

Management implications of long transients in ecological systems

Short Title: Managing Long Transients

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17 Abstract

18 The underlying biological processes that govern many ecological systems can create very long periods
19 of transient dynamics. It is often difficult or impossible to distinguish this transient behaviour from similar
20 dynamics that would persist indefinitely. In some cases, a shift from the transient to the long-term, stable
21 dynamics may occur in the absence of any exogenous forces. Recognizing the possibility that the state of
22 an ecosystem may be less stable than it appears is crucial to the long-term success of management strategies
23 in systems with long transient periods. Here we demonstrate the importance of considering the potential of
24 transient system behavior for management actions across a range of ecosystem organizational scales and
25 natural system types. Developing mechanistic models that capture essential system dynamics will be crucial
26 for promoting system resilience and avoiding system collapses.

27 **1. Introduction**

28 A major challenge facing the management of ecosystems worldwide is the fluctuation and variability in the
29 production of ecosystem services and benefits upon which humans rely. Invading species¹, shifting species
30 distributions², and environmental changes that alter both community composition^{3,4} and functional traits⁵
31 are expected to be increasingly important in ecosystems globally⁶. An additional challenge in the
32 management of ecological systems is that the current dynamics may not be the asymptotic (long term) state,
33 even though observations appear to show a steady pattern that resembles noise around an equilibrium or
34 regular oscillations. Many systems are in long transient states, exhibiting apparently stable dynamics, often
35 over dozens to hundreds of generations, but will ultimately experience a shift into a new, stable state⁷⁻¹¹.
36 Importantly, some state shifts within long transients may occur in the absence of influence by exogenous
37 factors, such as underlying environmental change.

38 Such long transients are surprisingly common across a range of species and systems, and the
39 importance of the long view for understanding ecological processes has long been recognized¹². Transient
40 dynamics over a long period of time are common and their appreciation is evidenced in part by the extended
41 network of Long Term Ecological Research (LTER) sites. Systems with slow variables or interactions
42 between slow (e.g. soil development, erosion) and fast (e.g. plant-herbivore interactions) variables¹³ that
43 often lead to system behavior such as tipping points¹⁴ can undergo long transients. High dimensional
44 systems are also more likely to experience transient behavior, such as systems with large spatial complexity
45 (e.g., metapopulations), or high food web dimensionality⁷. Quite often, the existence of transient behavior
46 is not apparent in observations of the system until after a shift in behavior has occurred. While this is similar
47 to the challenge posed by tipping points, an important observation is that shifts caused by transients can
48 occur in the absence of any underlying change in environmental conditions, such as nutrient loads or
49 temperature. Therefore, approaches to predicting regime shifts or tipping points developed around
50 identifying critical thresholds in environmental drivers will not apply to long transients, leaving a gap in
51 our ability to manage ecosystems that may be in a transient period. Recent classification of the underlying

52 causes of long transients^{15,16} creates an opportunity to look more closely at the implications of these
53 phenomena for managing ecosystems, and to expand our understanding of the impacts of management
54 interventions vis-à-vis transient behavior.

55 Adaptive management inherently acknowledges uncertainties and nonstationarity in the responses
56 of complex systems to human intervention^{17–20}. This often includes an understanding that ecosystem
57 responses to management actions can be slow. Underappreciated is the fact that long transients can occur
58 even in the absence of human intervention or changes in exogenous drivers, and that observations of
59 transient behavior in one system may appear as identical to asymptotic behavior in another system. If we
60 cannot distinguish between transient and asymptotic states, how can we manage for the future? What are
61 the consequences of failing to recognize a long transient? What are the relative costs when typical
62 management interventions interact with transient (versus asymptotic) dynamics? Here, we offer formal
63 explorations of the intersection between transient dynamics and ecosystem management, with the aim of
64 supporting adaptive management approaches and programs, and recommend that the adaptive management
65 framework incorporate assumptions about long transients (see Fig. 1).

66 Models that capture underlying system dynamics can be helpful in elucidating implications of long
67 transients for managing ecosystems. Closing the gap between theoretical studies and management
68 applications is an ongoing challenge, as summarized for the control of invasive species by Funk et al.²¹. As
69 they note, and as is backed up by a survey on incorporating climate change into management²², managers
70 are often eager to be able to incorporate results from ecological theory, but there are substantial barriers.
71 Here we use several models to illustrate some of the consequences of management actions for different
72 ecological systems with transient dynamics. Finally, we offer some general rules of thumb for managing
73 ecosystems, revealed by the case studies, that accommodate the ubiquity of transient behavior in ecological
74 systems.

75 2. Exploring management with long transients

76 We explore the consequences for management of long transients in ecological systems, using simulated
77 examples of long transients under potential management strategies. We use these models as a way to
78 develop a general understanding of how to manage in the face of transients. This both provides a guide to
79 cases where not enough is known to justify a detailed model and highlights how to develop approaches
80 when more detailed modeling efforts are justified²³. For each example, we associate an underlying
81 mechanistic model with the case, use the model to replicate the long transient, identify key features of the
82 dynamical landscape (e.g., saddles and ghost attractors) that have implications for management, and
83 evaluate management strategies under assumptions of transient versus asymptotic behavior.

84 *2.1 Marine Protected Areas: Managing transient responses in long-generation species*

85 Fisheries related to marine protected areas (MPAs) illustrate the importance of considering
86 transients, which may be long from a management standpoint, even if not in number of generations. From
87 a single species perspective, establishment of a marine protected area should change both the equilibrium
88 population level and the equilibrium age distribution of harvested fish species with relatively sedentary
89 adults by removing an age-specific mortality source, namely harvesting. A potential challenge in the
90 evaluation of the effectiveness of the marine protected area arises from not considering the transient nature
91 of the response and instead comparing the state of populations after too short a time to a new expected
92 equilibrium distribution. The arguments can be made more precise, but intuitively starting from the idea
93 that multiple generations would be required to approach a new equilibrium means that fish with a high age-
94 to-maturity, which implies long generation times, will take many decades reach a new stable state. More
95 details describing the general theory are given in several analyses of single population models with age
96 structure²⁴.

97 From a management standpoint, these issues become important in evaluating MPAs that have been
98 recently established, such as those created under the auspices of the California Marine Life Protection Act.

99 Here, a first challenge is that management evaluations regarding success or failure of MPAs to increase
100 previously-fished populations may be made on a relatively short time frame. Understanding the time frame
101 of the response, i.e., the length of the transient, is key²⁵. So even an examination of the simple conservation
102 implications of protection depends on an understanding of transients.

103 The goals of MPA establishment are much broader than increasing biomass inside the protected
104 area. After implementation of a marine protected area, one goal is to increase and stabilize yield from a
105 fishery that will be now be restricted to the part of the habitat where fishing is allowed. Such a scenario has
106 been analyzed using a two-patch metapopulation model with one fished area and one reserve area²⁶.
107 Understanding the transient response in yield is key to understanding how long-term goals for yield can be
108 met, even though yield may be reduced over the short term. If the results are extended beyond the linear
109 effects of age structure to include density dependence and interactions between species, as in the following
110 examples, the importance of transients for understanding the response of the system to management actions
111 becomes even more evident.

