

Transition to strong coupling regime in hybrid plasmonic systems: Exciton-induced transparency and Fano interference

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We present a microscopic model describing the transition to strong coupling regime for an emitter resonantly coupled to a surface plasmon in a metal-dielectric structure. We demonstrate that the shape of scattering spectra is determined by an interplay of two distinct mechanisms. First is the near-field coupling between the emitter and the plasmon mode which underpins energy exchange between the system components and gives rise to exciton-induced transparency minimum in scattering spectra prior the transition to strong coupling regime. The second mechanism is Fano interference between the plasmon dipole and the plasmon-induced emitter's dipole as the system interacts with the radiation field. We show that the Fano interference can strongly affect the overall shape of scattering spectra, leading to the inversion of spectral asymmetry that was recently reported in the experiment.

I. INTRODUCTION

Strong coupling between surface plasmons in metal-dielectric structures and excitons in semiconductors or dye molecules has recently attracted intense interest driven to a large extent by possible applications in ultrafast reversible switching [1–3], quantum computing [4, 5], and light harvesting [6]. In the strong coupling regime, coherent energy exchange between excitons and plasmons [7] leads to the emergence of mixed polaritonic states with energy bands separated by the anticrossing gap (Rabi splitting) [8]. For excitons coupled to cavity modes in microcavities, the Rabi splitting magnitudes are relatively small on the scale of several meV [9–11]. However, in hybrid plasmonic systems, where surface plasmons are coupled to excitons in J-aggregates [12–22], in various dye molecules [23–27] or in semiconductor nanostructures [28–31], the Rabi splittings can be much greater even reaching hundreds meV. For single excitons, however, achieving a strong exciton-plasmon coupling is a challenging task as it requires extremely small plasmon mode volumes, which can mainly be achieved in nanogaps [32–34].

At the same time, the scattering spectra of hybrid plasmonic systems, such as excitons in J-aggregates or colloidal QDs coupled to gap plasmons in nanoparticle-on-metal (NoM) systems [35–38] or those in two-dimensional atomic crystals conjugated with Ag or Au nanostructures [39–44], exhibit a narrow minimum even before reaching the strong coupling transition point. The emergence of such a minimum in the weak coupling regime is referred to as exciton-induced transparency (ExIT) [45–47], in analogy to electromagnetically-induced transparency (EIT) in pumped three-level atomic systems that is attributed to Fano interference between different excitation pathways. Recently, we have shown that, in the linear regime (i.e., in the absence of pump), the emergence of this minimum is due to imbalance of energy exchange between the emitter and plasmon in a narrow frequency interval [48]. Typically, the plasmon optical dipole moment significantly (by $\sim 10^4$) exceeds that of an exciton in a semiconductor quantum dot and so the emitter's direct interaction with the radiation field is relatively weak [49]. In this case, the ExIT minimum in scattering spectra is described, with a reasonably good accuracy, by the dressed plasmon model or by its classical ana-

logue – the coupled oscillators model, in which only the plasmon interacts with the radiation field, so that the scattering spectra show a narrow ExIT minimum on top of a broad plasmon band, while the overall spectral weight is tilted towards the higher frequency range [38, 47, 48].

On the other hand, in hybrid plasmonic systems, the *optical* interference between an exciton and a plasmon can arise from indirect coupling of exciton to the radiation field. Namely, if the incident light frequency is tuned to the plasmon resonance, the exciton dipole moment *induced* by the plasmon near field is not necessarily small, so that the exciton can substantially contribute, albeit indirectly, to the system optical transition. This gives rise to Fano interference between the plasmon and plasmon-induced exciton dipoles which can significantly affect the overall shape of optical spectra. As we show in this paper, such Fano interference effects can lead to *inversion of spectral asymmetry*, characterized by spectral weight shift towards lower frequency range, which was observed for excitons coupled to localized plasmon modes [22, 39, 40].

In this paper, we present a microscopic model for linear optical response of a single exciton resonantly coupled to a surface plasmon mode in a metal-dielectric structure which accounts for both ExIT and Fano interference effects as the system transitions to strong coupling regime. Starting with the canonical Hamiltonian with microscopic coupling parameters [50], we set up the system of Maxwell-Bloch equations for induced dipole moments which determine scattering spectrum of the hybrid plasmonic system. We further show that while the ExIT minimum results from the energy exchange imbalance in a narrow frequency interval, the overall spectral shape of scattering spectra is strongly affected by the Fano interference between radiating plasmon and plasmon-induced exciton dipoles. Specifically, we demonstrate that Fano interference can lead to an inversion of spectral asymmetry, consistent with the experiment [22, 39, 40].

II. THE SYSTEM HAMILTONIAN AND MICROSCOPIC COUPLING PARAMETERS

We consider a quantum emitter (QE) with dipole moment μ_e and excitation frequency ω_e situated at a position r_e near

a metal-dielectric structure characterized by complex dielectric function $\varepsilon(\omega, \mathbf{r}) = \varepsilon'(\omega, \mathbf{r}) + i\varepsilon''(\omega, \mathbf{r})$ supporting localized plasmon modes with frequencies ω_m interacting with external electromagnetic (EM) field $\mathbf{E}(t)$. For monochromatic EM field of frequency ω , in the rotating wave approximation (RWA), the system dynamics is described by the Hamiltonian

$$H = \hbar\omega_m \hat{a}^\dagger \hat{a} + \hbar\omega_e \hat{\sigma}^\dagger \hat{\sigma} + \hbar g (\hat{\sigma}^\dagger \hat{a} + \hat{a}^\dagger \hat{\sigma}) - (\boldsymbol{\mu}_m \cdot \mathbf{E} \hat{a}^\dagger e^{-i\omega t} + \boldsymbol{\mu}_e \cdot \mathbf{E} \hat{\sigma}^\dagger e^{-i\omega t} + \text{H.c.}), \quad (1)$$

where \hat{a}_m^\dagger and \hat{a}_m are the plasmon creation and annihilation operators, $\hat{\sigma}^\dagger$ and $\hat{\sigma}$ are the raising and lowering operators for the QE, while the parameters g and $\boldsymbol{\mu}_m$ characterize, respectively, plasmon's coupling to the QE and EM field.

