Ultracold neutron properties of the Eljen-299-02D deuterated scintillator

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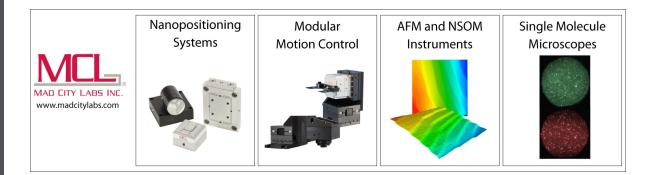
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experiments utilize trapped UCNs, which are neutrons with kine

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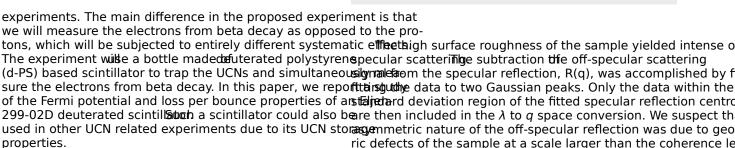
ABSTRACT

In this paperwe reportudies of the Fermipotentia and loss per bounce of tracold neutrons (UCNs) on a deuterated scintillator (Eljen-299-02D) hese UCN properties to fe scintillator enable its use in a wide variate variate variations in fundamental tron research.

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I. INTRODUCTION

energy less than 350 A while energy less than 360 A while energy less than In the Standard Modef particle physics, e free neutron total external reflection on materiaamdatuseir kinetic energy decay $(n \rightarrow p + \bar{e}_e)$ has a characteristic lifetime of about is on the same scale as their gravitatidmabgnetic potential 15 minThere are two different methods for measuringer energies he UCN bottle experiments utilize these UCN properiments that neasure the decay rate out from a cold neutron ties to trap the neutrons and measure numbers that remain after beams³ and experiments at measure the survival bottled a certain storage tinveith an average lifetime resofit879.5 ultracold neutrons (UCNsBy counting the number of protoes 0.4 sThese two methods differ by 8.7 s or 4.5 standard deviemitted from neutron beta decay in a well-calibrated cold ations (Fig1). Recently, some authors have suggested the possitron beamthe beam method measures the mean time for method beaution decay/oscillation channetseonfeutron decay trons to decay into protons, with an average result of 888.that bave so far eluded detection many experiments In the Standard Modehis time is equivale to taheuhave eliminated some of these decay¹charmels parameter tron lifetime with the exception metric process peutrons space still remains we propose a new experiment decaying into bound hydrogen atoms and electron antineuthenosutron beta decay lifetime by measuring the number of ne which has a calculated branching ratio $df 0^{7-9}$ The bottle trons and the number of beta decays similar to the beam lifetim



140

120

100

60

40

20

0

0

ntensity (A. U.) 80

II.FERMI POTENTIAL

methods with derror bands.

The Fermi potential of d-PS was measured using Asterbenationencertainty in the measurementingate the influence of flight neutron reflectometer at the Los Alamos Neutron Scattering Center (LANSCE). Asterix views a liquid moderator provid-

ing a pulsed polychromatic cold neutron beam with wavelengths λ , ranging from 4 Å to 13 Å he neutron beam divergence and spotsize on the sample were controlled by two settimating slits. Reflectivity, R(q), is defined as the ratio of the intensity of the reflected beam to the incident beam as a function of the neu tron momentum transfer vector normal to the reflecting surface, |q|, where $q = 4\pi \sin(\theta)/\lambda$. Total external reflection was measured up to a critical momentum transfer $\dot{1}6\pi\beta$ where β is the scattering length density of the sample. The relationship between β^2 and the Fermi potential_F, Vis given in Eq. (1), where the mass of the neutron,

$$V_F = \frac{2\pi h^2}{m_h} \beta. \tag{1}$$

Multiple neutron reflectometry experimentesperformed to measure **q**sing the polychromatic beam with incidence angles on the sample, ranging from approximately 00 m approxi-

mately 10% dq/q resolution. Scattered neutrons were colle FIG. 3. Neutron reflectometry data (symbols) and fits (lines) to d-PS for three sets a linear³He position sensitive detector as a function $df\lambda$, which simultaneously captured both the specular reflectiv and off-specular scattering originating from the surface ro of the fitted value. (Fig. 2).