112

113 *2.2 Invasion dynamics: Managing to stay on a low impact transient*

114 Suppose a non-native species arrives where a native competitor population is growing. If this low-
115 invader state is a transient due to a saddle crawl-by, versus a stable equilibrium (see Box 1 for definitions
116 and Fig. S1 for an illustration), preserving the system near this state may require perpetual, repeated
117 manipulations to move populations toward the stable manifold of the saddle. Manipulations that get closer
118 to the stable manifold will be most effective because the subsequent crawl-by is expected to be slower. If
119 we mistake the low-invader state for an equilibrium, our decision for how to manage could have disastrous
120 outcomes.

121 To illustrate this, we use a stochastic Lotka-Volterra competition model, which has an equilibrium
122 at $(N_1, N_2) = (K_1, 0)$ (N_1 is the density of the native with carrying capacity K_1 , and N_2 is invader density).

123 Our stochastic term allows immigration to re-establish populations after local extinction (Supplementary
124 Information), reflecting the fact that complete eradication is often unrealistic. Because invaders are initially
125 rare, $(K_1, 0)$ appears to be an attractor early on (Fig. 2A). However, if $(K_1, 0)$ is a saddle as in this
126 simulation, the dynamics will eventually crawl by this state as the invader establishes (Fig. 2B). In this
127 simulation, active management that promotes repeated crawl-bys of the saddle at $(K_1, 0)$ are required to
128 avoid establishment of the invader. Examples of such actions include invader removal (orange arrow, Fig.
129 2C), removal of both species i.e., to maximize the chance of reducing the invader to 0 (light blue), and
130 invader removal with native addition (red), because each of these moves the populations toward the stable
131 manifold of $(K_1, 0)$. Native addition alone (dark blue arrow) will not promote crawl-bys and is therefore
132 not predicted to be effective for managing this invasion. To confirm, we simulated the same model applying
133 one of these actions whenever the invasive population crossed a threshold value ($N_2 > 0.02$), provided the
134 last management action was at least a year ago (Fig. 2D). Indeed, native addition alone (dark blue trajectory)
135 requires much more frequent management and is much worse at controlling invader density than the other
136 strategies (Figs. 2D, S2-S3). Removal of both species (because we assume this makes it possible to get the
137 invader density closer to 0) is the most effective (Figs. S2-S3).

138 If we did not know $(K_1, 0)$ to be a saddle, we might reasonably conclude from data such as
139 simulated in Fig. 2A that it is actually a stable node. To understand the implications of this mistake, we fit
140 the Lotka-Volterra equations to simulated time series, assuming that $(K_1, 0)$ is a stable node. Evaluating
141 management options using this model would lead us to conclude that all strategies perform comparably
142 (Fig. 2E). If N_1 addition were the least labor-intensive (e.g. seed addition or stocking), it would likely be
143 chosen – a costly mistake (Fig. 2D). If we instead fit the Lotka-Volterra equations with $(K_1, 0)$ as a saddle,
144 we regain the insight that native addition is an inferior strategy, although due to parameter uncertainty, we
145 may underestimate how much so (Figs. 2F, S2-S3). At a more basic level, if a monitoring program was
146 directed solely at detecting the invasive species, i.e., the primary system component of interest, and not also
147 its competitor, i.e., a secondary system component, management strategies would be inadequate. We also

148 found that standard statistical time series approaches misspecify the dynamical landscape in this case
149 (Supplementary Information), making it easy, for example, to mistake a saddle for a stable equilibrium.
150 This illustrates that management interventions based on time series analyses that do not account for transient
151 dynamics can be at high risk of failure. An understanding of ecological dynamics can provide the basis for
152 invasive species management²⁷, as demonstrated for forest insect pests, and these lessons provide a
153 framework for other management problems.

154

155 *2.3 Grassland restoration: Managing to escape an undesirable persistent transient*

156 In long-term ecological research experiments at the Cedar Creek Ecosystem Science Reserve in
157 Minnesota, the competition between a biodiverse collection of native grasses and a duo of exotic European
158 species was studied before, during, and after several years of nitrogen deposition (representing increases in
159 atmospheric and/or agricultural nitrogen). The native grasses are only able to resist invasion by exotics in
160 a low nitrogen environment; therefore, during the years of nitrogen deposition, the system flips from a
161 native-dominated state to a less biodiverse, exotic-dominated state. More surprisingly, following cessation
162 of nitrogen deposition, the exotic-dominated state persists for decades, even after soil nitrogen levels have
163 returned to their original low state²⁸. In a case where biodiversity is a management objective, and the
164 identified major stressor is nutrient inputs, the lack of system response to manipulating the stressor is a
165 management challenge.

166 The observations suggest that in a low nitrogen environment the native-dominated state is stable,
167 and in a high nitrogen environment the exotic-dominated state is stable. Two possible hypotheses exist for
168 the persistence of the exotics after cessation of the nitrogen deposition: Hypothesis 1, where both the exotic-
169 dominated state and native-dominated state are stable in a low nitrogen environment (in other words, the
170 system is bistable), so cessation of nitrogen deposition does not return the system to the native-dominated
171 state; and Hypothesis 2, where in a low nitrogen environment the exotic-dominated state is a saddle point,
172 and because the system was brought close to the saddle by the years of nitrogen deposition, after cessation

173 of that deposition it exhibits a long transient, slowly crawling by the saddle before eventually recovering to
174 the biodiverse native state.

175 From a management point of view, if the goal is to restore biodiversity, Hypothesis 1 suggests that
176 management is definitely needed to escape the basin of attraction of the exotic-dominated state. Hypothesis
177 2 is more encouraging; the biodiverse state is expected to eventually recover on its own. But a delay of
178 decades before this recovery occurs may be undesirable, so management may be needed to speed the
179 recovery. One mechanism that has been proposed for what holds the system close to the exotic-dominated
180 state, causing stability (Hypothesis 1) or a long transient (Hypothesis 2), relates to the differing rate of
181 accumulation of leaf litters of the exotics versus native plants²⁹. In similar Park Grass experiments in
182 England, where the experimental plots were hayed twice yearly (mowed and leaf litter removed³⁰), the
183 biodiverse state recovered quickly.

184 In Brettin et al.³¹ and Meyer et al. (in prep.), a model of the Cedar Creek system is developed,
185 tracking the amount of nitrogen in the soil and in live and decaying plant tissue as the native and exotic
186 plants compete. Inspired by the Park Grass experiments, the model system can be hayed regularly using a
187 “flow-kick” approach, where the system is “kicked” by removing organic matter sources, then “flows” to
188 a new state on the dynamical landscape³². Biodiversity in the model system can be recovered by haying in
189 both low and high nitrogen environments, with differing levels of haying effort needed depending on model
190 hypotheses and parameters. This model approach could be used to explore trade-offs in management
191 regimes that combine some balance of nitrogen reduction vs haying in grassland maintenance and
192 restoration. Management intervention can speed the system towards recovery of the biodiverse state in both
193 the transient and asymptotic systems, but an additional option of low or no investment exists only if the
194 system is in a long transient.

195

196 *2.4 Lake eutrophication: Managing to escape a ghost attractor*

197 Reduction of phosphorus loading to freshwater lakes is a widely-used best-practice strategy to
198 reduce eutrophication^{33,22}. Simple heuristic models of a bistable regime can be used to illustrate that if
199 phosphorus reduction has been too limited, a lake may remain in a eutrophic stable state or in a bistable
200 regime (Fig. 3A, B). An alternative framing can be used to show that it is also possible for the system to
201 linger near a former attracting eutrophic state (Fig. 3C, i.e., ghost attractor, see Box 1 for definition) for
202 very long periods in a long transient.

