



The Black Hole Mass of the $z = 2.805$ Multiply Imaged Quasar SDSS J2222+2745 from Velocity-resolved Time Lags of the C IV Emission Line

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Abstract

We present the first results of a 4.5 yr monitoring campaign of the three bright images of multiply imaged $z = 2.805$ quasar SDSS J2222+2745 using the Gemini North Multi-Object Spectrograph and the Nordic Optical Telescope. We take advantage of gravitational time delays to construct light curves surpassing 6 yr in duration in the observed frame and achieve an average spectroscopic cadence of 10 days during the 8 months of visibility per season. Using multiple secondary calibrators and advanced reduction techniques, we achieve percent-level spectrophotometric precision and carry out an unprecedented reverberation mapping analysis, measuring both integrated and velocity-resolved time lags for the C IV emission line. The full line lags the continuum by $\tau_{\text{cen}} = 36.5_{-3.9}^{+2.9}$ rest-frame days. We combine our measurement with published C IV emission line lags and derive the $r_{\text{BLR}} - L$ relationship $\log_{10}(\tau/\text{day}) = (0.99 \pm 0.07) + (0.48 \pm 0.03)\log_{10}[\lambda L_{\lambda}(1350 \text{ \AA})/10^{44} \text{ erg s}^{-1}]$ with 0.30 ± 0.06 dex intrinsic scatter. The velocity-resolved lags are consistent with circular Keplerian orbits, with $\tau_{\text{cen}} = 86.2_{-5.0}^{+4.5}$, 25_{-15}^{+11} , and $7.5_{-3.5}^{+4.2}$ rest-frame days for the core, blue wing, and red wing, respectively. Using σ_{line} with the mean spectrum and assuming $\log_{10}(f_{\text{mean},\sigma}) = 0.52 \pm 0.26$, we derive $\log_{10}(M_{\text{BH}}/M_{\odot}) = 8.63 \pm 0.27$. Given the quality of the data, this system represents a unique benchmark for calibration of M_{BH} estimators at high redshift. Future work will present dynamical modeling of the data to constrain the virial factor f and M_{BH} .

Unified Astronomy Thesaurus concepts: Active galactic nuclei (16); Strong gravitational lensing (1643); Reverberation mapping (2019); Supermassive black holes (1663)

1. Introduction

The ability to measure precise black hole masses is critical to understanding the formation and accretion history of supermassive black holes (SMBHs) and their role in the evolution of their host galaxies over cosmic time. While stellar and gas kinematics can be used in nearby galaxies (e.g., Kormendy & Richstone 1995; Ferrarese & Ford 2005; McConnell & Ma 2013), these approaches are not feasible in the distant universe where the black hole sphere of influence cannot be resolved, with the exception of extraordinary cases (e.g., Gravity Collaboration et al. 2018). The technique of reverberation mapping (Blandford & McKee 1982; Peterson 1993, 2014) utilizes the gaseous broad emission line region (BLR) in the inner light days of active galactic nuclei (AGNs) to make M_{BH} measurements possible at cosmological distances.

Given its proximity to the central black hole, the BLR gas moves at speeds on the order of $10,000 \text{ km s}^{-1}$, leading to a Doppler broadening of emission lines that can be measured, ΔV . By monitoring the AGN over time, one can measure a time lag, τ , between fluctuations in the AGN continuum and the broad emission line strength. Assuming the motion of the gas is dominated by the black hole's gravity, these quantities

provide an estimate of the black hole mass,

$$M_{\text{BH}} = f \frac{c\tau\Delta V^2}{G}, \quad (1)$$

where f is a dimensionless virial factor of order unity that accounts for the unknown structure, kinematics, and orientation of the BLR.

The observed relation between the BLR radius and AGN luminosity (Kaspi et al. 2000, 2005; Bentz et al. 2013) has enabled “single-epoch” M_{BH} measurements in which τ and ΔV can be measured from a single spectrum. This opens up the possibility of using large spectroscopic surveys to measure thousands of black hole masses and study the coevolution of black holes and their host galaxies across cosmic time (e.g., Shen et al. 2011). However, the majority of reverberation mapping measurements are based on the $\text{H}\beta$ emission line, which is at optical wavelengths for local AGNs, making it suitable for ground-based campaigns. To extend the single-epoch method to higher redshifts requires the use of UV emission lines, most commonly C IV (Vestergaard 2002; Vestergaard & Peterson 2006) and Mg II (McLure & Jarvis 2002). However, the relationship between the $\text{H}\beta$, C IV, and Mg II BLRs is poorly understood, and the limited redshift and luminosity range of UV reverberation mapping measurements means that the $r_{\text{BLR}} - L$ relationships for these

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lines rely on extrapolations from more local AGNs. Additionally, differences between C IV and H β emission line profiles have called into question the validity of C IV as a single-epoch mass estimator (e.g., Baskin & Laor 2005; Shen & Kelly 2012), although other analyses have suggested that these issues are mitigated by proper data quality selection (e.g., Vestergaard & Peterson 2006).

A number of campaigns have aimed to improve the C IV $r_{\text{BLR}} - L$ relation by increasing the size and dynamic range of the sample of UV-based reverberation mapping M_{BH} measurements (Peterson et al. 2005, 2006; Kaspi et al. 2007; Trevese et al. 2014; Lira et al. 2018, 2020; Grier et al. 2019; Hoormann et al. 2019), but such measurements are complicated for a number of reasons. First, high- z measurements typically focus on high-luminosity AGNs to reach the required signal-to-noise ratio (S/N) of the spectra. These AGNs have large BLRs due to the $r_{\text{BLR}} - L$ relation, requiring long campaign durations, an obstacle that is only amplified by the cosmological $(1+z)$ time dilation. Additionally, high-luminosity AGNs tend to have smaller-amplitude fluctuations in the continuum compared to their lower-luminosity counterparts, but large fluctuations with distinct features are essential for measuring emission line time lags.

In this paper, we present an extraordinary object that solves all of these issues by means of strong gravitational lensing. A quasar at redshift $z=2.805$ that is lensed by a foreground galaxy cluster, SDSS J2222+2745 was discovered by Dahle et al. (2013) as part of the Sloan Giant Arcs Survey (Hennawi et al. 2008).¹¹ Due to the image magnifications ($\mu_A = 14.5 \pm 2.7$, $\mu_B = 10.8 \pm 4.3$, $\mu_C = 6.7 \pm 1.0$; Sharon et al. 2017), the quasar is visible at $g \sim 21$ despite being intrinsically dimmer, and the estimated C IV time lag is on the order of 100 days in the observed frame. Photometric monitoring of the brightest images, A, B, and C, has shown that image C leads the others by 2 yr ($\Delta\tau_{AB} = -42.44$ days and $\Delta\tau_{AC} = 696.65$ days; Dahle et al. 2015; Dyrlund 2019), meaning that all light curves can be extended by 2 yr, shortening the required campaign duration further. Finally, the leading image C was observed to undergo extreme flux variations between 2014 and 2016, brightening by over 1 mag in the g band, classifying it as an “extreme variability quasar” (EVQ; Rumbaugh et al. 2018). The EVQs are rarely found at $z \sim 3$, in part due to the high luminosities required for them to be observable from Earth, but the magnification effect of gravitational lensing allows us to overcome this obstacle. Since the trailing images necessarily follow the behavior of the leading image, they were guaranteed to undergo the same large-scale flux variations that are necessary for reverberation mapping measurements.

In Sections 2 and 3, we describe the spectroscopic and photometric monitoring campaigns and the procedures for data reduction and flux calibration. In Section 4, we describe the multicomponent model used to decompose the spectra into their individual components, and in Section 5, we describe the intercalibration between the spectroscopic and photometric emission line measurements. In Section 6, we present spectroscopic and photometric C IV and continuum light curves and measure velocity-resolved time lags, placing SDSS

J2222+2745 on the C IV $r_{\text{BLR}} - L$ relation. We conclude in Section 7. When necessary, we adopt a Λ CDM cosmology with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.3$, and $\Omega_\Lambda = 0.7$.

2. Observations

Spectroscopic observations were carried out using the Multi-Object Spectrograph at the Gemini Observatory North (GMOS-N; Hook et al. 2004). The spectra were taken in queue mode, with 6000 s of exposure time per lunation, between April and December when the target was visible. From 2016 June to 2016 December, observations consisted of four 1500 s exposures. In 2017, GMOS-N upgraded the CCDs from the previous e2v deep depletion (DD) device detectors to the current Hamamatsu detector array. The Hamamatsu detectors are physically thicker than the e2v DD detectors and therefore have a higher cosmic-ray hit rate, so we changed the observing strategy to use six 1000 s exposures for the duration of the campaign. The minimum observing conditions provided to the queue system were 80th percentile sky background (background V -band magnitude $\mu_V > 19.5$), 70th percentile cloud cover (signal loss $< 20\%$), and 70th percentile image quality (FWHM of image at $0.475 \mu\text{m} < 0''.35$).¹² All timing windows were scheduled at least 3 days from the full moon, and shorter windows were set when the target was close to the moon. The observing constraints were loosened and observations were allowed to be split across multiple nights during extended periods of unfavorable conditions. This was particularly important during the fall 2017 months, when weather on Maunakea was particularly bad, as well as spring 2020, when the telescopes were operating at limited capacity due to the COVID-19 pandemic.

We designed the slit mask with slitlets on the brightest quasar images, A, B, and C, and placed additional slitlets on three bright nearby stars to be used for flux calibration. The slitlets were $2''$ wide, which is much wider than the expected seeing and residual misalignments, minimizing slit losses. The same slit mask was used for the whole campaign duration. We used the B600 grating with 600 lines mm^{-1} centered at 6500 Å and the GG455 order blocking filter. After dithering and flux calibration, this setup gives coverage from ~ 5000 to 8200 Å at 1.0 Å pixel^{-1} with 2×2 binning (0.9 Å pixel^{-1} for the e2v DD detectors.) These choices provide simultaneous coverage of both the C IV $\lambda\lambda 1548.2, 1550.8$ and C III] $\lambda 1908.7$ emission lines. Calibration frames were taken every night that data were taken, including bias, flat, and CuAr arc lamp exposures.

We missed one full lunation in 2017 August and one-third of our time allocation in 2019 July due to poor weather. We also missed the 2020 April lunation due to the COVID-19 telescope shutdown, but were able to use the time to get an additional epoch in 2020 July. In total, we obtained spectra for 36 lunations from 2016 June to 2020 September. Nine of these were split across 2 nights, and one was split across 3 nights, giving a total of 47 epochs. The median S/Ns per pixel of the spectra after flux calibration are 30.7, 28.4, and 23.6 for images A, B, and C, respectively. The standard deviations of the distributions of S/N per pixel over the duration of the campaign were 6.0, 5.7, and 7.1.

In addition to spectroscopy, we obtained higher-cadence photometric observations with the Alhambra Faint Object

¹¹ The name SDSS J2222+2745 is used in some publications to refer to the foreground galaxy cluster or the full lens system. The quasar can be found in the NASA/IPAC Extragalactic Database (NED) with the identifier SDSS J2222+2745:[SBD2017].

¹² A detailed explanation of the observing conditions can be found at <https://www.gemini.edu/observing/telescopes-and-sites/sites#Constraints>.

Table 1
Standard Star Properties

Star	R.A. (J2000.0)	Decl. (J2000.0)	<i>u</i> (mag)	<i>g</i> (mag)	<i>r</i> (mag)	<i>i</i> (mag)	<i>z</i> (mag)	Spectral Type	Template File
stand1	22:22:04.30	+27:45:34.0	20.80 ± 0.06	19.66 ± 0.01	19.03 ± 0.01	18.74 ± 0.01	18.59 ± 0.03	K0V	G 149-25
stand2	22:22:06.23	+27:45:35.6	20.22 ± 0.04	19.04 ± 0.01	18.56 ± 0.01	18.35 ± 0.01	18.27 ± 0.02	G5V	G 11-45
stand3	22:22:05.36	+27:45:37.9	21.67 ± 0.12	19.78 ± 0.01	18.96 ± 0.01	18.67 ± 0.01	18.49 ± 0.03	K3IV	121146

Note. The three standard stars used for flux calibration along with their coordinates, SDSS photometry, fitted spectral type, and Indo-U.S. Library of Coudé Feed Stellar Spectra template file names.

Spectrograph and Camera (ALFOSC) at the 2.56 m Nordic Optical Telescope (NOT). Observations were taken with the SDSS_*g'*, SDSS_*i'*, and He I 588_6 (hereafter the *g*-, *i*-, and narrowband) filters with mean cadences of 18.3, 18.7, and 17.7 days for the *g*, *i*, and narrow band, respectively. The narrowband filter covers the core of the redshifted C IV emission line, providing higher-cadence measurements of the emission line flux to supplement the spectroscopy. Each night consisted of three 600 s exposures with the *g*- and narrowband filters and three 300 s for the *i*-band filter.