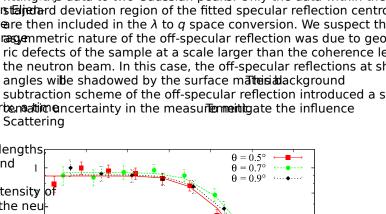
of incidentangles. An average scattering length density, was obtained by fitting the Fresnel reflectivity function to the multiple datasets. Three measurements

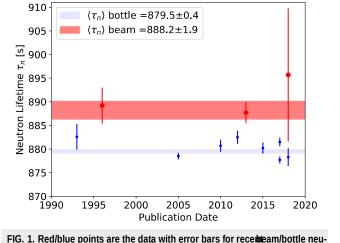
FIG. 2. Sample neutron reflectometry data for a neutron wavelength intervafi 10 Å-13 Å at 0.9[°]. The fit is a combination of two Gaussian fits centered around the specular and off-specular component.

1

Reflection angle (degrees)

0.014 0.015 0.016 0.017 0.018 0.019 0.02 $q(\text{\AA}^{-1})$





tron lifetime experiments. The red/blue bands are the average values for the two



Specular component Off-specular component

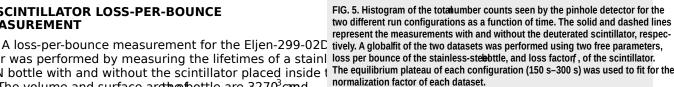
data $\theta = 0.9^{\circ}$ Combined fit

1.5

ARTICLE

0.5

FIG. 4. Schematic diagram for the loss-per-bounce measurement.



of background subtraction on the value of the Fermi potential, 10³ tiple measurements were made using different incident angles of neutron beam on the sample (Fig. 3).

The reflectivity curves were fitted using Fresnel's law for refle tion from an ideaInterfacewhich captureshe totalexternal nnt reflection of feutrons up to followed by a^{-4} drop in intensity. A normalization factor and the β for d-PS were the only the parameters used in the fit error estimates on the β parameters ter were based on² λ metrivalues obtained for β from fitting three independent measurements were $6.42^6 \pm 0.08 \times 10^{-10}$ $6.53 \pm 0.12 \times 10^{-2}$, and $6.48 \pm 0.11 \times 10^{-2}$, corresponding to Ferminotentials of 57.2 + 2.1 + 770.2 ing to Fermipotentials of $67.2 \pm 2.1 \text{ neW} / 0.0 \pm 3.1 \text{ neW} / d$ 168.7 ± 2.9 neWveraging the three measuremy eietds β of 6.48 ± 0.06 $\times^{6} 1^{20}$ ², corresponding to a Ferprotentia of 168.2 ± 1.5 neV.

III.SCINTILLATOR LOSS-PER-BOUNCE MEASUREMENT

lator was performed by measuring the lifetimes of a stain loss per bounce of the stainless-stebbtile, and loss factorf, of the scintillator. UCN bottle with and without the scintillator placed inside (The equilibrium plateau of each configuration (150 s-300 s) was used to fit for the tle.The volume and surface aretaefbottle are 3270³ cand 1350 cm respectivelynd the surface areat be scintillator is

292 cm The UCN bottle was connected to a port off the Losoxiameoselocity dependence of UCN entering the pinhole detect UCN source and was separated from the deuterium volum $\overline{q_B}$ by $\overline{s_B}^1$, $\overline{\tau_{binhole}}$ and $\overline{s_{eint}}$ represent the UCN loss rates due to neu-0.001 thick 1100 series aluminum foil aluminum foils a tron lifetime, stainless steel bottle, pinhole detector, and scintill calculated Fermi poterotial neVwhich sets the lower boundespectively,

