

# Predicted Optimal Bifunctional Electrocatalysts for the Hydrogen Evolution Reaction and the Oxygen Evolution Reaction Using Chalcogenide Heterostructures Based on Machine Learning Analysis of in Silico Quantum Mechanics Based High Throughput Screening

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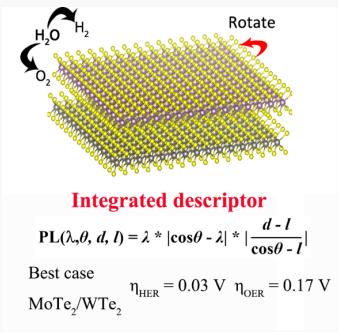
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**ABSTRACT:** Two-dimensional van der Waals heterostructure materials, particularly transition metal dichalcogenides (TMDC), have proved to be excellent photoabsorbers for solar radiation, but performance for such electrocatalysis processes as water splitting to form H<sub>2</sub> and O<sub>2</sub> is not adequate. We propose that dramatically improved performance may be achieved by combining two independent TMDC while optimizing such descriptors as rotational angle, bond length, distance between layers, and the ratio of the bandgaps of two component materials. In this paper we apply the least absolute shrinkage and selection operator (LASSO) process of artificial intelligence incorporating these descriptors together with quantum mechanics (density functional theory) to predict novel structures with predicted superior performance. Our predicted best system is MoTe<sub>2</sub>/WTe<sub>2</sub>, with a rotation of 300°, which is predicted to have an overpotential of 0.03 V for HER and 0.17 V for OER, dramatically improved over current electrocatalysts for water splitting.



There is an urgent need for clean and efficient sources of reliable energy to accommodate society demands of dramatically improved processes for clean renewable energy. In particular, electrocatalytic water splitting to produce H<sub>2</sub> (and O<sub>2</sub>) for use in hydrogen fuel cells to generate power is a most promising future source of energy. Consequently a great amount of research is being dedicated toward electrocatalytic water splitting in which two simultaneous chemical processes occur: the hydrogen evolution reaction (HER) and the oxygen evolution reaction.<sup>1</sup>

Previous experimental and computational studies reported that TMDC can be used in electrocatalytic water splitting. During the past decade, transition metal dichalcogenides (TMDC) have become a most promising 2D material for solar cells, catalysts, and lithium-ion batteries.<sup>2–6</sup> The excellent electrical conductivity and extraordinary catalytic performance of TMDC stem from the ability to effectively transfer electrons, suggesting that they could serve as superior HER cocatalysts.<sup>7</sup> Among the TMDC family, single-layer MX<sub>2</sub> (M = Mo, W; X = S, Se, Te, etc.) are the most studied. They have a direct bandgap,<sup>8</sup> and different MX<sub>2</sub> layers can be stacked to form novel heterojunction materials with deliberately adjusted bandgap.<sup>9</sup> Therefore, we combined these MX<sub>2</sub> monolayers under the condition of low mismatch to investigate their catalytic performance. Previous experimental research reported significant progresses in preparation and synthesis of two-dimensional heterojunctions that could produce high-quality 2D crystal optoelectronic devices.<sup>10,11</sup>

In this study, we consider vertical stacking of van der Waals heterojunction structures of MoS<sub>2</sub>/WS<sub>2</sub>, MoSe<sub>2</sub>/WSe<sub>2</sub>, MoS<sub>2</sub>/WSe<sub>2</sub>, MoSe<sub>2</sub>/WS<sub>2</sub>, MoTe<sub>2</sub>/WTe<sub>2</sub>, MoS<sub>2</sub>/WTe<sub>2</sub>, MoTe<sub>2</sub>/WS<sub>2</sub>, and MoTe<sub>2</sub>/WSe<sub>2</sub> as candidate bifunctional HER and OER catalysis. We consider the 2H phase structures for all TMDC, although the ground state of WTe<sub>2</sub> is known to be 1T.<sup>12,13</sup> In order to facilitate the comparison of the heterostructures, we chose the 2H phase of the MX<sub>2</sub> to construct the heterostructures.