For plasmonic nanostructures with characteristic size smaller than the radiation wavelength, the coupling parameters can be obtained microscopically by relating them to system geometry and local field [50]. For such systems, the plasmon modes are determined by the quasistatic Gauss equation [51] $\nabla \cdot [\varepsilon'(\omega_m, \mathbf{r}) \nabla \Phi_m(\mathbf{r})] = 0$, where $\Phi_m(\mathbf{r})$ is the mode potential that defines the mode field $\mathbf{E}_m(\mathbf{r}) = -\nabla \Phi_m(\mathbf{r})$, which we choose to be real. To determine the plasmon dipole moment for optical transitions, we recast the Gauss's law as $\nabla \cdot [\mathbf{E}_m(\mathbf{r}) + 4\pi \mathbf{P}_m(\mathbf{r})] = 0$, where $\mathbf{P}_m(\mathbf{r}) = \chi'(\omega_m, \mathbf{r}) \mathbf{E}_m(\mathbf{r})$ is the electric polarization vector and $\chi = (\varepsilon - 1)/4\pi$ is the plasmonic system susceptibility. The plasmon dipole moment has the form

$$\mathbf{p}_m = \int dV \mathbf{P}_m = \int dV \chi'(\omega_m, \mathbf{r}) \mathbf{E}_m(\mathbf{r}). \quad (2)$$

The Gauss's equation does not determine the overall field normalization [51], but the later can be found by matching the plasmon radiative decay rate and that of a localized dipole with excitation energy $\hbar\omega_m$. The plasmon radiative decay rate has the form [52] $\gamma_m^r = W_m^r/U_m$, where

$$U_m = \frac{1}{16\pi} \int dV \frac{\partial[\omega_m \varepsilon'(\omega_m, \mathbf{r})]}{\partial \omega_m} \mathbf{E}_m^2(\mathbf{r}), \quad (3)$$

is the plasmon mode energy [53, 54] and

$$W_m^r = \frac{p_m^2 \omega_m^4}{3c^3}, \quad (4)$$

is the radiated power (c is the speed of light) [8]. The normalized modes $\tilde{\mathbf{E}}_m(\mathbf{r})$ are thus determined by setting

$$\gamma_m^r = \frac{4\mu_m^2 \omega_m^3}{3\hbar c^3}, \quad (5)$$

where $\boldsymbol{\mu}_m$ is the mode optical transition matrix element. We then find the normalization relation as

$$\tilde{\mathbf{E}}_m(\mathbf{r}) = \frac{1}{2} \sqrt{\frac{\hbar\omega_m}{U_m}} \mathbf{E}_m(\mathbf{r}), \quad (6)$$

where the scaling factor $\sqrt{\hbar\omega_m/U_m}$ converts the plasmon energy U_m to $\hbar\omega_m$ in order to match the EM field energy (the

factor 1/2 reflects positive-frequency contribution). Accordingly, the plasmon optical transition matrix element in the Hamiltonian (1) takes the form [compare to Eq. (2)]

$$\boldsymbol{\mu}_m = \int dV \chi'(\omega_m, \mathbf{r}) \tilde{\mathbf{E}}_m(\mathbf{r}). \quad (7)$$

In a similar way, the plasmon non-radiative decay rate is $\gamma_m^{nr} = W_m^{nr}/U_m$, where $W_m^{nr} = \frac{1}{8\pi} \int dV \varepsilon''(\omega_m, \mathbf{r}) \mathbf{E}_m^2(\mathbf{r})$ is the power dissipated in the plasmonic structure due to Ohmic losses. In terms of normalized fields, the non-radiative rate takes the form

$$\gamma_m^{nr} = \frac{1}{2\pi\hbar\omega_m} \int dV \varepsilon''(\omega_m, \mathbf{r}) \tilde{\mathbf{E}}_m^2(\mathbf{r}), \quad (8)$$

and so the plasmon full decay rate is $\gamma_m = \gamma_m^{nr} + \gamma_m^r$. Note that in structures with a single metallic component, the standard expression [51] for γ_m^{nr} is recovered: $\gamma_m^{nr} = 2\varepsilon''(\omega_m)/[\partial\varepsilon'(\omega_m)/\partial\omega_m]$. The optical polarizability tensor of a plasmonic structure describing its response to the external field $\mathbf{E}e^{-i\omega t}$ has the form

$$\boldsymbol{\alpha}_m(\omega) = \frac{1}{\hbar} \frac{\boldsymbol{\mu}_m \boldsymbol{\mu}_m}{\omega_m - \omega - \frac{i}{2}\gamma_m}, \quad (9)$$

where we kept only the resonance term [52].

