# Transverse momentum dependent forward neutron single spin asymmetries in transversely polarized $p+p$ collisions at $\sqrt{s}=200 \mathrm{GeV}$ 

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In 2015, the PHENIX collaboration has measured very forward ( $\eta>6.8$ ) single spin asymmetries of inclusive neutrons in transversely polarized proton-proton and proton-nucleus collisions at a center of mass energy of 200 GeV . A previous publication from this data set concentrated on the nuclear dependence of such asymmetries. In this measurement the explicit transverse momentum dependence of inclusive neutron single spin asymmetries for proton-proton collisions is extracted using a bootstrapping unfolding technique on the transverse momenta. This explicit transverse momentum dependence will help improve the understanding of the mechanisms that create these asymmetries.

## I. INTRODUCTION

At the beginning of the era of polarized proton collisions at the relativistic heavy ion collider (RHIC), a dedicated experiment based on a prototype zero-degree calorimeter (ZDC) [1] was set up to initially study very forward neutral pion asymmetries in transversely polarized proton collisions in relation to earlier results that showed nonzero results [2]. Instead of finding a neutral pion asymmetry, that was only recently discovered at low transverse momentum by the RHICf experiment [3], a sizable neutron asymmetry was found in the forward direction of the transversely polarized proton beam [4].

Earlier theoretical studies related very forward neutron production to the one-pion-exchange (OPE) model [5-7] in which the exchange of one pion between the proton and another colliding particle can create the outgoing neutron. Such a model was reasonably successful in describing unpolarized, very forward neutron production as previously observed at the ISR [8]. However, a simple pion exchange model would not be able to describe any spin dependence of the observed neutron distributions. To accommodate that, an interference with another particle exchange would be necessary to have helicity-flip and nonflip amplitudes available that can create a single spin left-right asymmetry. Within the general framework of Regge theory [9], such an interference could be accomplished when adding also a scalar meson exchange and the resulting pseudoscalar-scalar meson interference would then create the asymmetry. Recent calculations of such an OPE based description of very forward neutron single spin asymmetries [10] are able to qualitatively describe the RHIC measurements which, by now, include transversely polarized proton-proton collisions at $\sqrt{s}=$ $62 \mathrm{GeV}, 200 \mathrm{GeV}$, as well as 500 GeV [11], although the transverse momentum information enters only indirectly via the different collision energies.

The very different asymmetries observed in protonnucleus collisions [12], with different sign and much larger magnitude, indicate that at high impact parameters and at least for high-Z nuclei ultraperipheral collisions (UPC) [13] also contribute to these asymmetries in a very different way. This data together with the recent very forward nonzero neutral pion result [3] may provide

[^1]crucial information to the underlying mechanisms that create these asymmetries.

So far, none of these results have been extracted with an explicit transverse momentum dependence while the different collision energies provide some indirect information on it. Obtaining it can directly test the proposed mechanism and the dependence that results from its theory calculation [10]. Therefore, extracting the actual transverse momentum dependence is the focus of this publication. A substantial understanding is required of the transverse momentum smearing in the PHENIX ZDCs. Also needed are determinations of systematic uncertainties in unfolding transverse momenta, which were studied via a Monte Carlo (MC) bootstrap method as described later.

In the following sections, the detector description, analyzed data sets and the forward neutron selection are covered. Next are described the procedure for unfolding the neutron single spin asymmetries as a function of the reconstructed transverse momenta to obtain the true transverse momentum dependence. Then, the final results are presented before summarizing.

## II. DATA SETS

In 2015, the PHENIX experiment recorded polarized proton-proton and proton-nucleus collision data at a center of mass energy of 200 GeV . In the proton-proton collision data, the beams were transversely polarized with the spin direction pointing vertically up or down with respect to the plane defined by the accelerator ring.

Inclusive neutrons were detected with the ZDC, which comprise 3 modules of $\mathrm{Cu}-\mathrm{W}$ alloy absorbers layered with optical fibers of 1.7 nuclear interaction lengths each (51 radiation lengths per module), covering a projected area of 10 cm by 10 cm transverse to the beam direction. The absorber layers of the ZDC are tilted 45 degrees upward to maximize the light yield from Čerenkov light. The location of the ZDCs is 18 m up and downstream of the PHENIX beam interaction point, thus covering a range of pseudorapidity $\eta>6.8$. The ZDC is used to measure the energy of forward neutrons, and its energy resolution is about $20 \%$ for neutron energies of 100 GeV . Between the first and the second module, approximately at the position of the maximal hadronic shower are located scintillator strip detectors with a projected width of 15 mm horizontally and vertically. This shower max detector (SMD) is used to determine the position of the neutrons
that are selected by calculating the weighted average of the deposited energy for all strip positions. The position resolution of the SMD for neutrons is $\approx 1 \mathrm{~cm}$. Additionally, the SMD is used for local polarimetry of the polarized beams by making use of the nonzero neutron asymmetries in proton-proton collisions and allowed to track the transverse spin orientation or confirm the spin orientation to be rotated in the longitudinal direction. See Ref. [14] for a more detailed detector description.

