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A polarization encoded photon-to-spin interface

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We propose an integrated photonics device for mapping qubits encoded in the polarization of a photon onto the spin state of a solid-state defect coupled to a photonic crystal cavity: a “polarization-encoded photon-to-spin interface” (PEPSI). We perform a theoretical analysis of the state fidelity’s dependence on the device’s polarization extinction ratio and atom–cavity cooperativity. Furthermore, we explore the rate-fidelity trade-off through analytical and numerical models. In simulation, we show that our design enables efficient, high fidelity photon-to-spin mapping.

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INTRODUCTION

Quantum networks are being developed to distribute entanglement across distant nodes. A central requirement common to most quantum network approaches is the development of efficient interfaces between spins and photonic qubits¹. Among the various photonic degrees of freedom, encoding in the polarization basis $\{|H\rangle, |V\rangle\}$ (horizontal and vertical) is attractive over number-state encoding because photon loss becomes a heralded error².

To couple the polarization-encoded photon qubit $|\psi_p\rangle = \alpha|H\rangle + \beta|V\rangle$ to an atomic memory in a network node, Duan and Kimble³ proposed the scheme illustrated in Fig. 1a. The incoming photon passes through a polarizing beam splitter (PBS) so that only the V polarization is reflected off a single-sided cavity whose mode couples with the $|\downarrow\rangle \leftrightarrow |\downarrow'\rangle$ transition. The H polarization is reflected off a mirror, and recombines with the V polarization to form an entangled spin-photon state: $|\psi_{\text{ent,out}}\rangle = -\alpha|H, \downarrow\rangle + \beta|V, \downarrow\rangle - \alpha|H, \uparrow\rangle - \beta|V, \uparrow\rangle$. Subsequent measurement of the photonic state heralds the transfer of the polarization qubit to the atom, as demonstrated in recent experiments using trapped neutral atoms⁴ and diamond color centers⁵.

However, in a free-space setup, a major technical challenge concerns the need to maintain stability of the phase difference between two spatially separated meters-long polarization paths⁴. In this paper, we propose a monolithic, micron-scale photonic structure that combines the H and V paths into one phase-stable architecture (Fig. 1b). We estimate that this system will enable state transfer fidelity exceeding 99%. This polarization-encoded photon-to-spin interface (PEPSI) greatly simplifies quantum networking with polarization-encoded photons coupled to atomic memories.

RESULTS

Device

Qubits based on single atoms such as solid-state color centers, neutral atoms, and trapped ions have emerged as promising systems for quantum networking applications. In particular, group-IV color centers in diamond are attractive candidates due to their excellent optical and spin coherence^{6–9}. In this paper, we focus on the negatively charged silicon-vacancy center (SiV) coupled to a diamond nanocavity, though the approach

generalizes to other stationary qubits such as neutral atoms⁴, trapped ions^{10,11}, and quantum dots^{12,13}.

As illustrated in Fig. 1b, the structure comprises (i) a polarization-dependent reflector (PDR) for the H (TE) mode and (ii) an over-coupled single-sided cavity for the V (TM) mode. The PEPSI collapses both interferometric arms into one co-propagating path that greatly suppresses phase instability stemming from environmental noise. In contrast, bulk optics suffer from thermal and vibrational fluctuations that incur phase noise, which requires phase stabilization costly in operation time⁵.

The PDR shown in Fig. 1c uses a corrugated photonic crystal design with periodicity $a = 184$ nm, width $W = 2.07a$, modulation amplitude $dW = 3.97a$. An adiabatic taper transfers photons to a 1D photonic crystal nanocavity coupled to the SiV. The remainder of this paper analyzes the performance this phase-stable device. Specifically, we investigate the impact of PEPSI device parameters on state transfer fidelity (see “Effects of device imperfections”), the rate-fidelity trade-off in a quantum network link (see “Quantum state transfer rate”), and extensions to a scalable photonic integrated circuit (PIC) platform (see “Discussion”).