Doping is commonly used to promote efficient electrocatalysis, but this may destabilize the initial structure. Instead, we propose to optimize the combination of two different TMDC where we also use the relative rotation of these heterostructures to improve electrocatalytic efficiency. Since the interactions between layers are dominated by van der Waals (i.e., or London) forces, we expected that their catalytic performance could be tuned while maintaining the original structure of the TMDC layers. We anticipated that stacking two TMDC layers with specific relative rotational angles might enhance performance. Indeed, Liu et al. put forward a new method to synthesize the 2D moiré superlattice.<sup>14</sup> Their study suggests that the two-dimensional moiré superlattice could

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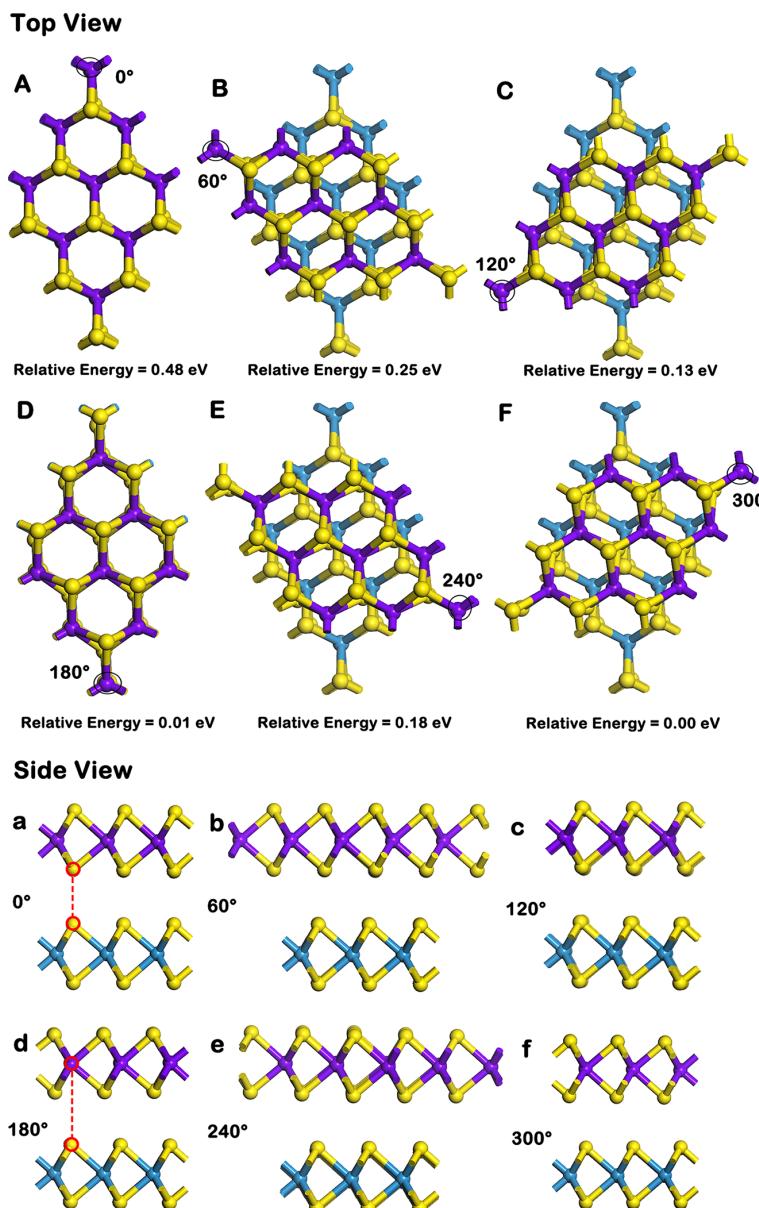


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**Figure 1.** Top view and the side view of the rotation process for the MoS<sub>2</sub>/WS<sub>2</sub> heterostructure for (A) 0°, (B) 60°, (C) 120°, (D) 180°, (E) 240°, and (F) 300°, respectively. We list the relative energies with respect to (F) for the optimized structures.

significantly improve the catalytic activity for a wide range of materials. Indeed, several experimental groups<sup>15–17</sup> have applied this method, reporting weak but stable coupling of MX<sub>2</sub> heterostructures with random rotational angles ( $0^\circ < \theta < 60^\circ$ ), which could help stabilize the overall structure. However, stable heterostructures with random relative rotations may not be easy to synthesize due to the large strain and lattice mismatch. For lattice-aligned interfaces, stacking with rotational angles that are multiples of 60° improves stability, making it more likely to be achievable experimentally.<sup>18,19</sup> Therefore, we constructed heterojunctions with relative rotational angles of 0°, 60°, 120°, 180°, 240°, and 300° for

all pairs of TMDC to develop a database that we use in our AI analysis.