The *g*-band photometric monitoring began in 2011 September, while the narrow- and *i*-band monitoring did not begin until 2016 June and July, respectively. The *g*-, *i*-, and narrowband photometry used in this paper extend until 2020 September, 2019 December, and 2019 October, respectively. Beginning on 2016 June 1, we obtained 86, 49, and 41 epochs for the *g*, *i*, and narrow band. The median S/N ± standard deviation in S/N over the duration of the campaign were (*g*, *i*, narrow) = (52 ± 24, 33.7 ± 9.7, 24.5 ± 8.0) for image A, (42 ± 19, 26.6 ± 7.6, 18.7 ± 6.8) for image B, and (40 ± 17, 23.7 ± 7.9, 18.6 ± 7.0) for image C.

3. Spectral Data Processing

Data processing began with bias subtraction, flat-fielding, and wavelength calibration using the GMOS IRAF¹³ routines provided by Gemini Observatory. An additional quantum efficiency (QE) correction step was added for all data taken after 2016 due to the different QEs of the Hamamatsu detector chips. Following these steps, we use a Python implementation of L.A.Cosmic (van Dokkum et al. 2012) to perform cosmic-ray cleaning on the 2D spectra. The quasar and standard star spectra are then extracted using the IRAF *apall* routine using an unweighted extraction with a fixed 2''74 aperture.

3.1. Flux Calibration

For each epoch, we obtain observations of three standard stars for the purpose of flux calibration. The stars are in three separate slits of the slit mask, and the observations are obtained simultaneously with the quasar observations. These stars have not been previously studied, so we use a spectral-type fitter (Pickles & Depagne 2010)¹⁴ with the Sloan Digital Sky Survey (SDSS; York et al. 2000) photometry to determine their spectral types. We then obtain a template spectrum based on that spectral type from the Indo-U.S. Library of Coudé Feed

Stellar Spectra (Valdes et al. 2004).¹⁵ The SDSS photometry used and the spectral type determined with the fitter are listed in Table 1.

Using the normalized template spectra and the SDSS magnitudes, we can compute a response function, $r(\lambda)$, to convert the observed spectra from units of counts s⁻¹ to physical units of erg s⁻¹ cm⁻² Å⁻¹. The response function accounts for the CCD sensitivity, as well as the transparency of the atmosphere as a function of wavelength. Assuming we know the true spectrum of the standard stars in flux units, this is simply

$$r(\lambda) = \text{template}(\lambda) / \text{star}(\lambda). \quad (2)$$

Prior to computing $r(\lambda)$, we need to fine-tune the wavelength solution, correct for the radial velocities of the standard stars, and convolve the template spectra by the point-spread function (PSF) of the observed spectra. These steps are described below.

3.1.1. Slit Positioning Correction

Since the slit width is much larger than the PSF, the positions of the quasar images and stars on the slit can affect the position in the wavelength dispersion direction on the CCD. If the radial velocities of the standard stars were known, we could use the stellar absorption features to determine this wavelength offset, but these values have not yet been measured.

Instead, we measure the position of the sharp H α absorption line for each standard star by cross-correlating each night's spectrum with the template spectrum in a 40 Å window centered on 6563 Å. Figure 1 shows the distribution of the measured wavelength offsets relative to $\lambda = 6562.8$ Å and the corresponding radial velocity. These are not necessarily the radial velocities of the stars relative to the heliocentric frame, since the wavelength offset includes a zero-point offset due to the positioning on the slit. Using the median values of these distributions, we assign for each star a “true” radial velocity for calibration purposes and determine the correct position of the H α line based on this value. We then add a fixed value in angstroms to each wavelength in the spectra so that H α is aligned to this reference wavelength, correcting for any offsets in slit positioning.

Assuming the positioning deviations in the slit are due only to linear shifts of the slit mask and not rotations, the shift should be the same for every object on the CCD. Figure 2 shows the wavelength shifts required for each of the three standard stars over the duration of the observing campaign. The wavelength shifts at each epoch are very similar for all three stars, as expected. We can therefore use these offsets to apply a shift to the quasar spectra, which should be affected in the same

¹³ IRAF was distributed by the National Optical Astronomy Observatory, which was managed by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation.

¹⁴ <https://lco.global/~apickles/SpecMatch/>

¹⁵ <https://www.noao.edu/cflib/>

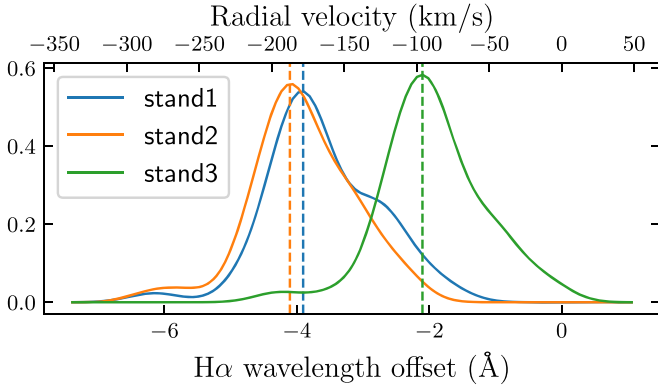


Figure 1. Distributions of the position of the H α absorption line relative to 6562.8 Å and the corresponding radial velocity for each of the three standard stars. Note that these are not necessarily true radial velocities, since they include a zero-point offset from the positioning of the stars on the slit.

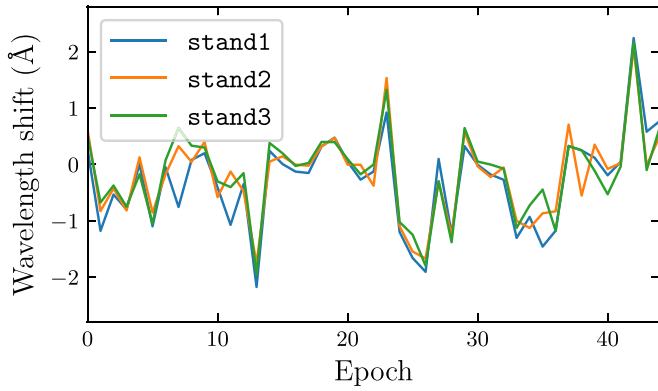


Figure 2. Wavelength offsets for each standard star to correct for variations in the positioning of the standard stars on the slits. The projected slit width is ~ 12.5 Å, so the measured deviations are well within the expected limits.

way. We calculate the mean of the offsets for the three standard stars and shift the three quasar spectra by this amount.

3.1.2. Radial Velocity and PSF Correction

Before calculating the response function, we need to shift the template spectra according to the stellar radial velocities, as well as convolve the templates with a PSF to match that of the observations. We use the radial velocities determined in the previous section, and the PSF determination is done as follows.

For simplicity, we assume that the PSF is Gaussian in wavelength with a standard deviation, σ_{PSF} . We also assume that σ_{PSF} is constant over the wavelength range of the spectra. After multiplying the wavelength axis of the template spectrum by a factor $\gamma = 1 + v/c$ to correct for the radial velocity of the star, we multiply the template by a pseudoresponse function, $\alpha + \beta\lambda$, and convolve with a Gaussian $\mathcal{N}(0, \sigma_{\text{PSF}}^2)$.

We then use the minimizer `scipy.optimize.minimize` (Virtanen et al. 2020) to find the parameters $\theta = (\alpha, \beta, \sigma_{\text{PSF}})$ that maximize the log-likelihood,

$$l = -\frac{1}{2} \sum_{\lambda \in [\lambda_{\min}, \lambda_{\max}]} \left[\frac{(f_{\text{obs}}(\lambda) - M(\lambda, \theta))^2}{\sigma_{\text{obs}}^2(\lambda)} + \ln(2\pi\sigma_{\text{obs}}^2(\lambda)) \right], \quad (3)$$

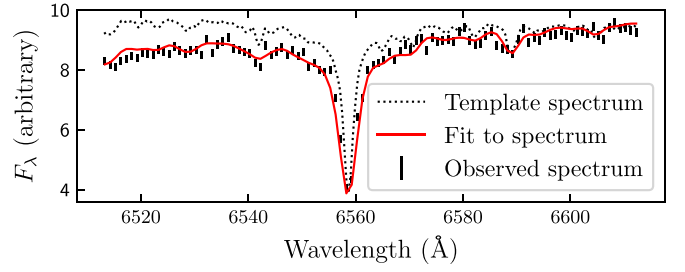


Figure 3. Standard star template spectrum corrected for radial velocity, scaled to match the observed flux values, and convolved to match the observed H α width. Note that the offset in the H α trough from $\lambda = 6562.8$ Å is due to the radial velocity of the observed star to which the template has been aligned.

where f_{obs} is the observed spectrum flux, σ_{obs} is the observed flux uncertainty, and M is our model,

$$M(\lambda; \alpha, \beta, \sigma_{\text{PSF}}^2) = [(\alpha + \beta\lambda)f_{\text{temp}}(\lambda)] * \mathcal{N}(0, \sigma_{\text{PSF}}^2), \quad (4)$$

where f_{temp} is the radial velocity-corrected template. We use a 50 Å radius window centered on the sharp H α absorption feature to do the fitting. An example fit is shown in Figure 3.

3.1.3. Calculating the Response Function

To calculate the response function, the template spectra are first shifted in wavelength according to the radial velocities determined in the previous step and then convolved with a Gaussian of width σ_{PSF} . The spectra are then linearly interpolated onto the wavelength scale of the observed standard star spectra. The response is then simply calculated, pixel by pixel, as $r(\lambda_i) = f_{\text{temp}}(\lambda_i)/f_{\text{stand}}(\lambda_i)$. Due to wavelength-dependent offsets in the three response functions arising from imperfect standard star template matches, we choose to use only the brightest standard star to compute the response function. We use the other two stars to perform sanity checks and estimate the uncertainty in the calibration.

3.2. Uncertainty Due to Flux Calibration

The flux calibration procedure described above has the potential to introduce additional uncertainty that is not accounted for in the formal propagation of uncertainty due to random noise. Photometric monitoring confirms that the standard stars do not vary significantly over the course of the observing campaign, so we can use them to estimate the magnitude of this additional calibration uncertainty.

We assume that the standard star spectrum remains constant over time with some mean spectrum, $m(\lambda)$. The uncertainty in the spectra can be described as a combination of the random noise for each epoch, $\sigma_i(\lambda)$, and an additional uncertainty source due to flux calibration, $\sigma_0(\lambda)$. Combined, the total uncertainty for each epoch is $\sigma_{\text{tot},i}^2(\lambda) = \sigma_i^2(\lambda) + \sigma_0^2(\lambda)$.

The response function is calculated with the brightest of the standard stars, stand2, so we use the other stars, stand1 and stand3, with the Markov Chain Monte Carlo (MCMC) code EMCEE (Foreman-Mackey et al. 2013) to explore the parameter space of $\sigma_0(\lambda)$ and $m(\lambda)$ and quantify the additional uncertainty due to the flux calibration. The log-likelihood function is

$$l(\lambda) = -\frac{1}{2} \sum_i \left[\frac{(d_i(\lambda) - m(\lambda))^2}{\sigma_{\text{tot},i}^2(\lambda)} + \ln(2\pi\sigma_{\text{tot},i}^2(\lambda)) \right], \quad (5)$$

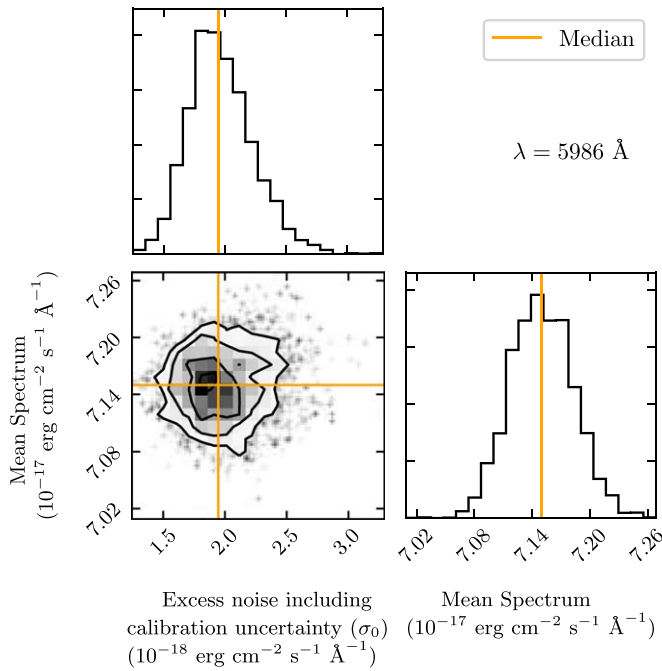


Figure 4. Corner plot showing the inference on the mean standard star 1 spectrum and the additional uncertainty due to calibration and other systematics. The example shown is for $\lambda = 5986 \text{ \AA}$, which falls on the C IV emission line. The median values are shown by the orange lines.

where $d_i(\lambda)$ is the observed flux-calibrated standard star spectrum and the sum is over all epochs. From the resulting MCMC samples, we can estimate the value of $\sigma_0(\lambda)$ for each wavelength bin.