Effects of device imperfections

To analyze the state transfer process, we consider a single photon $|\psi_p\rangle$ incident on a cavity-coupled spin qubit $|\psi_{s,i}\rangle = (|\uparrow\rangle + |\downarrow\rangle)/\sqrt{2}$. Using a Schrödinger picture evolution, we calculate the resulting spin state $|\psi_{s,f}(i)\rangle$ after detection of the reflected photon in the polarization diagonal basis $\{|D\rangle, |A\rangle\}$. Its overlap with the desired state transferred from the polarization qubit defines the state fidelity $\mathcal{F}$, of which we take the average¹⁴:

$$\mathcal{F} = \frac{1}{4} \sum_i \mathcal{F}_i = \frac{1}{4} \sum_i |\langle \phi_i | \psi_{s,f}(i) \rangle|^2, \quad (1)$$

where $|\phi_{1,2}\rangle = (|\downarrow\rangle \pm |\uparrow\rangle)/\sqrt{2}$, $|\phi_{3,4}\rangle = (|\downarrow\rangle \pm i|\uparrow\rangle)/\sqrt{2}$ (see Supplementary Note 2).

When a device is perfect such that a lossless PDR has infinite polarization extinction ratios and a nanocavity has perfect waveguide–cavity coupling ($\kappa_{wg}/k = 1$), the cavity reflection solely determines the fidelity that scales as $(C - 1)/(C + 1)$ in the large cooperativity limit⁴ (see “Methods” and Supplementary Note 3). However, when the PDR has finite extinction ratios and scattering losses, and the single-sided cavity has a reduced waveguide–cavity coupling efficiency $\kappa_{wg}/k < 1$, the need to

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balance losses becomes especially important to achieving high fidelity. For example, considering the desired state $|\phi_1\rangle$ where $\alpha = \beta = 1$, balancing losses entails matching the two coefficients $|r_{H,on} - r_{V,on}| = |r_{H,off} + r_{V,off}|$, which are both functions of PDR transmissivity/reflectivity and the cavity reflectivity (see “Methods”).

Figure 2a shows $\mathcal{F}$ as a function of the PDR’s width and modulation amplitude given a low scattering loss and fixed cavity parameters corresponding to our design: waveguide–cavity coupling $\kappa_{wg}/\kappa \approx 0.83$ and cooperativity $C = 100$, which has already been experimentally demonstrated in ref. ⁵. We find the upper bound of the fidelity is maximized at 99.978% (assuming perfect gate and detection fidelities) when $W = 380$ nm and $dW = 730$ nm, corresponding to transmission and reflection extinction ratios of 17.72 and 18.93 dB for 20 periodicities. In order to

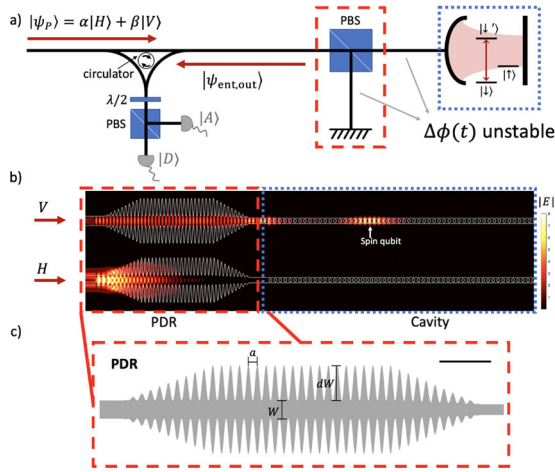


Fig. 1 Polarization-encoded photon-to-spin interface. **a** The Duan–Kimble scheme for polarization-spin mapping. The requirements of a high extinction polarizing beam splitter (PBS), strong cavity-atom coupling, and stabilization of the phase mismatch between arms $\Delta\phi(t)$ all make implementation with bulk optics challenging. **b** Our proposal for a phase-stable monolithic device (PEPSI) that implements the protocol in **a**. A polarization-dependent reflector (PDR, red dashed lines) then reflects H light while passing V light through to interact with the cavity-emitter system (blue dashed lines). **c** A zoom-in depiction of the PDR with geometry parameters a (periodicity), W (width), and dW (modulation amplitude). The scale bar corresponds to 1 μ m.

controllably balance losses to maximize the state transfer fidelity, we also include an H attenuator that only diminishes the incoming H light (see Supplemental Note 1). For each set of parameter values $\{dW, W\}$, we calculate the H attenuation factor η_H that maximizes $\mathcal{F}$ in Fig. 2b. For the particular design with $W = 380$ nm and $dW = 730$ nm, the optimal upper bound $\mathcal{F} = 99.978\%$ is reached when $\eta_H = 66\%$. In fact, by tuning η_H appropriately, we observe that $\mathcal{F}$ well exceeds 99% for any dW between 700 and 750 nm and similarly for any W between 360 and 420 nm, providing the PEPSI tolerance to fabrication errors.