In order to reduce the computational efforts of using density functional theory (DFT) to develop the data for large numbers of combinations, we used the LASSO (least absolute shrinkage and selection operator) to identify the physical descriptors that significantly affect the adsorption performance.<sup>20–22</sup> By evaluating the error characteristics of predictions for all possible descriptors, we propose the prediction equation for catalytic performance. With the help of machine learning and an optimized algorithm strategy, this saves an enormous amount of time for predicting and modifying structures and performance for new materials, while maintaining high

accuracy and convenience of DFT calculations. Thus, we trained the LASSO regression to extract linear correlations to predict new systems from calculated data. Many descriptors for single atom catalysts and intrinsic catalysts have been proposed, including d-band center,<sup>23,24</sup> generalized coordination number (GCN),<sup>25,26</sup> coordination number (CN),<sup>27</sup> electronegativity,<sup>28</sup> and formation energy.<sup>29</sup> Instead, we consider the rotation angle of TMDC heterojunctions as a descriptor to characterize their catalytic performance. Thus, we used four variables,

- the cosine of the rotational angle  $\theta$ ,
- the distance  $d$  between two secondary parts,
- the average bond length  $l$  of  $\text{MX}_2$ ,
- and the ratio of the bandgaps of two component materials  $E_{\text{grot}}$  and  $E_{\text{gsub}}$ , which is  $\frac{E_{\text{grot}}}{E_{\text{gsub}}}$  abbreviated as  $\lambda$ ,

which we introduce into LASSO to fit the linear regression. We used the LASSO algorithm to combine these separate variables into a large number of possible descriptors through various operations. This leads to a best-fit descriptor expression (1), called the LASSO performance descriptor PL,

$$\text{PL}(\lambda, \theta, d, l) = \lambda |\cos \theta - \lambda| \left| \frac{d - l}{\cos \theta - l} \right| \quad (1)$$

which contains all four variables. Substituting variable values into the descriptor expression, we found that a good linear relationship between the PL descriptor and the calculation results, which is  $y = -1.73x + 0.18$  for HER, and  $y = 1.04x + 0.6$  for OER. Consequently, we can use  $\text{PL}(\lambda, \theta, d, l)$  to predict HER and OER bifunctional catalytic performance of an enormous number of rotated TMDC heterostructures without an enormous number of expensive DFT calculations or cumbersome experiments.

**Basic Properties of the Heterostructure Materials.** To assess whether selected  $\text{MX}_2$  structures are suitable for electrocatalytic hydrogen production, we calculated the band structures of single-layer  $\text{MoS}_2$ ,  $\text{WS}_2$ ,  $\text{WSe}_2$ ,  $\text{MoSe}_2$ ,  $\text{MoTe}_2$ , and  $\text{WTe}_2$  using the Perdew–Burke–Ernzerhof (PBE) implementation of the generalized gradient approximation (GGA)<sup>30,31</sup> including the D3 empirical London dispersion correction with geometry optimization. The results are shown in Figure S1. Since PBE leads to systematic errors in band gaps, we estimate corrected band gaps using DFT+U methods.<sup>32</sup> This leads to the bandgaps of 1.68, 1.78, 1.32, 1.30, 1.08, and 1.04 eV for single-layer  $\text{MoS}_2$ ,  $\text{WS}_2$ ,  $\text{MoSe}_2$ ,  $\text{WSe}_2$ ,  $\text{MoTe}_2$  and  $\text{WTe}_2$ , respectively, which are consistent with the bandgaps of 1.68,<sup>33</sup> 1.81,<sup>33</sup> 1.44,<sup>34</sup> 1.25,<sup>35</sup> 1.07,<sup>34</sup> and 1.03 eV<sup>35</sup> reported in previous studies.

Previous studies have reported that  $\text{MX}_2$  monolayers have many excellent properties, but their catalytic activities in HER and OER catalysis are not adequate. We found that combining  $\text{MX}_2$  layers into a heterojunction allows the electronic properties to be tuned while preserving the exceptional characters of the original structures. Thus, we constructed a series of heterojunction structures with these  $\text{MX}_2$  layers. Then, we changed the angle between two  $\text{MX}_2$  layers to achieve lattice matching for best electrocatalysis performance.

**Binding Energy Analysis for the Heterostructures.** It is of great importance to determine the growth order of two different layers for vertically stacked heterostructures, that is, whether it is the  $\text{M}^{\text{A}}\text{X}_2^{\text{A}}/\text{M}^{\text{B}}\text{X}_2^{\text{B}}$  mode (where catalysis occurs on  $\text{M}^{\text{A}}\text{X}_2^{\text{A}}$ ) or the  $\text{M}^{\text{B}}\text{X}_2^{\text{B}}/\text{M}^{\text{A}}\text{X}_2^{\text{A}}$  mode (where catalysis occurs on

$\text{M}^{\text{B}}\text{X}_2^{\text{B}}$ ). Previous experiments indicate that  $\text{MoS}_2/\text{WS}_2$  has better catalytic performance for HER than  $\text{WS}_2/\text{MoS}_2$ .<sup>36</sup> Therefore, on the basis of the experiment, we expected that the reactions will occur on the more active Mo layer for vertically stacked heterojunction structures. Indeed, formation of van der Waals heterostructures of  $\text{MoTe}_2$  on  $\text{MoS}_2$  has been confirmed experimentally.<sup>37</sup> After constructing structures and calculating reaction surfaces, we considered rotation of  $\text{MoS}_2$  and  $\text{MoSe}_2$  on both  $\text{WS}_2$  and  $\text{WSe}_2$ , respectively. Optimized geometries of  $\text{MoS}_2/\text{WS}_2$  with six different rotation angles are shown in Figure 1. Each structure was rotated 60° counterclockwise on the basis of the previous structure, as illustrated by changes in the position of the circled atom Mo in Figure 1. Other systems were prepared following the same method.

