

Non-standard neutrino interactions and low energy experiments

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Abstract

We formulate an Effective Field Theory (EFT) for Non Standard neutrino Interactions (NSI) in elastic scattering with light quarks, leptons, gluons and photons, including all possible operators of dimension 5, 6 and 7. We provide the expressions for the cross sections in coherent neutrino-nucleus scattering and in deep inelastic scattering. Assuming single operator dominance we constrain the respective Wilson coefficient using the measurements by the COHERENT and CHARM collaborations. We also point out the constraining power of future elastic neutrino-nucleus scattering experiments. Finally, we explore the implications of the bounds for SMEFT operators above the electroweak breaking scale.

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I. INTRODUCTION

In the SM the neutrinos interact with matter through exchanges of W and Z bosons. In addition, in the presence of new physics, the neutrinos could interact with matter via new mediators. Such Non-Standard neutrino Interactions (NSI) were contemplated already 40 years ago by L. Wolfenstein in the seminal paper on neutrino oscillations in matter [1]. Since then the NSI were studied extensively, but with a strong focus on neutrino oscillations, see, e.g., [2–11]. The bounds from neutrino oscillations are limited in scope, since they are sensitive only to a subset of possible NSI. The common NSI effective Lagrangian relevant for neutrino oscillations contains only dimension 6 operators, see, e.g., [12],

$$\mathcal{L}'_{\text{NSI}} = \frac{G_F}{\sqrt{2}} \sum_{f,\alpha,\beta} (\bar{\nu}_\alpha \gamma_\mu P_L \nu_\beta) \left(\varepsilon_{\alpha\beta}^{fV} \bar{f} \gamma^\mu f + \varepsilon_{\alpha\beta}^{fA} \bar{f} \gamma^\mu \gamma_5 f \right). \quad (1)$$

The dimensionless coefficients $\varepsilon_{\alpha\beta}^{fV}, \varepsilon_{\alpha\beta}^{fA}$ parametrize the strength of the NSI relative to the SM weak force, controlled by the Fermi constant, $G_F \simeq 1.167 \times 10^{-5} \text{ GeV}^{-2}$. The indices α and β run over the three neutrino flavours, and f over light charged fermions, $f = e, u, d, s$.

Eq. (1) does contain all possible dimension 6 NSI operators. Still, these are not all the possible NSI. In these paper we list a complete basis of NSI operators up to and including dimension 7. The additional dimension 5 and dimension 7 operators either do not contribute to neutrino oscillations, because they lead to zero forward scattering matrix elements, or give contributions that are additionally suppressed by neutrino masses (tensor operators may be relevant for neutrino oscillations in polarized matter [6]). The dimension 5 and 7 NSI can be probed through neutrino inelastic scattering, and by precise measurements of solar neutrino scattering rates.

A qualitatively new set of NSI probes is opening up through the coherent neutrino scattering measurements. The first measurement of coherent neutrino scattering on nuclei was achieved by the COHERENT collaboration roughly a year ago, Ref. [13]. This result, and similar measurements in the future, now make it possible to probe a wide variety of NSI at low momenta exchanges.

The aim of present manuscript is to perform a systematic study of such NSI. We assume the NSI are described by an Effective Field Theory (EFT), i.e., that the new mediators are heavier than about $\mathcal{O}(100 \text{ MeV})$. In the analysis we include operators up to and including dimension 7, covering all possible chirality structures for neutrino currents. Our work

extends previous NSI analyses of coherent neutrino scattering, where a subset of EFT operators were discussed [14–21]. For projections of bounds on NSI from neutrino scattering in DUNE see [22, 23], while the potential of dark matter direct detection experiments for probing NSI using solar neutrinos was discussed in [20, 24–35]. For the potential of super-beam experiments to probe NSI, see [36]. For bounds on the neutrino dipole moment portal to heavy right-handed neutrino, see [37].

The paper is organized as follows. In Section II we formulate the EFT for coherent elastic neutrino-nucleus scattering ($\text{CE}\nu\text{NS}^1$) in the presence of NSI. The EFT valid at $\mu \sim 2 \text{ GeV}$ in which neutrinos couple to light quarks, gluons and photons, is nonperturbatively matched onto an EFT with nonrelativistic nucleons in Section III A, with the resulting $\text{CE}\nu\text{NS}$ cross sections given in Section III B. Section IV reviews bounds on NSI from neutrino oscillations, and Section V the deep inelastic scattering (DIS) probes of NSI, while Section VI contains our numerical analysis. In Section VII we explore the connection with physics above the scale of electroweak symmetry breaking, and draw our conclusions in Section VIII. Appendix A contains the definitions of nucleon form factors, Appendix B the predictions for the differential rates for various NSI operators, and Appendix C the numerical predictions for differential rates as functions of NSI Wilson coefficients.

II. OPERATOR BASIS FOR NSI

We are interested in the experiments where momenta exchanges are $q \lesssim \mathcal{O}(100\text{MeV})$, and thus well below the electroweak scale. The interactions of neutrinos with matter, i.e., with quarks, gluons, photons, electrons and muons, are described by an effective Lagrangian, obtained by integrating out the heavy degrees of freedom. These are the heavy SM particles: t, b, c quarks, τ lepton, W and Z bosons and the Higgs, as well as any heavy new physics particles.

The interaction Lagrangian for $\nu_\alpha \rightarrow \nu_\beta$ transition is given by a sum of non-renormalizable operators,

$$\mathcal{L}_{\nu_\alpha \rightarrow \nu_\beta} = \sum_{a,d=5,6,7} \hat{\mathcal{C}}_a^{(d)} \mathcal{Q}_a^{(d)} + \text{h.c.} + \dots, \quad \text{where} \quad \hat{\mathcal{C}}_a^{(d)} = \frac{\mathcal{C}_a^{(d)}}{\Lambda^{d-4}}. \quad (2)$$

¹ While not all of the NSI scatterings will be coherently enhanced we keep the, by now standard, $\text{CE}\nu\text{NS}$ terminology.

Here the $\mathcal{C}_a^{(d)}$ are dimensionless Wilson coefficients, while Λ can be identified, for $\mathcal{O}(1)$ couplings, with the mass of the new physics mediators. We consider a complete basis of EFT operators up to and including dimension seven. The sum in (2) runs over operator dimensions, $d = 5, 6, 7$, and operator labels, a , while in the notation we suppress the dependence on neutrino flavors α, β . The renormalization scale is fixed to $\mu = 2$ GeV, unless specified otherwise.

We first write down the full basis of EFT operators assuming neutrinos are Dirac fermions, and then comment below on what changes are needed, if neutrinos are Majorana. We use four-component notation, following the conventions of Ref. [38]. There is one dimension-five operator for each $\nu_\alpha \rightarrow \nu_\beta$ transition,²

$$\mathcal{Q}_1^{(5)} = \frac{e}{8\pi^2} (\bar{\nu}_\beta \sigma^{\mu\nu} P_L \nu_\alpha) F_{\mu\nu}, \quad (3)$$

where $F_{\mu\nu}$ is the electromagnetic field strength tensor. The dimension-six operators are

$$\mathcal{Q}_{1,f}^{(6)} = (\bar{\nu}_\beta \gamma_\mu P_L \nu_\alpha) (\bar{f} \gamma^\mu f), \quad \mathcal{Q}_{2,f}^{(6)} = (\bar{\nu}_\beta \gamma_\mu P_L \nu_\alpha) (\bar{f} \gamma^\mu \gamma_5 f). \quad (4)$$

The basis of dimension seven operators can be chosen such that there are four operators coupling neutrinos to photon or gluon field strengths,

$$\mathcal{Q}_1^{(7)} = \frac{\alpha}{12\pi} (\bar{\nu}_\beta P_L \nu_\alpha) F^{\mu\nu} F_{\mu\nu}, \quad \mathcal{Q}_2^{(7)} = \frac{\alpha}{8\pi} (\bar{\nu}_\beta P_L \nu_\alpha) F^{\mu\nu} \tilde{F}_{\mu\nu}, \quad (5)$$

$$\mathcal{Q}_3^{(7)} = \frac{\alpha_s}{12\pi} (\bar{\nu}_\beta P_L \nu_\alpha) G^{a\mu\nu} G_{\mu\nu}^a, \quad \mathcal{Q}_4^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\nu}_\beta P_L \nu_\alpha) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a, \quad (6)$$

three types of operators with chirality-flipping quark currents,

$$\mathcal{Q}_{5,f}^{(7)} = m_f (\bar{\nu}_\beta P_L \nu_\alpha) (\bar{f} f), \quad \mathcal{Q}_{6,f}^{(7)} = m_f (\bar{\nu}_\beta P_L \nu_\alpha) (\bar{f} i \gamma_5 f), \quad (7)$$

$$\mathcal{Q}_{7,f}^{(7)} = m_f (\bar{\nu}_\beta \sigma^{\mu\nu} P_L \nu_\alpha) (\bar{f} \sigma_{\mu\nu} f), \quad (8)$$

and four types of operators with additional derivatives on the neutrino currents,

$$\mathcal{Q}_{8,f}^{(7)} = (\bar{\nu}_\beta i \overleftrightarrow{\partial}_\mu P_L \nu_\alpha) (\bar{f} \gamma^\mu f), \quad \mathcal{Q}_{9,f}^{(7)} = (\bar{\nu}_\beta i \overleftrightarrow{\partial}_\mu P_L \nu_\alpha) (\bar{f} \gamma^\mu \gamma_5 f), \quad (9)$$

$$\mathcal{Q}_{10,f}^{(7)} = \partial_\mu (\bar{\nu}_\beta \sigma^{\mu\nu} P_L \nu_\alpha) (\bar{f} \gamma_\nu f), \quad \mathcal{Q}_{11,f}^{(7)} = \partial_\mu (\bar{\nu}_\beta \sigma^{\mu\nu} P_L \nu_\alpha) (\bar{f} \gamma_\nu \gamma_5 f). \quad (10)$$

² We use the phase convention in which the QED covariant derivative is $D_\mu \psi = (\partial_\mu + ie Q_\psi A_\mu) \psi$, with Q_ψ the electric charge of ψ . For Majorana neutrinos, for $\alpha = \beta$, one needs to include in the definitions of the operators an extra factor of $1/2$.

Here $G_{\mu\nu}^a$ is the QCD field strength tensor, $\tilde{G}_{\mu\nu} = \frac{1}{2}\varepsilon_{\mu\nu\rho\sigma}G^{\rho\sigma}$ its dual (and similarly for QED, $\tilde{F}_{\mu\nu} = \frac{1}{2}\varepsilon_{\mu\nu\rho\sigma}F^{\rho\sigma}$), and $a = 1, \dots, 8$ the adjoint color indices. The fermion label, $f = u, d, s, e, \mu$, denotes the light quarks, electrons or muons, while $(\bar{\nu}i\overset{\leftrightarrow}{\partial}_\mu\nu) = (\bar{\nu}i\partial_\mu\nu) - (\bar{\nu}i\overset{\leftarrow}{\partial}_\mu\nu)$. We assume flavor conservation for charged fermions, while we do allow changes of neutrino flavor.

For Dirac neutrinos the dimension 5 and dimension 7 operators, Eq. (3) and Eqs. (5)-(10), have a chirality flipping neutrino current. An incoming left-handed neutrino of flavor ν_α is converted to a right-handed neutrino of flavor ν_β . In contrast, the dimension 6 operators, Eq. (4), preserve the chirality of the incoming neutrino. For Dirac neutrinos there are then two additional dimension 6 operators, $\mathcal{Q}_{1,q}^{(6)'}$, $\mathcal{Q}_{2,q}^{(6)'}$, obtained from (4) through $P_L \rightarrow P_R$ replacements. These operators cannot be well tested in neutrino experiments, since the production of right-handed neutrinos through SM weak interactions is neutrino mass suppressed. We therefore do not consider the operators $\mathcal{Q}_{1,q}^{(6)'}$, $\mathcal{Q}_{2,q}^{(6)'}$ further in our analysis.

In the case of Majorana neutrinos the dimension 5 and dimension 7 operators, Eq. (3) and Eqs. (5)-(8), violate lepton number by two units (note that we use the conventions of Ref. [38] also for Majorana neutrinos). Furthermore, for a Majorana neutrino the operators $\mathcal{Q}_1^{(5)}$ in (3), $\mathcal{Q}_{7,f}^{(7)}$ in (8), and $\mathcal{Q}_{10,f}^{(7)}$, $\mathcal{Q}_{11,f}^{(7)}$ in (10) vanish identically for $\alpha = \beta$, and thus only mediate flavor changing transitions. Finally, for $\alpha = \beta$ we include in the definitions of the operators an extra factor of 1/2 to compensate for the additional Wick contraction so that our results for cross sections and the bounds on Wilson coefficients can be used without change (cf. App A of Ref. [39] for explicit normalization of such operators, albeit for DM interactions).

Note that in general the above operators are not Hermitian, and thus can have complex Wilson coefficients, $\mathcal{C}_a^{(d)}$. The exception are dimension 6 operators with $\alpha = \beta$, in which case the operators are Hermitian, and thus the corresponding Wilson coefficients are real (for these operators the “h.c.” in Eq. (2) should be dropped).

Note that the SM neutrino interactions with quarks are also described by the effective Lagrangian (2), though not all the operators are generated. The SM neutral currents (NC), i.e., due to the tree level Z exchanges, and the SM charged currents (CC), due to the tree level W exchanges, generate the operators $\mathcal{Q}_{1,f}^{(6)}$ and $\mathcal{Q}_{2,f}^{(6)}$, see Fig. 1. Integrating out the Z and W bosons gives for the Wilson coefficient relevant for neutrino scattering on matter,

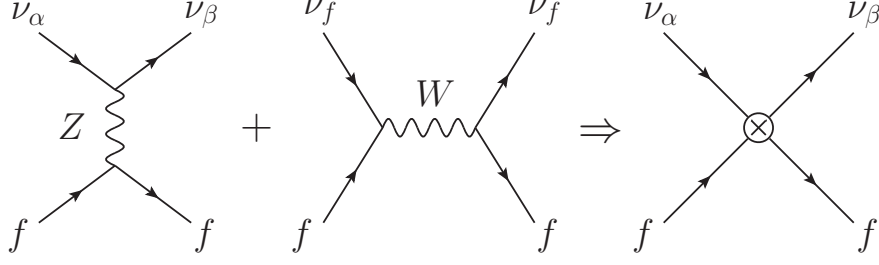


Figure 1: Integrating out the Z and W bosons at tree level NC and CC (left) generates the effective four-fermions interaction (right). The blob vertex indicates an operator insertion of $\mathcal{Q}_{1,f}^{(6)}$ and $\mathcal{Q}_{2,f}^{(6)}$.

i.e., on light quarks and electrons,

$$\hat{\mathcal{C}}_{1,u(d,s)}^{(6)}|_{\text{SM}} = \mp \frac{G_F}{\sqrt{2}} \left(1 - \frac{8(4)}{3} s_W^2 \right) \delta_{\alpha\beta}, \quad \hat{\mathcal{C}}_{2,u(d,s)}^{(6)}|_{\text{SM}} = \pm \frac{G_F}{\sqrt{2}} \delta_{\alpha\beta} \quad (11)$$

$$\hat{\mathcal{C}}_{1,e}^{(6)}|_{\text{SM}} = \frac{G_F}{\sqrt{2}} ((1 - 4s_W^2) \delta_{\alpha\beta} - 2\delta_{\alpha e} \delta_{\beta e}), \quad \hat{\mathcal{C}}_{2,e}^{(6)}|_{\text{SM}} = -\frac{G_F}{\sqrt{2}} (\delta_{\alpha\beta} - 2\delta_{\alpha e} \delta_{\beta e}), \quad (12)$$

where $s_W^2 \equiv \sin^2 \theta_W \simeq 0.2223$ with θ_W the weak mixing angle. The second terms in Eq. (12) are due to CC, cf. Fig. 1. In the presence of NSI the above SM Wilson coefficients are modified to

$$\hat{\mathcal{C}}_{1(2),f}^{(6)} = \hat{\mathcal{C}}_{1(2),f}^{(6)}|_{\text{SM}} + \hat{\mathcal{C}}_{1(2),f}^{(6)}|_{\text{NSI}}, \quad \text{with} \quad \hat{\mathcal{C}}_{1(2),f}^{(6)}|_{\text{NSI}} = \frac{G_F}{\sqrt{2}} \varepsilon_{\alpha\beta}^{fV(A)}, \quad (13)$$

where in the last equality we used the ε notation of the NSI Lagrangian, Eq. (1).

In the SM the dimension 5 and dimension 7 EFT operators, Eq. (3) and Eqs. (5)-(10), are suppressed by the neutrino masses and thus negligible for all practical purposes. In this case an appreciable Wilson coefficient would immediately signal the existence of NSI.

III. NSI AND ELASTIC SCATTERING

This section describes the nuclear response to the elastic neutrino scattering on nucleus A at low energies, $\nu A \rightarrow \nu A$, due to either the SM and/or NSI interactions. The calculation is done in several steps. In Section III A we first match onto an EFT describing neutrino interactions with non-relativistic protons and neutrons. The corresponding nuclear response to elastic neutrino scattering (CE ν NS) is given in Section III B. For ease of comparison we also give the naive dimensional analysis (NDA) estimates for CE ν NS cross sections induced by each of the EFT operators, while leaving the detailed numerical analysis for Section VI.

A. Interactions of neutrinos with nonrelativistic nucleons

The neutrons and protons inside nuclei are non-relativistic and their interactions are well described by a chiral EFT with nonrelativistic nucleons. The momentum exchange, q , in $\text{CE}\nu\text{NS}$ scattering is small so that nuclei remain intact, while neutrons and protons are non-relativistic throughout the scattering event. For instance, in the COHERENT experiment [13], the typical momentum exchange is $q \sim 30 - 70$ MeV. This is well below the cut-off of chiral EFT, $\Lambda_{\text{ChEFT}} \sim \mathcal{O}(1 \text{ GeV})$, so that the effective neutrino interactions in Eq. (2) can be included in the chiral EFT framework. We work at leading order in the chiral expansion for each of the EFT operators in (2), counting the light pseudoscalar masses to be parametrically of the order $m_\pi \sim \mathcal{O}(q)$. At leading chiral order the neutrino interacts only with a single nucleon, while interactions of a neutrino with two nucleons are suppressed by powers of q/Λ_{ChEFT} . The exception to this rule are the dimension seven Rayleigh operators, Eq. (5), which we discuss separately in Section III C.

The effective Lagrangian describing neutrino interactions with non-relativistic nucleons is given by

$$\mathcal{L}_{\text{NR}} = \sum_{i,N} c_{i,N}^{(d)}(q^2) \mathcal{O}_{i,N}^{(d)} (+\text{h.c.}), \quad (14)$$

where $N = n, p$, while d counts the number of derivatives in the operator, which gives the suppression of the operator in terms of soft momenta, $\mathcal{O}(q^d)$. The momentum exchanged, $q^\mu = (q^0, \vec{q})$, is given by,

$$q^\mu = k_2^\mu - k_1^\mu = p_1^\mu - p_2^\mu. \quad (15)$$

with $k_{1(2)}, p_{1(2)}$ the incoming(outgoing) nucleon and neutrino momenta, respectively, cf. Fig. 2. The nuclear recoil energy, $E_R = \vec{q}^2/2m_A$, can, for fixed neutrino energy, be anywhere between $E_{R,\text{min}} = 0$ for forward scattering, to a maximal value of $E_{R,\text{max}} \simeq 2E_\nu^2/m_A$ obtained in the case of neutrino back-scattering.

The matching of quark and gluon currents onto nonrelativistic nucleon currents is performed using heavy baryon chiral perturbation (HBChPT) theory [40, 41], while neutrino currents maintain their relativistic form. In this way one can explicitly show that the chirally leading interactions of neutrinos are with a single nucleon current. We write the non-relativistic operators in the Lagrangian (14) using the heavy nucleon formalism of HBChPT, where the nucleon mass is effectively integrated out. To the order we are working, the heavy

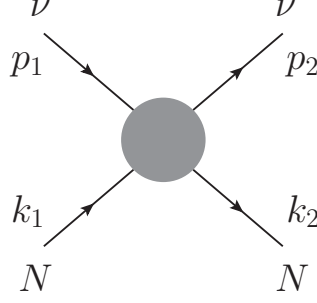


Figure 2: The kinematics of neutrino scattering on nucleons, $\nu(p_1)N(k_1) \rightarrow \nu(p_2)N(k_2)$.

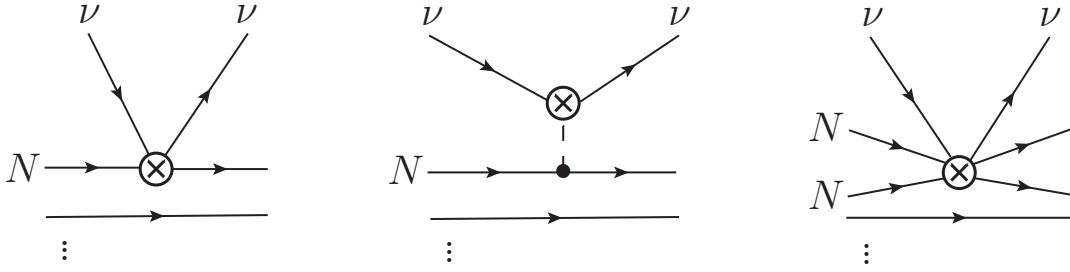


Figure 3: The chirally leading diagrams for the neutrino-nucleus scattering (the first and second diagrams), and a representative diagram for two nucleon scattering (the third diagram). The effective neutrino–nucleon and neutrino–meson interactions are denoted by a circle, the dashed line denotes a pion, and the dots represent the remaining $A - 2$ nucleon lines.

nucleon field, N_v , is given by

$$N = e^{-im_N v \cdot x} \left(1 + \frac{i \not{\partial}_\perp}{iv \cdot \partial + 2m_N - i\epsilon} \right) N_v, \quad (16)$$

where v^μ is the nucleon four-velocity, which we may take to coincide with the lab frame, $v^\mu = (1, 0, 0, 0)$, while $\partial_\perp^\mu = \partial^\mu - v^\mu v \cdot \partial$ is the soft momentum. The momentum due to the heavy nucleon mass, $m_N v^\mu$, has been factored out from the definition of N_v by the exponential prefactor.

The nonrelativistic operators in (14) are, for proton and with $d = 0$,

$$\mathcal{O}_{1,p}^{(0)} = (\bar{\nu}_\beta \gamma_\mu P_L \nu_\alpha) (v^\mu \bar{p}_v p_v), \quad \mathcal{O}_{2,p}^{(0)} = (\bar{\nu}_\beta \gamma_\mu P_L \nu_\alpha) (\bar{p}_v S_N^\mu p_v), \quad (17)$$

$$\mathcal{O}_{3,p}^{(0)} = (\bar{\nu}_\beta P_L \nu_\alpha) (\bar{p}_v p_v), \quad \mathcal{O}_{4,p}^{(0)} = (\bar{\nu}_\beta \sigma_{\mu\nu} P_L \nu_\alpha) (\bar{p}_v \sigma_\perp^{\mu\nu} p_v), \quad (18)$$

and a similar set of operators for neutrons with $p \rightarrow n$. Here we have defined $\gamma_\perp^\mu = \gamma^\mu - v^\mu \not{v}$, $\sigma_\perp^{\mu\nu} = \frac{i}{2} [\gamma_\perp^\mu, \gamma_\perp^\nu]$ and the spin operator $S_N^\mu = \gamma_5 \gamma_\perp^\mu / 2$. There are two relevant operators with

a single derivative, $d = 1$,

$$\mathcal{O}_{1,p}^{(1)} = (\bar{\nu}_\beta P_L \nu_\alpha) \left(\bar{p}_v \frac{i q \cdot S_N}{m_N} p_v \right), \quad \mathcal{O}_{2,p}^{(1)} = (\bar{\nu}_\beta P_L \nu_\alpha) \left(\bar{p}_v \frac{p_{12} \cdot S_N}{m_N} p_v \right), \quad (19)$$

and one relevant $d = 2$ operator,

$$\mathcal{O}_{1,p}^{(2)} = \frac{i q_\mu p_{12,\nu}}{m_N^2} (\bar{\nu} P_L \nu) (\bar{p}_v \sigma_\perp^{\mu\nu} p_v), \quad (20)$$

where $p_{12}^\nu = p_1^\nu + p_2^\nu$. We work in the isospin limit in which the proton and neutron masses are equal, so that $m_N = m_p = m_n \simeq 939$ MeV. Above, the nucleon operators with $\sigma_\perp^{\mu\nu}$ are related to the nucleon spin through

$$\bar{N}_v \sigma_\perp^{\mu\nu} N_v = -2\epsilon^{\mu\nu\alpha\beta} v_\alpha (\bar{N}_v S_{N,\beta} N_v), \quad (21)$$

where $\epsilon^{\mu\nu\alpha\beta}$ is the totally antisymmetric Levi-Civita tensor, with $\epsilon^{0123} = 1$. In (14) the Hermitian conjugation is present in the sum for almost all the operators – the exception are $\mathcal{O}_{1,p}^{(0)}, \mathcal{O}_{2,p}^{(0)}$ for $\alpha = \beta$, in which case the two operators are already Hermitian. The coefficients of these operators are thus real, while for the other operators they can be complex in general.

