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Isolation and characterization of a covalent Ce^{IV}-Aryl complex with an anomalous ¹³C chemical shift

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The synthesis of bona fide organometallic Ce^{IV} complexes is a formidable challenge given the typically oxidizing properties of the Ce^{IV} cation and reducing tendencies of carbanions. Herein, we report a pair of compounds comprising a Ce^{IV} – C_{aryl} bond [Li(THF)₄][Ce^{IV}(κ^2 -ortho-oxa) (MBP)₂] (**3-THF**) and [Li(DME)₃][Ce^{IV}(κ^2 -ortho-oxa)(MBP)₂] (**3-DME**), ortho-oxa = dihydro-dimethyl-2-[4-(trifluoromethyl)phenyl]-oxazolide, MBP²⁻ = 2,2'-methylenebis(6-tert-butyl-4-methylphenolate), which exhibit Ce^{IV} – C_{aryl} bond lengths of 2.571(7) – 2.5806(19) Å and strongly-deshielded, Ce^{IV} – C_{ipso} ¹³C{¹H} NMR resonances at 255.6 ppm. Computational analyses reveal the Ce contribution to the Ce^{IV} – C_{aryl} bond of **3-THF** is ~12%, indicating appreciable metal-ligand covalency. Computations also reproduce the characteristic ¹³C{¹H} resonance, and show a strong influence from spin-orbit coupling (SOC) effects on the chemical shift. The results demonstrate that SOC-driven deshielding is present for Ce^{IV} – C_{ipso} ¹³C{¹H} resonances and not just for diamagnetic actinide compounds.

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he bonding between lanthanides and ligands has been described as purely ionic^{1,2}. However, modern spectroscopic and computational techniques have challenged this simple assumption³⁻⁶. The covalency in M-X interactions can result in anomalous and diagnostic nuclear magnetic resonance shifts, $X = {}^{13}C$, ${}^{15}N$, ${}^{19}F$, ${}^{77}Se$, ${}^{125}Te$, resulting from participation of f-element orbital angular momentum⁷⁻¹³. Another important aspect of detailed f-element electronic structure is multiconfigurational character, as described in the model example of cerocene, $Ce(COT)_2$, COT = cyclooctatetraene ligand 14. The case for multiconfigurational character in cerocene has been made through X-ray absorption, SQUID magnetometry, and multireference computational studies and tied strongly to the characteristics of the cerium-carbon bonding¹⁵. Despite the interest surrounding f-element covalency and multiconfigurational effects, there are few examples of organometallic Ce^{IV} complexes¹⁶. The current literature is limited to metallocene Ce^{IV} complexes or α -heteroatom stabilized $Ce^{IV}-C$ σ -bonds. Reported examples of Ce^{IV} – metallocene bonding include Ce^{IV} complexes of cyclopentadienide, cyclooctatetraene dianion, and bispentalene dianion ligands $^{17-21}$. Complexes containing a Ce^{IV} – C σ -bond, however, are limited to either an N-heterocyclic carbene (NHC) complexes, e.g., Ce[L₄] (Fig. 1a), or a bis(iminophosphorano)methandiide complex, e.g., [Ce(BIPM^{TMS})(ODipp)₂] (Fig. 1a)^{22,23}. The latter examples are expected to have electronic structures that deviate significantly from typical organometallic alkyl, aryl, or alkynyl ligands due to the heteroatom αsubstitution $^{22-25}$. The scarcity of $Ce^{IV} - C$ containing-complexes likely arises from the unstable combination of strongly reducing carbanions and the oxidizing Ce^{IV} cation¹⁶. As a result, the formation of reactive, carbon-centered radicals and Ce^{III} species is observed. Our team has a long-standing interest in the isolation of redox stable Ce^{IV} species to elucidate the relationship between ligand field and the Ce^{III}/Ce^{IV} couple^{26–28}.

Herein, we expand our studies for the isolation of a pair of $Ce^{IV}-C_{aryl}$ compounds. These compounds display unusually high ^{13}C NMR shifts compared to other diamagnetic $M^{IV}-C_{aryl}$ compounds. Relativistic density functional calculations verify that the high NMR shifts are due to large SOC effects supported by the increased covalency of the $Ce^{IV}-C_{aryl}$ bond.

Results

Synthesis and structures of $Ce^{IV}-C_{aryl}$. Considering strategies to stabilize a $Ce^{IV}-C_{aryl}$ bond, we hypothesized that tethering

the aryl group to the Ce center would kinetically inhibit homolysis of the Ce - C bond. In addition, we sought a stericallyprotected Ce center to prevent reactivity at the ipso-carbon. Lastly, we chose a supporting ligand that would stabilize the Ce^{IV} oxidation state to prevent charge transfer and subsequent Ce - Cbond homolysis. With these considerations in mind, we aimed to prepare a $Ce^{IV} - C_{aryl}$ bond from the Ce^{IV} bis(methylene bisphenolate) complex $Ce(THF)_2(MBP)_2$, that was previously synthesized by members of the Schelter laboratory $(1, \text{ Fig. 2})^{29}$. Arvloxide ligands have been previously shown to both stabilize the Ce^{IV} oxidation state and high valent organometallic species of other metal species^{28–34}. Addition of a vellow solution of ortholithiated oxazoline 2 (Li-ortho-oxa) to a purple benzene solution of Ce(THF)₂(MBP)₂ (1) at room temperature resulted in an immediate color change of the solution to dark red. The ¹H NMR spectrum of the reaction mixture revealed loss of the pseudo C_{2v} symmetry of 1 and formation of a C₁ symmetric product. Likewise, there was also a shift in both the ⁷Li and ¹⁹F NMR resonances of 2, and the two methylene protons and methyl groups of the oxazoline were no longer degenerate in the ¹H NMR spectrum. All ¹H, ⁷Li, and ¹⁹F NMR resonances were well within the range of diamagnetic signals, leading to the assignment of the product of the reaction as $[Li(THF)_4][Ce(\kappa^2-ortho-oxa)(MBP)_2]$ (3-THF). Dark red X-ray quality crystals of 3-THF were grown over 3 days from a cooled $(-25 \, ^{\circ}\text{C})$ mixture of 3-THF in toluene and THF layered with pentane. The crystals were collected in 66% yield (Fig. 2). Alternatively, crystallizing from a cooled $(-25 \, ^{\circ}\text{C})$ solution of crude 3-THF in DME layered with pentane resulted in dark-red X-ray quality crystals of 3-DME over 3 days (Fig. 3). Crystals of 3-DME were collected in a slightly higher 75% yield. The differences in NMR data between 3-THF and 3-DME are negligible compared to experimental error. While compound 3-DME crystallizes with a single molecule in the asymmetric unit, compound 3-THF crystallizes with two independent molecules in the asymmetric unit, with only minor differences between the structures. The Ce - O(phenoxide) bond distances of 3-THF and **3-DME** (2.1636(13)-2.202(4) Å) compare well with the Ce – O (phenoxide) bond distances observed in the reported structure of $1 (2.113(2)-2.152(2) \text{ Å})^{29}$. The Ce – C bond distances of 3-THF and 3-DME are 2.571(7) - 2.5806(19) Å and are shorter than reported $Ce^{III} - C_{aryl}$ bond lengths: $2.621(4) - 2.64 \pm 0.02 \text{ Å}^{35,36}$. The difference in ionic radii between 6-coordinate Ce^{III} and Ce^{IV} is 0.14 Å; however, the difference between 3-THF and 3-DME and previous $Ce^{III}-C_{aryl}$ complexes is only 0.04 - 0.07 Å³⁷.