For rapid analysis we evaluated the stability of heterojunctions by calculating<sup>38</sup>

$$E_{\text{binding}} = E_{\text{bi}} - E_{\text{monoA}} - E_{\text{monoB}}$$

where  $E_{\text{bi}}$ ,  $E_{\text{monoA}}$  and  $E_{\text{monoB}}$  represent relative energies of heterojunction, layer A and layer B, respectively.

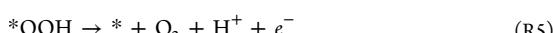
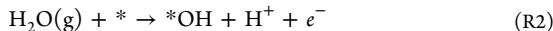
We show in Figure S2a that, as the layer rotates, the binding energy first decreases followed by a slight upward trend with 0° being the highest point. More detailed data are shown in Table S2. Since a more negative binding energy means increased stability, we confirmed the stability of all rotated structures. Figure S2a suggests that the binding energies of the heterojunctions depend on the angle. For each system, the binding energies and the angles follow a curved relationship. When the rotational angle is 180°, the binding energies of most of the systems reach the lowest value. Therefore, the most stable heterojunctions are the ones with a rotational angle of 180°. Since the stability of the heterojunctions depends on the layer spacing, we considered how the distance between layers of the heterojunctions depend on rotational angles, as shown in Figure S2b. From Figure S2a, we discovered that the layer spacing and the rotational angles are strongly correlated. Different optimized heterojunctions have different layer spacings, reflecting different strengths of van der Waals forces. The general trend is that layer spacing decreases with increasing angle and rises after 180°. For example, the initial distance between layers of the  $\text{MoTe}_2/\text{WTe}_2$  system is 3.787 Å. As the rotational angle increases, the layer spacing decreases reaching a minimum of 2.193 Å at 180°. As the rotational angle continues to increase, the interlayer distance increases again, reaching 3.605 Å at 300°, and finally returns to the initial structure. Originally, the upper and lower layers of the heterojunction were combined to obtain interactions between non-metal atoms of each (see Figure 1a); from the side view we see that the S atoms are opposite to the S atoms of the second layer. After rotation by 180°, these two layers have interactions between metal atoms and non-metal atoms (see Figure 1d), the S atoms are opposite to the metal atoms Mo of the other layer, which is relatively stronger. On the basis of the above analysis, we find that the heterojunctions with 180° rotation have the shortest layer distance and the most stable binding energy.

**Free Energy Analysis of the Heterostructures.** Calculations of HER and OER catalysis were based on the active surface of each system with catalytic performance estimated through reaction free energy of each step  $\Delta G = \Delta E + \Delta E_{\text{ZPE}} - T\Delta S$ , where  $\Delta E$  is the adsorption energy,  $\Delta E_{\text{ZPE}}$  is the zero point energy difference, and  $\Delta S$  is the entropy difference between initial state and adsorbed state.<sup>39</sup> Corresponding data of  $\Delta E_{\text{ZPE}}$

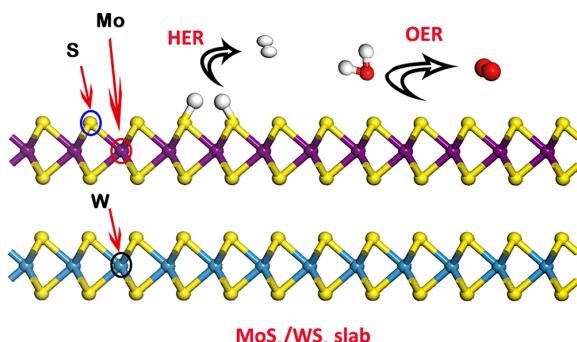
and  $\Delta S$  are listed in Table S1. In this calculation, we assume the Tafel mechanism for HER.<sup>40–43</sup>



whereas OER reaction consists of four steps:



In this sequence, each oxidation step produces an  $\text{H}^+$  and an electron, reducing the energy necessary to yield  $\text{O}_2$ . Regarding the selection of adsorption sites, we considered metal atom and non-metal atom adsorption sites at the edge and basal plane positions. When the rotational angle is  $0^\circ$ , the free energy of HER of  $\text{MoS}_2/\text{WS}_2$  is 0.29 eV at the edge site by adding 10 Å vacuum and 0.20 eV at the basal plane site; therefore, we chose the basal plane site as the adsorption site, which is consistent with the results reported by Ali<sup>44</sup> on similar 2H- $\text{MoS}_2$  materials. Moreover, although we constructed the structure in which the H atom is adsorbed at the metal site, we found that it goes to the non-metal site after geometry optimization. Therefore, we took the non-metal site on the basal plane as the reaction site, as shown in Figure 2. Other heterojunctions



