

Article

# Classification and Comparison of Dividing Walls for Distillation Columns

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Received: 27 April 2020; Accepted: 11 June 2020; Published: 16 June 2020



**Abstract:** A classification method is proposed to classify dividing walls into 5 types. Each type of dividing wall has its unique structural characteristics which impact its total vapor duty, construction complexity and controllability. Based on this classification, a comprehensive guideline to draw optimal dividing wall columns for any *n*-component distillation is provided.

**Keywords:** dividing wall column; process intensification; multicomponent distillation

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## 1. Introduction

Dividing wall columns (DWCs) are known to reduce the capital cost of a distillation process by putting multiple columns into a single shell [1–4]. The saving comes from the reduction of both the total number of column shells and the associated equipment pieces. However, besides capital cost saving, considerable literature also claims the use of dividing walls saves energy [5,6], but such conclusions are based on comparing DWCs with energy intensive column sequences and not with the corresponding thermodynamically equivalent sequences. Each DWC configuration has a thermodynamically equivalent simple column sequence [7]. For example, the well-known Wright's dividing wall column [8] (Figure 1a) is thermodynamically equivalent to the 3-component fully thermally coupled (FTC) configuration (Figure 1b) which is also known as Petlyuk configuration. Therefore, both versions have identical optimal heat duties. In these figures and all other figures in this article, ABC represents a mixture stream in which A is the most volatile component and C is the least volatile one. Filled circles represent condensers; unfilled circles represent reboilers. For a ternary distillation, the FTC configuration is known to have the lowest heat duty among all basic column configurations and their thermally coupled derivatives [9–12]. Therefore, its equivalent DWC in Figure 1a also has the same lowest heat duty. The energy saving of Wright's dividing wall column does not come from putting two columns within the FTC configuration into one single shell, but from the inherent thermodynamic properties of the FTC configuration itself.

Agrawal introduced DWC versions for ternary distillations using either side rectifier or side stripper column configurations [13]. Kaibel used the DWC depicted in Figure 1a to represent Brugma's quaternary column configurations [14,15]. Later in a series of publications, Madenoor Ramapriya, Tawarmalani and Agrawal (MTA) introduced a systematic method to draw DWC versions for any given thermally coupled column configuration [7,16,17]. Here a thermal coupling refers to a two-way vapor liquid mass transfer between the two columns. It is done to remove a reboiler or a condenser and generally results in lower heat duty [18]. In Figure 1b, the condenser at the top of column I is replaced with a thermal coupling, whereby, the vapor stream from the top of this column composed of mainly A and B is sent to the adjoining column II. A liquid stream is withdrawn from the same location as the vapor feed to column II and is fed at the top of the column I as reflux. This results in a thermal coupling between the location I and II at location AB. Similarly, another thermal coupling

exists between the bottom of column I and an intermediate location in the bottom half of the column II replacing the bottom reboiler of column I. As shown in Figure 1a, use of a dividing wall exploits the thermal coupling and merges the two columns in a single shell with all distillation sections 1 through 6 located appropriately.

It is worth noting that introduction of a dividing wall in a column shell does not guarantee that the resulting configuration represents a corresponding thermally coupled column configuration. Such examples can be found in a few US patents [19,20]. However, as discussed by Medenoor Ramapriya et al. [17], those configurations do not represent configurations such as a side rectifier or side stripper and therefore, are unlikely to provide the full benefits of the side rectifier or side stripper configurations. The MTA method ensures that a DWC analog of any given thermally coupled configuration can be correctly drawn.

Historically the practitioners have used the term DWC to refer the DWCS by Wright [8], Kaibel [14] and Agrawal [13]. However, the MTA method has enabled an exhaustive enumeration of DWCS corresponding to any given thermally coupled distillation configuration. For example, for a ternary separation, eight DWC configurations which differ in energy consumption and capital cost have been illustrated [7]. The number of feasible DWC configurations increase rapidly along with the number of basic configurations as the number of components to be separated increase in a feed mixture [21]. Therefore, given the huge number of DWCS, the common use of “DWC” to describe a given configuration is no longer adequate in specifying the dividing wall configuration. There is a need to search and classify available dividing wall options.

In this work, we classify all possible dividing walls into 5 types based on their unique structural characteristics reflecting their total vapor duty, construction complexity and controllability. For any given thermally coupled column configuration, this classification is expected to simplify choices of dividing wall columns and provide a common language regarding DWCS. We also demonstrate that for a ternary separation, the choice of a dividing wall depends on the feed conditions and finally we use several 5-component distillation examples to illustrate how to extend our classification beyond ternary separations.

## 2. Classification of Dividing Walls

Dividing walls are classified into 5 types based on the following three parameters: (1) the location of the ends of the dividing wall with respect to the top and bottom ends of the column shell, (2) the number of condensers and reboilers associated with the dividing wall, and (3) the number and type of transfer streams across the dividing wall. A DWC achieves ternary separation with only one dividing wall while a DWC achieving more than three component separation may contain multiple dividing walls which may belong to different types. For simplification, ternary separation is used to illustrate the classification in detail. It is worth noting that a ternary scheme can be used to separate any given feed mixture, even those containing more than three components, into three product streams, each of different composition.