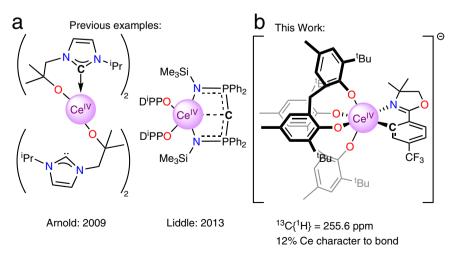


Fig. 1 Examples of $Ce^{IV} - C \sigma$ bonds. a Previous examples of complexes with formally $Ce^{IV} - C \sigma$ bonds, which are stabilized by either nitrogen²² or phosphorus heteroatoms²³. b This work detailing the synthesis and characterization of a $Ce^{IV} - C_{aryl}$ bond, including computational analysis. Carbon atoms bound to cerium are indicated with a $\bf C$.

Fig. 2 Syntheses of title Ce^{IV} – C_{aryl} compounds 3-THF and 3-DME. The complex 1 was treated with the isolable aryl lithium 2 to generate the title complexes 3-THF or 3-DME.

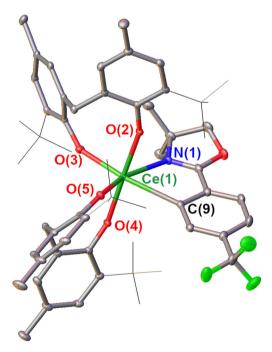


Fig. 3 Crystal structure of 3-DME. Thermal ellipsoid plot of the X-ray crystal structure of **3-DME** at the 30% probability level. For clarity, C-H hydrogens and the Li(DME)₃+ cation were removed; In addition *tert*-butyl groups are displayed in wireframe. Selected bond lengths in Å: Ce(1)–C(9): 2.5806(19); Ce(1)–N(1): 2.6176(16); Ce(1)–O(2): 2.1750(12); Ce(1)–O(3): 2.2062(13); Ce(1)–O(4): 2.1640(12); Ce(1)–O(5): 2.1636(13).

We ascribe this difference to the steric demand by the MTB ligands vs. the pentamethylcyclopentadienyl ligands used in the prior work. Previously reported complexes containing $Ce^{IV}-C\sigma$ -bonds are 2.652(7) – 2.705(2) Å and 2.385(2) – 2.441(5) Å for the Ce-C NHC and Ce-C(bis(iminophosphorano)methandiide) ligands, respectively 22,23,25 . With this data in hand, we assign this complex as a $Ce^{IV}-C_{aryl}$ complex.

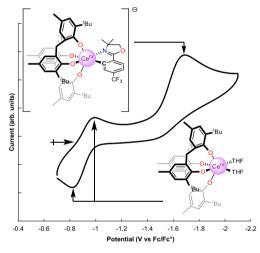


Fig. 4 Cyclic voltammagram of 3-THF. Solvent: THF; electrolyte 0.1 M [${}^{n}Pr_{4}N$][BAr ${}^{F}_{4}$]; [analyte] = 0.001 M; OCP = -0.815 V vs. Fc/Fc ${}^{+}$, noted by the right-facing arrow; $\nu = 100$ mV s ${}^{-1}$. The trace shows the reduction of **3** at $E_{pc} = -1.67$ V vs. Fc/Fc ${}^{+}$ with a return wave at $E_{1/2} = -0.94$ V vs. Fc/Fc ${}^{+}$, which is the Ce^{III}/Ce^{IV} couple of **1**²⁹. The waves corresponding to **1** do not appear in the first scan (Supplementary Figs. 18–19).

Electrochemical analysis. To better understand how the *ortho*-oxa⁻ group impacts the stability of the Ce^{IV} cation, electrochemistry was performed on **3-THF**. The $E_{\rm pa}$ of **3-THF**, -1.67 V vs. Fc/Fc⁺, shifts by -0.72 V relative to the $E_{1/2}$ of **1** (-0.94 V vs. Fc/Fc⁺), indicating that the *ortho*-oxa⁻ moiety significantly stabilizes the Ce^{IV} couple in THF. The reduction of **3-THF** is not reversible under the electrochemical conditions, although the event precedes a reversible oxidation at $E_{1/2} = -0.94$ V vs. Fc/Fc⁺ and an irreversible oxidation at $E_{\rm pa} = -0.43$ V (Supplementary Figs. 18–19). We postulate that the reduction of the Ce^{IV} center is followed by dissociation of the *ortho*-oxa⁻ fragment, producing **1** and **2**. Indeed, the return anodic scan comprises waves at $E_{1/2} = -0.94$ V vs. Fc/Fc⁺ and $E_{\rm pa} = -0.43$ V respectively, consistent with the previous assignment for compound **1** and inferred for compound **2** (Fig. 4)²⁹.

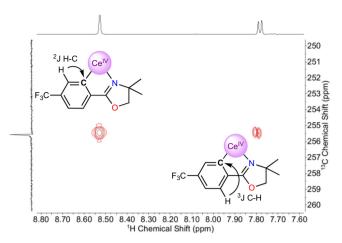


Fig. 5 Identification of the unusual ¹³**C resonance.** A portion of the HMBC spectrum showing the long-range C-H coupling to the ¹³C resonance at 255.6 ppm. An interpretation of the spectrum is inlaid, indicating that the signal at 255.6 ppm corresponds to the *ipso*-carbon.