203 This can be further illustrated using a general mathematical model of a system with alternative
204 stable states, applied to the case of eutrophication. Turbidity caused by high phosphorus loads consumed
205 by phytoplankton can be modeled³⁵ (Supplementary Information) to reveal the effects of the external
206 phosphorus input rate, a . A single attracting oligotrophic (clear water) equilibrium exists until a crosses a
207 threshold value, above which there are two stable states: one oligotrophic and one eutrophic, separated by
208 an unstable equilibrium (Fig. 3B). Further increases in a result in a single stable eutrophic state.

209 If there is a long transient, managers may impose a management action, monitor for decades and
210 see no change, then conclude the intervention has been unsuccessful. Instead, an adaptive management
211 strategy could be adopted, where the lake state is assessed periodically and further actions are taken to shift
212 the system to the desired oligotrophic state. We simulate these alternative management strategies and
213 assume a monitoring program returns lake state data every five years. If the lake is not in the desired state
214 after a 5-year observation period, phosphorus loading is further reduced (the parameter a is decreased by
215 either 0.01 or 0.1 (Fig. 4A, B). The model predicts that larger reductions in phosphorus inputs result in
216 shorter transients, while long transients are not uncommon for smaller reductions.

217 These simulations illustrate the tradeoffs between the magnitude and number of the management
218 actions and the time to reach the desired system state (Fig. 4C). For larger phosphorus loads below the
219 bifurcation threshold, the sequential application of more stringent nutrient reductions can speed the
220 attainment of an oligotrophic state when the system is in a long transient (Fig. 4B). An alternative approach

221 is to manage a state variable such as the internal phosphorus pool, for example by adding alum to lock
222 phosphorus in the sediments of deep lakes, and in that way reduce probable transient length (Fig. 4C). The
223 challenge facing managers is that restricting assessment to the period immediately following intervention
224 can have either catastrophic³⁶ or cost-prohibitive³⁷ effects. Management could take a longer view and weigh
225 the costs and benefits of additional intervention, novel intervention (i.e., changing state variable versus
226 parameter), and waiting. In a review of eight European and US lakes, Fastner et al.³⁸ noted that in all cases
227 phosphorus reduction was highly successful, although the response times varied from 5 to 30 years. When
228 there is a failure of phytoplankton to respond to management in a given timespan, other explanatory
229 mechanisms such as low water exchange rate, internal phosphorus release from sediments, or changes in
230 community structure³⁹⁻⁴¹ are sought, but long transients is another possibility, and one which could alter
231 our management response.

232

233 *2.5 Social-Ecological System: Managing to avoid a transient induced by slow and fast
234 time scales*

235 Here, as an illustration of management of a system with long transients owing to the interaction of
236 slow and fast variables¹⁵, we consider a model of a simple social-ecological system, based on a typical
237 midwestern United States lake with a sport fishery and lake residential development⁴² (Fig. 5). In this
238 system, there are two primary management objectives: a resilient fish population, and a human population
239 of visiting anglers and lake residents. The “fast” dynamics are trophic interactions among harvested (target),
240 predatory, and juvenile fish⁴³. Survival of the juvenile fish is governed by lake habitat, in the form of woody
241 debris (dead and downed trees)^{44,45}. Local and visiting anglers harvest adults of the target fish species.
242 Management occurs via harvest rules governing the per-angler catch in the sport fishery. Stock status and
243 harvest rules feed back to human angling effort and lakeshore development. Increased residential
244 development on the lake reduces woody debris, via removal of logs (to clear beaches for swimming, for
245 example) and deforestation of riparian trees, the source of woody debris^{46,47}. Reduced residential

246 development allows forest regeneration and woody debris accumulation, the “slow” variable that occurs at
247 the pace of tree growth and senescence, which can take decades. In this model, there are two equilibria in
248 the trophic dynamics, where harvest and fish recruitment rates balance: one is stable, and one is unstable.
249 Movements of the system away from the unstable equilibrium, for example in the case of lower recruitment,
250 can lead to depensatory dynamics and collapse of the target fish population. Changes in habitat can increase
251 or decrease the basin of the stable state.

252 Harvest rules can either be fixed, with a constant harvest rate, or adaptive, with harvest rate adjusted
253 based on information about the target fish stock status. Because of the feedbacks between habitat, fish
254 populations, harvest, and residential development, and the combination of slow (coarse woody debris
255 recruitment) and fast (harvest and trophic dynamics) variables in the system, long transient periods between
256 collapse and rebuilding can occur under fixed management rules (Fig. 6 A,C). Knowledge of the impact of
257 the slow variable, coarse woody debris supply, informs an adaptive management approach. During these
258 long transients, the model predicts both human participation and fish are lost from the system. Under no
259 harvest of the target fish, human participation is lost from the system (Fig. 6C). However, under adaptive
260 management rules, where harvest rates are adjusted in response to stock assessments of fish while
261 accounting for both slow and fast variables in the system, i.e., primary and secondary system components,
262 the system can remain in the desirable state, avoiding the long transient recovery phase after a collapse and
263 meeting both the social and ecological objectives (Fig. 6 B,D).

264

265 *2.6 Three species food chain: Managing to maintain chaotic transient persistence*

266 Transient dynamics can also have special implications for species extinction. In particular, model
267 explorations show that when population dynamics exhibit transient chaos^{48–50}, population densities change
268 chaotically for a finite period of time before suddenly converging to a stable equilibrium that may represent
269 asymptotic extinction of some species. Therefore the population dynamics of some species can appear to
270 be chaotic and apparently sustainable for a long time, and then move to extinction in a relatively short

271 period of time^{10,51}. This is associated with a chaotic ghost or a chaotic saddle¹⁶. If species extinction is
272 caused by the end of transient chaos, how can we intervene to prevent extinction^{52–55}?

273 A potential management strategy that maintains this transient chaos, and avoids extinction, can be
274 illustrated with a three-species food chain model⁵¹ (Supplementary Information). The resource and
275 consumer alone (without the top predator) can exhibit consumer-resource cycles, and so can the consumer
276 and predator, if the resource level is fixed. When the three species are together, the interaction of these
277 coupled nonlinear oscillators in the food chain can give rise to transient chaos.

278 For particular parameter settings (see Supplementary Information), the species can undergo chaotic
279 oscillations for a long, but finite, amount of time before converging on a consumer-resource limit cycle at
280 which the top predator is extinct. Predator extinction can be prevented by continually pushing the system
281 toward the chaotic saddle – in which all three species persist – indefinitely via small feedback control^{56–58}.
282 In general, the perturbations need to be applied only rarely, although they will be required in perpetuity
283 because the desired state is a transient. Because of the presence of a long chaotic transient, the magnitude
284 of the applied management perturbation can be made arbitrarily small⁵⁹. This suggests that the natural
285 dynamics of the populations need hardly be affected and yet predator extinction can be prevented over long
286 time scales.

