaluation have
been distributed in a private communication to ADF, where the QUASINANO set is
used, and will be provided by us upon request. A closely related test has recently
10 been done by combining DFTB3(3OB) and DFTB3(MIO) with the TS and MBD
dispersion correction models. In the supporting information of ref. 3, we directly
compare the intermolecular interactions and distances of molecular dimers (S66
set) obtained from different parametrizations (see Figure S7). In agreement with
our previous experience, the 3OB parameters are recommended for this system
class.

15 Hydrogen- and halogen-bonded molecules can be tougher to describe with
a simple point-charge electrostatic model. Ref. 71-73 in our paper try to correct
some of the systematic errors with additional pair-potentials. However, we found
that these additional corrections do improve the interaction energies in the
reference sets, but lead to only slight improvements in larger complexes.⁴ Thus,
20 we did not use these in our paper (DOI: 10.1039/C8FD00010G) and could not
detect major problems with the target molecules including halogens. However we
did not compare the energetic ranking in detail, as this was not sufficiently
accurate for any of our targets, and we recommend a subsequent energy evalua-
tion with a more accurate method.

1 Oliveira *et al.*, *J. Chem. Theory Comput.*, 2015, **11**, 5209.

2 Grimme *et al.*, *J. Chem. Theory Comput.*, 2017, **13**, 1989.

3 Mortazavi *et al.*, *J. Phys. Chem. Lett.*, 2018, **9**, 399.

4 Brandenburg *et al.*, *J. Phys. Chem. Lett.*, 2014, **5**, 4275.

30 (310:[322]322) **Christopher Taylor** enquired: You mentioned that you obtained
significantly improved results when performing a single-point calculation and
using an electrostatic multipole and empirical force field interaction model (*i.e.*
using the DMACRYS program). Can you clarify this – do you mean that you ran
35 only a single-point calculation in DMACRYS (*i.e.* the resulting structures are the
same as those from your DF-TB calculations, and not an energy minimum at the
multipole-and-force-field level of theory)? Or are you referring to the single-point
ab initio calculation required to obtain said multipoles (*i.e.* the structures are fully
minimised in DMACRYS after having been generated through DF-TB)?

40 **Gerit Brandenburg** replied: We did indeed follow the latter strategy, *i.e.* we
used the rigid DFTB3-D3 molecular geometries to compute the distributed charge
multipoles. Subsequently the DFTB3-D3 crystal geometry was relaxed with the
DMACRYS code by combining the multipole electrostatic with the empirical FIT
45 potential. This relaxation of the intermolecular degrees of freedom does not
notably increase the computational cost and we thus recommend including this
step. However, as a more general strategy, we have shown that even the inter-
molecular geometries of DFTB3-D3 (or DFTB3-MBD) can be used directly for
50 computed density functional based single-point energies.¹

1 Mortazavi *et al.*, *J. Phys. Chem. Lett.*, 2018, 9, 399.

311:[323]323) **Seiji Tsuzuki** said: I have two questions on the accuracy of DFT-B. The first question concerns the accuracy of the charge distributions obtained by the DFT-B method. The electrostatic interactions are important in determining the arrangement of molecules in crystals, since the electrostatic interaction is a highly directional interaction. It can be attractive or repulsive, depending on the orientation of the molecules. Therefore, accurate evaluation of the electrostatic interactions is important for crystal structure prediction. The accuracy of the calculated charge distributions can be judged by comparing the calculated dipole moment with the experimental one. *Ab initio* calculations show that a split valence basis set including polarization functions and electron correlation corrections are necessary for accurate calculation of the charge distributions. On the other hand, tight-binding calculations are semi-empirical calculations and use very small basis sets. I suspect that the DFT-B calculations cannot reproduce the experimental dipole moment well. Did you compare the dipole moments of molecules calculated by DFT-B with experimental values? I would like to know how large the errors of the calculated dipole moments are.

The second question concerns the accuracy of the calculated torsional potential by DFT-B. To reproduce the small energy difference between rotamers by *ab initio* calculations, a split valence basis set with polarization functions and electron correlation corrections are necessary. Is it possible to reproduce the experimental torsional potential by DFT-B? Have you compared the torsional potentials calculated by DFT-B with those obtained by high level *ab initio* calculations?

Gerit Brandenburg responded: The dipole moments are indeed a way to test the electrostatic interactions from DFTB3-D3. While similar studies have been conducted before, we have computed the dipole moment on a set of small semi-rigid molecules with experimental references; experimental values gathered in ref. 1. While DFT methods in converged basis set expansions (augmented triple-zeta or larger) indeed produce higher quality dipole moments, the results from DFTB3-D3 are reasonably good and actually better than those from a very recent tight-binding parametrization, GFN-xTB.² Correlations with the reference data (Pearson correlation and mean unsigned errors) are shown in Fig. 2. However, semi-empirical methods rely strongly on error compensations, *i.e.* the true test should be the total interaction energy that has been tested for molecular crystals in ref. 3.

It is correct that torsion potentials are crucial to describe the relative stabilities of molecular conformers. Individual torsions have sometimes been compared directly to high-level references. However, this is not trivial as any benchmark of full torsion potentials has to be based on multi-reference wavefunction methods. Thus, it is easier and more instructive to directly compare the relative stability of local equilibrium structures, *i.e.* molecular conformers. We have not done this for the target molecules in our paper (DOI: 10.1039/C8FD00010G), but in ref. 4 several established conformational benchmark sets were analyzed with different tight-binding approaches (including DFTB3-D3), showing reasonably good performance.