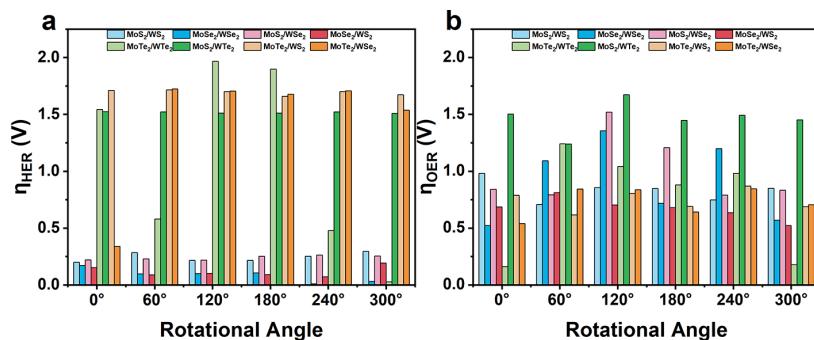
**Figure 2.** Schematic diagram of the  $0^\circ$ -rotated heterostructure  $\text{MoS}_2/\text{WS}_2$  configurations for overall water splitting. Purple represents the atom of Mo, yellow represents the atom S, and blue represents the atom W, respectively.

follow the same adsorption pattern. After optimization of  $^*\text{OH}$ ,  $^*\text{O}$ ,  $^*\text{OOH}$ , and  $^*\text{H}$  adsorption structures, reaction free energies  $\Delta G_{^*\text{OH}}$ ,  $\Delta G_{^*\text{O}}$ ,  $\Delta G_{^*\text{OOH}}$ , and  $\Delta G_{^*\text{H}}$  were calculated. For an ideal HER catalyst,  $\Delta G_{^*\text{H}}$  should be near 0 eV, while an ideal OER catalyst would have similar reaction free energies in those four charge transfer steps at zero potential ( $4.92 \text{ eV}/4 = 1.23 \text{ eV}$ ).<sup>45</sup> Following such criteria, we predicted the overpotential of HER ( $\eta_{\text{HER}}$ ) and OER ( $\eta_{\text{OER}}$ ) from free energy data listed in Tables S3–S10. This compares the catalytic performance among all systems, where  $\eta_{\text{HER}}$  equals  $|\Delta G_{^*\text{H}}|/e$  for HER and  $\eta_{\text{OER}}$  is determined by the potential limiting step, as is shown in the formula  $\eta_{\text{OER}} = \max[\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4]/e - 1.23$ . Here, a smaller  $\eta$  means a lower reaction barrier and better performance of the catalyst, as shown in Figure 3a for HER and Figure 3b for OER. Figures S3–S10 are the free-energy diagrams of the four-step reaction path of OER for each system at zero electrode potential. Corresponding diagrams of HER are also shown in Figures S11–S18.

As shown in Figure 3, the  $\text{MoS}_2/\text{WTe}_2$ ,  $\text{MoTe}_2/\text{WS}_2$ , and  $\text{MoTe}_2/\text{WSe}_2$  systems lead to rather poor electrocatalytic HER performance compared to other systems with overpotentials of HER higher than 1.5 V. This indicates that the heterostructures containing Te have less satisfactory HER performance than  $\text{MS}_2$  and  $\text{MSe}_2$ . In contrast among all systems with overpotential of HER less than 0.5 V, our results show that  $\text{MoSe}_2/\text{WSe}_2$  with a  $240^\circ$  rotation has the smallest  $\eta_{\text{HER}} = 0.01 \text{ V}$ , making this the best overall candidate for HER (see Figure S12 for details).

For the OER process most cases ( $\text{MoS}_2/\text{WS}_2$ ,  $\text{MoSe}_2/\text{WSe}_2$ ,  $\text{MoS}_2/\text{WSe}_2$ ,  $\text{MoSe}_2/\text{WS}_2$ ,  $\text{MoTe}_2/\text{WTe}_2$ ,  $\text{MoS}_2/\text{WTe}_2$ ,  $\text{MoTe}_2/\text{WS}_2$ , and  $\text{MoTe}_2/\text{WSe}_2$ ) have as the potential-determining step, the third step in which the adsorbed O atom reacts with an  $\text{H}_2\text{O}$  molecule to form the  $^*\text{OOH}$ . However, in the other two systems the final step that generates  $\text{O}_2$  determines the rate of the whole reaction process.<sup>46</sup> Overall,  $\text{MoTe}_2/\text{WTe}_2$  with no rotation has the lowest  $\eta_{\text{OER}} = 0.16 \text{ V}$ , whereas  $240^\circ$  rotated  $\text{MoSe}_2/\text{WSe}_2$  are best suited for electrocatalytic HER and  $0^\circ$   $\text{MoTe}_2/\text{WTe}_2$  are best suited for electrocatalytic OER.