### 2.1. Type 1

A dividing wall of type 1 (DW1) is located at the middle section of the column. The dividing wall starts at an intermediate location which is some stages below the feed point and terminates at an intermediate location some stages above the feed point. On one side of the dividing wall, the feed mixture is fed at an intermediate location and on the other side of the wall, the liquid feed at the top and the vapor feed at the bottom are fed from the distillation section located above and below the dividing wall respectively. This type of dividing wall has one condenser and one reboiler associated with it and does not have any intermediate transfer streams across the dividing wall. A ternary DWC containing DW1 is the same as the Wright’s DWC [8]. The feed ABC is fed to the middle section of the left side of the column and sloppily separated into two streams AB and BC. These two streams (liquid AB and vapor BC) travel to the other side of the dividing wall through the top and the bottom

sections respectively. Three product streams are produced: A from the top condenser, B as a side draw and C from the bottom reboiler. This separation procedure is exactly equivalent to the ternary FTC configuration, and as a result, both configurations have minimum heat duty requirement among all known ternary basic and their thermally coupled derivative configurations.

DW1 is attractive from both heat duty perspective and capital cost perspective. However, optimal operation of such DWCs could be particularly challenging as the control over the vapor split at the bottom is difficult [22]. The upward vapor flow from the bottom section to the middle section is split by the dividing wall into two streams, and this split is predetermined by the cross-sectional area on each side of the dividing wall to maintain equal pressure drops. This constraint could force DW1 to operate at some inefficient operating condition and lose its heat duty benefit. This operating issue has inspired researchers to look into other types of dividing wall columns.

## 2.2. Type 2

Type 2 dividing wall (DW2) extends an end of the dividing wall from an intermediate location in the column to the top section (DW2T, Figure 1c) or bottom section of the column (DW2B, Figure 1e). It is important to note that the intermediate location in the column is appropriately chosen either some stages below (DW2T) or some stages above (DW2B) the feed point to the column. DW2T requires two condensers due to the partition in the top section, and similarly, DW2B requires 2 reboilers. Inside the column, DW2 has no intermediate transfer stream from one side to the other side of the wall and thus inside the column, the only way a mixture stream that needs to be distilled enters the other side of the wall is either from the bottom (for DW2T) or from the top (for DW2B).

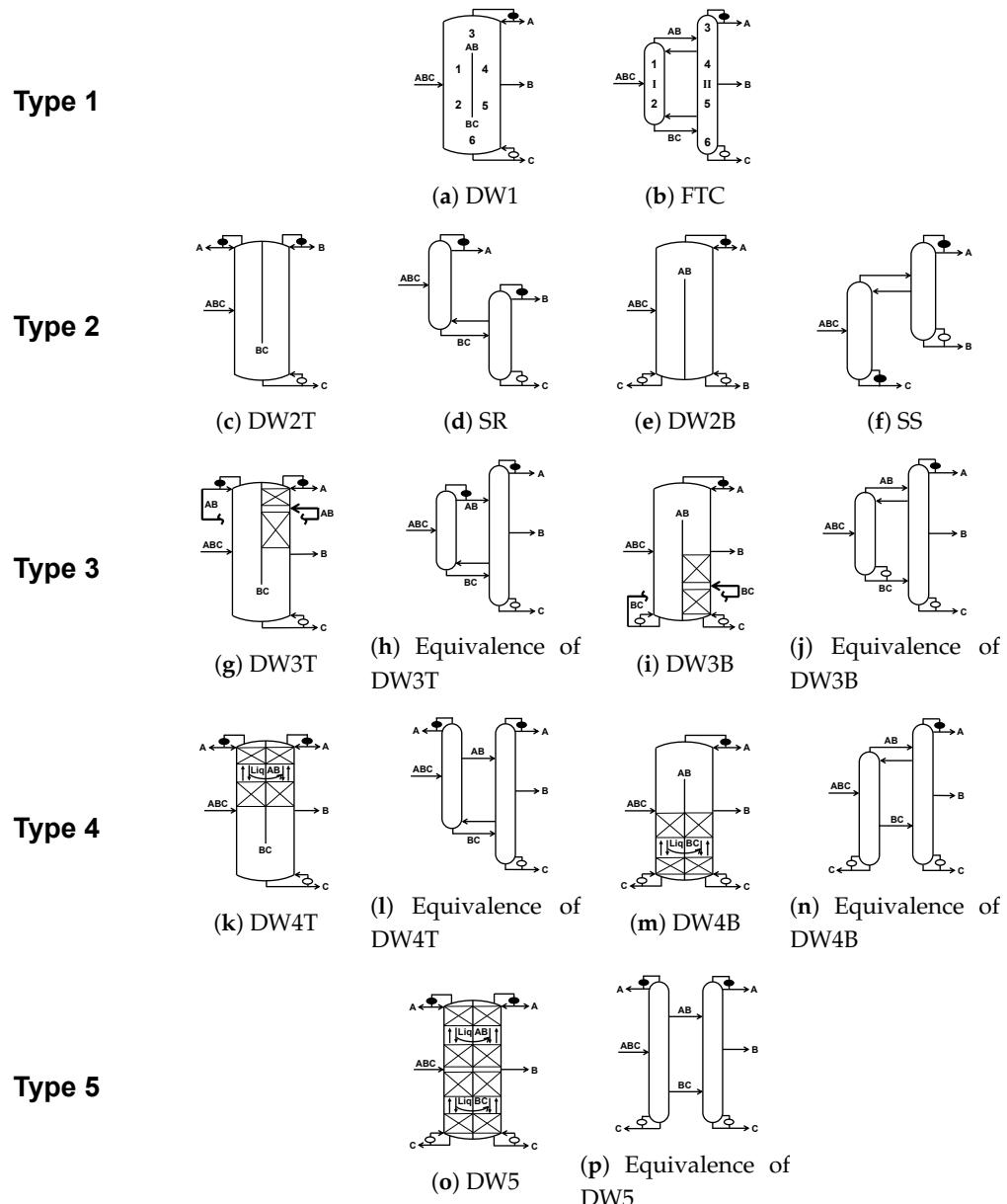
DW2T and DW2B are thermodynamically equivalent to the side-rectifier (SR, Figure 1d) and side-stripper (SS, Figure 1f) configurations respectively. On the left side of DW2T, an A/BC separation is performed, and A is collected from the top and on the right side, BC is further separated into B and C. Similarly for DW2B, AB/C is achieved on the left side of the dividing wall followed by A/B on the right side. Depending on the feed composition, these two configurations may require more total vapor duty than DW1, which could indicate less attractiveness in terms of energy consumption. Higher total vapor duty and one more condenser (DW2T) or reboiler (DW2B) also implies higher capital cost. However, the operating challenge of DW1 is substantially solved in DW2. For DW2T, the vapor split at the bottom of the wall is controlled by slightly changing the pressures of the two top condensers. For DW2B, since the dividing wall extends to the bottom, the issue naturally disappears. This type of dividing wall was first synthesized by Agrawal in 2001 [13], which provides an alternative to DW1 with better controllability.