Additionally, the state transfer fidelity intimately relates to the cavity parameters. Figure 2c shows that the state fidelity monotonically improves with the atom–cavity cooperativity since the cavity reflectivity $r \propto (C - 1)/(C + 1)$ approaches +1. For our device, the atom–cavity cooperativity of $C = 100$ gives $\mathcal{F} = 99.978\%$. We also analyze the fidelity’s dependence on the waveguide–cavity coupling strength. As a result of balanced losses, Fig. 2d indicates that the fidelity is maximized when $\kappa_{wg}/\kappa = 0.82$ and decreases as the waveguide–cavity coupling deviates from the optimal point. An under-coupled or critically coupled cavity would result in a severely degraded state transfer due to insufficient cavity reflection. On the other hand, over-coupling past $\kappa_{wg}/\kappa = 0.82$ would curtail the atom–cavity interaction and consequently lowers the fidelity. However, our calculation shows that the fidelity can still exceed 99% as long as κ_{wg}/κ falls between 0.73 and 0.93, granting again partial immunity to fabrication errors.

Quantum state transfer rate

We now analyze the performance of the PEPSI in facilitating quantum state transfer across a lossy network link by looking at the rate-fidelity trade-off for a device realized in simulation, parameterized in the section “Device”. We denote the probability of a photon entering and returning through the PDR as $\eta_H \eta_{PDR}^2 R_{cav}$, where R_{cav} is the cavity reflection coefficient and $1 - R_{cav}$ is the cavity decay rate into the environment (assume negligible transmission through the single-sided cavity). η_{PDR} is the transmission efficiency of the PDR. As shown in Fig. 3a, the protocol begins by initializing the spin qubit in a superposition state $(|1\rangle + |2\rangle)/\sqrt{2}$ in a time $\tau_{reset} = 30 \mu$ s as demonstrated in ref. ⁵. A photonic qubit $|\psi_p\rangle$ launched across the link with transmissivity η_{link} reaches the PDR shown in Fig. 3b. If the reflected photon is detected as described above with probability $p_{det} = \eta_{link} \eta_H \eta_{PDR}^2 R_{cav} \eta_{det}$, the spin qubit is projected to the state