¹³C NMR analysis. While the ¹H, ⁷Li, and ¹⁹F NMR of 3-THF and 3-DME showed minimal changes compared to the starting materials, the ¹³C{¹H} NMR of the *ipso*-carbon of both **3-THF** and 3-DME showed a significant shift (difference between 3-THF and **3-DME** is less than >0.05 ppm which is within error). Indeed, the *ipso*-¹³C{¹H} resonance was located at 255.6 ppm, well outside of the typical range for aryl resonances (100-170 ppm) and shifted by ~50 ppm downfield relative to the Li - C_{aryl} resonance for the starting material, 2 (Fig. 5). This ¹³C{¹H} shift is further downfield than observed for other characterized, diamagnetic MIV - Carvl interactions; the highest being $Th(2-C_6H_4CH_2NMe_2)_4$, which exhibits a $Th^{IV} - C$ ¹³ $C\{^1H\}$ signal at 230.8 ppm^{38,39}. The shift of the ¹³C{¹H} signal for the carbon atom bound to metal cations has been implicated as a reporter for the degree of covalency in felement cation-carbon bonds⁷⁻⁹. In this light, 3-THF and 3-DME have an anomalously high covalency for a M^{IV}-aryl interaction. As with the bond distance metrics, there are few salient examples of $Ce^{IV} - C \sigma$ -bonds for comparison of the ¹³C{¹H} NMR shifts. The compounds isolated by P. Arnold and co-workers display a 13C $\{^{1}H\}$ shift at ~213 ppm for the Ce^{IV}-NHC²². The compounds reported by Liddle contain Ce^{IV} – C (bis(iminophosphorano) methandiide) ¹³C{¹H} shifts in the range of 324.6-343.5 ppm, depending on the secondary ligands bound to the Ce^{IV} cation; [Ce $(BIPM^{TMS})(ODipp)_2$ exhibits a $^{13}C\{^1H\}$ shift of 324.6 ppm 23,25 . Notably, these compounds contain substantially different substituents attached to the Ce-C carbon, diminishing the significance of their comparison.

Computational bonding analysis. To further understand the nature of the $Ce^{IV} - C_{aryl}$ interaction, we turned to computations to assess the electronic structure of the anionic, cerium-containing portion of 3-THF (referred to as 3). The geometry of 3 was optimized starting from the structure of 3-THF determined by Xray crystallography, using density functional theory (DFT) with the B3LYP functional, all-electron Slater-type basis sets for all atoms, and other standard settings as detailed in the SI. The agreement between experiment and theory was excellent, with only minor differences in the Ce^{IV} - ligand bond lengths (≤0.02 Å). The MOs with the most Ce 4f character remain largely metal-centered and span the seven lowest unoccupied molecular orbitals (LUMO to LUMO + 6, Supplementary Figs. 13–19) of the complex, a common feature for CeIV compounds as well as for cerium species with a debated Ce^{IV}/Ce^{III} oxidation state^{3,15}. HOMO to HOMO -3 (Supplementary Figs. 26-29), for 3

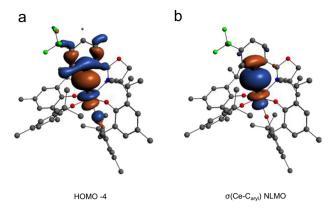


Fig. 6 MO's of 3 depicting the Ce-C_{aryl} **bond. a** The DFT/B3LYP frontier Kohn-Sham molecular orbital of **3** (HOMO - 4). **b** The two-center two-electron bonding NLMO. Atomic orbital contributions of the NLMOs and other bond properties of all the Ce containing bonds are listed in Table 1.

Table 1 NLM	ble 1 NLMO compositions and bond orders for 3.								
Bond/NLMO	%Ce (%s; %d; %f)	WBO ^[a]	MBO ^[b]	DI ^{QTAIM[c]}					
σ(Ce-C)	12 (5; 32; 62)	0.41	0.46	0.50					
σ(Ce-N)	4 (14; 49; 37)	0.15	0.11	0.25					
σ(Ce-O) ^[d]	3 (14; 50; 37)	0.41	0.46	0.62					
2xπ(Ce-O) ^[d]	4 (1; 38; 61)								

^aWiberg bond order in the natural atomic orbital (NAO) basis.

^bMayer-Mulliken bond order.

^cDelocalization index based on QTAIM Bader analysis.

dThe data are given as averages over the four Ce-O bonds.

are mostly delocalized phenoxide-centered orbitals, while HOMO-4 (Fig. 6) corresponds to the highest occupied orbital showing significant ligand-metal (Ce $^{\rm IV}-C_{\rm aryl}$) hybridization.

The metal-ligand bonding in 3 is characterized in Fig. 6 and Table 1 in terms of natural localized molecular orbitals (NLMOs) and bond orders. There are two two-center two-electron σ bonds describing the donation bonding between the aryl carbon and oxazolinide nitrogen and Ce, and $\sigma + 2\pi$ bonds describing the bonding between each of the O atoms and Ce (Supplementary Figs. 37–40). Among these, the $Ce^{IV}-C_{aryl}\ \sigma$ bond shown in Fig. 6 has the largest covalency, in terms of shared density, with 12% Ce contribution of which 32/62% involve 5d/4f. Previously reported $Ce^{IV} - C$ bonds contain 8–13% Ce contribution²⁵. Ce tends to be less covalent than U^{VI} (U^{VI} – C bonds 22–29% U) but similar to Th^{IV} (Th^{IV} – C_{aryl} bonds 10–15%)^{9,25,38,40}. In the remaining σ and π bonds with the N and O atoms, Ce contributes about 3-4% weight, suggesting that these bonds are mainly ionic. The bond ionicities are also reflected in the bond orders compiled in Table 1, all being significantly smaller than one (which would indicate a full single bond). In the sum of all interactions, however, Ce receives sizable electron donation from the surrounding ligands. For instance, the calculated Ce charge is +2.26 (Mulliken charge), +2.46 (Bader charge), and +2.44 (natural charge from a natural bond orbital (NBO) analysis) instead of the formal +4. The Ce natural electron configuration retrieved from the NBO analysis is 4f^{0.76}d^{0.60}, which deviates considerably from the formal 4f 05d0. The large Ce 4f electron count of 3 (0.76), associated mainly with the sizable $Ce - C_{aryl}$ bonding, is comparable to the calculated and experimentallydetermined Ce 4f electron counts in CeO_2 and $Ce(C_8H_8)_2^{41-43}$. We anticipate that this similarity has important implications

