

Search for Axionlike Particles Produced in e^+e^- Collisions at Belle II

F. Abudinén,⁴² I. Adachi,^{21,18} H. Aihara,¹¹⁵ N. Akopov,¹²¹ A. Aloisio,^{87,35} F. Ameli,³⁹ N. Anh Ky,^{32,11} D. M. Asner,² T. Aushev,²³ V. Aushev,⁷⁷ V. Babu,⁹ S. Baehr,⁴⁶ S. Bahinipati,²⁵ P. Bambade,⁹⁶ Sw. Banerjee,¹⁰⁵ S. Bansal,⁶⁸ J. Baudot,⁹⁷ J. Becker,⁴⁶ P. K. Behera,²⁷ J. V. Bennett,¹⁰⁹ E. Bernieri,⁴⁰ F. U. Bernlochner,⁹⁹ M. Bertemes,²⁹ M. Bessner,¹⁰² S. Bettarini,^{90,38} V. Bhardwaj,²⁴ F. Bianchi,^{93,41} T. Bilka,⁵ S. Bilokin,⁵² D. Biswas,¹⁰⁵ M. Bračko,^{107,76} P. Branchini,⁴⁰ N. Braun,⁴⁶ T. E. Browder,¹⁰² A. Budano,⁴⁰ S. Bussino,^{92,40} M. Campajola,^{87,35} G. Casarosa,^{90,38} C. Cecchi,^{89,37} D. Červenkov,⁵ M.-C. Chang,¹⁴ P. Chang,⁶¹ R. Cheaib,¹⁰⁰ V. Chekelian,⁵⁵ B. G. Cheon,²⁰ K. Chilikin,⁵⁰ K. Chirapatpimol,⁶ H.-E. Cho,²⁰ K. Cho,⁴⁷ S.-J. Cho,¹²² S.-K. Choi,¹⁹ D. Cinabro,¹¹⁹ L. Corona,^{90,38} L. M. Cremaldi,¹⁰⁹ S. Cunliffe,⁹ N. Dash,²⁷ F. Dattola,⁹ E. De La Cruz-Burelo,⁴ G. De Nardo,^{87,35} M. De Nuccio,⁹ G. De Pietro,⁴⁰ R. de Sangro,³⁴ M. Destefanis,^{93,41} A. De Yta-Hernandez,⁴ F. Di Capua,^{87,35} Z. Doležal,⁵ T. V. Dong,¹⁵ K. Dort,⁴⁵ D. Dossett,¹⁰⁸ G. Dujany,⁹⁷ S. Eidelman,^{3,50,64} T. Ferber,⁹ D. Ferlewicz,¹⁰⁸ S. Fiore,³⁹ A. Fodor,⁵⁶ F. Forti,^{90,38} B. G. Fulsom,⁶⁷ E. Ganiev,^{94,42} R. Garg,⁶⁸ A. Garmash,^{3,64} V. Gaur,¹¹⁸ A. Gaz,^{58,59} U. Gebauer,¹⁶ A. Gellrich,⁹ T. Geßler,⁴⁵ R. Giordano,^{87,35} A. Giri,²⁶ B. Gobbo,⁴² R. Godang,¹¹² P. Goldenzweig,⁴⁶ B. Golob,^{104,76} P. Gomis,³³ W. Gradl,⁴⁴ E. Graziani,⁴⁰ D. Greenwald,⁷⁹ C. Hadjivasiliou,⁶⁷ S. Halder,⁷⁸ O. Hartbrich,¹⁰² K. Hayasaka,⁶³ H. Hayashii,⁶⁰ C. Hearty,^{100,31} M. T. Hedges,¹⁰² I. Heredia de la Cruz,^{4,8} M. Hernández Villanueva,¹⁰⁹ A. Hershenhorn,¹⁰⁰ T. Higuchi,¹¹⁶ E. C. Hill,¹⁰⁰ H. Hirata,⁵⁸ M. Hoek,⁴⁴ M. Hohmann,¹⁰⁸ C.-L. Hsu,¹¹⁴ Y. Hu,³⁰ K. Inami,⁵⁸ G. Inguglia,²⁹ J. Irakkathil Jabbar,⁴⁶ A. Ishikawa,^{21,18} R. Itoh,^{21,18} P. Jackson,⁹⁸ W. W. Jacobs,²⁸ D. E. Jaffe,² E.-J. Jang,¹⁹ S. Jia,¹⁵ Y. Jin,⁴² C. Joo,¹¹⁶ A. B. Kaliyar,⁷⁸ J. Kandra,⁵ G. Karyan,¹²¹ Y. Kato,^{58,59} H. Kichimi,²¹ C. Kiesling,⁵⁵ C.-H. Kim,²⁰ D. Y. Kim,⁷⁵ H. J. Kim,⁴⁹ S.-H. Kim,⁷² Y.-K. Kim,¹²² T. D. Kimmel,¹¹⁸ K. Kinoshita,¹⁰¹ C. Kleinwort,⁹ P. Kodyš,⁵ T. Koga,²¹ S. Kohani,¹⁰² I. Komarov,⁹ S. Korpar,^{107,76} T. M. G. Kraetzschmar,⁵⁵ P. Križan,^{104,76} P. Krokovny,^{3,64} T. Kuhr,⁵² M. Kumar,⁵⁴ R. Kumar,⁷⁰ K. Kumara,¹¹⁹ S. Kurz,⁹ Y.-J. Kwon,¹²² S. Lacaprara,³⁶ C. La Licata,¹¹⁶ L. Lanceri,⁴² J. S. Lange,⁴⁵ I.