

# Knowledge-aware Coupled Graph Neural Network for Social Recommendation

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## Abstract

Social recommendation task aims to predict users' preferences over items with the incorporation of social connections among users, so as to alleviate the sparse issue of collaborative filtering. While many recent efforts show the effectiveness of neural network-based social recommender systems, several important challenges have not been well addressed yet: (i) The majority of models only consider users' connections, while ignoring the inter-dependent knowledge across items; (ii) Most of existing solutions are designed for singular type of user-item interactions, making them infeasible to capture the behavior heterogeneity; (iii) The dynamic nature of user-item interactions has been less explored in many social-aware recommendation techniques. To tackle the above challenges, this work proposes a **Knowledge-aware Coupled Graph Neural Network (KCGN)** that jointly injects the inter-dependent knowledge across items and users into the recommendation framework. KCGN enables the high-order user- and item-wise relation encoding by exploiting mutual information for global graph structure awareness. Additionally, we further augment KCGN with the capability of capturing dynamic multi-behavior user-item interactive patterns. Extensive experimental analysis on three real-world datasets demonstrate the superiority of our method against many strong baselines in a variety of settings. Source codes are available at: <https://github.com/xhcdream/KCGN>.

## Introduction

In recent years, social recommendation which aims to exploit users' social information for modeling users' preferences in recommendations, have attracted significant attention (Liu et al. 2019). As has been stated in many social-aware recommendation literature (Wu et al. 2019a; Chen et al. 2019b), social influences between users have high impacts on users' interactive behavior over items in various recommender scenarios, such as e-commerce (Lin, Gao, and Li 2019) and online review platforms (Chen et al. 2020a). Hence, researchers propose to incorporate social ties into the collaborative filtering architecture as side information to characterize connectivity information across users.

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The most common paradigm for state-of-the-art social recommender systems is to learn an embedding function, which unifies user-user and user-item relations into latent representations. To tackle this problem, many studies have developed various neural network techniques to integrate social information with the user-item interaction encoding as constraints. For example, attention-based mechanism has been utilized to aggregate correlations among different users (Chen et al. 2019a; Chen et al. 2019b). Furthermore, inspired by the recent advance of graph neural architectures, several attempts are built upon the message passing frameworks over the user-user social graph. For example, social influence is simulated with layer-wise diffusion scheme for information fusion (Wu et al. 2019a). GraphRec (Fan et al. 2019) employs the graph attention network to model the relational structures between users. To enable the modeling context-aware social effects, DANSER (Wu et al. 2019b) stacks two-stage of graph attention layer for distinguishing the multi-faceted social homophily and influence.

While these solutions have provided encouraging results, several important challenges have not been well addressed yet. In particular, *First*, in real-life scenarios, there typically exist relations between items which characterize item-wise fruitful semantics relatedness, and are helpful to understand user-item interactive patterns (Wang et al. 2019a). For instance, in online retailing systems, products of the same categories (*e.g.*, food & grocery, clothing & shoes) or complement with each other, could be correlated to enrich the knowledge representation of items (Xin et al. 2019). For online review platforms, the exploiting of dependencies among the venues with the same functionality, is able to provide external knowledge in assisting user preference learning (Yu et al. 2019). However, the majority of existing social recommender systems fail to capture item-wise relational structures, which can hardly distill the knowledge-aware collaborative signals from the co-interactive behaviors of users.

*Second*, To simplify the model design, most of current social recommendation methods have thus far focused on modeling singular type of interactive relations between users and items. Yet, many practical recommendation scenarios may involve the diversity of users' interaction behaviors over items (Cen et al. 2019; Xia et al. 2020). Take the

e-commerce site as an example, the effective encoding of multi-typed user-item interactive patterns (e.g., page view, add-to-favorite and purchase) and their underlying interdependencies (e.g., add-to-favorite activities may serve as useful indicators for making purchase decisions), is crucial to more accurately inference of user’s complex interest in social recommendation tasks.

