

Methodology for pH measurement in high alkali cementitious systems

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Abstract

A methodology for calibrating pH meters in highly alkaline solutions such as those relevant to cementitious systems is presented. This methodology uses an extended form of the Debye-Hückel equation to generate a calibration curve of pH vs. the measured electrochemical potential (mV) based on a series of aqueous alkali hydroxide solutions of known concentrations. This methodology is compared with the ‘built-in’ process of calibration based upon pH 4, 7, and 10 standard solutions. The built-in calibration process underestimates the real pH values by up to 0.3 log units, which is attributed to the alkali error. A spreadsheet for determining the calibration curve and its application to pH meter readings is provided as

Supporting Information. The implications of improperly calibrated pH meters on interpreting solution chemistry in cementitious systems are discussed.

1. Introduction

Measurement of pH is a quick, simple and cost-effective technique that is fundamental to analytical chemistry and widely used in cement science. Fresh Portland cement concrete typically has a $\text{pH} > 13$ [1]. Maintaining such a high pH is essential to ensure passivation of steel in reinforced concrete, thereby preventing structural deterioration [2,3]. The pH of the activator solution in an alkali-activated material plays a critical role in precursor dissolution [4,5], and high pH solutions (> 13) are typically employed for this purpose [6]. In both Portland cement and alkali-activated material systems, the formation of reaction products has also been shown to depend on pH [7–10].

Calibration of a pH meter is necessary for accurate pH measurements. pH meters are typically calibrated using standard solutions with pH values of 4, 7, and 10 – a process we refer to here as the ‘built-in’ pH meter calibration. Saturated aqueous $\text{Ca}(\text{OH})_2$ solution may be used as a pH 12.45 standard (at 25°C) [11]. However, these pH values are below the pH range of most cementitious systems; therefore, using the built-in calibration in cementitious systems will likely lead to systematic pH measurement errors. Through appropriate selection of solutions of known concentration, pH meters can be accurately calibrated to higher pH. Although versions of this methodology have been used for years in analyses of cementitious systems [1,12–17], it has been poorly explicitly disseminated and there has been relatively little uptake of it among the broader cement science community. This communication is intended to clarify this methodology to the cement science community at large. As such, a pH

calculator for NaOH and KOH solutions as a function of temperature and concentration is included in the Supporting Information and the relevant physical chemistry concepts underpinning these calculations are discussed here.

2. Background

Table 1. Nomenclature of terms

a_i	Activity of ion i
b_i	Molality (mol kg^{-1})
b_0	Standard molality, defined as 1 mol kg^{-1}
γ_i	Activity coefficient of ion i
z_i	Charge on ion i
I	Ionic strength, $= \frac{1}{2} \sum_i b_i z_i^2$ (mol kg^{-1})
$\dot{a}$	Distance of closest approach parameter of interacting ions in Debye-Hückel equation ($\text{\AA}$)
b_γ	Semi-empirical parameter in extended Debye-Hückel equation (kg mol^{-1})
A_γ	Electrostatic parameter in Debye-Hückel equation ($\text{kg}^{1/2} \text{mol}^{-1/2}$)
B_γ	Electrostatic parameter in Debye-Hückel equation ($\text{kg}^{1/2} \text{mol}^{-1/2} \text{\AA}^{-1}$)
x_{jw}	Amount of water, parameter in Debye-Hückel equation (mol)
X_w	Total amount of all species in the aqueous phase, parameter in Debye-Hückel equation (mol)
M_i	Molarity (mol L^{-1})

2.1. Activity of non-ideal solutions

We begin the description of our methodology to calibrate pH meters by expressing the acidity of a solution using pH values (Eq.(1)):

$$\text{pH} = -\log_{10}(a_{H^+}) = -\log_{10}\left(\gamma_{H^+} \frac{b_{H^+}}{b_0}\right) \quad (1)$$

where a_{H^+} is the activity of aqueous H^+ , b_{H^+} is the molality of aqueous H^+ (mol kg^{-1} , i.e., mol of aqueous H^+ per kg of solvent), b_0 is the standard molality which is defined as 1 mol kg^{-1} (included to make the activity dimensionless), and γ_{H^+} is the activity coefficient of aqueous H^+ . Activity is a measure of the effective concentration of an ion in solution, accounting for non-idealities that arise in real solutions. Molality is the preferred thermodynamic expression for concentration due to its independence of temperature and pressure, unlike molarity (mol L^{-1}).