NLMO ^b	$\sigma_{\rm iso}{}^{\rm SR}$, SR-ZORA			$\sigma_{iso}{}^{SO}$, SO-ZORA			$_{\Delta}$ SO d		
	Lc	NLc	$\mathbf{L} + \mathbf{NL}$	L	NL	$\mathbf{L} + \mathbf{NL}$	L	NL	$\mathbf{L} + \mathbf{NL}$
$\sigma(\text{Ce-C}_{\text{aryl}})$	-103	2	-102	–156	2	-154	-52	0	-52
$\Sigma \sigma(C_{aryl}-C_{1,2})$	-106	-5	-110	-94	-5	-99	12	-1	11
1s _{core} (C _{aryl})	201	0	201	202	0	202	1	0	1
$\Sigma_{ m other}$	-26	11	–15	-25	11	-14	1	0	1
Σ (all of above)	-34	8	-26	-73	8	-65	-38	-1	-39 ^e

^aDFT/PBEh-40 calculations. SR = scalar relativistic. SO = relativistic calculation including SOC. All shielding contributions are in ppm. The geometry orientation is such that the ¹³C corresponds to the origin of the cartesian axes and C-Ce bond aligns with the z-axis

regarding the electronic structure of 3, in the sense that it may potentially exhibit a multi-configurational ground-state wavefunction with Ce^{III/IV} character, similar to cerocene. However, further spectroscopic studies are needed, and are under way, to confirm this assignment for 3.

Computational chemical shift analysis. Computed ¹³C NMR chemical shifts for the *ipso*-carbon, with various approaches, are compiled in Supplementary Table 2. The NMR shift was sensitive to the applied DFT approximations, a common observation in NMR shift calculations for compounds containing lanthanides and actinides. The best agreement with the experiment (256 ppm) for the ipso-13C chemical shift in 3 was obtained with a PBE hybrid with 40% exact exchange, PBEh-40, which gave 259 ppm. The same functional previously provided excellent ligand chemical shifts in actinide complexes 40,44. PBEh-40 produced a similar cerium electronic structure (Mulliken/natural charge of +2.43/ +2.66, $4f^{0.58}5d^{0.59}$ NBO natural electron configuration, $Ce-C_{aryl}$ WBO of 0.37) as B3LYP. Reasonable agreement with the experimental chemical shift was obtained also with the KT2 functional (265 ppm), which is known to perform well in NMR calculations⁴⁵. The comparison between the ipso-¹³C chemical shift calculated without and with SOC, with PBEh-40/KT2, reveals a 40/51 ppm downfield shift caused by SOC, which is largely triggered by the Ce 4f and 5d involvement in the $Ce^{IV} - C_{aryl} \sigma$ bond.

In order to rationalize the anomalous ¹³C shift, we carried out an analysis of the DFT/PBEh-40 13 C isotropic shielding (σ_{iso}) in terms of NLMOs46,47. The NMR shielding data are gathered in Table 2 and the relevant NLMOs are shown in Supplementary Fig. 41. Note that these NLMOs are equivalent to those obtained with DFT/B3LYP. The analysis shows that the $\sigma(\text{Ce} - \text{C}_{\text{arvl}})$ covalent bond is the principal cause of the SOC-induced deshielding of the ipso-carbon. According to Table 2, the core orbital of the Ce-bound Carvl brings a diamagnetic contribution of roughly 200 ppm to σ_{iso} . This value is counterbalanced by two large, negative shielding contributions generated by the σ bonds involving the *ipso*-carbon, namely the $\sigma(\text{Ce} - \text{C}_{\text{arvl}})$ bond and the two $\sigma(C_{arvl} - C)$ bonds involving the two neighboring carbons of the aryl ring, denoted as C_1 and C_2 . From Table 2 it is evident that the $\sigma(Ce-C_{aryl})$ contribution to σ_{iso} is as important (without SOC) or even more important (with SOC) than the combined σ_{iso}

contributions generated by the $\sigma(C_{aryl}-C)$ NLMOs. Indeed, with SOC in particular, the $\sigma(Ce-C_{aryl})$ NLMO yields a dominant negative contribution to σ_{iso} of -154 ppm, of which -169 ppm is paramagnetic and 15 ppm is diamagnetic (not shown separately in Table 2), while the combined σ_{iso} contribution from the $\sigma(C_{arvl} - C_{1,2})$ NLMOs is -99 ppm. The overall SOC effects on the total isotropic shielding, σ_{iso} , add up to -39ppm. The largest contribution to this value is generated by the σ

(Ce - Carvl) NLMO, -52 ppm, and there are secondary contributions from the $\sigma(C_{aryl} - C_{1,2})$ NLMOs, 11 ppm (Table 2, last column), indicating that these orbitals are somewhat delocalized onto the metal. Hence, the covalent bonding between the Ce center and Carvl is the main contributor of the 13C SOC deshielding and this aspect is strongly related to the sizable Ce 4f and 5d character of the $\sigma(\text{Ce}-\text{C}_{\text{aryl}})$ NLMO: 53% f and 41% d with PBEh-40, or 62% f and 32% d with B3LYP, with the 4f likely generating most of the SOC deshielding.

Discussion

We have synthesized, characterized, and crystallized complexes featuring a $Ce^{IV} - C_{arvl}$ bond. The synthesis of the title complexes 3-THF and 3-DME was realized from the reaction of the lithiumaryl salt 2 with 1. Electrochemical analysis revealed that the aryl interaction resulted in a notable stabilization of the CeIV oxidation state, shifting the $E_{\rm pc}$ of Ce^{IV} reduction by 720 mV relative to the THF adduct. A combination of $^{13}C\{^{1}H\}$ NMR and DFT was used to investigate the covalency of the $Ce^{IV}-C_{aryl}$ bonding. ^{13}C {1H} NMR analysis revealed that the ipso-carbon was shifted to 255.6 ppm, an indicator of metal-ligand covalency in the Ce^{IV} – Carvl bond. This result was supported by NLMO analysis, which showed a 12% metal contribution to the $Ce^{IV} - C_{arvl}$ bond. We expect that these results will further inform fundamental bonding in high valent f-elements and be effective in guiding the preparation of other f-element organometallic complexes.