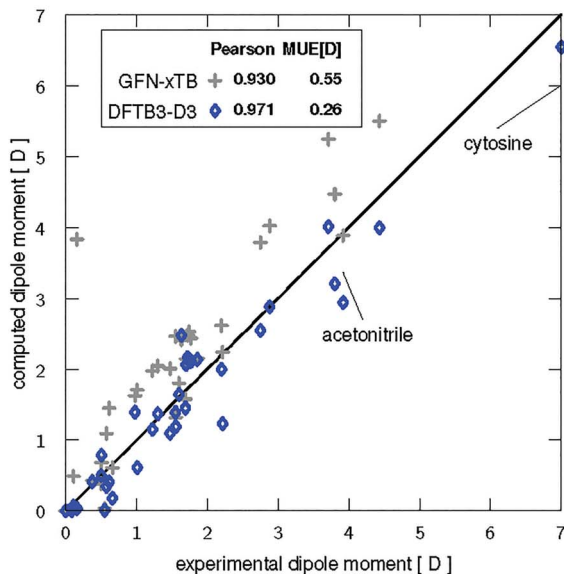


Fig. 2 Correlation with the reference data (Pearson correlation and mean unsigned errors).

1 Hickey *et al.*, *J. Phys. Chem. A*, 2014, **118**, 3678.

2 Grimme *et al.*, *J. Chem. Theory Comput.*, 2017, **13**, 1989.

3 Brandenburg *et al.*, *J. Phys. Chem. Lett.*, 2014, **5**, 1785.

4 S. Grimme, C. Bannwarth and P. Shushkov, *J. Chem. Theory Comput.*, 2017, **13**, 1989.

(312:[324]324) **Gregory Beran** asked: You noted that DFTB3-D3 provides useful predictions for the free energy contributions. Does it reproduce each individual phonon mode frequency well, or is it a case where good error cancellation occurs when summing over all the vibrational modes when computing free energies?

Gerit Brandenburg answered: In our paper (DOI: 10.1039/C8FD00010G), we computed free energy contributions based on the DFTB3-D3 model and contrasted it with rigid-body models. Some comparisons to higher-level DFT results and experimental measurements have been conducted.^{1,2} However, our analysis is indeed a rather coarse-grained one, as only integrated quantities (like free energy contributions) are analyzed. In this regard, Prof. Beran is correct and we do rely on compensation of errors.

In earlier studies, the covalent modes from DFTB have been analyzed.³ While the authors recommended a scaling factor, it is not clear how this would translate to soft non-covalent modes. Clearly, further detailed analysis for molecular crystals is needed in order to make faithful predictions. We would emphasize that methods need to be tested and validated for flexible pharmaceutical crystal structures to test the description of the coupling between the molecular and intermolecular modes, which seems likely have a significant effect on the relative free energies.

1 Brandenburg *et al.*, *J. Phys. Chem. Lett.*, 2017, **8**, 4319.

2 Buchholz *et al.*, *Cryst. Growth Des.*, 2017, 17, 4676.
3 Witek *et al.*, *J. Comput. Chem.*, 2004, 25, 1858.

(313:[325]325) **Marcus Neumann** remarked: Some years ago we introduced phonon free energies in GRACE based on our tailor-made force fields, and found out that those free energies actually had a negative impact on our energy rankings. Phonon free energies strongly depend on the vibrational frequencies of the soft modes, and small errors in the force calculations result in large errors in the phonon free energies. The energy ranking performance of DFTB3-D3 does not seem to be better than the performance of tailor-made force fields, so I would expect the same for its use in phonon free energy calculations. What evidence do you have that phonon free energies calculated with DFTB3-D3 actually improve the energy ranking performance?

Gerit Brandenburg replied: DFTB3-D3 based lattice energies are not satisfactory for a faithful energy ranking and might not outperform the tailor-made force field within GRACE. On the other hand, the equilibrium geometries seem to be of good quality, as shown by the small deviations w.r.t. experimental crystal structures. How this translates into the properties of second derivatives is not clear *a priori*, especially as the low-energy modes are most important for the entropy estimates. From the ranking of our computed energy landscapes, we have some indication of an improved ranking, *e.g.* for target XXVI the experimental structure is rank 2 based on lattice energies and moves to rank 1 upon inclusion of the DFTB3-D3 based free energy contributions. A direct comparison of free energy contributions from DFTB3-D3 with DFT based references has been recently done on a carbamazepine polymorph.¹ This has to be extended to broader tests. The contributions of paper 11895 (DOI: 10.1039/C8FD00048D) and paper 11896 (DOI: 10.1039/C8FD00066B) might be ideally suited to conduct this analysis.

1 Brandenburg *et al.*, *J. Phys. Chem. Lett.*, 2017, 8, 4319–4324.

(315:[326]326) **Johannes Hoja** asked: You mention in your paper that tighter convergence criteria had to be used in order to remove imaginary frequencies in the DFTB3-D3 phonon calculations. What were the tightest convergence settings necessary in order to avoid imaginary frequencies?

Gerit Brandenburg responded: The “tightened” optimization criteria correspond to the standard thresholds of CRYSTAL17, *i.e.* maximal gradient component of 0.00045 a.u., rms gradient of 0.0003, maximal displacement of 0.0018 a.u., and rms displacement of 0.0012 a.u. Additionally, the components of the dynamical matrix are computed by symmetric finite displacements (in contrast to the default of just one displacement).

