

Resonant Nanodiffraction X-ray Imaging Reveals Role of Magnetic Domains in Complex Oxide Spin Caloritronics

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125-Character Summary Sentence: X-ray nanodiffraction reveals the magnetism of spincaloritronic oxides and strategies for its control via lattice distortion.

Abstract

Spin electronic devices based on crystalline oxide layers with nanoscale thicknesses involve complex structural and magnetic phenomena, including the spatial distribution and hysteresis of magnetic domains and the coupling of the magnetism to elastic and plastic crystallographic distortion. The magnetism of buried nanoscale layers has a significant impact on spincaloritronic devices incorporating garnets and other oxides exhibiting the spin Seebeck effect. Synchrotron hard x-ray nanobeam diffraction techniques combine structural, elemental, and

magnetic sensitivity and allow the magnetic domain configuration and structural distortion to be probed in buried layers simultaneously. Resonant scattering at the Gd L₂ edge of Gd₃Fe₅O₁₂ layers yields magnetic contrast with both linear and circular incident x-ray polarization. Domain patterns have geometric features consistent with faceting to form low-energy domain wall orientations but are also coupled to elastic features linked to epitaxial growth. Nanobeam magnetic diffraction images reveal diverse magnetic microstructure within emerging SSE materials and a strong coupling of the magnetism to crystallographic distortion.

Introduction

Developments in the field of spin electronics promise to extend its scope far beyond the original vision of applications in computing and information technologies. In spintronic materials and devices the coupling of the charge and spin degrees of freedom led to successful applications such as giant magnetoresistance transducers and spin-transfer torque oscillators (1, 2). Recent discoveries have shown that an even far broader scope of applications can be accessed by the coupling of spin, charge and heat currents in one and the same material. One particularly promising extension of spintronic phenomena is in thermoelectric generation, broadly termed spin caloritronics (3). If optimized, thermoelectric technologies can enable the direct conversion of thermal energy to electrical power (4). In conventional thermoelectrics an electric current generated by a temperature gradient. For efficient devices good electric and poor thermal conductivity is required, vastly complicating the design of materials and devices (5, 6). Spin caloritronics provides a complementary novel approach based on the spin Seebeck effect (SSE). Here, a spin current is driven by a temperature gradient in a magnetic insulator with thermal transport properties far better suited to device applications (3, 7-9). This Letter reports the discovery of a diverse magnetic microstructure within emerging SSE materials and of a strong coupling of the magnetic structure to crystallographic distortion. A novel synchrotron hard x-ray resonant nanobeam diffraction method and a new magnetic contrast imaging mechanism provides combined structural and elemental specificity, uniquely allowing precise magnetic and structural information to be obtained simultaneously from nanoscale buried volumes. Advanced x-ray methods resolve long-standing uncertainties in the nanoscale magnetism and structure of the single-crystalline magnetic materials and, when combined with advances in synthesis and lithography, will enable new horizons in spin caloritronics and spintronic devices more generally.

The SSE is typically based on the development of a *spin* current in a magnetic insulator (MI) as a result of a temperature gradient. This spin current is injected into an adjacent high-atomic-number metal (HM) and transformed into an electrical (*charge*) current *via* the inverse spin-Hall effect, transducing the thermal gradient to an electrical current (8). The physics of SSE devices is currently described by a model in which thermopower in MI/HM bilayers results from magnonic spin currents (8, 9). Furthermore, the optimization of SSE devices in zero magnetic field requires a precise knowledge of the magnetic microstructure of the MI and the correlation between this magnetic microstructure and the generated voltage. In particular, in the absence of an external magnetic field, magnetic inhomogeneity arising from the three-dimensional distribution of magnetic domains can strongly influence the magnon propagation and therefore the spin current at the MI/HM interface and consequently degrade the thermoelectric efficiency (8, 10). The magnetic domain configuration is also affected by strain imposed by the substrate used to template the epitaxial growth of the MI, crystallographic and chemical defects, and the attached conducting HM layer in ways that are not yet known.

Here, we report the discovery of the zero-magnetic-field domain configuration within the garnet $\text{Gd}_3\text{Fe}_5\text{O}_{12}$ (GdIG), a prototypical SSE material for which the chemical and magnetic structure appears in Fig. 1A (4, 11). The thinness, nanoscale domain dimensions, and magnetic complexity of the magnetic garnet layers pose challenges for magneto-optical characterization (*e.g.* second-harmonic generation and magneto-optical imaging, and coupled optical/SSE measurements) (8, 12), polarized neutron reflectivity (13), photoemission microscopy (14), and magnetic force microscopy (15). As a result, magnetic microscopy methods have probed domains near surfaces or in bulk crystals or thick epitaxial layers relevant to magnetooptics rather than in the nanoscale buried layers of spin caloritronic devices (16, 17). Hard x-ray nanodiffraction, as described here, however, employs photon energies of several keV or more and couples both to the magnetism and the crystallographic nanoscale structure, providing a unique combination of layer-, site-, and element-specificity. The development of this hard x-ray ferromagnetic imaging approach extends previous imaging of ferromagnetic and antiferromagnetic materials (15, 18-21) by providing structural and magnetic sensitivity simultaneously.

X-ray nanobeam maps obtained for a GdIG thin film with thickness $\Delta = 21$ nm using beamline ID01 at the European Synchrotron Radiation Facility indicate that the magnetic domain morphology has a critical impact on the efficiency of the SSE voltage generation in devices based on GdIG. Structural features such as strain and nanoscale morphology appear to be related to the magnetic domain morphology and provide the means to control the domain pattern and thus optimize devices.

Thick (111)-oriented GdIG layers have domains of out-of-plane magnetization with alternating direction, separated by Bloch domain walls above about 190 K (15, 22, 23). Comparatively little experimental or theoretical insight is available into the complex magnetic configuration that can be expected in (001)-oriented nanoscale layers in zero magnetic field, due to the competition among effects arising from nanoscale geometry, elastic distortion, and magnetic anisotropy (15, 16, 24-26). Possible directions of magnetization within a magnetic domain in (001)-oriented GdIG are illustrated in Fig. 1B, under the assumption that the net magnetization of GdIG is along magnetically easy bulk $\langle 111 \rangle$ directions. There remains, however, significant uncertainty regarding the direction of magnetization in GdIG ultrathin layers due to shape anisotropy and magnetoelastic effects. In part, the uncertainty arises because of the lack of local nanoscale characterization that promises to be resolved by the x-ray methods presented in this Letter. The analysis presented below employs the bulk magnetic polarization as a guide to interpreting results, but the possibility that shape anisotropy leads to in-plane magnetization in ultrathin garnet layers remains open.

Results

The lithographically patterned Hall-bar SSE test structure shown in Fig. 1C consists of GdIG ridges capped by an HM layer consisting of a 2.8 nm-thick Pt film. A thermal gradient through the thickness of the GdIG/Pt bilayer is generated by applying a current in the Pt layer. The SSE voltage V_{SSE} is measured in a perpendicular in-plane direction using a set of lateral electrical contacts (see Materials and Methods). For magnetic fields larger than the magnetic saturation field $\mu_0 H_{\text{sf}} \approx 0.2$ T, the sign of V_{SSE} switches when the external magnetic field $\mu_0 \mathbf{H}$ (and therefore the overall magnetization $\mathbf{M}$ of the GdIG layer) is reversed. A further sign change of V_{SSE} as a function of temperature is obvious from Fig. 1D, which can be attributed to a competition of different

magnon branches in GdIG (see Materials and Methods) (4, 11). At lower magnetic fields, V_{SSE} has low-magnetic-field hysteresis, which can be ascribed to changes of the magnetic domain structure in the GdIG thin film (Fig. 1D). V_{SSE} can be expected to be maximized when the MI has exhibits single magnetic domain state with $\mathbf{M}$ perpendicular to both the temperature gradient and the direction along which the voltage is measured. We infer, therefore, that the hysteresis in V_{SSE} is an experimental signature of the mesoscale reconfiguration of the magnetic domain pattern in the presence of the applied magnetic field (27). Understanding and controlling the zero-field magnetic domain direction in the MI layer thus becomes a defining, but previously unexploited, aspect of the design of SSE devices.