10²

150

200

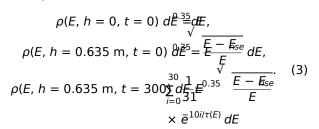
250

300

of the UCN energy spectrune bottle was raised 0.635 m from can have energy up to the Fermi potential of the nickel-phosphorus coated source guide (213 TeVS) ensures that the UCN will not $\tau(E)^{-1} = \overline{\beta}^{1} + \overline{s}(E)^{-1} + \overline{\beta}_{inhole}(E)^{-1} + \overline{s}_{cin}(E)^{-1}$. have enough energy to penetrate the Fermi potential of the scintilla-

tor (168 neV). The UCNs are loaded into the bottle for 300 n with paper, we used the initial velocity distribution as outlined upstream gate valves open. Once the UCN density is well seturate and 22, where the collision rate weighted velocity distr inside the bottle gate values are then classed he lifetime tion is $\rho v \sim \sqrt{2} \sqrt{T}$ This initial spectrum is then adjusted to account for curve of the bottle is extracted by monitoring the rate of UGN height difference and loading time as shown in here through a 0.635 cm diameter pinhole boron film (detector E and \vec{F}_{se} are the kinetic energies of the UCN and the rise in the The lifetime curves with and withthetscintillator are shown height of the beamline (64.8 neV), respectively. Here, we have a in Fig. 5. an energy range of 64.8 neV-186 neV for the initial spectrum. T

The analysis for the loss per bounce of the scintillator was affering of 186 neV was used instead of the source cut-of formed simultaneously using the two datasets: the loss peerbayy of 213 neV to match the Fermi potential of the stainless the stainless steel UCN bottle is a fitting parameter for both the stainless steel UCN bottle is a good approximation of and the loss per bounce of the scintillator is only relevant the the off energy of the spectrum since the UCN bottle is filled dataset with the scintillator. The spectral evolution model $y_{0} = y_{0} + f_{0} +$ UCN observed by the pinhole detector as a function of time u(E) The Los Alamos UCN source is pulsed at 0.1 Hz. To repre-the initial energy spectrum of the UCN, and $\tau(E)$ is the botten life time evolution of the initial spectrum properly, we sum time as a function of energy. An additional velocity weight activity spectra that have been evolved from t = 0 s to t = 300



Data No Scintillato Fit No Scintillato Data Scintillator Fit Scintillator

350 400

Time (s)

450

500

550

600

(2)

In our model we assume that initial elocity directions the systematic effects of input energy spectrum on the fit by of the UCN are sufficiently mixed that the kinetic theory for any ing the energy dependence of the results showed that interacting gas applies in the calculation of the wall interactive input energy spectrum varied from the χ + 1 region [Eq. (4)], where A is the total surface area of the material, with is the d franging from 4.86 to 4.94 χ 10 herefore we magnitude of the UCN velocity, and U is the volume of the both of the finate parameters to and μ_s and retained $\rho(E)$ A loss-per-bounce parameter, μ , is also added onto this equation to obtain the loss rate for each component,

 $\frac{1}{\tau_i} = \frac{A_i |v|_i \mu}{4U}.$ (4)

The measured is larger than a previous measurement of $3.5 \times 10^{4,24}$ but we suspect that the losses in both cases are dominately by the gaps in the joints of the vacuum assembly, and the gaps to volume ratio is smaller for long guides compared to our bottle or big by second to the discrepancy.

For μ_{s} we assumed an energy independent loss-per-bounce high accounts for the discrepancy. eter due to the combination of losses due to gaps in the system and the losses on the surface in the system are of uncertain the system and due to the UCN detector, which is a valid assumption since the field calculated value of the loss factor using the manufactur face area for the detector is 64 times larger than the surface of lementand isotopic omposition (97% deuterium the pinhole. For the anergy dependent loss-per-bounce modely) is 1×10 which is smaller than the measured value of that integrates over all incident angles is used where M_{1} , $4.9 \pm 0.8 \times 10$ which is smaller than the scintillator is due to is the Fermi potential of the scintillator, E is the kinetic energy is the private private for private the primary fluorescent emitter. One possible expotential. The fit for the loss per bounce in stainlessible and of is that the surface is rough at or below the UCN wavelend the scintillator is given as follows:

$$\mu_{scin}(E) = 2 \left[f \frac{V_F}{E} \sin^{-1} \frac{\sqrt{E}}{V_F} - \frac{\sqrt{V_F}}{E} - 1 \right].$$
 (5)