(317:[327]327) **Ivo Rietveld** opened the discussion of the paper by Claire S. Adjiman: The potentials in the calculations of the crystal structures are adjusted using sublimation enthalpy data. How do you guarantee that the sublimation enthalpy data is accurate and not affected by impurities, and that the data is for the correct polymorph? How is the precision of the sublimation data dealt with, in particular when the vapor pressure is low? Sublimation data cannot be used for

1 new polymorphs that are obtained purely by prediction. How is the available
sublimation data generalised within the code to improve the stability prediction
of unknown polymorphs?

5 **Claire Adjiman** answered: We have carefully selected data from the literature,
paying attention to the experimental methods used, but ultimately we cannot
guarantee the accuracy of all data points. The error in the data can be taken into
account by adjusting the weight given to each data point (*e.g.* in the maximum
10 likelihood approach, each data point is weighted based on the corresponding
variance). We investigated the impact of such weights on the parameters for the
hydrocarbons (*c.f.* Fig. 3 in the paper) and found that using equal weights for the
structural data and for the sublimation enthalpies led to parameters which gave
a good structure reproduction relative to what is achieved with a weight of 0 for
15 sublimation enthalpies, and a good quality of reproduction of the sublimation
enthalpies. We subsequently used equal weights. We do not use any information
on predicted or unknown polymorphs for parameter estimation. In our data set,
we have only one molecule with two polymorphs, tetracyanoethylene, and we
ensured that the parameters yielded the correct energy ranking of these two
20 polymorphs. In the future, we would like to include information on relative
energies in the objective function.

(318:[328]328) **Jonas Nyman** asked: Have you benchmarked your new force
field against the currently very popular X23 benchmark? Are some of the struc-
25 tures in the X23 set in your training and/or validation sets? Also, have the
parametrizations been automated in such a way that you could fit other functional
forms, such as a Lennard-Jones potential, or a damped Buckingham with addi-
tional higher-order C8/C10 dispersion terms?

30 **Claire Adjiman** replied: We have not benchmarked our force field against the
X23 data set. The following X23 structures are included in our training set: 1,4-
cyclohexanedione (CYHEXO), acetic acid (ACETAC07), adamantane (ADAMAN08),
anthracene (ANTCEN16), benzene (BENZEN06), imidazole (IMAZOL06), naph-
thalene (NAPHTA31), pyrazine (PYRAZI01), succinic acid (SUCANH14), triazine
35 (TRIZIN01), and trioxane (TROXAN). The parameter estimation code currently
does not allow the direct use of alternative potentials. However, it can be modified
relatively easily to work for the Lennard-Jones potential or a higher-order Buck-
ingham potential.

40 (319:[329]329) **Sharmarke Mohamed** remarked: The work presented in your
paper is a welcome contribution for practitioners of crystal structure prediction,
who for a long time have used model intermolecular potentials that have been
fitted to crystal structures that are often not representative of the systems under
45 study. In work conducted within my group, I have found that the FIT force field
actually performs well in modelling the intermolecular interactions in two-
component molecular salt systems. However this force field is not appropriate
for three-component molecular systems (*e.g.* cocrystal hydrates or ionic cocrys-
tals). The *ab initio* model used to fit the potential parameters is an important
50 factor in this and so it is very encouraging that the authors have developed and
tested a method for deriving potential parameters that can be tailored to different

1 *ab initio* models. I am curious, however, whether the authors feel that the lack of
complex molecular systems (*e.g.* hydrates, cocrystals, salts) in their dataset of 106
crystal structures will present challenges in the use of these potential parameters
for studies of multicomponent systems. Have the authors tested the trans-
5 ferability of these new parameter sets to multicomponent systems that display
competing intermolecular interactions? Could the authors also comment on the
typical cost in time (*i.e.* how many weeks?) that would need to be spent on using
the method proposed in this paper to derive system-specific parameters (*i.e.*
potential parameters for salt hydrates) using a specific *ab initio* model?
10

Claire Adjiman responded: Thank you for the positive comments. We have not
yet tested the proposed parameters for such multicomponent systems. In our
view, the dataset needs to be expanded to include hydrates and salts, as well as
flexible molecules, to increase the transferability. We are currently working in this
15 direction. The main cost in deriving parameters is to gather reliable data on
crystal structures with sufficient diversity. The computations are highly paral-
lelisable and their cost depends principally on the number of data points in the
training set. Using one core, the regression of the parameters corresponding to
one box in Fig. 2 of the paper requires approximately 150 days of wall time for
20 a single core. This is equivalent to about 20 h per local minimisation, and all
minimisations are independent of each other.

(320:[330]330) **Sten Nilsson Lill** asked: Your choice of functional (M06) is very
25 sensitive to the numerical grid accuracy. Did you apply a tight grid in your
calculations to ensure you had a stable final solution?

Claire Adjiman answered: Yes, we used a very tight grid for our calculations.