Deviations between activity and concentration arise from electrostatic interactions among ions in aqueous ionic solutions. Long range inter-ionic coulombic attractions affect ion activity predominantly at low concentrations, whereas short-range ion-ion and water-ion solvation interactions have additional effects at higher concentrations. Short-range ion-ion interactions (ion association) decrease ion activity through formation of ion-ion pairs, reducing the effective number of ions in solution. Water-ion solvation interactions (ion hydration) increase activity by effectively reducing the amount of solvent. In highly dilute aqueous environments, the difference between concentration and activity is negligible.

Debye-Hückel (DH) theory [18] was developed to calculate the mean activity coefficients of ions as a function of the concentration of ions in aqueous ionic solutions. DH theory as originally developed is applicable to dilute aqueous ionic solutions, in which short range

interactions are ignored by assuming a structureless solvent, and where the primary interactions between ions are long-range Coulombic forces. The theory results in the Debye-Hückel equation (Eq. (2)), which we define here using molalities:

$$\log_{10}\gamma_i = \frac{-A_\gamma z_i^2 \sqrt{I}}{1 + \dot{a} B_\gamma \sqrt{I}} + \log_{10} \frac{x_{jw}}{X_w} \quad (2)$$

where z_i is the charge of ion i in solution, $\dot{a}$ (Å) is the average distance of closest approach of two ions of opposite charge, I (mol kg⁻¹) is the ionic strength (defined in Table 1), and A_γ (kg^{1/2} mol^{-1/2}) and B_γ (kg^{1/2} mol^{-1/2} Å⁻¹) are parameters dependent on the temperature, density, and relative permittivity of the solvent (see Supporting Information). The average distance of closest approach, $\dot{a}$, does not in reality represent the sum of the ionic radii of the two ions, and in practice is adjusted to provide a best fit for the aqueous ionic solution of interest [19]. The second term in Eq. (2) contains the amount of water, x_{jw} (mol), and the total amount of species in the aqueous phase, X_w (mol) and changes the units of γ_i from molar fraction to molal fraction, aligning with our definition of activity. A more detailed derivation and explanation of this equation and related terms may be found in Wright [20]. The ionic strength is a measure of the molality of fully dissociated ions in solution, noting that only in very dilute solutions can salts be assumed to be completely dissociated. Eq. (2) is accurate in solutions up to moderate ionic strength, $I \leq 0.1$ mol kg⁻¹ [21].

Versions of the Debye-Hückel equation with an extended term have been used by researchers to extend the range of ionic strengths over which Debye-Hückel theory is valid. Helgeson extended the DH equation with a linear term [19];

$$\log_{10}\gamma_i = \frac{-A_\gamma z_i^2 \sqrt{I}}{1 + a B_\gamma \sqrt{I}} + b_\gamma I + \log_{10} \frac{x_{jw}}{x_w} \quad (3)$$