*Third*, The time dimension of the social recommendation deserves more investigation, so as to capture behavior dynamics under the behavior heterogeneity. Most of recent approaches ignore the dynamic nature of user-item interactions and assume that the factor influencing the interactive behavior is only the identity of items (Song et al. 2019). While there exist a handful of recent work that consider the sequential information in social recommendation (Song et al. 2019; Sun, Wu, and Wang 2018), their are limited in their intrinsic design for singular type of user-item relations. This makes them insufficient to yield satisfactory embeddings with the preservation of multiplex behavioral interaction signals in a dynamic manner for more complex scenarios.

While intuitively useful to integrate the above dimensions into social recommendation frameworks, two unique technical challenges arise in achieving this goal. Specifically, graph-structured neural network can be applied to naturally model the topological information of social node instances, such as the graph-based convolutional network (Wu et al. 2019a) or attention mechanism (Wu et al. 2019b; Fan et al. 2019). However, their non-linear aggregation functions can only learn the local proximity between users and are incapable of capturing the broader context of the graph structure (e.g., users with the isomorphic social structures) (You, Ying, and Leskovec 2019). Hence, how to jointly capture knowledge-aware user-user and item-item local relations, as well as retain the long-range social influence and item dependencies under global context, remains a significant challenge. Additionally, it is also very challenging to handle the dynamic multi-behavior user-item interactions, so as to capture the dynamic relation-aware structural dependencies across users and items with arbitrary duration.

**The Present Work.** In light of the aforementioned motivations and challenges, we study the social recommendation problem by proposing the **Knowledge-aware Coupled Graph Neural Network (KCGN)**. To jointly deal with the user-user and item-item local and global relational structure awareness, we incorporate the mutual information estimation schema into the coupled graph neural architecture. This design enables the collaboration between neural mutual information estimator and graph-structured representation learning paradigm, which preserves the node-level unique characteristics and graph-level substructure knowledge across users and items. In addition, to capture the dynamic multi-behavioral interactive patterns, we integrate a relation-aware message passing framework with the relative temporal encoding strategy, which endows KCGN with the capability of automatically learning the temporal user-specific temporal behavior dependencies and evolution of multi-behavior user-item interaction graph.

Our contributions can be highlighted as follows:

- We propose to capture both user-user and item-item with the developed coupled graph neural network. Through the joint modeling of user- and item-wise dependent structures, our KCGN can enhance the social-aware user embeddings with the preservation of knowledge-aware cross-item relations in a more thorough way.
- We propose a relation-aware graph neural module to encode the multi-behavior user-item interactive patterns, and further incorporate the temporal information into the message passing kernel to augment the learning of cross-behavior collaborative relations with behavior dynamics.
- We conduct extensive experiments on three real-world datasets to show the superiority of our KCGN when competing with 10 baselines from various research lines. Further studies on scalability evaluation validate the model efficiency of KCGN over several state-of-the-art social recommender systems. We also show that our model maintains strong performance in the cold-start scenarios when user-item interactions are sparse.

## Problem Definition

We first introduce key definitions of social recommendation with item relational knowledge and different types of user-item interactions. We consider a typical recommendation scenario, in which we have  $I$  users  $U = \{u_1, \dots, u_i, \dots, u_I\}$  and  $J$  items  $V = \{v_1, \dots, v_j, \dots, v_J\}$ . To capture the multi-behavioral user-item interaction signals, we define a multi-behavior interaction tensor as below:

**Definition 1 Multi-Behavior Interaction Tensor  $X$ .** We define a three-way tensor  $X \in \mathbb{R}^{I \times J \times K}$  to represent the different types of interactions between users and items, where  $K$  (indexed by  $k$ ) denotes the number of interaction types (page view, add-to-favorite, purchase). In  $X$ , the element  $x_{i,j}^k = 1$  if user interacts with item  $v_j$  under the behavior type of  $k$  and  $x_{i,j}^k = 0$  otherwise. To deal with the interaction dynamics, we also define a temporal tensor  $T \in \mathbb{R}^{I \times J \times K}$  with the same size of  $X$  to record the timestamp information ( $t_{i,j}^k$ ) of each corresponding interaction  $x_{i,j}^k$ .