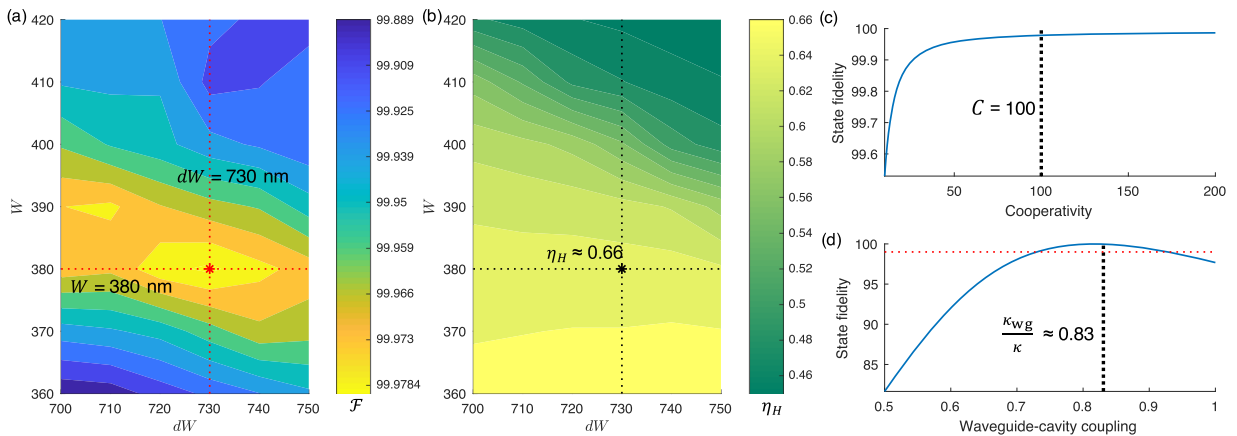


Fig. 2 Fidelity as a function of device imperfections. **a** $\mathcal{F}$ is plotted as a function of the two PDR geometry parameters: the width W and the modulation amplitude dW . $W = 380$ nm and $dW = 730$ nm are chosen for our particular device with an optimum $\mathcal{F} = 99.978\%$. **b** The optimal H polarization attenuation factor for balancing losses as a function of W and dW . **c**, **d** The state fidelity as functions of the atom–cavity cooperativity and waveguide–cavity coupling. The atom–cavity cooperativity is calculated using Eq. (15). The PDR is designed specifically for a single-sided cavity with $C = 100$. The waveguide–cavity coupling is tuned to $\kappa_{wg}/\kappa \approx 0.83$ to maximize fidelity within the allowable design space. The red dashed line indicates the threshold $\mathcal{F} = 99\%$, which is satisfied in the range $\kappa_{wg}/\kappa = [0.73, 0.93]$.

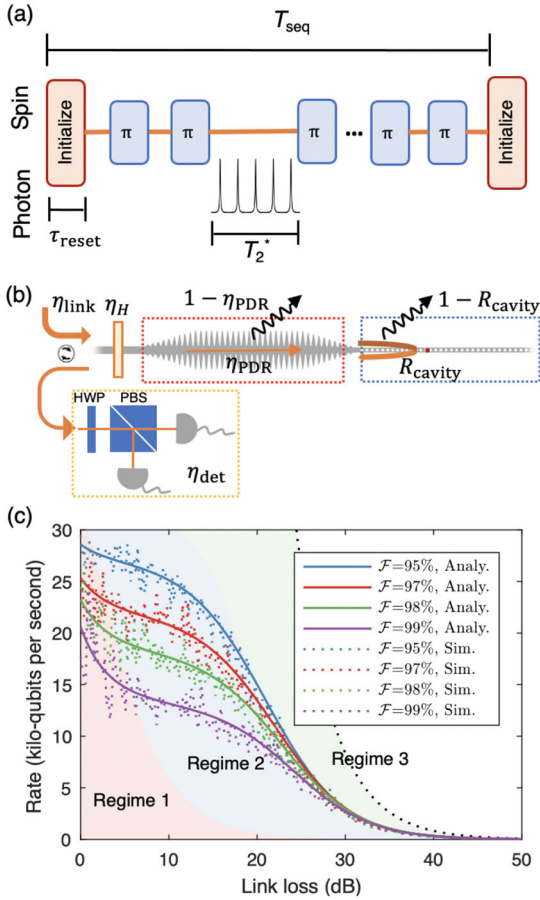


Fig. 3 Rate-fidelity trade-off as a function of link loss. **a** Pulse sequences for conducting quantum state transfer between a polarization qubit and a spin qubit. **b** A diagram depicting where scattering losses occur. **c** Transfer rate (kilo-qubits per second, operated at 5.81 MHz clock rate) as a function of link loss $1 - \eta_{\text{link}}$ for four fidelity constraints: $\mathcal{F} = 95, 97, 98$, and 99% . We plot both the analytical solutions (solid) and the Monte Carlo simulations (dashed). We categorize the rate as a function of link loss into Regime 1 (red), Regime 2 (blue), and Regime 3 (green). The black dashed line denotes the repeaterless bound for quantum key distribution protocols¹⁵.

$\alpha|\downarrow\rangle + \beta|\uparrow\rangle$ (see “Methods”) with fidelity given by Eq. (1). If no photon is detected, the protocol is repeated.

However, when $\eta_{\text{link}} \ll 1$, most transmission attempts do not interact with the spin, and time can be saved by not re-initializing on every transmission attempt. In particular, we consider a series of N photons injected into the link after spin re-initialization. These photons are interspersed by dynamical decoupling pulses (π -pulses in Fig. 3a) to maintain memory coherence. If the detector registers a click for the m th attempt, the receiver blocks the subsequent $N - m$ pulses. The complication is that any photon that reaches the cavity but is subsequently lost produces an unheralded error with probability $p_e = \eta_{\text{link}}\eta_H\eta_{\text{PDR}}(1 - R_{\text{cav}})$, since the environment projects the spin to a mixed state $\rho_{\text{mixed}} = \frac{1}{2}\mathbb{I}$. Thus, the optimum fidelity for a given device is achieved by re-initializing the spin qubit in advance of every photon transmission. However, the photon can also be either lost in the link before reaching the spin with probability $p_{\text{lost}} = 1 - p_e - p_{\text{det}}$ or heralded by the detector with probability p_{det} . Conditioned on not detecting a click, the probability of photon loss without contaminating the spin is $p_{\text{lost}}/(1 - p_{\text{det}})$, and therefore the probability of photon never reaching the spin after $m - 1 \leq N$ channel uses is $(p_{\text{lost}}/(1 - p_{\text{det}}))^{m-1}$.