287

288

289 3. General guidelines for management

290 Understanding the potential mechanisms that cause transient behavior leads to several subtle
291 enhancements of adaptive management frameworks to better account for transients (Fig. 1). Understanding
292 ecosystems as dynamical, transient, adaptive systems immediately shifts expectations about management
293 strategies and their impacts. While the resilience approach to managing ecosystems is increasingly well
294 known⁶⁰, and while expectations of nonstationary responses to management action underpin adaptive

295 management approaches⁶¹, the potential for long transients in the absence of changing environmental
296 conditions or management intervention is underappreciated in resource management. This tension is
297 reflected in, for example, the existence of two paradigms of rangeland vegetation dynamics: one that
298 assumes continuous and reversible vegetation dynamics versus one that encompasses nonlinear and
299 transient dynamics⁶². Fisheries management systems are often exceptions to this; for example, the Pacific
300 sardine fishery in the Gulf of California has experienced long transient behavior, and managers are now
301 grappling with how to manage the ecosystem under assumptions of transience⁶³.

302 We recognize that our work here is a small step towards producing the kind of information that
303 would be directly useful to practitioners, and that application of the ideas we develop here will require
304 further steps. Our contribution here is to indicate important issues that need to be taken into account when
305 developing plans for specific systems. Our work does emphasize the need to consider transients when
306 managing in the face of climate change and does provide the kinds of general principles that are important.
307 Here, we offer some general rules of thumb for accommodating the potential of transient behavior in natural
308 ecosystems.

309 *3.1 Plan*

310 The planning of management strategies should account for potentially lengthy transient dynamics
311 by evaluating the feasibility of management goals, the associated level of intervention required, and the
312 costs and benefits of maintaining a system in a transient state via intervention. This can be achieved in part
313 by confronting inherent assumptions about the system, such as whether the observed behavior is asymptotic
314 or transient. The development of alternative management actions is then informed by framing management
315 objectives according to whether the aim is to remain in the current state or leave it.

316 In general, the models upon which management actions are based should be subjected to a form of
317 “sensitivity analysis” that accounts for the risk of getting the dynamical regime of the system wrong
318 (equilibrium vs. transient). Mechanistic mathematical models that are constructed from first principles, fitted
319 to empirical data, and explored within realistic parameter ranges can help identify whether an ecosystem is

320 currently experiencing transient dynamics. For example, this was done to predict the long transients in the
321 extinction debt of butterflies in the UK⁶⁴. In addition, correctly identifying the likely transient mechanism,
322 where possible, can inform adaptive management strategies, such as the magnitude, direction, or target of
323 intervention. For example, the grasslands example suggests a flow-kick strategy for crawl-by transients;
324 while the lake eutrophication example suggests the best strategy for a ghost attractor may be a combination
325 of interventions targeting both system parameters and state variables. In some cases, exploitation of
326 transient dynamics, such as episodic booms in growth and reproduction, could be beneficial to management,
327 if properly identified⁶⁵.

328

329 *3.2 Implement Actions*

330 In addition to adjustments in management perspective, the implementation of management plans
331 may require revision to accommodate dynamical regime behavior. For example, in the Puget Sound estuary
332 of Washington State, USA, many recovery targets for a suite of ecosystem health indicators are based on
333 historical baselines, or ecological models that assume asymptotic behavior
334 (<https://www.psp.wa.gov/vitalsigns/>). In contrast, other management efforts are aimed at maintaining the
335 system in a transient state. For example, fishery harvesting targets may be aimed at maintaining a population
336 at its most productive density rather than the carrying capacity. Vaccination plans may not be able to
337 eliminate a disease (i.e., an asymptotic target), but aim to maintain the incidence rates at a very low, non-
338 equilibrium value and limit the size of any transient outbreaks. Plans that account for possible long transient
339 behavior will inherently be more resilient to unexpected system change.

340 Mathematical properties of transients may also translate into management rules of thumb. For
341 example, analogous to supporting management strategies that increase resilience by deepening or
342 broadening desirable basins of attraction (e.g., ⁶⁶), management strategies that aim to regularly place the
343 system along the stable manifold associated with a desirable saddle equilibrium can avoid settling at
344 unwanted attractors, as in the invasive species example given here. Modeling approaches that highlight the

345 most important state variables and parameters may be useful here, including the use of multiple models⁶⁷
346 and constructing models of intermediate complexity^{68,69}.

347

348 *3.3 Monitor*

349 Incorporating considerations of transient system behavior into management requires shifting
350 perspectives about the relevant timescales⁸. Observational data are often of insufficient duration to be
351 inclusive of the true asymptotic behavior of the system (but see ⁷⁰). If a change is observed, the inclination
352 is to wait longer (longer experimental runs, more system monitoring) for the system to revert to a stable
353 state; but this approach is ineffective if the system is in a long transient. Predicting how long a transient
354 may last is a particular challenge, as noted in the above lake eutrophication example, and a nominal amount
355 of stochasticity can increase greatly the time a system spends away from stable equilibrium. Furthermore,
356 high dimensionality in any domain – temporal, spatial, biological – can increase the potential for transient
357 behavior and the likelihood of its lingering. Programs that invest resources into monitoring at temporal and
358 spatial scales sufficient to encompass system dynamics, including fast and slow variables and feedbacks,
359 will most effectively accommodate transient behavior. Likewise, expanding monitoring programs to
360 include responses of primary and secondary components of ecosystems to management actions increases
361 the likelihood of appropriately capturing system dynamics.

362

363 *3.4 Learn*

364 The most effective way to learn about a system is to conduct an experiment, and indeed large-scale
365 experiments have resulted in some of the most powerful ecological lessons. While mathematical models of
366 the type presented here offer insights into the potential behaviors of natural systems, direct observation
367 following controlled manipulation is invaluable. The long-term grassland experiments at Cedar Creek
368 Ecosystem Science Reserve³¹ and the Park Grass Experiment⁷¹ allowed for observations about system
369 dynamics that inspired insights into long transient system behaviors. Large-scale and long-term

370 manipulations of lakes are another example where learning through manipulation reveals unexpected
371 system behaviors⁷². Marine protected areas or predator control programs are additional forms of
372 experimentation, albeit one with looser control over experimental boundaries. The network of Long Term
373 Ecological Research (LTER) sites, of which Cedar Creek is one member, have provided a wealth of insights
374 into system behaviors that play out over longer time scales, including tipping points, bistability, and long
375 transients⁷³⁻⁷⁷.

376 Governance systems that are flexible to timescale mismatches and multiple types of learning will
377 be most successful in managing transient behavior^{78,79}. Characterizing uncertainty, as a target of “learning
378 by doing,” is an important component of adaptive management⁸⁰. Whether observed dynamics are
379 asymptotic or transient is yet another relevant uncertainty for management. Evaluation of the effectiveness
380 of management actions related to managing regime shifts can be confounded by long transients. For
381 example, removal of planktivorous fish from Lake Christina in Minnesota to reduce eutrophication resulted
382 in persistent clear water states that lasted as long as 10 years after manipulation, but always degraded to a
383 turbid state over time. Long-term data suggest that the clear water state is now a transient and the turbid
384 state the sole stable state in this system due to changes in nutrient loading and the water regime³⁷; the clear
385 water state is only maintained through continual management action. Identifying the appropriate adaptation
386 of the management program in this case depends upon conceptualizing the transient system behavior.