Collision events were selected for this result by a logical OR of north and south ZDCs that require approximately an energy deposit of more than 15 GeV on either detector. Within the proton collisions were accumulated about 35 M neutron events that were triggered by the ZDCs.

## III. EVENT AND PARTICLE SELECTION CRITERIA

Neutron candidates in the north ZDC were selected by requiring more than $3 \%$ of the total deposited energy to be in the second ZDC module. This effectively rejects photon candidates, that deposited their energy in the first module due to being electromagnetic showers. Also nonzero hits in both horizontal and vertical SMDs are required to reliably estimate the neutron position and transverse momentum. Furthermore, the reconstructed neutron energies were selected between 40 and 120 GeV . The hit position as defined by the SMDs has to be within 0.5 to 4 cm in radius from the nominal beam position. Additionally, data under stable running conditions with no problems in the polarized beam diagnostics were selected. The transverse momentum $P_{T}$ is reconstructed from the neutron energy $E$, the radius of the average hit position $r$ and the distance from the interaction point $z_{Z D C}$ :

$$
\begin{equation*}
P_{T}=\frac{r}{z_{Z D C}} E \tag{1}
\end{equation*}
$$

The events that fulfill the above conditions are then binned in 4 transverse momentum bins of $[0.01,0.06$, $0.11,0.16,0.21] \mathrm{GeV} / c$ and 6 equidistant azimuthal angular bins that cover full azimuth around the polarized beam direction. The two spin states are kept separated for the unfolding, but to obtain the asymmetries needed in the bootstrap method of the MC, they are also directly calculated here as:

$$
\begin{equation*}
A_{N}(\phi)=\frac{1}{\langle P\rangle} \frac{N^{+}(\phi)-\mathcal{R} N^{-}(\phi)}{N^{+}(\phi)+\mathcal{R} N^{-}(\phi)} \tag{2}
\end{equation*}
$$

where $\langle P\rangle$ is the average beam polarization (for this running period $52 \%[15])$ and $N^{ \pm}$are the yields of neutrons in the up/down spin state as a function of azimuthal angle $\phi$ that is defined relative to the spin-up direction. $\mathcal{R}$ is the ratio of accumulated luminosities for the down and up spin states, and is close to unity in this analysis. The actual $A_{N}$ is then calculated by fitting a sine modulation to it with magnitude and phase as free parameters.

As systematic uncertainties, the amount of charged particle background (dominated by protons) and the uncertainty of the beam center position need to be evaluated. Unlike other years, no charge veto counter in front of the ZDC was installed in this running period. This resulted in a rather asymmetric charged hadron background predominantly from protons that are swept into the ZDC by the dipole magnet which joins and separates the two beams. The fraction of charged hadron background was statistically subtracted on the spin dependent yield level by applying the background fractions that were obtained in the 2008 running period when the charge veto counter was installed. The statistical uncertainties on these background fractions were then assigned as systematic uncertainties on the resulting raw asymmetries.

The central beam position relative to the ZDC also cannot be perfectly determined due to the large lever arm as well as varying beam conditions. As such, the assigned beam position was artificially varied by 1 cm horizontally and 0.5 cm vertically around the nominal beam position, respectively. All neutron positions, transverse momenta, and azimuthal angles were recalculated before evaluating the asymmetries. These variations were motivated by the uncertainties based on two independent methods of reconstructing the beam center positions using the ZDCs. The combined uncertainties on the asymmetries from charged background and beam position are then used as a basis for variation of the bootstrap MC method of unfolding the asymmetries as discussed in the next section. The uncertainties due to charged background and beam position remain negligible compared to the large systematic uncertainties this unfolding introduces.

## IV. TRANSVERSE MOMENTUM UNFOLDING

As hadronic showers develop a substantial size and the segmentation of the SMDs is limited, the reconstructed neutron energy and in particular the transverse momentum are smeared. The transverse momentum dependence of the single spin asymmetries is however of much interest for the understanding of the mechanism that creates these asymmetries.

We have performed detailed MC simulations using 5 different types of event generators as input to full GEANT3 [16] simulations of the forward region of PHENIX [17, 18] including the ZDCs, SMDs, the beampipe as well as the dipole magnet that merges and separates the incoming and outgoing beams and is responsible for an asymmetric spray from charged particles. These GEANT simulations have been shown to describe these effects, as well as differences between top and bottom that originate from the light collection and back scattering in the top part of the ZDC. The composition, energy and momentum distributions of particles in the far forward region are not very well understood in general, and there-
fore different types of generators were used to gauge the impact of these differences on the unfolded asymmetries. The three full generators PYTHIA6.1 [19], PYTHIA8.2 [20] and DPMJET3.1 [21] were applied, where in particular diffractive processes are handled very differently.