-S. Lee,²⁰ S. C. Lee,⁴⁹ P. Leitl,⁵⁵ D. Levit,⁷⁹ P. M. Lewis,⁹⁹ C. Li,⁵¹ L. K. Li,¹⁰¹ Y. B. Li,⁶⁹ J. Libby,²⁷ K. Lieret,⁵² L. Li Gioi,⁵⁵ Z. Liptak,¹⁰² Q. Y. Liu,¹⁵ D. Liventsev,^{119,21} S. Longo,⁹ T. Luo,¹⁵ C. MacQueen,¹⁰⁸ Y. Maeda,^{58,59} R. Manfredi,^{94,42} E. Manoni,³⁷ S. Marcello,^{93,41} C. Marinas,³³ A. Martini,^{92,40} M. Masuda,^{12,66} K. Matsuoka,^{58,59} D. Matvienko,^{3,50,64} F. Meggendorfer,⁵⁵ F. Meier,¹⁰ M. Merola,^{86,35} F. Metzner,⁴⁶ M. Milesi,¹⁰⁸ C. Miller,¹¹⁷ K. Miyabayashi,⁶⁰ R. Mizuk,^{50,23} K. Azmi,¹⁰⁶ G. B. Mohanty,⁷⁸ H.-G. Moser,⁵⁵ M. Mrvar,²⁹ F. J. Müller,⁹ R. Mussa,⁴¹ I. Nakamura,^{21,18} M. Nakao,^{21,18} H. Nakazawa,⁶¹ A. Natochii,¹⁰² C. Niebuhr,⁹ N. K. Nisar,² S. Nishida,^{21,18} M. H. A. Nouxman,¹⁰⁶ K. Ogawa,⁶³ S. Ogawa,⁸¹ H. Ono,⁶³ P. Oskin,⁵⁰ H. Ozaki,^{21,18} P. Pakhlov,^{50,57} A. Paladino,^{90,38} A. Panta,¹⁰⁹ E. Paoloni,^{90,38} S. Pardi,^{35,35} H. Park,⁴⁹ S.-H. Park,¹²² B. Paschen,⁹⁹ A. Passeri,⁴⁰ A. Pathak,¹⁰⁵ S. Patra,²⁴ S. Paul,⁷⁹ T. K. Pedlar,⁵³ I. Peruzzi,³⁴ R. Peschke,¹⁰² M. Piccolo,³⁴ L. E. Piilonen,¹¹⁸ G. Polat,¹ V. Popov,²³ C. Praz,⁹ E. Prencipe,¹³ M. T. Prim,⁴⁶ M. V. Purohit,⁶⁵ N. Rad,⁹ P. Rados,⁹ R. Rasheed,⁹⁷ M. Reif,⁵⁵ S. Reiter,⁴⁵ M. Remnev,^{3,64} I. Ripp-Baudot,⁹⁷ M. Ritter,⁵² M. Ritzert,¹⁰³ G. Rizzo,^{90,38} S. H. Robertson,^{56,31} D. Rodríguez Pérez,⁸⁵ J. M. Roney,^{117,31} C. Rosenfeld,¹¹³ A. Rostomyan,⁹ N. Rout,²⁷ D. Sahoo,⁷⁸ Y. Sakai,^{21,18} D. A. Sanders,¹⁰⁹ S. Sandilya,¹⁰¹ A. Sangal,¹⁰¹ L. Santelj,^{104,76} Y. Sato,⁸² V. Savinov,¹¹⁰ B. Scavino,⁴⁴ C. Schwanda,²⁹ A. J. Schwartz,¹⁰¹ R. M. Seddon,⁵⁶ Y. Seino,⁶³ A. Selce,^{91,39} K. Senyo,¹²⁰ J. Serrano,¹ M. E. Sevier,¹⁰⁸ C. Sfienti,⁴⁴ J.-G. Shiu,⁶¹ A. Sibidanov,¹¹⁷ F. Simon,⁵⁵ R. J. Sobie,^{117,31} A. Soffer,⁸⁰ E. Solovieva,⁵⁰ S. Spataro,^{93,41} B. Spruck,⁴⁴ M. Starič,⁷⁶ S. Stefkova,⁹ Z. S. Stottler,¹¹⁸ R. Stroili,^{88,36} J. Strube,⁶⁷ M. Sumihama,^{17,66} T. Sumiyoshi,⁸⁴ D. J. Summers,¹⁰⁹ W. Sutcliffe,⁹⁹ H. Svidras,⁹ M. Tabata,⁷ M. Takizawa,^{71,22,73} U. Tamponi,⁴¹ S. Tanaka,^{21,18} K. Tanida,⁴³ H. Tanigawa,¹¹⁵ P. Taras,⁹⁵ F. Tenchini,⁹ D. Tonelli,⁴² E. Torassa,³⁶ K. Trabelsi,⁹⁶ M. Uchida,⁸³ T. Uglov,^{50,23} K. Unger,⁴⁶ Y. Unno,²⁰ S. Uno,^{21,18} P. Urquijo,¹⁰⁸ Y. Ushiroda,^{21,18,115} S. E. Vahsen,¹⁰² R. van Tonder,⁹⁹ G. S. Varner,¹⁰² K. E. Varvell,¹¹⁴ A. Vinokurova,^{3,64} L. Vitale,^{94,42} E. Waheed,²¹ M. Wakai,¹⁰⁰ H. M. Wakeling,⁵⁶ C. H. Wang,⁶² M.-Z. Wang,⁶¹ X. L. Wang,¹⁵ A. Warburton,⁵⁶ M. Watanabe,⁶³ S. Watanuki,⁹⁶ J. Webb,¹⁰⁸ S. Wehle,⁹ M. Welsch,⁹⁹ C. Wessel,⁹⁹ J. Wiechczynski,³⁸ H. Windel,⁵⁵ E. Won,⁴⁸ L. J. Wu,³⁰ X. P. Xu,⁷⁴ B. Yabsley,¹¹⁴ W. Yan,¹¹¹ S. B. Yang,⁴⁸ H. Ye,⁹ M. Yonenaga,⁸⁴ C. Z. Yuan,³⁰ Y. Yusa,⁶³ L. Zani,¹ Q. D. Zhou,⁵⁸ and V. I. Zhukova⁵⁰