387

388 4. Conclusion

389 Adapting to environmental change is one of the greatest challenges facing natural resource
390 management. Adaptive management practices are increasingly favored, enhancing opportunities for
391 learning about system dynamics and successful approaches. Here, we argue that subtle enhancements to
392 adaptive management frameworks and thinking are needed to account for long transients in ecological
393 systems, given their ubiquity and the risks associated with ignoring their potential effects. Understanding

394 that observed dynamics may not be the final dynamics, and considering possible mechanisms driving
395 current patterns, can reduce such risks substantially, leading to better outcomes.

396 **References**

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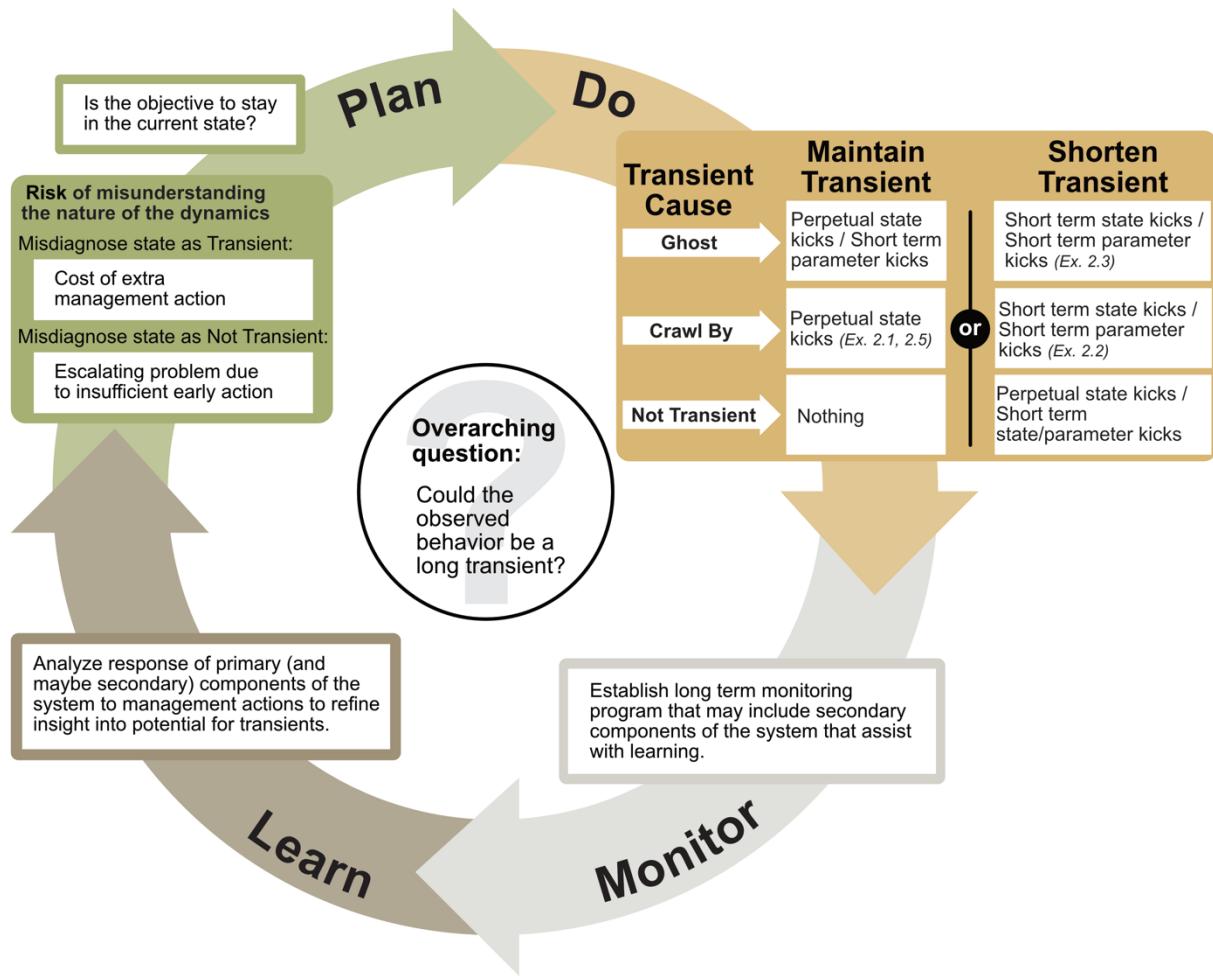
561 **Figures**

562 Box 1: Dynamical Systems Terminology (see Fig. S1 and ^{15,81,82} for further explanation)

Asymptotic dynamics	The behavior that a system will eventually exhibit and then retain indefinitely, if unperturbed; i.e. dynamics that are not transient.
Attractor	An invariant set that a dynamical system will naturally approach, unless perturbed away; an asymptotic state of the system.
Bifurcation	A qualitative change in a system's asymptotic dynamics, caused by gain, loss, or change in stability of an invariant set. Some examples that play a role in this review are crises, Hopf bifurcations, and saddle-node bifurcations.
Crawl-by	Dynamics that approach and then move away from a saddle slowly, causing the system to remain near the saddle for a significant time frame; amplified when the saddle is surrounded by a flat spot.
Flat spot	A region of the potential or quasi-potential surface that has very little curvature, so that the dynamics in this region (like the hypothetical ball rolling on this surface) are slow.
Ghost	A state or set of states that is not an invariant set under the current conditions, but was (or would be) an attractor under similar conditions, such as nearby parameter values.
Invariant set	Ecosystem states (like stable or unstable point equilibria or cyclic or chaotic sets) such that, if the ecosystem is precisely in one of these states, it will remain there in perpetuity unless perturbed.
Long transient	Non-asymptotic dynamics that persist over ecologically-relevant time scales of, roughly, dozens of generations or longer.
Node	A point equilibrium that is approached (if attracting) or departed from (if repelling) without oscillations.
Repellor	An invariant set that a dynamical system will naturally diverge away from, unless perturbed toward it.
Saddle	An invariant set that is attracting from some states and repelling from others; the dynamics may approach a saddle before ultimately moving away.
Slow-fast systems	Systems that incorporate processes that act on drastically different timescales, such as interacting species with very different generation times.