**Definition 2 User Social Graph  $G_u$ .**  $G_u = \{U, E_u\}$  represents the social relationships (edges  $E_u$ ) among users (nodes  $U$ ), where there exists an edge  $e_{i,i'}$  between user  $u_i$  and  $u_{i'}$  given they are socially connected.

**Definition 3 Item Inter-Dependency Graph  $G_v$ .** We further define  $G_v = \{V, E_v\}$  to represent the inter-dependent knowledge of items. In particular, we characterize the item-wise relations with a triple  $\{v_j, e_{j,j'}, v_{j'} | v_j, v_{j'} \in V\}$ , where edge  $e_{j,j'}$  describes the relationship between item  $v_j$  and  $v_{j'}$ , such as  $v_j$  and  $v_{j'}$  belong to the same product categories and have similar functionality, or are interacted by the same user under the same behavior type  $k$ .

**Task Formulation.** We formulate the studied recommendation task in this paper as: **Input:** multi-behavior interaction tensor  $X \in \mathbb{R}^{I \times J \times K}$ , user social graph  $G_u$  and item inter-dependent graph  $G_v$ . **Output:** a predictive function that effectively forecasts the future user-item interaction relations.

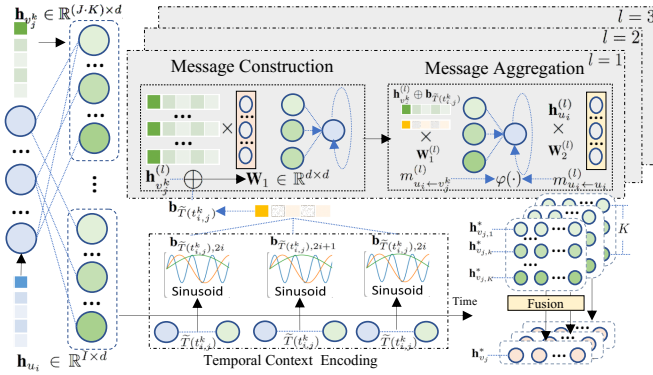


Figure 1: The architecture of multi-behavior interactive pattern modeling.  $\oplus$  denotes the element-wise addition.

## Methodology

### Multi-Behavior Interactive Pattern Modeling

To encode the multi-behavioral collaborative relations, we propose a relation-aware graph neural architecture, which is built upon the message passing paradigm (as shown in Figure 1), to empower KCGN capture the dedicated patterns of different types of user-item interactions. Specifically, given the multi-behavior interaction tensor  $\mathbf{X}$ , we first construct a multi-behavioral relation graph  $G_m$  by representing the interaction heterogeneity with type-specific item sub-vertices  $v_j \rightarrow (v_j^1, \dots, v_j^K)$ , where  $K$  denotes the number of interaction types. Each edge between  $u_i$  and  $v_j^k$  represents the corresponding interaction under  $k$ -th behavior type. After that, there are  $(I + J \cdot K)$  vertices in our multi-behavior graph  $G_m = (V_m, E_m)$ , where  $V_m = U \cup V'$  and  $v_j^k \in V'$ .

**Message Construction Phase.** We first generate the message between user vertex  $u_i$  and his/her interacted type-specific item vertex  $v_j^k$  as follows:

$$m_{u_i \leftarrow v_j^k} = \gamma(\mathbf{h}_{v_j^k}, \rho_{i,j}^k); \quad m_{v_j^k \leftarrow u_i} = \gamma(\mathbf{h}_{u_i}, \rho_{i,j}^k) \quad (1)$$

where  $\gamma(\cdot)$  denotes the information encoding function over the input feature embeddings  $\mathbf{h}_{v_j^k} \in \mathbb{R}^{(J \cdot K) \times d}$ ,  $\mathbf{h}_{u_i} \in \mathbb{R}^{I \times d}$ .  $\rho_{i,j}^k$  is the decay factor to normalize the propagated influence with node degrees (Chen et al. 2020b), *i.e.*,  $\rho = \frac{1}{\sqrt{|N_i| |N_j^k|}}$ , where  $N_i$  denotes the number of neighboring nodes of user  $u_i$  and  $N_j^k$  represents the number of connected user nodes of item  $v_j$  under the relation type of  $k$ . Hence, the constructed message can be unfolded as:

$$m_{u_i \leftarrow v_j^k} = \frac{1}{\sqrt{|N_i| |N_j^k|}} (\mathbf{h}_{v_j^k} \cdot \mathbf{W}_1) \quad (2)$$

where  $\mathbf{W}_1 \in \mathbb{R}^{d \times d}$  is the weight matrix. Similar operation is applied for the message from  $u_i$  to type-specific item  $v_j^k$ .