(Belle II Collaboration)

¹Aix Marseille Université, CNRS/IN2P3, CPPM, 13288 Marseille²Brookhaven National Laboratory, Upton, New York 11973³Budker Institute of Nuclear Physics SB RAS, Novosibirsk 630090

- ⁴*Centro de Investigacion y de Estudios Avanzados del Instituto Politecnico Nacional, Mexico City 07360*
- ⁵*Faculty of Mathematics and Physics, Charles University, 121 16 Prague*
- ⁶*Chiang Mai University, Chiang Mai 50202*
- ⁷*Chiba University, Chiba 263-8522*
- ⁸*Consejo Nacional de Ciencia y Tecnología, Mexico City 03940*
- ⁹*Deutsches Elektronen-Synchrotron, 22607 Hamburg*
- ¹⁰*Duke University, Durham, North Carolina 27708*
- ¹¹*Institute of Theoretical and Applied Research (ITAR), Duy Tan University, Hanoi 100000*
- ¹²*Earthquake Research Institute, University of Tokyo, Tokyo 113-0032*
- ¹³*Forschungszentrum Jülich, 52425 Jülich*
- ¹⁴*Department of Physics, Fu Jen Catholic University, Taipei 24205*
- ¹⁵*Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443*
- ¹⁶*II. Physikalisches Institut, Georg-August-Universität Göttingen, 37073 Göttingen*
- ¹⁷*Gifu University, Gifu 501-1193*
- ¹⁸*The Graduate University for Advanced Studies (SOKENDAI), Hayama 240-0193*
- ¹⁹*Gyeongsang National University, Jinju 52828*
- ²⁰*Department of Physics and Institute of Natural Sciences, Hanyang University, Seoul 04763*
- ²¹*High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801*
- ²²*J-PARC Branch, KEK Theory Center, High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801*
- ²³*Higher School of Economics (HSE), Moscow 101000*
- ²⁴*Indian Institute of Science Education and Research Mohali, SAS Nagar, 140306*
- ²⁵*Indian Institute of Technology Bhubaneswar, Satya Nagar 751007*
- ²⁶*Indian Institute of Technology Hyderabad, Telangana 502285*
- ²⁷*Indian Institute of Technology Madras, Chennai 600036*
- ²⁸*Indiana University, Bloomington, Indiana 47408*
- ²⁹*Institute of High Energy Physics, Vienna 1050*
- ³⁰*Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049*
- ³¹*Institute of Particle Physics (Canada), Victoria, British Columbia V8W 2Y2*
- ³²*Institute of Physics, Vietnam Academy of Science and Technology (VAST), Hanoi*
- ³³*Instituto de Fisica Corpuscular, Paterna 46980*
- ³⁴*INFN Laboratori Nazionali di Frascati, I-00044 Frascati*
- ³⁵*INFN Sezione di Napoli, I-80126 Napoli*
- ³⁶*INFN Sezione di Padova, I-35131 Padova*
- ³⁷*INFN Sezione di Perugia, I-06123 Perugia*
- ³⁸*INFN Sezione di Pisa, I-56127 Pisa*
- ³⁹*INFN Sezione di Roma, I-00185 Roma*
- ⁴⁰*INFN Sezione di Roma Tre, I-00146 Roma*
- ⁴¹*INFN Sezione di Torino, I-10125 Torino*
- ⁴²*INFN Sezione di Trieste, I-34127 Trieste*
- ⁴³*Advanced Science Research Center, Japan Atomic Energy Agency, Naka 319-1195*
- ⁴⁴*Johannes Gutenberg-Universität Mainz, Institut für Kernphysik, D-55099 Mainz*
- ⁴⁵*Justus-Liebig-Universität Gießen, 35392 Gießen*
- ⁴⁶*Institut für Experimentelle Teilchenphysik, Karlsruher Institut für Technologie, 76131 Karlsruhe*
- ⁴⁷*Korea Institute of Science and Technology Information, Daejeon 34141*
- ⁴⁸*Korea University, Seoul 02841*
- ⁴⁹*Kyungpook National University, Daegu 41566*
- ⁵⁰*P.N. Lebedev Physical Institute of the Russian Academy of Sciences, Moscow 119991*
- ⁵¹*Liaoning Normal University, Dalian 116029*
- ⁵²*Ludwig Maximilians University, 80539 Munich*
- ⁵³*Luther College, Decorah, Iowa 52101*
- ⁵⁴*Malaviya National Institute of Technology Jaipur, Jaipur 302017*
- ⁵⁵*Max-Planck-Institut für Physik, 80805 München*
- ⁵⁶*McGill University, Montréal, Québec, H3A 2T8*
- ⁵⁷*Moscow Physical Engineering Institute, Moscow 115409*
- ⁵⁸*Graduate School of Science, Nagoya University, Nagoya 464-8602*
- ⁵⁹*Kobayashi-Maskawa Institute, Nagoya University, Nagoya 464-8602*
- ⁶⁰*Nara Women's University, Nara 630-8506*
- ⁶¹*Department of Physics, National Taiwan University, Taipei 10617*
- ⁶²*National United University, Miao Li 36003*

- ⁶³Niigata University, Niigata 950-2181
- ⁶⁴Novosibirsk State University, Novosibirsk 630090
- ⁶⁵Okinawa Institute of Science and Technology, Okinawa 904-0495
- ⁶⁶Research Center for Nuclear Physics, Osaka University, Osaka 567-0047
- ⁶⁷Pacific Northwest National Laboratory, Richland, Washington 99352
- ⁶⁸Panjab University, Chandigarh 160014
- ⁶⁹Peking University, Beijing 100871
- ⁷⁰Punjab Agricultural University, Ludhiana 141004
- ⁷¹Theoretical Research Division, Nishina Center, RIKEN, Saitama 351-0198
- ⁷²Seoul National University, Seoul 08826
- ⁷³Showa Pharmaceutical University, Tokyo 194-8543
- ⁷⁴Soochow University, Suzhou 215006
- ⁷⁵Soongsil University, Seoul 06978
- ⁷⁶J. Stefan Institute, 1000 Ljubljana
- ⁷⁷Taras Shevchenko National University of Kiev, Kiev
- ⁷⁸Tata Institute of Fundamental Research, Mumbai 400005
- ⁷⁹Department of Physics, Technische Universität München, 85748 Garching
- ⁸⁰Tel Aviv University, School of Physics and Astronomy, Tel Aviv 69978
- ⁸¹Toho University, Funabashi 274-8510
- ⁸²Department of Physics, Tohoku University, Sendai 980-8578
- ⁸³Tokyo Institute of Technology, Tokyo 152-8550
- ⁸⁴Tokyo Metropolitan University, Tokyo 192-0397
- ⁸⁵Universidad Autonoma de Sinaloa, Sinaloa 80000
- ⁸⁶Dipartimento di Agraria, Università di Napoli Federico II, I-80055 Portici (NA)
- ⁸⁷Dipartimento di Scienze Fisiche, Università di Napoli Federico II, I-80126 Napoli
- ⁸⁸Dipartimento di Fisica e Astronomia, Università di Padova, I-35131 Padova
- ⁸⁹Dipartimento di Fisica, Università di Perugia, I-06123 Perugia
- ⁹⁰Dipartimento di Fisica, Università di Pisa, I-56127 Pisa
- ⁹¹Università di Roma "La Sapienza," I-00185 Roma
- ⁹²Dipartimento di Matematica e Fisica, Università di Roma Tre, I-00146 Roma
- ⁹³Dipartimento di Fisica, Università di Torino, I-10125 Torino
- ⁹⁴Dipartimento di Fisica, Università di Trieste, I-34127 Trieste
- ⁹⁵Université de Montréal, Physique des Particules, Montréal, Québec H3C 3J7
- ⁹⁶Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay
- ⁹⁷Université de Strasbourg, CNRS, IPHC, UMR 7178, 67037 Strasbourg
- ⁹⁸Department of Physics, University of Adelaide, Adelaide, South Australia 5005
- ⁹⁹University of Bonn, 53115 Bonn
- ¹⁰⁰University of British Columbia, Vancouver, British Columbia V6T 1Z1
- ¹⁰¹University of Cincinnati, Cincinnati, Ohio 45221
- ¹⁰²University of Hawaii, Honolulu, Hawaii 96822
- ¹⁰³University of Heidelberg, 68131 Mannheim
- ¹⁰⁴Faculty of Mathematics and Physics, University of Ljubljana, 1000 Ljubljana
- ¹⁰⁵University of Louisville, Louisville, Kentucky 40292
- ¹⁰⁶National Centre for Particle Physics, University Malaya, 50603 Kuala Lumpur
- ¹⁰⁷University of Maribor, 2000 Maribor
- ¹⁰⁸School of Physics, University of Melbourne, Victoria 3010
- ¹⁰⁹University of Mississippi, University, Mississippi 38677
- ¹¹⁰University of Pittsburgh, Pittsburgh, Pennsylvania 15260
- ¹¹¹University of Science and Technology of China, Hefei 230026
- ¹¹²University of South Alabama, Mobile, Alabama 36688
- ¹¹³University of South Carolina, Columbia, South Carolina 29208
- ¹¹⁴School of Physics, University of Sydney, New South Wales 2006
- ¹¹⁵Department of Physics, University of Tokyo, Tokyo 113-0033
- ¹¹⁶Kavli Institute for the Physics and Mathematics of the Universe (WPI), University of Tokyo, Kashiwa 277-8583
- ¹¹⁷University of Victoria, Victoria, British Columbia V8W 3P6
- ¹¹⁸Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061
- ¹¹⁹Wayne State University, Detroit, Michigan 48202
- ¹²⁰Yamagata University, Yamagata 990-8560
- ¹²¹Alikhanyan National Science Laboratory, Yerevan 0036
- ¹²²Yonsei University, Seoul 03722