The nonrelativistic coefficients in (14) are (summations are over $q = u, d, s$),

$$c_{1,p}^{(0)} = \sum_q F_1^{q/p} \hat{\mathcal{C}}_{1,q}^{(6)}, \quad (22)$$

$$c_{2,p}^{(0)} = 2 \sum_q F_A^{q/p} \hat{\mathcal{C}}_{2,q}^{(6)}, \quad (23)$$

$$c_{3,p}^{(0)} = F_G^p \hat{\mathcal{C}}_3^{(7)} + \sum_q \left(-Q_q \frac{e^2}{4\pi^2} \frac{2\bar{E}_\nu}{q^2} F_1^{q/p} \hat{\mathcal{C}}_1^{(5)} + F_S^{q/p} \hat{\mathcal{C}}_{5,q}^{(7)} + 2\bar{E}_\nu F_1^{q/p} (\hat{\mathcal{C}}_{8,q}^{(7)} + \hat{\mathcal{C}}_{10,q}^{(7)}) \right), \quad (24)$$

$$c_{4,p}^{(0)} = \sum_q F_{T,0}^{q/p} \hat{\mathcal{C}}_{7,q}^{(7)} \quad (25)$$

$$c_{1,p}^{(1)} = F_{\tilde{G}}^p \hat{\mathcal{C}}_4^{(7)} + \sum_q F_P^{q/p} \hat{\mathcal{C}}_{6,q}^{(7)}, \quad (26)$$

$$c_{2,p}^{(1)} = \sum_q 2m_N F_A^{q/p} (\hat{\mathcal{C}}_{9,q}^{(7)} + \hat{\mathcal{C}}_{11,q}^{(7)}), \quad (27)$$

$$c_{1,p}^{(2)} = \sum_q Q_q \frac{e^2}{4\pi^2} \frac{m_N}{2q^2} F_2^{q/p} \hat{\mathcal{C}}_1^{(5)}, \quad (28)$$

where $\bar{E}_\nu = (p_1 + p_2) \cdot v/2$ is the average energy of the neutrino before and after scattering. In COHERENT experiment the incoming neutrinos have energy ~ 16 -53 MeV, so that $\bar{E}_\nu \sim \mathcal{O}(q) \lesssim \mathcal{O}(m_\pi)$. The coefficients for neutrons are obtained through $p \rightarrow n$ replacement. The

form factors, F_i , describe the hadronization of quark and gluon currents. They are functions of $q^2 = -\vec{q}^2$ only, and their definitions are given in appendix A.

In order to derive the above expressions for the nonrelativistic coefficients in Eqs. (22)-(28) we used the non-relativistic reduction of the nucleon currents summarized in appendix A. We keep only the leading terms in the q/m_N expansion for each of the non-standard neutrino interaction operators, Eqs. (3)-(10). The leading contributions start at different orders in q expansion, depending on the structure of the NSI operators. For instance, the operators $Q_4^{(7)}, Q_{6,q}^{(7)}, Q_{9,q}^{(7)}$, and $Q_{11,q}^{(7)}$, all match onto non-relativistic operators with one derivative, and thus their contributions to the scattering amplitude start only at $\mathcal{O}(q)$. All the other operators have contributions already at $\mathcal{O}(q^0)$.

There are two specific exceptions, where these leading contributions naturally vanish. For the QED dipole operator, $Q_1^{(5)}$, the leading scattering on neutrons comes from operators with two derivatives. This is despite the $Q_1^{(5)}$ also contributing to the $\mathcal{O}(q^0)$ nonrelativistic operator, see Eq. (24). The reason is that for the neutron $\sum_q Q_q F_1^{q/N}(0) = 0$, so that in this case the contribution to (24) vanishes. Similarly, the absence of valence strange quarks in nucleons gives $F_1^{s/N}(0) = 0$, so that we need to keep the form factor $F_1^{s/N}(q^2)$ expanded to quadratic order. Note as well, that the contributions from the axial current form factor $F_{P'}(q^2)$ are proportional to the neutrino masses and thus neglected, even though $F_{P'}(q^2)$ is $1/m_\pi^2$ enhanced due to the pion pole, corresponding to the middle diagram in Fig. 3.

In summary, in Eqs. (22)-(28) most of the form factors are to be evaluated at $q^2 \rightarrow 0$,

$$F_i^{q/N}(q^2) = F_i^{q/N}(0) + \dots, \quad (29)$$

since this gives the chirally leading contribution, and we neglect the q^2/m_N^2 suppressed contributions, denoted above with the ellipsis. The three exceptions are the form factors $F_P^{q/N}$, $F_{\tilde{G}}^{q/N}$, and $F_1^{q/N}$ where we keep the q^2 dependence. The chirally leading contributions to $F_P^{q/N}$ and $F_{\tilde{G}}^{q/N}$ have pion and η pole contributions (corresponding to the second diagram in Fig. 3),

$$F_P^{q/N}(q^2) = \frac{m_N^2}{m_\pi^2 - q^2} a_{P,\pi}^{q/N} + \frac{m_N^2}{m_\eta^2 - q^2} a_{P,\eta}^{q/N} + \dots, \quad (30)$$

$$F_{\tilde{G}}^N(q^2) = \frac{q^2}{m_\pi^2 - q^2} a_{\tilde{G},\pi}^N + \frac{q^2}{m_\eta^2 - q^2} a_{\tilde{G},\eta}^N + b_{\tilde{G}}^N + \dots, \quad (31)$$

while for the vector form factor of the neutron we need to go to $\mathcal{O}(q^2)$,

$$F_1^{q/N}(q^2) = F_1^{q/N}(0) + F_1^{q/N'}(0)q^2 + \dots, \quad (32)$$

since for the strange quark $F_1^{s/N}(0) = 0$. For simplicity we keep quadratic orders in $F_1^{q/N}(q^2)$ also for $q = u, d$.³ The input values of the nonperturbative parameters are given in [42].

B. Nuclear response to nonstandard neutrino interactions

The NSI coupling neutrinos to nonrelativistic nucleon currents, Eq. (14), are of two types – the neutrinos either couple to the nucleon number operator, $\bar{N}_v N_v$, or to the nuclear spin, $\bar{N}_v S_N^\mu N_v$. In the notation of Ref. [43] the effective Lagrangian is

$$\mathcal{L}_{\text{NR}} = (\bar{\nu} l_0 P_L \nu) 1_N + 2(\bar{\nu} \vec{l}_5 P_L \nu) \cdot \vec{S}_N + \dots, \quad (33)$$

where the ellipsis denote terms with $P_R \nu$, irrelevant for our case where the incoming flux is due to left-handed neutrinos.⁴ The two Dirac structures are,

$$l_0 = c_{1,N}^{(0)} \not{v} + c_{3,N}^{(0)}, \quad (34)$$

$$l_5^\mu = -\frac{1}{2} c_{2,N}^{(0)} \gamma^\mu - c_{4,N}^{(0)} \epsilon^{\mu\nu\alpha\beta} v_\nu \sigma_{\alpha\beta} - \frac{i q^\mu}{2m_N} c_{1,N}^{(1)} - \frac{i p_{12}^\mu}{2m_N} c_{2,N}^{(1)} - \epsilon^{\mu\nu\alpha\beta} v_\nu \frac{i q_\alpha p_{12,\beta}}{m_N^2} c_{1,N}^{(2)}. \quad (35)$$

Note that only the spatial three-vector components of l_5^μ enter the leading order nonrelativistic Lagrangian, (33). The EFT counting is such that all components of neutrino momenta count as the neutrino energy, E_ν , while the nucleon currents are expanded in q/m_N , as discussed in the previous subsection. The results for the $c_{i,N}^{(d)}$ coefficients, that are in general functions of q^2 , are given in (22)-(28).

The cross sections for the neutrino–nucleus scattering is

$$\frac{d\sigma_A}{dE_R} = 2m_A \frac{d\sigma_A}{d\vec{q}^2} = \frac{m_A}{\pi E_\nu^2} \overline{\mathcal{M}^2}, \quad (36)$$

where E_R is the recoil energy of the nucleus and the averaged amplitude square is given by [44],

$$\overline{\mathcal{M}^2} = \frac{1}{2J_A + 1} \sum_{\text{spins}} |\mathcal{M}|^2 = \frac{4\pi}{2J_A + 1} \sum_{\tau, \tau'=0,1} \left(R_M^{\tau\tau'} W_M^{\tau\tau'} + R_{\Sigma'}^{\tau\tau'} W_{\Sigma'}^{\tau\tau'} + R_{\Sigma'}^{\tau\tau'} W_{\Sigma'}^{\tau\tau'} \right), \quad (37)$$

³ Incidentally, in this way we also capture the first nonzero term in $c_{3,n}^{(0)}$ from $\hat{\mathcal{C}}_1^{(5)}$ for scattering on neutrons, cf. Eq. (24). In that case the leading term in $c_{3,n}^{(0)}$ from $\hat{\mathcal{C}}_1^{(5)}$ cancels because neutron has zero electric charge. Note that the leading contribution from $\hat{\mathcal{C}}_1^{(5)}$ for neutrino scattering on neutrons is described by $c_{1,n}^{(2)}$, Eq. (28), while the contribution from $c_{3,n}^{(0)}$ is relatively $\mathcal{O}(q)$ suppressed.

⁴ A contribution to CE ν NS from right-handed neutrinos in the incoming flux requires two insertions of NSI interactions, one in the production and one in the scattering on nucleus, and is thus of second order in small perturbations.

where J_A is the spin of the target nucleus, the $W_{M,\Sigma',\Sigma''}(q)$ are the nuclear response functions and $\hat{q} \equiv \vec{q}/q$. The sum is over the isospin, $\tau, \tau' = 0, 1$, with the kinematic factors

$$R_M^{\tau\tau'} = \text{Tr} (P_L \not{p}_1 l_{0,\tau'}^\dagger \not{p}_2 l_{0,\tau}), \quad (38)$$

$$R_{\Sigma''}^{\tau\tau'} = \text{Tr} (P_L \not{p}_1 l_{5,\tau'}^\dagger \not{p}_2 l_{5,\tau}^i \hat{q}^i \hat{q}^j), \quad (39)$$

$$R_{\Sigma'}^{\tau\tau'} = \text{Tr} (P_L \not{p}_1 l_{5,\tau'}^\dagger \not{p}_2 l_{5,\tau}^i) (\delta^{ij} - \hat{q}^i \hat{q}^j), \quad (40)$$

where the summations over spatial indices, $i, j = 1, 2, 3$, are implied. In the evaluation of the kinematic factors we only keep the leading terms in E_R/E_ν and $E_\nu/m_N, q/m_N$, which gives (note that $E_R = \vec{q}^2/(2m_A)$)

$$R_M^{\tau\tau'} = (4E_\nu^2 - \vec{q}^2) c_{1,\tau}^{(0)} c_{1,\tau'}^{(0)*} + \vec{q}^2 c_{3,\tau}^{(0)} c_{3,\tau'}^{(0)*}, \quad (41)$$

$$\begin{aligned} R_{\Sigma''}^{\tau\tau'} = & \frac{\vec{q}^4}{4m_N^2} c_{1,\tau}^{(1)} c_{1,\tau'}^{(1)*} + \frac{E_\nu^2 \vec{q}^4}{4m_A^2 m_N^2} c_{2,\tau}^{(1)} c_{2,\tau'}^{(1)*} + \frac{\vec{q}^2}{16m_A^2} (4E_\nu^2 - \vec{q}^2) c_{2,\tau}^{(0)} c_{2,\tau'}^{(0)*} + 16E_\nu^2 c_{4,\tau}^{(0)} c_{4,\tau'}^{(0)*} \\ & + 2i \frac{E_\nu}{m_N} \vec{q}^2 (c_{1,\tau}^{(1)} c_{4,\tau'}^{(0)*} - c_{4,\tau}^{(0)} c_{1,\tau'}^{(1)*}) + 2i \frac{E_\nu^2 \vec{q}^2}{m_A m_N} (c_{2,\tau}^{(1)} c_{4,\tau'}^{(0)*} - c_{4,\tau}^{(0)} c_{2,\tau'}^{(1)*}) \\ & + \frac{E_\nu \vec{q}^4}{4m_A m_N^2} (c_{1,\tau}^{(1)} c_{2,\tau'}^{(1)*} + c_{1,\tau}^{(1)} c_{2,\tau'}^{(1)*}), \end{aligned} \quad (42)$$

$$\begin{aligned} R_{\Sigma'}^{\tau\tau'} = & \frac{1}{4} (4E_\nu^2 + \vec{q}^2) c_{2,\tau}^{(0)} c_{2,\tau'}^{(0)*} + (4E_\nu^2 - \vec{q}^2) \left(4c_{4,\tau}^{(0)} c_{4,\tau'}^{(0)*} + \frac{\vec{q}^4}{m_N^4} c_{1,\tau}^{(2)} c_{1,\tau'}^{(2)*} \right) \\ & - 2(4E_\nu^2 - \vec{q}^2) \frac{\vec{q}^2}{m_N^2} (c_{1,\tau}^{(2)} c_{4,\tau'}^{(0)*} + c_{4,\tau}^{(0)} c_{1,\tau'}^{(2)*}) \\ & + \frac{(4E_\nu^2 - \vec{q}^2) \vec{q}^2}{4m_N^2} \left(c_{2,\tau}^{(1)} c_{2,\tau'}^{(1)*} - 2i \frac{m_N}{m_A} (c_{2,\tau}^{(1)} c_{4,\tau'}^{(0)*} - c_{4,\tau}^{(0)} c_{2,\tau'}^{(1)*}) \right). \end{aligned} \quad (43)$$

Here $\tau, \tau' = 0, 1$ denote the isospin so that,

$$c_{i,0}^{(d)} = \frac{1}{2} (c_{i,p}^{(d)} + c_{i,n}^{(d)}), \quad c_{i,1}^{(d)} = \frac{1}{2} (c_{i,p}^{(d)} - c_{i,n}^{(d)}). \quad (44)$$

The non-relativistic coefficients describing neutrino interactions with protons and neutrons, $c_{i,p}^{(d)}$ and $c_{i,n}^{(d)}$, are listed in Eqs. (22)-(28).

Before proceeding, we give NDA estimates for the neutrino-nucleus scattering cross section (36), switching on a single NSI Wilson coefficient $\hat{C}_{1,q}^{(d)}$, Eqs. (3)-(10), at a time. Subtracting the contribution induced by the SM neutrino interactions gives the correction to the scattering cross section due to the presence of NSI,

$$\Delta\sigma_{\text{NSI}} \equiv \sigma - \sigma_{\text{SM}} \sim \mathcal{O}(R_\alpha W_\alpha). \quad (45)$$

Note that $\Delta\sigma_{\text{NSI}}$ can be negative, if NSI interfere with the SM. In the last equality in (45) we show the parametric dependence on kinematical factors and nuclear response functions, W_α , taking $E_R \sim \mathcal{O}(E_\nu^2/m_A)$. The subscript is any of $\alpha = M, \Sigma', \Sigma''$, depending on the Wilson coefficient $\hat{C}_{1,q}^{(d)}$.

In the long wavelength limit, $q \rightarrow 0$, the nuclear response functions, W_α , have the following parametric sizes,

$$W_M^{\tau\tau'} \sim \mathcal{O}(A^2), \quad W_{\Sigma'}^{\tau\tau'} \sim \mathcal{O}(1), \quad W_{\Sigma''}^{\tau\tau'} \sim \mathcal{O}(1). \quad (46)$$

The response functions $W_{\Sigma'}^{\tau\tau'}$ and $W_{\Sigma''}^{\tau\tau'}$ encode the response of nucleus to the transverse and longitudinal axial operators, and thus measure the spin content of the nucleus. The values of $W_{\Sigma',\Sigma''}^{\tau\tau'}$ depend critically on the details of the nuclear wave function and can be much smaller than (46) for nuclei with all protons and neutrons paired. The $W_M^{\tau\tau'}$ response functions count, in the long wavelength limit, the number of nucleons inside nucleus. This leads to coherent enhancement, also present for neutrino scattering through SM interaction – the tree level Z exchange, Eq. (11). The Z boson couples most strongly to neutrons, so that in the SM case the enhancement is $\mathcal{O}(N^2)$, where N is the number of neutrons in the nucleus. Depending on the flavor structure the NSI can be due to couplings to proton or neutrons or both.

The NSI operators, Eqs. (3)-(10), fall into three categories: the operators that interfere with the SM contribution, the operators that do not interfere with the SM but still lead to coherently enhanced scattering, and the operators that are not coherently enhanced. The NDA estimates of the scattering cross sections for each of the three sets of operators are as follows.

The operators that interfere with the SM contribution. These are the operators with quark vector currents, $\mathcal{Q}_{1,q}^{(6)}$ in (4). The SM contribution to the corresponding Wilson coefficient is given in Eq. (11). The NDA estimate of the NSI correction to the scattering cross section is

$$\Delta\sigma_{\text{NSI}} \sim \frac{E_\nu^2}{\Lambda^2} (\hat{C}_{1,q}^{(6)})_{\text{SM}} (C_{1,q}^{(6)})_{\text{NSI}} A^2, \quad (47)$$

where we used that the interference with the SM dominates over the purely NP contribution.

Coherently enhanced but no interference with the SM. The operators that lead to coherently enhanced scattering, but do not interfere with the SM contribution, are the ones that contribute to $c_{3,N}^{(0)}$ nonrelativistic coefficients. These are the dimension 5 magnetic dipole

operator, $\mathcal{Q}_1^{(5)}$, Eq. (3), and the set of dimension 7 operators, the $\mathcal{Q}_3^{(7)}$ operator in (6) that couples the neutrino current to gluons, the operator $\mathcal{Q}_{5,q}^{(7)}$ in (7) that couples neutrino and quark scalar currents, and the operators $\mathcal{Q}_{8,q}^{(7)}$, $\mathcal{Q}_{10,q}^{(7)}$ in Eqs. (9), (10) that involve derivatives on the neutrino currents. The corresponding modification of the scattering cross section is parametrically,

$$\Delta\sigma_{\text{NSI}} \sim \frac{E_\nu^2}{\Lambda^4} \left[\frac{m_N}{\Lambda} \left(\mathcal{C}_3^{(7)} + \mathcal{O}(0.05)\mathcal{C}_{5,q}^{(7)} \right) + \frac{E_\nu}{\Lambda} \left(\mathcal{C}_{8,q}^{(7)} + \mathcal{C}_{10,q}^{(7)} \right) + \frac{\alpha_{\text{EM}}}{4\pi} \frac{\Lambda}{E_\nu} \mathcal{C}_1^{(5)} \right]^2 A^2. \quad (48)$$

Here we counted $q \sim \mathcal{O}(E_\nu)$, and only show the parametric dependence, neglecting $\mathcal{O}(1)$ factors. All the Wilson coefficients are due to NP. Above we thus dropped the NSI subscripts on the Wilson coefficients.

No coherent enhancement. The remaining operators do not receive coherent enhancement. The correction to the neutrino scattering cross section is then parametrically given by

$$\Delta\sigma_{\text{NSI}} \sim \frac{E_\nu^2}{\Lambda^2} (\hat{C}_{2,q}^{(6)})_{\text{SM}} (C_{2,q}^{(6)})_{\text{NSI}} + \frac{E_\nu^4}{\Lambda^6} \left[\frac{E_\nu^2}{m_\pi^2} \mathcal{C}_4^{(7)} + \frac{m_N m_q}{m_\pi^2} \mathcal{C}_{6,q}^{(7)} + \frac{m_q}{E_\nu} \mathcal{C}_{7,q}^{(7)} \right]^2. \quad (49)$$

To shorten the expression we did not include additional numerical suppressions present for the case of strange quarks.

C. Scattering from Rayleigh operators

Finally, we include the estimates for the CE ν NS induced by the Rayleigh operators, $\mathcal{Q}_1^{(7)}$ and $\mathcal{Q}_2^{(7)}$ in (5). The CP even Rayleigh operator $\mathcal{Q}_1^{(7)}$ leads to a coherently enhanced cross section, given by Eq. (36) with the following matrix element squared [45] (for earlier work see [46, 47])

$$\begin{aligned} \overline{\mathcal{M}}^2 = \frac{4\pi}{2J_A + 1} \vec{q}^2 |\hat{C}_1^{(7)}|^2 & \left(\frac{\sqrt{2}}{6} \frac{\alpha^2}{\pi^{3/2}} Z(Z-1) Q_0 \bar{F}_{pp}(q) \right. \\ & \left. + \frac{1}{3} \left(\frac{\alpha}{4\pi} \right)^2 m_N \sqrt{\sum_{\tau, \tau'=0,1} a_{F,\tau}^{(0)} a_{F,\tau'}^{(0)*} W_M^{\tau\tau'}} \right)^2. \end{aligned} \quad (50)$$

The first term is due to a contribution from two-body currents, calculated in Ref. [45], where the two photon lines attach to two different protons in the nucleus, while the second contribution is due to both photon lines attaching to the same proton. The two contributions to the cross section scale as $\sigma \propto \mathcal{O}(Z^4 Q_0^2/m_N^2)$ and $\sigma \propto \mathcal{O}(Z^2)$, respectively (not showing

the common factors and interference terms). For $Q_0/m_N \sim 0.1$ the two contributions are parametrically of the same size for light nuclei $Z \sim \mathcal{O}(10)$, while the first term dominates for heavy nuclei, $Z \sim \mathcal{O}(50)$.

For the 2-proton form factor we use the phenomenological ansatz from Ref. [45],

$$\bar{F}_{pp}(q) = e^{-\bar{q}^2/2} \left[1 + \frac{1}{4}c_1 - \frac{\pi^{3/2}}{2\sqrt{2}}\bar{q} + \left(\frac{5}{3} - \frac{5}{12}c_1 + c_2 \right) \bar{q}^2 \right], \quad (51)$$

with $\bar{q} = |\vec{q}|/Q_0$ and $Q_0 = (0.5 \text{ GeV}) \times (0.3 + 0.9A^{1/3})^{-1}$ the inverse of the charge radius of the target nucleus. In the numerics we set the unknown coefficients to $c_{1,2} = 1$, while varying them in the range $c_{1,2} \in [-1, 1]$ does not change results appreciably.

The single nucleon matrix elements of the di-photon operators are not well known. We parametrize them as

$$\langle N_v | F_{\mu\nu} F^{\mu\nu} | N_v \rangle = \frac{\alpha}{4\pi} a_{F,N}^{(0)} m_N \langle N_v | \bar{N}_v N_v | N_v \rangle, \quad (52)$$

$$\langle N_v | F_{\mu\nu} \tilde{F}^{\mu\nu} | N_v \rangle = \frac{\alpha}{4\pi} a_{\tilde{F},N}^{(1)} \langle N_v | \bar{N}_v \frac{i\vec{q} \cdot \vec{S}_N}{m_N} N_v | N_v \rangle, \quad (53)$$

with $a_{3,N}^{(0)}(q^2)$ and $a_{1,N}^{(1)}(q^2)$ the form factors. The NDA estimates for their values are, for $q^2 \sim 0$,

$$a_{F,p}^{(0)} \sim \mathcal{O}(1), \quad a_{F,n}^{(0)} \sim 0, \quad \text{and} \quad a_{\tilde{F},p}^{(1)} \sim a_{\tilde{F},n}^{(1)} \sim \mathcal{O}(1). \quad (54)$$

With these definitions the contributions to neutrino scattering due to two photon exchanges with a single nucleon are obtained by setting the coefficient of the $\mathcal{O}_{3,N}^{(0)}$ operator to $c_{3,N}^{(0)} = a_{F,N}^{(0)} m_N \alpha^2 / (48\pi^2)$ for contributions from the $\mathcal{Q}_1^{(7)}$ operator, while for the CP-odd Rayleigh operator, $\mathcal{Q}_2^{(7)}$, one can set the coefficient of the $\mathcal{O}_{1,N}^{(1)}$ non-relativistic operator to $c_{1,N}^{(1)} = a_{\tilde{F},N}^{(1)} \alpha^2 / (32\pi^2)$.