Maps of the magnetic domain structure within the GdIG layer covered by a thin Pt thin film without an applied magnetic field were obtained by combining synchrotron x-ray nanodiffraction with x-ray resonant magnetic scattering (XRMS). XRMS employs precise control of the incident x-ray polarization and yields a diffracted intensity that depends on the magnetization (28). Three relevant settings incident polarization are illustrated in Fig. 1E: circular polarizations with left (L) and right (R) helicity and linear polarization in the x-ray scattering plane, termed π polarization. As demonstrated below, using these three polarizations allows the scattering contrast between magnetic domains to be distinguished from the scattering arising from the atomic structure. Experiments were conducted using the magnetic sensitivity of the L_2 resonance of the Gd ions within the GdIG layer using photon energies near 7.94 keV. We therefore probe the magnetic domain structure of the magnetic Gd sublattice. The nanobeam measurements were conducted using an x-ray beam focused to a full-width-at-half-maximum spot size of 200 nm with the sample at a temperature of 5 K, at which the Gd^{3+} ions have a large saturated magnetization. The structure factor at the (008)-x-ray reflection weights all 12 Gd^{3+} ions in the structural unit cell equally and includes a negligible non-resonant x-ray magnetic scattering contribution from Fe^{3+} ions (29). Further experimental details are in Materials and Methods.

Magnetic information can be extracted from the diffracted x-ray intensity using flipping ratios, precisely defined normalized differences between intensities recorded with different incident polarizations. We employ two flipping ratios closely linked to the magnetism of the Gd^{3+} ions: (i) F_{cir} , measured with opposite incident beam helicities and generally used in imaging approaches based on magnetic dichroism in absorption; and (ii) F_{π} , the normalized difference between intensities measured with π -polarized and the purely charged scattering component, that we introduce here. F_{cir} is familiar from x-ray scattering studies conducted using radiation scattered nearly parallel to the incident beam. π polarization is useful at large angles between the incident and diffracted beams, e.g. those of Bragg reflections. π polarization, does not, however, provide magnetic contrast for small scattering angles and thus has not been considered in previous studies employing only absorption contrast (30).

The flipping ratios are defined in terms of the diffracted x-ray intensities I_L , I_R , and I_{π} measured with left-, right-, and π -polarized incident beams as $F_{cir} = \frac{I_L - I_R}{2(I_L + I_R)}$ and $F_{\pi} = \frac{I_{\pi} - \alpha(I_L + I_R)}{\beta(I_L + I_R)}$.

The factors $\alpha = \frac{\cos^2 2\theta}{1 + \cos^2 2\theta}$ and $\beta = \frac{2}{1 + \cos^2 2\theta}$ describe the polarization dependence of the scattering of linearly polarized light and depend on the Bragg angle θ . The sum $I_L + I_R$ yields purely structural information, which allows comparison of the crystallographic and magnetic structures. The circular flipping ratio F_{cir} can be expected to have maxima when the magnetization of the Gd sublattice lies in the scattering plane defined by the incident and diffracted x-ray beams (28). Similarly, F_{π} can be expected to reach a maximum when the magnetization is perpendicular to the

scattering plane (28). These initial assumptions are consistent with more complete calculations using the FDMNES package (31).

Key features of the structure and magnetism of the GdIG layer at low temperature are revealed in Fig. 2 in x-ray nanobeam maps of a lithographically defined square around which the surrounding GdIG thin film was removed. An optical micrograph of this region appears in Fig. 2A. Maps of the flipping ratios F_{cir} and F_{π} in Figs. 2B and 2C show the distribution of magnetic domains within the GdIG layer. The point-to-point variation of F_{cir} and F_{π} in Figs. 2B and C is on the order of 1% and exhibits complementary contrast between the two flipping ratios that is distinct from the intensity variation in the structural image. As expected, no magnetic contrast is obtained in maps acquired with linear polarization in the plane of the surface, termed σ polarization (see plot in Supplementary Materials). We focus now on the F_{cir} signal, which has a larger magnitude than F_{π} and which is thus readily amenable to further analysis.

The resonant character of the magnetic contrast was probed by repeating the nanobeam mapping at several x-ray photon energies spanning the Gd L_2 edge, as illustrated in Fig. 3A. The sign and magnitude of F_{cir} vary rapidly as a function of photon energy, with comparatively low magnetic contrast for photon energies far from the resonance, i.e. at 7.932 and 7.946 keV. The energy dependence of the flipping ratio F_{cir} predicted using the FDMNES package is shown in Fig. 3B, assuming the Gd magnetization pointing along the cubic $\langle 111 \rangle$ directions (31). All of the predicted values of F_{cir} reach a relative maximum near 7.940 keV, with a strong dependence on the direction of the Gd magnetization. With the assumption that the probed area has the bulk magnetic structure with magnetic easy directions along $\langle 111 \rangle$, large positive and negative values of F_{cir} are expected for magnetizations along $[111]$ and $[\bar{1}\bar{1}\bar{1}]$ (or $[1\bar{1}\bar{1}]$ and $[\bar{1}\bar{1}1]$) because these directions lie within the plane containing the incident and diffracted x-ray beams (28).

The measured magnetic contrast between domains of opposite values of F_{cir} is shown as a function of photon energy in Fig. 3C. The magnetic contrast was measured using the integrated intensities in regions at the bottom left and bottom right of the images in Fig. 3A. By comparing the predicted and observed contrasts, we identify areas with large positive and negative values of F_{cir} to be regions with $[111]$ and $[\bar{1}\bar{1}\bar{1}]$ directions of the magnetization of GdIG, respectively. The maximum contrast is 1.6% at 7.940 keV. The maxima of the observed and predicted contrast agree and occur at the maximum in the total x-ray fluorescence, also shown in Fig. 3C. The close agreement between the predicted F_{cir} and fluorescence and the experimental observations of these quantities allows us to use the simulation to interpret the magnetic contrast reliably and to obtain maps of the distribution of the Gd-magnetization in the GdIG thin film.

Maps of F_{cir} were acquired for a second GdIG area at a photon energy of 7.938 keV and are shown in Fig. 4A. The precision of the experiment permits the unambiguous distinction of at least three values of F_{cir} at this photon energy, corresponding to different orientations of the Gd magnetization. Comparing the measured contrast with the contrast expected based on the predicted flipping ratios with these three ranges of F_{cir} , the local orientation of the Gd-magnetization within several domains can be determined to within an uncertainty of the sign of the magnetization. A diagram of the directions of the magnetic axes within the region mapped in Fig. 4A is shown in Fig. 4B.

As is apparent from both Figs. 2A and 4B, domain walls in the GdIG layer are in some places oriented in preferred crystallographic directions over distances of tens of micrometers. The domain boundaries in Fig. 4A have in-plane $\langle 110 \rangle$, $\langle 100 \rangle$ and approximately $\langle 310 \rangle$ orientations,

and the same domain-wall orientations are also apparent in regions of Figs. 2B and 3A. A detailed free-energy analysis (see Materials and Methods) predicts that in (001)-oriented GdIG thin films, the shape anisotropy causes the magnetization to be along $\langle 110 \rangle$ directions, i.e. in the plane of the film rather than $\langle 111 \rangle$ as in bulk GdIG, and that the Néel walls form with a four-fold magnetic anisotropy along one of the four in-plane $\langle 110 \rangle$ directions. The magnetic contrast for the $\langle 110 \rangle$ magnetization configuration can be expected to follow the same qualitative photon-energy dependence discussed above, with large magnitudes of F_{cir} observed when the magnetic moment is in the scattering plane. The calculations also show that the in-plane $\langle 100 \rangle$ boundary is expected to be a low-energy 90° Néel wall.