The QE-plasmon coupling in the Hamiltonian (1) is expressed via normalized plasmon mode fields as [50]

$$\hbar g = -\boldsymbol{\mu}_e \cdot \tilde{\mathbf{E}}_m(\mathbf{r}_e). \quad (10)$$

To present the coupling in a cavity-like form, we use the original plasmon mode fields (6) to obtain [7]

$$g^2 = \frac{2\pi\mu_e^2 \omega_m}{\hbar\mathcal{V}}, \quad \frac{1}{\mathcal{V}} = \frac{2[\mathbf{n}_e \cdot \mathbf{E}_m(\mathbf{r}_e)]^2}{\int dV [\partial(\omega_m \varepsilon')/\partial\omega_m] \mathbf{E}_m^2}, \quad (11)$$

where \mathcal{V} is projected plasmon mode volume characterizing plasmon field confinement at the emitter position \mathbf{r}_e along its dipole orientation \mathbf{n}_e [52, 54, 55]. The plasmon mode volume defines the Purcell factor characterizing radiation enhancement of a QE near a plasmonic structure:

$$F_p = \frac{\gamma_{e \rightarrow m}}{\gamma_e^r} = \frac{6\pi c^3 Q_m}{\omega_m^3 \mathcal{V}} \quad (12)$$

where $Q_m = \omega_m/\gamma_m$ is plasmon quality factor, $\gamma_e^r = 4\mu_e^2 \omega_m^3/3\hbar c^3$ is the emitter's radiative decay rate (at plasmon resonance frequency) and $\gamma_{e \rightarrow m}$ is the rate of energy transfer (ET) from QE to plasmon, given by

$$\gamma_{e \rightarrow m} = \frac{8\pi\mu_e^2 Q_m}{\hbar\mathcal{V}}. \quad (13)$$

Comparing Eqs. (11) and (13), we obtain a relation between the QE-plasmon coupling and decay rates:

$$g^2 = \frac{1}{4} \gamma_m \gamma_{e \rightarrow m} = \frac{F_p}{4} \gamma_m \gamma_e^r. \quad (14)$$

Thus, all coupling parameters in the Hamiltonian characterizing plasmon interactions with the QE and EM field are expressed via system parameters and related to plasmon and QE decay rates. Below, we employ these microscopic expressions to elucidate the role of ExIT and Fano interference in scattering spectra of hybrid plasmonic systems.

III. OPTICAL DIPOLE MOMENT OF A HYBRID PLASMONIC SYSTEM

We are interested in the linear response of hybrid plasmonic system to the external EM field. We assume that there is only a single excitation in the system and disregard any non-linear effects. In this case, we can approximate the QE by bosonic operators to setup Maxwell-Bloch (MB) equations for non-diagonal elements of density matrix (polarizations) $\rho_e(t)$ and $\rho_m(t)$ related to QE and plasmon induced dipoles as $\mathbf{p}_e(t) = \boldsymbol{\mu}_e \rho_e(t)$ and $\mathbf{p}_m(t) = \boldsymbol{\mu}_m \rho_m(t)$, respectively. Using the Hamiltonian (1), in the linear approximation, the MB equations for $\rho_m(t)$ and $\rho_e(t)$ are obtained in a standard manner as

$$\begin{aligned} i\dot{\rho}_m &= (\omega_m - i\gamma_m/2)\rho_m + g\rho_e - \boldsymbol{\mu}_m \cdot \mathbf{E} e^{-i\omega t}, \\ i\dot{\rho}_e &= (\omega_e - i\gamma_e/2)\rho_e + g\rho_m - \boldsymbol{\mu}_e \cdot \mathbf{E} e^{-i\omega t}, \end{aligned} \quad (15)$$

where dot stands for the time-derivative and γ_e is the QE spectral linewidth assumed much smaller than γ_m .

In the steady-state case, substituting $\rho_m(t) = \rho_m e^{-i\omega t}$ and $\rho_e(t) = \rho_e e^{-i\omega t}$, we find

$$\rho_m = \frac{(\omega_e - \omega - \frac{i}{2}\gamma_e) \boldsymbol{\mu}_m \cdot \mathbf{E} - g\boldsymbol{\mu}_e \cdot \mathbf{E}}{(\omega_m - \omega - \frac{i}{2}\gamma_m)(\omega_e - \omega - \frac{i}{2}\gamma_e) - g^2} \quad (16)$$

and

$$\rho_e = \frac{(\omega_m - \omega - \frac{i}{2}\gamma_m) \boldsymbol{\mu}_e \cdot \mathbf{E} - g\boldsymbol{\mu}_m \cdot \mathbf{E}}{(\omega_m - \omega - \frac{i}{2}\gamma_m)(\omega_e - \omega - \frac{i}{2}\gamma_e) - g^2}. \quad (17)$$

The system's induced dipole moment is $\mathbf{p}_s = \mathbf{p}_m + \mathbf{p}_e = \boldsymbol{\mu}_m \rho_m + \boldsymbol{\mu}_e \rho_e$. To elucidate the processes contributing to \mathbf{p}_s , we define QE polarizability tensor (in RWA) as

$$\boldsymbol{\alpha}_e(\omega) = \frac{1}{\hbar} \frac{\boldsymbol{\mu}_e \boldsymbol{\mu}_e}{\omega_e - \omega - \frac{i}{2}\gamma_e}, \quad (18)$$

and introduce *plasmon-induced* QE dipole moment as

$$\mathbf{q}_e(\omega) = \boldsymbol{\alpha}_e(\omega) \tilde{\mathbf{E}}_m(\mathbf{r}_e) = \frac{\boldsymbol{\mu}_e \boldsymbol{\mu}_e \cdot \tilde{\mathbf{E}}_m(\mathbf{r}_e)}{\hbar \omega_e - \omega - \frac{i}{2}\gamma_e}. \quad (19)$$