The CP odd Rayleigh operator leads to spin-dependent interactions, both from the single nucleon matrix element, (53), as well as from the 2 nucleon contributions. The two nucleon contributions arise from one photon interacting with the proton charge, and the second photon with the magnetic moment of the other nucleon, be it proton or neutron. The single nucleon and two nucleon contributions to the cross section are parametrically $\sigma \propto \mathcal{O}((q/m_N)^2)$ and $\sigma \propto \mathcal{O}((ZqQ_0/m_N^2)^2)$ (not showing the common factors and interference terms). The two-body current contribution is thus expected to dominate for heavy nuclei, $Z \sim 50$, while for light nuclei, $Z \sim 10$ the single current contributions are important. The formalism for the two-body current contribution was worked out in [45], however, without

deriving estimates for the resulting form factor. In the phenomenological analysis we thus conservatively ignore the 2-nucleon term and take as nonzero only the $a_{\tilde{F},N}^{(1)}$ coefficient, using the NDA estimate in (54). While this estimate for the cross section does not capture the largest contribution for heavy nuclei, where the NDA suggest the cross section to be $\sim (ZQ_0/m_N)^2 \sim 20$ times bigger for $Z \sim 50$, the resulting error on bounds on Λ will be only $\sim (ZQ_0/m_N)^{2/3} \sim 3$, which suffices in view of other uncertainties in our estimates for this particular operator.

IV. NSI AND NEUTRINO OSCILLATIONS IN MATTER

Neutrino oscillation data bound a subset of NSI – the ones that result in a nonzero forward scattering amplitude. The forward scattering of neutrinos on electrons and nuclei gives rise to matter effects in neutrino oscillations, described by an effective potential [48]. In this section we review the simplest case – electrically neutral unpolarized medium at rest. For extension to a polarized medium see [6], while for extensions to sterile neutrinos see, e.g., [49–51].

In the SM the effective potential receives contributions from both CC and NC. The NC contribution is neutrino flavor universal. It induces an overall phase shift in neutrino oscillation that is not observable (though it needs to be considered for oscillations into sterile neutrinos). The CC contributes to forward scattering of electron neutrinos on electrons. Electron neutrino scattering on an isotropic, homogeneous gas of unpolarized electrons is therefore described by the following effective Hamiltonian, see, e.g., [48],

$$\overline{\mathcal{H}}_{\text{eff}}^{\text{CC}} \Big|_{\text{SM}} = \sqrt{2}G_F n_e (\bar{\nu}_{eL} \gamma^0 \nu_{eL}), \quad (55)$$

where n_e is the number density of electrons. The resulting potential energy,

$$\mathcal{V}_{\text{eff}}^{(h)} = \langle \nu_\alpha(p, h) | \int_V d^3x \overline{\mathcal{H}}_{\text{eff}}^{\text{CC}} | \nu_\alpha(p, h) \rangle = \sqrt{2}G_F n_e \frac{(E_\nu - h|\vec{p}|)}{2E_\nu} \delta_{\alpha e}, \quad (56)$$

leads to a change in the oscillation frequency for electron neutrinos. Here p is the neutrino momentum, α its flavor and h its helicity. The integral is performed over a finite volume V which is also included in the normalization of the states, $|\nu_\alpha(p, h)\rangle = (2E_\nu V)^{-1/2} a^{(h)\dagger}(p)|0\rangle$, and thus drops out in the final result. Since weak interactions couple to left-handed fields, the $h = -1$ ultrarelativistic neutrinos obtain the effective potential energy

$$\mathcal{V}_{\text{eff}}^{(-)} \simeq \sqrt{2}G_F n_e \delta_{\alpha e}, \quad (57)$$

while the positive helicity, $h = +1$, neutrinos are exposed to a negligible effective potential, $\mathcal{V}_{\text{eff}}^{(+)} \sim \mathcal{O}(m_\nu^2/E)$.

The above SM results are readily extended to NSI that couple neutrinos to the charged fermion vector current, i.e., the operators $\mathcal{Q}_{1,f}^{(6)}$ in Eq. (4). These lead to nonzero forward scattering amplitudes and thus induce an effective potential (the dependence on neutrino flavors is implicit)

$$\mathcal{V}_{\text{eff}}^{(-)} \Big|_{\text{NSI}} \simeq -\hat{\mathcal{C}}_{1,e}^{(6)} \Big|_{\text{NSI}} n_e - \left(\hat{\mathcal{C}}_{1,u}^{(6)} \Big|_{\text{NSI}} + 2\hat{\mathcal{C}}_{1,d}^{(6)} \Big|_{\text{NSI}} \right) n_n - \left(2\hat{\mathcal{C}}_{1,u}^{(6)} \Big|_{\text{NSI}} + \hat{\mathcal{C}}_{1,d}^{(6)} \Big|_{\text{NSI}} \right) n_p. \quad (58)$$

Here $n_p = n_e$ is the number density of protons, equal to the number density of electrons in an electrically neutral medium, and n_n the number density of neutrons. The global fits to neutrino oscillation data then lead to severe bounds on the parameters $\epsilon_{\alpha\beta}$ (see Section VI).

The other NSI operators are poorly constrained from neutrino oscillations. This is most easily seen by analyzing the effects of NSI using the nonrelativistic basis, Eqs. (17)-(20). The matrix elements of spin-dependent operators, $\mathcal{O}_{2,p}^{(0)}, \mathcal{O}_{4,p}^{(0)}, \mathcal{O}_{1,p}^{(1)}, \mathcal{O}_{2,p}^{(1)}, \mathcal{O}_{1,p}^{(2)}$, vanish for unpolarized medium, and thus are not bounded by global fits of neutrino oscillations. The two sets of operators that have non-vanishing forward scattering elements are the operators $\mathcal{O}_{1,N}^{(0)}$ and $\mathcal{O}_{3,N}^{(0)}$. The $\mathcal{O}_{1,N}^{(0)}$ leads to the effective potential in (58), while the operator $\mathcal{O}_{3,N}^{(0)}$ results in an effective Hamiltonian

$$\overline{\mathcal{H}}_{\text{eff}} \supset -c_{3,N}^{(0)} n_N (\bar{\nu}_{\alpha R} \nu_{\beta L}), \quad (59)$$

where n_N is the nucleon number density. This gives the effective potential that is suppressed by the neutrino mass matrix, $\mathcal{V}_{\text{eff}}^{(h)} \simeq -c_{3,N}^{(0)} n_N m_N (m_\nu)_{\alpha\beta}$, and thus gives only extremely weak constraints on NSI.

V. NSI AND DEEP INELASTIC SCATTERING

For completeness we include the bounds on NSI that arise from deep inelastic neutrino–nucleon scattering (DIS). While the DIS data were obtained at much higher momenta exchanges, $q \sim \mathcal{O}(10 \text{ GeV})$, the constraints are severe enough that the EFT description may still be valid at least in parts of the parameter space. Throughout this section we thus assume that the EFT Lagrangian in Eq. (2) is valid also for DIS. We comment on the validity of this assumption in Section VI where we confront predictions with data.

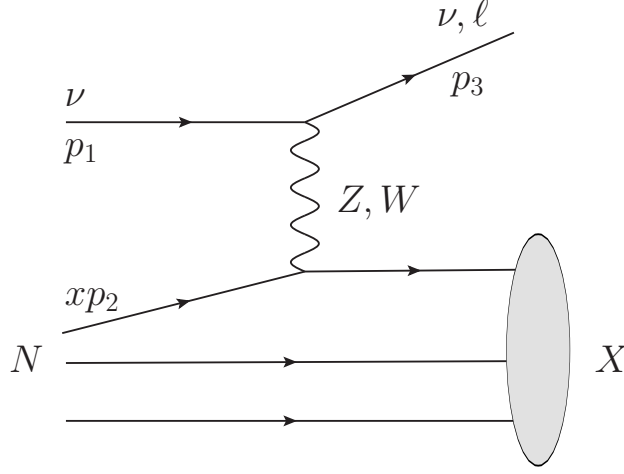


Figure 4: Kinematics in neutrino Deep Inelastic Scattering (DIS).

In neutrino–nucleus DIS the typical momentum exchange, q , is much larger than the inverse radius of the nucleus. The total cross section is therefore an incoherent sum of contributions from neutrino scattering on protons and neutrons inside the nucleus,

$$\sigma_\nu = Z\sigma_{\nu p} + (A - Z)\sigma_{\nu n}, \quad (60)$$

where

$$\sigma_{\nu N} = \int_0^1 dx \sum_j \hat{\sigma}_{\nu j}(x) f_{j/N}(x) + \dots, \quad N = n, p. \quad (61)$$

The ellipses indicate power suppressed corrections to the factorization [52]. The sum runs over the partons, $j = u, d, s, c, g, \gamma$, with $f_{j/N}(x)$ the corresponding parton distribution functions (PDF) for the nucleon N .

The kinematics of the process are shown in Fig. 4, with $p_1(p_3)$ the incoming neutrino (outgoing lepton) momentum, p_2 the incoming nucleon momentum a fraction x of which is carried by the parton, and we sum over the hadronic final state, X . We work in the limit of large neutrino energy, E_ν , and large momentum exchanged, q^2 , i.e., $E_\nu \gg m_N$ and $q^2 \gg m_N^2$. The usual DIS variables, the partonic center of mass energy squared, $\hat{s}$, and the fraction, y , of incident neutrino energy transferred to the hadronic system, are,

$$\hat{s} = (p_1 + xp_2)^2 \simeq 2xm_N E_\nu, \quad y = 1 - \frac{E'_{\nu(\ell)}}{E_\nu}, \quad (62)$$

where $E'_{\nu(\ell)}$ is the out-going neutrino (lepton) energy.

The double-differential neutrino–nucleon DIS cross section is,

$$\frac{d^2\sigma_{\nu N}}{dxdy} = \sum_j \frac{|\mathcal{M}_{\nu j}|^2}{16\pi xs} f_{j/N}(x), \quad (63)$$

where $\hat{s} = xs$. We neglect the intrinsic charm content of the proton, take the off-diagonal CKM matrix elements to zero, while $V_{ud}, V_{cs} \rightarrow 1$. In νq and $\bar{\nu}\bar{q}$ ($\bar{\nu}q$ and $\nu\bar{q}$) scattering, the total spin of the initial state is $J = 0(1)$, so that the cross section is y independent (has $(1-y)^2$ angular dependence).

We will be interested in neutrino DIS measurements by the CHARM collaboration [53], which used the target material that is to a very good approximation isoscalar, i.e., composed of equal number of protons and neutrons. The average neutrino–nucleon scattering cross section for an isoscalar target is given by,

$$\frac{d^2\sigma_{\nu N}}{dxdy} = \frac{1}{2} \left(\frac{d^2\sigma_{\nu p}}{dxdy} + \frac{d^2\sigma_{\nu n}}{dxdy} \right). \quad (64)$$

For an isoscalar target the SM predictions for the CC neutrino–nucleon scattering, $\nu N \rightarrow \ell^- X$ and $\bar{\nu} N \rightarrow \ell^+ X$, are,

$$\left. \frac{d^2\sigma_{\nu N}^{(\text{CC})}}{dxdy} \right|_{\text{SM}} = \frac{G_F^2 m_N E_\nu}{\pi} x \left\{ u(x) + d(x) + 2s(x) + [\bar{u}(x) + \bar{d}(x)] (1-y)^2 \right\}, \quad (65)$$

$$\left. \frac{d^2\sigma_{\bar{\nu} N}^{(\text{CC})}}{dxdy} \right|_{\text{SM}} = \frac{G_F^2 m_N E_\nu}{\pi} x \left\{ \bar{u}(x) + \bar{d}(x) + 2\bar{s}(x) + [u(x) + d(x)] (1-y)^2 \right\}, \quad (66)$$

where we assumed isospin symmetry,

$$u(x) \equiv f_{u/p}(x) = f_{d/n}(x), \quad d(x) \equiv f_{d/p}(x) = f_{u/n}(x), \quad s(x) \equiv f_{s/p}(x) = f_{s/n}(x). \quad (67)$$

and similarly for antiquarks, $\bar{q}(x) \equiv f_{\bar{q}/p}(x)$. In (65), (66) we integrated out the W , and traded the m_W dependence for the Fermi constant, G_F .

The NC neutrino–nucleon scattering is, in the SM, given by,

$$\begin{aligned} \frac{d^2\sigma_{\nu N}^{(\text{NC})}}{dxdy} = \frac{m_N E_\nu}{\pi} x \Big\{ & \left(\hat{C}_{L,u}^2 + \hat{C}_{L,d}^2 \right) \sum_{q=u,d} (q(x) + \bar{q}(x) (1-y)^2) \\ & + \left(\hat{C}_{R,u}^2 + \hat{C}_{R,d}^2 \right) \sum_{q=u,d} (q(x) (1-y)^2 + \bar{q}(x)) \\ & + 2 \left[\hat{C}_{L,s}^2 (s(x) + \bar{s}(x) (1-y)^2) + \hat{C}_{R,s}^2 (s(x) (1-y)^2 + \bar{s}(x)) \right] \Big\}, \end{aligned} \quad (68)$$

where

$$\hat{C}_{R,q} = \frac{1}{\sqrt{2}} \left(\hat{C}_{1,q}^{(6)} + \hat{C}_{2,q}^{(6)} \right), \quad \hat{C}_{L,q} = \frac{1}{\sqrt{2}} \left(\hat{C}_{1,q}^{(6)} - \hat{C}_{2,q}^{(6)} \right), \quad (69)$$

with the Wilson coefficients given in (11). The antineutrino cross section is obtained by exchanging $L \leftrightarrow R$.

The NSI, Eq. (2), only affect the NC scattering cross section in (68). The matrix elements squared, Eq. (63), come from a sum of the EFT operators,

$$|\mathcal{M}_{\nu j}|^2 = \left| \sum_{i,d} \mathcal{M}_{i;\nu j}^{(d)} \right|^2 = \sum_{i,d} |\mathcal{M}_{i;\nu j}^{(d)}|^2 + \sum_{i \neq k, d, d'} 2\text{Re} \left(\mathcal{M}_{i;\nu j}^{(d)} \mathcal{M}_{k;\nu j}^{(d')*} \right), \quad (70)$$

where $\mathcal{M}_{i;\nu j}^{(d)}$ is the matrix element of the operator $\mathcal{Q}_i^{(d)}$ for neutrino scattering on parton j . The dimension six operators only interfere among themselves, since the spin average of the axial-vector Dirac structure and the scalar or tensor currents vanishes. This gives,

$$|\mathcal{M}_{\nu q}^{(6)}|^2 = 16\hat{s}^2 \left[\left(\hat{\mathcal{C}}_{1,q}^{(6)} \right)^2 (1 + (1-y)^2) + \left(\hat{\mathcal{C}}_{2,q}^{(6)} \right)^2 (1 + (1-y)^2) + 2y(2-y)\text{Re} \hat{\mathcal{C}}_{1,q}^{(6)} \hat{\mathcal{C}}_{2,q}^{(6)*} \right], \quad (71)$$

where the Wilson coefficients contain both the SM contributions and the NSI correction, cf. eq. (13). The matrix elements squared for dimension 5 and dimension 7 operators are

$$|\mathcal{M}_{1;\nu\gamma}^{(5)}|^2 = 8 \left| \frac{e}{8\pi^2} \hat{\mathcal{C}}_1^{(5)} \right|^2 \hat{s}y, \quad (72)$$

$$|\mathcal{M}_{1;\nu\gamma(3;\nu g)}^{(7)}|^2 = 16 \left| \frac{\alpha(s)}{12\pi} \hat{\mathcal{C}}_{1(3)}^{(7)} \right|^2 \hat{s}^3 y^3, \quad (73)$$

$$|\mathcal{M}_{2;\nu\gamma(4;\nu g)}^{(7)}|^2 = 16 \left| \frac{\alpha(s)}{8\pi} \hat{\mathcal{C}}_{2(4)}^{(7)} \right|^2 \hat{s}^3 y^3, \quad (74)$$

$$|\mathcal{M}_{5(6),q;\nu q}^{(7)}|^2 = 8m_q^2 \left| \hat{\mathcal{C}}_{5(6),q}^{(7)} \right|^2 \hat{s}^2 y^2, \quad (75)$$

$$|\mathcal{M}_{7,q;\nu q}^{(7)}|^2 = 64m_q^2 \left| \hat{\mathcal{C}}_{7,q}^{(7)} \right|^2 \hat{s}^2 (2(1-y)^2 + 2 - y^2), \quad (76)$$

$$|\mathcal{M}_{8(9),q;\nu q}^{(7)}|^2 = 64 \left| \hat{\mathcal{C}}_{8(9),q}^{(7)} \right|^2 \hat{s}^3 y(y-1), \quad (77)$$

$$|\mathcal{M}_{10(11),q;\nu q}^{(7)}|^2 = 32 \left| \hat{\mathcal{C}}_{10(11),q}^{(7)} \right|^2 \hat{s}^3 y(y-1). \quad (78)$$

The remaining non-zero interference terms are,

$$\text{Re} \left(\mathcal{M}_{5,q;\nu q}^{(7)} \mathcal{M}_{7,q;\nu q}^{(7)*} \right) = 16\hat{s}^2 y(y-2)m_q^2 \text{Re} \left(\hat{\mathcal{C}}_{5,q}^{(7)} \hat{\mathcal{C}}_{7,q}^{(7)} \right), \quad (79)$$

$$\text{Re} \left(\mathcal{M}_{8(9),q;\nu q}^{(7)} \mathcal{M}_{10(11),q;\nu q}^{(7)*} \right) = 64\hat{s}^3 y(y-1) \text{Re} \left(\hat{\mathcal{C}}_{8(9),q}^{(7)} \hat{\mathcal{C}}_{10(11),q}^{(7)} \right). \quad (80)$$

In order to calculate DIS cross sections, we use the **ManeParse** package [54] to get the quarks and gluon PDFs (we use the CT10 NLO pdf set), while we take the photon PDF from [55].

VI. CONSTRAINTS ON NEW NEUTRINO INTERACTIONS

Utilizing the results from Sections III-V we now derive the bounds on the NSI Wilson coefficients, Eq. (2), from neutrino oscillations, CE ν NS [13], DIS [56] and from searches for neutrino dipole moment [57]. We also explore the reach of future CE ν NS measurements in reactor experiments [58]. We restrict the analysis to interactions of ν_e and ν_μ since these are the NSI probed in CE ν NS. The results are summarized in Figs. 6 and 7.

A. Constraints on NSI from oscillations

The oscillation data constrain the NSI contributions to the operators $\mathcal{Q}_{1,f}^{(6)}$, Eq. (4). The global fits to oscillation data allow at 95% C.L. [9] (in the notation of Eq. (13))

$$-0.182 < \varepsilon_{ee}^{eV} < 0.264, \quad -0.120 < \varepsilon_{\mu\mu}^{eV} < 0.120, \quad (81)$$

$$-0.008 < \varepsilon_{ee}^{uV} < 0.618, \quad -0.111 < \varepsilon_{\mu\mu}^{uV} < 0.402, \quad (82)$$

$$-0.012 < \varepsilon_{ee}^{dV} < 0.361, \quad -0.103 < \varepsilon_{\mu\mu}^{dV} < 0.361. \quad (83)$$

There are also bounds on operators that change neutrino flavor, or involve ν_τ (for details see Ref. [9]). The oscillations do not constrain NSI couplings to strange quarks, because the corresponding forward scattering matrix elements vanish.

The above ranges on $\varepsilon_{\alpha\beta}^{fV}$ imply the following lower bounds on the NP scale, for $f = e(u, d)$, setting $\mathcal{C}_{1,f}^{(6)} = 1$ in Eq. (2),

$$\nu_e \rightarrow \nu_e : \quad \Lambda > 571 \text{ (373, 488) GeV}, \quad (84)$$

$$\nu_\mu \rightarrow \nu_\mu : \quad \Lambda > 847 \text{ (463, 488) GeV}. \quad (85)$$

B. Constraints on NSI from CE ν NS

Roughly a year ago the COHERENT collaboration measured for the first time the cross section for coherent neutrino-nucleus scattering [13] (see also data release in [59]). The target was 14.6 kg of CsI[Na], while stopped pion decays, $\pi^+ \rightarrow \nu_\mu (\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu)$, acted as a source of neutrinos. The resulting time integrated neutrino fluxes per energy interval, ϕ_{ν_i} , are well known [19],

$$\phi_{\nu_e}(E_\nu) = \mathcal{N} \frac{192 E_\nu^2}{m_\mu^3} \left(\frac{1}{2} - \frac{E_\nu}{m_\mu} \right), \quad (86)$$

$$\phi_{\bar{\nu}_\mu}(E_\nu) = \mathcal{N} \frac{64E_\nu^2}{m_\mu^3} \left(\frac{3}{4} - \frac{E_\nu}{m_\mu} \right), \quad (87)$$

$$\phi_{\nu_\mu}(E_\nu) = \mathcal{N} \delta \left(E_\nu - \frac{m_\pi^2 - m_\mu^2}{2m_\pi} \right). \quad (88)$$

Here m_π (m_μ) is the charged pion (muon) mass, E_ν the energy of the neutrino, and $\mathcal{N} = rN_{\text{POT}}/(4\pi L^2)$ the time integrated neutrino flux, for each flavor, reaching the COHERENT detector. It depends on $N_{\text{POT}} = 1.73 \times 10^{23}$, the delivered number of protons on target (POT), on $r = 0.08$, the number of neutrinos per flavor produced for each POT, and on $L = 19.3\text{m}$, the distance between the neutrino source and the detector.

The expected number of CE ν NS events for each neutrino flavor, $\alpha = \nu_e, \nu_\mu, \bar{\nu}_\mu$, is

$$\frac{dN_\alpha}{dE_R} = \sum_{N=n,p} n_N \int_{E_{\nu,\min}}^{E_{\nu,\max}} dE_\nu \phi_\alpha(E_\nu) \frac{d\sigma_A(E_\nu)}{dE_R}, \quad (89)$$

where E_R is the nuclear recoil energy, E_ν the energy of the incoming neutrino, and n_N the number of nucleons of type $N = n, p$, in the detector. The lower boundary in the integration over E_ν is given by $E_{\nu,\min} \approx \sqrt{M_A E_R/2}$, the minimal energy neutrinos need to have in order to induce nuclear recoil energy E_R . The upper integration boundary, $E_{\nu,\max}$, is given by the highest energy in the incoming neutrino flux. The ν_e and $\bar{\nu}_\mu$ are produced in muon decay and thus have the maximal energy $E_{\nu,\max} = m_\mu/2$, while ν_μ is produced in pion decay, and has $E_{\nu,\max} \approx 30$ MeV. The maximal nuclear recoil energy deposited by ν_e and $\bar{\nu}_\mu$ in the detector is thus $E_{R,\max} \simeq 47$ keV, while for ν_μ it is $E_{R,\max} \simeq 15$ keV. The differential elastic neutrino–nucleus scattering cross section, $d\sigma_A/dE_R$, is given in Eq. (36).

The prediction for the total number of CE ν NS events expected in the COHERENT experiment is obtained by integrating Eq. (89) over $E_R \in [0, 47]$ keV, convoluted with the signal acceptance fraction for COHERENT, given in Fig. S9 of [13] (which has an onset at about 4.25 keV). The experimentally allowed difference from the SM prediction then translates into bounds on the Wilson coefficients for the NSI operators, $\hat{\mathcal{C}}_a^{(d)}$, Eq. (2), using Eqs. (37), (41)-(44), and (22)-(28).