Discussion

The fine-scale domain pattern and the distribution of domain wall directions in Fig. 2 indicate that effects beyond the domain-wall energy contribute to determining the magnetic microstructure. The small-scale distribution of domain directions is further apparent in Fig. 5A, which shows maps of F_{cir} acquired at 7.938 keV at several scales from a region within Fig. 2. The region imaged in Fig. 5A is identical to Fig. 3, which permits regions of high and low F_{cir} in Fig. 5A to be assigned to $[111]$ and $[\bar{1}\bar{1}\bar{1}]$ magnetization, respectively. The domains exhibit a complex arrangement in which some regions of domain walls are clearly oriented with crystallographic facets, while others are disordered at the smallest imaged scale. Free energy calculations (see Materials and Methods) reveal that the energy degeneracy of the in-plane magnetization directions is removed due to the magnetocrystalline anisotropy and thus indicate that the domain pattern occurs within a complex energetic landscape in which domain walls also interact with a spatially complex strain field.

A structural investigation reveals that the synthesis of the GdIG epitaxial layers results in the spontaneous formation of a nanoscale crystalline microstructure, as in maps of the lattice tilt along the direction of the beam footprint shown in Fig. 5B. Here, the orientation of the lattice, Fig. 5B, exhibits variations on the order of 10^{-3}° over μm -scale distances. Previous nanobeam studies in other epitaxial systems indicate that this tilting pattern can arise from complex series of effects including extended defects and surface steps (32). The tilt images and the map of the total diffracted intensity shown in Fig. 5C both span the same regions as the magnetic maps in Fig. 5A. A similar pattern of spatial variation appears in the overall diffracted intensity in Fig. 5C.

The structural results in Fig. 5 indicate that exploiting the influence of crystallographic microstructure on the domain configuration and magnetic anisotropy will make it possible to develop garnet-based devices with structurally controlled magnetism. Such approaches have previously been employed at far larger length scales to tune the magnetic anisotropy in garnets, including by varying of the epitaxial mismatch between the garnet film and its substrate (33, 34). It is now clear that this structural approach to the control of domain patterns is applicable at the nanoscale.

Conclusion

The imaging study presented here represents an important first step in combining nm-resolution structural and magnetic probes to address challenges in spintronics. The ability to reveal the coupling between magnetism and crystallographic structure is an important distinction between

magnetic diffraction and magnetic imaging using x-ray spectroscopy. The future use of nanobeam magnetic diffraction includes the possibility of providing an additional contrast mechanism based on the incident-angle dependence of the magnetic scattering cross sections by studying different Bragg reflections. Present developments in x-ray sources provide the optical brilliance required to investigate room-temperature nanoscale magnetic domains, for which exploiting the weaker magnetic resonance of the Fe resonance edge will be essential. Ptychographic analysis will permit the simultaneous and rapid reconstruction of magnetic and structural information at the nanometer scale and in 3D, as is presently possible with studies of the crystallographic structure (35). Finally, combining nanobeam diffraction with time-resolved techniques, including those based at x-ray free-electron laser light sources, has the potential to open up new fields based on understanding the coupling between the dynamics of the crystal lattice, nanoscale domain patterns, and the magnetic functionality (36, 37).

The magnetic structure of GdIG revealed here has potentially profound consequences for the design of materials for spintronic devices based on the spin-Seebeck effect. The diversity of domain directions apparent in magnetic images indicates that the low-magnetic-field SSE is significantly affected by the vector addition of electric fields from regions of different magnetization. The discovery of the domain morphology at zero field and the apparent interaction of the domain walls with the crystallographic distortion offer a novel way to enhance low-field SSE by optimizing the structural properties of the device. This can be done, in principle, through the selection of oxide substrates with optimized symmetry and lattice parameter and through the nanomechanical design of the SSE device. More generally, the results suggest that further opportunities will arise in the interaction of structural and magnetic effects at the nanoscale, for example, the discovery of new types of domain walls that cannot be stabilized by magnetic fields alone, analogously to the formation of charged domain walls in improper ferroelectrics.

Materials and Methods

GdIG Thin Film Fabrication and Characterization

GdIG has a cubic crystal structure with a large unit cell in which magnetism arises from both Fe^{3+} and Gd^{3+} ions. The Fe^{3+} ions are in inequivalent octahedral (16a) and tetrahedral (24d) sites and Gd^{3+} ions are located at (24c) dodecahedral sites. In bulk, GdIG is ferrimagnetic, with a Curie temperature $T_C = 560$ K and Fe^{3+} magnetic moments on the octahedral and tetrahedral sites along opposite directions in the $\langle 111 \rangle$ family, a total of eight possible local directions of the magnetization. The difference in the number of Fe^{3+} ions on the two inequivalent sites leads to a net Fe magnetization. The Gd sublattice magnetization has a direction opposite the net Fe magnetization at zero magnetic field and has a magnitude that increases at low temperature and serves as a reliable marker of the local magnetization (4, 38).

The GdIG thin film was deposited on a single crystalline, (100)-oriented gadolinium gallium garnet ($\text{Gd}_3\text{Ga}_5\text{O}_{12}$, GGG) substrate by pulsed laser deposition (PLD) using a KrF excimer laser and a stoichiometric GdIG target. Optimized structural and magnetic properties of the GdIG thin films were obtained by using a substrate temperature of 450°C , a pure oxygen atmosphere of 25 μbar , a laser energy fluence of 2.0 J/cm^2 at the target surface, and a frequency of the excimer laser of 10 Hz. We here focus on a 21 nm thick GdIG thin film. The high crystalline quality and low mosaicity of the GdIG layer was demonstrated by finite thickness fringes around the GdIG 400 reflection as well as by the low full width at half maximum (FWHM) of the rocking curve

around the 400 reflection of less than 0.02° . The GdIG with an out-of-plane lattice constant of 1.258 ± 0.002 nm, which is slightly larger than the bulk value of 1.247 nm due to the compressive in-plane strain imposed by the GGG substrate. The GdIG thin film was covered *in situ*, without breaking the vacuum, with a 2.8 nm thick Pt layer deposited via electron beam evaporation at room temperature.

For the longitudinal SSE experiment, the GdIG/Pt bilayer is patterned into a Hall bar mesa structure, as shown in Fig. 1C, using optical lithography and Ar ion beam milling. A temperature gradient across the GdIG/Pt interface along the surface normal z was generated by sourcing a large current of 6 mA along the Hall bar in x -direction. The longitudinal resistance of the Pt layer is exploited for on-chip thermometry. The transverse voltage V_{SSE} (along the y -direction) was measured as a function of the magnetic field applied along the x -direction for three different temperatures 20 K, 150 K, and 300 K. A current reversal method was employed to exclude any spurious asymmetric effects (39).

As illustrated in Fig. 1D, V_{SSE} has opposite signs at a fixed value of $\mu_0 H$ above the magnetic saturation field for temperatures below and above the magnetic compensation temperature, $T_{comp} = 288$ K, at which the total remnant magnetization passes through zero due to the net cancellation of the magnetizations of the Fe and Gd sublattices. At a finite magnetic field, the direction of the total magnetization including both the Gd and Fe sublattices reverses at T_{comp} , causing the observed sign change of V_{SSE} between 300 K and 150 K. Another sign change of V_{SSE} can be observed between 150 K and 20 K due to the competition of the heat-to-spin current conversion efficiency from different magnon branches (4, 11).

X-ray Nanobeam Diffraction Experimental Details

X-ray nanobeam diffraction experiments were conducted at the ID01 beamline of the European Synchrotron Radiation Facility. A two-bounce horizontal deflection Si [111] monochromator produced an incident beam with linear polarization in the horizontal plane with energy bandwidth $\Delta E/E \approx 10^{-4}$. An x-ray phase plate was added to the beamline to allow the incident polarization to be selected (40). A quarter-wave setting was employed to convert the incident linear σ -polarized photons from the undulator insertion device to left- and right-circular polarized light. A second, half-wave setting was used to produce incident π -polarized light.

For the experiments described in the main text, the incident photon energy E was tuned to the Gd L_2 absorption edge near $E = 7.94$ keV to maximize the scattering sensitivity to the Gd magnetic moments via x-ray resonant scattering (41). The incident x-ray beam was focused to a spot on the sample using a Fresnel zone plate (FZP) with outermost zone width of 100 nm. The beam focused to the first order focus of the zone plate was selected with an order-sorting aperture. At the Gd L_2 edge, the Bragg angle for the GdIG 008 reflection is 30.06° . The focused beam cross section had a FWHM of 200 nm, leading to a footprint on the surface at the Bragg condition of 200 nm (along horizontal direction of the maps in Figs. 2 to 4) $\times$ 400 nm (along the vertical direction in the maps). Maps of the intensity of the GdIG 008 reflection were acquired by scanning the FZP using a piezoelectric stage. The change in the effective diffracted beam angle during the scans was orthogonal to the angle analyzed to form the tilt map shown in Fig. 5B. The sample was cooled in a continuous flow helium cryostat.