Given a detector click on the m th attempt, the probability that at least one error has occurred in the preceding $m - 1$ bins is

$$P_{\text{error}}(m) = 1 - \left(\frac{p_{\text{lost}}}{1 - p_{\text{det}}} \right)^{m-1}. \quad (2)$$

The average error probability is found by summing over all possible sequences up to a total of N attempts, each sequence weighted by $P(m\text{th click})$, the probability of detecting a click on the m th attempt:

$$P_{\text{error}} = \sum_{m=1}^N P_{\text{error}}(m)P(m\text{th click}) \\ = 1 - (1 - p_{\text{det}})^N - p_{\text{det}} \frac{1 - p_{\text{lost}}^N}{1 - p_{\text{lost}}}.$$

The average state fidelity after the protocol that uses sequences of length N before resetting the memory is then:

$$\mathcal{F} = \langle \psi_{\text{ideal}} | (1 - P_{\text{error}}) \rho_{0,\text{eff}} + P_{\text{error}} \rho_{\text{mixed}} | \psi_{\text{ideal}} \rangle, \quad (4)$$

where $|\psi_{\text{ideal}}\rangle$ is the ideal transferred quantum state and $\rho_{0,\text{eff}}$ is the effective density matrix incorporating device imperfections and detection error (see “Methods”). We can solve Eq. (4) for the maximum number of channel uses before spin re-initialization N_{max} under a given fidelity constraint, e.g. $\mathcal{F} = 99\%$.

Each sequence (duration T_{seq} as denoted in Fig. 3a) of N_{max} transmission attempts has a probability $P_{\text{success}} = 1 - (1 - p_{\text{det}})^{N_{\text{max}}}$ to detect at least one click. The number of failed sequences (i.e. each sequence of N_{max} attempts without clicks followed by a memory reset) before a successful one is given by the geometric distribution. Thus, the average time of failed sequences per detector click is

$$T_{\text{failures}} = \frac{(1 - p_{\text{det}})^{N_{\text{max}}}}{1 - (1 - p_{\text{det}})^{N_{\text{max}}}} [N_{\text{max}}\tau_{\text{pulse}} + \tau_{\text{reset}}], \quad (5)$$

where $4\tau_{\text{pulse}}$ is an effective pulse time accounting for repetition rate and dynamical decoupling π pulses (see Supplemental Note 4). After these failures, there is a successful sequence where the m th bin yields a click, which takes an average time of:

$$T_{\text{success}} = \tau_{\text{reset}} + \sum_{m=1}^{N_{\text{max}}} P(m\text{th click}) m\tau_{\text{pulse}} \\ = \tau_{\text{reset}} + \tau_{\text{pulse}} \left(\frac{P_{\text{success}}}{p_{\text{det}}} - N_{\text{max}}(1 - p_{\text{det}})^{N_{\text{max}}} \right).$$

The average quantum state transfer rate is then the inverse of the time per success:

$$\bar{r} = \frac{1}{T_{\text{failures}} + T_{\text{success}}}. \quad (7)$$

In Fig. 3c, we explore the trade-off between the heralded state fidelity $\mathcal{F}$ and the average rate accounting for both polarizations (see “Methods”). We verify our analytical solutions with Monte Carlo simulations, and show that the PEPSI can achieve transfer rate exceeding 1 kilo-qubits per second even at high link loss ~ 30 dB.

We divide the rate into three regimes. In Regime 1 (shaded red) where N_{max} is low, high-fidelity state transfer prohibits increasing N_{max} to offset losses in the channel, causing an exponential rate loss that intensifies for higher fidelity constraint, e.g. $\mathcal{F} = 99\%$. On the other hand, for a more relaxed fidelity constraint, e.g. $\mathcal{F} = 95\%$, the spin does not need to be re-initialized as frequently and the rate does not fall off as drastically.