In the numerical analysis we take only a single NSI Wilson coefficient at a time to be nonzero (apart from the SM contributions, Eq. (11)). For simplicity we assume that the NSI affect either only ν_e or only ν_μ . To derive the 90 % C.L. allowed ranges for $\hat{\mathcal{C}}_a^{(d)}$ we follow

opers.	F_i	σ_{F_i}	σ_α	opers.	F_i	σ_{F_i}	σ_α
$\hat{\mathcal{C}}_1^{(5)}, \hat{\mathcal{C}}_{1,u/d}^{(6)}, \hat{\mathcal{C}}_{8,u/d;10,u/d}^{(7)}$	$F_1^{u,d/N}(0)$	0%	0.28	$\hat{\mathcal{C}}_3^{(7)}$	$F_G^N(0)$	2%	0.28
$\hat{\mathcal{C}}_{1,s}^{(6)}, \hat{\mathcal{C}}_{8,s;10,s}^{(7)}$	$F_1^{s/N}(0)$	50%	0.57	$\hat{\mathcal{C}}_4^{(7)}$	$F_{\tilde{G}}^N(q)$	20%	0.39
$\hat{\mathcal{C}}_{2,u/d}^{(6)}, \hat{\mathcal{C}}_{9,u/d;11,u/d}^{(7)}$	$F_A^{u,d/N}(0)$	3 – 7%	0.34	$\hat{\mathcal{C}}_{7,u}^{(7)}$	$F_{T,0}^{u/N}(0)$	2%	0.34
$\hat{\mathcal{C}}_{2,s}^{(6)}, \hat{\mathcal{C}}_{9,s;11,s}^{(7)}$	$F_A^{s/N}(0)$	16%	0.37	$\hat{\mathcal{C}}_{7,d}^{(7)}$	$F_{T,0}^{d/N}(0)$	4%	0.34
$\hat{\mathcal{C}}_{5,u/d}^{(7)}$	$F_S^{u,d/N}(0)$	28 – 31%	0.40	$\hat{\mathcal{C}}_{7,s}^{(7)}$	$F_{T,0}^{s/N}(0)$	270%	2.7
$\hat{\mathcal{C}}_{5,s}^{(7)}$	$F_S^{s/N}(0)$	18%	0.33	$\hat{\mathcal{C}}_{6,q}^{(7)}$	$a_{P,(\pi/\eta)}^{q/N}$	4 – 11%	0.35

Table I: Form factors uncertainties, σ_{F_i} , and the resulting relative theoretical uncertainties on CE ν NS cross sections, σ_α , for different Wilson coefficients $\hat{\mathcal{C}}_a^{(d)}$ (see the main text). Unless specified, the uncertainty is the same for all quark flavors and for both nucleons. For $F_{T,0}^{q/N}(0)$ the quark masses are fixed to $m_u = 2.3$ MeV, $m_d = 4.8$ MeV, $m_s = 95$ MeV.

the COHERENT collaboration [13, 60] and define,

$$\chi^2(\hat{\mathcal{C}}_a^{(d)}, \alpha) = \frac{\left(N_{\text{meas}} - N_{\text{th}}(\hat{\mathcal{C}}_a^{(d)})(1 + \alpha)\right)^2}{\sigma_{\text{stat}}^2} + \left(\frac{\alpha}{\sigma_\alpha}\right)^2, \quad (90)$$

where $N_{\text{meas}} = 142$ is the number of detected CE ν NS events, $\sigma_{\text{stat}} = 31$ its statistical uncertainty, and $N_{\text{th}}(\hat{\mathcal{C}}_a^{(d)})$ the number of CE ν NS events when Wilson coefficient $\hat{\mathcal{C}}_a^{(d)}$ is taken to be nonzero. The theoretical uncertainties are taken into account by marginalizing χ^2 over the parameter α . The relative theory error, σ_α , on the prediction for $N_{\text{NSI}}(\hat{\mathcal{C}}_a^{(d)})$, depends on which Wilson coefficient $\hat{\mathcal{C}}_a^{(d)}$ we consider, and is a quadratic sum of errors from: the uncertainty on signal acceptance ($\pm 5\%$), neutrino flux ($\pm 10\%$), quenching factor ($\pm 25\%$), from nuclear response functions W_i (estimated conservatively, both for scattering on I and Cs, as $\pm 10\%$ for W_M , which multiplies the $F_1^{q/N}$, F_G^N , $F_S^{q/N}$ form factors, and $\pm 20\%$ for $W_{\Sigma, \Sigma'}$ response functions, multiplying the other form factors), and from the nucleon form factors (σ_{F_i} listed in Table I). The central values for the form factors and the uncertainties are taken from [42]. The resulting σ_α are shown in Table I for each of the Wilson coefficients. For the dipole, $\hat{\mathcal{C}}_1^{(5)}$, in general two NR operators contribute, $\mathcal{O}_{3,N}^{(0)}$ and $\mathcal{O}_{1,N}^{(2)}$. However, for heavy elements the latter is negligible, giving the estimate for σ_α in Table I. The central values for W_i are taken from [44]. Our estimates for the theoretical errors on W_i are educated guesses. While this suffices at present, since these are subleading to the other uncertainties, a dedicated study would be desired in the future.

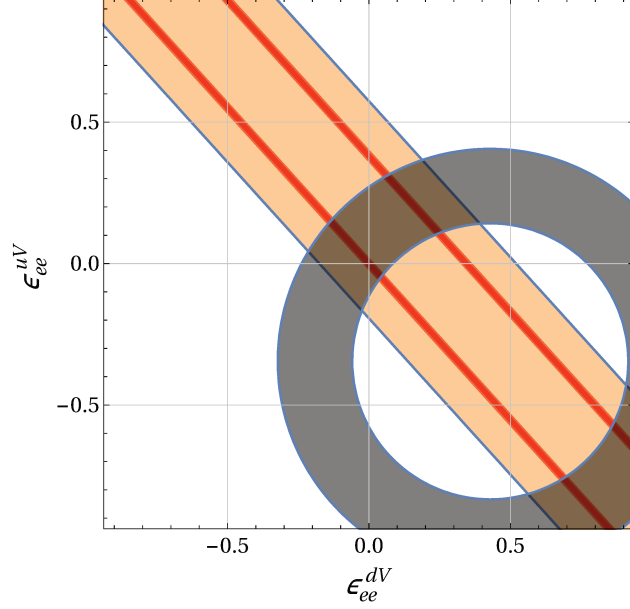


Figure 5: The regions allowed at 90% C.L. for electron neutrino NSI with vector up and down quark currents (1). The black, orange and red regions correspond to CHARM, COHERENT and expected NaI 2T constraints, respectively, see text for details.

Our prediction for the SM rate in the COHERENT detector is $N_{\text{th}}(\hat{\mathcal{C}}_a^{(d)}|_{\text{SM}}) = 188 \pm 53$ events. Comparison of this prediction with the COHERENT measurement gives the following 90% C.L. bounds on the NSI due to dimension 6 operators,

$$-0.11 < \varepsilon_{ee}^{uV} < 0.49, \quad -0.10 < \varepsilon_{ee}^{dV} < 0.44, \quad (91)$$

$$-0.06 < \varepsilon_{\mu\mu}^{uV} < 0.12, \quad -0.06 < \varepsilon_{\mu\mu}^{dV} < 0.11. \quad (92)$$

This is comparable to the sensitivity obtained in the global fits to the oscillation data, cf. Eqs. (82), (83). The limits on $\varepsilon_{\alpha\beta}^{uV}, \varepsilon_{\alpha\beta}^{dV}$ are correlated, see Fig. 5 for the case of ν_e . For NSI couplings to the strange quark we obtain a relatively weak bound, $|\varepsilon_{ee,\mu\mu}^{sV}| \lesssim 10^3$, because the sensitivity comes only from the $\mathcal{O}(q^2)$ term in the expansion of $F_1^{s/N}(q^2)$, see Eq. (32). The axial couplings ε_{ee}^{qA} and $\varepsilon_{\mu\mu}^{qA}$ are also poorly constrained, since they lead to spin-dependent interactions that are not coherently enhanced.

We collect the 90% C.L. bounds on the NSI coefficients in Table II for $\nu_e \rightarrow \nu_X$ transitions and in Table III for $\nu_\mu \rightarrow \nu_X$ transitions. The bounds on $\hat{C}_a^{(d)} = C_a^{(d)}/\Lambda^{d-4}$ are converted to lower bounds on the NP scale, Λ , setting the dimensionless Wilson coefficients to $C_a^{(d)} = 1$. The two tables also contain bounds from deep inelastic scattering, Section VIC, and

the expected reach from the proposed 2 ton NaI experiment [61], cf. Table IV. For easier comparison the bounds are also illustrated with barcharts in Fig. 6 for dimension 5 and dimension 7 operators, and in Fig. 7 for dimension 6 operators. For dimension 6 operators with vector couplings to quarks there are two possibilities. For flavor diagonal transitions, $\nu_\mu \rightarrow \nu_\mu$ and $\nu_e \rightarrow \nu_e$, the NSI contributions interfere with the SM. The resulting bounds are shown in Fig. 7 (left). If the transition is not flavor diagonal, the bounds are weaker, shown in the right panels in Fig. 7. For all the other operators the final neutrino, ν_X , can be of any neutrino flavor, including sterile neutrinos.

The bound on $\hat{C}_{7,s}^{(7)}$ is controlled by the s -quark tensor form factor $F_{T,0}^{s/N}$, which is not well known. At present it is even consistent with zero, which implies that there is no reliable bound on the $\hat{C}_{7,s}^{(7)}$. In Tables II, III we use the central value $F_{T,0}^{s/N}/m_s = 3.2 \cdot 10^{-4}$ from [42], with $\sigma_{F_i} = 0$, to gauge the rough potential reach of COHERENT, once lattice determinations of $F_{T,0}^{s/N}$ become precise enough. We use a similar approach for the Rayleigh operators, $\hat{C}_{1,2}^{(7)}$ where we (i) use the phenomenological form factor for two body currents for $\hat{C}_1^{(7)}$, Eq. (51), (ii) neglect the two-body current contributions for $\hat{C}_2^{(7)}$, and (iii) and use the NDA estimates (54) for the non perturbative single nucleon matrix elements, and do not assign any associated errors to these approximations. The bounds shown are thus just giving a rough potential reach of CE ν NS experiments once theoretical errors will be under control (with probably a better guesstimate for $\hat{C}_1^{(7)}$ than $\hat{C}_2^{(7)}$).

Tables II, III show in the case of dimension 6 operators the bounds for flavor non-diagonal processes $\nu_e \rightarrow \nu_X$ with $X \neq e$, and $\nu_\mu \rightarrow \nu_X$ with $X \neq \mu$, respectively. For flavor diagonal transitions, $\nu_e \rightarrow \nu_e$ or $\nu_\mu \rightarrow \nu_\mu$, the bounds on NSI from the COHERENT measurement are instead

$$\mathcal{C}_{1,u(d,s)}^{(6)} : \quad \Lambda > 417(440, 1.1) \text{ GeV} \quad (\nu_e), \quad \Lambda > 443(458, 1.7) \text{ GeV} \quad (\nu_\mu), \quad (93)$$

$$\mathcal{C}_{2,u(d,s)}^{(6)} : \quad \Lambda > 22.9(11.7, 4.5) \text{ GeV} \quad (\nu_e), \quad \Lambda > 23.1(11.9, 4.6) \text{ GeV} \quad (\nu_\mu), \quad (94)$$

The relative sizes of bounds in Tables II, III are easy to understand using approximate scalings in Eqs. (47)-(49). The $\mathcal{O}(A^2)$ enhancements of operators $\mathcal{Q}_1^{(5)}$, $\mathcal{Q}_{1,q}^{(6)}$, $\mathcal{Q}_3^{(7)}$, $\mathcal{Q}_{5,q}^{(7)}$ and $\mathcal{Q}_{8,q}^{(7)}$, $\mathcal{Q}_{10,q}^{(7)}$, Eq. (48), translate into more stringent bounds for Λ . The bounds are significantly weaker for the remaining non-enhanced operators. The bounds on operators with strange quarks are also weaker, since the corresponding form factors are smaller.

The bounds on NSI from CE ν NS experiments are set to improve in the future with a

Lower bounds on Λ in GeV, $\nu_e \rightarrow \nu_X$ transitions							
$\hat{C}_{i,q}^{(d)}$	COHERENT	CHARM	NaI 2T	$\hat{C}_{i,q}^{(d)}$	COHERENT	CHARM	NaI 2T
$\hat{C}_1^{(5)}$	$3.3 \cdot 10^3$	4.5	$8.3 \cdot 10^3$	$\hat{C}_{7,u}^{(7)}$	$1.3 \cdot \left(\frac{2.3 \text{ MeV}}{m_u}\right)^{1/3}$	7.5	$2.9 \cdot \left(\frac{2.3 \text{ MeV}}{m_u}\right)^{1/3}$
$\hat{C}_{1,u}^{(6)}$	603	349	993	$\hat{C}_{7,d}^{(7)}$	$1 \cdot \left(\frac{4.8 \text{ MeV}}{m_d}\right)^{1/3}$	8.7	$2.4 \cdot \left(\frac{4.8 \text{ MeV}}{m_d}\right)^{1/3}$
$\hat{C}_{1,d}^{(6)}$	632	349	$1.04 \cdot 10^3$	$\hat{C}_{7,s}^{(7)\dagger}$	$0.33 \cdot \left(\frac{95 \text{ MeV}}{m_s}\right)^{1/3}$	19	$0.75 \cdot \left(\frac{95 \text{ MeV}}{m_s}\right)^{1/3}$
$\hat{C}_{1,s}^{(6)}$	1.1	239	4.8	$\hat{C}_{8,u}^{(7)}$	64	75	83.4
$\hat{C}_{2,u}^{(6)}$	19.1	349	78.2	$\hat{C}_{8,d}^{(7)}$	59	68	86.2
$\hat{C}_{2,d}^{(6)}$	9.8	349	46.4	$\hat{C}_{8,s}^{(7)}$	1.2	56	7.7
$\hat{C}_{2,s}^{(6)}$	4.5	239	15.4	$\hat{C}_{9,u}^{(7)}$	2.2	75	5.3
$\hat{C}_1^{(7)\dagger}$	1.7	5.6	2.2	$\hat{C}_{9,d}^{(7)}$	1.4	68	3.7
$\hat{C}_2^{(7)\dagger}$	0.01	6.4	0.02	$\hat{C}_{9,s}^{(7)}$	0.74	56	1.8
$\hat{C}_3^{(7)}$	21	31	27.3	$\hat{C}_{10,u}^{(7)}$	57	67	83.4
$\hat{C}_4^{(7)}$	0.9	36	1.6	$\hat{C}_{10,d}^{(7)}$	59	61	86.2
$\hat{C}_{5,u}^{(7)}$	11	3.8	17.3	$\hat{C}_{10,s}^{(7)}$	2.8	50	7.7
$\hat{C}_{5,d}^{(7)}$	14.4	4.5	22.3	$\hat{C}_{11,u}^{(7)}$	2.2	67	5.3
$\hat{C}_{5,s}^{(7)}$	16.4	9.9	23.7	$\hat{C}_{11,d}^{(7)}$	1.4	61	3.7
$\hat{C}_{6,u}^{(7)}$	1.3	3.8	2.1	$\hat{C}_{11,s}^{(7)}$	0.74	50	1.8
$\hat{C}_{6,d}^{(7)}$	1.7	4.5	2.7	—	—	—	—
$\hat{C}_{6,s}^{(7)}$	1.3	9.9	2.1	—	—	—	—

Table II: The 90 % C.L. lower bounds on Λ from COHERENT, CHARM, and NaI 2T for $\nu_e \rightarrow \nu_X$, ($X \neq e$, for $X = e$ see main text) NSI Wilson coefficients, $\hat{C}_a^{(d)}$, Eq. (2), setting $C_a^{(d)} = 1$, and assuming only one such NSI Wilson coefficient is nonzero. For $\hat{C}_{7,s}^{(7)}$ ($\hat{C}_{1,2}^{(7)}$) we use only the central value of the form factor (NDA estimates) so the bounds are merely indicative, see main text for details.

number of new detectors either already taking data or being planned. The COHERENT collaboration is operating a 10kg Ge detector, a 22kg single-phase liquid Ar detector, and a 185 kg NaI[Tl] scintillating crystal detector [61]. The liquid Ar may increase to 1ton, and NaI[Tl] to 2 tons, in the future [62], cf. Table IV. To take full advantage of these experimental progress an increased precision in the predictions of nuclear response functions and nuclear form factors will be called for.

In Tables II and III we show the expected improvements in the sensitivity to NSI due

Lower bounds on Λ in GeV, $\nu_\mu \rightarrow \nu_X$ transitions							
$\hat{C}_{i,q}^{(d)}$	COHERENT	CHARM	NaI 2T	$\hat{C}_{i,q}^{(d)}$	COHERENT	CHARM	NaI 2T
$\hat{C}_1^{(5)}$	$4.8 \cdot 10^3$	47.1	$1.2 \cdot 10^4$	$\hat{C}_{7,u}^{(7)}$	$1.4 \cdot \left(\frac{2.3 \text{ MeV}}{m_u}\right)^{1/3}$	16.1	$3.4 \cdot \left(\frac{2.3 \text{ MeV}}{m_u}\right)^{1/3}$
$\hat{C}_{1,u}^{(6)}$	726	826	$1.2 \cdot 10^3$	$\hat{C}_{7,d}^{(7)}$	$1.2 \cdot \left(\frac{4.8 \text{ MeV}}{m_d}\right)^{1/3}$	18.3	$2.7 \cdot \left(\frac{4.8 \text{ MeV}}{m_d}\right)^{1/3}$
$\hat{C}_{1,d}^{(6)}$	767	697	$1.3 \cdot 10^3$	$\hat{C}_{7,s}^{(7)\dagger}$	$0.4 \cdot \left(\frac{95 \text{ MeV}}{m_s}\right)^{1/3}$	37.7	$0.9 \cdot \left(\frac{95 \text{ MeV}}{m_s}\right)^{1/3}$
$\hat{C}_{1,s}^{(6)}$	1.74	463	5.8	$\hat{C}_{8,u}^{(7)}$	64.7	160.6	94.5
$\hat{C}_{2,u}^{(6)}$	23.1	826	94.3	$\hat{C}_{8,d}^{(7)}$	67.5	143.4	97.7
$\hat{C}_{2,d}^{(6)}$	11.9	697	55.5	$\hat{C}_{8,s}^{(7)}$	3.2	109.1	8.7
$\hat{C}_{2,s}^{(6)}$	4.6	463	18.5	$\hat{C}_{9,u}^{(7)}$	2.4	160.6	6
$\hat{C}_1^{(7)\dagger}$	1.9	12.3	2.5	$\hat{C}_{9,d}^{(7)}$	1.6	143.4	4.2
$\hat{C}_2^{(7)\dagger}$	0.01	12.5	0.02	$\hat{C}_{9,s}^{(7)}$	0.8	109.1	2
$\hat{C}_3^{(7)}$	23.7	67.9	31.2	$\hat{C}_{10,u}^{(7)}$	64.7	143.1	94.5
$\hat{C}_4^{(7)}$	1	77.8	1.8	$\hat{C}_{10,d}^{(7)}$	67.5	127.7	97.7
$\hat{C}_{5,u}^{(7)}$	12.6	8.2	19.7	$\hat{C}_{10,s}^{(7)}$	3.2	97.2	8.7
$\hat{C}_{5,d}^{(7)}$	15.6	9.4	25.5	$\hat{C}_{11,u}^{(7)}$	2.4	143.1	6
$\hat{C}_{5,s}^{(7)}$	19	19.3	27.1	$\hat{C}_{11,d}^{(7)}$	1.6	127.7	4.2
$\hat{C}_{6,u}^{(7)}$	1.5	8.2	2.4	$\hat{C}_{11,s}^{(7)}$	0.8	97.2	2
$\hat{C}_{6,d}^{(7)}$	1.9	9.4	3.1	—	—	—	—
$\hat{C}_{6,s}^{(7)}$	1.5	19.3	2.4	—	—	—	—

Table III: The 90 % C.L. lower bounds on Λ from COHERENT, CHARM and NaI 2T for $\nu_\mu \rightarrow \nu_X$ ($X \neq \mu$, for $X = \mu$ see main text) NSI Wilson coefficients, $\hat{C}_a^{(d)}$, Eq. (2), setting $C_a^{(d)} = 1$, and assuming only one such NSI Wilson coefficient is nonzero. For $\hat{C}_{7,s}^{(7)}$ ($\hat{C}_{1,2}^{(7)}$) we use only the central value of the form factor (NDA estimates) so the bounds are merely indicative, see main text for details.

to the 2 ton NaI detector proposed by the COHERENT Collaboration [61], with the same neutrino source but with a baseline of 28m and a lower energy threshold of ~ 13 keV. Furthermore, in the projections we assume that the total theoretical uncertainty is reduced 10-fold compared to the present ones, quoted in Table I. This would give the projected total theoretical uncertainties $\sigma_{F_i} \sim 3 - 5\%$. This will require more precise determinations of the neutrino flux, which is already planned, as well as a much better knowledge of the quenching factors, and major advances in the purely theoretical inputs – the form factors and nuclear

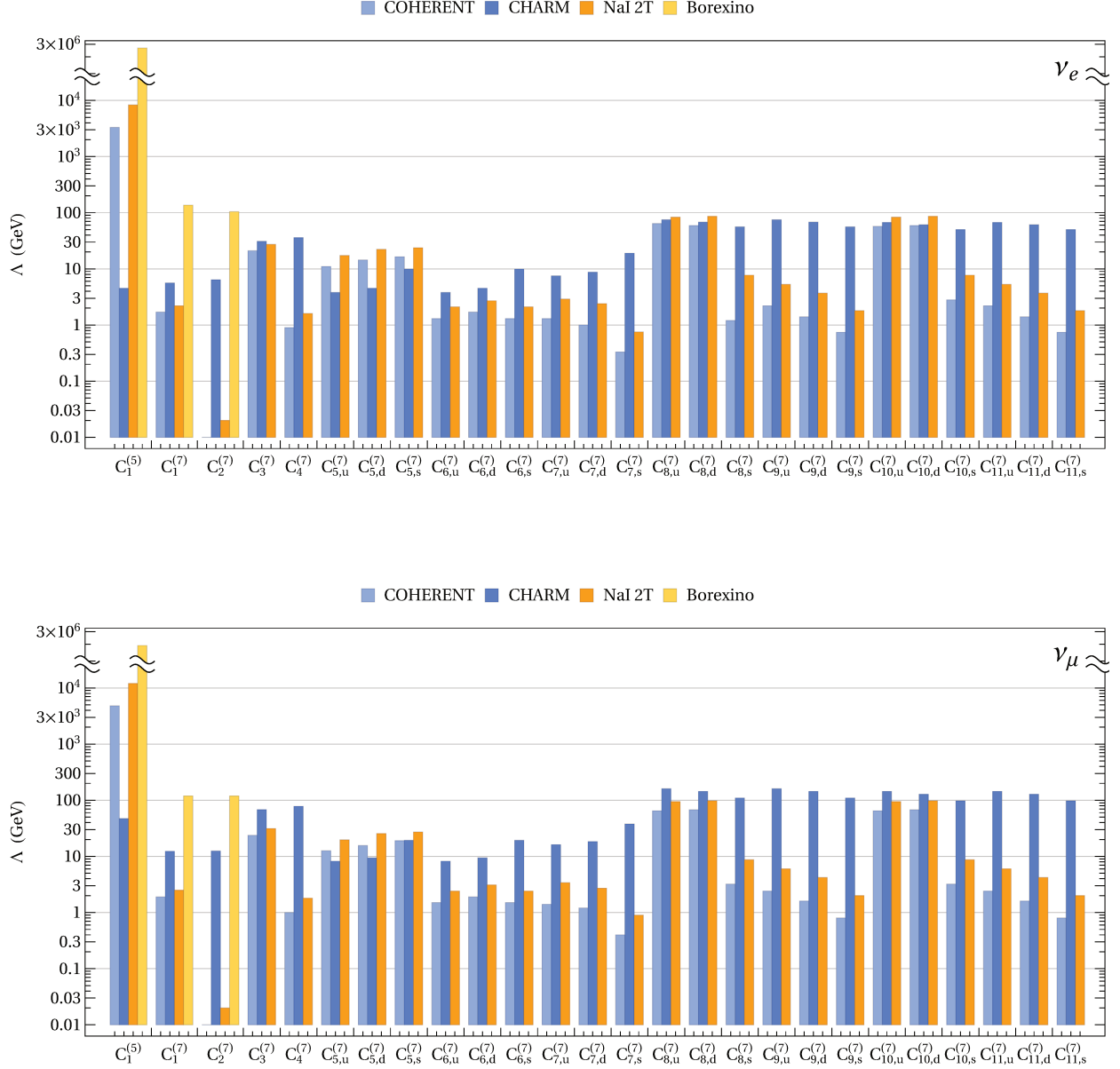


Figure 6: Limits from COHERENT, CHARM, Borexino, and projected limits from a NaI 2T experiment on the scale Λ of dimension 5 and dimension 7 NSI operators for electron neutrinos (top) and muon neutrinos (bottom).

response functions entering the SM prediction. While such a decrease of uncertainties may be aggressive, they do give us a useful gauge of the potential reach of $\text{CE}\nu\text{NS}$ experiments.