## 2.3. Type 3

Similar to Type 2, a Type 3 dividing wall (DW3) starts at an intermediate location and extends the other end of the wall either to the top or the bottom of the column, however, it requires a liquid transfer stream from a condenser or reboiler located on one side of the wall to an intermediate location on the other side of the wall. This type of dividing wall also contains two configurations: one with the dividing wall extended to the top (DW3T, Figure 1g), the other one with the dividing wall extended to the bottom (DW3B, Figure 1i). Two condensers and one reboiler are associated with the dividing wall in DW3T and similarly one condenser and two reboilers with DW3B. The liquid stream containing mainly components A and B from the condenser AB is fed to an intermediate location of the column in DW3T. Similarly, a liquid stream containing components B and C is fed from the bottom of the column at reboiler BC to an intermediate location of the column in DW3B.

This liquid transfer stream, which distinguishes DW3 from DW2, creates a feed location at an intermediate location in the column. The extra feed location increases the construction complexity and generally improves the energy performance of the configuration. DW3T and DW3B are thermodynamically equivalent to the two-column configurations in Figure 1h,j respectively. These two configurations have structures similar to FTC configuration, with the only difference that one of the

thermal couplings is replaced by a condenser (DW3T) or reboiler (DW3B). Configurations Figure 1h,j were first proposed by Agrawal and Fidkowski in [23], and the corresponding DWCs were synthesized later by Madenoor Ramapriya et al. [7]. These configurations are shown to frequently have less energy consumption than the SS and SR configurations [23]. Since at least one end of the dividing wall is at the top or the bottom, DW3 is also easily controlled. Therefore, although DW3 is likely to require more capital to build due to the extra liquid transfer stream, however, it may still be the most attractive economic alternative for an application due to lower heat duty and improved operability.



**Figure 1.** (a): Wright's DWC (DW1), (b): Thermodynamic Equivalence of Wright's DWC (FTC), (c): DW2T, (d): SR, (e): DW2B, (f): SS, (g): DW3T, (h): Thermodynamic Equivalence of DW3T from Agrawal and Fidkowski [23], (i): DW3B, (j): Thermodynamic Equivalence of DW3B from Agrawal and Fidkowski [23], (k): DW4T, (l): Thermodynamic Equivalence of DW4T, (m): DW4B (n): Thermodynamic Equivalence of DW4B, (o): DW5, (p): Thermodynamic Equivalence of DW5.

#### 2.4. Type 4

Type 4 dividing wall (DW4) also extends from an intermediate location to either the top or the bottom of the column and requires a liquid transfer stream from one side to the other side of the wall

(Figure 4). Likewise, it has one reboiler and two condensers (Figure 1k) or two reboilers and one condenser (Figure 1m) associated with it. Different from DW3, the liquid transfer stream in DW4 is from one intermediate location of the column on one side of the wall to another intermediate location on the other side of the wall, which requires two breaks in the column sections. This could add more capital investment, but the gain is also apparent: DW4 retains the same least total vapor duty as DW1 and has no operating difficulty. These two configurations are thermodynamically equivalent to the column configurations shown in Figure 1l,n respectively. These two column configurations are section rearrangement versions of the FTC configuration along with the conversion of one of the two-way thermal coupling into Agrawal's liquid-only transfer(ALT) [16,24] and hence thermodynamically equivalent to the FTC configuration [13,25–27].