(321:[331]331) **Seiji Tsuzuki** enquired: I have a question about the exchange-
30 repulsion potential in your force field. You showed that the performance of the
calculation of sublimation energy is improved by the improvement of the force
field, but the calculated sublimation energies still have large errors in some cases.
It is well known that the exchange-repulsion potentials of hydrogen and halogen
35 atoms have strong anisotropy. The importance of the anisotropy of hydrogen
atoms in reproducing the crystal packing of hydrocarbon molecules by force field
calculations was suggested by Williams in the 1970s. I believe that it is necessary
to consider the anisotropy of exchange-repulsion interactions to improve the
40 performance of the calculation of sublimation energies. Why don't you use
anisotropic exchange-repulsion potentials for the calculation of the sublimation
energies?

Claire Adjiman responded: I agree that it is often important to include
45 anisotropy in the calculations. We have designed our parameter estimation code
so that the parameters can easily be re-estimated as one makes changes to the
lattice energy model, either in the *ab initio* components of the model (intra-
molecular energy and electrostatics) or in the form of the repulsion-dispersion
potential. In this paper, we focused on re-parameterising the most common
50 potential, the isotropic Buckingham, for one specific level of theory for the DFT

1 calculations (M06/6-31G(d,p)). In the future, we intend to re-use the methodology
and code to develop anisotropic potentials.

5 (322:[332]332) **Luca Iuzzolino** said: You have shown that the new repulsion-
dispersion parameters improve the absolute energies of the crystal structures that
were considered in this study. Is this also true for the relative energy differences
between polymorphic forms of the same molecules?

10 **Claire Adjiman** replied: The relative stability of TCNE polymorphs in the
training set is correctly reproduced. We have not yet tested other polymorphic
systems.

15 (324:[333]333) **Sarah Price** remarked: It is about time that something was done
to improve the FIT potential. In 1996, David Coombes fitted a polar hydrogen
potential to allow modelling of some hydrogen-bonded structures when used with
in combination with Williams' old parameters from papers from the 1980s.
Williams had fitted his parameters to few crystal structures and very few subli-
20 mation energies. The fluorine parameters have given some problems, probably
because of the sublimation energy used in derivation, but generally it is
surprising how many hundreds of CSP studies we have been able to do with the
FIT potential, given how it was derived. I look forward to trying your new sets of
parameters, with distributed multipoles for a good quality of charge density.
25 However, I notice that you haven't got many cross-terms for two heteroatoms,
such as nitrogen-oxygen, which we would need for amide hydrogen bonding.
What are the difficulties? Would you advise trying combination rules for the
missing parameters?

30 **Claire Adjiman** answered: Thank you for the positive comments. In the first
instance, I would indeed advise using standard combining rules. The main
limiting step is the creation of the training and validation sets, curating the data
to ensure high reliability and adequate coverage of different types of structures.
We are currently working to expand the set of parameters published here to
35 include fluorine as well as heteroatom cross-interactions.

(800:[334]334) **Alan Hare** asked: Following up on the question of intra-
molecular smoothing: is the discontinuity in the potential true or apparent?
While sometimes there can be an abrupt separation between two proximate,
40 distinct functions, in others – like melting “squares of chocolate”, as the poster
reminded me! – a single, continuous function may really straddle the divide, or
the “break between squares”... which can itself sometimes be transformed into
a simpler function. On reflection, am I right in thinking that in the intramolecular
case – with its multiplicity of rotations – the discontinuity is truly an abrupt one?
45 If so, I imagine that smoothing across it may involve the use of a hyperbolic
tangent (or possibly sigmoidal) function close to the “cut-over”, so to speak. Or do
you have another way of handling it altogether?

50 **Claire Adjiman** responded: This relates to the poster presented by Isaac Sugden.
The functions are discontinuous because that there are two different values
for the intramolecular energy at the boundary between two local approximate

1 models (LAM points). This is because in the early versions of this approach each
LAM has a well-defined region of use and we switch abruptly between LAMs as we
5 cross boundaries. I have sketched this roughly to help visualise what happens (see
Fig. 3). In an intuitive sense, how abrupt the discontinuity is depends on how
different the two function values are. Regardless, the discontinuities are always
10 expected to be present. These discontinuities are not physical – they are artefacts
of the local models used. In this work, we corrected this by replacing the use of
a single LAM by an average of all the LAMs. The average is weighted so that the
LAM nearest to the current point of interest carries the most weight. We compute
the weight of each LAM so that it decays exponentially as the distance between the
point of interest and the LAM point increases.

15 (804:[335]335) **Gerit Brandenburg** communicated: The authors made a nice
effort in parameterizing the FIT potential for use in organic molecular crystal
structure prediction containing the elements H, C, N, O and Cl. While hydrogen
has parameters that depend on its binding motif, other elements have a single set
of parameters. Considering the London dispersion interaction, this might be
20 a crude approximation, especially for carbon, which has quite a large variety in its
dynamic polarizability. Fig. 4 shows computed (TD-DFT) dispersion coefficients
for carbon in different environments, which are then used as references in the D3
dispersion correction scheme.¹ As the range of C_6^{CC} is from 20 to about 50 a.u., this
might be relevant for the FIT type potential. The D3 coefficients are