In NaI detector the neutrino recoils on both the iodine and sodium nuclei. For the SM neutrino interactions the scattering on iodine completely dominates. The coherently enhanced cross section is ~ 40 times larger for neutrino scattering on iodine as it is for

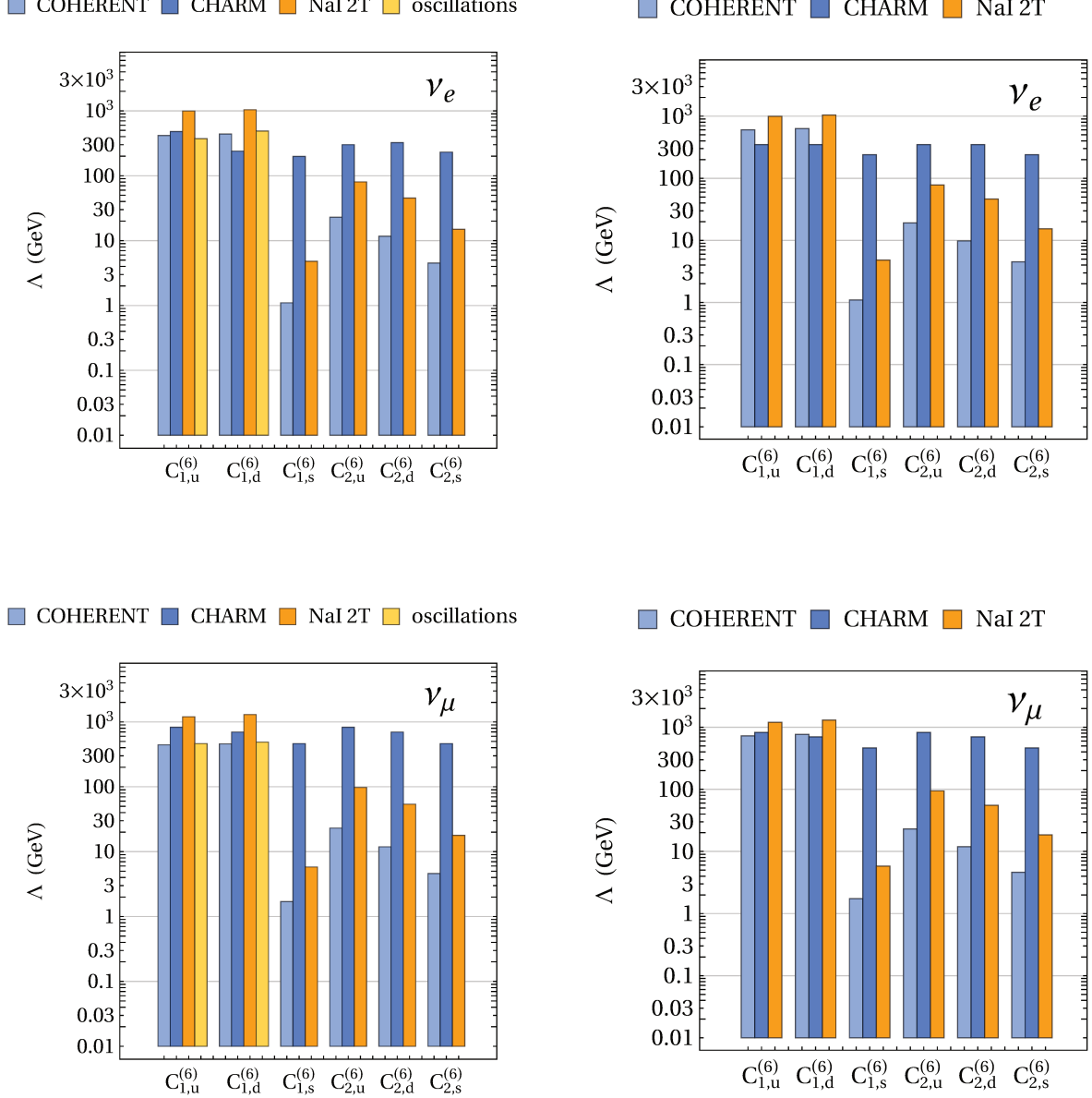


Figure 7: Limits from COHERENT, CHARM, neutrino oscillations and projected limits from a NaI 2T experiment on the scale Λ of dimension 6 operators for electron neutrinos (top) and muon neutrinos (bottom). The two panels on the left correspond to lepton flavor conserving operators ($\nu_i \rightarrow \nu_i$), the ones on the right to lepton flavor violating operators ($\nu_i \rightarrow \nu_j$, $i \neq j$).

sodium. This is the case also for coherently enhanced NSI interactions, where scattering on iodine similarly dominates. Spin-dependent interactions, on the other hand, can be comparable, depending on the operator. We find that scattering on iodine dominates except for the operators $\mathcal{Q}_{2,q}^{(6)}$, $\mathcal{Q}_{7,q}^{(7)}$ and $\mathcal{Q}_{9,q}^{(7)}$, for which the main contribution to the scattering rate

	T_{th}	Baseline (m)	Target	Mass (kg)	Source
NaI 2T COH[61]	13 keV	28	NaI	2000	SPD
Ge COH[61]	5 keV	22	Ge	10	SPD
LAr COH [61]	20 keV	29	Ar	22	SPD
RED100 [58]	500 eV	19	Xe	100	3 GW reactor
MINER [63]	10 eV	1	$^{72}\text{Ge}+^{28}\text{Si}$	30	1 MW reactor
CONNIE [64]	28 eV	30	Si	1	3.8 GW reactor
RICOCHET [65]	50-100 eV	<10	Ge/Zn	10	8.54 GW reactor
NU-CLEUS [66]	20 eV	<10	$\text{CaWO}_4, \text{Al}_2\text{O}_3$	0.001	8.54 GW reactor
νGEN [67]	350 eV	10	Ge	4×0.4	3 GW reactor
CONUS [68]	<300 eV	17	Ge	4	3.9 GW reactor
TEXONO [69]	150-200 eV	28	Ge	1	2×2.9 GW reactors

Table IV: A list of proposed experiments to detect $\text{CE}\nu\text{NS}$ using (anti)neutrinos from Stopped Pion Decay (SPD) or from reactors, with recoil energy threshold, T_{th} , the distance from the source, the target material and its mass given in 2nd to 4th columns.

is from sodium, while the two cross sections are of the same order for $\mathcal{Q}_1^{(5)}$. The expected bounds from $\nu_{e,\mu} \rightarrow \nu_X$ scattering are shown in Tables II and III.

For flavor diagonal transitions, $\nu_{e,\mu} \rightarrow \nu_{e,\mu}$, the expected bounds on dimension 6 operators from the NaI 2T detector are,

$$\mathcal{C}_{1,u(d,s)}^{(6)} : \quad \Lambda > 993(1040, 4.8) \text{ GeV} \quad (\nu_e), \quad \Lambda > 1200(1300, 5.8) \text{ GeV} \quad (\nu_\mu), \quad (95)$$

$$\mathcal{C}_{2,u(d,s)}^{(6)} : \quad \Lambda > 80.3(45.2, 14.9) \text{ GeV} \quad (\nu_e), \quad \Lambda > 97.6(53.8, 17.8) \text{ GeV} \quad (\nu_\mu), \quad (96)$$

While COHERENT uses stopped pions as a source of neutrinos, there are also a number of planned or already operating $\text{CE}\nu\text{NS}$ experiments that use reactor antineutrinos, see Table IV as well as, e.g., Refs. [15, 70, 71]. Reactors produce large quantities of low energy electronic antineutrinos. On average about ~ 6 antineutrinos are produced per fission, for a total of $\sim 2 \times 10^{20} \bar{\nu}_e$ per second per GW of thermal reactor power [71–73], with a maximum energy of ~ 8 MeV.

As two representative examples of reactor $\text{CE}\nu\text{NS}$ experiments we chose the proposed RED100 [58] and MINER [63] experiments, and checked their respective sensitivities to different NSI, assuming in both cases a total uncertainty of $\sigma_{F_i} \sim 10\%$. RED100 has a

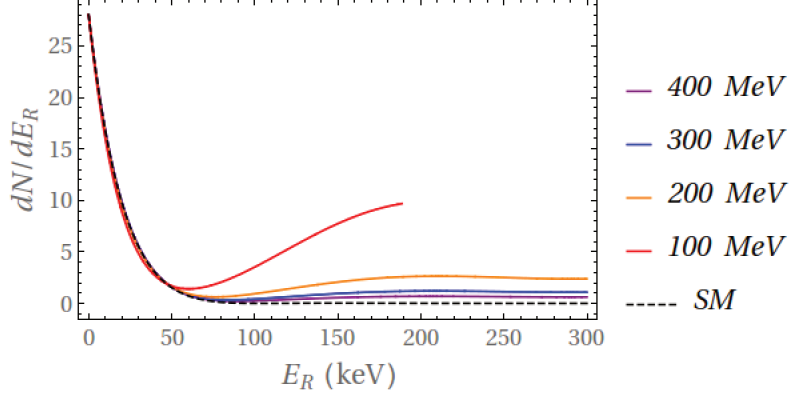


Figure 8: Effect at high recoil energy of the operator $\mathcal{Q}_4^{(7)}$, assuming $\hat{\mathcal{C}}_4^{(7)} = 0.1 \text{ GeV}^{-3}$, for four different neutrino energies, using monochromatic neutrino beams for illustration. The black dashed line is the SM rate.

proposed 100kg target of liquid Xenon, with a baseline of 19m from a 1GW reactor and an energy threshold of 500 eV. While this energy threshold is lower than for stopped pion decay experiments, it is the highest among the reactor experiments. MINER [63] has a proposed 30kg detector composed of ^{72}Ge and ^{28}Si in 2:1 ratio, with a baseline of 1m from a 1MW detector and a very low energy threshold of 10 eV.

Because of lower thresholds, both RED100 and MINER would have one to two orders of magnitude better sensitivity to the neutrino dipole moment, $\hat{\mathcal{C}}_1^{(5)}$, compared to NaI 2T. The reach for the vector NSI current operators, $\hat{\mathcal{C}}_{1,u(d)}^{(6)}$ could exceed the ones from global oscillation fits, while there would be also an appreciable improvement on the derivative couplings, $\hat{\mathcal{C}}_{8,q}^{(7)}, \hat{\mathcal{C}}_{10,q}^{(7)}$. The operators inducing spin-dependent interactions, on the other hand, cannot be probed better in these experiments, since xenon has a smaller nuclear spin than iodine, while ^{72}Ge and ^{28}Si have nuclear spin 0.

Future experiments can improve their sensitivity to specific NSI operators by changing experimental conditions. As just stated, lowering the energy threshold improves the sensitivity to the magnetic monopole operator $\mathcal{Q}_1^{(5)}$, whose contribution is enhanced by the $1/\vec{q}^2$ photon pole, cf. Eqs. (24), (48). For instance, the CONNIE collaboration proposes a 1kg Si detector with the energy threshold of 28 eV that would be situated 30m away from the reactor [64]. Taking all the other parameters as in our projection for the NaI 2T limit, leads to a projected limit for $\mathcal{Q}_1^{(5)}$ of $\Lambda \simeq 50 \text{ TeV}$, to be compared with 8.3 TeV at NaI 2T, Table II.

Varying the neutrino energy, E_ν , as well as increasing the range of nuclear recoil energies, E_R , can also be beneficial. In this way one could uncover $\vec{q}^2$ dependence of the neutrino scattering cross section that differs from the SM one. We illustrate this in Fig. 8, taking as the example the $\mathcal{Q}_4^{(7)}$ operator. The $\mathcal{Q}_4^{(7)}$ operator matches onto the NR operator $\mathcal{O}_{1,N}^{(1)}$, whose matrix element squared starts at $\mathcal{O}(\vec{q}^4)$ and is independent of E_ν , see Eq. (42). In contrast, the SM matrix element squared grows with neutrino energy, $\propto E_\nu^2$. For high enough recoil energies, $E_R \sim \mathcal{O}(100 \text{ keV})$, and neutrino energies $E_\nu \sim \mathcal{O}(100 \text{ MeV})$, there is clear distinction between the scattering rate with and without the presence of $\mathcal{Q}_4^{(7)}$ (the NP scale was taken very low in Fig. 8 to exaggerate the effect).

C. Constraints on NSI from deep inelastic scattering

The CHARM neutrino detector [74] was composed of 78 plates of marble (CaCO_3) with a total fiducial mass of 87.4 tons. The target is to a very good approximation an isoscalar – the correction to the cross section from the isotriplet component is $\mathcal{O}(0.2\%)$ [56]. Data were recorded exposing the detector to neutrinos and antineutrinos from the CERN 400 GeV SPS proton beam dump.

In our analysis we focus on the ratio of NC and CC total cross sections for electron neutrinos and antineutrinos that has been measured to be [53]

$$R_e = \frac{\sigma(\nu_e N \rightarrow \nu_e X) + \sigma(\bar{\nu}_e N \rightarrow \bar{\nu}_e X)}{\sigma(\nu_e N \rightarrow e^- X) + \sigma(\bar{\nu}_e N \rightarrow e^+ X)} = 0.406 \pm 0.140, \quad (97)$$

where an equal flux of ν_e and $\bar{\nu}_e$ has been assumed, while similarly for muon neutrinos [75]

$$R_{\nu_\mu} = \frac{\sigma(\nu_\mu N \rightarrow \nu_\mu X)}{\sigma(\nu_\mu N \rightarrow \mu^- X)} = 0.3093 \pm 0.0031, \quad (98)$$

The ratios R_e and R_{ν_μ} are predicted in the SM to be [76, 77]

$$R_e^{\text{SM}} = 0.3221 \pm 0.0006, \quad R_{\nu_\mu}^{\text{SM}} = 0.3156 \pm 0.0006. \quad (99)$$

The dominant theoretical uncertainty in the two predictions is due to the approximation that the target was taken to be an isospin singlet, which is correct within $\mathcal{O}(0.2\%)$.

Since the neutrino CC cross section is strongly constrained, we can assume that NSI only affect NC transitions. The ratio R_e in Eq. (99) then receives the NSI correction as

$$R_e^{\text{NSI}} = R_e^{\text{SM}} + \frac{\Delta\sigma^{\text{NSI}}}{\sigma_{\text{CC}}}, \quad (100)$$

where σ_{CC} is the total neutrino and antineutrino CC cross section and $\Delta\sigma_{\text{NSI}}$ is the NSI contribution to the NC cross section. In the analysis we take only a single NSI operator at a time to be nonzero. Similarly, R_{ν_μ} is modified to

$$R_{\nu_\mu}^{\text{NSI}} = R_{\nu_\mu}^{\text{SM}} + \frac{\Delta\sigma_{\text{NSI}}^{\nu_\mu}}{\sigma_{\text{CC}}^{\nu_\mu}}, \quad (101)$$

where the cross sections in the ratios now refer to the muonic neutrino only. Comparing Eqs. (100) and (101) with the experimental results in Eqs. (97) and (98), gives the upper bound on the allowed sizes of NSI Wilson coefficients, $\hat{\mathcal{C}}_a^{(d)}$, Eq. (2). Taking the dimensionless Wilson coefficients to be $\mathcal{C}_a^{(d)} = 1$, this translates to a 90% CL lower bound on NP scale Λ for each NSI operator, given in Tables II and III. These bounds are also shown as dark blue bars in Figs. 6 and 7.

The relative values of bounds are easily understood from the matrix elements in Eqs. (72)-(76). In particular, the two scalar operators $\mathcal{Q}_{5,q}^{(7)}$ and $\mathcal{Q}_{6,q}^{(7)}$ have exactly the same matrix elements and thus the same bounds for given flavor q . The difference between the bounds on Λ for three light quark flavors comes predominantly from the factor m_q that is part of the definition of the operators, leading to $\sim (m_s/m_{u,d})^{1/3}$ larger Λ exclusion for the strange quark. The matrix element of the tensor operator, $\mathcal{Q}_{7,q}^{(7)}$, is bigger, cf. Eq. (76), which translates to roughly factor of 2 more stringent bounds on Λ .

In the case of flavor diagonal transitions, the bounds on dimension 6 operators are

$$\mathcal{C}_{1,u(d,s)}^{(6)} : \quad \Lambda > 480(239, 198) \text{ GeV} \quad (\nu_e), \quad \Lambda > 826(697, 463) \text{ GeV} \quad (\nu_\mu), \quad (102)$$

$$\mathcal{C}_{2,u(d,s)}^{(6)} : \quad \Lambda > 301(324, 231) \text{ GeV} \quad (\nu_e), \quad \Lambda > 826(697, 463) \text{ GeV} \quad (\nu_\mu), \quad (103)$$

For the reader's convenience we translate the CHARM bounds on dimension 6 operators also into the bounds on ε_i parameters, Eq. (1). For the electron neutrino, one obtains

$$-0.11 < \varepsilon_{ee}^{uV} < 0.27, \quad -0.38 < \varepsilon_{ee}^{uA} < 0.69, \quad (104)$$

$$-0.24 < \varepsilon_{ee}^{dV} < 0.08, \quad -0.59 < \varepsilon_{ee}^{dA} < 0.44, \quad (105)$$

$$-0.74 < \varepsilon_{ee}^{sV} < 1.60, \quad -1.17 < \varepsilon_{ee}^{sA} < 1.01, \quad (106)$$

while for the muon neutrino

$$-0.03 < \varepsilon_{\mu\mu}^{uV} < 0.06, \quad -0.11 < \varepsilon_{\mu\mu}^{uA} < 0.08, \quad (107)$$

$$-0.05 < \varepsilon_{\mu\mu}^{dV} < 0.02, \quad -0.31 < \varepsilon_{\mu\mu}^{dA} < 0.15, \quad (108)$$

$$-0.20 < \varepsilon_{\mu\mu}^{sV} < 0.11, \quad -0.54 < \varepsilon_{\mu\mu}^{sA} < 0.40. \quad (109)$$

For the case of the electron neutrino these bounds are comparable, yet somewhat stronger, than the bounds from oscillations for vector currents involving u and d quarks, Eqs. (82) and (83), and are significantly stronger for the case of the muon neutrino.

Note that for a number of operators the bounds on Λ from the CHARM experiment are comparable to the momentum exchange $q \sim \mathcal{O}(10 \text{ GeV})$. This means that the EFT analysis may be applicable only for strongly coupled mediators, with couplings larger than $\mathcal{O}(1)$. Another general comment regarding CHARM constraints on NSI is that for light mediators these are comparatively less effective than CE ν NS constraints where the momentum exchange is smaller.

D. Other constraints

The contribution to the neutrino scattering rates due to the neutrino magnetic moment has a pole at $\vec{q}^2 = 0$, cf. Fig. 9 in Appendix B. This means that experiments with lower E_R thresholds will have better sensitivity to the magnetic moment. Furthermore, scattering on electrons will in general lead to lower $\vec{q}^2$. Measurements of solar neutrinos scattering on electrons in Borexino [57] give the current most stringent limits on the magnetic moment μ_{ν_α} , or, equivalently, on the Wilson coefficient $\mathcal{C}_1^{(5)}$,

$$\mathcal{C}_1^{(5)} : \quad \Lambda > 2.7 \cdot 10^6 \text{ GeV} \quad (\nu_e); \quad \Lambda > 1.8 \cdot 10^6 \text{ GeV} \quad (\nu_\mu). \quad (110)$$

The measured neutrino scattering rates in Borexino can also be translated in a bound on Rayleigh operators $\mathcal{C}_{1,2}^{(7)}$. The neutrino interactions mediated by the two Rayleigh operators result either in $\nu A \rightarrow \nu A$ scattering through 1-loop matrix elements or in $\nu A \rightarrow \nu A \gamma$, i.e., with an emission of an extra photon. In the Borexino experiment both processes lead to the same signal. Using the results from Section III C for the 1-loop contribution, with NDA estimates for the single nuclear matrix elements and neglecting two-body currents for $\mathcal{Q}_2^{(7)}$ operator, and adding the cross section for the process with a photon emission, give the total NSI scattering rate. Comparing it with the Borexino measurement [57] of the solar neutrino flux gives

$$\mathcal{C}_1^{(7)} : \quad \Lambda > 136 \text{ GeV} \quad (\nu_e), \quad \Lambda > 119 \text{ GeV} \quad (\nu_\mu), \quad (111)$$

$$\mathcal{C}_2^{(7)} : \quad \Lambda > 104 \text{ GeV} \quad (\nu_e), \quad \Lambda > 119 \text{ GeV} \quad (\nu_\mu). \quad (112)$$

A different set of bounds on NSI operators (4)-(10) comes from collider experiments. For a proper analysis we need to extend the EFT analysis to above the electroweak symmetry breaking scale, which we do in the next section. However, some of the bounds directly apply to the operators (4)-(10). For instance, the searches for dark matter can be re-interpreted as bounds on NSI operators with two neutrinos replacing the two DM particles in the final state.

The monojet searches at CMS and ATLAS [78–80] thus result in lower limits of $\Lambda \gtrsim 1$ TeV for (axial-)vector current operators, Eq. (4), $\Lambda \gtrsim 200$ GeV for gluon-gluon operators, Eq. (6), $\Lambda \gtrsim 40$ GeV for scalar operators, Eq. (7), and $\Lambda \gtrsim 20$ GeV for tensor current operators, Eq. (8), after converting to our normalization of the operators. The monophoton searches bound di-photon operators, Eq. (5), giving $\Lambda \gtrsim 30$ GeV [81]. These bounds, apart from (axial-)vector current operators, are quite weak, with values of Λ allowed that are even below the kinematical cuts on p_T and/or MET. One may thus question the applicability of the EFT with the actual bounds from colliders in reality even weaker, unless the couplings are large. We do not attempt to correct for these effects since this is beyond the scope of present manuscript, see, however, [82] on how to properly obtain EFT bounds from LHC searches.

Once the EFT is uplifted above the electroweak scale, the bounds from collider searches can become more severe. For instance, searches for charged fermion contact interactions at LEP [83] give constraints on the $SU(2)_L \times U(1)_Y$ symmetric operators, defined in Eqs. (116)-(119) below. These operators result in dimension 6 NSI operators (4) below the electroweak scale, but with bounds on Λ from LEP of about $\mathcal{O}(1 \text{ TeV})$ even when coupling only to leptons (see Section VII for details).

VII. NSI ABOVE THE ELECTROWEAK SCALE

In this Section we turn to the question of how the NSI interactions (2) are generated. Since the bounds on many of the operators are relatively mild, cf. Tables II and III, it is possible that light NP could be responsible for their generation. This interesting direction was pursued, e.g., in Refs. [34, 35, 84, 85].

The other option is that the NP responsible for NSI is heavy, heavier than the electroweak scale. If this is the case, the NP states can be integrated out leading to an EFT that is valid between the scale of NP, Λ , and the electroweak scale, v_{EW} , with the effective Lagrangian (see also [86–89])

$$\mathcal{L}_{\text{EW}} = \sum_{a,d} \frac{C_a^{(d)}}{\Lambda^{d-4}} Q_a^d, \quad (113)$$

where Q_a^d are $SU(2)_L \times U(1)_Y$ invariant operators. In constructing the electroweak (EW) EFT operators we add to the SM field content the right-handed neutrino, ν_R , which is a SM singlet. This allows for SM neutrinos to be either Dirac or Majorana. In the rest of this Section we discuss the bounds on operators Q_a^d and their matchings onto the low energy EFT for NSI, Eq. (2). We only consider operators that do not violate lepton number, since the lepton number violating operators are severely constrained by bounds on neutrinoless double beta decay.

The two dimension 6 operators in EW EFT that lead to a neutrino magnetic dipole moment are (throughout this section we do not display generational indices on leptonic fields, and assume flavor conservation for quark currents)

$$Q_{1,B}^{(6)} = \frac{g_1}{8\pi^2} (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger L_L) B^{\mu\nu}, \quad Q_{1,W}^{(6)} = \frac{g_2}{8\pi^2} (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger \tau^a L_L) W^{a,\mu\nu}, \quad (114)$$

where $\tilde{H} = i\sigma_2 H^*$, with H the Higgs doublet, L_L the lepton doublet, $B_{\mu\nu}$ and $W_{\mu\nu}^a$ the hypercharge and $SU(2)_L$ field strengths, and τ^a the $SU(2)_L$ generator in the fundamental representation. Both of the above operators contribute below the EW scale to the dimension five magnetic dipole operator, Eq. (3),

$$\hat{C}_1^{(5)} = \frac{v_{\text{EW}}}{\sqrt{2}\Lambda^2} \left(C_{1,B}^{(6)} + \frac{1}{2} C_{1,W}^{(6)} \right), \quad (115)$$

where $v_{\text{EW}} \simeq 246$ GeV is the Higgs vev. If either $Q_{1,B}^{(6)}$ or $Q_{1,W}^{(6)}$ are generated in the UV, the neutrinos will have magnetic moments. The exception is, if the two contributions cancel against each other, i.e., for $2\hat{C}_{1,B}^{(6)} = -\hat{C}_{1,W}^{(6)}$, in which case the neutrino magnetic moment vanishes.