DW4 provides a controllable dividing wall column without sacrificing any total vapor duty benefit. However, it is likely to require more capital expenditure. Therefore, the choice between DW2, DW3, and DW4 will be a trade-off between capital cost and energy consumption.

### 2.5. Type 5

Type 5 dividing wall (DW5) is the only dividing wall that does not have one of its end at an intermediate location of the column and instead starts from the bottom and goes all the way to the top of the column. It has two associated condensers and two reboilers, and the communication between two sides of the dividing wall is through two liquid transfer streams, all between the intermediate locations of the column. This configuration is also thermodynamically equivalent to a section rearrangement version of the FTC (Figure 1p) hence it also requires least total vapor duty [13,25–27]. However, since it requires two liquid transfer streams, it is likely to be of interest only for some particular cases.

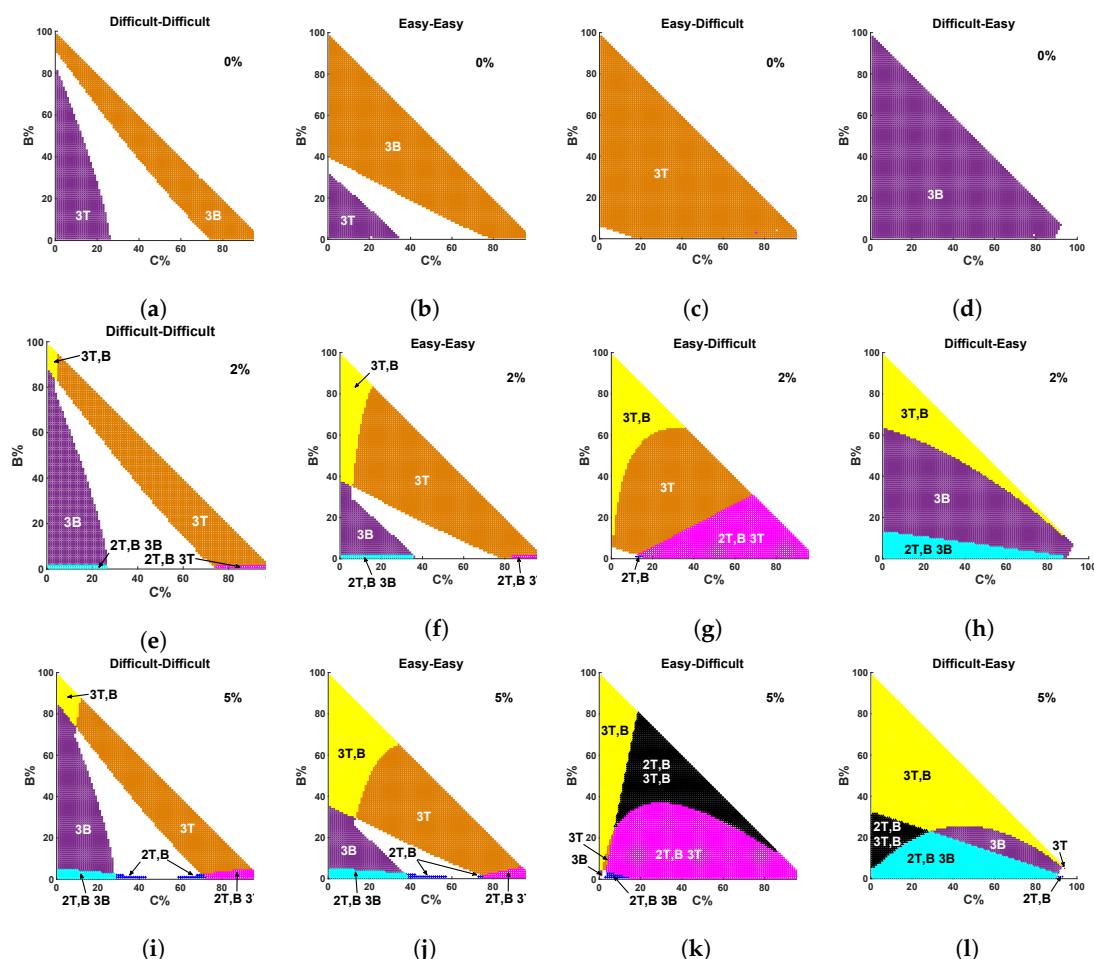
## 3. Comparison of Minimum Total Vapor Duty

In the classification section, all the dividing walls are classified into 5 types, in which DW1, DW4, and DW5 always have the same minimum total vapor duty. The optimal operating condition of DW1 could be hard to achieve under all operating conditions due to the difficulty in controlling the bottom vapor split. DW4 and DW5, however, get rid of this control difficulty while maintaining the same total vapor duty as DW1. But the trade-off is the addition of an extra liquid transfer stream from one side to the other side of the wall. The other two practically operable alternatives, DW2 and DW3, sacrifice some total vapor duty benefit, but keep the structural simplicity.