111

112 where b_γ (kg mol⁻¹) is a semi-empirical parameter, known as the extended term. In his
 113 model, a common distance of closest approach was assumed by Helgeson for all ions in a
 114 given aqueous ionic solution – values of $\dot{a}$ were calculated for various solutions, with $\dot{a}$
 115 taking a common value for all ions in that solution. This assumption makes the Helgeson
 116 extension to the DH equation more accurate in solutions in which the primary salt
 117 concentration exceeds that of other aqueous ions. Additionally, the effects of short-range
 118 water-ion solvation interactions are captured by the extended term, b_γ (kg mol⁻¹). Helgeson
 119 described the solvation of an ion in solution using the Born equation [22], as corrected by
 120 Bjerrum [23], to calculate values of b_γ for various aqueous ionic solutions. The applicability
 121 of the Helgeson form of the Debye-Hückel (H-DH) equation at high ionic strengths depends
 122 on the aqueous ionic solution of interest. For aqueous NaOH and KOH solutions, the H-DH
 123 equation is accurate up to ionic strengths of 4.5 mol kg⁻¹, determined by Helgeson as the
 124 range of validity for the extended term, b_γ , through comparison of activity coefficients
 125 reported in the literature to those computed using the H-DH equation [19]. Two other notable
 126 forms of the extended DH equation are the Davies' equation and the Truesdell-Jones equation
 127 – these are discussed in the Supporting Information and are applicable at moderate to high
 128 ionic strengths, ($I < 0.1$ mol kg⁻¹, and $I < 1$ mol kg⁻¹, respectively) [26,27].

129

130 The Pitzer equations are suitable for high ionic strengths and mixed ion aqueous ionic
 131 solutions ($I > 1$ mol kg⁻¹) [28,29]; however, they require specific interaction parameters
 132 between aqueous species to be defined, which are numerous in cementitious systems (Ca²⁺,
 133 CaOH⁺, SiO(OH)₃⁻, SiO₂(OH)₂²⁻, etc.). Therefore, the Pitzer equations are less pragmatic for

application in cementitious systems than the extended forms of the DH equation and are not discussed further here.

2.2. pH measurement with a glass combination electrode

While activity cannot be directly measured, electrochemical potential can. pH is most commonly determined indirectly through measurement of an electrochemical potential using a pH meter, which typically consists of a glass combination electrode and a meter. The electrochemical potential of standard solutions with precisely known pH can be measured using a glass combination electrode, and a calibration curve of pH vs. electrochemical potential is generated by the meter. This built-in calibration curve is used to convert electrochemical potentials measured by the glass combination electrode in an analyte to pH. The electrochemical potential measured by the glass combination electrode, E_T , may be written as (Eq. (4)):

$$E_T = \varepsilon + E(a_{H^+}) \quad (4)$$

where ε (mV) is an electrochemical potential due to a combination of smaller potentials that are artifacts of the design of the glass combination electrode, (see Supporting Information), and $E(a_{H^+})$ (mV) is an electrochemical potential that is a function of solution pH. While Eq. (4) is similar to the Nernst equation ($E = E_0 - 2.303 \frac{RT}{F} pH$), Eq. (4) is more appropriate in this context as the measured electrochemical potential, E_T , is not a linear function over the entire pH scale, as is implied by the Nernst equation. Despite this non-linearity, calibrations performed relating $E(a_{H^+})$ to pH are generally assumed to be linear. This is valid over most

of the pH range, but not for highly acidic or alkaline solutions, where linearity between electrochemical potential and pH is lost.

The Ag/AgCl glass combination electrode with ion selective membrane is the most common type of electrode used in pH meters. The potential of interest in this paper is the gel layer potential, $E(a_{H^+})$, which occurs at the ion selective membrane of the glass combination electrode. It arises due to the difference between H^+ activity in the external analyte electrolyte and the inner buffer electrolyte. The glass membrane is a silicate glass with ion inclusions, typically Ca^{2+} , Na^+ , and Li^+ , but the exact glass composition depends on the analyte ions towards which the membrane is designed to be selective [30,31]. The gel layer potential, which is generated across the glass membrane when in contact with the analyte, arises through formation of a charged hydrated gel layer produced on either side of the glass membrane [32,33].