Additionally, an empirical distribution of forward neutrons in longitudinal and transverse momentum was used to mimic an OPE model. In this case, a pion that balances the energy and momentum between the incoming proton and the thrown neutron (i.e. $p \rightarrow \pi^{+}+n$ ) was collided with the other beam using pythia8 again (i.e. $\pi+p)$. Moreover, as the forward pA results have indicated [12], ultraperipheral collisions can also play a role in forward neutron production although that will be more prominent in proton-nucleus collisions. Therefore, the yield and distribution of photons from the other beam was simulated using starlight [22] and collided with the proton beam using PYTHIA8 again.

As none of these generators is intrinsically spin dependent, spin effects ( $w$ in the following expression) were simulated by reweighting generated events as a function of true transverse momentum and azimuthal angle where the spin state was randomly assigned. Three different functional forms were used in the reweighting to provide as much flexibility as possible for the true transverse momentum dependence of the single spin asymmetries. The most general parameterization is a 3rd order polynomial in the transverse momentum with a vanishing constant term due to the requirement for the asymmetry to vanish at zero transverse momentum:

$$
\begin{equation*}
w=\left(a \cdot P_{T, g}+b \cdot P_{T, g}^{2}+c \cdot P_{T, g}^{3}\right) \sin \left(\phi_{g}+\lambda \cdot \pi\right) \tag{3}
\end{equation*}
$$

where $P_{T, g}$ and $\phi_{g}$ are the true transverse momenta and azimuthal angles, respectively and $\lambda( \pm 1)$ is the spin state while $a, b$ and $c$ are free parameters that are varied. A second functional form (with $a$ and $b>0$ free parameters) is based on a power-law behavior:

$$
\begin{equation*}
w=\left(a \cdot P_{T, g}^{b}\right) \sin \left(\phi_{g}+\lambda \cdot \pi\right) \tag{4}
\end{equation*}
$$

and the last parameterization (with $a$ and $b$ free parameters) follows an exponential form that eventually reaches an asymptotic constant:

$$
\begin{equation*}
w=a\left(1-\mathrm{e}^{b \cdot P_{T, g}}\right) \sin \left(\phi_{g}+\lambda \cdot \pi\right) \tag{5}
\end{equation*}
$$

In the power law parameterization, only positive powers are allowed to avoid unphysical nonzero asymmetries at zero transverse momentum.
For each set of parameters, functional form, and MC generator, the single spin asymmetries were extracted from the reconstructed kinematic variables that included these weights based on the true variables.

In a first step, the reconstructed asymmetries that were obtained from the data are compared to the reconstructed asymmetries from MC for a large number of variations of the parameters. The quality of a set of parameters, functional form and MC generator in reproducing the data asymmetries was evaluated by calculating
the $\chi^{2}$ between the actual data points and the smeared asymmetry points. While the MC statistics are generally large enough, many functional forms can describe the data within the experimentally measured uncertainties.

Figure 1 displays the functional forms probed for the OPE motivated MC generator. The regions where a parametrization results in a $\chi^{2}$ below 10 units is also visualized to highlight the range of reasonable parameterizations. Despite the different transverse momentum distributions of forward neutrons in the different MC generators, their best asymmetry distributions are very similar for each set of functional forms. In all functional forms, a rapidly rising asymmetry is preferred at small $P_{T}$, while at intermediate transverse momentum (within the second and third data points) no large variation in the asymmetries is visible. The exponential function generally prefers the asymptotic value to be reached already at these transverse momenta. At higher transverse momenta above $0.2 \mathrm{GeV} / c$, the sensitivity is very limited for all functional forms despite a nonzero smearing into the observed range. As such, the slightly rising, constant or even diminishing asymmetries at high transverse momenta can describe the measured data reasonably well.

In a second step, the spin-dependent data yields that are two-dimensional in reconstructed transverse momentum and azimuthal angle are unfolded using the spindependent, weighted smearing matrices obtained for each set of parameters, functional form and MC generator set. For the unfolding itself, the TSVDUnfold package of ROOT [23] based on a regularized singular value decomposition [24] was used. After the unfolding, the asymmetries are calculated from the unfolded yields as described above. The best parameterization for each functional form and MC generator is used to obtain the central point of the unfolded asymmetries and statistical uncertainties. The impact of the variation of parameters is evaluated by obtaining the root mean square (RMS) of the spread of unfolded asymmetries which are weighted by the inverse of their respective $\chi^{2}$ to take the quality of a parameter set into account. These uncertainties are also displayed in Fig. 1, together with the unfolded asymmetries using the OPE generator.