Using the full wavelength resolution, σ_0 is too small to be measurable compared to the random uncertainty. In order to make a measurement, we increase the S/N by binning the spectra into wavelength bins of 5 \AA width. A corner plot showing the posterior distribution for one of the wavelength bins is shown in Figure 4. The orange lines show the median values for the two parameters $\sigma_0(\lambda)$ and $m(\lambda)$.

Figure 5 shows $m(\lambda)$ and $\sigma_0(\lambda)$ along with the binned spectra and σ_i for each of the individual epochs. Note that the spectra have been binned by a factor of 5 in the wavelength scale, so the random uncertainties are reduced by a factor of $1/\sqrt{5}$. Thus, on the unbinned wavelength scale, the random uncertainty still dominates over the calibration uncertainty for most wavelengths.

3.3. Correcting the Uncertainties for All Spectra

With the results of Section 3.2, we can now correct the uncertainties on all of the spectra to include the additional uncertainty due to flux calibration. For a general spectrum from epoch i , this is a simple correction:

$$\sigma_{q,i,tot} = \sqrt{\sigma_{q,i}^2 + \left(\frac{\sigma_{f,0}}{f_i}\right)^2 \cdot q_i^2}. \quad (6)$$

Here f_i is the spectrum of the standard star used to determine the calibration uncertainty, $\sigma_{f,0}$ is the inferred calibration uncertainty spectrum, q_i is the science spectrum, and $\sigma_{q,i}$ is the random uncertainty for that science spectrum.

Since we had to bin the standard star spectrum in order to make a measurement of $\sigma_{f,0}$, we do not have a measurement at

every pixel in the science spectra. To make the correction, we first linearly interpolate $\sigma_{f,0}$ back onto the wavelength scale of the science spectra and then calculate the uncertainties at every wavelength pixel according to Equation (6). The spectrum of quasar image A for the first epoch with its adjusted total uncertainty is shown in Figure 6.

4. Fitting the Spectra

Measuring the black hole mass using reverberation mapping methods requires an accurate measurement of the broad emission line flux and shape. Contaminating emission or absorption lines in the vicinity of the broad emission line of interest can lead to over- or underestimates of the broad emission line flux in different parts of the line profile. It is important, then, to disentangle all components of the spectra and isolate, e.g., the C IV emission line.

To do so, we construct a model spectrum that consists of several components, described below. We then fit that model to the data using the PYTHON programs `scipy.optimize.minimize` and `emcee`. We first use `scipy.optimize.minimize` to find the maximum-likelihood fit and then use `emcee` to explore the parameter space, allowing us to assign uncertainties to our fits.

4.1. Components

1. *AGN featureless continuum.* We model the AGN featureless continuum using a power law, $F_\lambda = C_{5000} \lambda^\alpha$, where C_{5000} is the normalization at 5000 \AA , observed frame, and α is the spectral index. Both of these parameters are free to vary for every epoch.
2. *C IV $\lambda\lambda 1548.2, 1550.8$.* The C IV is modeled as a sum of a fourth-order Gauss–Hermite function and two narrower Gaussians at the doublet central wavelengths. We initially attempted to model the line using only the Gauss–Hermite component but were unable to simultaneously fit the broad wings and the strong core of the line. The combination of the three functions allows the Gauss–Hermite function to fit the broad line profile, and the narrower Gaussian component fits the core of the line. After fitting to the mean spectrum, all Gauss–Hermite parameters were allowed to vary, while the narrow Gaussian components were kept fixed for each epoch.
3. *Narrow absorption on C IV $\lambda\lambda 1548.2, 1550.8$.* There are two strong absorption features near the peak of the C IV emission line. Since masking these features removes important information needed to adequately fit the emission line, we model the absorption with two narrow Gaussians with amplitudes ranging from zero to -1 and sharing a common width. After summing all other components, we apply the absorption by multiplying the model by $1 - A_1 \mathcal{N}(\lambda_1, \sigma^2) - A_2 \mathcal{N}(\lambda_2, \sigma^2)$, where A_i are the amplitudes, λ_i are the central wavelengths, and σ is the shared standard deviation of the Gaussians. After fitting to the mean spectrum, these components are kept fixed for each epoch.
4. *C III] $\lambda 1908.7$.* The C III] is modeled with a fourth-order Gauss–Hermite function plus a narrow Gaussian at the central wavelength. All Gauss–Hermite parameters are allowed to vary for each epoch, while the narrow Gaussian components are kept fixed.

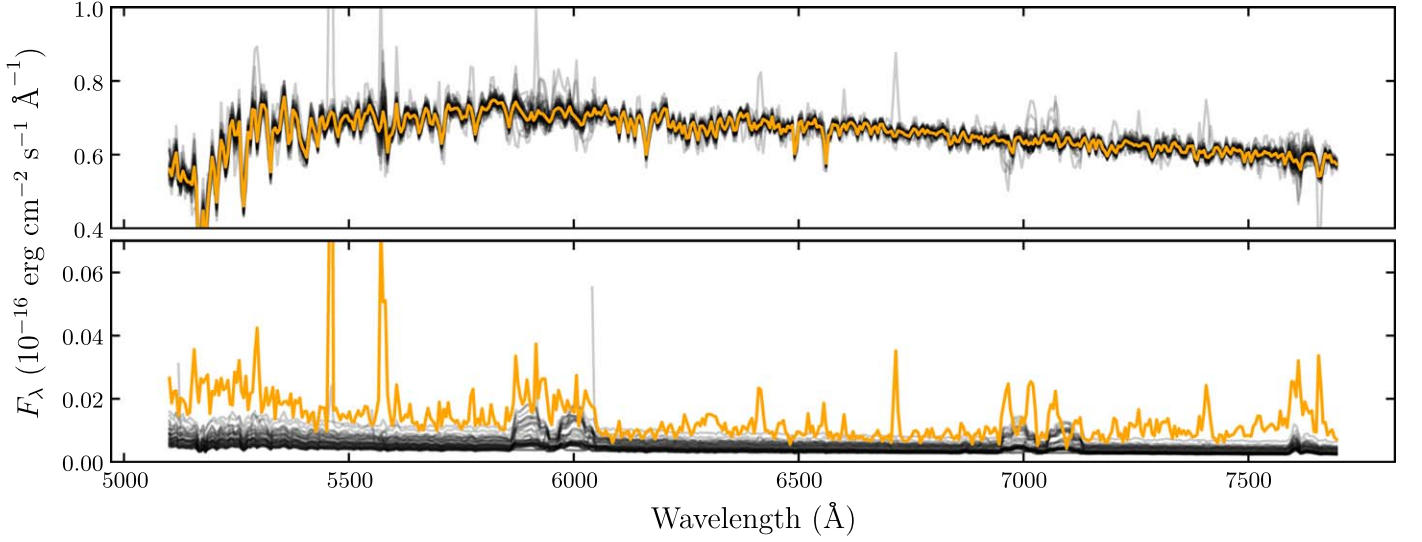


Figure 5. Top panel: inferred mean spectrum $m(\lambda)$ (orange) and flux-calibrated individual spectra (gray) for the standard star `stand1`. Bottom panel: inferred $\sigma_0(\lambda)$ (orange) and the individual spectra's random uncertainty (gray). The spectra shown here have been rebinned to wavelength bins of 5 Å.

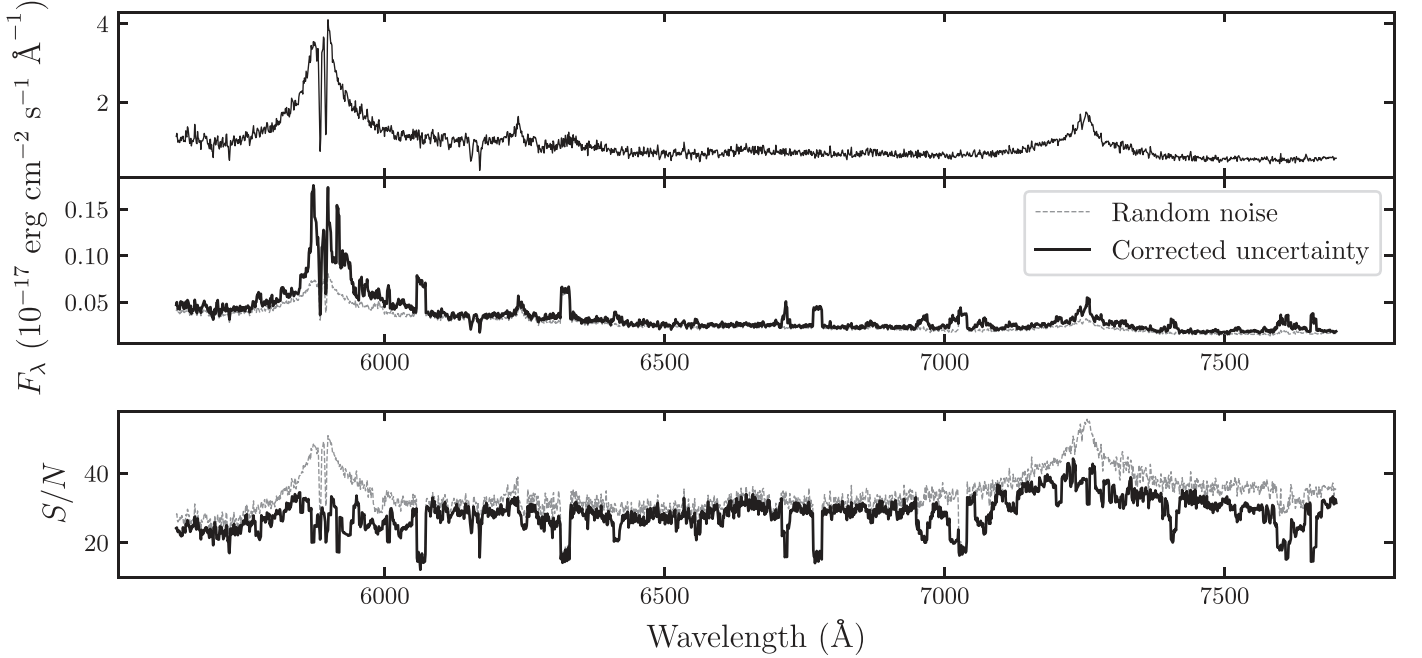


Figure 6. Top panel: spectrum of quasar image A for the first epoch. Middle panel: original random uncertainty (dotted line) and corrected uncertainty (solid line) including calibration uncertainty and other additional sources of noise. Bottom panel: original S/N calculated using only random uncertainty (dotted line) and the S/N with the corrected uncertainty (solid line).

5. Si IV + O IV] $\lambda 1400$. The Si IV + O IV] blend is modeled using a single broad Gaussian. Once fit to the mean spectrum, the amplitude and width are allowed to vary for each epoch, but the centroid is fixed.
6. O III] $\lambda\lambda 1660.8, 1666.2$. The O III] doublet is modeled as a single blended line with a narrow and broad Gaussian component, both centered on the same wavelength. The broad component parameters are allowed to vary for each epoch, while the narrow component is fixed.
7. He II $\lambda 1640.4$. The He II line is modeled with a narrow and broad Gaussian component. The broad component

parameters are allowed to vary for each epoch, while the narrow component is fixed.

8. N IV] $\lambda 1486.5$. The N IV] emission line, located in the blue wing of C IV, is modeled using a broad Gaussian. All parameters are allowed to vary for each epoch.
9. N III] $\lambda 1750$. The broad N III] emission line lies between the C IV and C III] emission lines and is modeled as a single Gaussian. We are able to fit this component in the mean spectra of each observing season, but the S/N of the individual spectra is not high enough to constrain the fit. We therefore keep this component fixed when fitting each epoch.