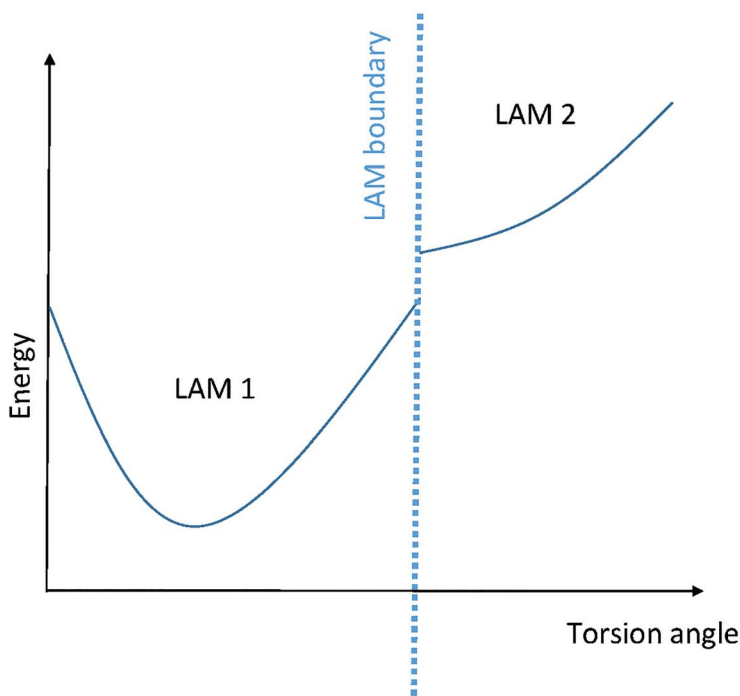


Fig. 3 Abrupt switching between LAMs at LAM boundary.

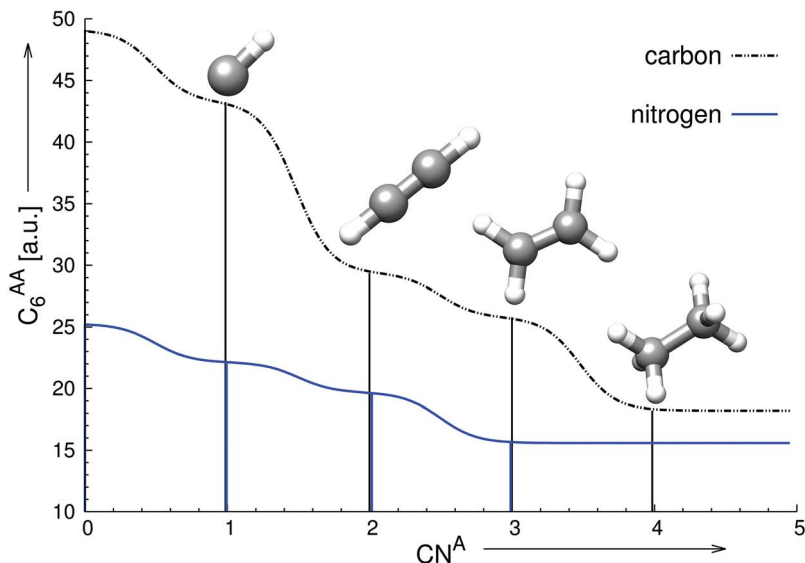


Fig. 4 CN dependent atom pairwise dispersion coefficient for homoatomic pairs C_6^{AA} as a function of the coordination number CN^A . The reference points $C_6^{AA,ref}$ are drawn as vertical sticks in the respective colors (black for carbon, blue for nitrogen). Figure reproduced with permission from ref. 3.

computationally easily accessible and yield high-quality inter-molecular dispersion coefficients (see Fig. 2 in ref. 2). Are the authors considering using environment dependent parameters for elements other than H?

- 1 S. Grimme, J. Antony, S. Ehrlich and H. Krieg, *J. Chem. Phys.*, 2010, **132**, 154104.
- 2 E. Caldeweyher and J. G. Brandenburg, *J. Phys.: Condens. Matter*, 2018, **30**, 213001.
- 3 S. Grimme, A. Hansen, J. G. Brandenburg and C. Bannwarth, *Chem. Rev.*, 2016, **116**, 5105.

Claire Adjiman communicated in reply: It is indeed an approximation not to take into account the environment of other elements. We strive for a balance between the accuracy of the model and the statistical significance of the parameter values. As we increase the number of atom types and hence the number of parameters, we are likely to achieve greater accuracy, at the cost of decreased statistical significance as data scarcity is an issue. The set of atom types chosen has so far provided a good balance between accuracy and significance, with enough data available in most cases for training and validation of the models. We note that the parameters are effective values rather than a reflection of intrinsic repulsive–dispersive interactions: as such, we include multiple atom environments in the data set for training and obtain parameters that provide an average interaction. In addition, as discussed in the paper, the repulsion–dispersion term in our model of lattice energy includes all the aspects that are not taken into account in the model, such as entropic contributions or polarizability. This is very different in concept to the D3 coefficients, for which the objective is to obtain an intrinsic value of the dispersive interactions only. Thus, the proposed repulsion–dispersion potential contains an empirical correction of the potential. One could

1 in principle modify our model to use D3 coefficients and introduce a different
empirical correction.

5 (325:[336]336) **Marcus Neumann** opened a general discussion of the papers by
Alexandre Tkatchenko, Jan Gerit Brandenburg and Claire S. Adjiman: Calculating
the relative stabilities of crystal polymorphs is at the very heart of organic crystal
structure prediction. Yet very little reliable information, especially for larger
10 molecules, is available in the scientific literature. Experimental error bars are
missing in most cases. If we really want to make progress in the energy ranking
accuracy, a reliable experimental energy benchmark must be established. Ideally,
20–100 polymorphic enthalpy and free energy differences should be measured,
each by different methods and different researchers.