OER is kinetically difficult since it involves the transfer of 4 electrons, usually with a high overpotential. We consider that the ideal catalyst for OER would have a similar energy required for each step instead of a high energy barrier for one step that prevents the reaction from proceeding. As shown in Figure S7, the  $0^\circ$ -rotated  $\text{MoTe}_2/\text{WTe}_2$  structure needs 1.12 eV for an  $\text{H}_2\text{O}$  molecule to decompose on the substrate to generate



**Figure 3.** Relationships of the rotational angle with  $\eta_{\text{HER}}$  and  $\eta_{\text{OER}}$  for each system.

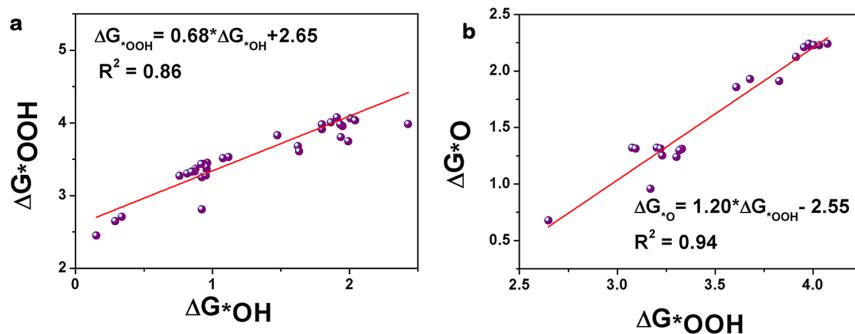


Figure 4. Linear relationships between adsorption free energies: (a)  $\Delta G_{\text{OOH}}$  and  $\Delta G_{\text{OH}}$ ; (b)  $\Delta G_{\text{O}}$  and  $\Delta G_{\text{OOH}}$ .

$^*\text{OH}$ . Another proton and electron are then lost from  $^*\text{OH}$  to form the  $^*\text{O}$  structure, which requires 1.07 eV. Subsequently, another  $\text{H}_2\text{O}$  molecule reacts with  $^*\text{O}$  to form  $^*\text{OOH}$ . This step requires 1.35 eV energy. The final step, in which  $^*\text{OOH}$  loses a proton and an electron to generate a free oxygen molecule, is the rate-determining step for the whole reaction with the energy change of 1.39 eV. Overall, the energy required in each step is similar, which promotes favorable reaction kinetics.

For HER, we use the Tafel mechanism, which requires the least energy change. For example, as shown in Figure S12, a proton and an electron forms  $^*\text{H}$  on  $\text{MoSe}_2/\text{WSe}_2$ . Then, a second  $\text{H}^+$  and  $e^-$  form a hydrogen molecule, but less energy is required, making the reaction faster. Thus, the 240°-rotated structure performs best for HER. The DFT analysis finds that the  $\text{MoTe}_2/\text{WTe}_2$  system with a rotational angle of 300° exhibits exceptional bifunctional HER ( $\eta_{\text{HER}} = 0.03$  V) and OER ( $\eta_{\text{OER}} = 0.17$  V) catalytic activities for complete water splitting compared to other  $\text{MX}_2$  heterojunctions.

As mentioned above, four free energies were calculated for each heterojunction system; hence, a total of 192 data points were obtained from 48 optimized systems. Our initial analysis suggested that there may be a linear correlation between free energies of HER and OER. We studied the relationship of  $\Delta G_{\text{O}}$ ,  $\Delta G_{\text{OH}}$ , and  $\Delta G_{\text{OOH}}$ , which we fitted using linear regressions as shown in Figure 4. The relationships are as follows:

$$\Delta G_{\text{OOH}} = 0.68 \times \Delta G_{\text{OH}} + 2.65 \quad (R^2 = 0.86)$$

$$\Delta G_{\text{O}} = 1.20 \times \Delta G_{\text{OOH}} - 2.55 \quad (R^2 = 0.94)$$

Root mean squared error (RMSE,  $R^2$ ) was employed to estimate the prediction performance of the models in this study for linear regression.<sup>47</sup> The best accuracy is achieved between two variables when  $R^2$  approaches 1. From the linear regression equations listed above, we see that the relationships  $\Delta G_{\text{OOH}}$  is adequate to derive the other free energy changes to describe the correlation between OER catalytic performance for most TMDC systems tested. However, since obtaining  $\Delta G_{\text{OOH}}$  requires DFT calculations, we want to identify the reactivity of a TMDC system based on inherent properties that could be expressed in terms of a universal descriptor for OER catalysis.