Although the gel layer potential, $E(a_{H^+})$, is designed to change only as a function of analyte H^+ ion activity (over a wide range of H^+ activities and analyte chemistries), no glass membrane is ever wholly selective to one specific ion [34]. In highly alkaline solutions the hydrated gel layer has a negative structural charge and is charge-balanced significantly by aqueous alkali metal complexes (e.g., Na^+) in addition to H^+ , as described by Baucke [35]. Cheng described the gel layer potential as a capacitor, in which the surface charge density, caused by adsorbed ions (e.g., H^+ , OH^- , Na^+), yields a potential across the glass membrane [36]. In any case, the presence of positively charged alkali ions in the gel layer artificially lowers the measured pH as alkali ions, rather than H^+ ions, contribute to the gel layer potential. This phenomenon is known as the alkali error [37–39]. It arises when measuring pH of highly alkaline aqueous solutions; the effect is relatively weak in the case of K^+ ,

moderate for Na^+ , and strong for Li^+ . Standard solutions of pH 4, 7, and 10 are thus insufficient to calibrate a pH meter for measurement of highly alkaline aqueous solutions. Calibrating a pH meter with solutions of similar chemistry and ionic strength to the analyte is a means of providing a valid calibration curve by mitigating the systematic errors discussed above, including the alkali error [40].

In the context of cement science, the observed discrepancies between measured and actual pH can significantly alter interpretation of experimental results. As discussed in the introduction, the evolution of a (solid/liquid) cementitious system depends on the OH^- concentration in its aqueous phase. Dissolution rates of a wide range of minerals and cement hydration products have shown strong dependences on pH, with small differences in pH potentially corresponding to large changes in rates of dissolution [41–46]. Similarly, the rates and distributions of reaction products vary with pH [4,7]. For example, pH affects silicate speciation in aqueous alkali silicate solutions [47], and the relative stabilities of calcium (alkali) (alumino)silicate hydrate (C-(N-)A-S-H) and portlandite [48], and zeolites and alkali aluminosilicate (hydrate) gel [7,49–51]. We draw attention to the fact that misinterpretation of pore solution chemistry of a cementitious system can lead to mis-characterization of its solid phases due to the intrinsic link between solid and liquid phases (e.g., equilibrium phenomena), which is relevant to systems involving pure solid phases, binders, mortar, and concrete. Aqueous solutions of NaOH and KOH are of interest in cementitious systems due to their use in AAMs and the relatively high concentrations of these alkali metals (K especially) in hydrated Portland cement.

The H-DH equation allows calculation of the activity of OH^- , and hence pH, up to ionic strengths of 4.5 mol kg^{-1} for single component aqueous systems [19] or $1\text{--}3 \text{ mol kg}^{-1}$ in

multi-component cementitious systems [48]. For solutions of known molarity, a calibration curve can be constructed through the electrochemical response of the pH meter in solution and the pH determined using the H-DH equation for each solution. By accounting for the alkali error in this way, the pH of an analyte can be accurately determined. We demonstrate the use of this methodology in the following sections of this paper.

3. Experimental procedures

3.1. NaOH and KOH standards, and LiOH solutions

NaOH and KOH standards were prepared with the following concentrations: 0.0001 M (mol L⁻¹), 0.0005 M, 0.001 M, 0.005 M, 0.01 M, 0.05 M, 0.1 M, 0.2 M, 0.5 M, 1 M, 2 M, and 3 M. NaOH and KOH standards were made by diluting commercial solutions of 3 (±0.005) M NaOH (BDH Chemicals) and 8 (±0.005) M KOH (Ricca), respectively. Dilutions were performed by transferring quantities of Na(K)OH commercial solution into volumetric flasks and filling to their marks with high purity water (18.2 MΩ cm, Millipore). The as-ordered Na(K)OH commercial solutions were stored in high-density polyethylene (HDPE) bottles. All prepared solutions were stored in clean HDPE bottles upon preparation.