15 Having talked to several experimentalists in academia about the issue, it seems
that getting funding for such an endeavour is very difficult because accurate
thermodynamic measurements by themselves are not considered innovative. As
a community, we should try to convince a national or transnational funding
agency to support the accurate measurement of polymorphic energy differences.

20 **Claire Adjiman** responded: I concur that it is important to generate such
a benchmark data set. This could be done through collaborative projects where one
student works across experimental and computational groups, measuring some
data and assessing/improving the state-of-the-art in modelling. This would provide
a coherent scientific problem and expose the students to different tools/learnings,
25 and by working in tandem such projects may be more compelling for both
researchers and funders. Of course one can imagine doing this across a larger
consortium of collaborators, where we might explore a broader range of properties.
ITN or COST would be good ways forward. There is also the example of the UNIFAC
consortium, which has been obtaining data and developing models for fluid phase
30 equilibria for many years, first in academia and now as an independent company.¹

1 http://unifac.ddbst.de/unifac_.html

35 **Ivo Rietveld** responded: As an experimentalist, I would like to add a few points.
First of all, it is hard to give a PhD student such a subject, because he or she
should at least have to deal with a scientific problem that will lead to a proper
scientific thesis (and answer...?). Just data as such will not be enough, but in the
end we also look for precise thermodynamic rankings, so it is a matter of
40 matching the right substances with the right scientific questions. That will
remain a sort of case-by-case issue.

Second of all, precision is difficult, also experimentally. The experimentalists
may claim small error bars, and certainly with calorimetry and X-ray diffraction
we are good at determining differences, as long as we do it on the same equip-
45 ment(!), but again everything depends on the system, and whether the chemical
compound can be measured with the precision that is required for computer
calculations. Therefore, from an experimental point of view, the database is
probably easier to define not in terms of substances, but in terms of transition
values of which we are very confident. For ROY, for example (with which I am in
50 fact not very familiar), there may be phases that are extremely well documented,
whereas others are not because they are an experimental nightmare.

1 I think therefore that this question may be resolved by some sort of COST (or
other!) network, where the uptake into the database of experimental systems that
we are studying for other reasons anyway can be discussed. A decision to take up
5 a substance or transition in the database within this COST network will initiate
additional measurements by other experimentalists and calculations by compu-
tationists to come to consolidated transition values between very specific poly-
morphs. This latter part will likely need extra funding, but we may be able to
leverage funding within such a COST network. This COST network should also
10 function as quality control of the experimental values and computational values.

For the precise measurements, we may be able to apply for grants that
15 emphasise the industrial development of scientific findings, particularly if all the
large European pharmaceutical companies can be involved in the grant applica-
tion. Some validation work may be done by a number of post-docs and papers may
be published in the same vein as the polymorph prediction blind tests. Why not
discuss the experimental and computational caveats and how we interpret, say,
the experimental and computational results of 10 polymorphic transitions
towards a rigorous database? More importantly: who is in?

20 **Alexandre Tkatchenko** responded: I strongly concur with Marcus and others as
well. Perhaps the effort of encouraging our experimental colleagues would have
a higher chance of success if all the participants (theorists, experimentalists and
industry) show strong interest and push each other. For a start, it would be good if
industry decided to disclose existing thermodynamic data for interesting poly-
25 morphic systems. I am sure this data is lying around in different companies.
High-level quantum-chemical calculations are also very relevant and should be
done. One current problem with non-canonical CCSD(T) and QMC is that accu-
racy is very hard to control to the required level of 1 kJ mol^{-1} , especially for larger
molecules. So far, the accuracy of these methods in periodic calculations has been
30 assessed by comparing to experiments, and never for energy differences between
polymorphs. In this case, glycine, oxalic acid and coumarin (mentioned by Qiang
Zhu) would be good systems to which to start applying QMC/CCSD(T). Regarding
challenging systems, axitinib and ROY are good ones going forward. However, in
the case of ROY, my understanding is that it is hard to ensure that experiments
35 measure pristine and non-defect structures.

Christian Schön responded: I strongly concur with Marcus Neumann. I have
40 tried for many years to convince my experimental solid chemistry colleagues to
perform systematic analyses of their syntheses of well-defined systems,
producing quantitative outcomes as function of synthesis parameters, in order to
provide data to sharpen our theoretical tools for modeling chemical syntheses.
But in the end, nobody was willing to give a student this endeavor – I guess it is
45 not “sexy” enough (no new compounds or crystal structures being produced, *etc.*)
and it might be too difficult to publish such a study. (I have heard similar
complaints from people in the phase diagram community – they have a hard
time getting funding agencies interested unless the chemical system has
important applications.) I can see that a similar problem would appear in the
50 accurate measurement of free energy differences, and I would strongly support
such a measurement campaign.

1 **Qiang Zhu** responded: I agree. I think the first step is to create a good poly-
morph data set that can present the real challenges in energy ranking. Currently,
the X23 set has been studied a lot,^{1,2} but it seems to me that many methods
5 produce nice results at about the same level. Do they really reflect the challenge in
energy ranking? I have two systems which strongly oppose this conclusion –
coumarin³ and ROY (DOI: 10.1039/C8FD00039E). These might be very small
molecules by Marcus Neumann's standards, but most methods still fail to
reproduce the ranking nicely. As a community, we need to come up with a plan to
10 create a list of challenges and then work it out. This requires a synergy between
experiment and theory.