We present a search for the direct production of a light pseudoscalar a decaying into two photons with the Belle II detector at the SuperKEKB collider. We search for the process $e^+e^- \rightarrow \gamma a$, $a \rightarrow \gamma\gamma$ in the mass range $0.2 < m_a < 9.7 \text{ GeV}/c^2$ using data corresponding to an integrated luminosity of $(445 \pm 3) \text{ pb}^{-1}$. Light pseudoscalars interacting predominantly with standard model gauge bosons (so-called axionlike particles or ALPs) are frequently postulated in extensions of the standard model. We find no evidence for ALPs and set 95% confidence level upper limits on the coupling strength $g_{a\gamma\gamma}$ of ALPs to photons at the level of 10^{-3} GeV^{-1} . The limits are the most restrictive to date for $0.2 < m_a < 1 \text{ GeV}/c^2$.

DOI: [10.1103/PhysRevLett.125.161806](https://doi.org/10.1103/PhysRevLett.125.161806)

Axions and axionlike particles (ALPs) are predicted by many extensions of the standard model (SM) [1]. They occur, for example, in most solutions of the strong CP problem [2]. ALPs share the quantum numbers of axions, but differ in that their masses and couplings are independent. ALPs with sub-MeV/ c^2 masses are interesting in the context of astrophysics and cosmology and are cold dark matter (DM) candidates, whereas ALPs with $\mathcal{O}(1 \text{ GeV}/c^2)$ masses generally relate to several topics in particle physics [3–5]. Most notably, heavy ALPs can connect the SM particles to yet undiscovered DM particles [6]. ALPs that predominantly couple to $\gamma\gamma$, γZ^0 , and $Z^0 Z^0$ are experimentally much less constrained than those that couple to gluons or fermions. The latter interactions typically lead to flavor-changing processes that can be probed in rare decays [7]. In this Letter we will consider the case that the ALP a predominantly couples to photons, with coupling strength $g_{a\gamma\gamma}$, and has negligible coupling strength $g_{a\gamma Z}$ to a photon and a Z^0 boson, so that $\mathcal{B}(a \rightarrow \gamma\gamma) \approx 100\%$; we follow the notation for couplings introduced in Ref. [6]. In the MeV/ c^2 to GeV/ c^2 mass range, the current best limits for ALPs with photon couplings are derived from a variety of experiments. These limits come from $e^+e^- \rightarrow \gamma + \text{invisible}$ and beam-dump experiments for light ALPs [6,8,9], from $e^+e^- \rightarrow \gamma\gamma$ [10,11] and coherent Primakoff production off a nuclear target [12] for intermediate-mass ALPs, and from peripheral heavy-ion collisions [13] for heavy ALPs.

We search for $e^+e^- \rightarrow \gamma a$, $a \rightarrow \gamma\gamma$ in the ALP mass range $0.2 < m_a < 9.7 \text{ GeV}/c^2$ in the three-photon final state. The signature in the center-of-mass (c.m.) system is a monoenergetic photon recoiling against the $a \rightarrow \gamma\gamma$ decay. The energy of the recoil photon is

$$E_{\text{recoil}}^{\text{c.m.}} = \frac{s - m_a^2}{2\sqrt{s}},$$

where $\sqrt{s}$ is the c.m. collision energy. We search for an ALP signal as a narrow peak in the squared recoil-mass distribution $M_{\text{recoil}}^2 = s - 2\sqrt{s}E_{\text{recoil}}^{\text{c.m.}}$, or as a narrow peak in the squared-invariant-mass distribution $M_{\gamma\gamma}^2$, computed using the two-photon system, depending on which provides the better sensitivity. We note that in the future a larger Belle II dataset will be available to calibrate the photon covariance matrix, which in turn will allow the use of kinematic fitting of the three photons to the known beam four-momentum, thus improving the sensitivity. In our search range, the width of the ALP is negligible with respect to the experimental resolution, and the ALP lifetime is negligible, thus it decays promptly. The dominant SM background process is $e^+e^- \rightarrow \gamma\gamma\gamma$. The analysis selection, fit strategy, and limit-setting procedures are optimized and verified based on Monte Carlo simulation, i.e., without looking at data events, to avoid experimenter's bias.

We use a data set corresponding to an integrated luminosity of $(496 \pm 3) \text{ pb}^{-1}$ [14] collected with the Belle II detector at the asymmetric-energy e^+e^- collider SuperKEKB [15], which is located at the KEK laboratory in Tsukuba, Japan. Data were collected at the c.m. energy of the $\Upsilon(4S)$ resonance ($\sqrt{s} = 10.58 \text{ GeV}$) from April to July 2018. The energies of the electron and positron beams are 7 and 4 GeV, respectively, resulting in a boost of $\beta\gamma = 0.28$ of the c.m. frame relative to the laboratory frame. We use a randomly chosen subset of the data, approximately 10%, to validate the selection, and we then discard it from the final data sample. The remaining data set is used for the search and corresponds to an integrated luminosity of $(445 \pm 3) \text{ pb}^{-1}$.

The Belle II detector consists of several subdetectors arranged around the beam pipe in a cylindrical structure [16,17]. Only the components that are relevant to this analysis are described below. Photons are measured and identified in the electromagnetic calorimeter (ECL) consisting of CsI(Tl) crystals. The ECL provides both an energy and a timing measurement. A superconducting solenoid situated outside of the calorimeter provides a 1.5 T magnetic field. Charged-particle tracking is done using a silicon vertex detector (VXD) and a central drift chamber (CDC). Only one azimuthal octant of the VXD was present during the 2018 operations. The z axis of the

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laboratory frame coincides with that of the solenoid and its positive direction is approximately that of the incoming electron beam. The polar angle θ is measured with respect to this direction. Events are selected only by the hardware trigger, and no further software trigger selection is applied. Trigger energy thresholds are very low and no vetoes for abundant QED scattering processes are applied.