The variation of the unfolded asymmetries is displayed in Fig. 2 for each transverse momentum bin and parameterization, while spreads from the different MC generators had been combined equally. The central values from these distributions have been taken as the final asymmetry values while the rms value is taken as the uncertainty due to the various parameterizations.

In addition to these uncertainties, further systematic uncertainties are studied by varying the regularization parameter in the TSVDUnfold method as well as the uncertainties due to the statistical uncertainties on the smearing matrices themselves. However, most of these values are within the boundaries of the uncertainties obtained from the variation of parameters and functional forms. Only those systematic contributions that exceed the aforementioned uncertainties have been added


FIG. 1. True asymmetry parameterizations as a function of transverse momentum for (a) a 3rd order polynomial dependence "Pol3," (b) a power-law dependence "Power Law," and (c) an exponential dependence "Exponential". The shaded regions represent the regions where the $\chi^{2}$ between the smeared asymmetries related to this parameterization and the asymmetries reconstructed from data (solid [blue] squares) is below 10 units. The dashed lines represent the best matching parameterizations. Also displayed are the unfolded asymmetries (a) solid [dark green] squares, (b) solid [orange] circles, and (c) solid [red] hyphens, as obtained from the best parameterizations of the OPE generator. The rms ranges of unfolded asymmetries are visualized as shaded boxes for the various MC generators.


FIG. 2. Relative likelihood distributions of unfolded asymmetries for each transverse momentum bin for all sets of parameters of each functional form weighted by the inverse of its $\chi^{2}$. All different MC generators distributions have been combined in these panels. The distributions of the 3rd order polynomial parameterization (shaded [light green] area "Pol3"), power law behavior (vertically hatched [light orange] area "Power Law") and exponential (horizontally hatched [light red] area "Exponential") have been stacked in these figures. The overall central and rms values are also displayed.


FIG. 3. Neutron transverse single spin asymmetries as a function of the true transverse momentum. The data points represent the unfolded asymmetries obtained via the average over all parameterizations and MC generators. The uncertainty boxes represent the systematic uncertainties due to the parameterization, functional form, MC generator and unfolding procedure.

TABLE I. Neutron single spin asymmetries as a function of transverse momentum after unfolding transverse-momentum and azimuthal-angular smearing. $\Delta A_{N}$ corresponds to the statistical uncertainties while the last two columns specify the upper and lower systematic uncertainties $\delta A_{N}$.

| $\left\langle P_{T}\right\rangle(\mathrm{GeV} / c)$ | $A_{N}$ | $\Delta A_{N}$ | $\delta A_{N}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.043 | -0.039 | $\pm 0.003$ | +0.014 | -0.014 |
| 0.085 | -0.050 | $\pm 0.002$ | +0.013 | -0.013 |
| 0.132 | -0.055 | $\pm 0.002$ | +0.022 | -0.014 |
| 0.180 | -0.053 | $\pm 0.001$ | +0.017 | -0.017 |

in quadrature.

## V. RESULTS

The inclusive neutron asymmetries obtained from the average of all parameterizations and MC generators are displayed in Fig. 3 as a function of the true transverse momentum. The final results are tabulated in Table I.

The absolute values of the asymmetries are consistent with an increase with transverse momentum but show an indication of leveling off at higher transverse momenta. A simple linear dependence as suggested by [10], as well as the central values of transverse momentum integrated asymmetries at different collision energies [4, 18], seems not necessarily to be preferred by the data. However, a simple linear dependence cannot be excluded within uncertainties either. From the MC reweighting exercise no substantial differences between the different MC generators have been seen.

Taking into account the indication of very different asymmetries in ultraperipheral collisions in protonnucleus collisions [12, 13] and in particular a different sign, it appears that the UPC contribution to the protonproton collisions is limited in this $p_{T}$ region. This is expected given the electromagnetic nature of the interaction being proportional with $Z^{2}$. However, in these inclusive results some contribution from UPC events may remain, which could alter the transverse momentum behavior in comparison to the purely hadronic theoretical calculations.

## VI. SUMMARY

In summary, the PHENIX experiment has measured for the first time the transverse momentum dependence of very forward neutron single spin asymmetries in protonproton collisions at a center of mass energy of 200 GeV . With these measurements the first reliable tests of the
suggested mechanisms producing such forward neutron asymmetries can be performed. While the uncertainties from the unfolding are very sizable, a simple linear transverse momentum dependence as suggested in [10] is not inconsistent; however, the asymmetries appear to level off at higher transverse momenta. Instead, a much slower rise of the asymmetries or even a turnaround at larger transverse momenta is favored when considering the best parameterizations. To understand the mechanisms in even more detail, the correlations with other detector activity will be useful.

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