Then, the hybrid system dipole moment can be decomposed into three contributions:

$$\mathbf{p}_s = \mathbf{p}_{dp} + \mathbf{p}_{int} + \mathbf{p}_{de}. \quad (20)$$

The main contribution comes from the *dressed plasmon* characterized by induced dipole moment

$$\mathbf{p}_{dp} = \frac{1}{\hbar} \frac{\boldsymbol{\mu}_m (\boldsymbol{\mu}_m \cdot \mathbf{E})}{\omega_m + \Sigma_m(\omega) - \omega - \frac{i}{2}\gamma_m}, \quad (21)$$

where

$$\Sigma_m(\omega) = -\frac{g^2}{\omega_e - \omega - \frac{i}{2}\gamma_e} = -\mathbf{q}_e(\omega) \cdot \tilde{\mathbf{E}}_m(\mathbf{r}_e), \quad (22)$$

is plasmon's self-energy due to its interactions with the QE. Specifically, the imaginary part of self-energy determines the ET rate from the plasmon to QE as

$$\gamma_{m \rightarrow e}(\omega) = -2\Sigma_m''(\omega) = \frac{g^2 \gamma_e}{(\omega - \omega_e)^2 + \gamma_e^2/4}, \quad (23)$$

which represents a Lorentzian centered at QE frequency ω_e and maximum value $\gamma_{m \rightarrow e} \equiv \gamma_{m \rightarrow e}(\omega_e) = 4g^2/\gamma_e$.

The QE-plasmon *interference* term has the form

$$\mathbf{p}_{int} = \frac{1}{\hbar} \frac{\boldsymbol{\mu}_m (\mathbf{q}_e \cdot \mathbf{E}) + \mathbf{q}_e (\boldsymbol{\mu}_m \cdot \mathbf{E})}{\omega_m + \Sigma_m(\omega) - \omega - \frac{i}{2}\gamma_m}, \quad (24)$$

and describes *indirect*, i.e., mediated by plasmon, interactions of QE with the EM field. The last term represents dressed QE contribution,

$$\mathbf{p}_{de} = \frac{1}{\hbar} \frac{\boldsymbol{\mu}_e (\boldsymbol{\mu}_e \cdot \mathbf{E})}{\omega_e + \Sigma_e(\omega) - \omega - \frac{i}{2}\gamma_e}, \quad (25)$$

where

$$\Sigma_e(\omega) = -\frac{g^2}{\omega_m - \omega - \frac{i}{2}\gamma_m}, \quad (26)$$

is the QE self-energy, whose imaginary part now determines the ET rate from the QE to plasmon as

$$\gamma_{e \rightarrow m}(\omega) = -2\Sigma_e''(\omega) = \frac{g^2 \gamma_m}{(\omega - \omega_m)^2 + \gamma_m^2/4}, \quad (27)$$

which represents a Lorentzian centered at plasmon frequency ω_m and maximum value $\gamma_{e \rightarrow m} \equiv \gamma_{e \rightarrow m}(\omega_m) = 4g^2/\gamma_m$, matching Eq. (14). Importantly, in a narrow frequency interval $|\omega - \omega_e| \lesssim \gamma_e$, the *reverse* plasmon-QE ET rate $\gamma_{m \rightarrow e}$ exceeds the direct QE-plasmon ET rate $\gamma_{e \rightarrow m}$:

$$\frac{\gamma_{m \rightarrow e}}{\gamma_{e \rightarrow m}} = \frac{\gamma_m}{\gamma_e} \gg 1. \quad (28)$$

Although the overall ET balance over the entire frequency range is preserved, the ET *imbalance* in the frequency interval $\sim \gamma_e$ leads to emergence of the ExIT minimum in the dressed plasmon spectra [48]. For a typical case $\mu_e/\mu_m \ll 1$, the dressed emitter's dipole moment (25) is negligible small relative to dressed plasmon's dipole moment (21) and can be omitted. While the dressed plasmon approximation, i.e., $\mathbf{p}_s \approx \mathbf{p}_{dp}$, describes, with a reasonable accuracy, the position and magnitude of the ExIT minimum in terms of energy exchange between the QE and plasmon, it does *not* account for QE interactions with the EM field. The latter is included *indirectly* in the interference term (24) via plasmon-induced QE dipole moment \mathbf{q}_e , which, as we show below, gives rise to Fano interference that strongly affects the overall shape of scattering spectra as the system transitions to strong coupling regime.

IV. EXCITON-INDUCED TRANSPARENCY VS. FANO INTERFERENCE

The scattering cross-section $\sigma_s^{sc}(\omega)$ of a hybrid plasmonic system is obtained by normalizing the radiated power $W_s =$