Methods

General considerations. See Supplementary Methods for further details.

Ce(THF)₂(MBP)₂ (1). We previously reported a synthesis of 1 that could not be separated from the lithium halide byproducts²⁹. This revised method provides clean 1. In an N₂ filled drybox, to a clear, colorless solution of H₂MBP (0.270 g, 0.793 mmol, 2 equiv) in 4 mL of THF in a 20 mL scintillation vial with a Teflon coated stir bar, was added a yellow solution of Ce(OtBu)4(THF)2 (0.200 g, 0.396 mmol, 1 equiv) in a 6 mL solution of 2:1 THF:benzene at room temperature with stirring. The reaction immediately turned an intense purple color and was stirred for 1 h. The volatile materials were removed under reduced pressure, the residue was triturated with 2 mL of benzene to liberate the tert-butanol byproduct, and the volatile materials were again removed under reduced pressure. The resulting purple solid was transferred onto a medium porosity fritted filter and washed with 5×2 mL of pentane. The purple solid was dried under reduced pressure for 3 h. Yield: 0.311 g, 0.324 mmol, 82%.

NMR data for this complex was not previously reported and is provided here: ¹H NMR (400 MHz, THF- d_8) δ: 7.15 (s, 4H), 6.79 (s, 4H), 5.01 (d, J = 13.4 Hz, 2H) 3.51 (d, *J* = 14.0 Hz, 2H), 2.31 (s, 12 H), 1.44 (s, 36 H).

 $^{13}\text{C}\{^{1}\text{H}\}$ NMR (100 MHz, THF- $d_{8})$ δ : 168.12, 137.25, 134.45, 129.13, 128.17, 124.12, 35.40, 34.99, 31.15, 20.93.

The quantity of THF present for 1 was verified by ¹H-NMR in C₆D₆.

[Li(THF)][ortho-oxa] (2). Synthesis adapted from similar compounds⁴⁸. In a N₂ filled drybox, a solution containing H-ortho-oxa (1.217 g, 5.0 mmol, 1 equiv) and 10 mL of hexanes in a 20 mL scintillation vial with a Teflon coated stir bar was

^bThe NLMOs are shown in Supplementary Fig. 41.

[°]L and NL indicate contributions from the Lewis and non-Lewis parts of the NLMO. dDefined as $\sigma_{\rm iso}^{\rm SO}-\sigma_{\rm iso}^{\rm SR}$.

 $^{^{6}}$ SOC effects of +1/-39 ppm on the reference/probe shielding cause the +40 ppm SOC change in the chemical shift quoted in the text.

placed in a $-30\,^{\circ}\text{C}$ freezer for 30 mins. The vial was removed from the freezer and, while stirring, a solution of n-butyl lithium (2.5 M, 5 mmol, 2 mL) was added dropwise over 5 min. The solution turned from colorless to yellow to brown and a yellow solid precipitated. The reaction mixture was stirred for 50 min at room temperature, after which the solid was collected by filtration over a coarse-porosity fritted-filter and subsequently washed with $3\times2\,\text{mL}$ of hexanes and $1\times2\,\text{mL}$ of pentane. The tan solid was then dried under reduced pressure for 2 h. The solid was then dissolved in minimal THF at rt and then placed in a $-30\,^{\circ}\text{C}$ freezer overnight. Yellow crystalline blocks formed and were collected over a coarse-porosity fritted-filter and washed with $3\times2\,\text{mL}$ of pentane. The yellow blocks were dried for 2 h under reduced pressure. Yield: $0.831\,\text{g}$, $2.59\,\text{mmol}$, 52%.

 1 H NMR (400 MHz, THF- d_{8}) δ: 8.28 (s, 1H), 7.57 (d, J = 8.0 Hz, 1H), 7.07 (dd, J = 8.0, 2.7 Hz, 1H), 4.17 (s, 2H), 1.34 (s, 6H).

 $^{13}\text{C}^{\{1\text{H}\}}$ NMR (101 MHz, THF- d_8) &: 203.98, 172.88, 143.18 (q, J=2.2 Hz), 137.45 (q, J=3.3 Hz), 127.47 (q, J=274.1 Hz), 127.31 (q, J=28.2 Hz), 124.46, 119.28 (q, J=4.0 Hz), 80.39, 66.58, 29.03.

 $^{19}\mathrm{F}$ NMR (376 MHz, THF- $d_8)$ δ : –64.29

⁷Li NMR (156 MHz, THF- d_8) δ: 2.08

Anal. Cal. for $C_{12}H_{11}F_3LiNO\bullet(C_4H_8O)_{0.5}$: C, 58.96; H, 5.30; N, 4.91. Found C, 59.41; H, 5.41; N, 4.75.

The quantity of THF present for 2 was verified by ¹H-NMR in C₆D₆.

[Li(THF)₄][Ce(ortho-oxa)(MBP)₂ (3-THF). In an N₂ filled drybox, two 20 mL scintillation vials were placed in a $-30\,^{\circ}\mathrm{C}$ freezer. One contained a dark purple solution of 1 (0.200 g, 0.208 mmol, 1 equiv) in 4 mL of benzene with a Teflon coated stir bar and the other contained a yellow solution of 2 (0.067 g, 0.208 mmol, 1 equiv) in 4 mL of benzene. After cooling for 30 min, the now frozen solution of 2 was removed from the freezer and allowed to thaw. Immediately upon thawing, the frozen solution of 1 was removed from the freezer and the solution of 2 was added dropwise at rt over 2 min. Upon mixing, the solution immediately changed from a dark purple to a dark red color and was allowed to stir for 5 min at rt. At this point the volatile materials were removed under vacuum. The resulting solid was redissolved in a mixture of 3 mL of toluene and 8 drops of THF in an 8 mL scintillation vial. This solution was layered with 5 mL of pentane and placed in a $-30\,^{\circ}\mathrm{C}$ freezer for 3 days. During this time, red crystals formed, and were collected by filtration over a medium porosity fritted filter and washed with cold pentane 5 × 2 mL. Yield: 0.198 g, 0.137 mmol, 66%.