We use BABAYAGA@NLO [18–21] to generate SM background processes $e^+e^- \rightarrow e^+e^-(\gamma)$, $e^+e^- \rightarrow \gamma\gamma(\gamma)$. We use PHOKHARA9 [22] to generate SM background processes $e^+e^- \rightarrow P\gamma(\gamma)$, where P is a SM pseudoscalar meson (π^0, η, η'). This includes production via the radiative decay of the intermediate vector resonances ρ , ω , and ϕ . The largest pseudoscalar background contribution for this analysis comes from $e^+e^- \rightarrow \omega\gamma, \omega \rightarrow \pi^0\gamma$ with a boosted π^0 decaying into overlapping photons. We use the same generators to calculate the cross sections of the respective processes. We use MADGRAPH5 [23] to simulate signal events, including the effects of initial-state radiation (ISR) in event kinematics [24], for different hypotheses for m_a in step sizes approximately equal to the signal resolution in our search range.

We use GEANT4 [25] to simulate the interactions of particles in the detector, taking into account the nominal detector geometry and simulated beam-backgrounds adjusted to match the measured beam conditions. We use the Belle II software framework [26] to reconstruct and analyze events.

All selection criteria are chosen to maximize the Punzi figure of merit for 5σ discovery [27]. Quantities are defined in the laboratory frame unless otherwise specified. Photon candidates are reconstructed from ECL clusters with no associated charged tracks. We select events with at least three photon candidates with energy E_γ above 0.65 GeV (for $m_a > 4 \text{ GeV}/c^2$) or 1.0 GeV (for $m_a \leq 4 \text{ GeV}/c^2$). This ALP-mass-dependent threshold is used to avoid shaping effects on the background distribution in the mass fit range. The following selection variables are not dependent on the ALP mass. All three photon candidates must be reconstructed with polar angles $37.3 < \theta_\gamma < 123.7^\circ$. This polar-angle region provides the best calorimeter energy resolution, avoids regions close to detector gaps, and offers the lowest beam background levels. If more than three photons pass the selection criteria, we select the three most energetic ones and the additional photons are ignored in the calculation of any variables. This occurs in fewer than 0.2% of all events. We reduce contamination from beam backgrounds by requiring that each photon detection time t_i is compatible with the average weighted photon time

$$\bar{t} = \frac{\sum_{i=1}^3 (t_i / \Delta t_i^2)}{\sum_{j=1}^3 (1 / \Delta t_j^2)},$$

where Δt_i is the energy-dependent timing range that includes 99% of all signal photons, and is between 3 ns

(high E_γ) and 15 ns (low E_γ). The requirement is $|(t_i - \bar{t}) / \Delta t_i| < 10$, which is insensitive to global time offsets. The invariant mass $M_{\gamma\gamma\gamma}$ of the three-photon system must satisfy $0.88\sqrt{s} \leq M_{\gamma\gamma\gamma} \leq 1.03\sqrt{s}$ to eliminate kinematically unbalanced events coming from cosmic rays, beam-gas backgrounds, or two-photon production. We reject events that have tracks originating from the interaction region to suppress background from $e^+e^- \rightarrow e^+e^-\gamma$. We require a θ_γ separation between any two photons of $\Delta\theta_\gamma > 0.014 \text{ rad}$, or an azimuthal angle separation of $\Delta\phi_\gamma > 0.400 \text{ rad}$ to reduce background from photon conversions outside of the tracking detectors. Following a data-sideband analysis using $M_{\gamma\gamma\gamma} < 0.88\sqrt{s}$, we additionally apply a loose selection, based on a multivariate shower-shape classifier that uses multiple Zernike moments [28], on the most isolated of the three photons. This criterion reduces the number of clusters produced by neutral hadrons and by particles that do not originate from the interaction point. The selection procedure results in three ALP candidates per event from all possible combinations of the three selected photons.

The resulting M_{recoil}^2 and $M_{\gamma\gamma}^2$ distributions are shown in Fig. 1 together with the stacked contributions from the luminosity-normalized simulated samples of SM backgrounds. The expected background distributions are dominated by $e^+e^- \rightarrow \gamma\gamma\gamma$ with a small contribution from $e^+e^- \rightarrow e^+e^-\gamma$ due to tracking inefficiencies. We find contributions from cosmic rays, assessed in data-taking periods without colliding beams, neither significant nor peaking in photon energy or invariant mass. The data shape agrees well with simulation except for a small and localized excess seen in the low-mass region $M_{\gamma\gamma}^2 < 1 \text{ GeV}^2/c^4$. The excess is broad [see the inset in Fig. 1(b)] and not consistent with an ALP signal, for which we expect a much smaller width in this region (see the inset in Fig. 2). As described later, the signal extraction does not directly depend on the background predictions because we fit the background only using data, thus any discrepancy between data and simulation has little impact on the result. Triggers based on 1 GeV threshold energy sums in the calorimeter barrel are found to have $\epsilon_{\text{trg}} = 1.0$ for the ALP selection, based upon studies of radiative Bhabha events.

The ALP selection efficiency is determined using large simulated signal samples, and varies smoothly between 20% (low m_a) and 34% (high m_a). The number of candidates in data is $3.6 \pm 0.9\%$ ($4.2 \pm 1.1\%$) higher than in the simulation for the $E_\gamma > 0.65 \text{ GeV}$ ($E_\gamma > 1.0 \text{ GeV}$) selection. No correction is applied and we assign the sum of the full difference and its uncertainty as a systematic uncertainty for the selection efficiency. We assess the difference in the photon-energy reconstruction between data and simulation by using radiative muon-pair events in which we compare the predicted recoil energy calculated from the muon-pair momenta with the energy of the photon