LiOH solutions (concentrations of 0.0001 M (mol L⁻¹), 0.0005 M, 0.001 M, 0.005 M, 0.01 M, 0.05 M, 0.1 M, 0.2 M, 0.5 M, 1 M, 2 M, and 3 M) were prepared by addition of appropriate quantities of reagent grade lithium hydroxide monohydrate flakes (> 98%, Alfa Aesar) to a 500 mL volumetric flask and filling to the mark with high purity water (18.2 MΩ cm, Millipore) once flakes had completely dissolved. Calibrations used freshly prepared solutions to mitigate effects of carbonation of alkalis. The use of analytical grade salts in the

case of LiOH can lead to higher deviations ($\pm 2\%$) from the target concentrations than the use of standard solutions in the cases of KOH and NaOH. This has been taken into account in the calculated uncertainties of pH values reported here, resulting in a deviation of <0.001 pH units for the LiOH solutions.

3.2. pH measurements

A typical pH meter offers the possibility to read out i) the pH values directly based on the built-in calibration using pH 4, 7, and 10 standard solutions ('built-in calibration') or ii) the mV electrochemical potential (mV). All pH measurements were performed with a Thermo Orion Ag/AgCl combination triode stored in KCl solution with Automatic Thermal Correction probe at 22°C . Between measurement of each analyte, the pH meter was rinsed using water purified by reverse osmosis ($18\text{ M}\Omega\text{ cm}$) (Millipore) and gently dabbed dry using delicate wipes (Kimtech). Approximately 10 mL of prepared aqueous Na(K)OH solution was transferred to a 15 mL polypropylene (PP) centrifuge tube. The solution was gently agitated for a few seconds, and the electrochemical potential was recorded after 2 minutes (when the reading had stabilized). Samples were not stirred during pH measurements [52]. The main sources of error in this study were the accuracy of the pH meter and glass combination electrode in measuring the electrochemical potential ($\pm 0.2\text{ mV}$), and the error in the built-in calibration slope recorded ($\pm 0.5\%$). Errors in the calculated pH values are based on the standard deviation of recorded temperatures ($\pm 0.5^\circ\text{C}$) during measurement of the pH of solutions. Error propagation calculations are included in the Supporting Information.

3.3. Fitted calibration curve calculations

The pH of the solution was calculated from the solution concentrations using the H-DH equation for aqueous NaOH and KOH solutions and known equilibrium constants for Na(K)OH dissociation at the measurement (laboratory) temperature (22°C) from [53]. The calculated pH values were then plotted against the measured electrochemical potentials of prepared Na(K)OH solutions using the pH meter, and the data fitted using a calibration curve ('fitted calibration'). The use of NaOH or KOH solutions for the fitted calibration directly takes into account the alkali error, as the same alkali error occurs both during the calibration and the measurement accounting for the systematic error. Electrochemical potentials of analytes are also measured using electrochemical potential (mV) readings from the pH meter, and the fitted calibration curve is used to convert the readings to pH. We provide a spreadsheet for the determination of this calibration curve and application to pH meter readings of sample solutions as Supporting Information.

3.4. Preparation of alkali-activated biomass ash samples

Application of this methodology to a real cementitious system is also demonstrated here. Alkali-activated biomass ash experiments were prepared using 0.5 and 1 molal aqueous NaOH solutions (ACS Reagent grade water, RICCA Chemical Company; NaOH $\geq 97\%$, Sigma Aldrich) as activators at a constant liquid/solid ratio of 25 (i.e. 2 g of solid in 50 mL of solution). Solids consisted of highly siliceous biomass ash (sourced from Silverton Pulp & Papers Pvt. Ltd. In Muzzafarnagar, Uttar Pradesh, India) and $\text{Ca}(\text{OH})_2$ ($\geq 98\%$, Macron Fine Chemicals), mixed at a ratio of 1.75 g ash : 0.25 g $\text{Ca}(\text{OH})_2$. The composition of the biomass ash, determined by X-ray fluorescence and loss on ignition tests, showed siliceous ash (61 mass% SiO_2) with high unburnt carbon (26 mass%). The phase composition (determined by X-ray diffraction) showed a primarily amorphous ash (90 mass%) with presence of quartz,

albite, cristobalite, sylvite and arcanite. The materials and conditions of reaction were chosen to mimic a masonry product previously developed in [54]. Samples were mixed continuously in a tube rotator (Fisherbrand™ Multi-Purpose Tube Rotator, Fisher Scientific) to ages of 3 and 28 days to explore dissolution and reaction kinetics.