The dimension six operators $\mathcal{Q}_{1(2),f}^{(6)}$, Eq. (4), can arise from the following four-fermion operators in the EW EFT (for $i = j$ the $Q_{4F,ii}^{(6)}$ operator is equivalent to $Q_{3F,ii}^{(6)}$ and should be dropped),

$$Q_{1F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu L_L^i) (\bar{Q}_L^j \gamma^\mu Q_L^j), \quad Q_{2F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu \tau^a L_L^i) (\bar{Q}_L^j \gamma^\mu \tau^a Q_L^j), \quad (116)$$

$$Q_{3F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu L_L^i) (\bar{L}_L^j \gamma^\mu L_L^j) , \quad Q_{4F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu \tau^a L_L^i) (\bar{L}_L^j \gamma^\mu \tau^a L_L^j) , \quad (117)$$

$$Q_{5F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu L_L^i) (\bar{e}_R^j \gamma^\mu e_R^j) , \quad Q_{6F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu L_L^i) (\bar{u}_R^j \gamma^\mu u_R^j) , \quad (118)$$

$$Q_{7F,ij}^{(6)} = (\bar{L}_L^i \gamma_\mu L_L^i) (\bar{d}_R^j \gamma^\mu d_R^j) , \quad (119)$$

which will then give for the Wilson coefficients of dimension 6 operators below electroweak scale ($u_1 = u$, $d_1 = d$, $d_2 = s$ and α the lepton flavor, not displayed on l.h.s.)

$$\hat{C}_{1(2),u_1}^{(6)} = \frac{1}{2\Lambda^2} \left[\pm \left(C_{1F,\alpha 1}^{(6)} + \frac{1}{4} C_{2F,\alpha 1}^{(6)} \right) + C_{6F,\alpha 1}^{(6)} \right] , \quad (120)$$

$$\hat{C}_{1(2),d_i}^{(6)} = \frac{1}{2\Lambda^2} \left[\pm \left(C_{1F,\alpha i}^{(6)} + \frac{1}{4} C_{2F,\alpha i}^{(6)} \right) + C_{7F,\alpha i}^{(6)} \right] , \quad (121)$$

$$\hat{C}_{1(2),e}^{(6)} = \frac{1}{2\Lambda^2} \left[\pm \left(C_{3F,\alpha 1}^{(6)} + \frac{1}{4} C_{4F,\alpha 1}^{(6)} \right) + C_{5F,\alpha 1}^{(6)} \right] . \quad (122)$$

The problem with generating large contributions to $\hat{C}_{1(2),f}^{(6)}$ Wilson coefficients in this way is that the dimension 6 operators in Eq. (116) are extremely well bounded. Translating the results from [77, 90] the bounds for $Q_{nF,ij}^{(d)}$ for electrons coupling to first generations quarks, $i = 1, j = 1$ are $\Lambda > 4.7; 4.8; 3.4; 4.4; 3.3; 3.5$ TeV, while for muons, $i = 2, j = 1$, $\Lambda > 1.6; 3.1; 3.6; 3.6; 1.0; 0.4$ TeV, where respectively $n = 1, 2, 3, 5, 6, 7$, and we set $C_{nF,ij}^{(6)} = 1$ (for $Q_{4F,21}^{(d)}$ the bound is of the same order as for $Q_{3F,21}^{(d)}$, but a precise determination would require a correlation matrix to properly account for the change of basis). For electron-quark couplings the most stringent bounds come from measurements of $d \rightarrow ue\nu$ transitions and atomic parity violation, and are much more severe than the bounds from neutrino scattering. For muon-quark couplings the most stringent bound for $Q_{2F,21}^{(6)}$ is from $d \rightarrow u\mu\nu$ transitions, while for the other operators, $Q_{1F,2i}^{(6)}$, $Q_{6F,2i}^{(6)}$, $Q_{7F,2i}^{(6)}$, it is mainly from neutrino scattering. The severe bounds from transitions involving charged leptons can be avoided in the special case, where $C_{1F,i}^{(6)} = \frac{1}{4} C_{2F,i}^{(6)}$, with all the other Wilson coefficients zero, since then the quarks only couple to neutrinos.

Another option is that the leading contributions arise from dimension eight operators with two Higgs insertions (see also, e.g., [91]),

$$Q_{1F',i}^{(8)} = (\bar{L}_L \tilde{H} \gamma_\mu \tilde{H}^\dagger L_L) (\bar{Q}_L^i \gamma^\mu Q_L^i) , \quad Q_{2F'}^{(8)} = (\bar{L}_L \tilde{H} \gamma_\mu \tilde{H}^\dagger L_L) (\bar{L}_L \gamma^\mu L_L) , \quad (123)$$

$$Q_{3F'}^{(8)} = (\bar{L}_L \tilde{H} \gamma_\mu \tilde{H}^\dagger L_L) (\bar{e}_R \gamma^\mu e_R) , \quad Q_{4F'}^{(8)} = (\bar{L}_L \tilde{H} \gamma_\mu \tilde{H}^\dagger L_L) (\bar{u}_R \gamma^\mu u_R) , \quad (124)$$

$$Q_{5F',i}^{(8)} = (\bar{L}_L \tilde{H} \gamma_\mu \tilde{H}^\dagger L_L) (\bar{d}_R^i \gamma^\mu d_R^i) . \quad (125)$$

After the Higgs obtains a vev only the neutrino is projected out of the lepton doublet, $\tilde{H}^\dagger L_L \rightarrow \nu_L v_{\text{EW}}/\sqrt{2}$. The Wilson coefficients for low energy dimension 6 operators are in this case,

$$\hat{\mathcal{C}}_{1(2),u_1}^{(6)} = \frac{v_{\text{EW}}^2}{2\Lambda^4} \left(\pm C_{1F',1}^{(8)} + C_{4F'}^{(8)} \right), \quad \hat{\mathcal{C}}_{1(2),d_i}^{(6)} = \frac{v_{\text{EW}}^2}{2\Lambda^4} \left(\pm C_{1F',i}^{(8)} + C_{5F'}^{(8)} \right), \quad (126)$$

$$\hat{\mathcal{C}}_{1(2),e}^{(6)} = \frac{v_{\text{EW}}^2}{2\Lambda^4} \left[\pm C_{2F'}^{(8)} + C_{3F'}^{(8)} \right]. \quad (127)$$

Since these operators only lead to couplings of quarks to the neutrinos and not to charged leptons, this relaxes some of the bounds. The remaining bounds are “inevitable”, as they come from processes that involve neutrinos – these are the bounds discussed at the end of Section VID.

The gauge-gauge operators in (5) and (6) can arise from dimension eight operators

$$Q_{1B}^{(8)} = \frac{\alpha_1}{12\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) B^{\mu\nu} B_{\mu\nu}, \quad Q_{2B}^{(8)} = \frac{\alpha_1}{8\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) B^{\mu\nu} \tilde{B}_{\mu\nu}, \quad (128)$$

$$Q_{1W}^{(8)} = \frac{\alpha_2}{12\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) W^{a,\mu\nu} W_{\mu\nu}^a, \quad Q_{2W}^{(8)} = \frac{\alpha_2}{8\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) W^{a,\mu\nu} \tilde{W}_{\mu\nu}^a, \quad (129)$$

$$Q_{3W}^{(8)} = \frac{\alpha_{12}}{12\pi} (\bar{\nu}_R \tilde{H}^\dagger \tau^a L_L) W^{a,\mu\nu} B_{\mu\nu}, \quad Q_{4W}^{(8)} = \frac{\alpha_{12}}{8\pi} (\bar{\nu}_R \tilde{H}^\dagger \tau^a L_L) W^{a,\mu\nu} \tilde{B}_{\mu\nu}, \quad (130)$$

$$Q_{1G}^{(8)} = \frac{\alpha_s}{12\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) G^{a,\mu\nu} G_{\mu\nu}^a, \quad Q_{2G}^{(8)} = \frac{\alpha_s}{8\pi} (\bar{\nu}_R \tilde{H}^\dagger L_L) G^{a,\mu\nu} \tilde{G}_{\mu\nu}^a, \quad (131)$$

giving the Wilson coefficients

$$\hat{\mathcal{C}}_{1(2)}^{(7)} = \frac{v_{\text{EW}}}{\sqrt{2}\Lambda^4} \left(C_{1(2)B}^{(8)} + C_{1(2)W}^{(8)} + \frac{1}{2} C_{3(4)W}^{(8)} \right), \quad \hat{\mathcal{C}}_{3(4)}^{(7)} = \frac{v_{\text{EW}}}{\sqrt{2}\Lambda^4} C_{1(2)G}^{(8)}. \quad (132)$$

The reinterpretation of the 8 TeV ATLAS W +MET search, Ref. [92], bounds $Q_{1(2)W}^{(8)}$ to $\Lambda \gtrsim 0.7(0.8)$ TeV [93], while the 7 TeV ATLAS Z +MET search, Ref. [94], gives bounds on $Q_{1B}^{(8)}, \dots, Q_{4W}^{(8)}$ operators of roughly comparable strength, but with the details depending on the relative sizes of photon and Z exchange contributions [95].

The operators (7) and (8) can arise from the following dimension six operators

$$Q_{1R,i}^{(6)} = (\bar{\nu}_R L_L) (\bar{Q}_L^i u_R^i), \quad Q_{2R,i}^{(6)} = (\bar{\nu}_R \sigma_{\mu\nu} L_L) (\bar{Q}_L^i \sigma_{\mu\nu} u_R^i), \quad (133)$$

$$Q_{3R,i}^{(6)} = (\bar{\nu}_R L_L) (\bar{d}_R^i Q_L^i), \quad Q_{4R,i}^{(6)} = (\bar{\nu}_R \sigma_{\mu\nu} L_L) (\bar{d}_R^i \sigma_{\mu\nu} Q_L^i), \quad (134)$$

$$Q_{5R}^{(6)} = (\bar{\nu}_R L_L) (\bar{e}_R L_L), \quad Q_{6R}^{(6)} = (\bar{\nu}_R \sigma_{\mu\nu} L_L) (\bar{e}_R \sigma_{\mu\nu} L_L). \quad (135)$$

The resulting Wilson coefficients are

$$\hat{\mathcal{C}}_{5,u_i(d_i)}^{(7)} = \frac{\text{Re } C_{1(3)R,i}^{(6)}}{2m_{u_i(d_i)} \Lambda^2}, \quad \hat{\mathcal{C}}_{6,u_i(d_i)}^{(7)} = \frac{\text{Im } C_{1(3)R,i}^{(6)}}{2m_{u_i(d_i)} \Lambda^2}, \quad \hat{\mathcal{C}}_{7,u_i(d_i)}^{(7)} = \frac{C_{2(4)R,i}^{(6)}}{2m_{u_i(d_i)} \Lambda^2}, \quad (136)$$

$$\hat{\mathcal{C}}_{5,e}^{(7)} = \frac{\text{Re } C_{5R}^{(6)}}{2m_e \Lambda^2}, \quad \hat{\mathcal{C}}_{6,e}^{(7)} = \frac{\text{Im } C_{5R}^{(6)}}{2m_e \Lambda^2}, \quad \hat{\mathcal{C}}_{7,e}^{(7)} = \frac{C_{6R}^{(6)}}{2m_e \Lambda^2}. \quad (137)$$

The bounds on these chirality flipping operators are quite stringent. For instance, from $pp \rightarrow \ell + \cancel{E}_T + X$ searches at the LHC we can expect bounds on the NP scale of the operators (133)-(135) at the order of $\Lambda \gtrsim \mathcal{O}(5\text{TeV})$ and at the similar level from semileptonic decays of light pseudoscalar mesons. (This estimate is based on the bounds for tensor current SM-EFT operators with left-handed neutrinos obtained in [96], which only give quadratic corrections to the SM rates, as do the operators (133)-(135). A dedicated analysis of operators with right-handed neutrinos is called for, which, however, is beyond the scope of our work.)

No such bounds exist for dimension eight operators,

$$Q_{1H,i}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger L_L) (\bar{Q}_L^i \tilde{H} u_R^i), \quad Q_{2H,i}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger L_L) (\bar{Q}_L^i \tilde{H} \sigma_{\mu\nu} u_R^i), \quad (138)$$

$$Q_{3H,i}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger L_L) (\bar{Q}_L^i H d_R^i), \quad Q_{4H,i}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger L_L) (\bar{Q}_L^i H \sigma_{\mu\nu} d_R^i), \quad (139)$$

$$Q_{5H}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger L_L) (\bar{L}_L H e_R), \quad Q_{6H}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger L_L) (\bar{L}_L H \sigma_{\mu\nu} e_R). \quad (140)$$

$$Q_{7H,i}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger \tau^a L_L) (\bar{Q}_L^i \tau^a \tilde{H} u_R^i), \quad Q_{8H,i}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger \tau^a L_L) (\bar{Q}_L^i \tau^a \tilde{H} \sigma_{\mu\nu} u_R^i), \quad (141)$$

$$Q_{9H,i}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger \tau^a L_L) (\bar{Q}_L^i \tau^a H d_R^i), \quad Q_{10H,i}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger \tau^a L_L) (\bar{Q}_L^i \tau^a H \sigma_{\mu\nu} d_R^i), \quad (142)$$

$$Q_{11H}^{(8)} = (\bar{\nu}_R \tilde{H}^\dagger \tau^a L_L) (\bar{L}_L \tau^a H e_R), \quad Q_{12H}^{(8)} = (\bar{\nu}_R \sigma_{\mu\nu} \tilde{H}^\dagger \tau^a L_L) (\bar{L}_L \tau^a H \sigma_{\mu\nu} e_R), \quad (143)$$

which, after the Higgs obtains the vev, have the form $(\bar{\nu}_R \dots \nu_L)(\bar{f} \dots f)$. The relevant constraints on these operators thus come only from neutrino scattering experiments, discussed in the previous section. In principle there are also constraints from Higgs decaying to four body final states, $h \rightarrow 2j\nu\bar{\nu}$. However, these are at present much less constraining.

The Wilson coefficients of the low energy EFT operators (7) and (8), generated from the above operators, are

$$\hat{\mathcal{C}}_{5\{6\},u_i}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_{u_i}} \text{Re}\{\text{Im}\} \left(C_{1H,i}^{(8)} + \frac{1}{4} C_{7H,i}^{(8)} \right), \quad \hat{\mathcal{C}}_{7,u_i}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_{u_i}} \left(C_{2H,i}^{(8)} + \frac{1}{4} C_{8H,i}^{(8)} \right), \quad (144)$$

$$\hat{\mathcal{C}}_{5\{6\},d_i}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_{d_i}} \text{Re}\{\text{Im}\} \left(C_{3H,i}^{(8)} + \frac{1}{4} C_{9H,i}^{(8)} \right), \quad \hat{\mathcal{C}}_{7,d_i}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_{d_i}} \left(C_{4H,i}^{(8)} + \frac{1}{4} C_{10H,i}^{(8)} \right), \quad (145)$$

$$\hat{\mathcal{C}}_{5\{6\},e}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_e} \text{Re}\{\text{Im}\} \left(C_{5H}^{(8)} + \frac{1}{4} C_{11H}^{(8)} \right), \quad \hat{\mathcal{C}}_{7,e}^{(7)} = \frac{1}{\Lambda^4} \frac{v_{\text{EW}}^2}{2m_e} \left(C_{6H}^{(8)} + \frac{1}{4} C_{12H}^{(8)} \right). \quad (146)$$

Finally, the dimension 7 low energy EFT operators with derivatives on the neutrino current, Eqs. (9) and (10), can arise from the following electroweak EFT dimension 8 operators,

$$Q_{1D,i}^{(8)} = \partial_\mu (\bar{\nu}_R \sigma^{\mu\nu} \tilde{H}^\dagger L_L) (\bar{Q}_L^i \gamma_\nu Q_L^i), \quad Q_{2D,i}^{(8)} = (\bar{\nu}_R i \overleftrightarrow{\partial}_\mu \tilde{H}^\dagger L_L) (\bar{Q}_L^i \gamma^\mu Q_L^i), \quad (147)$$

$$Q_{3D}^{(8)} = \partial_\mu (\bar{\nu}_R \sigma^{\mu\nu} \tilde{H}^\dagger L_L) (\bar{L}_L \gamma_\nu L_L), \quad Q_{4D}^{(8)} = (\bar{\nu}_R i \overleftrightarrow{\partial}_\mu \tilde{H}^\dagger L_L) (\bar{L}_L \gamma^\mu L_L), \quad (148)$$

$$Q_{5D,i}^{(8)} = \partial_\mu (\bar{\nu}_R \sigma^{\mu\nu} \tilde{H}^\dagger L_L) (\bar{u}_R^i \gamma_\nu u_R^i), \quad Q_{6D,i}^{(8)} = (\bar{\nu}_R i \overleftrightarrow{\partial}_\mu \tilde{H}^\dagger L_L) (\bar{u}_R^i \gamma^\mu u_R^i), \quad (149)$$

$$Q_{7D,i}^{(8)} = \partial_\mu (\bar{\nu}_R \sigma^{\mu\nu} \tilde{H}^\dagger L_L) (\bar{d}_R^i \gamma_\nu d_R^i), \quad Q_{8D,i}^{(8)} = (\bar{\nu}_R i \overleftrightarrow{\partial}_\mu \tilde{H}^\dagger L_L) (\bar{d}_R^i \gamma^\mu d_R^i), \quad (150)$$

$$Q_{9D}^{(8)} = \partial_\mu (\bar{\nu}_R \sigma^{\mu\nu} \tilde{H}^\dagger L_L) (\bar{e}_R \gamma_\nu e_R), \quad Q_{10D}^{(8)} = (\bar{\nu}_R i \overleftrightarrow{\partial}_\mu \tilde{H}^\dagger L_L) (\bar{e}_R \gamma^\mu e_R). \quad (151)$$

After the Higgs obtains the vev, the operators have the form of (neutrino current) $\times$ (charged fermion current). The most relevant bounds on these operators are, again, due to neutrino scattering experiments discussed in the previous Sections. The matching gives for the low energy Wilson coefficients

$$\hat{C}_{8\{9\},u_i}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{2D,i}^{(8)} + C_{6D,i}^{(8)} \right), \quad \hat{C}_{10\{11\},u_i}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{1D,i}^{(8)} + C_{5D,i}^{(8)} \right), \quad (152)$$

$$\hat{C}_{8\{9\},d_i}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{2D,i}^{(8)} + C_{8D,i}^{(8)} \right), \quad \hat{C}_{10\{11\},d_i}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{1D,i}^{(8)} + C_{7D,i}^{(8)} \right), \quad (153)$$

$$\hat{C}_{8\{9\},e}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{4D}^{(8)} + C_{10D}^{(8)} \right), \quad \hat{C}_{10\{11\},e}^{(7)} = \frac{v_{\text{EW}}}{\Lambda^4} \text{Re}\{\text{Im}\} \left(C_{3D}^{(8)} + C_{9D}^{(8)} \right). \quad (154)$$

VIII. CONCLUSIONS

In this manuscript we obtained predictions for CE ν NS in the presence of nonstandard neutrino interactions described by an EFT at 2 GeV. Our analysis covers the complete basis of EFT operators up to and including dimension 7, and thus covers most of the viable models as long as the mediators are heavier than about 100 MeV. We recast the recent measurement of CE ν NS by the COHERENT collaboration using a CsI detector to obtain bounds on the EFT operators, assuming that only one NSI operator at the time contributes appreciably. The main results are collected in Figures 6 and 7, where they are compared with the bounds on NSI from neutrino oscillations, the solar neutrino flux measurements at Borexino, and from deep inelastic scattering. The obtained bounds apply to incoming electron or muon neutrinos scattering either through flavor diagonal interaction, or even, if the neutrino flavor changes (including scattering to sterile neutrinos).

We see that already now the CE ν NS measurements lead to the most stringent limits for some of the NSI operators, for instance for scalar currents. The NSI reach of CE ν NS experiments is set to significantly improve in the future, with a number of new experiments either already running or being planned. In Figures 6 and 7 we also show the projected limits for the NaI 2 ton detector planned by the COHERENT collaboration, also assuming

that systematic errors can be decreased by an order of magnitude. The new experiments, as we show in the paper, can also increase their sensitivity to NSI by modifying running conditions, such as the incoming neutrino energy, the nuclear recoil energy thresholds, but also by trying to perform measurements at higher recoil energies. For this it will be important to investigate how well one can distinguish between NSI and the subleading corrections to our predictions (for instance from q^2 dependence of nuclear form factors away from zero recoil point, see, e.g., [97]).

When using our results it is important to note their validity. The DIS bounds assume that the mediators are heavier than a few 10s of GeV, the COHERENT bounds that they are heavier than about 100 MeV, while Borexino and oscillation bounds apply also to very light mediators (a typical momentum exchange in solar neutrinos scattering on electrons in Borexino is $q \sim \text{few } 100 \text{ keV} - 1 \text{ MeV}$, which sets the lower bound on mediator mass, such that use of EFT is justified for interpreting Borexino measurement). For light mediators, with masses below 10 GeV the bounds from DIS would get suppressed, and similarly for COHERENT bounds for mediators lighter than a few 10s MeV. It is easy to recast our bounds also in such cases, but one does need at least simplified models for the mediators in that case (some examples are, e.g., [98–100]). More challenging would be to extend our work to the intermediate range of $q^2 \sim (\text{few}) \text{ GeV}^2$, where neither ChPT methods that we used, nor the factorization used for DIS, apply. The benefit, on the other hand, is that many of the neutrino experiments are taking data precisely in this theoretical difficult intermediate regime, so that any theoretical advances would be highly desired.

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Appendix A: Nucleon form factors and nonrelativistic limits

The nucleon form factors, F_i , in Eqs. (22)-(28), are defined as [42],

$$\langle N' | \bar{q} \gamma^\mu q | N \rangle = \bar{u}'_N \left[F_1^{q/N}(q^2) \gamma^\mu + \frac{i}{2m_N} F_2^{q/N}(q^2) \sigma^{\mu\nu} q_\nu \right] u_N, \quad (\text{A1})$$

$$\langle N' | \bar{q} \gamma^\mu \gamma_5 q | N \rangle = \bar{u}'_N \left[F_A^{q/N}(q^2) \gamma^\mu \gamma_5 + \frac{1}{2m_N} F_{P'}^{q/N}(q^2) \gamma_5 q^\mu \right] u_N, \quad (\text{A2})$$

$$\langle N' | m_q \bar{q} q | N \rangle = F_S^{q/N}(q^2) \bar{u}'_N u_N, \quad (\text{A3})$$

$$\langle N' | m_q \bar{q} i \gamma_5 q | N \rangle = F_P^{q/N}(q^2) \bar{u}'_N i \gamma_5 u_N, \quad (\text{A4})$$

$$\langle N' | \frac{\alpha_s}{12\pi} G^{a\mu\nu} G_{\mu\nu}^a | N \rangle = F_G^N(q^2) \bar{u}'_N u_N, \quad (\text{A5})$$

$$\langle N' | \frac{\alpha_s}{8\pi} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a | N \rangle = F_{\tilde{G}}^N(q^2) \bar{u}'_N i \gamma_5 u_N, \quad (\text{A6})$$

$$\begin{aligned} \langle N' | m_q \bar{q} \sigma^{\mu\nu} q | N \rangle = \bar{u}'_N & \left[F_{T,0}^{q/N}(q^2) \sigma^{\mu\nu} + \frac{i}{2m_N} \gamma^{[\mu} q^{\nu]} F_{T,1}^{q/N}(q^2) \right. \\ & \left. + \frac{i}{m_N^2} q^{[\mu} k_{12}^{\nu]} F_{T,2}^{q/N}(q^2) \right] u_N, \end{aligned} \quad (\text{A7})$$

where we suppressed the dependence of nucleon states on their momenta, $\langle N' | \equiv \langle N(k_2) |$, $|N\rangle \equiv |N(k_1)\rangle$, and similarly, $\bar{u}'_N \equiv u_N(k_2)$, $u_N \equiv u_N(k_1)$, while $k_{12}^\mu = k_1^\mu + k_2^\mu$ and $q^\mu = k_2^\mu - k_1^\mu$, and $\gamma^{[\mu} q^{\nu]} = \gamma^\mu q^\nu - q^\mu \gamma^\nu$.

The form factors, F_i , are functions of q^2 only.