$(\omega^4/3c^3)|\mathbf{p}_s(\omega)|^2$ with the incident flux $S = (c/8\pi)E^2$ [8]. In the following, we disregard the relatively small direct QE coupling with the EM field but include the indirect coupling via plasmon-induced dipole moment, so that the induced system dipole includes the interference term: $\mathbf{p}_s \approx \mathbf{p}_{dp} + \mathbf{p}_{int}$. The resulting expression for $\sigma_s^{sc}(\omega)$ is quite cumbersome as it depends sensitively on mutual polarizations of the incident light \mathbf{E} , the plasmon dipole moment $\boldsymbol{\mu}_m$ and the QE dipole moment $\boldsymbol{\mu}_e$. Here, to simplify the analysis, we consider the case when all dipole moments are parallel to the incident field, i.e. $\boldsymbol{\mu}_e \parallel \boldsymbol{\mu}_m \parallel \mathbf{E}$, so that the coupling between the system components and to the EM field is strongest. In this case, the two terms in the numerator in Eq. (24) are equal, and using Eqs. (19) and (22), we obtain

$$\sigma_s^{sc}(\omega) = \frac{8\pi\omega^4}{3\hbar^2c^4} \left| \frac{\mu_m^2 (\omega_e + \omega_F - \omega - \frac{i}{2}\gamma_e)}{(\omega_m - \omega - \frac{i}{2}\gamma_m)(\omega_e - \omega - \frac{i}{2}\gamma_e) - g^2} \right|^2, \quad (29)$$

where $\omega_F = -2g\mu_e/\mu_m$ is QE frequency shift due to Fano interference between the plasmon and plasmon-induced QE dipole moments as the system interacts with the EM field. In fact, this shift is the only difference between the current model and dressed plasmon model (with $\mathbf{p}_s \approx \tilde{\mathbf{p}}_m$), which does not include the interference effects [48]. To highlight the role of Fano interference, we relate the scattering cross-section (29) to dressed plasmon scattering cross-section $\sigma_{dp}^{sc}(\omega)$, which is obtained from (29) by setting $\omega_F = 0$, as

$$\sigma_s^{sc}(\omega) = \sigma_{dp}^{sc}(\omega)F(\omega), \quad (30)$$

where $F(\omega)$ is the Fano function,

$$F(\omega) = \frac{(\delta - q)^2 + 1}{\delta^2 + 1}. \quad (31)$$

Here, $\delta = 2(\omega - \omega_e)/\gamma_e$ is frequency detuning in units of linewidth and q is the Fano parameter:

$$q = \frac{2\omega_F}{\gamma_e} = -\frac{4g\mu_e}{\gamma_e\mu_m}. \quad (32)$$

The Fano function has asymmetric shape that depends on the sign of parameter q . Using Eq. (14), the magnitude of q can be expressed via the Purcell factor as

$$|q| = \frac{2\gamma_e^r}{\gamma_e} \sqrt{\frac{F_p}{\eta_m}}, \quad (33)$$

where $\eta_m = \gamma_m^r/\gamma_m$ is the plasmon radiation efficiency. Although the ratio γ_e^r/γ_e is typically very small ($\sim 10^{-5}$) due to the broadening of spectral linewidth γ_e by phonons or vibrons, for small nanostructures we have $F_p \gg 1$ and $\eta_m \ll 1$, implying that, in a plasmonic hot spot, the actual value of q can be appreciable.

To elucidate the interplay between Fano interference and ExIT, we recall that, in the scattering spectra, the ExIT minimum emerges in the weak coupling regime as a narrow dip on the top of a wide plasmon band. The plasmon scattering

cross-section is obtained by setting $g = 0$ in Eq. (29) and, for $\boldsymbol{\mu}_m \parallel \mathbf{E}$, has the form

$$\sigma_m^{sc}(\omega) = \frac{8\pi\omega^4}{3\hbar^2c^4} \frac{\mu_m^4}{(\omega_m - \omega)^2 + \gamma_m^2/4}. \quad (34)$$

To trace the emergence of ExIT minimum, we recast the dressed plasmon scattering cross-section as $\sigma_m^{sc}(\omega)R(\omega)$, where the function

$$R(\omega) = \left| \frac{(\omega_m - \omega - \frac{i}{2}\gamma_m)(\omega_e - \omega - \frac{i}{2}\gamma_e)}{(\omega_m - \omega - \frac{i}{2}\gamma_m)(\omega_e - \omega - \frac{i}{2}\gamma_e) - g^2} \right|^2 \quad (35)$$

modulates the plasmon band, and so the system scattering cross-section is factorized as

$$\sigma_s^{sc}(\omega) = \sigma_m^{sc}(\omega)R(\omega)F(\omega). \quad (36)$$

In the frequency interval $|\omega_m - \omega|/\gamma_m \ll 1$, using the relation (14), the function $R(\omega)$ simplifies to

$$R(\omega) = \frac{\delta^2 + 1}{\delta^2 + (1+p)^2}, \quad (37)$$

where the parameter

$$p = \frac{\gamma_{e \rightarrow m}}{\gamma_e} = \frac{4g^2}{\gamma_m\gamma_e} \quad (38)$$

characterizes the ExIT minimum depth. The ExIT function (37) describes the emergence of spectral minimum due to excessively large plasmon-QE ET in the frequency interval $\sim \gamma_e$. Specifically, in the weak coupling regime, the dressed plasmon decay rate has the form $\gamma_{dp}(\omega) = \gamma_m + \gamma_{m \rightarrow e}(\omega)$. Using Eq. (23) and the relation (14), we obtain

$$\gamma_{dp}(\omega) = \gamma_m \left(1 + \frac{p}{\delta^2 + 1} \right), \quad (39)$$

implying linewidth increase by factor $(1+p)$ in the frequency interval $|\omega - \omega_e| \sim \gamma_e$ which, in turn, leads to the ExIT minimum in the dressed plasmon spectrum.