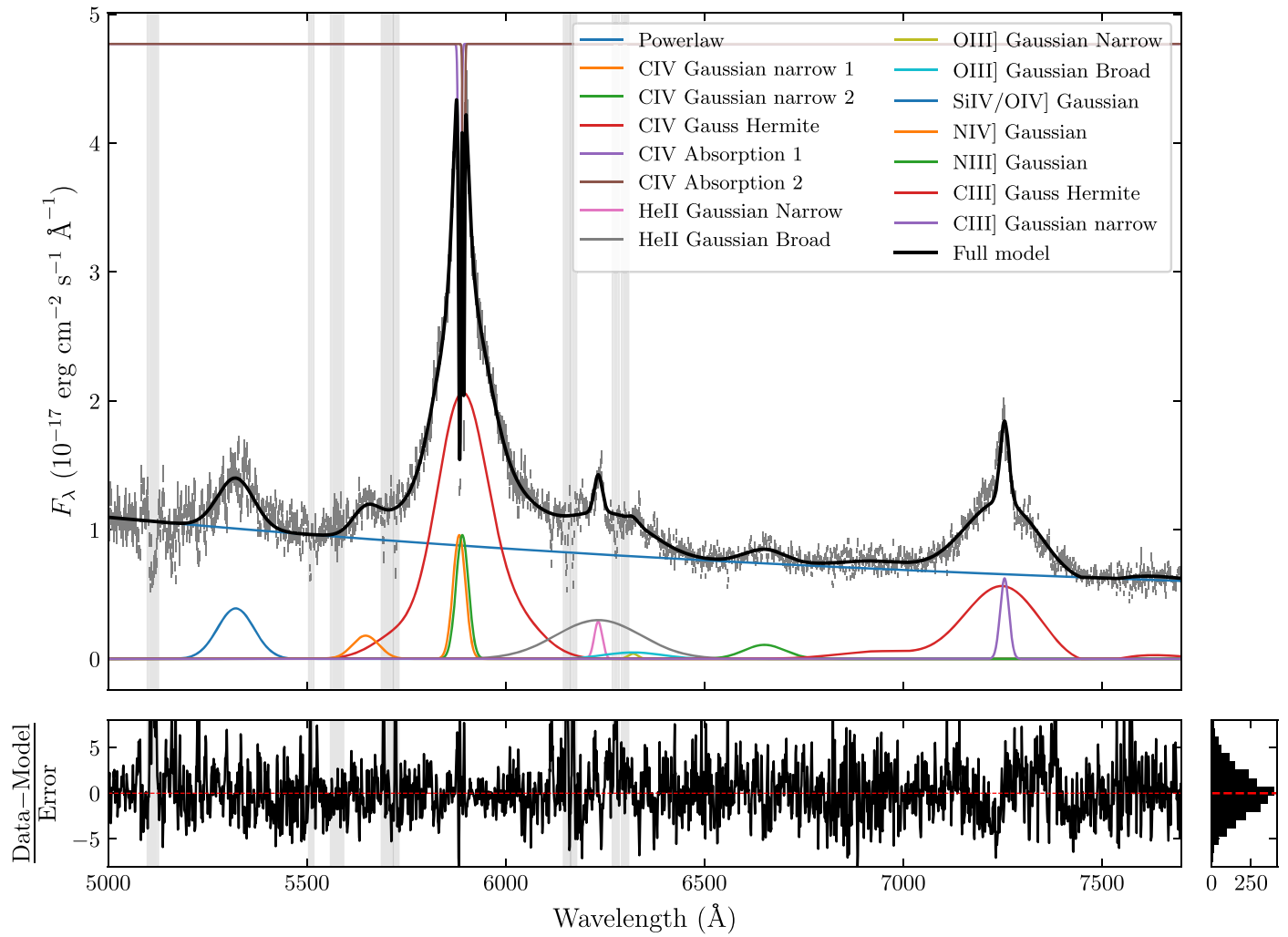


Figure 7. Example model fit to the quasar image A spectrum from 2017 June 21. The top panel shows the data in gray, the total model fit in black, and the individual components in color. Gray shaded bands indicate wavelength ranges that were masked out during the fitting procedure due to either bad pixels or unmodeled absorption features. The normalized residuals are shown in the bottom panel.

4.2. Fitting Procedure

Before fitting the spectra for each individual epoch, we fit the mean quasar spectrum of each image to provide the initial parameter guesses. We start with the mean spectrum of image A, which is the brightest of the three images and thus has the highest S/N. Initially, we mask all of the emission and absorption features and fit the featureless power-law continuum to the unmasked regions. We then unmask the C IV emission line and fit the Gauss–Hermite function, narrower Gaussians, and two absorption features, keeping the power-law parameters and absorption trough widths fixed. Allowing the absorption width to vary at this stage typically led to one of the absorption features encompassing both absorption troughs, and the fits failed to converge. Next, we keep the Gauss–Hermite and power-law components fixed and allow all parameters in the narrow C IV Gaussians and two absorption features to vary. Finally, we allow all of the model parameters to vary.

We then unmask the emission features near C IV and add the O III], He II, Si IV + O IV], N III], and N IV] components to the model. We keep the parameters of the power-law, C IV, and absorption components fixed and allow all parameters of the new components to vary, and then we repeat the fit allowing all parameters to vary. Finally, we unmask the C III] broad

emission line, introduce the C III] Gauss–Hermite and Gaussian components to the model, and fit the entire model, allowing all parameters to vary. This becomes the best-fit model for the quasar image A mean spectrum.

Next, we fit the image B and C mean spectra in two steps. Starting with the best-fit model for the image A spectrum, we allow the power-law index, power-law normalization, and amplitudes of all other components to vary while keeping everything else fixed. We then do the fit again, keeping only the emission line centroids and absorption line centroids and widths fixed. This provides the best-fit model for the mean spectra of images B and C.

Using the best-fit models for the three mean spectra as the starting guesses, we then proceed to fit the per-season mean spectra. Finally, we use the resulting fits as the starting guesses to fit the spectra for each individual epoch. For this stage, all broad components are allowed to vary except N III] (see Section 4.1), and all narrow components are kept fixed. An example fit to one of the quasar spectra is shown in Figure 7.

5. Broad- and Narrowband Photometry

Throughout the spectroscopy campaign, we also obtained narrow- and broadband photometry of the three quasar images

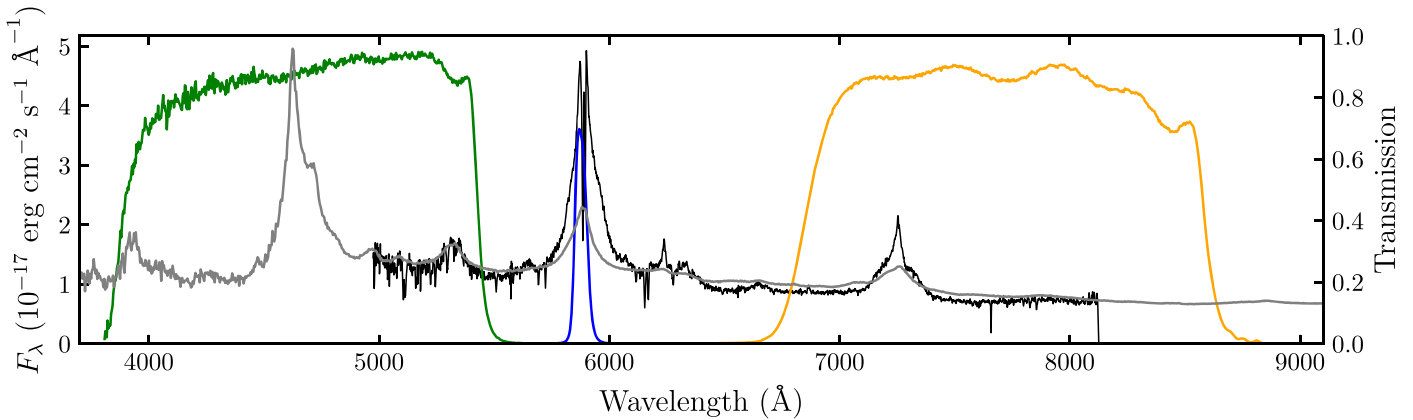


Figure 8. Broad- and narrowband filter transmission curves shown in relation to the SDSS J2222+2745 mean quasar spectrum (black) and the Vanden Berk et al. (2001) mean quasar spectrum (gray). The green, orange, and blue curves are the g -, i -, and narrowband filter transmission curves, respectively. Note that the Vanden Berk et al. (2001) spectrum is plotted with an arbitrary scale and is only meant to show the positions of the emission lines in relation to the filters.

at roughly twice the spectroscopic cadence. The higher-cadence photometry provides g - and i -band continuum light curves, as well as narrowband C IV measurements to supplement the spectroscopic observations. The transmission curves of the three filters are shown in Figure 8, plotted on the quasar mean spectrum.

The broad- and narrowband filters provide reasonable estimates of the continuum and C IV line flux, respectively, but these measurements are imperfect, since the broadband filters cover emission line regions and the narrowband filter includes both the C IV emission line and the power-law continuum. To disentangle these components, we can examine nights in which we obtained both spectroscopy and photometry and produce conversion factors between the three measurements. The spectral range of the data does not extend all the way to the ends of the broadband filters, so we utilize the mean quasar spectrum from Vanden Berk et al. (2001), also shown in Figure 8.

Since the Vanden Berk et al. (2001) spectrum consists of emission lines plus a power-law continuum that are not of equal strength to the quasar spectrum, we need to rescale the Vanden Berk et al. (2001) spectrum. We first subtract a power-law continuum fit from the Vanden Berk et al. (2001) spectrum so that we are left with only the emission line component. We then multiply by a scale factor to match the C IV emission line strength of the SDSS J2222+2745 mean spectrum. Finally, we add the power-law continuum component of the SDSS J2222+2745 mean spectrum, leaving us with an extended estimate of the SDSS J2222+2745 spectrum. Here we are assuming that the line ratios from the Vanden Berk et al. (2001) spectrum are the same as the line ratios of the quasar mean spectrum, and we do not allow for any variations in these values.

Next, we integrate the power-law continuum component, as well as the full rescaled Vanden Berk et al. (2001) spectrum, over the g - and i -band transmission curves to determine the continuum contribution to the flux in the two bands. Doing so, we find that 89% of the flux in the g band and 85% of the flux in the i band comes from the continuum. We perform the same procedure using the mean spectra for each individual season and find that the continuum fractions do not change by more than 5% throughout the campaign.

Using these percentages, we scale the measured broadband photometry to obtain the continuum fluxes in these bands. We then use these two values to determine the power-law index

and normalization for each photometric epoch. As a check on the method, the power-law determinations from the g - and i -band photometry can be compared with spectra on days where the spectroscopic and photometric observations overlap. Three example fits are shown in Figure 9.

Finally, we integrate the power-law continuum fit over the narrowband filter transmission curve to determine the continuum contribution in this band for every epoch. Subtracting this from the narrowband measurements, we are left with the C IV contribution to these fluxes.

6. Results and Discussion

6.1. Light Curves

Using the model fits to the data from Section 4, we measure emission line fluxes in a number of ways. First, we take the Gauss–Hermite fits to the spectra that represent the broad C IV emission component. For each spectrum, we take the sample of fits from the MCMC chains and compute the integrated C IV Gauss–Hermite flux for each. From these values, we compute the median integrated flux value and 68% confidence interval. The benefit of this approach is that we can calculate the full contribution of broad C IV despite the strong absorption in the core, all while maintaining realistic uncertainty estimates. While we do lose the information contained in the residuals of the emission line fits, integrating over the full emission line profile likely averages this information out. The resulting light curve is shown in the top panel of Figure 10. Each data point is shifted in time using the measured gravitational time delays of $\Delta\tau_{AB} = -42.44$ and $\Delta\tau_{AC} = 696.65$ days (Dyrlund 2019), setting image B as the reference. The fluxes are then scaled using the measured magnitude offsets from gravitational lensing of $\Delta m_{AB} = 0.353$ and $\Delta m_{AC} = 0.515$ (Dyrlund 2019).

In addition, we find evidence for microlensing in image B, which affects the compact continuum source but not the extended BLR. Since the magnifications were measured using the g -band continuum, which is affected by microlensing, we need to apply a correction factor of $\Delta m = 0.072$ to all emission line measurements on image B. This correction is discussed further in Section 6.6.