In the derivations of Eqs. (22)-(28) a non-relativistic reduction of nucleon currents is required. Counting $v \cdot \partial \sim \mathcal{O}(q^2)$, with q the typical soft three-momentum, the leading terms are [42]

$$\bar{N} N \rightarrow \bar{N}_v N_v + \mathcal{O}(q^2), \quad (\text{A8})$$

$$\bar{N} i \gamma_5 N \rightarrow \frac{1}{m_N} \partial_\mu (\bar{N}_v S_N^\mu N_v) + \mathcal{O}(q^3), \quad (\text{A9})$$

$$\bar{N} \gamma^\mu N \rightarrow v^\mu \bar{N}_v N_v + \mathcal{O}(q), \quad (\text{A10})$$

$$\bar{N} \gamma^\mu \gamma_5 N \rightarrow 2 \bar{N}_v S_N^\mu N_v + \mathcal{O}(q^2), \quad (\text{A11})$$

$$\bar{N} \sigma^{\mu\nu} N \rightarrow \bar{N}_v \sigma_\perp^{\mu\nu} N_v + \mathcal{O}(q), \quad (\text{A12})$$

$$\bar{N} \sigma^{\mu\nu} i \gamma_5 N \rightarrow 2 \bar{N}_v S_N^{[\mu} v^{\nu]} N_v + \mathcal{O}(q). \quad (\text{A13})$$

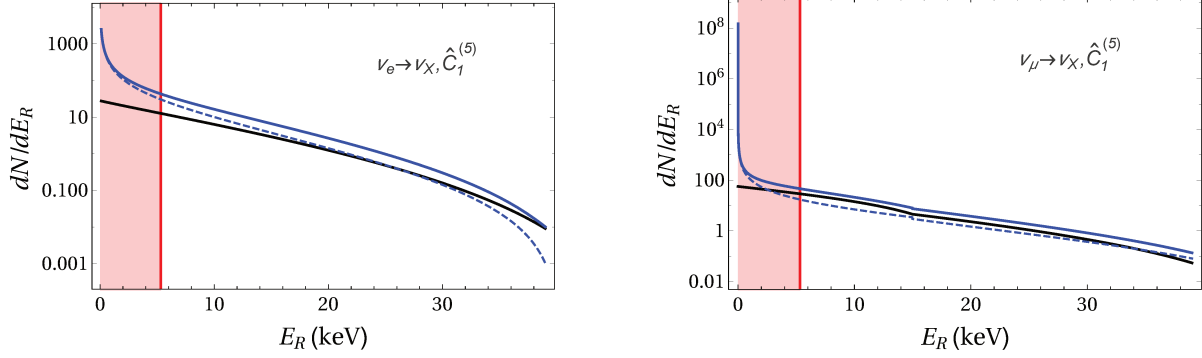


Figure 9: The $\nu_e \rightarrow \nu_X$ (left) and $\nu_\mu \rightarrow \nu_X$ (right) rates in the COHERENT CsI detector including $\mathcal{Q}_1^{(5)}$ NSI operator contribution, for $\hat{C}_a^{(5)} = 1/\Lambda_{a,\min}$, where $\Lambda_{a,\min}$ is taken to be the corresponding lower bound in Tables II and III, respectively. The SM rate is denoted by the solid black line, dashed blue line denotes the NSI only prediction, and solid blue line the sum of the two. The vertical red line denotes the energy threshold of the detector.

Appendix B: The NSI predictions for differential rates in COHERENT

In this appendix we show the differential scattering rates in the presence of NSI, dN/dE_R , for the CsI[Ti] detector of the COHERENT collaboration. In the numerical evaluations only one NSI operator, Eqs. (3)-(10), is taken to be nonzero. We set its Wilson coefficient to

$$\hat{\mathcal{C}}_a^{(d)} = \left(\frac{1}{\Lambda_{a,\min}} \right)^{d-4}, \quad (\text{B1})$$

where $\Lambda_{a,\min}$ is the current lower limit for this operator, as obtained in Section VIB from the COHERENT measurement, and listed in Tables III and II.

The predicted differential scattering rates, dN/dE_R , Eq. (89), are plotted in Figures 9-12. For the nuclear response functions, W_i , we use the values from [44], while the value of nuclear form factors are taken from [42]. In Figures 9-12 we show separately the scattering rates due to the ν_e (left panels) and $\nu_\mu + \bar{\nu}_\mu$ (right panels) incoming neutrinos. The corresponding fluxes are given in Eqs. (86)-(88). Note from eq. (24) that the operators $\mathcal{Q}_{8,q}^{(7)}$ and $\mathcal{Q}_{10,q}^{(7)}$ have the same matrix element and will give rise to the same differential scattering rate; same happens for the operators $\mathcal{Q}_{9,q}^{(7)}$ and $\mathcal{Q}_{11,q}^{(7)}$, see eq. (26).

The neutrinos are due to stopped muons, which sets the maximal recoil energy, $E_{R,\max}$, to be around 47 keV for $\nu_e \rightarrow \nu_X$ and $\bar{\nu}_\nu \rightarrow \nu_X$, and about 15 keV for $\nu_\mu \rightarrow \nu_X$ transitions. The muon neutrino flux is monoenergetic, with $E_\nu \approx 30$ MeV. As a consequence, for $\bar{\nu}_\mu \rightarrow \nu_X$

scattering there is an abrupt drop in the predicted differential rate, dN/dE_R , at $E_R \approx 15$ keV, since none of the $\bar{\nu}_\mu$ can contribute to more energetic recoils. This discontinuity is clearly visible for $\mathcal{Q}_{2,q}^{(6)}$, see Fig. 10 bottom right, $\mathcal{Q}_1^{(7)}, \dots, \mathcal{Q}_4^{(7)}$, see Fig. 11 right, and for $\mathcal{Q}_{5,q}^{(7)}, \dots, \mathcal{Q}_{8(10),q}^{(7)}$, see Figures 12 right, and Fig. 13 upper right.

For SM prediction there is no such discontinuity in dN/dE_R at $E_R \approx 15$ keV, but rather only a change in the slope of dN/dE_R . The spin-independent scattering induced by the SM neutrino interaction with quarks contains the kinematical pre-factor $(2E_\nu^2 - \vec{q}^2)$, see the coefficient of $c_{1,\tau}^{(0)} c_{1,\tau'}^{(0)*}$ in (42). This prefactor goes to zero when the maximal E_R for given value of E_ν is reached, i.e., when the incoming neutrinos backscatter. This means that the contribution from $\bar{\nu}_\mu \rightarrow \nu_X$ to the SM dN/dE_R scattering rate goes to zero at $E_R \approx 15$ keV.

In order to obtain the number of events predicted in the CsI[Tl] COHERENT experiment the predictions in the left and the right panels of Figs. 9-12 need to be added up, and then convoluted with the signal acceptance fraction of the detector. At present the acceptance has a lower threshold at around 4.25 keV, denoted as a vertical red line in Figures 9-12.

From the figures we see that a number of operators lead to a significantly different E_R dependence compared to the SM predictions. The magnetic dipole moment leads to dN/dE_R that has a pole at $\vec{q}^2 = 0$, clearly showing a significant increase in the rate at small values of E_R , see Fig. 9. Lowering the energy threshold can thus lead to an increase sensitivity to this NSI operator, as long as the background can be kept low. In other case probing larger recoils may be beneficial. For instance, the scattering matrix element due to $\mathcal{Q}_{1,s}^{(6)}$ is proportional to $F_1^{s/N'}(0)\vec{q}^2$ and thus grows with the increased E_R , see Fig. 10 (top). A dedicated analysis is required to see to what extent this contribution can be distinguished from the subleading corrections in the SM rate that come from the q^2 dependence of the $F_1^{u/N}$ and $F_1^{d/N}$ form factors, and from the uncertainties in the nuclear response function W_M .

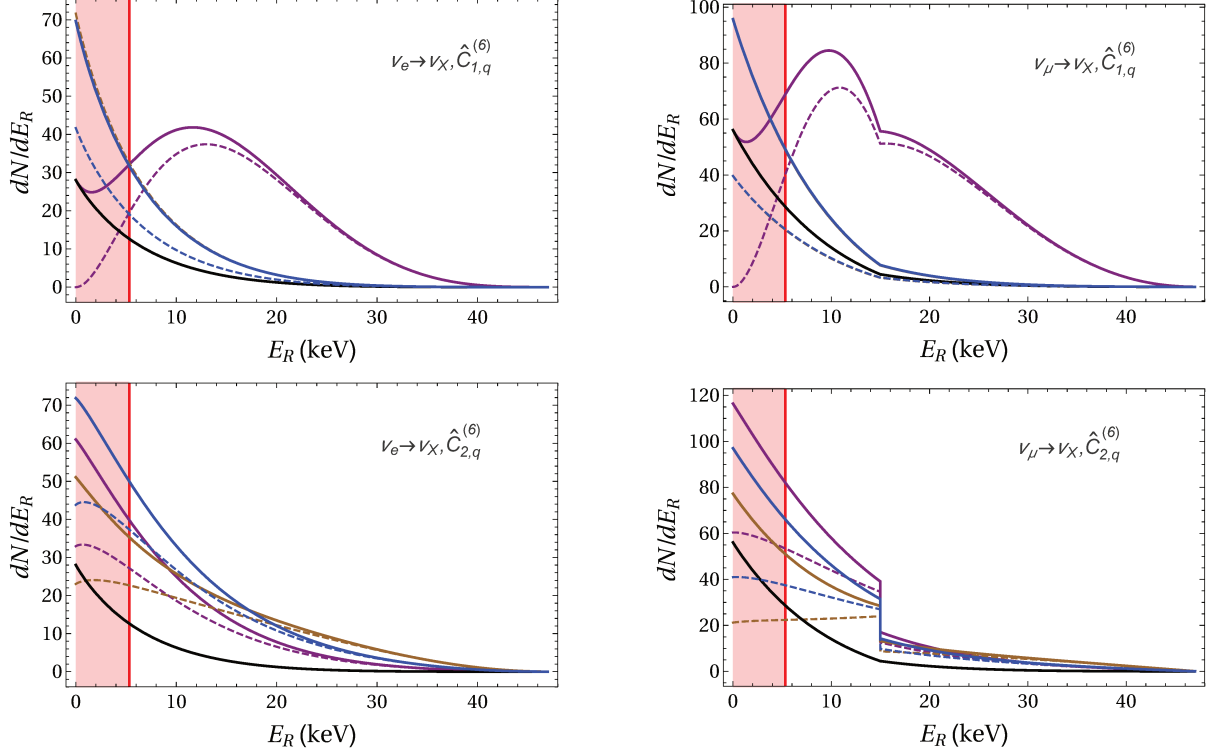


Figure 10: The $\nu_e \rightarrow \nu_e$ (left) and $\nu_\mu \rightarrow \nu_\mu$ (right) scattering rates in the presence of a single NSI operator, either $\mathcal{Q}_{1,q}^{(6)}$ (top) or $\mathcal{Q}_{2,q}^{(6)}$ (bottom), setting $\hat{C}_a^{(6)} = 1/\Lambda_{a;\text{min}}^2$, where $\Lambda_{a;\text{min}}$ is taken to be the corresponding lower bound in Tables II and III, respectively. The SM event rate is denoted by the black solid line, dashed lines denote NSI only and solid lines the sum of SM and NSI contributions (with blue, brown and purple representing couplings to up, down and strange quark currents, respectively). The energy threshold of the experiment is denoted by the vertical red line.

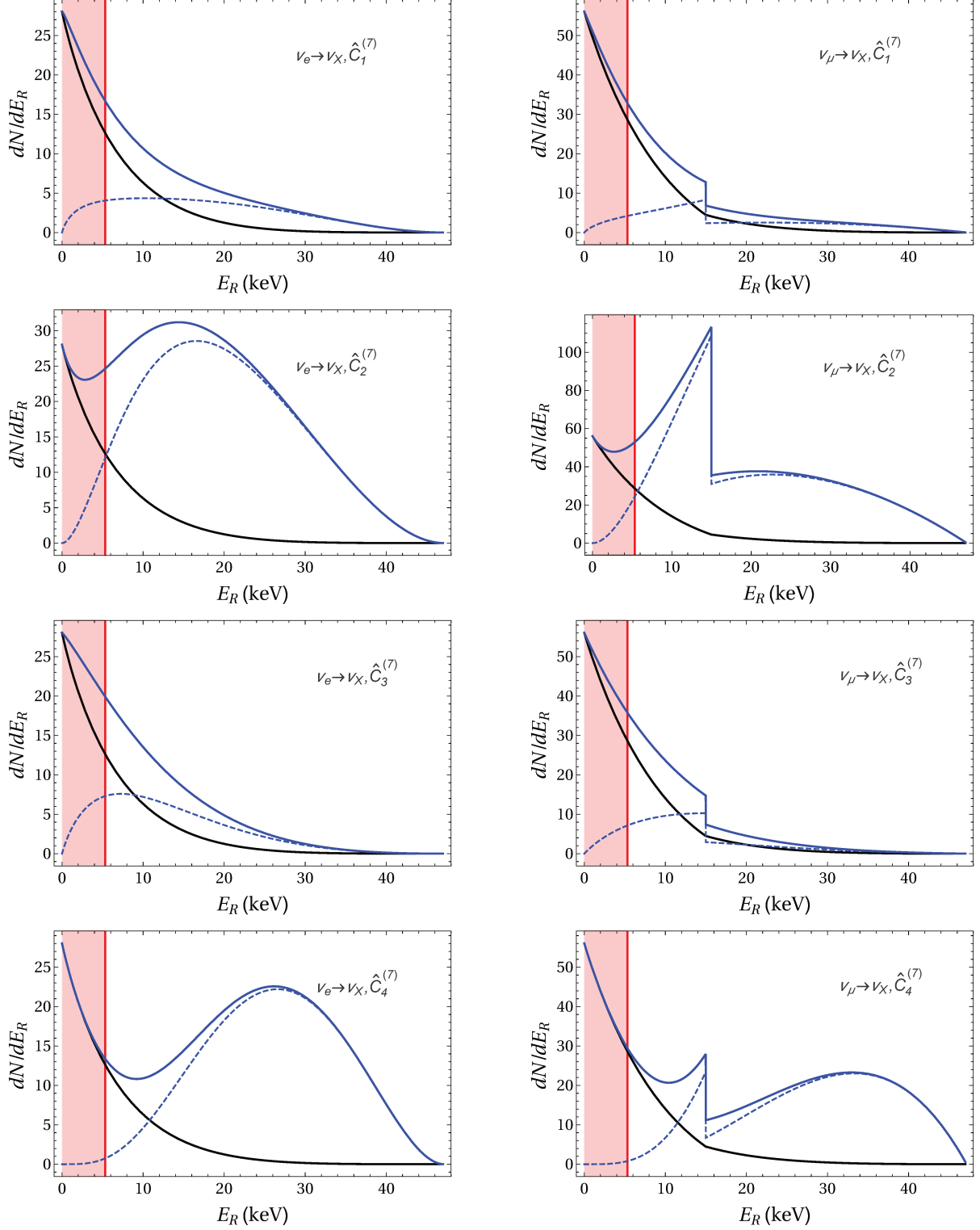


Figure 11: The $\nu_e \rightarrow \nu_X$ (left) and $\nu_\mu \rightarrow \nu_X$ scattering rates in COHERENT CsI detector in the presence of NSI operators $\mathcal{Q}_1^{(7)}$, $\mathcal{Q}_2^{(7)}$, $\mathcal{Q}_3^{(7)}$, $\mathcal{Q}_4^{(7)}$ (top to bottom) setting $\hat{C}_a^{(7)} = 1/\Lambda_{a,\min}^3$. The notation is as in Fig. 9.

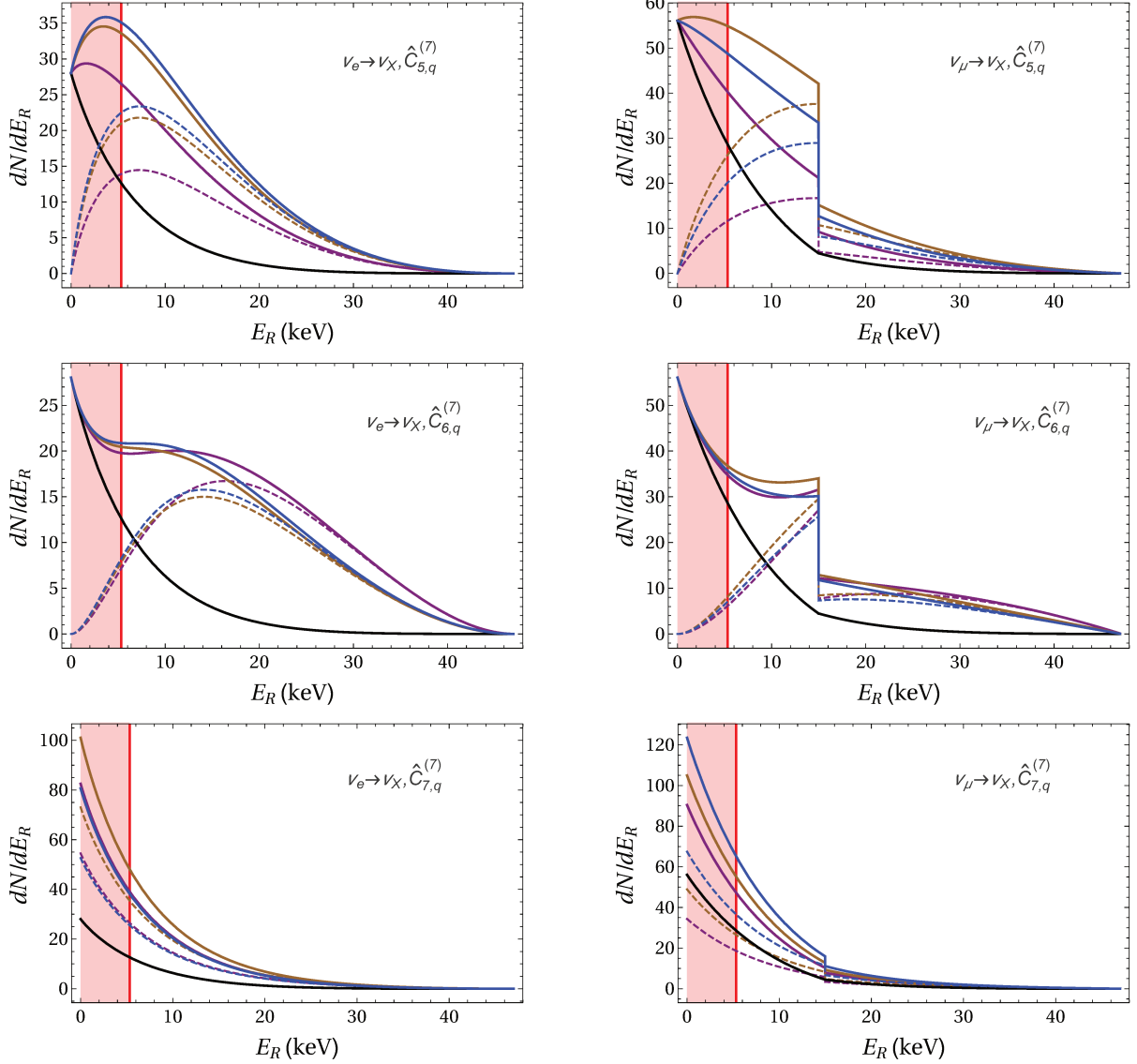


Figure 12: The $\nu_e \rightarrow \nu_X$ (left) and $\nu_\mu \rightarrow \nu_X$ scattering rates in COHERENT CsI detector in the presence of NSI operators $\mathcal{Q}_{5,q}^{(7)}$, $\mathcal{Q}_{6,q}^{(7)}$, $\mathcal{Q}_{7,q}^{(7)}$, (top to bottom) setting $\hat{C}_a^{(7)} = 1/\Lambda_{a;\min}^3$. The notation is as in Fig. 10.

A very striking difference in the kinematical dependence of dN/dE_R arises in the case of monoenergetic neutrino beams, as already mentioned above. This can be seen in Figures 10-13 (right panels). Observing experimentally any such discontinuity would be a clear signal for the presence of NSI. The discontinuity is especially pronounced for $\mathcal{Q}_2^{(7)}$, $\mathcal{Q}_4^{(7)}$, Fig. 11, and $\mathcal{Q}_{6,q}^{(7)}$, Fig. 12, since these operators contribute to the non-relativistic operator $\mathcal{O}_{1,N}^{(1)}$, see Eqs. (26), (53). This leads to an additional $\vec{q}^4$ dependence in the scattering rate, see Eq. (42). For NSI generated by $\mathcal{Q}_2^{(7)}$, $\mathcal{Q}_4^{(7)}$, or $\mathcal{Q}_{6,q}^{(7)}$ operators the sensitivity increases for higher

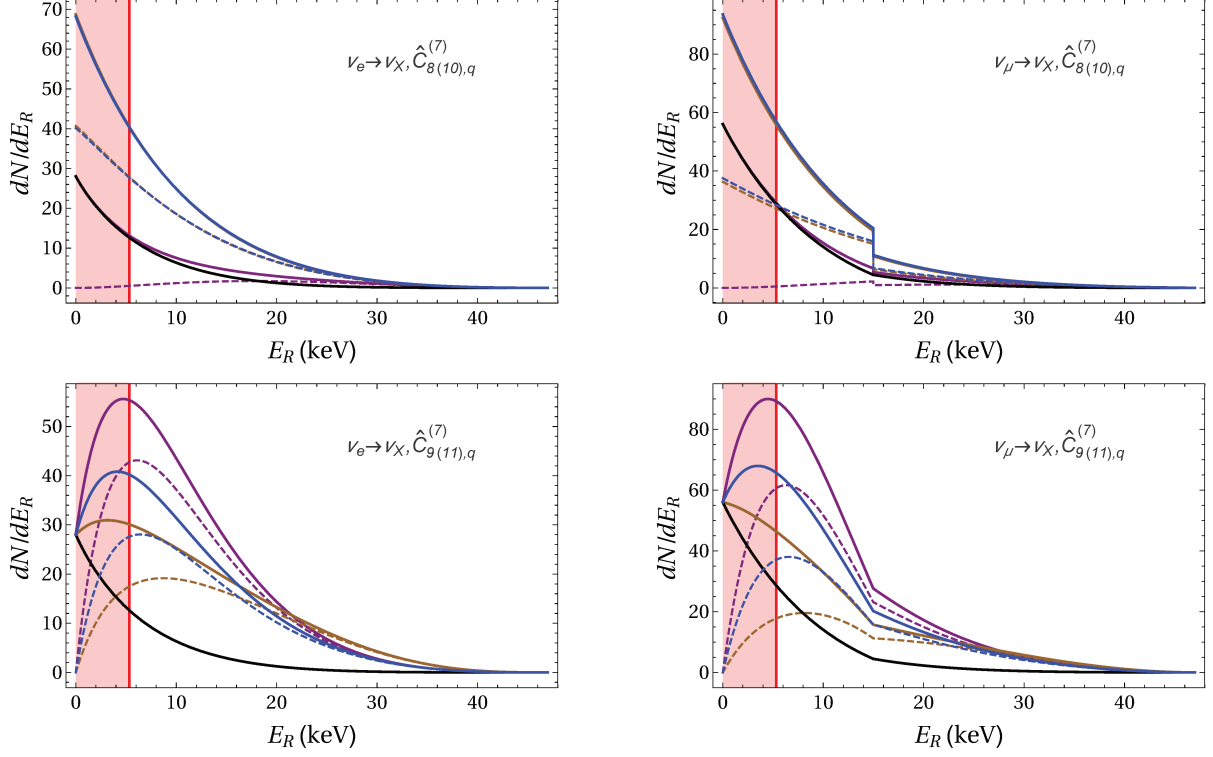


Figure 13: Same as Fig. 12 but for $\mathcal{Q}_{8,q}^{(7)}$ (top) and $\mathcal{Q}_{9,q}^{(7)}$ (bottom).

E_R recoils. $\mathcal{Q}_2^{(7)}$, $\mathcal{Q}_4^{(7)}$, or $\mathcal{Q}_{6q}^{(7)}$ operators the sensitivity increases for higher E_R recoils. This was also illustrated in the main text, in Fig. 8.

The operators $\mathcal{Q}_1^{(7)}$, $\mathcal{Q}_3^{(7)}$ and $\mathcal{Q}_{5,q}^{(7)}$ match onto the nonrelativistic operator $\mathcal{O}_{3,N}^{(0)}$ which leads to a $\vec{q}^2$ prefactor in the scattering rate instead of the $4E_\nu^2 - \vec{q}^2$ one for the SM, see Eq. (41). This different E_R dependence clearly shows in Figures 11 and 12 (left panels). Similar comment applies to the $\mathcal{Q}_{9,q}^{(7)}$ operator, which matches onto $\mathcal{O}_{2,N}^{(1)}$, which leads to a kinematic prefactor E_R^2 in the scattering event rate, cf. Eq. 42, and thus a very different recoil dependence compared to the SM rate, see Fig. 13.

Appendix C: Numerical values of CE ν NS scattering cross sections

In this appendix we provide numerical expressions for CE ν NS differential cross sections in the presence of a single nonzero NSI operator $\mathcal{Q}_a^{(d)}$. We normalize the NSI cross sections to the SM, so that they take the form

$$\frac{(d\sigma/dE_R)_{\text{NSI}}}{(d\sigma/dE_R)_{\text{SM}}} = 1 + g_a^{(d)}(E_\nu, E_R)\hat{\mathcal{C}}_a^{(d)} + f_a^{(d)}(E_\nu, E_R)|\hat{\mathcal{C}}_a^{(d)}|^2. \quad (\text{C1})$$

These expressions are valid for any neutrino flavor scattering on nuclei, $\nu_\alpha A \rightarrow \nu_\beta A$. Here E_ν is the energy of incoming neutrino, and E_R the recoil energy of the nucleus.