Thus, in the weak coupling regime, the ExIT and Fano interference effects are distinct and described by different factors in the scattering cross-section (36). While the ExIT factor $R(\omega)$ leads to a narrow minimum at the QE frequency position, the Fano factor $F(\omega)$ is an asymmetric function of ω that affects the overall shape of the scattering spectra. Remarkably, as we show in numerical calculations below, the Fano interference effect is most visible for intermediate and strong QE-plasmon coupling as it shifts the spectral weight between polaritonic bands resulting in the *inversion* of spectral asymmetry.

V. NUMERICAL RESULTS AND DISCUSSION

In this section, we present the results of numerical calculations for a QE situated at a distance d from the tip of an

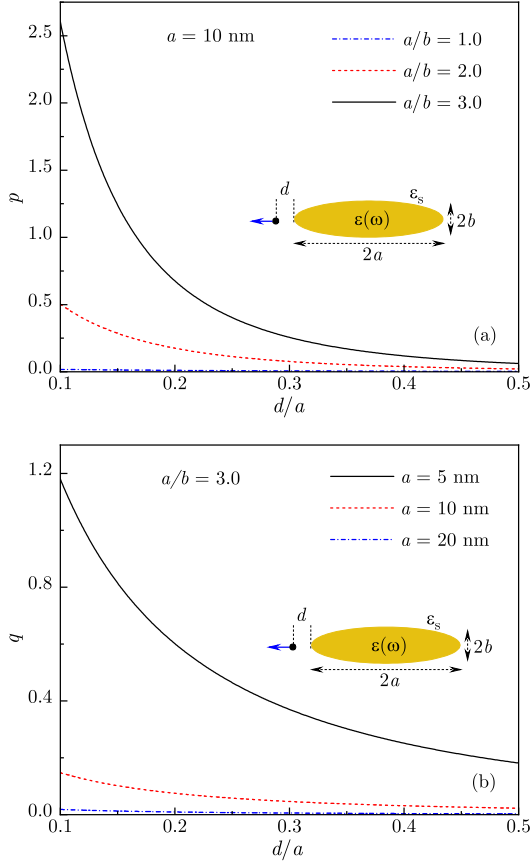


FIG. 1. (a) The ExIT parameter p is plotted against the QE distance d to the tip of Au nanorod of length $2a = 20$ nm placed for different values of aspect ratio $a/b = 1.0, 2.0$ and 3.0 . (b) The Fano parameter q is plotted against the distance d at nanorod aspect ratio $a/b = 3.0$ for different values of nanorod length $2a = 40$ nm, 20 nm and 10 nm. Inset: Schematics of a QE situated at a distance d from the tip of Au nanorod in water for QE dipole moment oriented along the nanorod axis.

Au nanorod in water with excitation frequency in resonance with the surface plasmon frequency, $\omega_e = \omega_m$. The nanorod was modeled by a prolate spheroid with semi-major and semi-minor axes a and b , respectively, the QE's dipole orientation was chosen along the nanorod symmetry axis, the Au experimental dielectric function was used in all calculations [56], and the dielectric constant of water was taken as $\epsilon_s = 1.77$. We used the standard spherical harmonics for calculations of the local fields near prolate spheroid to obtain the plasmon parameters μ_m, γ_m, η_m , the QE-plasmon coupling g and the Purcell factor F_p , which determine the ExIT parameter p and Fano parameter q . The QE spectral linewidth γ_e was chosen much smaller than the plasmon decay rate, $\gamma_e/\gamma_m = 0.1$, and its radiative decay time was chosen $\tau_e^r = 10$ ns, which are typical values for excitons in quantum dots. Note that the QE radiative decay rate γ_e^r is much smaller than its spectral linewidth: for our system we have $\gamma_e^r/\gamma_e \sim 10^{-5}$.

In Fig. 1, we plot the calculated ExIT parameter p , given by Eq. (38), and the Fano parameter q , given by Eq. (32), against

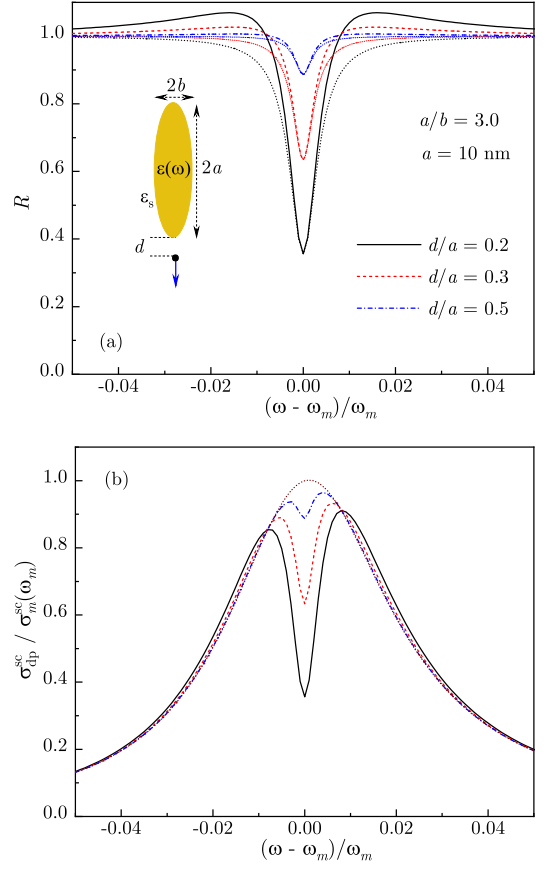


FIG. 2. (a) The ExIT function $R(\omega)$, given by Eq. (35), and its asymptotic expression (dotted lines), given by Eq. (37), are shown for a QE near the tip of Au nanorod with aspect ratio $a/b = 3.0$ and length $2a = 20$ nm at distances $d/a = 0.5, 0.3$, and 0.2 . (b) Normalized scattering cross-section in the dressed plasmon approximation is shown for the same system parameters. Dotted line is the plasmon band. All curves are calculated for $\omega_e = \omega_m$. Inset: Schematics of a QE situated at a distance d from the tip of Au nanorod in water for QE dipole moment oriented along the nanorod axis.