1 A. Otero-de-la-Roza and E. R. A. Johnson, *J. Chem. Phys.*, 2012, **137**, 054103.

2 A. M. Reilly and A. Tkatchenko, *J. Phys. Chem. Lett.*, 2013, **4**, 1028.

3 A. G. Shtrukenberg, Q. Zhu, D. J. Carter, L. Vogt, J. Hoja, E. Schneider, H. Song, B. Pokroy, I.
Polishchuk, A. Tkatchenko, A. R. Oganov, A. L. Rohl, M. E. Tuckermanekj and B. Kahr,
15 *Chem. Sci.*, 2017, **8**, 4926.

(326:[337]337) **Gerit Brandenburg** remarked: The electronic structure
community has made some substantial developments in the past years, with
CCSD(T) being applicable to large and sometimes periodic systems (mostly
20 relying on embedding or localization schemes). We have contributed to this
endeavour by extending the applicability of Quantum Monte Carlo to organic
crystals.¹ This approach can potentially be used to compute the static lattice
energies of large molecular crystals and their polymorphs (~200 atoms per unit
cell) in a reasonable time frame.

This could ideally be complemented by experimental relative stabilities to
independently test the capabilities of CSP methods to predict relative lattice
energies (*vs.* high-level theory) and relative free energy differences (*vs.* experi-
ment). This is closely connected to Marcus Neumann's previous question and
similarly requires funding to afford the substantial CPU time.

As an add-on concerning the CPU time: the computation of a lattice energy for
benzene and anthracene crystals with sub-chemical accuracy (regarding the
thresholds we can control) requires 6000 and 74 000 CPU hours. The time will
clearly depend on the system size (roughly cubic scaling with the number of
35 atoms), the target accuracy (*e.g.* reducing it from 0.5 kJ mol⁻¹ to 0.1 kJ mol⁻¹
increases the CPU time by an order of magnitude), and the employed time step
(doubling it halves the CPU time), which varies a lot with the target molecule.
Once a decision on target crystal structures has been made, more quantitative
estimates are possible.

1 A. Zen, J. G. Brandenburg, J. Klimeš, A. Tkatchenko, D. Alfè and A. Michaelides, *Proc. Natl.
Acad. Sci. USA*, 2018, **115**, 1724–1729.

Matthew Ryder replied: I agree that this approach could yield valuable insights
45 into the capabilities of different CSP methods to predict lattice energies.

(328:[338]338) **Christian Schön** addressed Johannes Hoja and Gerit Branden-
burg: It looks like we are getting good results on the energy evaluation front for
molecules and molecular crystals. But what about the quality/computational
expense of your methods for applications to molecules on surfaces? Can you
50 handle this as “just another application” of your methods, or would one still need

1 years of new developments/adaptations? What about the size of the (flexible)
molecules – do you envision computing proteins on this level of accuracy?

5 **Johannes Hoja** answered: Our methods can be and have already been used to
study the adsorption of molecules on surfaces (chemisorption, physisorption, and
intermediate situations). Based on the Tkatchenko–Scheffler dispersion model,
the vdW^{surf} method was developed to also incorporate screening effects from the
substrate electrons.¹ Examples of applications of the DFT+vdW^{surf} and DFT+MBD
10 methods can be found in ref. 2–5. These calculations provide accurate adsorption
energies and geometries, and can readily be carried out on state-of-the-art
computing facilities. Several DFT+MBD single-point energies could be obtained
for isolated small proteins.

15 1 V. G. Ruiz, W. Liu, E. Zojer, M. Scheffler and A. Tkatchenko, *Phys. Rev. Lett.*, **108**, 146103.

2 V. G. Ruiz, W. Liu and A. Tkatchenko, *Phys. Rev. B*, **93**, 035118.

3 R. J. Maurer, V. G. Ruiz, J. Camarillo-Cisneros, W. Liu, N. Ferri, K. Reuter and A.
Tkatchenko, *Progr. Surf. Sci.*, 2016, **91**, 72–100.

4 Y. Jiang, S. Yang, S. Li and W. Liu, *Sci. Rep.*, 2016, **6**, 39529.

5 S. Yang, Y. Jiang, S. Li and W. Liu, *Carbon*, 2017, **111**, 513–518.

20 **Gerit Brandenburg** answered: Molecules adsorbed on surfaces are indeed
technically just another application. The computational expense grows (typically
cubic scaling) with the size of the system and one has to converge the size of the
unit cell to remove artificial interactions of the molecule with itself, *i.e.* to
converge to the low-coverage adsorption, as well as the thickness of the surface
25 layer. However, one has to carefully control the accuracy of the vdW corrected
density functional as it is less established compared to organic crystals. This
holds in particular for conducting surfaces, as the vdW corrections rely on local
response models that might not be justified for conductors. Even the water
adsorption on a wide gap hBN surface can be a challenge.¹ As the corresponding
30 measurements are not trivial and reference quality calculations are rare, we need
more experience for a better quality assessment.

VdW-inclusive DFT can be applied to small protein crystals like crambin
within standard codes.² GPU accelerated program codes have been used for
35 studying protein ligand binding affinities,³ and linear scaling codes can be used
to study the ion channel gramicidin A.⁴

1 Y. S. Al-Hamdani, M. Rossi, D. Alfè, T. Tsatsoulis, B. Ramberger, J. G. Brandenburg, A. Zen,
G. Kresse, A. Grüneis, A. Tkatchenko and A. Michaelides, *J. Chem. Phys.*, 2017, **147**, 44710.