563

Adaptive Management with Transients

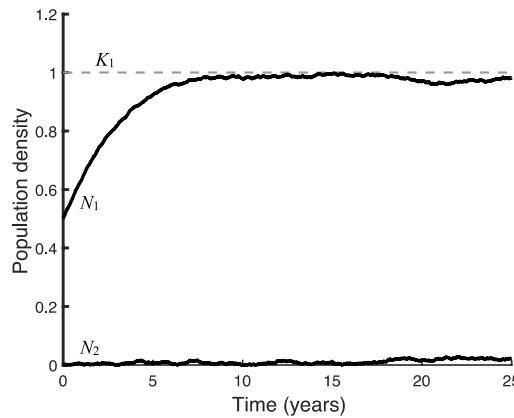


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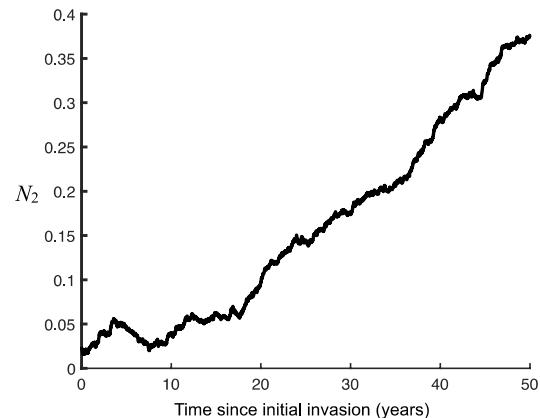
565 Figure 1: A modified adaptive management cycle that includes consideration of potential long
 566 transient system behavior. In general, the question of whether the observed behavior system
 567 could be a long transient should inform management. During the planning phase ("Plan:"),
 568 managers should consider the potential risks associated with mis-specifying the system
 569 dynamics, and categorize management objectives in terms of whether the goal is to remain on or
 570 leave the current state. Management actions, or interventions ("Do"), are thus informed by this
 571 objective, with implications for the type, duration, and cost of interventions that vary by transient
 572 type. Monitoring programs ("Monitor") should be designed as long-term programs to capture
 573 multiple life cycles of the primary ecosystem components, and of important secondary
 574 ecosystem components whose interactions have strong influence on primary components.
 575 Finally, learning from the system responses to management actions ("Learn") should include
 576 evaluation of potential transient behavior, and analysis of the secondary components of the
 577 ecosystem to refine insight into system dynamics.

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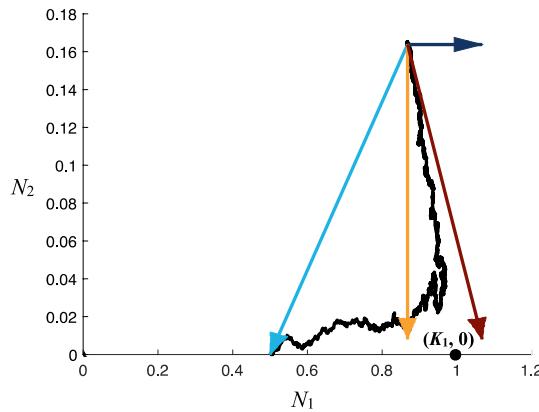
(A) Initial invasion (pre-management)



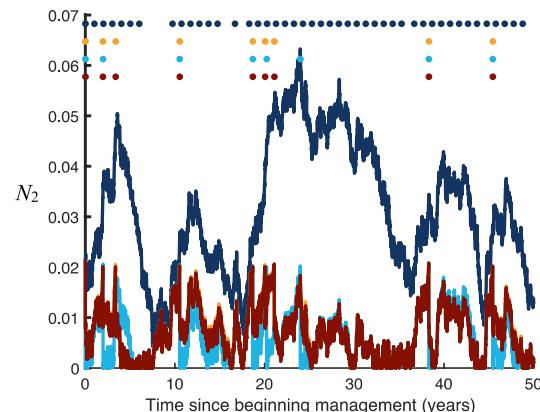
(B) Subsequent invader dynamics without management



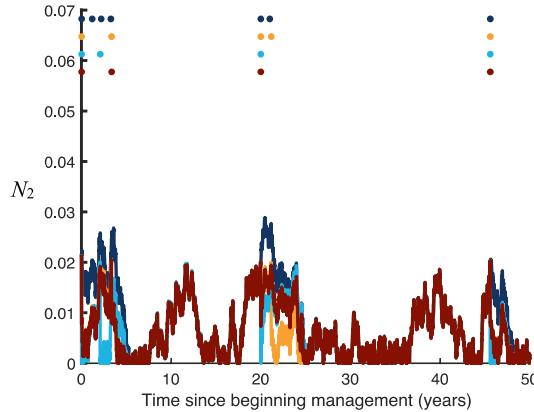
(C) Illustration of management actions



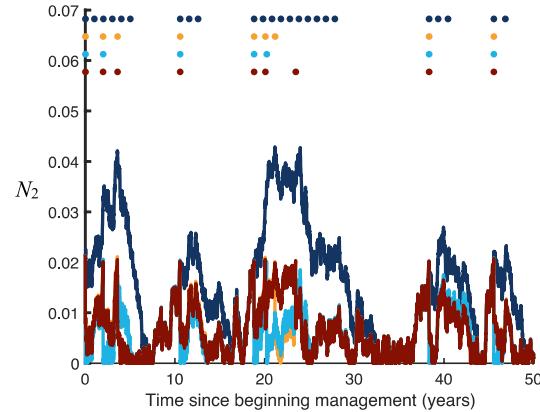
(D) Management applied to true model (saddle at $(K_1, 0)$)