4. pH meter calibration

The linear calibration curve fittings for prepared aqueous NaOH and KOH solutions are respectively shown in Figure 1 (A) and (B). The alkali error associated with measuring the pH of LiOH solutions is also demonstrated (Figure 1 (C)). The pH is calculated using the Henderson-Hasselbalch equation (Eq. (3)) and methodology presented here and in the Supporting Information. The measured built-in pH is based on an extrapolated calibration curve using pH 4, 7, and 10 standard solutions. The divergence at high pH (Figure 1A, inset) demonstrates the alkali error and the need to apply the methodology presented here when measuring highly alkaline solutions, i.e., in analysis of cementitious systems.

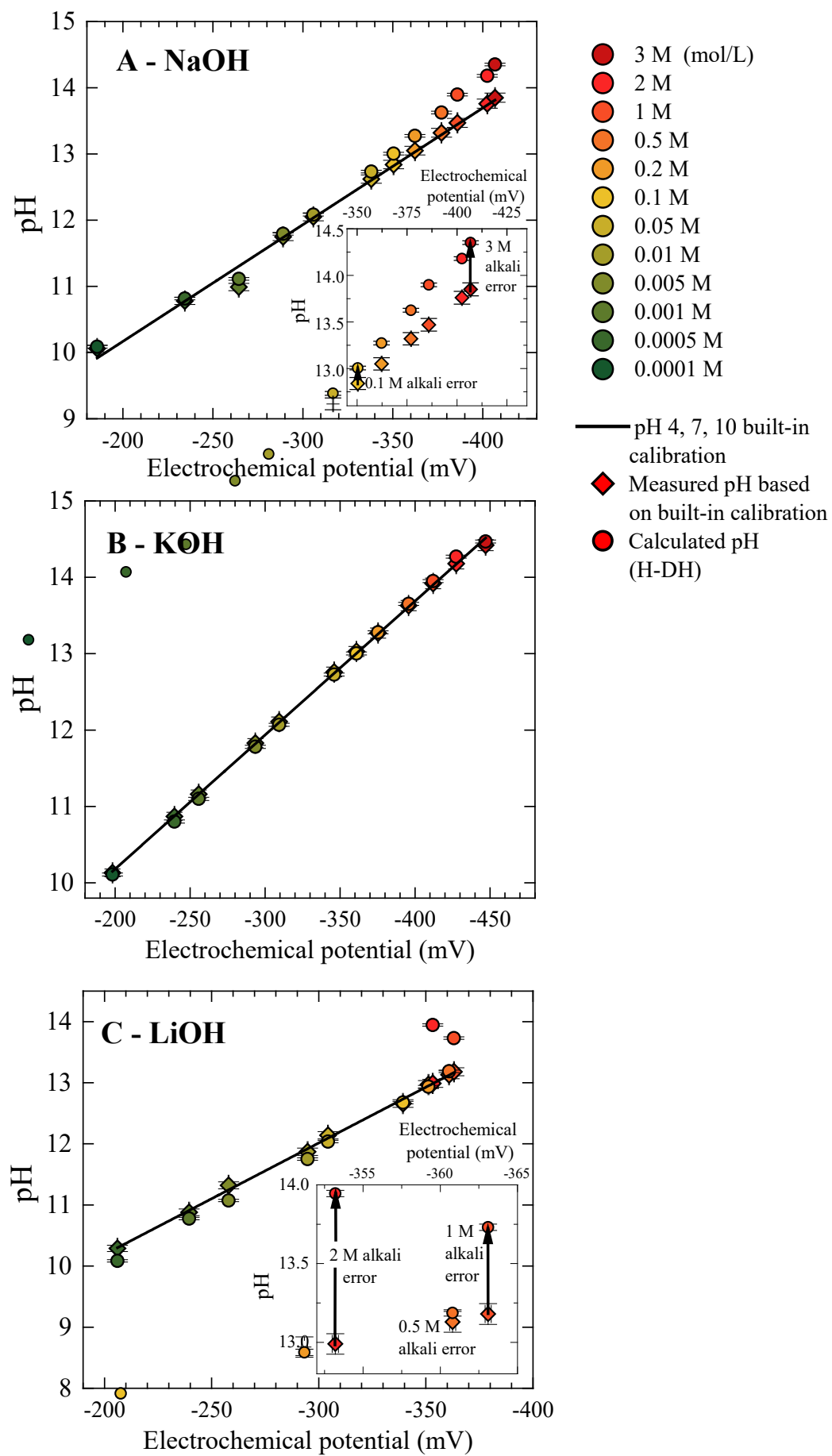


Figure 1. Calibration curves for aqueous NaOH (A), KOH (B), and LiOH (C) solutions of known concentration up to 3 M based upon pH values calculated using the H-DH equation (circles) and those measured by the pH meter using standard solutions of pH 4, 7, and 10 (triangles) at 22 °C. The deviation between the calculated pH and the uncorrected, extrapolated built-in calibration curve from pH 4, 7, 10 standards (black line) is a result of the alkali error at high pH, which is more pronounced for Li⁺ and Na⁺ than K⁺. The solution molarities at which the alkali error is significant are shown in the inset graphs. For LiOH solutions, the pH was calculated using the Davies' equation, as the H-DH equation is not valid for LiOH solutions.