The total vapor duty of a certain separation is highly dependent on the feed composition and the relative volatility of each component in the feed. To comprehensively evaluate the performance of these 5 types of dividing wall columns, it is essential to analyze the total vapor duty for different feed composition with different relative volatility sets. For an ABC mixture feed, in which A is the most volatile component and C is the least volatile component, four representative relative volatility sets are chosen:  $\alpha_{AB} = 2.5 \alpha_{BC} = 2.5$  for easy-easy separation,  $\alpha_{AB} = 1.1 \alpha_{BC} = 1.1$  for difficult-difficult separation,  $\alpha_{AB} = 2.5 \alpha_{BC} = 1.1$  for easy-difficult separation and  $\alpha_{AB} = 1.1 \alpha_{BC} = 2.5$  for difficult-easy separation [23]. For each relative volatility set and saturated liquid feeds, minimum total vapor duties of all 5 types of dividing wall columns over the entire composition range are calculated to distill pure saturated liquid product streams A, B, and C using the Global Minimization Algorithm (GMA) developed by Nallasivam et al. [28]. For configurations with more than one reboiler, minimum total vapor duty refers to the minimum of the sum of vapor duty in each of the reboiler. From the minimum total vapor duty perspective, the five types of dividing walls can be divided into three categories. In the first category, DW1, DW4 and DW5, each representing the same FTC configuration, have identical minimum total vapor duties which is the lowest among all the minimum total vapor duties from the DWs. The other two types of dividing walls DW2 and DW3, generally have different minimum total vapor duties and constitute remaining categories. Depending on the feed conditions and product specifications, the minimum total vapor duty from either DW2 or DW3 may or may not be the lowest total vapor duty. For a given application, it is critical to know the relative differences between

the minimum total vapor duties of DW2, DW3 and the lowest heat duty. If the total vapor duty requirements of DW2 and DW3 are similar to DW1, DW4, or DW5, then it is better to choose DW2 or DW3 due to the structural simplicity and operational feasibility. Otherwise, DW4 or DW5 could be a better choice due to heat duty and operation considerations.

Figure 2 identifies the composition range in which DWC in DW2 or DW3 also have the lowest total vapor duty (Figure 2a–d, less than 2% (Figure 2e–h), and less than 5% (Figure 2i–l) above the lowest heat duty of DW1, DW4, or DW5. In all the figures, the x-axis is the mole fraction of C component in the feed and the y-axis is the mole fraction of B. The mole fraction of A is then calculated by difference. In Figure 2a–d, DW3B has the lowest heat duty in the purple regions, which is the same as that of DW1, DW4, and DW5. For the feed with composition and relative volatility set lying in these region, DW3B is likely the most attractive dividing wall option due to its structural and operational simplicity with no heat duty penalty. Likewise, DW3T is likely to be the most attractive in the orange regions. It is clear that in Figure 2a–d, DW3 is the most attractive configuration in a significant composition range. For a difficult-difficult separation (Figure 2a), the regions for DW3 is 60% of the total area in which purple region is 35% and the orange region is 25%. For an easy-easy separation (Figure 2b), this number becomes 81% and when it comes to easy-difficult separation (Figure 2c) or difficult-easy separation (Figure 2d), DW3 almost always has the lowest total vapor duty for almost every feed composition (99%).



**Figure 2.** (a–d): Composition region in which the minimum total vapor duty of DW2 or DW3 is also the lowest total vapor duty, (e–h): Composition region in which the minimum total vapor duty of DW2 or DW3 is within 2% above the lowest total vapor duty, (i–l): Composition region in which the minimum total vapor duty of DW2 or DW3 is within 5% above the lowest total vapor duty. Region with no identification (also no color) refer to lowest heat duty DW1, DW4, or DW5.

However, DW2 never shows up anywhere in Figure 2a–d, which indicates DW2 never achieves the lowest total vapor duty, but for structure and operation consideration, DW2 could be an excellent choice, which necessitates further investigation into the situation when some total vapor duty penalty may be acceptable. Figure 2e–l show the region where the minimum total vapor duties of DW2 and DW3 are within 2% and 5% of the lowest total vapor duties respectively. When 2% total vapor duty penalty is acceptable, DW2 begins to show up in certain composition ranges. The region for DW2 is minor for difficult-difficult and easy-easy separation (Figure 2e,f), which only account for 1% of the total area. However, for easy-difficult or difficult-easy separation (Figure 2g,h), this region is comparatively larger, which is 28% and 12% respectively. If the acceptable total vapor duty penalty continues increasing to 5%, the region for DW2 increases to 4%, 4%, 80% and 31% for difficult-difficult, easy-easy, easy-difficult and difficult-easy separation respectively (Figure 2i–l). Then at least for easy-difficult and difficult-easy separation, DW2 still stands an excellent chance to be the overall most attractive configuration. Moreover, this total vapor duty comparison, along with the structural analysis in the classification section, provides a guideline to choose the proper DWCs. For a given feed composition and relative volatility information, the relative total vapor duty benefit for all 5 types DWC can be easily evaluated from Figure 2. The optimal DWC configuration is then chosen through a comprehensive consideration of the total vapor duty, structural complexity and operational difficulty.