 $^{1}\mathrm{H}$ NMR (500 MHz, THF- d_{8}) &: 8.53 (s, 1H), 7.78 (d, J=8.0 Hz, 1H), 7.12 (d, J=7.5 Hz, 1H), 7.01 (s, 2H), 6.92 (s, 2H), 6.75 (s, 1H), 6.66 (s, 1H), 6.62 (s, 1H), 6.58 (s, 1H), 5.10 (d, J=13.4 Hz, 1H), 4.72 (d, J=13.5 Hz, 1H), 4.32 (s, 1H), 4.01 (s, 1H), 3.23 (d, J=13.4 Hz, 1H), 3.10 (d, J=13.6 Hz, 1H), 2.27 - 2.05 (m, 12H), 1.57 (s, 3H), 1.45 (s, 9H), 1.39 (s, 9H), 1.24 (s, 3H), 1.16 (s, 9H), 1.08 (s, 9H).

 $^{13}\text{C}\{^1\text{H}\}$ NMR (126 MHz, THF- d_8) &: 255.58, 174.49, 168.21, 167.40, 166.81, 137.97, 137.72, 137.33, 137.11, 136.98, 136.79, 135.03, 134.90, 134.58, 132.58 (q, J=3.1 Hz), 131.11 (q, J=29.3 Hz), 128.85, 128.75, 128.61, 127.02, 126.64 (q, J=177 Hz), 126.08, 124.25, 124.11, 123.95, 123.60, 120.18 (q, J=4.1 Hz), 82.35, 68.88, 35.89, 35.71, 35.60, 35.03, 32.46, 31.54, 31.09, 30.97, 30.16, 21.31, 21.17.

 19 F NMR (470 MHz, THF- d_8) δ : -62.44

⁷Li NMR (194 MHz, THF- d_8) δ: −0.57

X-ray quality crystals were obtained from a vapor diffusion of pentane into concentrated solutions of 3 in a solution consisting of 1:2 THF:tolulene in a $-30\,^{\circ}$ C freezer.

Anal. Cal. for $C_{74}H_{99}CeF_3LiNO_9\bullet(C_7H_8)$: C, 65.61; H, 7.66; F, 3.95; N, 1.03. Found C, 65.21; H, 6.65; N, 1.30. Best result of three attempts.

UV-Vis: $\lambda=460$ nm ($\epsilon=7533$ Lmol $^{-1}$ cm $^{-1}$), $\lambda=292$ nm ($\epsilon=24,426$ Lmol $^{-1}$ cm $^{-1}$).

[Li(DME)₃**][Ce(ortho-oxa)(MBP)**₂ **(3-DME)**. In an N₂ filled drybox, two 20 mL scintillation vials were placed in a - 30 °C freezer. One contained a dark purple solution of 1 (0.100 g, 0.104 mmol, 1 equiv) in 2 mL of benzene with a Teflon coated stir bar and the other contained a yellow solution of 2 (0.034 g, 0.104 mmol, 1 equiv) in 2 mL of benzene. After cooling for 30 min, the now frozen solution of 2 was removed from the freezer and allowed to thaw. Immediately upon thawing, the frozen solution of 1 was removed from the freezer and the solution of 2 was added dropwise at rt over 2 min. Upon mixing, the solution immediately changed from a dark purple to a dark red color and was allowed to stir for 5 min at rt. At this point the volatile materials were removed under reduced pressure. The resulting solid was dissolved in of 3 mL of DME in an 8 mL scintillation vial. This solution was layered with 5 mL of pentane and placed in a -30 °C freezer for 3 days. During this time, red crystals formed, and were collected by filtration over a medium porosity fritted filter and washed with cold pentane 5×2 mL. Yield: 0.111 g, 0.079 mmol, 75%.

 $^1\mathrm{H}$ NMR (500 MHz, THF- d_8) &: 8.53 (s, 1H), 7.80 (d, J=7.9 Hz, 1H), 7.13 (dd, J=8.1 Hz, 2.6 Hz, 1H), 7.01 (s, 2H), 6.91 (s, 2H), 6.76 (s, 1H), 6.68 (s, 1H), 6.64 (s, 1H), 6.59 (s, 1H), 5.12 (d, J=13.3 Hz, 1H), 4.72 (d, J=13.4 Hz, 1H), 4.33 (d, J=7.6 Hz, 1H), 4.01 (d, J=6.6 Hz 1H), 3.24 (d, J=13.6 Hz, 1H), 3.11 (d, J=13.6 Hz, 1H), 4.01 (d, J=13.6 Hz, 1H), 3.11 (d, J=13.6 Hz, 1H), 4.01 (d, J=13.6

13.6 Hz, 1H), 2.24 (s, 3H), 2.19 (s, 9H), 1.58 (s, 3H), 1.46 (s, 9H), 1.40 (s, 9H), 1.25 (s, 3H), 1.17 (s, 9H), 1.09 (s, 9H).

 $^{13}\text{C}^{\{1\text{H}\}}$ NMR (126 MHz, THF-d₈) &: 255.61, 174.55, 168.23, 167.46, 166.87, 138.03, 137.77, 137.40, 137.18, 137.05, 136.84, 135.08, 134.94, 134.63, 132.65 (q, J= 3.5 Hz), 131.18 (q, J= 29.5 Hz), 129.03, 128.82, 128.66, 127.22 (q, J= 177 Hz), 127.06, 126.14, 124.29, 124.18, 123.99, 123.66, 120.24 (q, J= 4.0 Hz), 82.41, 68.93, 35.94, 35.76, 35.68, 35.09, 32.52, 31.59, 31.14, 31.03, 30.22, 21.36, 21.21

¹⁹F NMR (470 MHz, THF- d_8) δ : -62.44

⁷Li NMR (194 MHz, THF- d_8) δ: -0.57

X-ray quality crystals were obtained from a layering of pentane on top of a saturated solution of 3-DME in DME (1:1, DME:Pentane).

Anal. Cal. for $C_{70}H_{101}CeF_3LiNO_{11}$: C, 62.90; H, 7.62; N, 1.05. Found C, 62.45; H, 7.32; N, 1.55.

Data availability

Crystallographic data for the structures reported in this article have been deposited at the Cambridge Crystallographic Data Center (CCDC) under deposition nos. CCDC 1998883 (3-THF) and 2043597 (3-DME). These data can be obtained free of charge from the Cambridge Crystallographic Data Centre via www.ccdc.cam.ac.uk/data_request/cif. All other data supporting the findings of this study are available within the Article and its Supplementary Information and from the corresponding authors upon reasonable request.