The intensity maps were repeated for incident left, right, and π -polarized light. The flipping ratios F_{cir} and F_π discussed in the text were computed at each pixel of the map by (i) correcting the

measured diffracted intensity to remove source intensity variations by using the signal from an intensity normalization detector located before the diamond phase plate and (ii) separately correcting the left-, right-, and π -polarized signals to account for the small difference in the intensity of the x-ray beams transmitted through the phase plate at the angular settings resulting in these polarizations.

Supplementary Materials

Supplementary Text

Fig. S1. Measured and simulated Poincaré coefficients of incident x-ray beam.

Fig. S2. Predicted flipping ratios for π polarization.

Fig. S3. Maps of total intensity and F_{cir} , F_{π} , and F_{σ} flipping ratios.

Fig. S4. Magnetic model.

References (42-50).

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Figures and Tables

Fig. 1. Magnetic structure of GdIG. (A) Atomic structure and magnetic moments in one atomic layer of the GdIG cubic unit cell, highlighting oxygen octahedrons and tetrahedra. Arrows indicate the directions of the magnetic moments of Gd^{3+} ions (red) and Fe^{3+} ions on tetragonal (light green) and octahedral (dark green) sites. (B) Directions of the total magnetization $\mathbf{M}$ under the assumption of bulk-like $\langle 111 \rangle$ magnetization directions in a (001)-oriented GdIG thin film. (C) Hall-bar spin-Seebeck effect device consisting of a patterned GdIG magnetic insulator and a thin Pt conductor. (D) Magnetic-field hysteresis of V_{SSE} at 20 K, 150 K, and 300 K. (E) Electric field polarization vectors for right (R)-, left (L)-, and π -polarized incident x-ray nanobeams.

Fig. 2. Domain imaging in GdIG SSE devices. (A) Optical micrograph of a patterned GdIG layer from which GdIG has been removed in the area outside the light square. X-ray nanobeam diffraction maps of (B) circular-polarization flipping ratio F_{cir} and (C) linear π -polarization flipping ratio F_{π} in the same region. The areas of nearly uniform contrast at the edges of the images in (B) and (C) are in regions from which the GdIG layer had been removed and in which there is vanishingly low diffracted intensity.

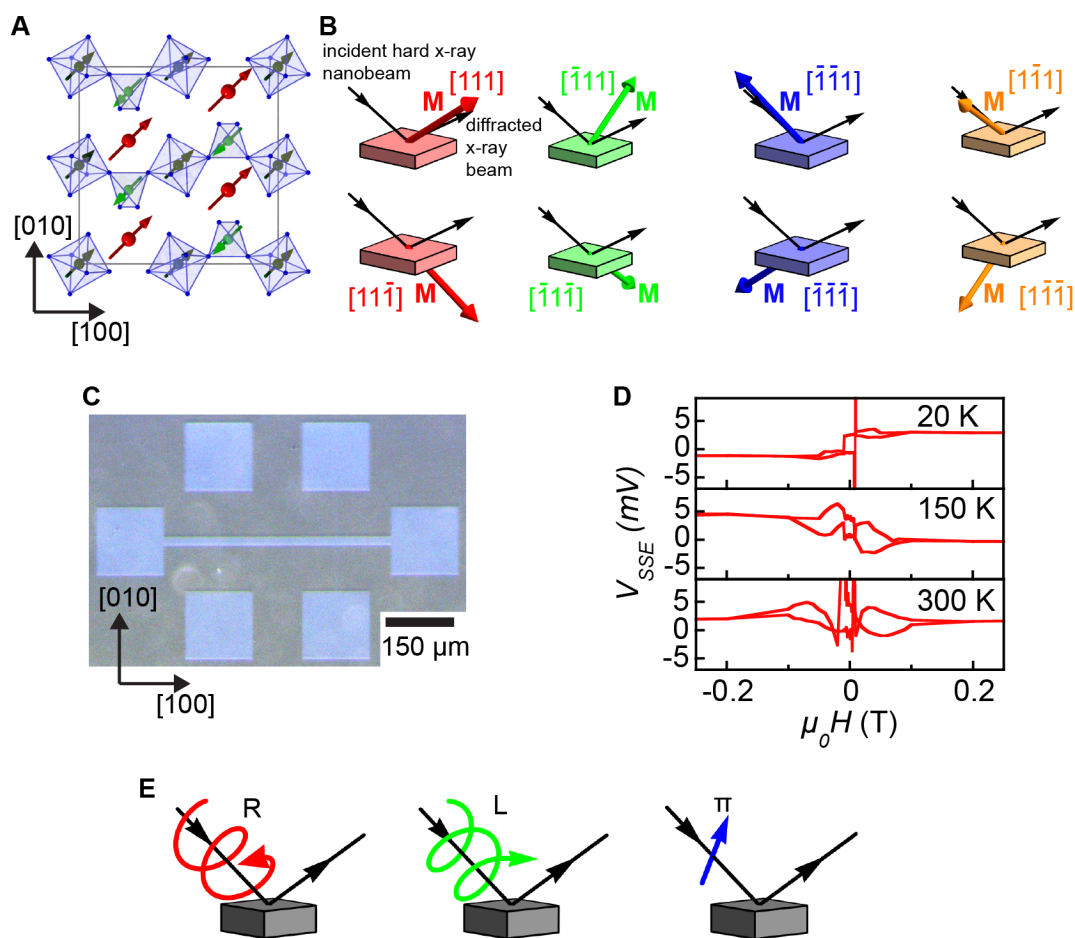
Fig. 3. X-ray photon energy dependence of resonant scattering contrast. (A) Maps of F_{cir} of the same region of the GdIG layer for several photon energies near the Gd L_2 resonance. (B) Predicted F_{cir} for four $\langle 111 \rangle$ magnetization directions. (C) Observed and predicted contrast of F_{cir} measured for regions of (A) with opposite values of F_{cir} (lower panel). X-ray fluorescence intensity as a function of photon energy (upper panel).

Fig. 4. Magnetic domain wall orientation and magnetic structure. (A) Nanobeam diffraction map of F_{cir} within a region of the GdIG pattern with large magnetic domains. The footprint of the incident and diffracted x-ray beams is horizontal. The nearly uniform contrast at the edges of the image in (A) are in regions from which the GdIG layer had been removed. (B) Schematic of the in-plane projection of the magnetization of the domains. The edges of the patterned GdIG layer are indicated by dashed lines.

Fig. 5. Interaction between Crystallographic and Magnetic Microstructure. (A) Nanobeam diffraction maps of F_{cir} at micrometer length-scales. The in-plane crystallographic directions are shown in the diagram below the images. (B) Crystallographic tilt towards the [010] (vertical) direction. (C) Integrated diffracted x-ray intensity at the 008 Bragg reflection. The magnetic response to the structural variation in (B) and (C) competes with the development of facets along directions of the lowest domain boundary energy.