It is worth noting that we have evaluated all five types of dividing walls in the context of total vapor duty. This analysis is useful when one is concerned about the heat duty for distillation. However, when work rather than heat is used as in a cryogenic distillation or a heat pumped distillation, results could be quite different [29]. In such cases, for optimal dividing wall choice, it is essential to perform appropriate optimization using exergy as described by Agrawal and coresearchers [29,30].

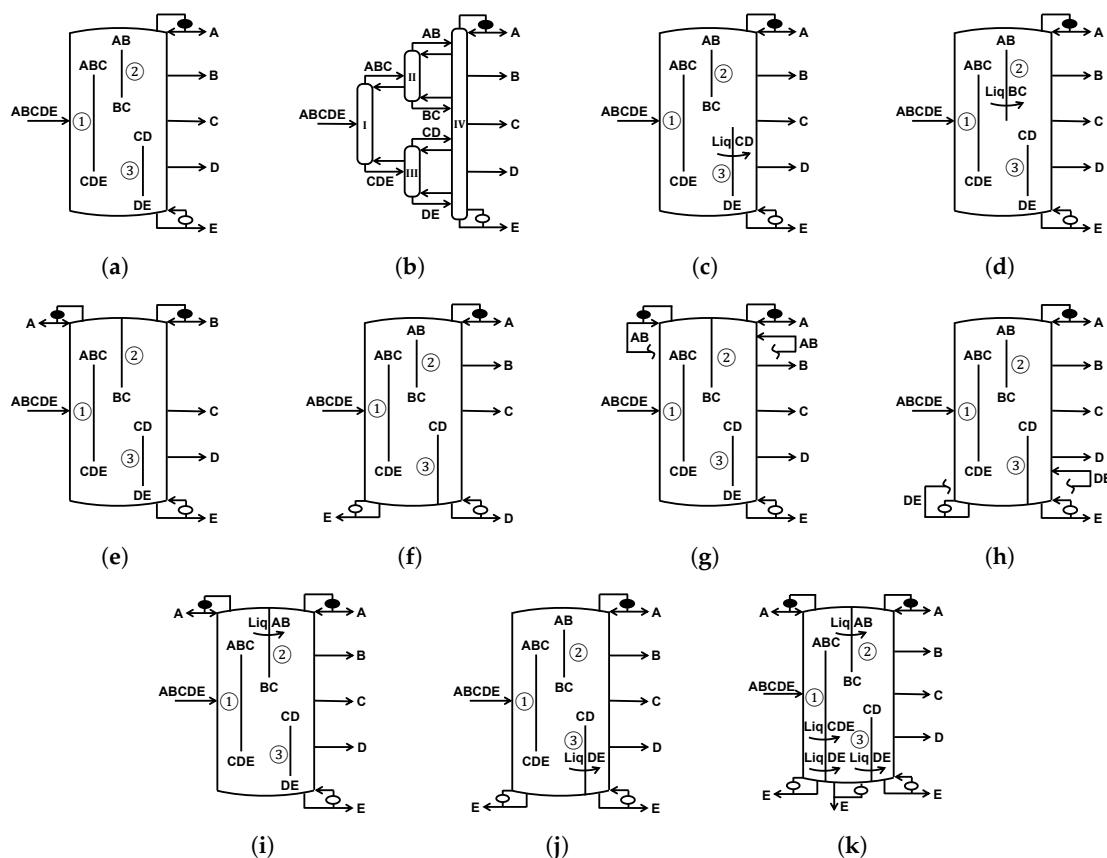
#### 4. Extending Dividing Walls to beyond Ternary Separations

For feed mixtures containing four or more components that need to be distilled into four or more product streams, one needs more than two distillation columns providing large number of distillation column configuration options with thermal couplings [21]. However, all the thermal coupling column configurations, especially those that do not represent satellite column configurations [22], can still be represented with the five types of dividing walls that have already been described. We will illustrate this with a few examples.

Figure 3a is a configuration that distills a feed mixture into 5 product streams: A, B, C, D and E [17]. The feed mixture is denoted as ABCDE in which the relative volatility decreases monotonically from A to E. This DWC contains three dividing walls inside one column shell, which are denoted as ①, ② and ③. On the left side of dividing wall ①, the feed stream ABCDE is separated into streams ABC and CDE which go to the right side of this dividing wall through the top and the bottom section respectively. Similar procedures take place on the left side of dividing walls ② and ③ wherein ABC is separated into AB and BC and CDE is separated into CD and DE respectively. On the right side of dividing walls ② and ③, streams AB, BC, CD and DE are separated into A, B, C, D and E. The thermodynamically equivalent column configuration of this DWC is shown in Figure 3b. In this column configuration, Column I separates the feed mixture ABCDE into ABC and CDE, which is corresponding to the left side of dividing wall ① in Figure 3a. Columns II and III separate ABC into AB and BC, CDE into CD and DE which are corresponding to the left side of dividing walls ② and ③ respectively. Column IV, from which all five products are collected, is corresponding to the right side of dividing walls ② and ③. Conversely, one can easily draw the DWC in Figure 3a from the given column configuration in Figure 3b.