the distance to nanorod tip d normalized by a . Fig. 1(a) shows the ExIT parameter $p = F_p \gamma_e^r / \gamma_e$ for three different values of nanorod aspect ratio: $a/b = 1.0$ (sphere), 2.0 and 3.0 . Note that the Purcell factor near the tip of elongated particle ($a/b = 3.0$) is much greater than that for a nanosphere ($a/b = 1.0$), so that $p > 1$ in the former case while being negligibly small in the latter case. In Fig. 1(b), we show distance dependence of the Fano parameter q for fixed nanorod aspect ratio $a/b = 3.0$ and different lengths $2a = 40$ nm, 20 nm and 10 nm. The Fano parameter is largest for the smallest nanorod with $2a = 10$ nm and is significantly reduced for larger nanorods with $2a = 20$ nm and 40 nm. Both p and q sharply decrease as the QE moves away from the hot spot near nanorod tip.

In Fig. 2, in order to illustrate the emergence of ExIT, we show the evolution of function $R(\omega)$, given by Eq. (35), and of dressed plasmon's scattering cross-section $\sigma_{dp}^{sc}(\omega) = \sigma_m^{sc}(\omega)R(\omega)$ (i.e., without Fano interference effect) with decreasing QE-nanorod distance for $2a = 20$ nm and $a/b = 3.0$.

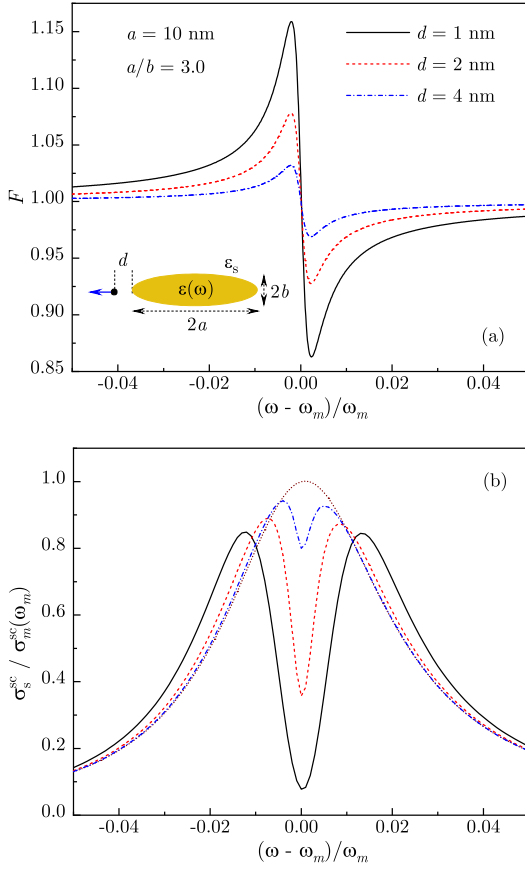


FIG. 3. (a) The Fano function $F(\omega)$, given by Eq. (31), is shown for a QE near the tip of Au nanorod with aspect ratio $a/b = 3.0$ and length $2a = 20$ nm at distances $d/a = 0.5, 0.3$, and 0.2 . (b) Normalized scattering cross-section, given by Eq. (36), is shown for the same system parameters. Dotted line is the plasmon band. All curves are calculated for $\omega_e = \omega_m$. Inset: Schematics of a QE situated at a distance d from the tip of Au nanorod in water for QE dipole moment oriented along the nanorod axis.

With decreasing d , the function $R(\omega)$ develops a minimum, as shown in Fig. 2(a), which modulates the plasmon scattering spectrum, as shown in Fig. 2(b). As discussed in the previous section, the double-peak structure of $\sigma_{dp}^{sc}(\omega)$ is caused by ET imbalance between the QE and plasmon in a narrow frequency interval. In order to highlight the role of ExIT parameter p , we plot in Fig. 2(a) the asymptotic expression for $R(\omega)$, given by Eq. (37), for each value of QE-nanorod distance d (dotted lines). Clearly, in the weak coupling regime (small p), the ExIT function Eq. (37) accurately describes the spectral minimum (blue curves), while for larger p (i.e., closer to the tip) the spectrum develops "wings" outside the minimum region as the system undergoes strong coupling transition. The onset of strong coupling transition can be seen in Fig. 2(b) as well, as for $d/a = 0.5$ and 0.3 , the scattering spectrum develops a narrow ExIT minimum at QE frequency on top of unchanged plasmon band, while for $d/a = 0.2$, the overall spectral width slightly increases signaling the emergence of Rabi splitting. We note that the ExIT function Eq. (37) accurately reproduces