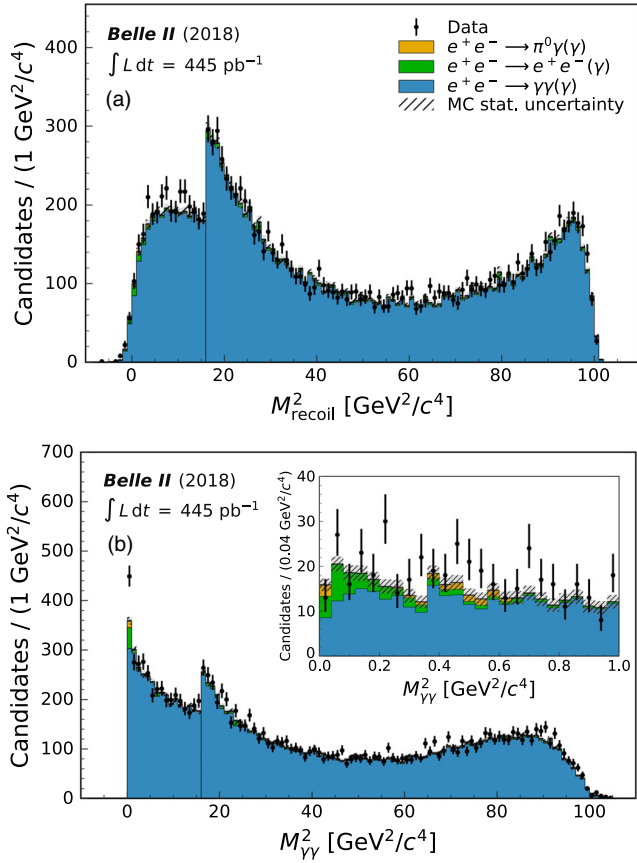


FIG. 1. M_{recoil}^2 distribution (a) and $M_{\gamma\gamma}^2$ distribution (b) together with the stacked contributions from the different simulated SM background samples. For $M^2 \leq 16 \text{ GeV}^2/c^4$, the selection is $E_\gamma > 1.0 \text{ GeV}$; for $M^2 > 16 \text{ GeV}^2/c^4$, it is $E_\gamma > 0.65 \text{ GeV}$. Simulation is normalized to luminosity. The inset in (b) shows an enlargement of the low-mass region $M_{\gamma\gamma}^2 < 1 \text{ GeV}^2/c^4$.

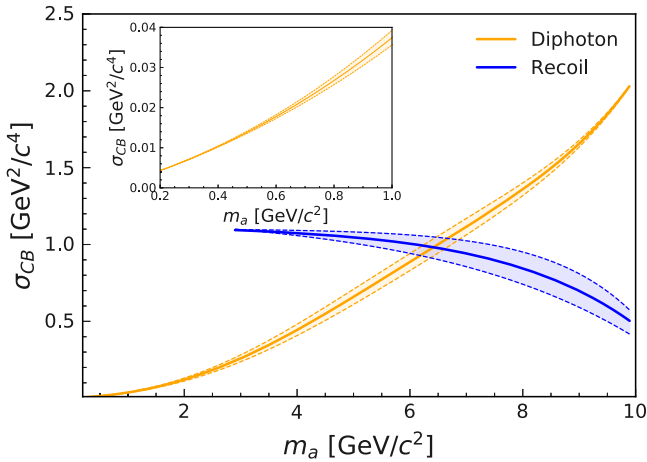


FIG. 2. $M_{\gamma\gamma}^2$ and M_{recoil}^2 resolutions with uncertainty as a function of ALP mass m_a . The inset shows an enlargement of the low-mass region $m_a < 1 \text{ GeV}/c^2$.

candidate. We correct for the observed linear energy bias that ranges from 0 (low energy) to 0.5% (high energy). We vary the energy selection by $\pm 1\%$ and the angular-separation selection by the approximate position resolution of $\pm 5 \text{ mrad}$, and take the respective full difference in the signal selection efficiency with respect to the nominal selection as a systematic uncertainty. We add these three uncertainties in quadrature assuming no correlations amongst them. The total relative uncertainty due to the selection efficiency is approximately 5.5% for ALP masses above $0.5 \text{ GeV}/c^2$, and increases to approximately 8% for the lightest ALP masses considered. As additional systematic checks we vary the photon-timing selection by ± 1 and the shower-shape classifier selection by $\pm 5\%$ to account for possible between data and simulation samples, the invariant mass $M_{\gamma\gamma}$ selection by $\pm 0.002 \text{ GeV}/c^2$ to account for uncertainties in the beam energy, and the polar-angle-acceptance selection by propagating the effect of a $\pm 2 \text{ mm}$ shift of the interaction point relative to the calorimeter to account for maximal possible misalignment of the ECL. For all of these checks, we find that they have a negligible effect on the signal selection efficiency, so we do not associate any systematic uncertainty with them.

We extract the signal yield as a function of m_a by performing a series of independent binned maximum-likelihood fits. We use 100 bins for each fit range. The fits are performed in the range $0.2 < m_a < 6.85 \text{ GeV}/c^2$ for the $M_{\gamma\gamma}^2$ spectrum, and in the range $6.85 < m_a < 9.7 \text{ GeV}/c^2$ for the M_{recoil}^2 spectrum. The resolution of $M_{\gamma\gamma}^2$ worsens with increasing m_a , while that of M_{recoil}^2 improves with increasing m_a (see Fig. 2). The transition between $M_{\gamma\gamma}^2$ and M_{recoil}^2 fits is determined as the point of equal sensitivity obtained using background simulations.

The signal probability density function (PDF) has two components: a peaking contribution from correctly reconstructed signal photons and a combinatorial-background contribution from the other two combinations of photons. We model the peaking contribution using a Crystal Ball (CB) function [29]. The mass-dependent CB parameters used in the fits to data are fixed to those obtained by fitting simulated events. For the simulated M_{recoil}^2 distribution, the CB mean is found to be unbiased. For the simulated $M_{\gamma\gamma}^2$ distribution, we observe a linear bias of the CB mean of about 0.5% resulting from the combination of two photons with asymmetric reconstructed-energy distributions. This bias is determined to have negligible impact on the signal yield and mass determination; therefore, no attempt to correct for it is made. Combinatorial-background contributions from the wrong combinations of photons in signal events are taken into account by adding a mass-dependent, one-dimensional, smoothed kernel density estimation (KDE) [30] PDF obtained from signal simulation. The fits are performed in steps of m_a that correspond to half the CB width (σ_{CB}) for the respective squared mass. This results in

a total of 378 fits to the $M_{\gamma\gamma}^2$ distribution and 124 fits to the M_{recoil}^2 distribution. CB signal parameters are interpolated between the known simulated masses, and the KDE shape is taken from the simulation sample generated with the closest value of m_a to that assumed in the fit.

The photon-energy resolution $\sigma(E_\gamma)/E_\gamma$ in simulation is about 3% for $E_\gamma = 0.65$ GeV and improves to about 2% for $E_\gamma > 1$ GeV. Using the same muon-pair sample as used for the photon-energy bias study, we find that the photon energy resolution in simulation is better than that in data by at most 30% at low energies. Therefore, we apply an energy-dependent additional resolution smearing to our simulated signal samples before determining the CB resolution parameter σ_{CB} ; we assume conservatively that the full observed difference between data and simulation is due to the photon-energy-resolution difference. We assign half of the resulting mass-resolution difference as a systematic uncertainty. The effect of a ± 2 mm shift of the interaction point relative to the calorimeter is found to have a negligible impact on the mass resolution and is not included as a systematic uncertainty.