(E) Management applied to fitted model with node at $(K_1, 0)$



(F) Management applied to fitted model with saddle at $(K_1, 0)$

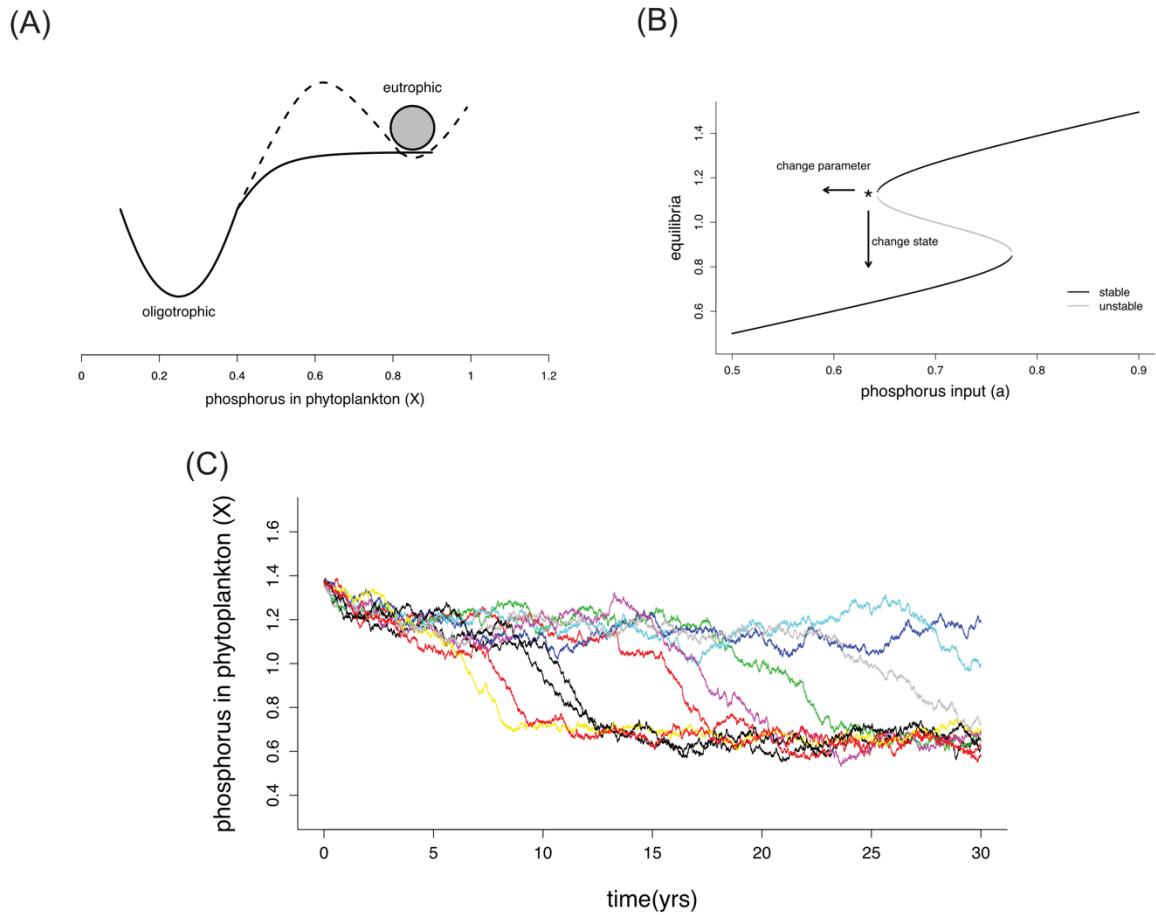


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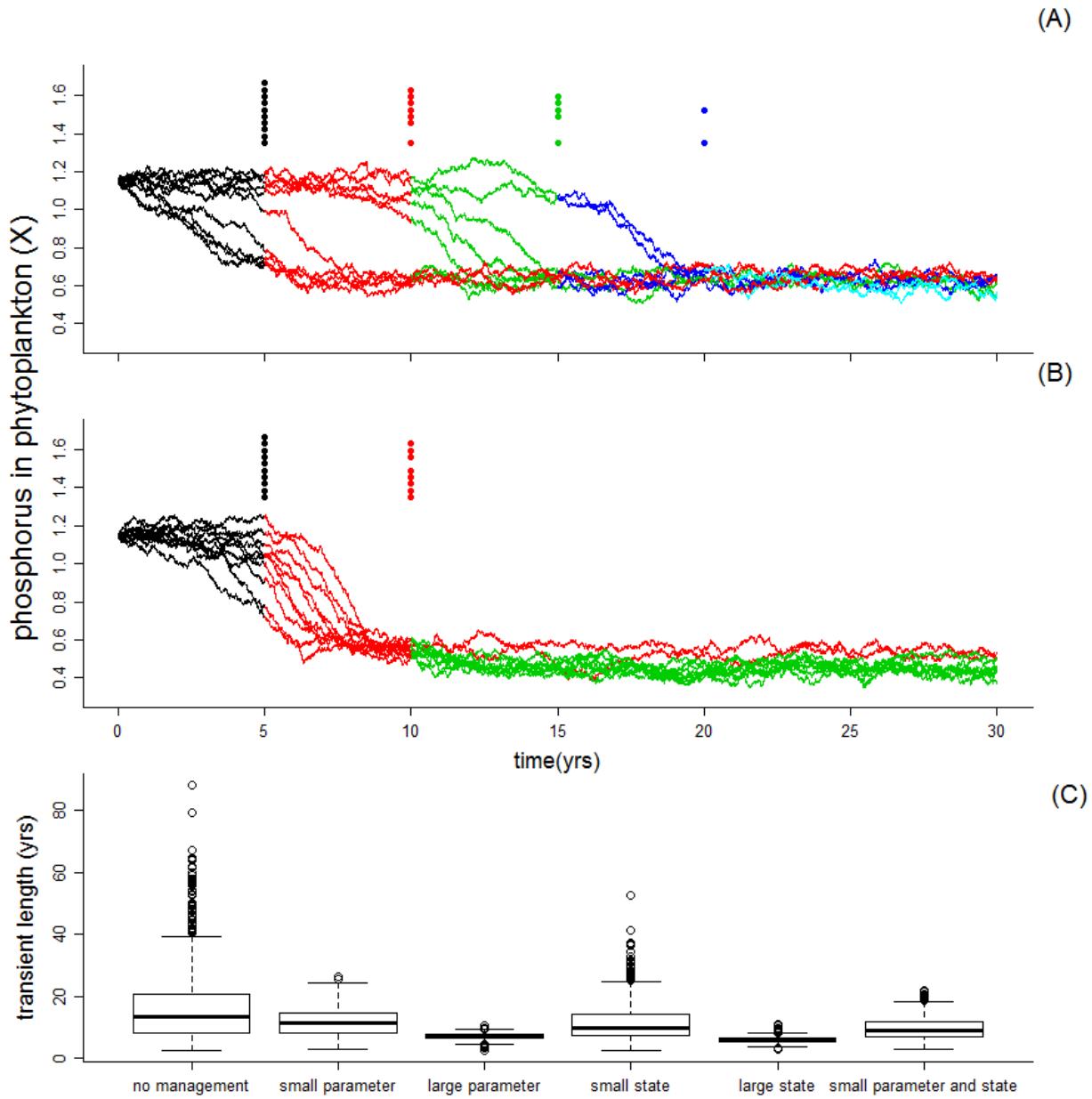
580 Figure 2: From Example 2.2. (A) Example times series from a realization of the stochastic
581 Lotka-Volterra competition model (see Supplementary Information), where N_1 is the population
582 density of the native species (with carrying capacity K_1) and N_2 is the density of the invader. (B)
583 A simulation of the unmanaged invader population under the same conditions as (D-F), as a
584 baseline. (C) Illustration of relevant features of the state space. The black trajectory shows the

585 combination of (N_1, N_2) population densities through time, proceeding counterclockwise. Arrows
586 show the effect of each management action (light blue: removal of both species; orange: N_2
587 removal only; red: N_1 addition with N_2 removal; dark blue: N_1 addition only). The x-axis is the
588 stable manifold of the saddle at ($K_1, 0$); this is the direction along which the saddle is attracting.
589 Management actions that move the system closer to the stable manifold promote additional
590 crawl-bys and sustain the transient ($K_1, 0$) state for longer. (D-F) Time series of abundance under
591 simulated management actions, with colors matching the management strategies illustrated in
592 (C). All four lines (as well as the trajectory in (B)) experienced the same sequence of stochastic
593 perturbations, so differences between the colored lines within a panel are due only to differences
594 in the management strategy. (Differences between panels are also due to differences in the
595 interspecific competition coefficients used in simulation.) Colored dots along the top of the graph
596 mark the times that a management action was triggered (i.e. times at which N_2 exceed 0.02 that
597 were at least 1 year past the previous management action) under each strategy.