All three dividing walls in this DWC belongs to DW1 as they start at an intermediate location and end at another intermediate location. In a ternary DWC, such a dividing wall never associates with any liquid transfer stream, because once a liquid transfer stream is introduced, one end of the dividing wall must be extended to the top or to the bottom, which results in other types of dividing walls. In a more than three component separation, there are cases when a liquid transfer stream is

introduced, but the end of the dividing wall does not extend all the way to the top or the bottom [17]. It extends towards the top or the bottom but still terminates at some intermediate location, as shown in Figure 3c,d. The configuration in Figure 3c can be obtained by extending the dividing wall ③ in Figure 3a towards but not all the way to the top, and a liquid stream is introduced to transfer liquid CD from one side of the dividing wall to the other. Similarly, the configuration in Figure 3d can be obtained by extending the dividing wall ② in Figure 3a. Dividing wall ③ in Figure 3c and dividing wall ② in Figure 3d represent cases of Type 1 dividing walls with liquid transfers from one side to the other side of the wall. These DWCs are described in previous work by Madenoor Ramapriya et al. [7]. These two dividing walls are still classified as DW1. There is no additional condenser or reboiler used in all these configurations which leads to poor controllability of these DWCs since the vapor splits at the bottom of the dividing walls are not regulated.



**Figure 3.** 5-component DWC examples: (a): a DWC containing DW1, (b): Thermodynamic equivalence of (a), (c,d): two DWCs containing DW1, (e,f): two DWCs containing DW2, (g,h): two DWCs containing DW3, (i,j): two DWCs containing DW4, (k): an easy-to-operate DWC.

Some controllable DWCs for a five component distillation are shown in Figure 3e–j, which contain one or more dividing walls that belong to either DW2, DW3, or DW4 [17]. Note that while DWC configuration in Figure 3i–k are thermodynamically equivalent to the one in Figure 3a, the four other configurations in Figure 3e–h are not. In Figure 3e,f, two DWCs containing DW2 (dividing wall ② in Figure 3e and dividing wall ③ in Figure 3f) have better controllability than the Figures only containing DW1 (Figure 3a,c,d) due to the additional condenser (in Figure 3e) or reboiler (in Figure 3f). DWCs in Figure 3e or Figure 3f can be obtained by replacing dividing wall ② or ③ in Figure 3a by DW2T or DW2B respectively. On the left side of dividing wall ② in Figure 3e, ABC is separated into A and BC and A is collected from the condenser on the left top of the DWC. BC travels from the bottom of this dividing wall to the right and is further separated into B and C. Likewise, In Figure 3f, dividing wall ③ is converted to type 2, CDE is separated into CD and E whereby E is collected from the reboiler

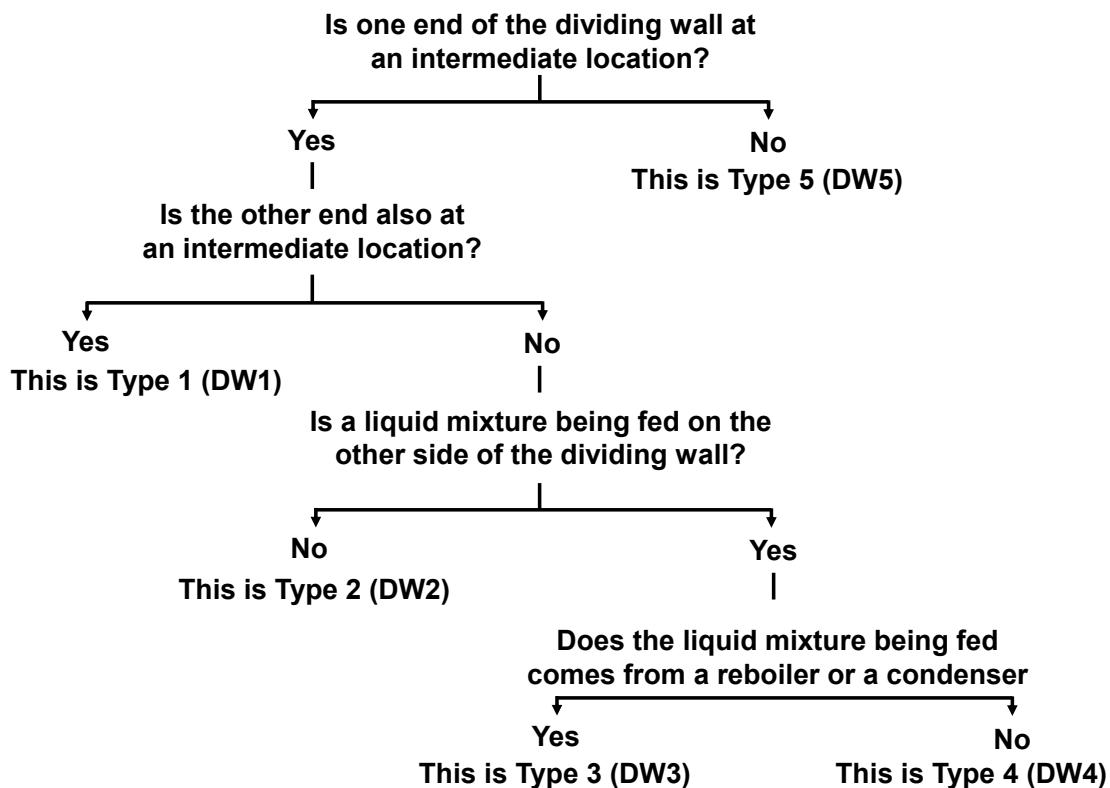
on the left bottom of the DWC. CD travels to the right side at the top of this dividing wall and is further separated into C and D. Furthermore, DWCs in Figure 3g–j can be obtained by converting dividing wall ② or ③ to DW3 or DW4. Similar to the ternary case, the operational advantages of these DWCs are retained since the vapor splits are easily controlled by the additional condenser or reboiler associated with the dividing walls. For configurations in Figure 3e–h, their minimum total heat duty can also be calculated by transferring them back into their column configuration equivalence using MTA [7] method and then calculating the minimum heat duty of those configurations via GMA [28].