Next, we take the full model fits to the spectra and subtract all model components except the C IV emission and absorption components. This procedure leaves the emission line data for C IV but with the contaminating components in the emission

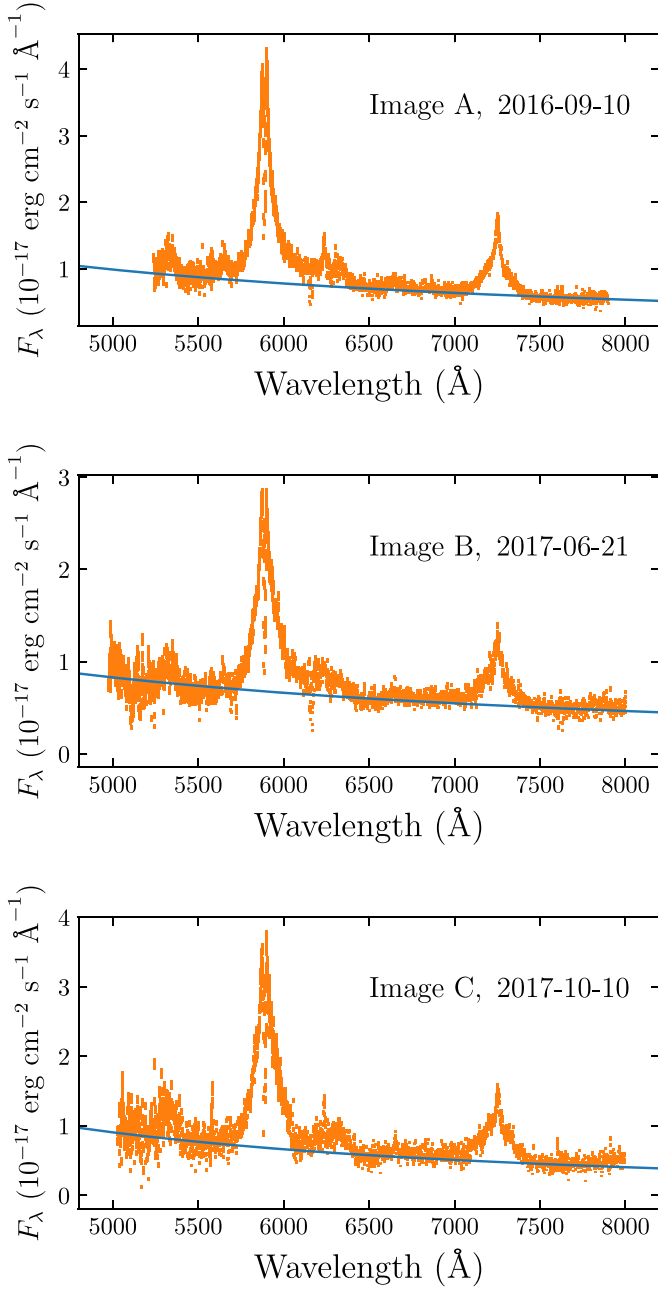


Figure 9. Comparison of the power law determined only from broadband photometry (blue) to a spectrum taken on the same day (orange). The examples shown are, from top to bottom: image A, 2016 September 9; image B, 2017 June 21; and image C, 2017 October 10.

line wings removed and the continuum subtracted. Using this method, we retain the information contained in the residuals of the spectral fits and can directly compare the measurements to the narrowband photometry, which also includes the narrow C IV emission and absorption features. With these spectra, we compute the C IV emission line flux for each epoch integrated over four wavelength windows, 5650–5780 Å (–12,420 to –5800 km s^{–1}), 5780–5848 Å (–5800 to –2340 km s^{–1}), 5904–6000 Å (510–5400 km s^{–1}), and 6000–6130 Å (5400–12,020 km s^{–1}), and the narrowband transmission curve, the results of which are shown in Figures 10 and 11.

Finally, we include the measurements from the narrowband photometry to supplement the light curve measured from the

spectra. Using the procedure described in Section 5, we use the *g*- and *i*-band photometry to calculate the continuum contribution in the narrowband filter. We then subtract these values from the measured narrowband photometry to produce the light curve shown in the third panel of Figure 10. The combined narrowband light curve from spectroscopy and photometry is shown in the fourth panel.

6.2. Emission Line Time Lags

We use cross-correlation analysis to measure the lag between the continuum and emission line fluctuations and the flux randomization and random subset selection method (FR/RSS; Peterson et al. 1998) to estimate uncertainties. We compute the lags for each emission line light curve compared to the *g*-band continuum from photometry.

For each light curve, we produce 1000 sample light curves by taking a random subset of the observed light curve and shifting the fluxes randomly according to their uncertainties. We then compute the interpolated cross-correlation function (ICCF; Gaskell & Peterson 1987; White & Peterson 1994) for every light curve in the sample and compute the lag τ_{peak} at which the ICCF reaches its peak value r_{max} and the lag centroid defined by

$$\tau_{\text{cen}} = \frac{\int \tau r(\tau) d\tau}{\int r(\tau) d\tau} \quad (7)$$

for $r(\tau) \geq 0.8r_{\text{max}}$, where $r(\tau)$ is the correlation coefficient. The ICCFs and lag distributions are shown in Figure 12. We then calculate the median values and 68% confidence intervals for τ_{cen} and τ_{peak} , which are reported in Table 2.

In Figure 13, we show the light curve for the C IV Gauss–Hermite emission component plotted alongside the *g*-band continuum light curve. Also shown is the C IV Gauss–Hermite light curve shifted in time by the measured time lag of $\tau_{\text{cen}} = 36.5$ days (converted to the observed frame). The emission line light curve clearly tracks the fluctuations of the *g*-band continuum until MJD – 50,000 \approx 9600. Additional future monitoring data are necessary to shed light on the reason for the decrease in flux beyond this point.

In most cases, both τ_{cen} and τ_{peak} are in close agreement with each other. Notable exceptions are the measurements for the bluest wavelength bin, although they are consistent to within the uncertainties. Examining Figure 12, it is clear that the disagreement is an artifact of the double-peaked nature of the distribution of ICCF centroids, and the lag measurements for this light curve have large uncertainties as a result. This is unsurprising, given that this light curve is for a low-S/N part of the spectrum.

In Figure 14, we show the lag measurements for the four velocity bins and within the narrowband filter. There is a clear velocity structure in the line profile, with the core of the line responding on longer timescales and the wings responding on shorter timescales. This behavior is expected if the emission near the core of the line is produced by gas that is farther from the BLR center and the wing emission is produced by the high-velocity gas closer to the center. The symmetry of the velocity-lag structure suggests that the C IV-emitting gas motions are dominated by bound circular orbits rather than inflowing or outflowing motions (see, e.g., Bentz et al. 2009, Figure 10). We also show virial envelopes defined by $v^2 = GM_{\text{vir}}/c\tau$ for three choices of M_{vir} : 1×10^8 , 2×10^8 , and $4 \times 10^8 M_{\odot}$.

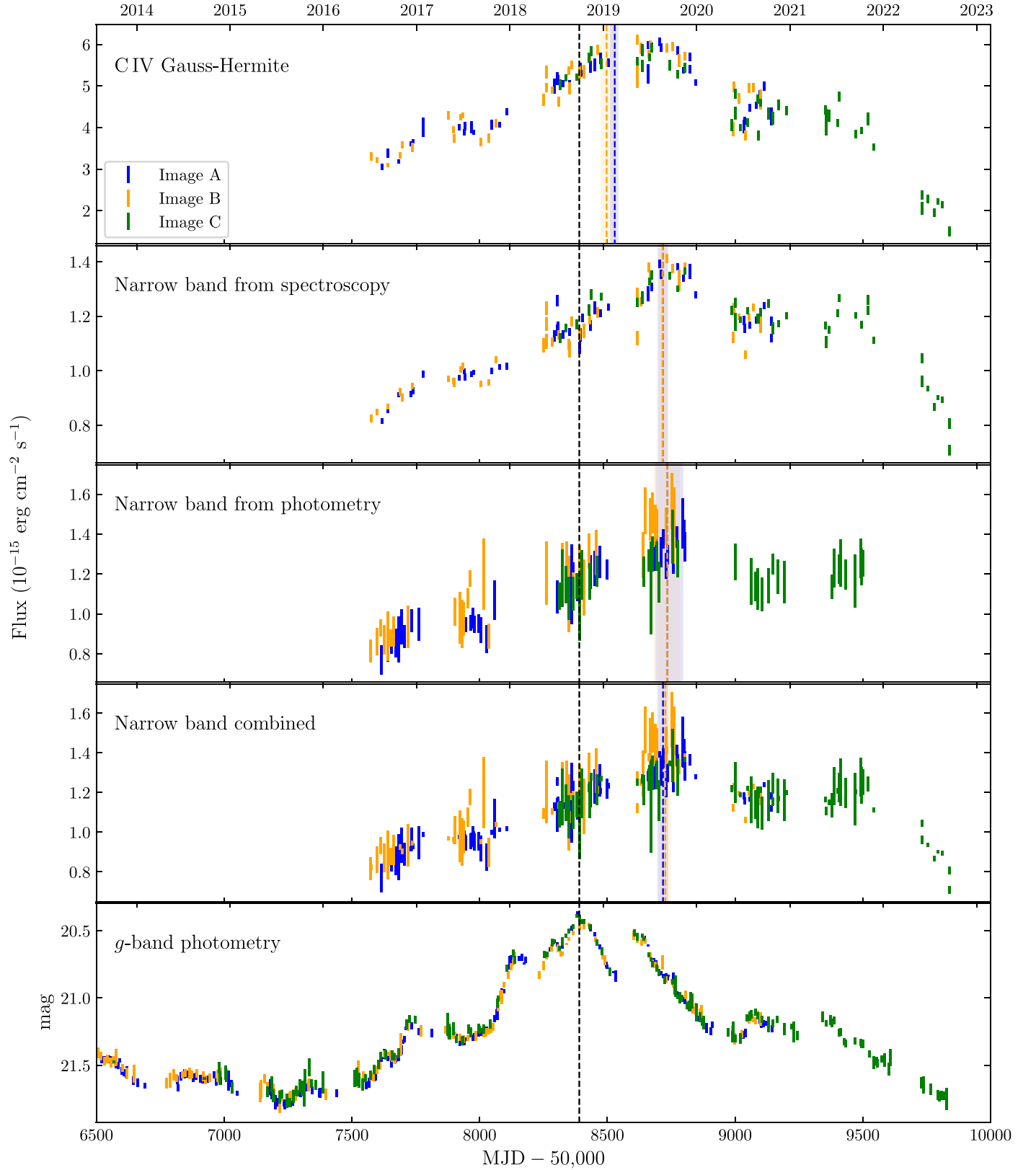


Figure 10. The C IV emission line light curves and g-band continuum light curve. The blue, orange, and green points correspond to quasar images A, B, and C, respectively. All data points have been shifted to the trailing image B observed frame and scaled to match the brighter image A flux using the measured gravitational lensing time delays and relative magnifications given in Section 6.1. In addition, a correction factor of $\Delta m = 0.072$ has been applied to all image B emission line measurements, as discussed in Section 6.6. The vertical dashed black line marks the peak of the g-band light curve at $\text{MJD} - 50,000 = 8390$. The vertical blue and orange dashed lines and shaded bands show the τ_{cen} and τ_{peak} lags (Section 6.2), respectively, shifted relative to $\text{MJD} - 50,000 = 8390$.

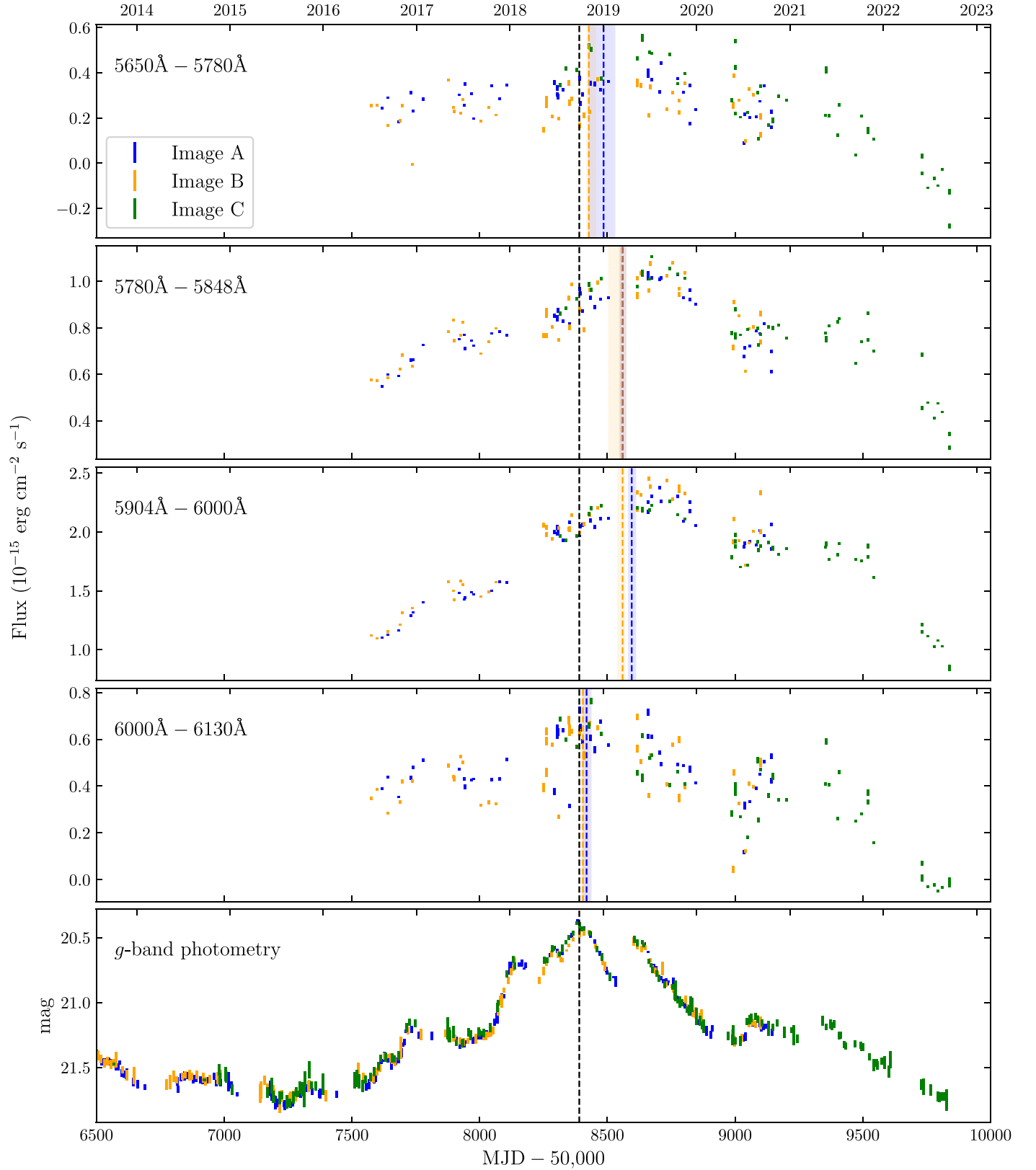


Figure 11. Same as Figure 10 but showing the four wavelength windows.