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References

- Raymond, K. N. & Eigenbrot, C. W. Structural criteria for the mode of bonding of organoactinides and -lanthanides and related compounds. *Acc. Chem. Res.* 13, 276–283, https://doi.org/10.1021/ar50152a005 (1980).
- 2. Kaltsoyannis, N. & Scott, P. The f elements. (Oxford University Press, 1999).
- Löble, M. W. et al. Covalency in Lanthanides. An X-ray Absorption Spectroscopy and Density Functional Theory Study of LnCl₆^{x-} (x = 3, 2). J. Am. Chem. Soc. 137, 2506–2523 (2015).
- Cheisson, T. et al. Multiple Bonding in Lanthanides and Actinides: Direct Comparison of Covalency in Thorium(IV)- and Cerium(IV)-Imido Complexes. J. Am. Chem. Soc. 141, 9185–9190, https://doi.org/10.1021/ iacs.9b04061 (2019).
- Kerridge, A. Quantification of f-element covalency through analysis of the electron density: insights from simulation. *Chem. Commun.* 53, 6685–6695 (2017)
- Kaindl, G., Schmiester, G., Sampathkumaran, E. V. & Wachter, P. Pressureinduced changes in L^{III} x-ray-absorption near-edge structure of CeO₂ and CeF₄: Relevance to 4f-electronic structure. *Phys. Rev. B.: Condens. Matter* 38, 10174–10177 (1988).
- Williams, U. J. et al. Synthesis, Bonding, and Reactivity of a Cerium(IV) Fluoride Complex. *Inorg. Chem.* 53, 27–29 (2014).
- Lewis, A. J., Carroll, P. J. & Schelter, E. J. Stable Uranium(VI) Methyl and Acetylide Complexes and the Elucidation of an Inverse Trans Influence Ligand Series. J. Am. Chem. Soc. 135, 13185–13192 (2013).
- Mullane, K. C. et al. ¹³C NMR Shifts as an Indicator of U-C Bond Covalency in Uranium(VI) Acetylide Complexes: An Experimental and Computational Study. *Inorg. Chem.* 58, 4152-4163 (2019).
- Smiles, D. E., Wu, G., Hrobárik, P. & Hayton, T. W. Use of ⁷⁷Se and ¹²⁵Te NMR Spectroscopy to Probe Covalency of the Actinide-Chalcogen Bonding in [Th(En){N(SiMe₃)₂}₃] (E = Se, Te; n = 1, 2) and Their Oxo-Uranium(VI) Congeners. *J. Am. Chem. Soc.* 138, 814–825 (2016).
- Staun, S. L., Sergentu, D.-C., Wu, G., Autschbach, J. & Hayton, T. W. Use of ¹⁵N NMR spectroscopy to probe covalency in a thorium nitride. *Chem. Sci.* 10, 6431–6436 (2019).
- Smiles, D. E., Wu, G., Hrobárik, P. & Hayton, T. W. Synthesis, Thermochemistry, Bonding, and ¹³C NMR Chemical Shift Analysis of a Phosphorano-Stabilized Carbene of Thorium. *Organometallics* 36, 4519–4524 (2017).
- Rungthanaphatsophon, P., Huang, P. & Walensky, J. R. Phosphorano-Stabilized Carbene Complexes with Short Thorium(IV) – and Uranium (IV)–Carbon Bonds. Organometallics 37, 1884–1891 (2018).
- Walter, M. D., Booth, C. H., Lukens, W. W. & Andersen, R. A. Cerocene Revisited: the Electronic Structure of and Interconversion Between Ce₂(C₈H₈)₃ and Ce(C₈H₈)₂. Organometallics 28, 698–707 (2009).
- Smiles, D. E. et al. The duality of electron localization and covalency in lanthanide and actinide metallocenes. Chem. Sci. 11, 2796–2809 (2020).
- Anwander, R., Dolg, M. & Edelmann, F. T. The difficult search for organocerium(iv) compounds. Chem. Soc. Rev. 46, 6697–6709 (2017).