One easy-to-operate DWC for this separation is shown in Figure 3k. Madenoor Ramapriya et al. have shown that for any thermally coupled column configuration, there is always an easy-to-operate DWC version [17]. A further conclusion one can draw through the analysis in this paper is that, an easy-to-operate DWC does not contain DW1 and a DWC that contains DW1 is difficult to operate. In the DWC shown in Figure 3k, all three dividing walls belong to DW4. Dividing wall ① belongs to DW4B and two liquid transfer stream, liquid CDE and liquid DE are introduced. dividing wall ② and dividing wall ③ belong to DW4T and DW4B respectively and one liquid transfer stream is associated with each one of these two dividing walls. This DWC has two condensers and three reboilers which could be independently adjusted to tune the vapor split at the bottom of dividing wall ②.

## 5. Conclusions

Dividing walls are classified into 5 types based on three parameters as shown in Figure 4: (1) the location of the two ends of the dividing wall (2) the number of condensers and reboilers associated with the dividing wall, and (3) the number and type of transfer streams across the dividing wall. The parameter that differentiates Type 1 dividing wall, DW1, from the rest of the Type 2 through 5 dividing walls is the fact that within a column shell, this dividing wall starts at an intermediate location and ends at another intermediate location. The bottom end of the dividing wall is at least a few separation stages below the feed location and the top end is at least a few separation stages above the feed location. While for a three-component feed separation, no liquid stream is transferred from an intermediate location on one side of the wall to an intermediate location on the other side of the wall, this may or may not hold for distillation of feeds containing higher number of components into more than three product streams. All the types 2, 3 and 4 (DW2, DW3 and DW4) are different from the type 5 (DW5) in that these dividing walls start at an intermediate location of the column shell and terminate either at the top or the bottom of the column shell, whereas DW5 traverses from the bottom to the top of the column shell. When the dividing wall starts at an intermediate location that is some separation stages above the feed location, then it extends to the bottom of the column shell providing us with DW2B, DW3B or DW4B. Similarly, when the intermediate location is some separation stages below the feed location, then the other end of the dividing wall extends to the top of the column shell leading to DW2T, DW3T or DW4T. While in type 2 dividing wall, DW2, no liquid mixture is fed at an intermediate location on the other side of the wall, the other two type 3 and 4 (DW3 and DW4) do have such a feed. DW3 has a mixture stream transferred from either a condenser (for DW3T) or a reboiler (for DW3B) to an intermediate location on the dividing wall within the column while in DW4, one such stream is transferred from an intermediate location on one side to an intermediate location on the other side of the dividing wall.

For a ternary mixture, the minimum total vapor duty analysis shows that while DW1, DW4, and DW5 always have the lowest total vapor duty, DW3 also often leads to the same lowest total vapor duty. DW2 also has a good chance to be attractive if a small total vapor duty penalty is allowed. The optimal DWC configuration is chosen through a comprehensive analysis of total vapor duty, energy demand, structural complexity and operation difficulty. We demonstrate that the classification method is easily extendable to more than three component separations.



**Figure 4.** Classification of dividing walls into five types. Type 1 is due to Wright [8], Type 2 is from Agrawal [13] and Type 3,4 and 5 are due to MTA [7,17].

**Author Contributions:** Conceptualization, Z.C. and R.A.; methodology, Z.C. and R.A.; software, Z.C.; validation, Z.C.; formal analysis, Z.C. and R.A.; investigation, Z.C. and R.A.; resources, Z.C. and R.A.; data curation, Z.C.; writing—original draft preparation, Z.C.; writing—review and editing, Z.C. and R.A.; visualization, Z.C.; supervision, R.A.; project administration, R.A.; funding acquisition, R.A. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by the National Science Foundation under Cooperative Agreement No. EEC-1647722. Any opinions, findings and conclusions or recommendations expressed in this material are those of the author(s) and do not necessarily reflect the views of the National Science Foundation.

**Acknowledgments:** We would like to acknowledge CISTAR (Center for Innovative and Strategic Transformation of Alkane Resources) for funding.

**Conflicts of Interest:** The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

## Abbreviations

The following abbreviations are used in this manuscript:

DWC	dividing wall column
GMA	global minimization algorithm
SR	side rectifier
SS	side stripper
FTC	fully thermally coupled
ALT	Agrawal's liquid-only transfer
MTA	Madenoor Ramapriya, Tawarmalani and Agrawal

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