6.3. Radius–Luminosity Relation

Using the measured lags, we can place SDSS J2222+2745 on the BLR radius–luminosity relationship for C IV. Since the quasar luminosity varied significantly over the duration of the

campaign (~ 1.5 mag in the g band), the placement on the $r_{\text{BLR}} - L$ relation depends on when the luminosity measurement is made. Additionally, the luminosity calculation depends on the intrinsic magnification of the images due to gravitational lensing. We use the mean quasar spectrum for each image with

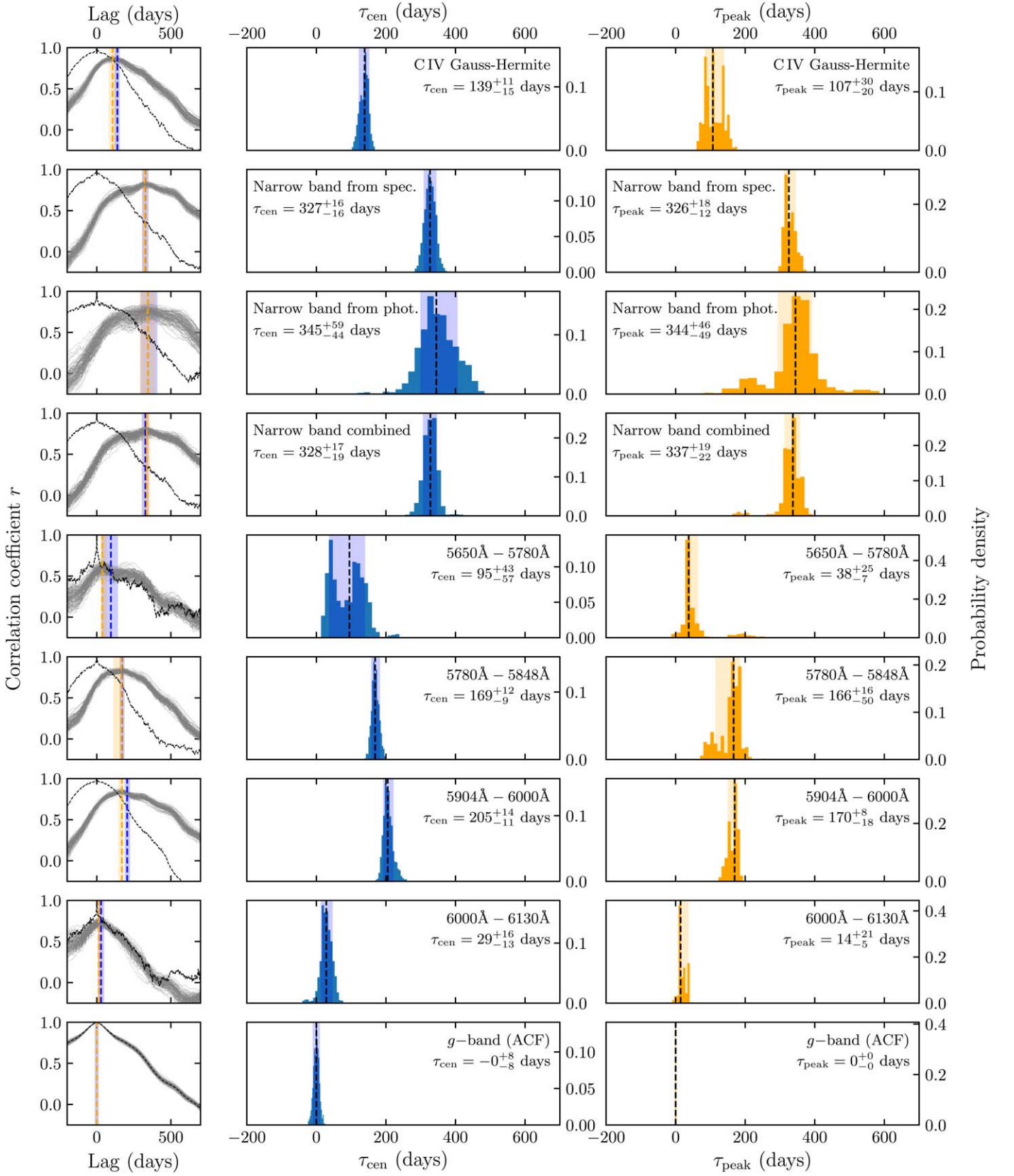


Figure 12. Left: distribution of ICCFs calculated using the FR/RSS method (gray). The vertical dashed blue and orange lines show the median τ_{cen} and τ_{peak} values, respectively, and the shaded regions show the 68% confidence intervals. The black dashed line is the autocorrelation function for comparison. Middle: distribution of τ_{cen} values. The medians and 68% confidence intervals are indicated by the vertical dashed lines and shaded regions. Right: same as the middle panel but for τ_{peak} . In the bottom panel, we show the g -band autocorrelation function. Note that all lags here are in the observed frame.

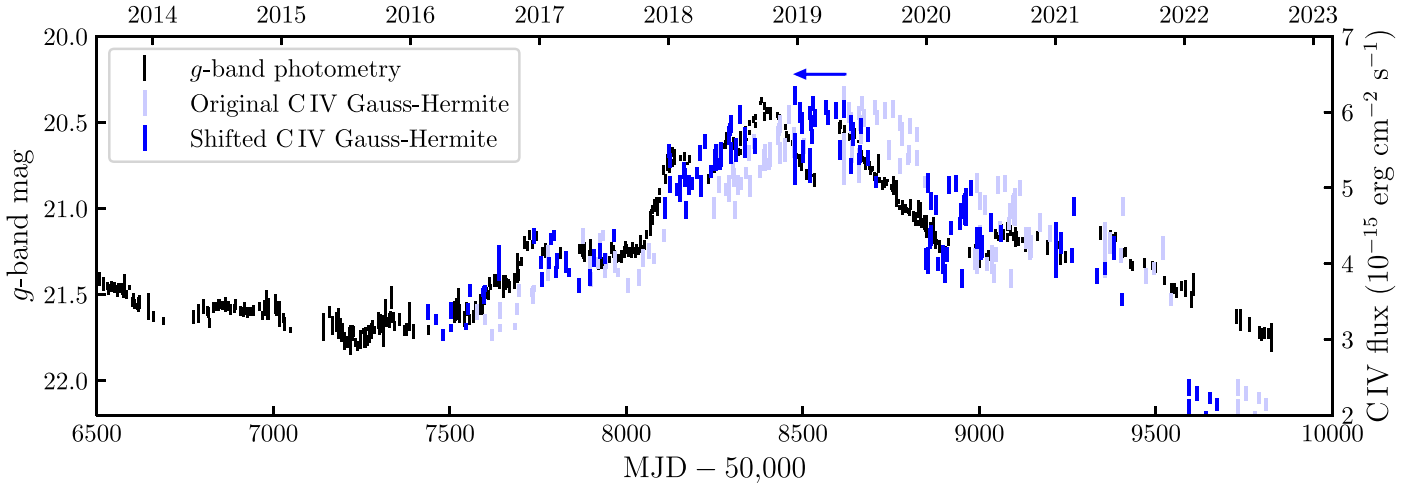


Figure 13. Light curves for the g -band photometry and C IV Gauss-Hermite component. The C IV light curve has been shifted by the measured time delay $\tau_{\text{cen}} = 139$ days (observed frame) to align with the g -band continuum light curve.

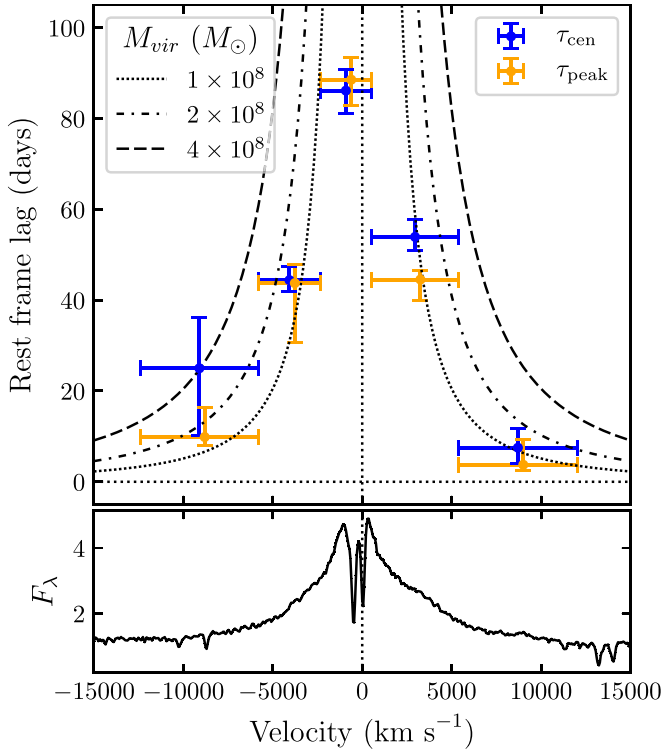


Figure 14. Top: rest-frame emission line lag measurements, τ_{cen} and τ_{peak} for the four wavelength windows and combined narrowband filter light curves (central bin). The x -axis error bars indicate the wavelength ranges of the windows, and the y -axis error bars are the 1σ uncertainties on the lag measurements. Since the middle bin uses the narrowband filter, we simply show the error bars extended to the edges of the neighboring windows. We shift the τ_{peak} measurements by $+300 \text{ km s}^{-1}$ for visibility purposes. Virial envelopes are overplotted for three choices of $M_{\text{vir}} = M_{\text{BH}}/f$. Bottom: mean quasar image A C IV profile. The y -axis units are $10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$.

the magnifications determined by Sharon et al. (2017) through lens modeling to measure the mean $\lambda L_{\lambda}(1350 \text{ \AA})$. Taking the average of the measurements for each quasar image, we find $\log_{10} [\lambda L_{\lambda}(1350 \text{ \AA}) / \text{erg s}^{-1}] = 44.66 \pm 0.18$. Next, we take the minimum and maximum luminosities reached over the duration of the campaign to find that the quasar ranged from $\log_{10} [\lambda L_{\lambda}(1350 \text{ \AA}) / \text{erg s}^{-1}] = 44.32$ to 45.10 . We show the results for τ_{cen} in Figure 15 along with previous measurements

Table 2
Rest-frame Emission Line Lags

Light Curve	τ_{cen} (days)	τ_{peak} (days)
C IV Gauss-Hermite	$36.5^{+2.9}_{-3.9}$	$28.1^{+8.0}_{-5.4}$
Narrowband from spec.	$85.9^{+4.2}_{-4.2}$	$85.5^{+4.6}_{-3.3}$
Narrowband from phot.	91^{+12}_{-12}	91^{+12}_{-13}
Narrowband combined	$86.2^{+4.5}_{-5.0}$	$88.6^{+4.9}_{-5.8}$
5650–5780 \AA ($-12,420$ to -5800 km s^{-1})	25^{+11}_{-15}	$9.9^{+6.6}_{-1.8}$
5780–5848 \AA (-5800 to -2340 km s^{-1})	$44.4^{+3.1}_{-2.4}$	$43.8^{+4.2}_{-13.2}$
5904–6000 \AA (510 – 5400 km s^{-1})	$53.9^{+3.7}_{-2.9}$	$44.5^{+2.0}_{-4.6}$
6000–6130 \AA (5400 – $12,020 \text{ km s}^{-1}$)	$7.5^{+4.2}_{-3.5}$	$3.7^{+5.5}_{-1.2}$

Note. Rest-frame emission line lags measured using cross-correlation analysis.

by Peterson et al. (2005, 2006; seven points), Kaspi et al. (2007; one point), Lira et al. (2018, 2020; six points), Hoormann et al. (2019; two points), and Grier et al. (2019; 16 points, “gold sample” only, ICCF lags). We omit two data points from Lira et al. (2018; CT250 and CT320), since either the median or 1σ uncertainties include negative lags. All luminosities shown here have been corrected for Galactic extinction, except those of Grier et al. (2019), and none have been corrected for extinction intrinsic to the AGNs’ host galaxies or along the lines of sight. The luminosities also have not been corrected for host galaxy starlight, although this contribution is expected to be minimal.