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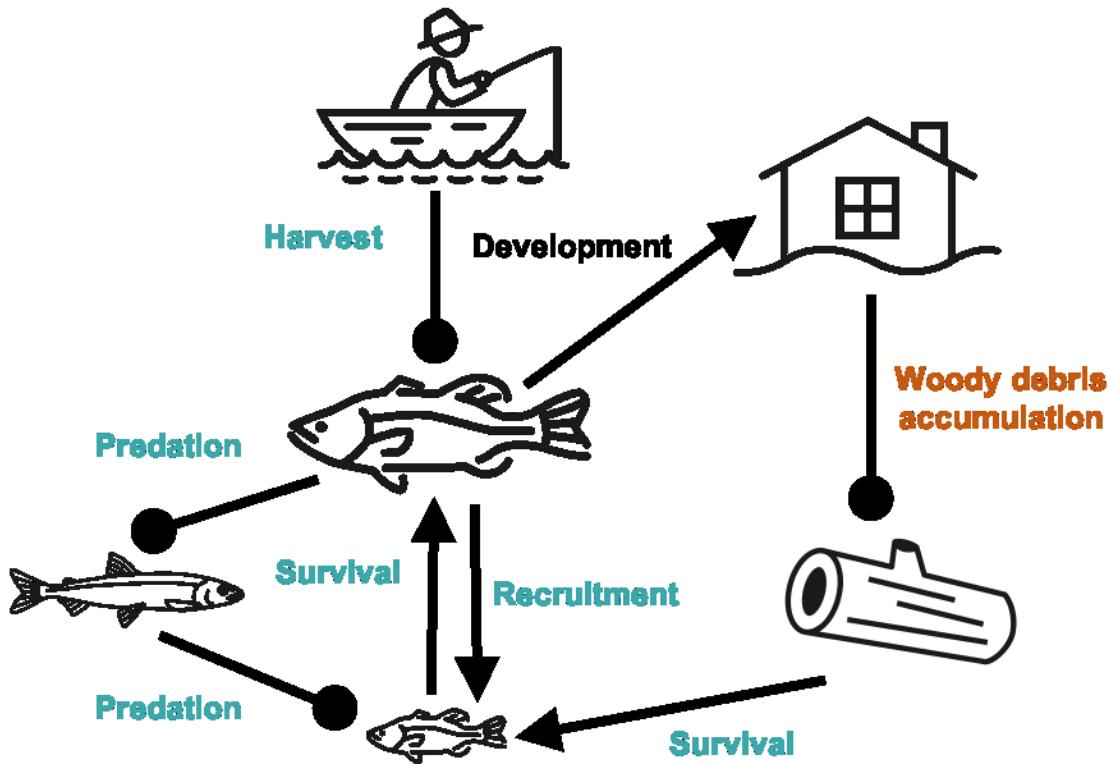


601 Figure 3: From example 2.4. (A) In this ball in cup representation of the lake system,
 602 management actions erode the stability of the eutrophic state (former stability given by the
 603 dashed lines), which shifts the landscape to the solid curve. However, the system (ball) remains
 604 close to the eutrophic ghost attractor for a long time. (B) Bifurcation diagram showing the
 605 current state of the system (*) and the value of the stable and unstable equilibria. (C) Example
 606 times series from realizations of the model (see Supplementary Information).



608

609 Figure 4: From example 2.4. A-B: Trajectories of lake turbidity moving from eutrophic
 610 conditions in the vicinity of a former attractor to a stable oligotrophic state. The lake is managed
 611 by re-evaluating every 5 years and, if not within 20% of desired state, the phosphorus loading (a)
 612 is reduced by 0.01 (A) or 0.1 (B) for each management event. The colour of the trajectory
 613 changes when a management action is taken, and dots above indicate the year of those actions.
 614 (C) Boxplots of time to reach the stable oligotrophic state for 1,000 replicate simulations for a
 615 close to the bifurcation boundary. The system is managed by evaluating lake state every 5 years
 616 and either reducing phosphorus loading, a, by 0.01 (small parameter) or 0.1 (large parameter);
 617 adjusting the system state down by 0.05 (small state), or 0.25 (large state); or adjusting both a
 618 and the system state by 0.01 and 0.05, respectively.

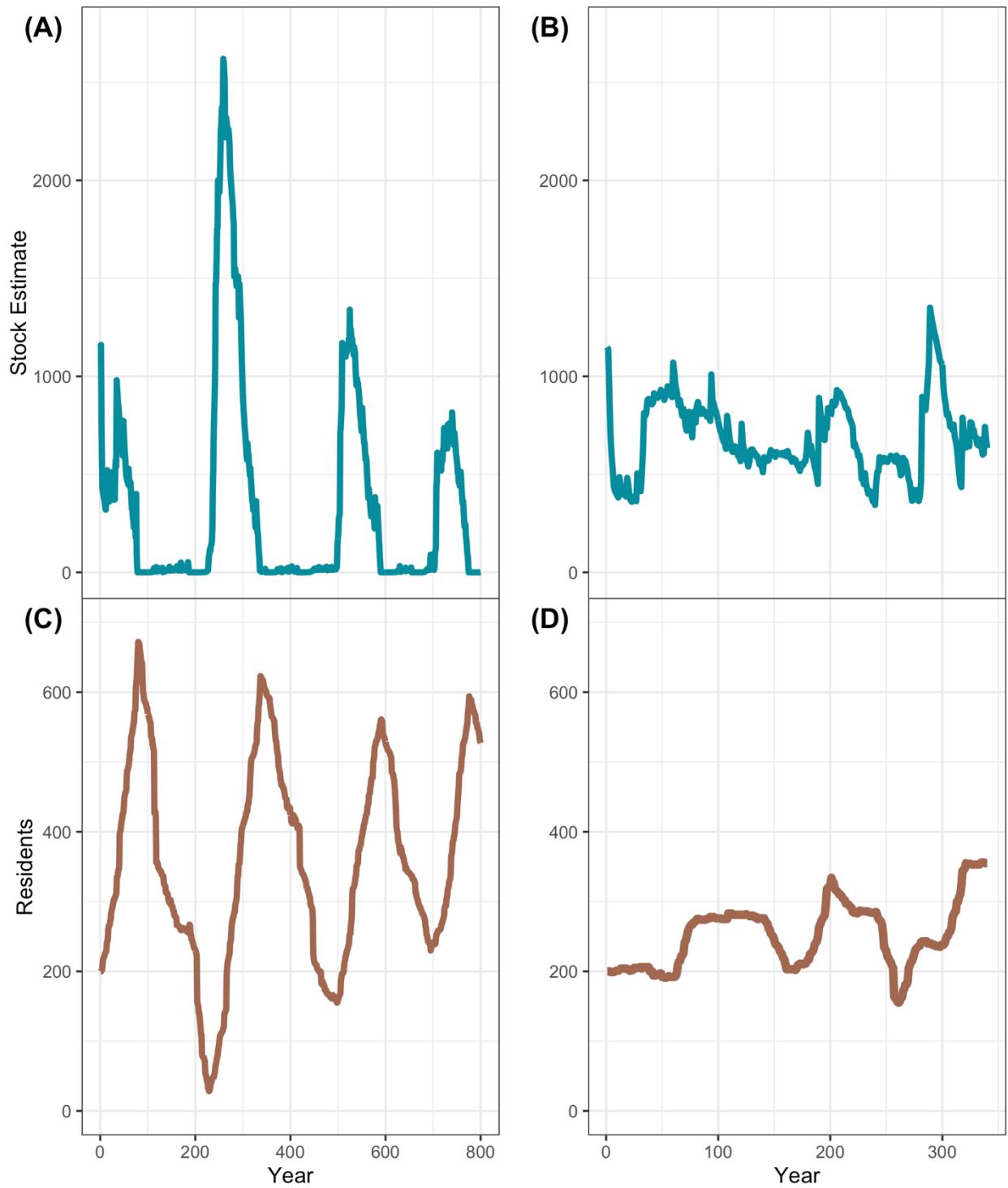


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620 Figure 5. Schematic of a social-ecological system with slow and fast variables that produces long
 621 transients under fixed management schemes. Dots are negative effects; arrows are positive
 622 effects. Fast variables are in blue; slow variables are in red. See text for additional description.
 623 Model adapted from Carpenter and Brock 2004.

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627 Figure 6: From example 2.5 Results of a fixed (A, C) versus adaptive (B, D) management
 628 strategy for a simulated social-ecological system showing target fish stock assessment (A, B) and
 629 human use of the lake (C, D). Note different x-axis scales; the longer time scales for the fixed
 630 management strategy shows the long-period cycles in the system.