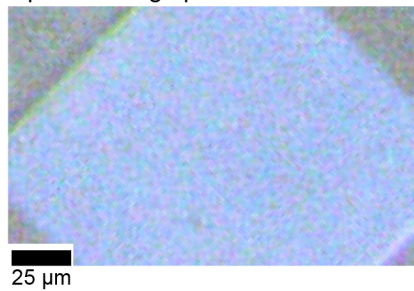
Figures

Fig. 1

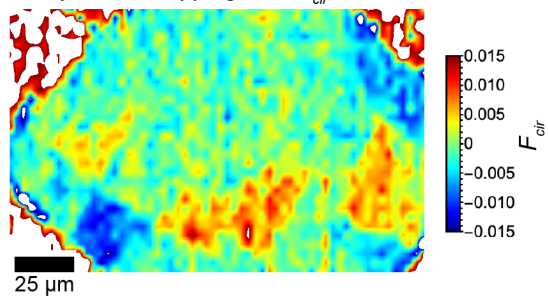


8 **Fig 2.**

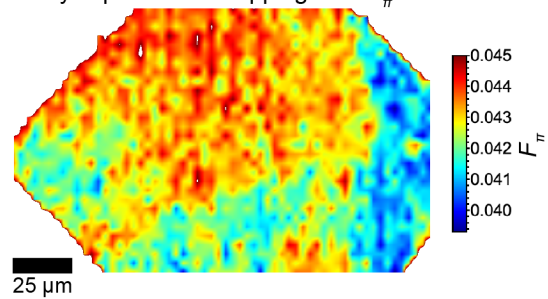
A optical micrograph



B x-ray circular flipping ratio F_{cir}



C x-ray π -polarization flipping ratio F_{π}



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Fig. 3.

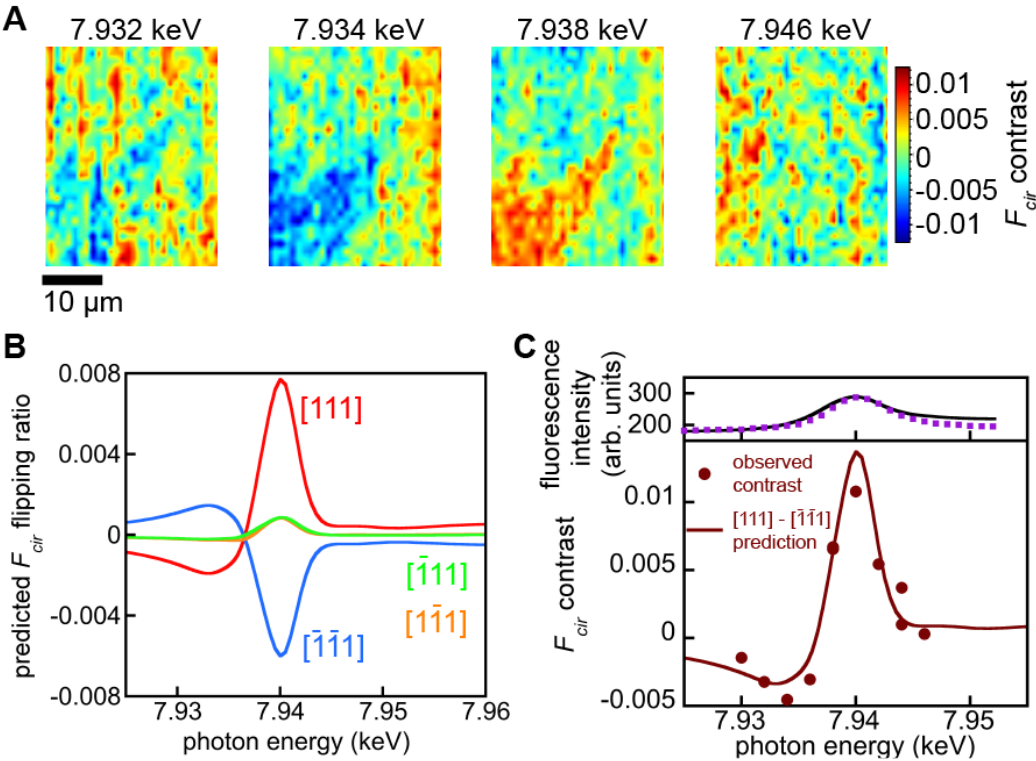
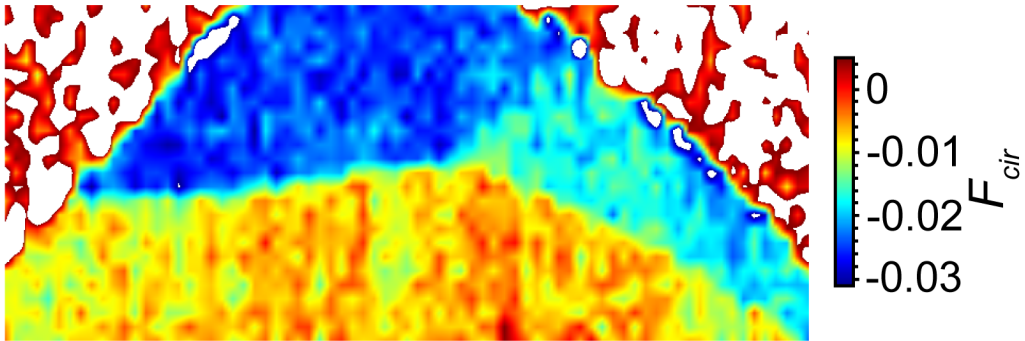
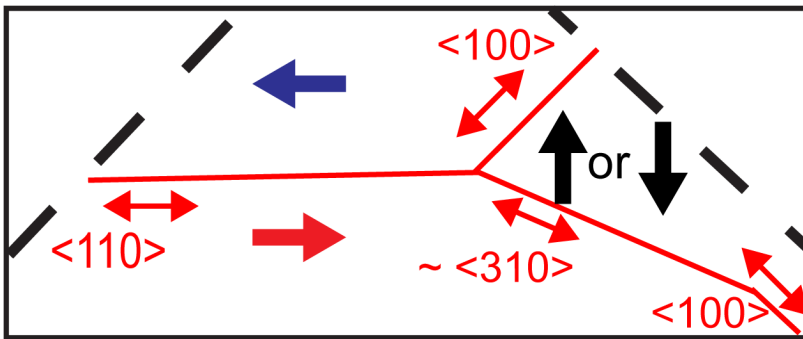


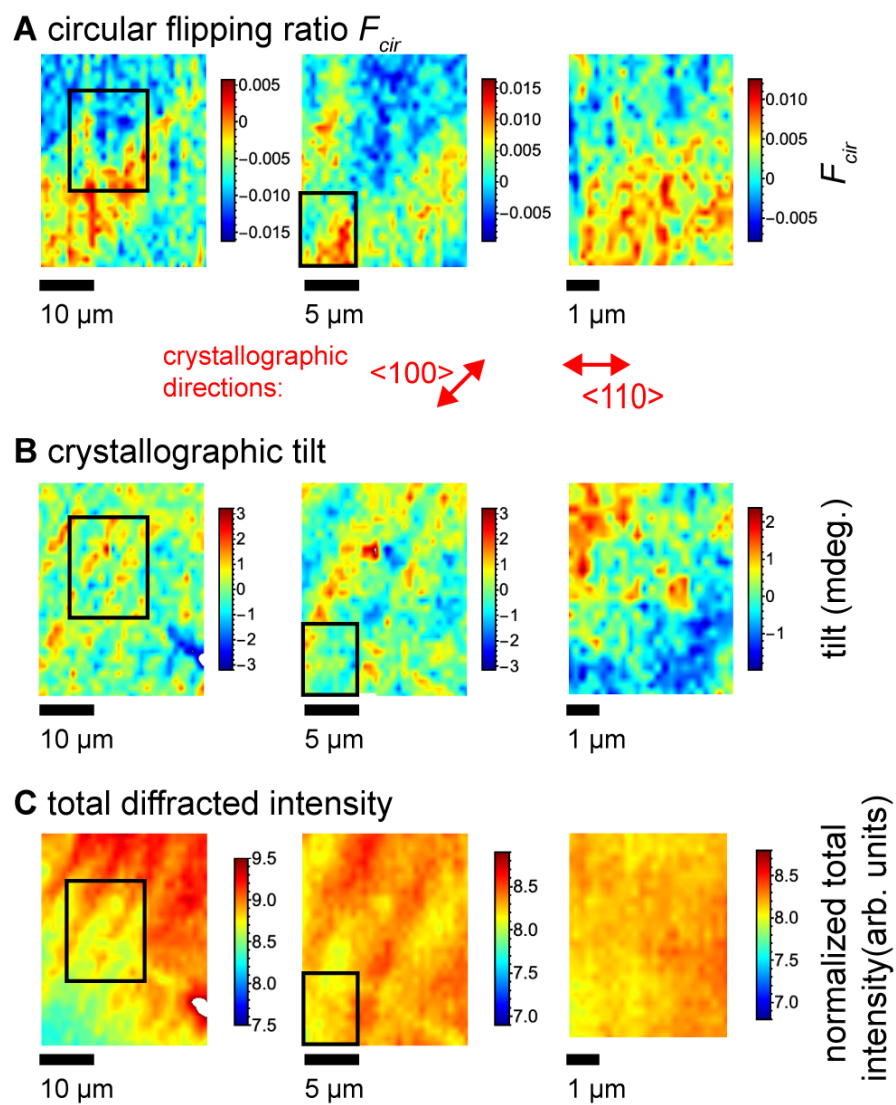
Fig. 4.