While the calculated pH (H-DH) does trend above the measured pH, the alkali error for pH measurement in aqueous KOH solutions is not statistically significant. In contrast, the alkali error for NaOH is up to 0.5 pH units in 3 M NaOH. The alkali error for LiOH solutions is even greater – the alkali error for 2 M LiOH solutions is 1 pH unit. The extent of the alkali error in LiOH solutions precludes any meaningful direct pH measurements above concentrations of 0.5 M LiOH [55]. This trend is explained in terms of ion size: K⁺ ions (internuclear radius in aqueous solution of 2.8 Å [56]) are significantly less mobile through the glass membrane than Na⁺ ions (internuclear radius in aqueous solution of 2.3 Å [56]) and Li⁺ ions (internuclear radius in aqueous solution of 2.1 Å [56]), due to their smaller ion size [38,57].

The H-DH equation used above is designed for aqueous NaOH and KOH solutions [19] up to ionic strengths of 4.5 mol kg⁻¹ [19], but in multi-component cementitious systems this range is typically taken as 1-3 mol kg⁻¹ [48]. Parameters for the H-DH equation have also been calculated for other aqueous ionic solutions (HCl, LiCl, MgCl₂, SrCl₂, CaCl₂, BaCl₂, AlCl₃, HBr, LiBr, NaBr, MgBr₂, SrBr₂, CaBr₂, BaBr₂, HI, NaI, MgI₂, SrI₂, CaI₂, BaI₂, KF) [19]. The temperature at which the pH is recorded is important for H-DH calculations – the dissociation constants of NaOH, KOH, and H₂O change with temperature (see Supporting Information [58], affecting the OH⁻ concentration.

5. Application to cementitious systems

To demonstrate the utility of the methodology presented, pH values of filtrates taken from a series of alkali-activated biomass ash samples were measured. In each case, we use the NaOH fitted calibration curve (Figure 1A) to convert the measured electrochemical potential to pH. Details on how these samples were made are given in the Section 3.4. The results of the pH measurements and calculations using the methodology presented here are shown in Table 2.