**Physical Descriptors Predicted by the LASSO Regression Approach.** Our DFT calculations revealed a relationship between the free energy between HER and OER. We used the least absolute shrinkage and selection operator

(LASSO)<sup>48–50</sup> in this study, since it automatically finds the most suitable descriptor using the input variables. LASSO is of great help in dealing with this problem giving a linear model with sparse coefficients. By applying a penalty function, LASSO tends to use fewer coefficients thereby reducing less relevant dependent variables. Normally, the input parameters for a machine learning model might be the atomic radius, electronegativity, valence electron number, and density of the atoms.<sup>51</sup> Instead, we used structural parameters that greatly influence the heterojunctions including rotational angle ( $\cos \theta$ ) and layer spacing ( $d$ ) according to their relationship aforementioned, as well as the bond length ( $l$ ), and the ratio of the bandgaps of two component materials,  $E_{\text{grot}}$  and  $E_{\text{gsub}}$ ,  $\frac{E_{\text{grot}}}{E_{\text{gsub}}}$

which is abbreviated to  $\lambda$ , as input parameters. In the descriptor, the distances between layers are the direct and vertical distance between the non-metal atoms of the heterojunction, the bond lengths are the average bond length between the metal and non-metal atoms in the rotated systems, and the band gaps are the top and bottom monolayers of the heterostructure that are available in the online database. Through these descriptors, we used LASSO linear regression to derive a linear equation for supervised learning, effectively predicting the catalytic performance of two-dimensional heterojunction materials of other systems and reducing unnecessary calculations. Combining the parameters affecting the heterojunction structures with the LASSO linear regression, we established a predictive model for screening the superior overpotential for OER performance of heterojunctions. In this calculation, we used five variables as inputs, the ratio of band gaps, rotational angles and their cosine values, distances between layers, and bond length, and we use  $\eta_{\text{OER}}$  as the output. Due to the limited size of the data set (48 points), the code for big data analysis was deployed in MATLAB.<sup>29</sup> By modifying the code specifically for this work, we obtained proper descriptors for the linear regression. We found the most suitable descriptor through the following three steps:

Step 1, set up primary variables mentioned above to run a big data code that generates a descriptor set.

Step 2, narrow down the top descriptors for  $\eta_{\text{OER}}$  by LASSO.

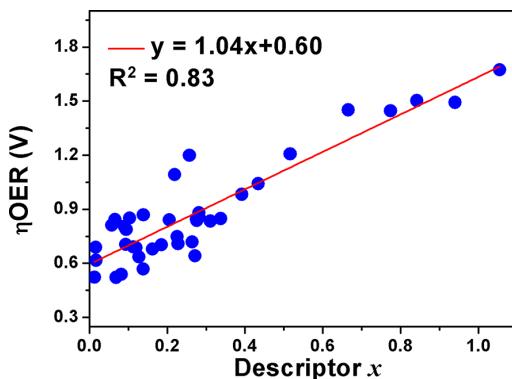
Step 3, further analyze to find the best descriptor.

In step 1, we generated 257 703 possible descriptors by combining one or more input values through operations including addition, subtraction, multiplication, division, absolute value, square, and square root. From these descriptors, LASSO fitted an equation that best describes the linear relationship. We repeated the procedure 50 times,

standardizing the remaining 90% of the training data each time before the LASSO step. After these treatments,  $\eta_{\text{OER}}$  were found to be perfectly fitted by the descriptor

$$PL(\lambda, \theta, d, l) = \lambda|\cos \theta - \lambda| \left| \frac{d - l}{\cos \theta - l} \right| \quad (2)$$

where  $\lambda = \frac{E_{\text{g}_{\text{rot}}}}{E_{\text{g}_{\text{sub}}}}$ . The fitted equation leads to  $y = 1.04x + 0.6$ ,  $R^2 = 0.83$  for OER, as shown in Figure 5. This establishes that



**Figure 5.** Relationships between the descriptor  $PL(\lambda, \theta, d, l) = \lambda|\cos \theta - \lambda| \left| \frac{d - l}{\cos \theta - l} \right|$  and catalytic performance for OER, the relationship between the descriptor  $x$  and  $\eta_{\text{OER}}$  that was fitted by LASSO regression.

simple combinations of existing intrinsic properties can be found to fit a linear relationship for OER. We found that the linear relationship for HER can be fitted using the same descriptor, leading to  $y = -1.73x + 0.18$ ,  $R^2 = 0.80$ . Therefore, we conclude that the descriptor  $PL(\lambda, \theta, d, l) = \lambda|\cos \theta - \lambda| \left| \frac{d - l}{\cos \theta - l} \right|$  is able to fit the electrocatalytic performance of both HER and OER effectively. Then we used this equation from the LASSO regression to predict the overpotentials of HER and OER. We used the  $\eta_{\text{OER}}$  to derive  $\Delta G^*_{\text{O}_2}$ ,  $\Delta G^*_{\text{OOH}}$ , and  $\Delta G^*_{\text{OH}}$ , as shown in Figure 4. The final universal activity descriptor is composed of physical properties obtained from the LASSO regression.