A circular flipping ratio F_{cir}



B





Supplementary Materials for

Resonant Nanodiffraction X-ray Imaging Reveals Role of Magnetic Domains in Complex Oxide Spin Caloritronics

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This PDF file includes:

Supplementary Text

Fig. S1. Measured and simulated Poincaré coefficients of incident x-ray beam.

Fig. S2. Predicted flipping ratios for π polarization.

Fig. S3. Maps of total intensity and F_{cir} , F_{π} , and F_{σ} flipping ratios.

Fig. S4. Magnetic model.

Supplementary Text

Incident x-ray beam preparation and polarization characterization. The incident x-ray beam was prepared in a specified polarization using a diamond phase plate (28). The x-ray phase plate consisted of a diamond crystal with a nominal thickness $t=800\text{ }\mu\text{m}$ and a [110] surface normal, mounted at an angle of 45° so that there were equal projections of the incident horizontal x-ray polarization onto the σ and π polarizations of the diffracting diamond planes. The plate was set with an angular orientation with respect to the incident beam such that the diamond (111) planes were misoriented by 54.74° with respect to the plane of the surface with diffraction in a Laue diffraction geometry. The effective thickness of the crystal at Bragg angle θ_B was thus $t_{eff}=t/\sin(35.26^\circ+\theta_B)$.

The phase shift δ between the two orthogonal linear components of the x-ray beam for when the diamond is misoriented by $\Delta\theta$ with respect to the Bragg condition is given by (28):

$$\delta = \frac{r_e^2 \lambda^3 t_{eff} \sin(2\theta_B) \text{Re}(F^+ F^-)}{2\pi V^2} \frac{1}{\Delta\theta}$$

Here r_e is the classical radius of the electron, λ is the x-ray wavelength, F^+ and F^- are the structure factors of the diamond 111 and $\bar{1}\bar{1}\bar{1}$ reflections, and V is the volume of the diamond unit cell. The vector sum of the two linear components produces an altered transmitted polarization depending on the value of δ .

The transmitted beam polarization is described by the Poincaré coefficients for circular and linear polarization, P_c and P_L (28):

$$P_c = \sin(\delta) \quad (1a)$$

$$P_L = \cos(\delta) \quad (1b)$$

The polarization of the incident x-ray beam was characterized by measuring and normalizing the intensities I_H and I_V of the horizontally and vertically polarized components of the beam. These intensities were measured using scattering to 90 degrees in the vertical and horizontal directions, respectively. The Poincaré coefficients were determined from the intensities using (28,42):

$$P_L = \frac{I_H - I_V}{I_H + I_V}$$
$$|P_c| = (1 - P_L^2)^{1/2}$$

This approach does not allow the sign of P_c to be determined.

The measured and predicted values of the P_L and P_c are shown in Figs. S1(a) and S1(b). The measured curve accurately follows the prediction. There are two notable artifacts in analysis shown in Fig. S1:

(1) The intensities I_H and I_V were measured using polyimide foils mounted at 45° with respect to the beam and scattering in the horizontal and vertical directions, respectively. The intensities were not measured on an absolute scale and were thus normalized with respect to the maxima and minima of each signal, respectively. This approach likely introduces an artificially large value of the linear polarization P_L because the value of I_V is underestimated at its minimum.

(2) The prediction does not account for the finite angular divergence and energy spread of the incident x-ray beam. The high-frequency oscillations apparent at low values of the angular deviation are thus not observed in the data. The predicted oscillations at angular offsets with a magnitude of more than approximately 0.05° , however, are accurately reproduced in the experimental data.

The three angular settings of the phase plate for the vertical linear polarization and the two circular polarizations are illustrated as dashed lines in Fig. S1. The Poincaré coefficients at these angular settings are: (i) $P_L = -0.92$, termed π -polarized in the text, (ii) $|P_c| = 0.986$ and (iii) $|P_c| = 0.996$. Settings (ii) and (iii) represent opposite helicities of circular polarization. The Poincaré coefficients are very close to 1 and are thus assumed to be exactly 1 in the analysis of the magnetic scattering experiments.

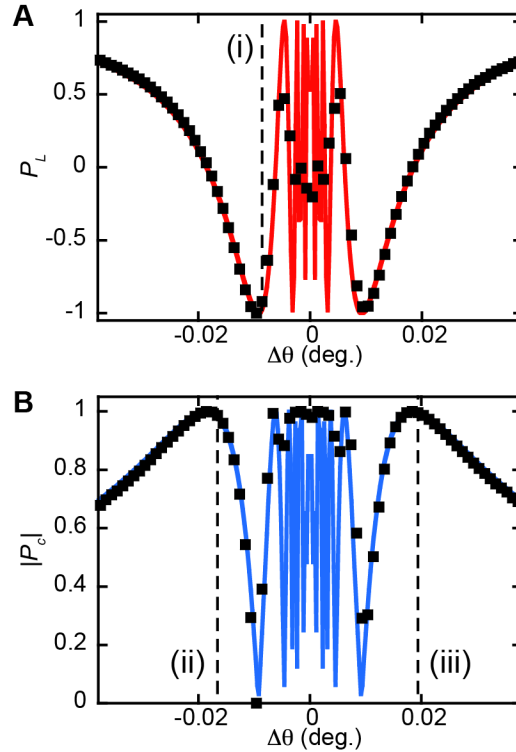


Fig. S1. Measured and simulated Poincaré coefficients of incident x-ray beam. (A) Measured (square points) linear and (B) circular components of the x-ray radiation after the x-ray phase plate, plotted as a function of the offset between angular setting of the phase plate and the diamond 111 Bragg angle. Vertical lines indicate the angular settings of the phase plate for (i) π linear polarization and (ii) L and (iii) R circular polarizations. The polarization predicted using equations (1a) and (1b) are plotted as solid lines.

Prediction of magnetic diffraction intensity. The intensities of diffracted x-rays from the 008 reflection were predicted for L- and R-circular and π -polarized linear incident polarization using the FDMNES software package. This code can work either using the multiple scattering theory under the muffin-tin approximation on the potential shape, or within the finite difference method with a free shape potential. In the present study, the first approach proved to be sufficient.

Simulations were relativistic, including the spin-orbit interaction, and considered both dipole and quadrupole transition channels. The FDMNES simulations thus incorporate a more comprehensive physical description than analytic formulae, as for example in (28).

A first guess of the electronic configuration was obtained by applying the Hund rule. The FDMNES code then solves the Dyson equation to calculate the electronic structure inside a cluster centered on the resonant atom. For the calculation reported here, the cluster had a 5 Å radius and contains 39 atoms. The resonant atomic form factors were then calculated from the electronic structure. The reflection intensities were obtained by considering also the non-resonant magnetic and Thomson terms, taking into account the magnetic space group and the incoming polarization.

The flipping ratios F_{cir} and F_{π} were calculated from the predicted intensities using the formulas given in the text. The predicted values of F_{cir} and F_{π} for a range of photon energies spanning the Gd L_2 edge are shown in Fig. 3b of the text and Fig. S2, respectively.