**Temporal Context Encoding Scheme.** Inspired by the recommendation techniques with modeling of temporal information (Sun et al. 2019; Huang et al. 2019), in our framework, we allow the user-item interactions happening at different timestamps interweave with each other, by introducing a temporal context encoding scheme to model the

dynamic dependencies across different types of users' behaviors. Motivated by the positional encoding algorithm in Transformer architecture (Vaswani et al. 2017; Sun et al. 2019; Wu et al. 2020), we map the timestamp  $t_{i,j^k}$  of individual interaction  $x_{i,j^k}^k$  into separated time slot as:  $\tilde{T}(t_{i,j^k}^k)$ . Formally, we employ the sinusoid functions to generate the relative time embedding for each edge  $e_{i,j^k}^k \in E_m$  in  $G_m$  as:

$$\begin{aligned} \mathbf{b}_{\tilde{T}(t_{i,j^k}^k), 2i} &= \sin(\tilde{T}(t_{i,j^k}^k)/10000^{\frac{2i}{d}}) \\ \mathbf{b}_{\tilde{T}(t_{i,j^k}^k), 2i+1} &= \cos(\tilde{T}(t_{i,j^k}^k)/10000^{\frac{2i+1}{d}}) \end{aligned} \quad (3)$$

where  $(2i)$  and  $(2i+1)$  denotes the element index with the even and odd position in embedding  $\mathbf{b}_{\tilde{T}(t_{i,j^k}^k)}$ , respectively.

**High-Order Message Aggregation Phase.** We incorporate the propagated message between user  $u_i$  and item  $v_j^k$ , as well as temporal context  $\mathbf{b}_{\tilde{T}(t_{i,j^k}^k)}$  on their interaction edge  $e_{i,j^k}^k$ , into our information propagation paradigm as:

$$\begin{aligned} \mathbf{h}_{u_i}^{(l+1)} &= \varphi \left( \sum_{(j,k) \in N_{u_i}} m_{u_i \leftarrow v_j^k}^{(l)} + m_{u_i \leftarrow u_i}^{(l)} \right) = \varphi \left( \frac{1}{|N_{u_i}^{(l)}|} \mathbf{h}_{u_i}^{(l)} \mathbf{W}_2^{(l)} \right. \\ &\quad \left. + \sum_{(j,k) \in N_{u_i}} \frac{1}{|N_{v_j^k}^{(l)}|} ((\mathbf{h}_{v_j^k}^{(l)} \oplus \mathbf{b}_{\tilde{T}(t_{i,j^k}^k)}) \mathbf{W}_1^{(l)}) \right) \end{aligned} \quad (4)$$

where  $\varphi(\cdot)$  denotes the LeakyReLU function to perform the transformation.  $m_{u_i \leftarrow u_i}^{(l)}$  is the self-propagated message with the weight matrix  $\mathbf{W}_2^{(l)} \in \mathbb{R}^{d \times d}$ .  $\oplus$  denotes the element-wise addition.  $l$  is the index of  $L$  graph layers. We finally generate the user/item embeddings (*i.e.*,  $\mathbf{h}_{u_i}^*$ ,  $\mathbf{h}_{v_j^k}^*$ ) with the following concatenation operation  $\parallel$  as:

$$\begin{aligned} \mathbf{h}_{u_i}^* &= (\mathbf{h}_{u_i}^{(0)} \parallel \mathbf{h}_{u_i}^{(1)} \parallel \dots \parallel \mathbf{h}_{u_i}^{(L)}) \\ \mathbf{h}_{v_j^k}^* &= (\mathbf{h}_{v_j^k}^{(0)} \parallel \mathbf{h}_{v_j^k}^{(1)} \parallel \dots \parallel \mathbf{h}_{v_j^k}^{(L)}) \end{aligned} \quad (5)$$

We generate the summarized representation  $\mathbf{h}_{v_j^k}^*$  over all item sub-vertex embeddings  $\mathbf{h}_{v_j^k}^*$  ( $k \in [1, \dots, K]$ ) with a gating mechanism (Ma, Kang, and Liu 2019), to differentiate the importance of type-specific behavioral patterns.