Below we give the numerical values for the coefficients $g_a^{(d)}$ and $f_a^{(d)}$ for CE ν NS on nuclei ^{23}Na , Ge, ^{127}I and Xe. For Germanium and Xenon we calculate the average cross sections for natural abundance of stable isotopes, namely ^{70}Ge , ^{72}Ge , ^{73}Ge , ^{74}Ge and ^{76}Ge for Germanium and ^{128}Xe , ^{129}Xe , ^{130}Xe , ^{131}Xe , ^{132}Xe and ^{134}Xe for Xenon. For the numerical evaluation we use the nuclear response functions from [43, 44]. We only quote central values for the coefficients $g_a^{(d)}$ and $f_a^{(d)}$, but comment when these estimates are particularly uncertain.

Since only dimension 6 operators interfere with the SM amplitude for CE ν NS, these are the only ones that have both $g_a^{(d)}$ and $f_a^{(d)}$ nonzero, while for dimension 5 and dimension 7 operators $g_a^{(d)} = 0$. are the dimension six operators. For dimension 6 operators we provide the $g_a^{(d)}$ and $f_a^{(d)}$ functions both for the NSI notation that uses the ε parameters and for our notation with the canonically normalized Wilson coefficients. In the results we only keep the lowest order in E_R in the expressions of $g_{a,q}^{(d)}(E_\nu, E_R)$ and $f_{a,q}^{(d)}(E_\nu, E_R)$. These quoted results for these functions are thus reliable for recoil energies up to $E_R \sim 10 - 20$ keV, while for higher energies one needs to take into account corrections from higher powers of E_R .

1. Numerical results for CE ν NS on ^{23}Na

To shorten the notation we define the following functions of incoming neutrino energy, E_ν , and nuclear recoil, E_R ,

$$D = [(E_\nu/\text{MeV})^2 - 10.8(E_R/\text{keV})]^{-1}, \quad (\text{C2})$$

$$R_A = [(E_\nu/\text{MeV})^2 + 10.8(E_R/\text{keV})]D, \quad \text{for CE}\nu\text{NS on } ^{23}\text{Na}. \quad (\text{C3})$$

$$R_T = [(E_\nu/\text{MeV})^2 - 7.97(E_R/\text{keV})]D, \quad (\text{C4})$$

We first give the results for NSI parametrized by ε_i , Eq. (1). Using ε_i , instead of the Wilson coefficients $\hat{\mathcal{C}}_{1,q(2,q)}^{(6)}$ in Eq. (C1), the corresponding coefficients are

$$g_\varepsilon^{uV} = -12.2, \quad f_\varepsilon^{uV} = 37.0, \quad (\text{C5})$$

$$g_\varepsilon^{dV} = -12.5, \quad f_\varepsilon^{dV} = 39.2, \quad (\text{C6})$$

$$g_\varepsilon^{sV} = 3.20 \cdot 10^{-6} \left(\frac{E_R}{\text{keV}} \right), \quad f_\varepsilon^{sV} = 2.56 \cdot 10^{-12} \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C7})$$

$$g_\varepsilon^{uA} = 1.86 \cdot 10^{-3} R_A, \quad f_\varepsilon^{uA} = 1.34 \cdot 10^{-3} R_A, \quad (\text{C8})$$

$$g_\varepsilon^{dA} = -6.53 \cdot 10^{-4} R_A, \quad f_\varepsilon^{dA} = 1.65 \cdot 10^{-4} R_A, \quad (\text{C9})$$

$$g_\varepsilon^{sA} = -7.19 \cdot 10^{-5} R_A, \quad f_\varepsilon^{sA} = 2.00 \cdot 10^{-6} R_A, \quad (\text{C10})$$

where the function R_A for $\text{CE}\nu\text{NS}$ on ^{23}Na is given in (C3).

We give next the results for NSI induced scattering rates for dimension 5, 6 and 7 operators. For dimension 5 operator the nonzero coefficient in the $\text{CE}\nu\text{NS}$ scattering cross section, Eq. (C1), is for ^{23}Na

$$f_1^{(5)} = 6.36 \cdot 10^7 \left(\frac{E_\nu}{\text{MeV}}\right)^2 \left(\frac{E_R}{\text{keV}}\right)^{-1} D, \quad (\text{C11})$$

with D given in (C2). For dimension 6 operators the coefficients in Eq. (C1) are for $\text{CE}\nu\text{NS}$ on ^{23}Na

$$g_{1,u}^{(6)} = -1.05 \cdot 10^6, \quad g_{1,d}^{(6)} = -1.08 \cdot 10^6, \quad g_{1,s}^{(6)} = 0.276 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C12})$$

$$f_{1,u}^{(6)} = 2.75 \cdot 10^{11}, \quad f_{1,d}^{(6)} = 2.92 \cdot 10^{11}, \quad f_{1,s}^{(6)} = 1.90 \cdot 10^{-2} \left(\frac{E_R}{\text{keV}}\right)^2, \quad (\text{C13})$$

$$g_{2,u}^{(6)} = 1.61 \cdot 10^2 R_A, \quad g_{2,d}^{(6)} = -56.3 R_A, \quad g_{2,s}^{(6)} = -6.20 R_A, \quad (\text{C14})$$

$$f_{2,u}^{(6)} = 9.96 \cdot 10^6 R_A, \quad f_{2,d}^{(6)} = 1.22 \cdot 10^6 R_A, \quad f_{2,s}^{(6)} = 1.49 R_A, \quad (\text{C15})$$

with the R_A function given in (C3). For dimension 7 operators the coefficients are, for $\text{CE}\nu\text{NS}$ on ^{23}Na , given by

$$f_1^{(7)} = -26.3 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_2^{(7)} = 2.44 \cdot 10^{-4} \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C16})$$

$$f_3^{(7)} = 1.34 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_4^{(7)} = 1.05 \cdot 10^{-3} \left(\frac{E_R}{\text{keV}}\right)^4 D, \quad (\text{C17})$$

$$f_{5,u}^{(7)} = 8.65 \cdot 10^7 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,d}^{(7)} = 3.95 \cdot 10^8 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,s}^{(7)} = 5.79 \cdot 10^8 \left(\frac{E_R}{\text{keV}}\right) D, \quad (\text{C18})$$

$$f_{6,u}^{(7)} = 77.3 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,d}^{(7)} = 3.67 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,s}^{(7)} = 59.7 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C19})$$

$$f_{7,u}^{(7)} = 2.79 \cdot 10^2 R_T, \quad f_{7,d}^{(7)} = 80.3 R_T, \quad f_{7,s}^{(7)} = 7.74 \cdot 10^{-2} R_T, \quad (\text{C20})$$

while for operators with derivatives on neutrino currents the coefficients are,

$$f_{8(10),u}^{(7)} = 6.88 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),u}^{(7)} = 4.30 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C21})$$

$$f_{8(10),d}^{(7)} = 7.29 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),d}^{(7)} = 52.8 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C22})$$

$$f_{8(10),s}^{(7)} = 1.90 \cdot 10^{-2} \left(\frac{E_\nu}{\text{MeV}}\right)^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{9(11),s}^{(7)} = 0.642 \left(\frac{E_R}{\text{keV}}\right). \quad (\text{C23})$$

The g coefficients are zero for all dimension 7 operators. The D and R_T functions are given in Eqs. (C2) and (C4), respectively. Note that for the Rayleigh operators in Eq. (C16) we used the NDA estimates from Section III C, which are only very approximate.

2. Numerical results for CE ν NS on Ge

For Germanium we give cross section for natural abundances of Ge in the detector. To shorten the notation we define the following three functions,

$$D = [(E_\nu/\text{MeV})^2 - 34.2(E_R/\text{keV})]^{-1}, \quad (\text{C24})$$

$$R_A = [(E_\nu/\text{MeV})^2 + 34.2(E_R/\text{keV})] D, \quad \text{for CE}\nu\text{NS on Ge}, \quad (\text{C25})$$

$$R_T = [(E_\nu/\text{MeV})^2 - 25.3(E_R/\text{keV})] D. \quad (\text{C26})$$

We start with the results for NSI parametrized by ε_i , Eq. (1). Using ε_i instead of $\hat{\mathcal{C}}_{1,q(2,q)}^{(6)}$ in Eq. (C1), the corresponding coefficients for CE ν NS on Ge are given by

$$g_\varepsilon^{uV} = -10.9, \quad f_\varepsilon^{uV} = 29.7, \quad (\text{C27})$$

$$g_\varepsilon^{dV} = -11.8, \quad f_\varepsilon^{dV} = 35.0, \quad (\text{C28})$$

$$g_\varepsilon^{sV} = 9.33 \cdot 10^{-6} \left(\frac{E_R}{\text{keV}} \right), \quad f_\varepsilon^{sV} = 2.18 \cdot 10^{-11} \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C29})$$

$$g_\varepsilon^{uA} = -8.19 \cdot 10^{-5} R_A, \quad f_\varepsilon^{uA} = -2.42 \cdot 10^{-5} R_A, \quad (\text{C30})$$

$$g_\varepsilon^{dA} = 2.02 \cdot 10^{-4} R_A, \quad f_\varepsilon^{dA} = -1.46 \cdot 10^{-4} R_A, \quad (\text{C31})$$

$$g_\varepsilon^{sA} = -7.15 \cdot 10^{-6} R_A, \quad f_\varepsilon^{sA} = -1.85 \cdot 10^{-7} R_A. \quad (\text{C32})$$

Next, we give the coefficients in the expression for cross section Eq. (C1) using our notation for the NSI operators. The dimension 5 magnetic dipole operator does not interfere with the SM contribution, and thus only has the quadratic term nonzero. For CE ν NS on Ge we have

$$f_1^{(5)} = 1.44 \cdot 10^7 \left(\frac{E_\nu}{\text{MeV}} \right)^2 \left(\frac{E_R}{\text{keV}} \right)^{-1} D, \quad (\text{C33})$$

with D given in (C24). For dimension 6 operators the cross section coefficients for CE ν NS on Ge are given by

$$g_{1,u}^{(6)} = -9.40, \quad f_{1,u}^{(6)} = 2.21 \cdot 10^{11}, \quad (\text{C34})$$

$$g_{1,d}^{(6)} = -1.02 \cdot 10^6, \quad f_{1,d}^{(6)} = 2.60 \cdot 10^{11}, \quad (\text{C35})$$

$$g_{1,s}^{(6)} = 0.804 \left(\frac{E_R}{\text{keV}} \right), \quad f_{1,s}^{(6)} = 1.62 \cdot 10^4 \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C36})$$

$$g_{2,u}^{(6)} = -7.06 R_A, \quad f_{2,u}^{(6)} = -1.80 \cdot 10^5 R_A, \quad (\text{C37})$$

$$g_{2,d}^{(6)} = 17.4 R_A, \quad f_{2,d}^{(6)} = -1.10 \cdot 10^6 R_A, \quad (\text{C38})$$

$$g_{2,s}^{(6)} = -0.616 R_A, \quad f_{2,s}^{(6)} = -1.37 \cdot 10^3 R_A, \quad (\text{C39})$$

where the R_A is given in (C25).

For dimension 7 operators only the f_a^d coefficients in CE ν NS cross section expression are nonzero. For CE ν NS on Ge they are given by

$$f_1^{(7)} = 1.36 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_2^{(7)} = 2.27 \cdot 10^{-4} \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C40})$$

$$f_3^{(7)} = 3.60 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_4^{(7)} = 1.54 \cdot 10^{-3} \left(\frac{E_R}{\text{keV}}\right)^4 D, \quad (\text{C41})$$

$$f_{5,u}^{(7)} = 2.30 \cdot 10^8 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,d}^{(7)} = 1.07 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,s}^{(7)} = 1.56 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad (\text{C42})$$

$$f_{6,u}^{(7)} = 71.8 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,d}^{(7)} = 3.41 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,s}^{(7)} = 55.5 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C43})$$

$$f_{7,u}^{(7)} = 25.5 R_T, \quad f_{7,d}^{(7)} = 7.41 R_T, \quad f_{7,s}^{(7)} = 7.14 \cdot 10^{-3} R_T, \quad (\text{C44})$$

while for dimension 7 operators with derivatives in the neutrino current, the coefficients are

$$f_{8(10),u}^{(7)} = 5.53 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),u}^{(7)} = 24.6 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C45})$$

$$f_{8(10),d}^{(7)} = 6.50 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),d}^{(7)} = 1.50 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C46})$$

$$f_{8(10),s}^{(7)} = 0.162 \left(\frac{E_\nu}{\text{MeV}}\right)^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{9(11),s}^{(7)} = 0.188 \left(\frac{E_R}{\text{keV}}\right). \quad (\text{C47})$$

The D and R_T functions for CE ν NS on Ge are given in (C24) and (C26), respectively. Note that for the Rayleigh operators in Eq. (C40) we used the NDA estimates from Section III C, which are only very approximate.

3. Numerical results for CE ν NS on ^{127}I

In order to shorten the notation we define functions,

$$D = [(E_\nu/\text{MeV})^2 - 59.6(E_R/\text{keV})]^{-1}, \quad (\text{C48})$$

$$R_A = [(E_\nu/\text{MeV})^2 + 59.6(E_R/\text{keV})] D, \quad \text{for CE}\nu\text{NS on } ^{127}\text{I}, \quad (\text{C49})$$

$$R_T = [(E_\nu/\text{MeV})^2 - 44.0(E_R/\text{keV})] D. \quad (\text{C50})$$

The cross section coefficients in Eq. (C1) for CE ν NS on ^{127}I for dimension 6 NSI operators, using the ε_i notation, are given by

$$g_\varepsilon^{uV} = -10.3, \quad f_\varepsilon^{uV} = 26.4, \quad (\text{C51})$$

$$g_\varepsilon^{dV} = -11.5, \quad f_\varepsilon^{dV} = 33.0, \quad (\text{C52})$$

$$g_\varepsilon^{sV} = 1.56 \cdot 10^{-5} \left(\frac{E_R}{\text{keV}}\right), \quad f_\varepsilon^{sV} = 6.05 \cdot 10^{-11} \left(\frac{E_R}{\text{keV}}\right)^2, \quad (\text{C53})$$

$$g_\varepsilon^{uA} = 3.47 \cdot 10^{-5} R_A, \quad f_\varepsilon^{uA} = 3.47 \cdot 10^{-5} R_A, \quad (\text{C54})$$

$$g_\varepsilon^{dA} = 6.69 \cdot 10^{-4} R_A, \quad f_\varepsilon^{dA} = -2.89 \cdot 10^{-4} R_A, \quad (\text{C55})$$

$$g_\varepsilon^{sA} = 1.20 \cdot 10^{-5} R_A, \quad f_\varepsilon^{sA} = -9.22 \cdot 10^{-8} R_A, \quad (\text{C56})$$

with R_A for CE ν NS on ^{127}I given in (C49).

For dimension 5 operator we have, for CE ν NS on ^{127}I ,

$$f_1^{(5)} = 6.80 \cdot 10^6 \left(\frac{E_\nu}{\text{MeV}} \right)^2 \left(\frac{E_R}{\text{keV}} \right)^{-1} D, \quad (\text{C57})$$

and $g_1^{(5)} = 0$, while for dimension 6 operators the NSI cross section coefficients are given by

$$g_{1,u}^{(6)} = -8.87 \cdot 10^5, \quad f_{1,u}^{(6)} = 1.96 \cdot 10^{11}, \quad (\text{C58})$$

$$g_{1,d}^{(6)} = -9.90 \cdot 10^5, \quad f_{1,d}^{(6)} = 2.45 \cdot 10^{11}, \quad (\text{C59})$$

$$g_{1,s}^{(6)} = 1.34 \left(\frac{E_R}{\text{keV}} \right), \quad f_{1,s}^{(6)} = 0.449 \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C60})$$

$$g_{2,u}^{(6)} = 75.0 R_A, \quad f_{2,u}^{(6)} = 3.63 \cdot 10^6 R_A, \quad (\text{C61})$$

$$g_{2,d}^{(6)} = -57.7 R_A, \quad f_{2,d}^{(6)} = 2.15 \cdot 10^6 R_A, \quad (\text{C62})$$

$$g_{2,s}^{(6)} = -1.03 R_A, \quad f_{2,s}^{(6)} = 6.854 \cdot 10^2 R_A, \quad (\text{C63})$$

with function R_A for CE ν NS on ^{127}I given in (C49). For dimension 7 operators the cross section coefficients for CE ν NS on ^{127}I are given by

$$f_1^{(7)} = 1.30 \cdot 10^3 \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad f_2^{(7)} = 2.41 \cdot 10^{-4} \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad (\text{C64})$$

$$f_3^{(7)} = 5.75 \cdot 10^9 \left(\frac{E_R}{\text{keV}} \right) D, \quad f_4^{(7)} = 2.67 \cdot 10^{-2} \left(\frac{E_R}{\text{keV}} \right)^4 D, \quad (\text{C65})$$

$$f_{5,u}^{(7)} = 3.65 \cdot 10^8 \left(\frac{E_R}{\text{keV}} \right) D, \quad f_{5,d}^{(7)} = 1.72 \cdot 10^9 \left(\frac{E_R}{\text{keV}} \right) D, \quad f_{5,s}^{(7)} = 2.48 \cdot 10^9 \left(\frac{E_R}{\text{keV}} \right) D, \quad (\text{C66})$$

$$f_{6,u}^{(7)} = 76.4 \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad f_{6,d}^{(7)} = 5.16 \cdot 10^2 \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad f_{6,s}^{(7)} = 83.9 \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad (\text{C67})$$

$$f_{7,u}^{(7)} = 9.06 R_T, \quad f_{7,d}^{(7)} = 2.61 R_T, \quad f_{7,s}^{(7)} = 2.51 \cdot 10^{-3} R_T, \quad (\text{C68})$$

while for dimension 7 operators with derivatives in the neutrino current, the coefficients are

$$f_{8(10),u}^{(7)} = 4.91 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}} \right)^2 D, \quad f_{9(11),u}^{(7)} = 49.6 \left(\frac{E_R}{\text{keV}} \right), \quad (\text{C69})$$

$$f_{8(10),d}^{(7)} = 6.12 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}} \right)^2 D, \quad f_{9(11),d}^{(7)} = 1.81 \left(\frac{E_R}{\text{keV}} \right), \quad (\text{C70})$$

$$f_{8(10),s}^{(7)} = 0.449 \left(\frac{E_\nu}{\text{MeV}} \right)^2 \left(\frac{E_R}{\text{keV}} \right)^2 D, \quad f_{9(11),s}^{(7)} = 0.115 \left(\frac{E_R}{\text{keV}} \right), \quad (\text{C71})$$

The D and R_T functions for CE ν NS on ^{127}I are given in (C48) and (C50), respectively.

4. Numerical results for CE ν NS on Xe

Here we show the numerical results for NSI induced corrections to CE ν NS on Xe targets, assuming natural abundances of Xe isotopes (for numerical results of cross section on single isotopes, see [101]). To shorten the expressions we define three functions for incoming neutrino energy, E_ν , and nuclear recoil energy, E_R ,

$$D = [(E_\nu/\text{MeV})^2 - 61.3(E_R/\text{keV})]^{-1}, \quad (\text{C72})$$

$$R_A = [(E_\nu/\text{MeV})^2 + 61.3(E_R/\text{keV})]D, \quad \text{for CE}\nu\text{NS on Xe}, \quad (\text{C73})$$

$$R_T = [(E_\nu/\text{MeV})^2 - 44.9(E_R/\text{keV})]D. \quad (\text{C74})$$

For dimension 6 operators we have, using ε_i , notation for CE ν NS on Xe,

$$g_\varepsilon^{uV} = -10.2, \quad f_\varepsilon^{uV} = 25.9, \quad (\text{C75})$$

$$g_\varepsilon^{dV} = -11.4, \quad f_\varepsilon^{dV} = 32.6, \quad (\text{C76})$$

$$g_\varepsilon^{sV} = 1.59 \cdot 10^{-5} \left(\frac{E_R}{\text{keV}} \right), \quad f_\varepsilon^{sV} = 6.31 \cdot 10^{-11} \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C77})$$

$$g_{\varepsilon^{uA}} = 1.48 \cdot 10^{-5} R_A, \quad f_{\varepsilon^{uA}} = 4.32 \cdot 10^{-5} R_A, \quad (\text{C78})$$

$$g_{\varepsilon^{dA}} = -3.74 \cdot 10^{-5} R_A, \quad f_{\varepsilon^{dA}} = 2.75 \cdot 10^{-5} R_A, \quad (\text{C79})$$

$$g_{\varepsilon^{sA}} = 1.35 \cdot 10^{-6} R_A, \quad f_{\varepsilon^{sA}} = 3.56 \cdot 10^{-8} R_A, \quad (\text{C80})$$

with the R_A function given in (C73).

For dimension 5 operator the only nonzero coefficient is for quadratic dependence on the Wilson coefficient. For CE ν NS on Xe we have

$$f_1^{(5)} = 6.38 \cdot 10^6 \left(\frac{E_\nu}{\text{MeV}} \right)^2 \left(\frac{E_R}{\text{keV}} \right)^{-1} D, \quad (\text{C81})$$

with the D function given in (C72). For dimension 6 operators the CE ν NS on Xe cross section coefficients are given by

$$g_{1,u}^{(6)} = -8.77 \cdot 10^5, \quad f_{1,u}^{(6)} = 1.92 \cdot 10^{11}, \quad (\text{C82})$$

$$g_{1,d}^{(6)} = -9.85 \cdot 10^5, \quad f_{1,d}^{(6)} = 2.42 \cdot 10^{11}, \quad (\text{C83})$$

$$g_{1,s}^{(6)} = 1.37 \left(\frac{E_R}{\text{keV}} \right), \quad f_{1,s}^{(6)} = 0.469 \left(\frac{E_R}{\text{keV}} \right)^2, \quad (\text{C84})$$

$$g_{2,u}^{(6)} = 1.28 R_A, \quad f_{2,u}^{(6)} = 3.21 \cdot 10^4 R_A, \quad (\text{C85})$$

$$g_{2,d}^{(6)} = -3.23 R_A, \quad f_{2,d}^{(6)} = 2.05 \cdot 10^5 R_A, \quad (\text{C86})$$

$$g_{2,s}^{(6)} = 0.116 R_A, \quad f_{2,s}^{(6)} = 2.64 \cdot 10^5 R_A, \quad (\text{C87})$$

where the R_A function is given in (C73). For dimension 7 operators only the f_a^d coefficients are nonzero,

$$f_1^{(7)} = 2.08 \cdot 10^3 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_2^{(7)} = 1.38 \cdot 10^{-4} \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C88})$$

$$f_3^{(7)} = 5.82 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_4^{(7)} = 3.08 \cdot 10^{-3} \left(\frac{E_R}{\text{keV}}\right)^4 D, \quad (\text{C89})$$

$$f_{5,u}^{(7)} = 3.69 \cdot 10^8 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,d}^{(7)} = 1.74 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad f_{5,s}^{(7)} = 2.52 \cdot 10^9 \left(\frac{E_R}{\text{keV}}\right) D, \quad (\text{C90})$$

$$f_{6,u}^{(7)} = 43.7 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,d}^{(7)} = 2.08 \cdot 10^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{6,s}^{(7)} = 33.8 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad (\text{C91})$$

$$f_{7,u}^{(7)} = 4.97 R_T, \quad f_{7,d}^{(7)} = 1.43 R_T, \quad f_{7,s}^{(7)} = 1.28 \cdot 10^{-3} R_T, \quad (\text{C92})$$

while the operators with derivatives on the neutrino current have the following coefficients for CE ν NS on Xe

$$f_{8(10),u}^{(7)} = 4.80 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),u}^{(7)} = 7.81 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C93})$$

$$f_{8(10),d}^{(7)} = 6.06 \cdot 10^{10} \left(\frac{E_\nu}{\text{MeV}}\right)^2 D, \quad f_{9(11),d}^{(7)} = 49.8 \left(\frac{E_R}{\text{keV}}\right), \quad (\text{C94})$$

$$f_{8(10),s}^{(7)} = 0.469 \left(\frac{E_\nu}{\text{MeV}}\right)^2 \left(\frac{E_R}{\text{keV}}\right)^2 D, \quad f_{9(11),s}^{(7)} = 6.44 \cdot 10^{-2} \left(\frac{E_R}{\text{keV}}\right). \quad (\text{C95})$$

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