- Greco, A., Cesca, S. & Bertolini, W. New π-cyclooctatetraenyl and π-cyclopentadienyl complexes of cerium. *J. Organomet. Chem.* 113, 321–330 (1976).
- Kilimann, U., Herbst-Irmer, R., Stalke, D. & Edelmann, F. T. An Efficient Access to Organocerium(IV) Complexes: Synthesis and Structure of Bis[1,3,6-tris(trimethylsilyl)cyclooctatetraene]cerium(IV). Angew. Chem. Int. Ed. 33, 1618–1621 (1994).
- Balazs, G. et al. Cerium(III) and Cerium(IV) Bis(η⁸-pentalene) Sandwich Complexes:synthetic, Structural, Spectroscopic, and Theoretical Studies. Organometallics 26, 3111–3119 (2007).
- Schneider, D., Harmgarth, N., Edelmann, F. T. & Anwander, R. Ceric Cyclopentadienides Bearing Alkoxy, Aryloxy, Chlorido, or Iodido Co-Ligands. Chem. -Eur. J. 23, 12243–12252 (2017).
- Sutton, A. D., Clark, D. L., Scott, B. L. & Gordon, J. C. Synthesis and Characterization of Cerium(IV) Metallocenes. *Inorganics* 3, 589–596 (2015).
- 22. Casely, I. J., Liddle, S. T., Blake, A. J., Wilson, C. & Arnold, P. L. Tetravalent cerium carbene complexes. *Chem. Commun.*, 5037–5039, (2007).
- Gregson, M. et al. A Cerium(IV)-Carbon Multiple Bond. Angew. Chem. Int. Ed. 52, 13016–13019 (2013).
- Arnold, P. L., Casely, I. J., Zlatogorsky, S. & Wilson, C. Organometallic Cerium Complexes from Tetravalent Coordination Complexes. Helv. Chim. Acta 92, 2291–2303 (2009).
- Gregson, M. et al. The inverse-trans-influence in tetravalent lanthanide and actinide bis(carbene) complexes. *Nat. Commun.* 8, 14137 (2017).
- Robinson, J. R., Carroll, P. J., Walsh, P. J. & Schelter, E. J. The Impact of Ligand Reorganization on Cerium(III) Oxidation Chemistry. *Angew. Chem.* Int. Ed. 51, 10159–10163 (2012).
- Levin, J. R., Dorfner, W. L., Dai, A. X., Carroll, P. J. & Schelter, E. J. Density Functional Theory as a Predictive Tool for Cerium Redox Properties in Nonaqueous Solvents. *Inorg. Chem.* 55, 12651–12659 (2016).
- Piro, N. A., Robinson, J. R., Walsh, P. J. & Schelter, E. J. The electrochemical behavior of cerium(III/IV) complexes: Thermodynamics, kinetics and applications in synthesis. *Coord. Chem. Rev.* 260, 21–36 (2014).
- Mahoney, B. D., Piro, N. A., Carroll, P. J. & Schelter, E. J. Synthesis, Electrochemistry, and Reactivity of Cerium(III/IV) Methylene-Bis-Phenolate Complexes. *Inorg. Chem.* 52, 5970–5977 (2013).
- Robinson, J. R. et al. Tuning Reactivity and Electronic Properties through Ligand Reorganization within a Cerium Heterobimetallic Framework. J. Am. Chem. Soc. 135, 19016–19024 (2013).
- Halter, D. P. et al. Electrocatalytic H₂O Reduction with f-Elements: mechanistic Insight and Overpotential Tuning in a Series of Lanthanide Complexes. J. Am. Chem. Soc. 140, 2587–2594 (2018).
- Watanabe, T., Matsuo, T. & Kawaguchi, H. A Tantalum(V) Carbene Complex: formation of a Carbene–Bis(phenoxide) Ligand by Sequential Proton and Hydride Abstraction. *Inorg. Chem.* 45, 6580–6582 (2006).
- Akagi, F., Ishida, Y., Matsuo, T. & Kawaguchi, H. Synthesis and reactivity of niobium complexes having a tripodal triaryloxide ligand in bidentate, tridentate, and tetradentate coordination modes. *Dalton T.* 40, 2375–2382 (2011).
- Manz, T. A., Fenwick, A. E., Phomphrai, K., Rothwell, I. P. & Thomson, K. T.
 The nature of aryloxide and arylsulfide ligand bonding in dimethyltitanium
 complexes containing cyclopentadienyl ligation. *Dalton Trans.*, 668–674,
 (2005).
- Maron, L., Werkema, E. L., Perrin, L., Eisenstein, O. & Andersen, R. A. Hydrogen for Fluorine Exchange in C₆F₆ and C₆F₅H by Monomeric [1,3,4-(Me₃C)₃C₅H₂]₂CeH: Experimental and Computational Studies. J. Am. Chem. Soc. 127, 279–292 (2005).
- 36. Werkema, E. L. & Andersen, R. A. Fluorine for Hydrogen Exchange in the Hydrofluorobenzene Derivatives $C_6H_xF_{(6-2)}$, where x=2, 3, 4 and 5 by Monomeric $[1,2,4-(Me_3C)_3C_5H_2]_2$ CeH: the Solid State Isomerization of $[1,2,4-(Me_3C)_3C_5H_2]_2$ Ce $(2,3,4,5-C_6HF_4)$ to $[1,2,4-(Me_3C)_3C_5H_2]_2$ Ce $(2,3,4,6-C_6HF_4)$. *J. Am. Chem. Soc.* **130**, 7153–7165 (2008).
- Shannon, R. Revised effective ionic radii and systematic studies of interatomic distances in halides and chalcogenides. *Acta Crystallogr. Sect. A* 32, 751–767 (1976).
- Pedrick, E. A., Hrobárik, P., Seaman, L. A., Wu, G. & Hayton, T. W. Synthesis, structure and bonding of hexaphenyl thorium(iv): observation of a nonoctahedral structure. *Chem. Commun.* 52, 689–692 (2016).
- Seaman, L. A. et al. Comparison of the Reactivity of 2-Li-C₆H₄CH₂NMe₂ with MCl₄ (M=Th, U): Isolation of a Thorium Aryl Complex or a Uranium Benzyne Complex. *Angew. Chem. Int. Ed.* 52, 10589–10592 (2013).
- Seaman, L. A. et al. A Rare Uranyl(VI)–Alkyl Ate Complex [Li (DME)_{1,5}]₂[UO₂(CH₂SiMe₃)₄] and Its Comparison with a Homoleptic Uranium(VI)–Hexaalkyl. *Angew. Chem. Int. Ed.* 52, 3259–3263 (2013).
- Mooßen, O. & Dolg, M. Two interpretations of the cerocene electronic ground state. Chem. Phys. Lett. 594, 47–50 (2014).

- Hay, P. J., Martin, R. L., Uddin, J. & Scuseria, G. E. Theoretical study of CeO₂ and Ce₂O₃ using a screened hybrid density functional. *J. Chem. Phys.* 125, 034712 (2006).
- Halbach, R. L., Nocton, G., Booth, C. H., Maron, L. & Andersen, R. A. Cerium Tetrakis(tropolonate) and Cerium Tetrakis(acetylacetonate) Are Not Diamagnetic but Temperature-Independent Paramagnets. *Inorg. Chem.* 57, 7290–7298 (2018).
- Hrobárik, P., Hrobáriková, V., Greif, A. H. & Kaupp, M. Giant Spin-Orbit Effects on NMR Shifts in Diamagnetic Actinide Complexes: Guiding the Search of Uranium(VI) Hydride Complexes in the Correct Spectral Range. Angew. Chem. Int. Ed. 51, 10884–10888 (2012).
- Keal, T. W. & Tozer, D. J. The exchange-correlation potential in Kohn–Sham nuclear magnetic resonance shielding calculations. *J. Chem. Phys.* 119, 3015–3024 (2003).
- Autschbach, J. Analyzing NMR shielding tensors calculated with twocomponent relativistic methods using spin-free localized molecular orbitals. J. Chem. Phys. 128, 164112 (2008).
- Autschbach, J. & Zheng, S. Analyzing Pt chemical shifts calculated from relativistic density functional theory using localized orbitals: The role of Pt 5d lone pairs. *Magn. Reson. Chem.* 46, S45–S55 (2008).
- Jantzi, K. L., Guzei, I. A. & Reich, H. J. Solution and Solid-State Structures of Lithiated Phenyloxazolines. Organometallics 25, 5390–5395 (2006).

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Author contributions

G.B.P. and E.J.S conceived this project. G.B.P. performed the synthesis, electrochemical, NMR, and UV-Vis experiments. M.R.G. and P.J.C. collected and solved the X-ray structures. G.B.P., P.J.W., and E.J.S. analyzed the experimental data. D.-C.S. and J.A. conducted the theoretical computations and analyzed the results. G.B.P., D.-C.S., J.A., P.J. W. and E.J.S. participated in drafting the paper. All authors discussed the results and contributed the preparation of the final paper.

Competing interests

The authors declare no competing interests.

Additional information

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