Using these data, we fit a linear regression of the form

$$\log_{10} \left(\frac{\tau_{\text{C IV}}}{\text{days}} \right) = \alpha + \beta \log_{10} \left[\frac{\lambda L_{\lambda}(1350 \text{ \AA})}{10^{44} \text{ erg s}^{-1}} \right] + \mathcal{N}(0, \epsilon^2), \quad (8)$$

where $\mathcal{N}(0, \epsilon^2)$ is a normal distribution with mean zero and variance ϵ^2 , and ϵ is the intrinsic scatter. We use the IDL routine `linmix_err` (Kelly 2007), which assumes Gaussian uncertainties, so we take the mean of the upper and lower uncertainties when they are not equal. Since the majority of

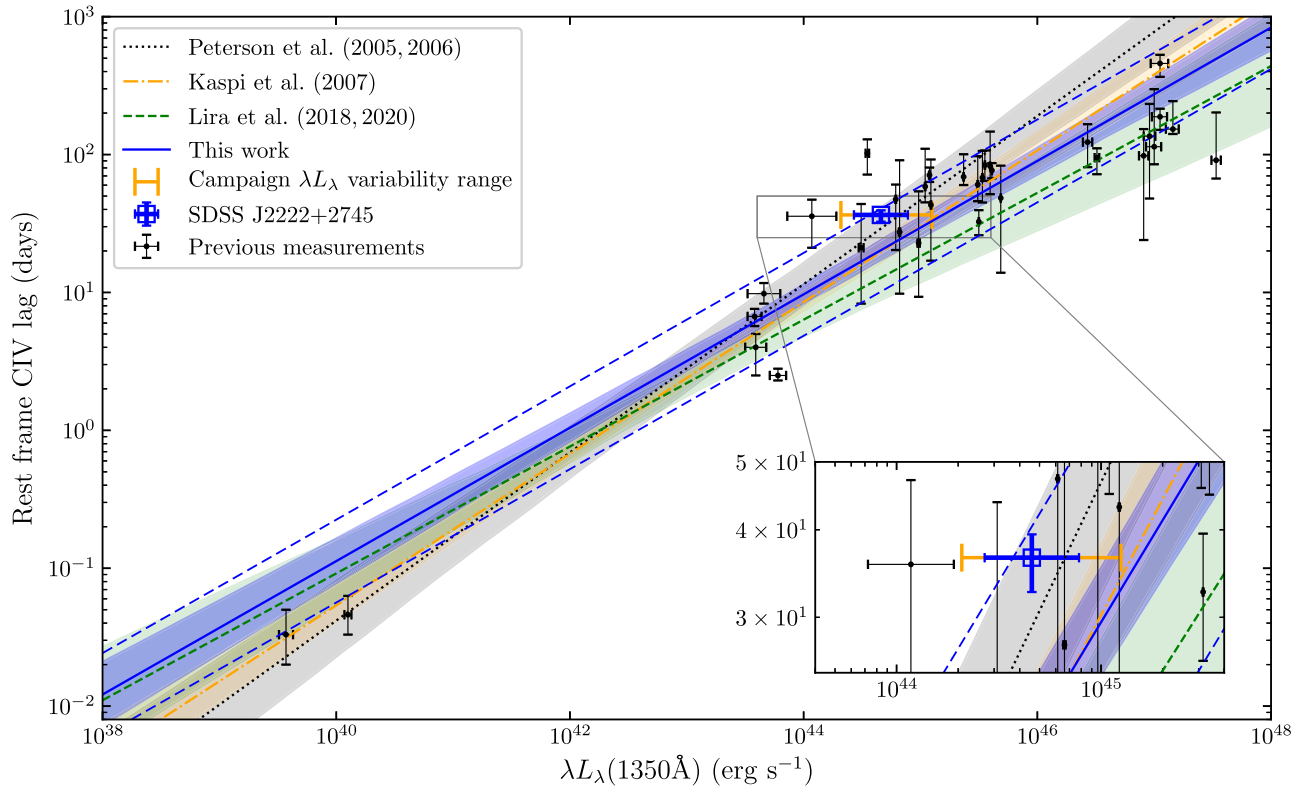


Figure 15. The C IV BLR radius–luminosity relation. Black points with error bars represent previous measurements in the literature, and the blue open square is SDSS J2222+2745. The orange bars show the range over which SDSS J2222+2745 fluctuated in $\lambda L_{\lambda}(1350 \text{ \AA})$ over the duration of the campaign. The four diagonal lines with shaded bands are the median and 68% confidence intervals of the fits to the $r_{\text{BLR}} - L$ relation presented by Peterson et al. (2005), Kaspi et al. (2007), Lira et al. (2018), and this work. The confidence interval bands are calculated by producing 1000 Monte Carlo line iterations based on the reported fits, assuming Gaussian uncertainties, and computing the 68% confidence interval at each λL_{λ} value. The dashed blue lines indicate the intrinsic scatter for the fit from this work and are offset by $\epsilon = 0.30$ dex from the best-fit line. We show a zoomed-in inset of the region around the SDSS J2222+2745 data point to show more detail.

the points available in the literature do not include campaign variability in the x -axis uncertainties, we do not take into account the campaign variability for SDSS J2222+2745 when performing the fits. We find a slope $\alpha = 0.99 \pm 0.07$, intercept $\beta = 0.48 \pm 0.03$, and intrinsic scatter $\epsilon = 0.30 \pm 0.06$. The fit is plotted in Figure 15 along with the three fits by Peterson et al. (2005), Kaspi et al. (2007), and Lira et al. (2018). We do not include the fits by Hoormann et al. (2019) and Grier et al. (2019), since they were calculated before the lag corrections were presented by Lira et al. (2020).

Correcting for reddening intrinsic to the AGNs or along the lines of sight will move the points to the right in Figure 15. Conversely, correcting for the host galaxy starlight will move the points to the left. These competing and unknown factors, combined with the fact that campaign variability is not included in most quoted λL_{λ} measurements, mean that the x -axis uncertainties in this figure are underestimated, and the uncertainty on the fitted relation is underestimated as well. The quasar SDSS J2222+2745 lies 0.26 dex above the mean $r_{\text{BLR}} - L$ relation, but this offset can be explained by the large intrinsic scatter, uncertainties in the fit, and large variability in λL_{λ} over the duration of the campaign.

We should note that the lag measurement for SDSS J2222+2745 is extremely well secured due to the combination of high quasar variability, high cadence monitoring, and high-S/N data. However, the fit to the $r - L$ relation is primarily driven by the sheer quantity of data points from large-scale campaigns such as that described by Grier et al. (2019), even with the

bigger uncertainties. While these types of campaigns are certainly beneficial, future fits to the $r - L$ relation would benefit greatly from more high-precision measurements covering a wider range in λL_{λ} . Of course, adding these data points will be a challenging task, given the complications of C IV-based reverberation mapping campaigns described in Section 1.

6.4. Black Hole Mass

To determine the black hole mass, we need to know the width of the broad C IV emission line and the scale factor f (Equation (1)). The emission line width is measured on either the mean or rms spectrum as the FWHM or line dispersion, defined by

$$\sigma_{\text{line}}^2 = \left(\frac{\sum_i \lambda_i^2 F_i}{\sum_i F_i} \right) - \lambda_0^2, \quad (9)$$

where

$$\lambda_0 = \frac{\sum_i \lambda_i F_i}{\sum_i F_i}. \quad (10)$$

Due to the strong absorption features in the core of C IV, estimating the peak in order to measure the FWHM is infeasible. Similarly, while the line dispersion does not depend on an estimate of the emission line peak, the absorption will significantly affect this measurement. Since neither measurement is possible on the data, we measure the emission line

Table 3
Emission Line Widths and Black Hole Mass Measurements

Image	Mean Spectrum		rms Spectrum	
	FWHM km s ⁻¹	σ_{line} km s ⁻¹	FWHM km s ⁻¹	σ_{line} km s ⁻¹
A	7925 ± 100	4499 ± 80	7705 ± 372	6100 ± 286
B	7555 ± 93	4209 ± 69	7848 ± 665	5477 ± 199
C	7700 ± 96	4018 ± 87	11,400 ± 860	5774 ± 202
Combined	7734 ± 59	4261 ± 49	9219 ± 458	5907 ± 148
$\log_{10}(M_{\text{vir}}/M_{\odot}) = \log_{10}(M_{\text{BH}}/M_{\odot}) - \log_{10}f$				
A	8.65 ± 0.04	8.16 ± 0.04	8.62 ± 0.06	8.42 ± 0.06
B	8.61 ± 0.04	8.10 ± 0.04	8.65 ± 0.09	8.33 ± 0.05
C	8.62 ± 0.04	8.06 ± 0.05	8.97 ± 0.08	8.37 ± 0.05
Combined	8.63 ± 0.04	8.11 ± 0.04	8.79 ± 0.06	8.40 ± 0.05
$\log_{10}(M_{\text{BH}}/M_{\odot})$				
A	9.37 ± 0.51	8.67 ± 0.26	...	9.05 ± 0.14
B	9.30 ± 0.51	8.63 ± 0.26	...	8.96 ± 0.13
C	9.32 ± 0.50	8.57 ± 0.27	...	9.00 ± 0.13
Combined	9.35 ± 0.51	8.63 ± 0.27	...	9.02 ± 0.13

Note. Emission line widths, virial product, and black hole mass measurements. We give the measurements for each of the individual quasar images, as well as the combined spectra. The f values used to calculate M_{BH} are $\log_{10}f_{\text{C IV};\text{rms},\sigma} = 0.63 \pm 0.12$, $\log_{10}f_{\text{C IV};\text{mean},\sigma} = 0.52 \pm 0.26$, and $\log_{10}f_{\text{C IV};\text{mean},\text{FWHM}} = 0.69 \pm 0.50$. We do not compute the value based on the FWHM and rms spectrum for the reasons described in Section 6.4.

widths using the Gauss–Hermite fits to the broad C IV emission.

To measure the emission line widths and estimate the uncertainties, we follow the Monte Carlo technique described by Peterson et al. (2004), modified to fit our data set and spectral decompositions. Given the N epochs in the data set, we randomly select N of these spectra, with replacement. From each, we randomly select one C IV Gauss–Hermite fit from the posterior sample of the spectral decomposition for that night. We then use this time series of spectra to compute the mean and rms spectra and calculate the two line width measures. We repeat this procedure for 1000 realizations and compute the mean and standard deviation of the distribution of measured line widths. We perform this procedure for each quasar image individually and with the combined data set, the results of which are reported in Table 3.

We pair the line width measurements with $\tau_{\text{cen}} = 36.5^{+2.9}_{-3.9}$ from Section 6.2 to determine the virial product, $M_{\text{vir}} = M_{\text{BH}}/f$, reported in Table 3. The correct conversion f between M_{vir} and M_{BH} depends on a number of factors, including the BLR geometry and kinematics, and will vary from one AGN to another. Since this information is generally not available, one typically chooses f such that the sample of reverberation-mapped AGNs is aligned with quiescent galaxies in the $M - \sigma_*$ plane. While numerous studies have calibrated f to the $M - \sigma_*$ relation using the H β BLR, we are not aware of any that have done so for the C IV BLR. Those that do calibrate C IV-based M_{BH} measurements do so using single-epoch methods with the $r_{\text{BLR}} - L$ relation (see, e.g., Park et al. 2017), but the virial factor f cannot be extracted from the fitted relations.