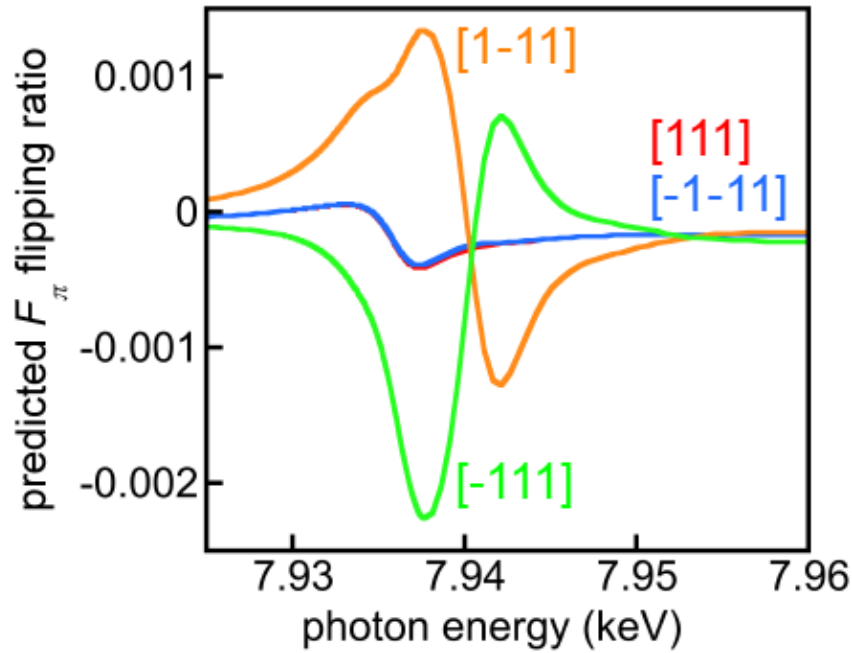


Fig. S2. Predicted flipping ratios for π polarization. Predicted values of the π -polarization flipping ratio F_{π} as a function of incident photon energy.

Absence of Magnetic Contrast with Linear σ Incident Polarization. Magnetic scattering contrast is not apparent in maps collected with σ linear incident polarization, in which the linear polarization is in the plane of the sample surface. A σ -polarized incident x-ray beam was prepared by setting the diamond phase plate offset angle $\Delta\theta$ to -0.86° . Under these conditions the Poincaré coefficients given by extrapolating from Fig. S1 are $P_L \approx 1$ and $|P_c| = 0$, corresponding to σ polarization. The maps of the diffracted intensity acquired with σ polarization were analyzed using a flipping ratio defined as $F_{\sigma} = \frac{I_{\sigma} - \alpha(I_L + I_R)}{\beta(I_L + I_R)}$. The factors α and β are given in the main text and correct the intensities I_L and I_R accounting for the Lorentz polarization factor in the total intensity.

Maps of the total intensity, F_{cir} , F_{π} , and F_{σ} acquired at a photon energy of 7.938 keV are shown in Figs. 3A to D for a region near the edge of the lithographically defined GdIG feature. Maps of F_{cir} and F_{π} have magnetic contrast with a magnitude similar to the maps shown in Figs. 2 and 3. This contrast is absent in the image in Fig. S3D of the σ -polarization flipping ratio F_{σ} . The point-to-point variation of F_{σ} is smaller than for F_{cir} and F_{π} and exhibits contrast corresponding to the noise in the x-ray measurement, with no correlation to the magnetic features.

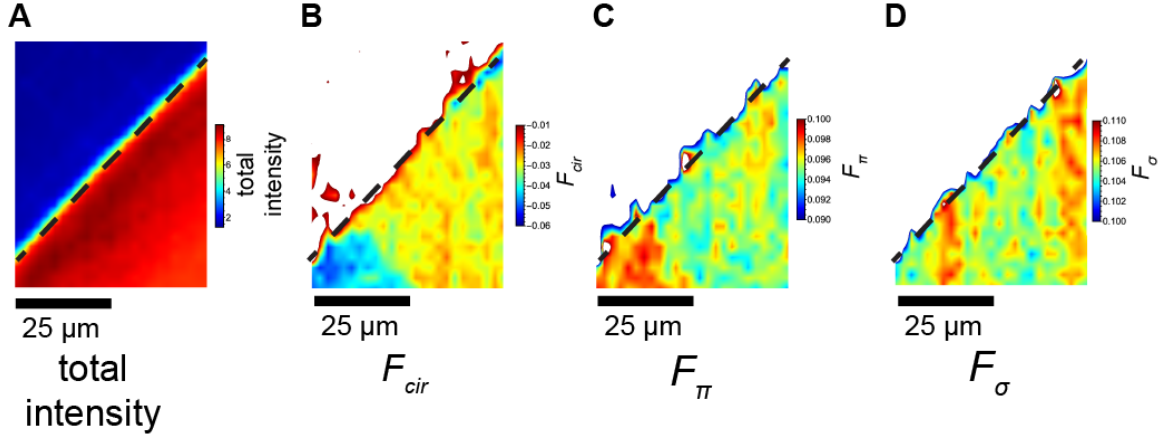


Fig. S3. Maps of total intensity and F_{cir} , F_{π} , and F_{σ} flipping ratios. Nanobeam diffraction maps of the edge of a patterned GdIG region in which the GdIG layer is present below the dashed line. (A) Total intensity, sum of images acquired with L and R incident polarization, and flipping ratios (B) F_{cir} , (C) F_{π} , and (D) F_{σ} .

Free energy analysis and domain-wall energy calculation. The total magnetic anisotropy energy density of the (001)-oriented GdIG thin film f_{tot} is the sum of the magnetocrystalline anisotropy energy density f_{anis} , the magnetic shape anisotropy energy density f_{shape} , the magnetoelastic energy density f_{melast} , and the elastic energy density f_{elast} (43). Specifically, $f_{anis} = K_1(m_1^2m_2^2 + m_2^2m_3^2 + m_3^2m_1^2) + K_2m_1^2m_2^2m_3^2$ with the 1st and 2nd order cubic anisotropy constants K_1 and K_2 , respectively, and $f_{shape} = 0.5\mu_0M_s^2m_3^2$ with the saturation magnetization M_s . Here $(m_1, m_2, m_3) = (\sin\theta\cos\phi, \sin\theta\sin\phi, \cos\theta)$ are the directional cosines of the magnetization defined in the crystallographic reference system using the angles defined in the inset of Fig. S4A. The cubic anisotropy constants at 5 K are $K_1 = -2.164 \times 10^4 \text{ J/m}^3$, $K_2 = (0 \pm 0.9) \times 10^3 \text{ J/m}^3$ (44), μ_0 is the vacuum permeability, and $M_s = 5.52 \times 10^5 \text{ A/m}$ (4). The energy densities f_{melast} and f_{elast} can be expressed as:

$$f_{melast} = B_1 \left[e_{11}(m_1^2 - \frac{1}{3}) + e_{22}(m_2^2 - \frac{1}{3}) + e_{33}(m_3^2 - \frac{1}{3}) \right] + B_2(2m_1m_2e_{12} + 2m_1m_3e_{13} + 2m_2m_3e_{23}) \quad (1)$$

$$f_{elast} = \frac{1}{2}c_{11}(e_{11}^2 + e_{22}^2 + e_{33}^2) + c_{12}(e_{11}e_{22} + e_{22}e_{33} + e_{11}e_{33}) + 2c_{44}(e_{12}^2 + e_{23}^2 + e_{13}^2) \quad (2)$$

The magnetoelastic coupling coefficients at ~ 5 K are: $B_1 = -1.5\lambda_{100}(c_{11}-c_{12}) = -1.659 \times 10^6 \text{ J/m}^3$ and $B_2 = -3\lambda_{111}c_{44} = 9.181 \times 10^5 \text{ J/m}^3$. The elastic stiffness coefficients are $c_{11} = 2.731 \times 10^{11} \text{ Pa}$, $c_{12} = 1.250 \times 10^{11} \text{ Pa}$ and $c_{44} = 0.741 \times 10^{11} \text{ Pa}$ (45). The anisotropic magnetostriction coefficients are