As the link loss increases in Regime 2 (shaded blue), the number of transmission attempts per memory reset also increases. However, the time per success is still dominated by memory reset time in this regime where $\tau_{\text{reset}} > N_{\text{max}}\tau_{\text{pulse}}$. As a result, the rate of increase for the number of sequences prior to detecting a click stays constant, and the rate consequently remains relatively flat.

However, in Regime 3 (shaded green) when the number of transmission attempts per sequence increases such that $N_{\max} T_{\text{PEPSI}} > T_{\text{reset}} \eta_{\text{link}}$ becomes the rate-limiting factor. In this regime, the rate thus approaches the channel-limited bound (black dashed) given by $\propto \eta_{\text{link}}/T_{\text{pulse}}$ ¹⁵.

DISCUSSION

Practical quantum repeater nodes will likely require multiplexing over a large number of qubits. To this end, we consider the PEPSI PIC illustrated in Fig. 4. An incoming photonic qubit $|\psi_P\rangle$ enters through a PDR followed by a Mach–Zehnder interferometer (MZI) tree network, which routes the photon to a quantum memory. The PIC with >GHz modulation of the MZIs¹⁶ can perform state mapping across the memory array simultaneously by sending multiplexed photons to different atom-coupled cavities. As a result, the transfer rate improves by a factor of N_{cav} equivalent to the number of memories connected to the tree network. The architecture can also produce heralded entanglement by sending a photon that enters an MZI 50:50 beam splitter immediately before entering any two neighboring memories. Repeated heralding then produces a cluster of entangled nodes useful for quantum key distribution protocols.

Furthermore, an active PIC provides tunability essential for efficient quantum state transfer. For example, aluminum nitride photonic circuits have integrated 128 diamond waveguide-coupled color centers¹⁷ and can enable piezoelectric spectral tuning of photonic crystal cavities¹⁸ and diamond color center emission^{19,20}. Integration by pick-and-places allows post-selecting high-performing devices, and additional on-chip waveplates and polarizers in conjunction with the PDR (collectively termed as a tunable PDR in Fig. 4) can then optimally balance losses to achieve high transfer fidelity. Multiple emitters may also be implanted²¹ to increase the number of devices containing SiV⁻ oriented along the applied magnetic field's direction.

In summary, we introduced a phase-stable architecture for high-fidelity quantum state transfer between photonic polarization and spin qubits: the fundamental elements of a quantum repeater network. Our simulations and calculations show that the PEPSI can achieve state fidelity exceeding 99% at kilo-qubits per second transfer rate by carefully balancing losses. We note that the source of infidelity considered in the analyses addresses only the mode-mismatch error. Namely, the loss imbalance that arises from non-optimal transmissivities and reflectivities of the PDR and the nanocavity. Additional qubit errors concerning dephasing, spectral diffusion, and charge-state instability will require further investigation^{22,23}. Therefore, the calculated fidelity of 99.978% is realistically an upper bound. Nevertheless, beyond color centers in diamond, our scheme applies to other quantum memories including rare-earth ions^{24–26} and neutral atoms²⁷ that may

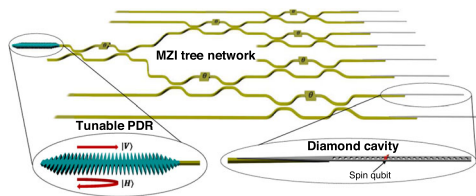


Fig. 4 Implementation in a PIC. A PIC incorporating diamond nanocavities. The V polarization passes through a tunable PDR (a combination of a PDR, active on-chip waveplates and polarizers) and enters an MZI tree network, which routes the photon to an atom-coupled cavity for quantum state transfer. Simulation (see Supplemental Note 7) indicates that an adiabatic taper can provide near-unity coupling efficiency between the PIC and the diamond waveguides.

exhibit lower qubit errors. Lastly, we proposed a multiplexing PIC platform for state mappings across a quantum memory array via an MZI tree network. As PIC platforms have scaled beyond tens of individually controllable components²⁸, our nanophotonic spin-photon interface should extend these gains to large-scale multiplexed quantum repeaters²⁹ and even photonic cluster states³⁰.