We have used an iterative approach in our analysis: first, init (a) guesses of fid μ_s are used to evolve the UCN energy spectrum to 300 schent that energy spectrum is used as an input into a global chi-squared minimization of two datasets. The iteration is comple when the initiguess values for fid μ_s match the centralues from the minimization, yielding a result. Of \pm 0.8 \times^4 10 for the scintillator and an energy independents per bounce for stainless steed $\mu_{ss} = 5.4 \pm 0.1 \times^4$ 100th $\chi^2/\nu = 177.17/177$. The error in the global determined by taking the limits of the $\chi^2 + 1$ region for the fits shown in Fig6. We also studied

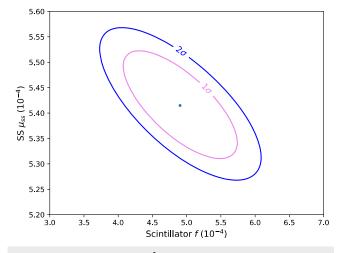


FIG. 6. Contour map showing the² minimum of the globalit as a function off and μ_{ss} . The reduced chi-squared χ^2/ν , is 1.0. The error (*p*) in the globalit was determined using the² +1 regions.

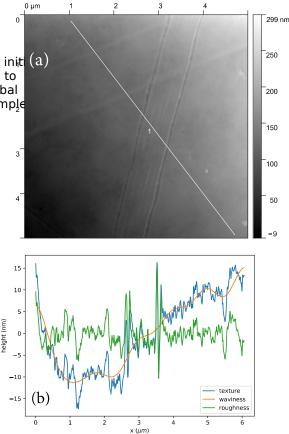


FIG. 7. (a) Sample profilometry data of a 5 \times 5 μ m² spot on the deuterated polystyrene scintillator. (b) Line out from left to right as indicated by the white line in (a). The waviness was subtracted from data (texture) to obtain the roughness plot.

scaleIn this case he loss-per-bounce parameteril) be modified due to the modification of the Europai potential Equa-

tion, (6) shows the effect on the loss-per-bounce parhameter, This work was supported by the Los Alamos National $k_c = 2mV/\hbar^2$ is the critical wavelength for the neutron, σ is the ring transformed program (Project 2001,90048 ER) ational height variation of the surface roughneeds is the correlation Science Foundation (Grand PHY1914133) and U.S.Departlength of the roughness, ment of EnergOffice of Nuclear Physics (Grant Dep FG02-

$$\mu' = \mu' \frac{2\partial k_c^2}{1 + \frac{2\partial k_c^2}{1 + 0.85 \eta k + 23 \eta v^2}}.$$
 (6)

ACKNOWLEDGMENTS

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A measurement of the surface roughness of the scintillatoand setul discussions.

formed using a Bruker Dimension Icon atomic force microscope.

The instrument was operated in the PeakForce tapping mode with

a standard ScanAsyst-Air tip. We sampled multiples ports 5 parta availability

on the scintillator and obtained surface roughness by fitting to heedata that support the findings of this study are available outs (Fig7).Since the loss-per-bounce parameter is only affected the corresponding author upon reasonable request. by roughness comparable to the wavelengthrofiwe esti-

mated the surface roughness by separating out the long wavelength waviness features from the short wavelength roughness. The analy-

sis was performed using Gwycalisoranning probe microscopy. Byrne, P. G. Dawber, C. G. Habeck, S. J. Smidt, J. A. Spain, and A. P. William analysisoftwareWe found that he average roughnessinges Europhys. Lett. 33, 187 (1996).

from 2 nm to 8 n**a**md the correlation length ranges from 40JnmNico,M. S. DeweyD. M. GilliamF. E. WietfeldtX. Fei,W. M. Snow, to 200 nnwhich is only a 2% correction on the loss-per-bounce Greend, Pauwels. EykensA. Lamberty, V. Gesteland RD. Scott, parameter in the worase. These results indicate that sur-

parameter in the worase. These results indicate that surface roughness of the scintillator is not enough to account W.M. S. Dewey, M. Gilliam, G. L. Greene, B. Laptey, S. Nico, differences. 4. P. Serebrow, E. Varlamov, G. Kharitonov, K. Fomin, Y. N. Pokotilovski, Geltenbort, A. Krasnoschekowa, S. Lasakow, R. Taldaev,