In all, we predicted both HER and OER performance for eight different heterostructures, namely,  $\text{MoS}_2/\text{WS}_2$ ,  $\text{MoSe}_2/\text{WSe}_2$ ,  $\text{MoS}_2/\text{WSe}_2$ ,  $\text{MoSe}_2/\text{WS}_2$ ,  $\text{MoTe}_2/\text{WTe}_2$ ,  $\text{MoS}_2/\text{WTe}_2$ ,  $\text{MoTe}_2/\text{WS}_2$ , and  $\text{MoTe}_2/\text{WSe}_2$ . We selected vertical stacking structures by comparing bandgaps for various stacking patterns. All heterojunctions constructed here were confirmed to be stable. On the basis of calculating the binding energy of five heterostructures for multiple rotational angles, we found that the most stable structures have a rotational angle of  $180^\circ$ . From reaction free energy analysis of HER and OER catalysis, we discovered that the catalytic performance could be significantly improved by rotating the heterojunction structure. Among all calculated structures, we found that  $\text{MoTe}_2/\text{WTe}_2$  with a rotational angle of  $300^\circ$  has the best overall performance for  $\eta_{\text{HER}}$  and  $\eta_{\text{OER}}$ , leading to an overpotential of 0.03 V for HER and 0.17 V for OER. These results are better than any current water splitting catalyst.

In order to find the correlation between heterostructures and reaction free energy, we included the following

descriptors: rotational angle, bond length, layer distance, and bandgap in the LASSO regression analysis. Through scanning combinations of descriptors using LASSO, we found the best descriptor from the linear regression to be  $PL(\lambda, \theta, d, l) = \lambda|\cos \theta - \lambda| \left| \frac{d - l}{\cos \theta - l} \right|$ . These results validate our application of LASSO regression of electrocatalytic 2D heterostructure screening catalytic performance of novel TMDC for OER and HER easily without complicated experiments or calculations.

**Computational Methods.** We carried out spin-polarized density functional theory (DFT) calculations using VASP.<sup>52</sup> We employed the Perdew–Burke–Ernzerhof (PBE) functional<sup>50,51</sup> within the generalized gradient approximation (GGA)<sup>53</sup> to describe the exchange–correlation energy between electrons. We included van der Waals attraction using the DFT-D3 scheme.<sup>30</sup> Interactions between the nuclei and core electrons were described by the projector augmented wave (PAW) method.<sup>54–56</sup> The plane-wave basis set cutoff energy was set at 450 eV. A vacuum slab of 15 Å was set throughout all calculations to avoid interactions between repeated images.

We used a  $3 \times 3$  supercell and  $3 \times 3 \times 1$   $k$ -point mesh for all systems. The convergence criteria for energy and force were set to  $1.0 \times 10^{-5}$  eV and  $-0.05$  eV/Å for each atom. GGA+U was set to be 3.4 eV for the d electrons.

For calculations of band structures and density of states (DOS), we employed the Dudarev DFT+U<sup>32</sup> formalism to treat the d states of  $\text{MoS}_2$ ,  $\text{MoSe}_2$ , and  $\text{MoTe}_2$  and f states of  $\text{WS}_2$ ,  $\text{WSe}_2$ , and  $\text{WTe}_2$ , using  $U$  values of 3.4 eV to deal with these strongly correlated systems.

The lattice parameters of monolayer  $\text{MoS}_2$  and  $\text{WS}_2$  are  $a = b = 9.498$  Å, of  $\text{WSe}_2$  and  $\text{MoSe}_2$  are  $a = b = 9.981$  Å, and of monolayer  $\text{MoTe}_2$  and  $\text{WTe}_2$  are  $a = b = 10.67$  Å; thus, their structures are quite similar. A series of heterostructures were built by  $\text{MX}_2$  monolayers combining with each other. Adsorbates of  $^*{\text{H}}$ ,  $^*{\text{O}}$ ,  $^*{\text{OH}}$ , and  $^*{\text{OOH}}$  were added at the position of the S atom in calculations of adsorption patterns.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcllett.9b03875>.

Calculation method of HER and OER activity; structures of heterojunctions; free-energy diagrams for HER and OER of all heterojunctions; tables of binding energies, adsorption free energies, and corrections for gas phase free energies, entropies, and enthalpies (PDF)

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**Notes**

The authors declare no competing financial interest.

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