We describe the backgrounds by polynomials of the minimum complexity consistent with the data features. Polynomials of second to fifth order are used: second for $0.2 < m_a \leq 0.5 \text{ GeV}/c^2$, fourth for $0.5 < m_a \leq 6.85 \text{ GeV}/c^2$, and fifth for $6.85 < m_a \leq 9.7 \text{ GeV}/c^2$. The background polynomial parameters are not fixed by simulation but are free parameters of each data fit. Each fit is performed in a mass range that corresponds to $-20\sigma_{\text{CB}}$ to $+30\sigma_{\text{CB}}$ for $M_{\gamma\gamma}^2$, and $-25\sigma_{\text{CB}}$ to $+25\sigma_{\text{CB}}$ for M_{recoil}^2 . In addition, the fit ranges are constrained between $M_{\gamma\gamma}^2 > 0 \text{ GeV}^2/c^4$ and $M_{\text{recoil}}^2 < 100.5 \text{ GeV}^2/c^4$. The choice of the order of background polynomial and fit range is optimized based on the following conditions: giving a reduced χ^2 close to one, providing locally smooth fit results, and being consistent with minimal variations between adjacent fit ranges. Peaking backgrounds from $e^+e^- \rightarrow P\gamma$ are very small compared to the expected statistical uncertainty on the signal yield and found to be modeled adequately by the polynomial background PDF.

The systematic uncertainties due to the signal efficiency and the signal mass resolution are included as Gaussian nuisance parameters with a width equal to the systematic uncertainty. The systematic uncertainty due to the background shape, which is the dominant source of systematic uncertainty, is estimated by repeating all fits with alternative fit ranges changed by $\pm 5\sigma_{\text{CB}}$ and with the polynomial orders modified by ± 1 . For each mass value m_a , we report the smallest of all signal significance values determined from each background model. The local significance including systematic uncertainties is given by $S = \sqrt{2 \ln(\mathcal{L}/\mathcal{L}_{\text{bkg}})}$, where $\mathcal{L}$ is the maximum likelihood for the fit, and $\mathcal{L}_{\text{bkg}}$ is the likelihood for a fit to the background-only hypothesis. The local significances,

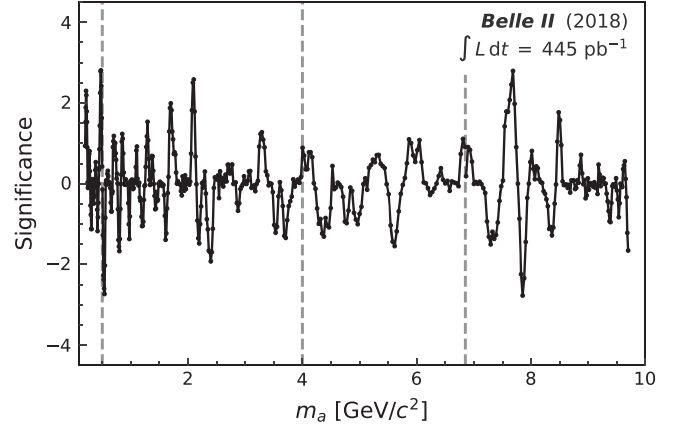


FIG. 3. Local signal significance S multiplied by the sign of the signal yield, including systematic uncertainties, as a function of ALP mass m_a . The vertical dashed lines indicate (from left to right) changes in the default background PDF ($0.5 \text{ GeV}/c^2$), in the photon energy selection criteria ($4.0 \text{ GeV}/c^2$), and in the invariant-mass determination method ($6.85 \text{ GeV}/c^2$).

multiplied by the sign of the signal yield, are shown in Fig. 3. The largest local significance, including systematic uncertainties, is found near $m_a = 0.477 \text{ GeV}/c^2$ with a value of $S = 2.8\sigma$.

By dividing the signal yield by the signal efficiency and the integrated luminosity, we obtain the ALP cross section σ_a . We compute the 95% confidence level (C.L.) upper limits on σ_a as a function of m_a using a one-sided frequentist profile-likelihood method [31]. For each m_a fit result, we report the least stringent of all 95% C.L. upper limits determined from the variations of background model and fit range. We convert the cross section limit to the coupling limit using

$$\sigma_a = \frac{g_{a\gamma\gamma}^2 \alpha_{\text{QED}}}{24} \left(1 - \frac{m_a^2}{s}\right)^3,$$

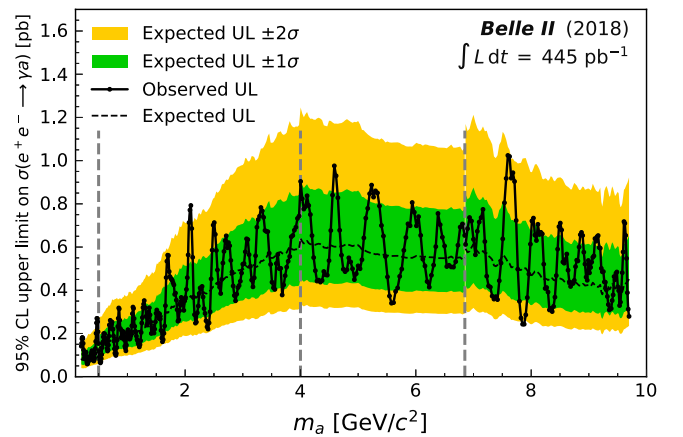


FIG. 4. Expected and observed upper limits (95% C.L.) on the ALP cross section σ_a . The vertical dashed lines are the same as those in Fig. 3.

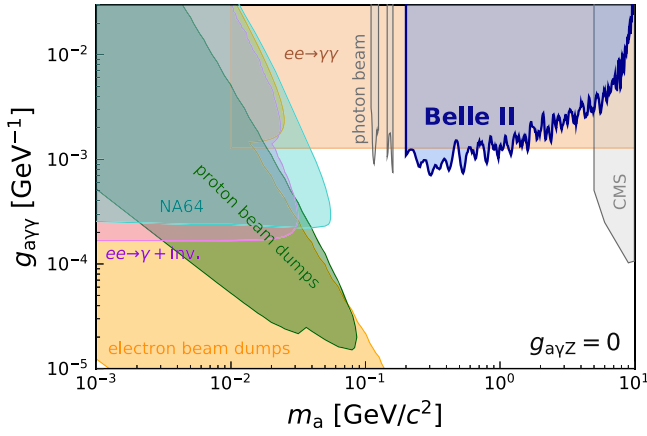


FIG. 5. Upper limit (95% C.L.) on the ALP-photon coupling from this analysis and previous constraints from electron beam-dump experiments and $e^+e^- \rightarrow \gamma + \text{invisible}$ [6,9], proton beam-dump experiments [8], $e^+e^- \rightarrow \gamma\gamma$ [11], a photon-beam experiment [12], and heavy-ion collisions [13].