METHODS

State transfer fidelity calculations

An incoming qubit is encoded on the polarization of a photon:

$$|\psi_P\rangle = \alpha|H\rangle + \beta|V\rangle. \quad (8)$$

With the spin qubit prepared in an even superposition state $|\psi_A\rangle = (|\downarrow\rangle + |\uparrow\rangle)/\sqrt{2}$, the joint spin-photon state would be

$$|\psi_{\text{joint},i}\rangle = \alpha|H, \downarrow\rangle + \alpha|H, \uparrow\rangle + \beta|V, \downarrow\rangle + \beta|V, \uparrow\rangle. \quad (9)$$

This photon then hits an imperfect PDR with field reflection (transmission) coefficients r_i (t_i) for the polarization $i \in \{H, V\}$. The transmitted output is incident on a nanophotonic cavity coupled to a spin qubit. Since only the $|\downarrow\rangle \rightleftharpoons |\downarrow'\rangle$ (see Fig. 1a) transition is resonant with the cavity mode, the photon experiences a spin-dependent cavity reflection $r_{\text{cav}} \in \{r_{i,\text{uncoupled}}, r_{i,\text{coupled}}\}$. The output joint photon-spin system after the HWP (that transform $H \rightarrow H + V$, $V \rightarrow V - H$) is in the state:

$$\begin{aligned} |\psi_f\rangle = & |H\rangle \otimes [(ar_{H,\text{on}} - \beta r_{V,\text{on}})|\downarrow\rangle \\ & + (ar_{H,\text{off}} - \beta r_{V,\text{off}})|\uparrow\rangle] \\ & + |V\rangle \otimes [(ar_{H,\text{on}} + \beta r_{V,\text{on}})|\downarrow\rangle \\ & + (ar_{H,\text{off}} + \beta r_{V,\text{off}})|\uparrow\rangle], \end{aligned} \quad (10)$$

where

$$r_{H,\text{on}} = r_H + \frac{r_{H,\text{coupled}} t_H^2}{1 - r_{H,\text{coupled}} r_H}, \quad (11)$$

$$r_{H,\text{off}} = r_H + \frac{r_{H,\text{uncoupled}} t_H^2}{1 - r_{H,\text{uncoupled}} r_H}, \quad (12)$$

$$r_{V,\text{on}} = r_V + \frac{r_{V,\text{coupled}} t_V^2}{1 - r_{V,\text{coupled}} r_V}, \quad (13)$$

$$r_{V,\text{off}} = r_V + \frac{r_{V,\text{uncoupled}} t_V^2}{1 - r_{V,\text{uncoupled}} r_V}. \quad (14)$$

The state-dependent cavity reflection coefficients can be derived from using the input-output formalism^{31,32}:

$$r(\omega) = 1 - \frac{\kappa_{\text{wg}}}{i(\omega_c - \omega) + \frac{\kappa}{2}} \frac{1}{1 + \frac{g^2}{(i(\omega_c - \omega) + \frac{\kappa}{2})(i(\omega_a - \omega) + \frac{\gamma}{2})}}, \quad (15)$$

$$= \frac{C - 1}{C + 1} \quad (\text{large } C \text{ limit}), \quad (16)$$

where κ , γ , and g are the cavity total decay, atom relaxation, and atom-cavity coupling rates. κ_{wg} is the cavity decay rate into the waveguide. $(\omega_c - \omega)$ and $(\omega_a - \omega)$ are the cavity and atom detuning, respectively. $C = \frac{4g^2}{\kappa\gamma}$ is the atom-cavity cooperativity. In the uncoupled case, $g = 0$ and a bare reflection off the cavity gives the photon $a - 1$ phase. On the other hand, the coupled state results in $a + 1$ phase. The relative phase conditioned on the atomic state forms the basis behind the state transfer protocol detailed in ref. 3.

Finally, a detection of an $|D\rangle$ or $|A\rangle$ photon heralds mapping of the input photonic state onto the spin with an additional Hadamard rotation on the spin (and a conditional π rotation). We can calculate the state fidelity by Eq. (1).

Transfer rate calculations

In the state transfer rate calculations, we consider the detection, scattering loss, and error paths for both polarization modes and compute the average rate. Here we consider the transmission efficiency $\eta_{A,V/H}$ through the H attenuator to be 79.8% for the V polarization and 52.6% for the H polarization (see Supplementary Note 4). We denote the

power transmission and reflection coefficients of the PDR as $T_{V/H}$ and $R_{V/H}$. The cavity reflectivity $R_{cav,V/R_{cav,H}}$ is the average reflectivity between on- and off-resonance cases for the V/H polarization, respectively: $R_{cav,V} = (|r_{cavity-V}|^2 + |r_{coup-V}|^2)/2 = 82.2\%$, $R_{cav,H} = 95.8\%$ basing on our simulated device and $C = 100$.