$\lambda_{100} = 7.47 \times 10^{-6}$ and $\lambda_{111} = -4.13 \times 10^{-6}$ (46). The elastic stiffness and the magnetostriction coefficients are reported from measurements at 4.2 K using GdIG single crystals. From $\sigma_{i3} = 0$ (the condition of stress-free surfaces) and the magnetoelastic equation of state $\sigma_{i3} = \partial(f_{\text{melast}} + f_{\text{elast}})/\partial e_{i3}$ ($i = 1, 2, 3$), one can derive $e_{33} = \frac{B_1 - 3c_{12}(e_{11} + e_{22}) - 3B_1 m_3^2}{3c_{11}}$, $e_{13} = -\frac{B_2 m_1 m_3}{2c_{44}}$ and $e_{23} = -\frac{B_2 m_2 m_3}{2c_{44}}$. Plugging in the expressions of e_{i3} into Eqs. (1) and (2), omitting all terms that are independent of m_i ($i=1, 2, 3$), one has, (47, 48)

$$\begin{aligned} \Delta f_{\text{tot}}(m_1, m_2, m_3) = & B_1(e_{11}m_1^2 + e_{22}m_2^2) + \left[\frac{1}{2}\mu_0 M_s^2 + \frac{B_1^2}{3c_{11}} - \frac{B_1 c_{12}}{c_{11}}(e_{11} + e_{22}) \right] m_3^2 \\ & + K_1 m_1^2 m_2^2 + \left(K_1 - \frac{B_2^2}{2c_{44}} \right) (m_1^2 + m_2^2) m_3^2 \\ & + K_2 m_1^2 m_2^2 m_3^2 - \frac{B_1^2}{c_{11}} m_3^4 \end{aligned} \quad (3)$$

Minimizing Eq. (3) with respect to m_i (or equivalently the angles θ and φ) allows us to determine the global and local energy minima under biaxial in-plane strains e_{11} , e_{22} , and e_{12} . Assuming that the 21-nm-thick (001) GdIG film is coherently strained by the cubic (001)-oriented GGG substrate, one has $e_{11} = e_{22} = -9.636 \times 10^{-3}$, calculated from the experimentally measured out-of-plane lattice mismatch. Due to the epitaxial growth of GdIG on GGG, we do not expect any shear strain in the film plane ($e_{12} = 0$).

A plot of f_{tot} as a function of θ and φ is shown in Fig. S4A. The magnetic easy axis of the film is predicted by minimizing f_{tot} , as shown in Figs. 4A and B (49). The large saturation magnetization of GdIG at low temperature causes the demagnetization term $\frac{1}{2}\mu_0 M_s^2 m_3^2$, to be dominant, favoring in-plane magnetization, i.e. a magnetically easy (001)-plane. This is despite the fact that the biaxial compressive in-plane lattice mismatch strains ($e_{11} = e_{22} < 0$) favors a perpendicular magnetization along the [001] or [00-1] directions via the finite magnetoelastic coupling.

The anisotropy obtained from Eq. (3) and shown in Figs. S4A and B predicts that GdIG thin films have an in-plane magnetic easy axis. Based on this prediction, it is reasonable to assume that the in-plane boundary oriented along $\langle 110 \rangle$ boundary, as in Fig. 4B, is a 180° Néel wall, across which magnetization rotates, for instance, from [110] to $[\bar{1}\bar{1}0]$. If the films were isotropic with respect to in-plane magnetization, the magnetization rotation could occur along any direction in the (110) plane. However, due to the predicted four-fold in-plane magnetic anisotropy (Fig. S4B), caused by the magnetocrystalline anisotropy, the total energy will be minimized when the propagation vector of magnetization rotation is along one of the four in-plane easy directions, such as k_1 ($[1\bar{1}0]$).

The energy density of a 180° Néel wall is given by (50):

$$\begin{aligned} \sigma^{180} &= 2\sqrt{A} \int_0^\pi \sqrt{g(\beta)} d\beta \\ g(\beta) &= \Delta f_{\text{tot}}(m'_1, m'_2, m'_3) \end{aligned}$$

Here (m'_1, m'_2, m'_3) are the direction cosines of the magnetization defined in the crystallographic reference system and can be expressed using angles α and β . Here $m'_i = R_{ij}m_j$ ($i, j=1,2,3$), where the rotation matrix R_{ij} depends on α :

$$R_{rotate}(\alpha) = \begin{bmatrix} \frac{\sqrt{2}}{2} \cos \alpha & \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \sin \alpha \\ -\frac{\sqrt{2}}{2} \cos \alpha & \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \sin \alpha \\ -\sin \alpha & 0 & \cos \alpha \end{bmatrix}$$

while $(m_1, m_2, m_3) = (\sin \beta, \cos \beta, 0)$ for a 180° Néel wall. The isotropic exchange coefficient A only influences the absolute magnitude of the wall energy density.

The 90° Néel wall energy density is half of that for a 180° Néel wall. Thus, its energetically favorable propagation vector should likewise follow one of the four easy in-plane directions such as k_1 . For example, consider that magnetization rotates from $[110]$ by 90° to $[1\bar{1}0]$ with a propagation vector along $[1\bar{1}0]$ as well, the 90° Néel wall boundary should then be 45° with respect to both $[110]$ and $[1\bar{1}0]$, that is, the $[100]$ direction.

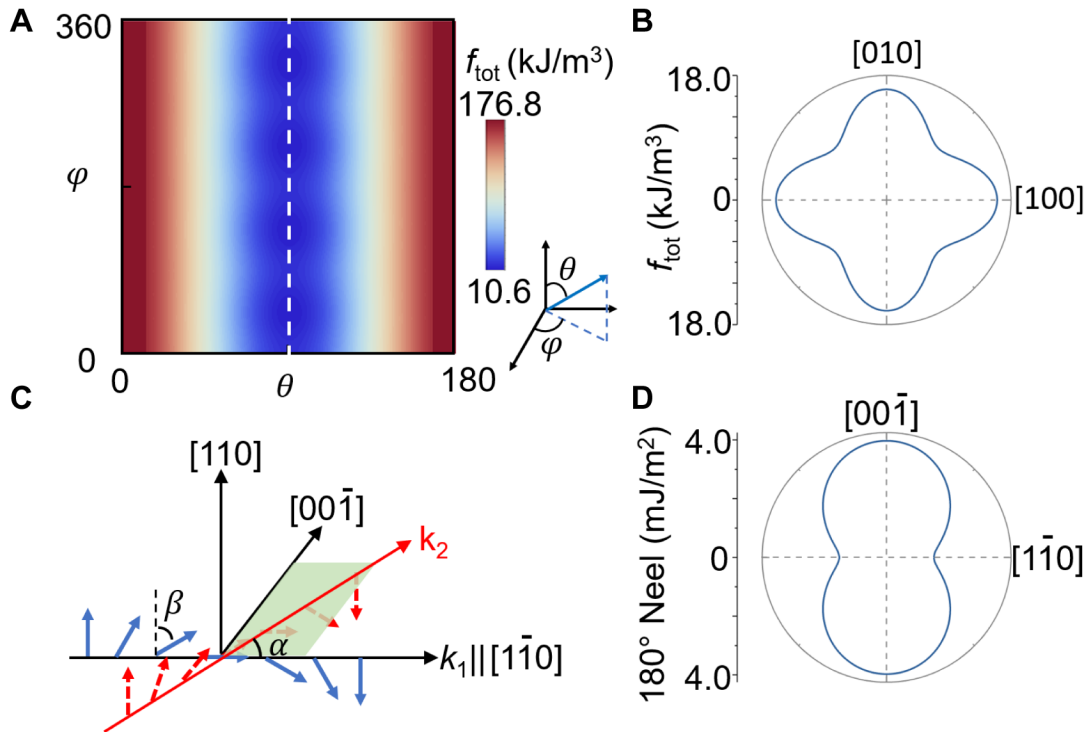


Fig. S4. Magnetic model. (A) Magnetic anisotropy energy density f_{tot} of the (001) GdIG thin film as a function of the azimuth angles θ and φ defined in the inset. (B) Variation of f_{tot} as a function of φ for in-plane magnetization (i.e. with $\theta=90^\circ$). (C) Schematic of a 180° Néel Wall with an in-plane $[110]$ boundary. The local magnetization (red or blue arrows) varies cycloidally across the $[110]$ boundary. α is defined the angle between the propagation vector k_2 and $[1-10]$ and β is the angle between the local magnetization and the $[110]$ boundary. (D) Calculated 180° Néel wall energy density as a function of the propagation vector direction parameterized by the angle α .