where α_{QED} is the electromagnetic coupling [6]. This calculation does not take into account any energy dependence of α_{QED} and $g_{a\gamma\gamma}$ itself [32]. An additional 0.2% collision-energy uncertainty when converting σ_a to $g_{a\gamma\gamma}$ results in a negligible additional systematic uncertainty. Our median limit expected in the absence of a signal and the observed upper limits on σ_a are shown in Fig. 4. The observed upper limits on the photon couplings $g_{a\gamma\gamma}$ of ALPs, as well as existing constraints from previous experiments, are shown in Fig. 5. Additional plots and numerical results can be found in the Supplemental Material [33]. Our results provide the best limits for $0.2 < m_a < 5 \text{ GeV}/c^2$. This region of ALP parameter space is completely unconstrained by cosmological considerations [34]. The remaining mass region below $0.2 \text{ GeV}/c^2$ is challenging to probe at colliders due to the poor spatial resolution of photons from highly boosted ALP decays, and irreducible peaking backgrounds from π^0 production.

In conclusion, we search for $e^+e^- \rightarrow \gamma a$, $a \rightarrow \gamma\gamma$ in the ALP mass range $0.2 < m_a < 9.7 \text{ GeV}/c^2$ using Belle II data corresponding to an integrated luminosity of 445 pb^{-1} . We do not observe any significant excess of events consistent with the signal process and set 95% C.L. upper limits on the photon coupling $g_{a\gamma\gamma}$ at the level of 10^{-3} GeV^{-1} . These limits, the first obtained for the fully reconstructed three-photon final state, are more restrictive than existing limits from LEP-II [11]. In the future, with increased luminosity, Belle II is expected to improve the sensitivity to $g_{a\gamma\gamma}$ by more than one order of magnitude [6].

We thank the SuperKEKB group for the excellent operation of the accelerator; the KEK cryogenics group for the efficient operation of the solenoid; and the KEK computer group for on-site computing support. This work was supported by the following funding sources:

Science Committee of the Republic of Armenia Grant No. 18T-1C180; Australian Research Council and research Grants No. DP180102629, No. DP170102389, No. DP170102204, No. DP150103061, No. FT130100303, and No. FT130100018; Austrian Federal Ministry of Education, Science and Research, and Austrian Science Fund No. P 31361-N36; Natural Sciences and Engineering Research Council of Canada, Compute Canada and CANARIE; Chinese Academy of Sciences and research Grant No. QYZDJ-SSW-SLH011, National Natural Science Foundation of China and research Grants No. 11521505, No. 11575017, No. 11675166, No. 11761141009, No. 11705209, and No. 11975076, Liaoning Revitalization Talents Program under Contract No. XLYC1807135, Shanghai Municipal Science and Technology Committee under Contract No. 19ZR1403000, Shanghai Pujiang Program under Grant No. 18PJ1401000, and the CAS Center for Excellence in Particle Physics (CCEPP); the Ministry of Education, Youth and Sports of the Czech Republic under Contract No. LTT17020 and Charles University Grants No. SVV 260448 and No. GAUK 404316; European Research Council, 7th Framework PFI-FA-2013-622527, Horizon 2020 Marie Skłodowska-Curie Grant Agreement No. 700525 “NIOBE,” and Horizon 2020 Marie Skłodowska-Curie RISE project JENNIFER2 Grant Agreement No. 822070 (European grants); L’Institut National de Physique Nucléaire et de Physique des Particules (IN2P3) du CNRS (France); BMBF, DFG, HGF, MPG, AvH Foundation, and Deutsche Forschungsgemeinschaft (DFG) under Germany’s Excellence Strategy—EXC2121 “Quantum Universe”—Grant No. 390833306 (Germany); Department of Atomic Energy and Department of Science and Technology (India); Israel Science Foundation Grant No. 2476/17 and United States-Israel Binational Science Foundation Grant No. 2016113; Istituto Nazionale di Fisica Nucleare and the research grants BELLE2; Japan Society for the Promotion of Science, Grant-in-Aid for Scientific Research Grants No. 16H03968, No. 16H03993, No. 16H06492, No. 16K05323, No. 17H01133, No. 17H05405, No. 18K03621, No. 18H03710, No. 18H05226, No. 19H00682, No. 26220706, and No. 26400255, the National Institute of Informatics, and Science Information NETwork 5 (SINET5), and the Ministry of Education, Culture, Sports, Science, and Technology (MEXT) of Japan; National Research Foundation (NRF) of Korea Grants No. 2016R1D1A1B01010135, No. 2016R1D1A1B02012900, No. 2018R1A2B3003643, No. 2018R1A6A1A06024970, No. 2018R1D1A1B07047294, No. 2019K1A3A7A09033840, and No. 2019R1I1A3A01058933, Radiation Science Research Institute, Foreign Large-size Research Facility Application Supporting project, the Global Science

Experimental Data Hub Center of the Korea Institute of Science and Technology Information and KREONET/GLORIAD; Universiti Malaya RU grant, Akademi Sains Malaysia and Ministry of Education Malaysia; Frontiers of Science Program Contracts No. FOINS-296, No. CB-221329, No. CB-236394, No. CB-254409, and No. CB-180023, and SEP-CINVESTAV research Grant No. 237 (Mexico); the Polish Ministry of Science and Higher Education and the National Science Center; the Ministry of Science and Higher Education of the Russian Federation, Agreement No. 14.W03.31.0026; University of Tabuk research Grants No. S-1440-0321, No. S-0256-1438, and No. S-0280-1439 (Saudi Arabia); Slovenian Research Agency and research Grants No. J1-9124 and No. P1-0135; Agencia Estatal de Investigacion, Spain Grant No. FPA2014-55613-P and No. FPA2017-84445-P, and Grant No. CIDEAGENT/2018/020 of Generalitat Valenciana; Ministry of Science and Technology and research Grants No. MOST106-2112-M-002-005-MY3 and No. MOST107-2119-M-002-035-MY3, and the Ministry of Education (Taiwan); Thailand Center of Excellence in Physics; TUBITAK ULAKBIM (Turkey); Ministry of Education and Science of Ukraine; the US National Science Foundation and research Grants No. PHY-1807007 and No. PHY-1913789, and the US Department of Energy and research Grants No. DE-AC06-76RLO1830, No. DE-SC0007983, No. DE-SC0009824, No. DE-SC0009973, No. DE-SC0010073, No. DE-SC0010118, No. DE-SC0010504, No. DE-SC0011784, and No. DE-SC0012704; and the National Foundation for Science and Technology Development (NAFOSTED) of Vietnam under Contract No. 103.99-2018.45.

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