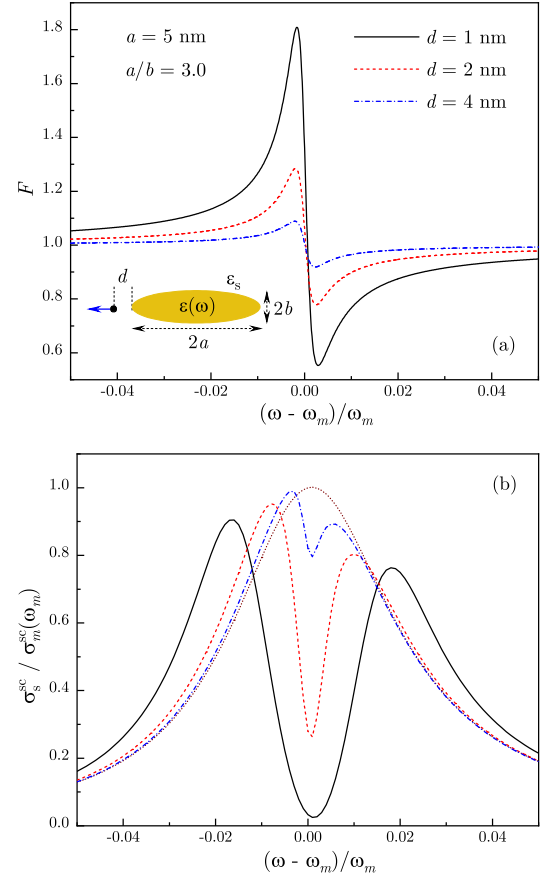


FIG. 4. (a) The Fano function $F(\omega)$, given by Eq. (31), is shown for a QE near the tip of Au nanorod with aspect ratio $a/b = 3.0$ and length $2a = 10$ nm at distances $d/a = 0.5, 0.3$, and 0.2 . (b) Normalized scattering cross-section, given by Eq. (36), is shown for the same system parameters. Dotted line is the plasmon band. All curves are calculated for $\omega_e = \omega_m$. Inset: Schematics of a QE situated at a distance d from the tip of Au nanorod in water for QE dipole moment oriented along the nanorod axis.

the central part of ExIT minimum for any distance d .

While the dressed plasmon model describes the position and depth of ExIT minimum relatively well, it predicts a sustained asymmetry as the spectral weight as the higher frequency region of scattering spectrum carries a larger spectral weight [see Fig. 2(b)]. In the absence of QE coupling to the EM field, emission takes place from the plasmonic antenna, whose power spectrum is $\propto \omega^4$ due to larger radiation rate at higher frequencies. Therefore, in the presence of double peak structure due to either ExIT minimum or Rabi splitting centered at resonance frequency $\omega = \omega_m = \omega_e$, the higher frequency peak is enhanced. Note that similar scattering spectra are predicted by the classical model of coupled oscillators which disregards optical interference effects [38, 47]. Below we demonstrate that extending the dressed plasmon model to include Fano interference between the plasmon antenna and plasmon-induced QE dipole, as described in Eq. (36), can strongly affect the overall shape of scattering spectra.

In Fig. 3, we plot the Fano function and scattering spec-

tra for a QE situated at several distances from the tip of Au nanorod with aspect ratio $a/b = 3.0$ and overall length $2a = 20$ nm. As indicated above, we consider the case of QE's dipole moment oriented along the normal to tip surface (see inset in Fig. 3), so that the Fano parameter q is positive. For nanorod of this length, q is relative small [see Fig. 1(b)] and so the Fano function's variation ranges from about 2% for $d = 4$ nm to 15% for $d = 1$ nm, as the QE-plasmon coupling g increases close to the tip [see Fig. 3(a)]. Importantly, for $q > 0$, the spectral shape of the Fano function, which enters in the scattering cross-section (36), leads to the suppression of higher frequency region and enhancement of lower frequency region. As a result, the aforementioned asymmetry of dressed plasmon scattering spectra in Fig. 2(b) is largely compensated, and so the full scattering spectra are now close to symmetric [see Fig. 3(b)].

In Fig. 4, we show the Fano function and scattering spectra for a small nanorod of length 10 nm. With decreasing nanostructure size and, hence, the reduction of plasmon mode volume, the QE-plasmon coupling increases and so does the Fano parameter q , which now reaches values $q \sim 1$ [see Fig. 1(b)]. In this case, the Fano function variation is larger as well, reaching about 80% close to the nanorod tip [see Fig. 4(a)]. As a result, the scattering spectra, shown in Fig. 4(b), exhibit *inversion* of spectral asymmetry relative to the dressed plasmon spectra [see Fig. 2(b)], with the lower frequency peak now substantially higher than the higher frequency peak. Note that for smallest d , the system has clearly transitioned to strong coupling regime since the double-peak structure is well beyond the plasmon resonance envelope. We stress that although the mechanisms of ExIT and Fano interference are distinct,

as discussed in the previous section, the two effects are intimately related as Fano interference manifests itself via redistribution of spectral weight across the ExIT minimum in the scattering spectra.

VI. CONCLUSIONS

In this paper, we developed a model for exciton-induced transparency (ExIT) and Fano interference in hybrid plasmonic systems comprised of a single emitter resonantly coupled to a surface plasmon in a metal-dielectric structure. We have shown that the shape of scattering spectra is determined by two distinct mechanisms. First is near-field coupling between the emitter and plasmon that defines the energy spectrum of hybrid system. This mechanism relies upon energy exchange between the system components and gives rise to the ExIT minimum in scattering spectra and, in the strong coupling regime, to the Rabi splitting of polaritonic bands. The second mechanism is the Fano interference between the plasmon and the plasmon-induced emitter's dipoles as the system interacts with the radiation field. Although the Fano interference does not significantly affect the position or magnitude of ExIT minimum, it determines the overall shape of scattering spectra. Specifically, the Fano interference leads to the inversion of spectral asymmetry that was recently reported in the experiment [22, 39, 40].

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