Since the geometry and kinematics of the two BLRs are not necessarily the same, and since H β and C IV emission line profiles tend to differ, the H β -based f values may not be the

same as those needed for C IV-based measurements. However, since M_{BH} for an AGN is fixed regardless of which emission line is used to calculate it, we can use the relationship between the virial products $M_{\text{vir},\text{H}\beta}$ and $M_{\text{vir},\text{C IV}}$ to convert between $\log_{10}f_{\text{H}\beta}$ and $\log_{10}f_{\text{C IV}}$ according to

$$\begin{aligned} \log_{10}f_{\text{C IV}} + \log_{10}(M_{\text{vir},\text{C IV}}/M_{\odot}) \\ = \log_{10}f_{\text{H}\beta} + \log_{10}(M_{\text{vir},\text{H}\beta}/M_{\odot}). \end{aligned} \quad (11)$$

Dalla Bontà et al. (2020) examined a sample of AGNs with M_{vir} available from both the C IV and H β emission lines and found that the two are consistent with each other when the line dispersion and mean spectrum are used. Given that we have multiple line width measurements, we use the data they present to compute the offset $\alpha = \log_{10}(M_{\text{vir},\text{H}\beta}/M_{\odot}) - \log_{10}(M_{\text{vir},\text{C IV}}/M_{\odot})$ for each pair of line width and spectrum so that $\log_{10}f_{\text{C IV}} = \log_{10}f_{\text{H}\beta} + \alpha$. We find $\alpha_{\text{mean},\sigma} = 0.087 \pm 0.007$, $\alpha_{\text{rms},\sigma} = -0.021 \pm 0.028$, and $\alpha_{\text{mean},\text{FWHM}} = 0.694 \pm 0.008$, skipping $\alpha_{\text{rms},\text{FWHM}}$, since Dalla Bontà et al. (2020) do not provide those measurements.

For the H β -based $f_{\text{rms},i}$ measurements, we use the values reported by Woo et al. (2015), found by aligning a sample of reverberation-mapped AGNs with the $M - \sigma_*$ relation for quiescent galaxies: $\log_{10}f_{\text{H}\beta;\text{rms},\sigma} = 0.65 \pm 0.12$ and $\log_{10}f_{\text{H}\beta;\text{rms},\text{FWHM}} = 0.05 \pm 0.12$. For $f_{\text{mean},i}$, we use the results of Williams et al. (2018), who examined a sample of 17 AGNs with BLR modeling: $\log_{10}f_{\text{H}\beta;\text{mean},\sigma} = 0.43 \pm 0.26$ and $\log_{10}f_{\text{H}\beta;\text{mean},\text{FWHM}} = 0.00 \pm 0.50$. Applying the offsets, we have $\log_{10}f_{\text{C IV};\text{rms},\sigma} = 0.63 \pm 0.12$, $\log_{10}f_{\text{C IV};\text{mean},\sigma} = 0.52 \pm 0.26$, and $\log_{10}f_{\text{C IV};\text{mean},\text{FWHM}} = 0.69 \pm 0.50$. We use these to compute the black hole masses reported in Table 3.

We caution that the masses reported here are highly dependent on f and the conversion between $f_{\text{H}\beta}$ and $f_{\text{C IV}}$. Further research is necessary to determine the appropriate f for more reliable calibration of C IV-based M_{BH} measurements. The correct value can be determined through alignment of C IV reverberation-mapped AGNs with the $M - \sigma_*$ relation or via direct modeling of the BLR, the latter of which will be the topic of a future paper with these data.

6.5. Correlated Variability of Observed Color and Luminosity

Since the light for the three quasar images passes through different parts of the lensing galaxy cluster, each image experiences a different amount of extinction. We can assess this by comparing the $g - i$ photometry for the three images on matching dates. First, we take the dates on which we obtained photometry and shift them by the measured lensing time delays. We then group the g - and i -band photometry by observing season and compute the median $g - i$ for each image. For the seasons in which data overlap, we compute the $g - i$ offsets between the images and then calculate the mean offset relative to image A to find $(g - i)_{\text{A}} - (g - i)_{\text{B}} = -0.059$ and $(g - i)_{\text{A}} - (g - i)_{\text{C}} = 0.059$. The $g - i$ light curves are shown in the first panel of Figure 16, where the crosses indicate the median $g - i$ for each image and observing season. In the second panel, we shift images B and C by the measured offsets to align with image A.

In the third and fourth panels, we show $g - i$ plotted against the g - and i -band photometry. Here the g - and i -band photometry for images B and C has been shifted according to the measured relative magnifications $\Delta m_{\text{A},\text{B}}$ and $\Delta m_{\text{A},\text{C}}$, and the i band has been adjusted according to the above measured $g - i$ offsets. There is a clear trend in which $g - i$ increases

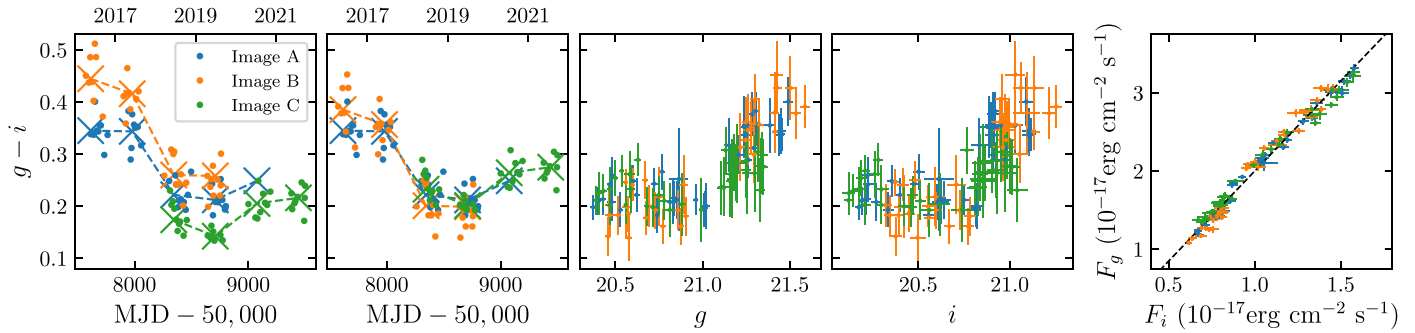


Figure 16. First panel: change in observed color over the duration of the observing campaign. The crosses mark the per-season mean $g - i$ for each image. Second panel: same as the first panel, but the three light curves have been corrected for differential extinction. Third and fourth panels: change in observed color vs. g - and i -band photometry. The i band has been corrected for differential extinction. Fifth panel: comparison of g - and i -band fluxes, scaled to match the image A flux level. A linear fit to the data is shown by the dashed black line.

with both g and i for $g > 21.0$ and $i > 20.5$. In the fifth panel, we show the g -band flux plotted against the i -band flux. The data are well fit by a straight line $F_g = (2.31 \pm 0.03)(F_i - 10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}) + (2.00 \pm 0.01) \times 10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}$. This indicates that the change in $g - i$ is not due to a change in the AGN power-law continuum slope but rather the effect of AGN variability over a constant contribution from the red host galaxy.

6.6. Systematic Offset in the Image B C IV Emission Line

The image magnifications reported by Dyrland (2019) are measured using the g -band continuum light curve. However, when plotting the emission line light curves using these magnifications, we find that the image B light curves lie systematically below the other two light curves. We attribute this effect to differential microlensing, which will affect the small-scale accretion disk but not the more extended BLR.

To quantify the effect, we use the narrowband C IV light curves from spectroscopy. First, we linearly interpolate the image B light curve onto the image A light-curve time values. We simply linearly interpolate the error bars, so we account for additional uncertainty in the interpolation by introducing a parameter δ , such that

$$\sigma_{B',\text{tot}}^2 = \sigma_{B'}^2 + (\delta B')^2, \quad (12)$$

where B' is the interpolated light curve, $\sigma_{B'}$ is the interpolated uncertainty, and $\sigma_{B',\text{tot}}^2$ is the total uncertainty on B' . We then maximize the log-likelihood

$$l(\alpha, \delta) = -\frac{1}{2} \sum_i \left[\frac{(A_i - \alpha B_i)^2}{\sigma_{\text{tot},i}^2(\delta)} - \ln(2\pi\sigma_{\text{tot},i}^2[\delta]) \right], \quad (13)$$

where $\sigma_{\text{tot},i}^2(\delta) = \sigma_{A,i}^2 + \sigma_{B',\text{tot},i}^2(\delta)$, and α is the scale factor required to bring B into alignment with A . Using the code EMCEE (Foreman-Mackey et al. 2013), we measure the median and 68% confidence intervals of the MCMC chains for the parameter α to find $\alpha = 1.179^{+0.010}_{-0.011}$, with $\log_{10} \delta = -3.0 \pm 0.2$. We repeat this same process again, instead interpolating the image A light curve onto the image B light curve, and find $\alpha = 1.181^{+0.011}_{-0.012}$, with $\log_{10} \delta = -2.8 \pm 0.2$. We then perform the same procedure using the continuum-subtracted narrowband photometry light curves to get $\alpha = 1.066^{+0.016}_{-0.016}$ and $\alpha = 1.069^{+0.017}_{-0.018}$, each with negligible δ .

These correction factors should match each other, since the two sets of light curves are measuring the same thing. There are two potential sources for the discrepancy: (1) if the photometry aperture and slit allow different amounts of AGN or host galaxy light through to the detector or (2) if the two continuum subtraction methods have a systematic offset. We do not expect point (1) to be the issue, since we use a large ($2''$) slit to avoid any slit losses. Examining the raw, continuum-unsubtracted spectra and photometry confirms that both narrowband measurements are closely aligned. It is more likely that point (2) is the issue, since the continuum estimate from photometry is based solely on the g - and i -band photometry. While the continuum estimates under C IV appear to be in good agreement with the g -band continuum light curve, we do not take these measurements to be as reliable as the spectra-based measurements due to the larger uncertainties involved.

We apply an $\alpha = 1.180$ correction to all emission line light curves for image B before computing the cross-correlation functions. We also perform tests in which we use $\alpha = 1.068$ for the narrowband photometry but find that the lag measurements are consistent to within the uncertainties.

7. Summary

We have presented the first results of a 4.5 yr spectroscopic and photometric monitoring campaign of the multiply imaged quasar SDSS J2222+2745 at $z = 2.805$. Our main results can be summarized as follows.

1. After performing percent-level spectrophotometric flux calibration, we produce emission line light curves spanning more than 6 yr in duration in the observed frame. We give light curves for the integrated C IV emission line, a narrowband filter covering the C IV core, and four wavelength ranges covering the blue and red wings of C IV.
2. We measure integrated and velocity-resolved C IV emission line lags with respect to the g -band continuum. The integrated C IV lag is $\tau_{\text{cen}} = 36.5^{+2.9}_{-3.9}$ days in the rest frame (139^{+11}_{-15} days observed frame). We see velocity-resolved lag structure in which the core of the line responds the slowest ($86.2^{+4.5}_{-5.0}$ days) and the wings respond the fastest (25^{+11}_{-15} and $7.5^{+4.2}_{-3.5}$ days for the blue and red wings, respectively). This behavior is consistent with BLR gas that is in circular Keplerian motion.

3. We place SDSS J2222+2745 on the $r_{\text{BLR}} - L$ relation with 33 data points from the literature and fit a linear regression to the data, finding $\log_{10}(\tau/\text{days}) = (0.99 \pm 0.07) + (0.48 \pm 0.03)\log_{10}[\lambda L_{\lambda}(1350 \text{ \AA})/10^{44} \text{ erg s}^{-1}]$ with an intrinsic scatter of 0.32 ± 0.06 dex. The quasar SDSS J2222+2745 lies 0.26 dex above the mean relation but is consistent with the relation when campaign variability, intrinsic scatter, and all sources of uncertainty are considered.
4. We calculate emission line widths and pair these with the measured lags to obtain the virial product, $M_{\text{vir}} = M_{\text{BH}}/f$, for the four combinations of the (mean, rms) spectrum and (FWHM, σ_{line}) emission line widths. Assuming values of f based on $H\beta$, we compute the black hole mass for each combination.

Future analyses with these data will include measurements of the broad C III] $\lambda 1908.7$ emission line. We aim to extend this campaign through the end of 2022 for a full campaign duration of 6.5 yr (8.5 yr with gravitational time delays), which will provide the data for more detailed analyses of the geometry and kinematics of the C IV and C III] BLRs and an absolute calibration of the f factor and the inferred black hole mass.

The data presented here are based in part on observations obtained at the international Gemini Observatory, a program of NSF's NOIRLab, which is managed by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation on behalf of the Gemini Observatory partnership: the National Science Foundation (United States), National Research Council (Canada), Agencia Nacional de Investigación y Desarrollo (Chile), Ministerio de Ciencia, Tecnología e Innovación (Argentina), Ministério da Ciência, Tecnologia, Inovações e Comunicações (Brazil), and Korea Astronomy and Space Science Institute (Republic of Korea). The Gemini data were obtained from programs GN-2016B-Q-28, GN-2017A-FT-9, GN-2017B-Q-33, GN-2018A-Q-103, GN-2018B-Q-143, GN-2019A-Q-203, GN-2019B-Q-232, GN-2020A-Q-105, and GN-2020B-Q-132 (PI: Treu) and processed using the Gemini IRAF package.

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This research made use of Astropy,¹⁶ a community-developed core Python package for astronomy (Astropy Collaboration et al. 2013, 2018).

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¹⁶ <http://www.astropy.org>

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