2 Piane *et al.*, *Chem. Sci.*, 2016, **7**, 1496; CRYSTAL17 code.

3 Ehrlich *et al.*, *ChemPhysChem*, 2017, **18**, 898; TerraChem code.

4 Todorović *et al.*, *J. R. Soc. Interface*, 2013, **10**, 20130547; CONQUEST code.

(329:[339]339) **Christian Schön** addressed Johannes Hoja and Gerit Branden-
burg: What is a “large” molecule in the context of your energy calculations?

45 **Johannes Hoja** replied: The calculation time for molecular crystals does not
directly depend on the size of the involved molecules, but rather on the number of
atoms present in the unit cell of the studied molecular crystal. The largest unit cell
in our study of the latest blind test systems consists of about 1000 atoms.

1 **Gerit Brandenburg** replied: From my experience this mainly depends on the type of application. The examples given in the answer to the previous question range from 1000 to 10 000 atoms per unit cell and would be considered large.

5 (330:[340]340) **Christian Schön** addressed Johannes Hoja and Gerit Brandenburg: Where would you place the current limits of your calculations, *i.e.* what kind of computational facilities (and what kind of time scales/levels of global optimization) are needed for which size of system?

10 **Johannes Hoja** responded: I believe that for production calculations the upper limit of PBE+TS or PBE+MBD lattice relaxations and subsequent PBE0+MBD energy calculations would be around 100 structures, and that vibrational free energies in the harmonic approximation could be calculated for tens of structures. The computation time actually required highly depends on the sizes of the sampled unit cells, and for the phonon calculations, also on the unit cell shape and symmetry. In general, a cluster with more than 500 cores would be advisable for these kinds of calculations. For example, a PBE+TS lattice optimization with subsequent PBE0+MBD energy evaluation and PBE+TS vibrational free energies (with settings as described in the paper) for Form A of system XXIII (172 atoms per unit cell) would require about 1100 CPU hours.

20 **Gerit Brandenburg** responded: Different codes scale differently and not all can fully use HPC facilities; for instance CRYSTAL17 has been shown to scale well up to 32 000 cores.¹ A DFT based re-ranking of crystal energy landscapes (or lists of putative polymorphs) has been conducted for the 6th CSP blind test;² the CPU time for local optimizations of 5000 structures are presented in Table S9 using 71 000 to 3 200 000 CPU hours. 100 000 CPU hours would amount to approximately 16 d elapsed time on a 256-core machine.

30 1 Erba *et al.*, *J. Chem. Theory Comput.*, 2017, **13**, 5019.
2 Reilly *et al.*, *Acta Cryst. B*, 2016, **72**, 439.

35 (331:[341]341) **Christian Schön** enquired: Experimental colleagues tell me that there is a net transfer of charge between the molecule and the metal surface. Does this complicate the calculations for you, or can you predict this charge transfer quantitatively?

40 **Johannes Hoja** answered: Van der Waals-inclusive DFT calculations capture charge transfer effects in principle, but I am not aware of any benchmark calculations.

45 **Gerit Brandenburg** answered: Technically this is not an issue, as the electron density is relaxed self-consistently. One can partition the self-consistent density to molecules, which would correspond to the charge transfer when compared to neutral molecules. However, some of the most frequently used DFT approaches of the generalized gradient type have a systematic error of too strong electron density delocalization, *i.e.* for a quantitative comparison to experiments one probably has to use a hybrid functional that reduces this error.

1 (340:[342]342) **Marcus Neumann** commented: Regarding a previous question
about the CPU time requirements for PBE(0)+MBD+Fvib, I would like to mention
that we recently implemented the approach in GRACE and are in the possession
5 of some early CPU time benchmark results. The actual QM calculations were
carried out with FHIaims through a driver implemented in GRACE. For blind test
compound XXVI, we found that it is possible to process about 4 crystal structures
on 384 modern Intel XEON cores in 1 day.

10 (345:[345]345) **Christian Schön** addressed Johannes Hoja and Gerit Branden-
burg: What kind of codes support your methods – only FHI-AIMS?

15 **Johannes Hoja** replied: To my knowledge the Tkatchenko–Scheffler (TS) and
the many-body dispersion (MBD) methods are implemented in FHI-aims,
Quantum Espresso, VASP, CASTEP, ADF, Q-Chem, and DFTB+. Furthermore,
a general many-body dispersion library is currently in development.¹

1 <https://github.com/azag0/libmbd>

20 **Gerit Brandenburg** replied: Both D3 as well as MBD dispersion corrections are
implemented to be used in conjunction with DFTB3 or DFT in freely available
codes.^{1,2} Additionally, several codes support the corrections; a non-complete list:
VASP (D3 and MBD), FHI-aim (D3 and MBD), ADF (D3 and MBD), DFTB+ (D3 and
25 MBD), CRYSTAL17 (D3) CP2K (D3), Orca (D3), Turbomole (D3), Psi4 (D3),
Gaussian (D3), QuantumEspresso (older D2 and TS), CASTEP (older D2 and TS),
and Siesta (older D2).

1 <http://www.thch.uni-bonn.de/tc/dftd3>

2 <http://www.fhi-berlin.mpg.de/~tkatchen/MBD>

30 Conflicts of interest

Julian Helfferich and Marcus Neumann work for a company that develops
35 software for organic crystal structure prediction. There are no other conflicts to
declare.