V. CONCLUSION

The Fermi potential for the Eljen-299-02D scintillator was ellembort, K. P. Hickerson, M. A. Hoffbauer, A. T. Holley, A. Komives, C.-Y. sured using a neutron reflectometry beamline at LANSCE (Asterix) T. MacDonald, M. Makela, C. L. Morris, J. D. Ortiz, J. Ramsey, D. J. S with a value of 168.2 ± 1.5 neV, consistent with the calculated value of 165.8 neV he measured loss factor of 4.9 ± 0.6 liok not be explained by the roughnetseos factor of 4.9 ± 0.6 liok not be explained by the roughnetseos factor of 4.9 ± 0.6 liok not be explained by the roughnetseos factor surfacientiar anomalous UCN losses have been explained by Ref. 25, where the transformed by Ref. 25, where the surface of the metals was the culprit. Poly St Kabl, Phys. Lett. B 24, 601 (1967). is hydrophobibut one can imagine a similar adsorption method and the origin 0.5 cm anomaly, one should study the for the scintillator before and the origin 0.5 cm and b. Grinstein, Phys. Rev. Lett. 120, 191801 (2018).

Regardless of the origin of the anomald**the llosss**, factor ¹²Z. Tang, M. Blatnik, L. J. Broussard, J. H. Choi, S. M. Clayton, C. Cude-Woods measurement did demonstrate the utility of the scintillato.indurate D. E. Fellers, E. M. Fries, P. Geltenbort, F. Gonzalez, K. P. Hickerson, ping UCNs and detecting electrons from neutron beta decay should be adealy should Lin. S. W. Macdonald, M. Makela, C. L. Morris, C. M. O'Shaughness taneously, which can be used in future UCN based "beam Rill that the, B. Plaster, D. J. Salvat, A. Saunders, Z. Wang, A. R. Young, and B and beta decay correlation experimentseasured loss factor ¹³Z, Sun F. AdamekB. AllgeierM. BlatnikT. J. Bowlest, J. Broussard/l. is also sufficient to achieve the targeted statistical sensitivity from R. Carr, S. ClaytonC. Cude-Woods. Currie F. B. DeesX. Ding, proposed neutron beta decay lifetime experiment using a gl-NFARGBone, A. García, P. Geltenbort, S. Hasan, K. P. Hickerson, J. Hoaglan tillator bottle. Taking the UCN spectrum and density obtaineed figure E. HoganA. T. HolleyT. M. Ito, A. KnechtC. Y. Liu, J. Liu, M. Ref. 19, we estimate the decays per measurement cycle to the beatween mei, J. W. Martin, D. Melconian, M. P. Mendenhall, S. D. Moore 2180 and 5640 events for a nominal 2 I volume, with an of set Mation P. Pitt, B. Plaster, C. RamseyR. Rios, D. J. Salvata. Saunders, time of 134 s and 206 s, respectively. The storage times for the time of the time strates, C. Swank, G. Swift, E. Tatar, R. B. Vogelaar, and lower-bound estimates were determined using the time of model 2. Wang, W. Wei, J. Wexler, T. Womack, C. Wrede, A. R. Young, and decay count is equal to the remaining UCN populabitarin B. A. Zeck, Phys. Rev. C **97**, 052501 (2018); arXiv:1803.10890. 1 sstatisticadensitivity on the neutron beta decay lifetime **Wi**. McKeen, A. E. Nelson, S. Reddy, and D. Zhou, Phys. Rev. Lett. **121**, 0614 require approximately 180 to 460 measurement cycles. (2018). ¹⁵Z. Berezhiani, R. Biondi, P. Geltenbort, I. A. Krasnoshchekova, V. E. Vazati and S. M. Clayton, C. Culahan, A. V. Vassiljev, and O. M. Zherebtsov, Eur. Phys. J. C 78, 717 (2018).
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