Table 2. OH⁻ concentrations and pH of samples measured using calibration curve (calculated from H-DH equation, Figure 1A, circles) at 22 °C.

Initial b_{NaOH} (mol kg ⁻¹)	Biomass Ash Mass (g)	Ca(OH) ₂ Mass (g)	Curing time (days)	Electro- chemical potential (mV)	Built-in ¹ pH (-)	$b_{[\text{OH}^-]}$ ² (mol kg ⁻¹)	Fitted ² pH (-)
0.5	0	0	3	-372.4	13.33±0.07	0.406	13.62±0.02
			28	-371.3	13.31±0.07	0.385	13.60±0.02
	2	0	3	-361.9	13.15±0.07	0.244	13.41±0.02
			28	-352.4	12.97±0.06	0.153	13.22±0.02
	1.75	0.25	3	-365.2	13.21±0.07	0.287	13.48±0.02
			28	-356.4	13.04±0.07	0.186	13.30±0.02
1	0	0	3	-381.4	13.49±0.07	0.617	13.80±0.02
			28	-380.1	13.46±0.07	0.582	13.77±0.02
	2	0	3	-372.6	13.32±0.07	0.410	13.62±0.02
			28	-369.4	13.26±0.07	0.352	13.56±0.02
	1.75	0.25	3	-374.9	13.37±0.07	0.457	13.67±0.02
			28	-372.3	13.31±0.07	0.404	13.62±0.02

¹ Obtained directly from the built-in pH meter calibration using pH 4, 7, and 10 standard solutions. The differences from the calculated pH values are due to the alkali error

² OH⁻ concentration and fitted pH calculated from fitted calibration curve derived using the H-DH equation

Differences between the calculated and measured pH, i.e., the alkali error, are consistently on the order of 0.3 pH units, corresponding to an underestimation of b_{OH^-} by 0.25 mol kg⁻¹ if the built-in calibration is used. Samples with higher pH values differ more greatly from the actual pH, as expected. For context, at 22 °C the calculated (H-DH) pH values of 1 and 0.5 mol kg⁻¹ aqueous NaOH solutions are 13.86 and 13.59, respectively. The difference of 0.27 pH units is

similar to the discrepancy caused by the alkali error (0.3 pH units), demonstrating the effect of this phenomenon in analysis of cementitious systems.

6. Conclusions

A methodology for calibrating pH meters in solutions of high alkali content ($\text{pH} > 13$) has been presented. The Helgeson extension to the Debye-Hückel (H-DH) equation was used to calculate the pH of aqueous ionic solutions of known molarity. The H-DH equation was chosen because of its practicality and accuracy at high ionic strengths (approaching 4.5 mol kg^{-1}). We provide a spreadsheet for the determination of this calibration curve and application to pH meter readings of sample solutions as Supporting Information. The value of this methodology was demonstrated for a binder consisting of biomass ash, $\text{Ca}(\text{OH})_2$ and aqueous NaOH activator. The discrepancies, caused by the alkali error, between the actual, fitted pH (calculated using the H-DH) and the measured pH (based on the built-in pH 4, 7, 10 standards calibration) were highlighted. The built-in calibration underestimated the real pH values by up to 0.3 pH units in aqueous NaOH solution, which illustrates the importance of a properly calibrated pH meter to prevent erroneous interpretations of the pH of cementitious systems. Discrepancies between built-in calibration and real, fitted pH values were more pronounced for aqueous LiOH solutions compared to aqueous NaOH solutions, but less so for aqueous KOH solutions.

7. Supporting information

Two files are provided as supporting information: (1) a document containing additional descriptions of (S1) other forms of the extended Debye-Hückel equation, (S2)

electrochemical potentials in glass combination electrodes, and (S3) the error analysis performed here; and (2) a spreadsheet embedded with calculations and a step-by-step procedure to use the method described here, to measure pH in high alkali cementitious systems.

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9. Conflicts of interest

The authors declare no conflicts of interest.

10. References

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