In order to detect a V(H) photon, it has to either undergo a roundtrip as denoted by Fig. 3b with probability $\eta_{link}\eta_{a,V}T_{V,R_{cav,V}}T_{V,\eta_{det}}$ ($\eta_{link}\eta_{a,H}T_{H,R_{cav,H}}T_{H,\eta_{det}}$) or reflect off the PDR upon the first pass with probability $\eta_{link}\eta_{a,V}R_{V,\eta_{det}}$ ($\eta_{link}\eta_{a,H}R_{H,\eta_{det}}$), where $\eta_{det} = 93.6\%$ is the detection efficiency accounting for the PBS, the HWP, and the photon detector (see Supplementary Note 4). The average detection probability is then

$$p_{det} = \frac{\eta_{link}}{2} (\eta_{a,V}T_{V,R_{cav,V}} + R_V + \eta_{a,H}T_{H,R_{cav,H}} + R_H)\eta_{det}. \quad (17)$$

The photon can also scatter off en route to the PDR with probability $1 - \eta_{link}$ or by the PDR, contributing to the probability of photon loss without erroring:

$$p_{lost} = 1 - \eta_{link} + \eta_{link} \left(1 - \frac{\eta_{a,V} + \eta_{a,H}}{2} \right) + \frac{\eta_{link}}{2} (\zeta_V + \zeta_H), \quad (18)$$

where $\zeta_V = 1 - T_V - R_V$ and $\zeta_H = 1 - T_H - R_H$.

Lastly, as addressed in the section “Quantum state transfer rate”, the photon can be lost after interacting with the atom–cavity system, hence yielding an unheralded error. Specifically, we consider errors arising from the V photon scattering after cavity interaction and the small amount of H photon leaking into the cavity:

$$p_e = 1 - p_{det} - p_{lost}. \quad (19)$$

The probabilities are used to compute P_{error} , which is the probability of at least one unheralded error occurring after detecting the first and only click on the m th attempt within N attempts. After which, we can calculate the average state fidelity:

$$\mathcal{F} = \langle \psi_{ideal} | (1 - P_{error})\rho_0 + P_{error}\rho_{mixed} | \psi_{ideal} \rangle, \quad (20)$$

where ρ_0 is the density matrix corresponding to a single attempt considering only device imperfections.

Monte Carlo simulations

Numerical simulations were performed in MATLAB (MathWorks Inc.). For each attempt, a probability value p_{random} is chosen out of a uniform distribution $U(0, 1)$. p_{random} then determines if the photon is lost in the device before reaching the spin (p_{lost}), lost in the device after the spin (p_e), or detected (p_{det}). Each simulation trial terminates once the photon is detected, and the total experimental time is recorded. A trial can consist of multiple sequences, and each sequence has the number of attempts up to N_{max} , which depends on the fidelity constraint and the link loss. Each Monte Carlo data point presented in Fig. 3c is the average rate of 100 simulation trials.

The oscillation in the Monte Carlo simulations (dashed lines in Fig. 3c) is an artifact from discretizing the number of attempts required to achieve a certain fidelity constraint given a fixed link loss (see Supplementary Note 4). The allowable N_{max} is first analytically calculated assuming a continuous variable, then fed into the Monte Carlo simulations to validate the transfer rate calculations. The origin of the artifact can be understood by considering the trade-off between fidelity and the number of attempts. Recall that every undetected photon can be scattered before reaching the emitter–cavity system. Hence, time can be saved by not re-initializing the spin qubit as $N_{attempts}$ increases. In other words, as link loss increases, it is advantageous to increase the number of attempts. If an integer number of attempts Z is fixed, increasing the link loss consequently lowers the transfer rate until the number of attempts increases to the next integer $Z + 1$. After which, the rate increases suddenly and manifests in a sinusoidal behavior in simulations.

DATA AVAILABILITY

Data available on request from authors.

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AUTHOR CONTRIBUTIONS

K.C.C. performed the FDTD simulations in designing the PEPSI. K.C.C. and E.B. calculated the average state fidelity and the transfer rate. D.E. conceived the idea. All authors contributed to writing and revising the manuscript.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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