### Knowledge-aware Coupled Graph Neural Module

To jointly inject the user- and item-wise inter-dependent knowledge into our user preference modeling, we develop a knowledge-aware coupled graph neural network which enables the collaboration between the mutual information learning and graph representation paradigm. While many efforts have been devoted to modeling graph structural information, they are limited in their ability in capturing both local and global graph substructure awareness (Velickovic et al. 2019), such as the user- and item-specific social/knowledge signals and high-order relationships across users/items. KCGN is equipped with a dual-stage graph learning paradigm (As shown in Figure 2).

**Local Relational Structure Modeling.** We first learn the user- and item-specific specific embeddings ( $\mathbf{z}_{u_i}$ ,  $\mathbf{z}_{v_j}$ ) which preserves the local connection information over user social

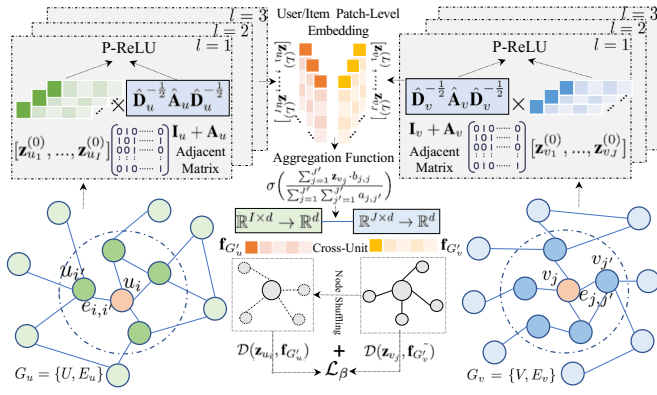


Figure 2: The architecture of joint encoding of user-user and item-item inter-dependent relational structures.

graph  $G_u$  and item inter-dependent graph  $G_v$  with the following graph-based update functions ( $\mathbf{z}_{u_i}^0 = \mathbf{h}_{u_i}^*$ ,  $\mathbf{z}_{v_j}^0 = \mathbf{h}_{v_j}^*$ ):

$$\begin{aligned} [\mathbf{z}_{u_1}^{(l+1)}, \dots, \mathbf{z}_{u_I}^{(l+1)}] &= \varphi([\mathbf{z}_{u_1}^{(l)}, \dots, \mathbf{z}_{u_I}^{(l)}] \cdot \eta(G_s)) \\ [\mathbf{z}_{v_1}^{(l+1)}, \dots, \mathbf{z}_{v_J}^{(l+1)}] &= \varphi([\mathbf{z}_{v_1}^{(l)}, \dots, \mathbf{z}_{v_J}^{(l)}] \cdot \eta(G_t)) \end{aligned} \quad (6)$$

where  $\eta(\cdot)$  denotes the adjacent relations of  $G_u$  and  $G_v$  with the symmetric normalization strategy in the information aggregation across the neighboring users/items, *e.g.*,  $\eta(G_v) = \hat{\mathbf{D}}_v^{-\frac{1}{2}} \hat{\mathbf{A}}_v \hat{\mathbf{D}}_v^{-\frac{1}{2}}$ . Hence,  $\hat{\mathbf{A}}_v$  is the addition of identity matrix  $\mathbf{I}_v$  and adjacent matrix  $\mathbf{A}_v$ , so as to incorporate the information self-propagation (Chen et al. 2020b).

**Joint Encoding of Local and Global Dependencies.** In this graph learning paradigm, we aim to inject both local and global-level relational structures over the both the user social graph and knowledge-aware item relation graph into our learned latent user/item representations. Different from the existing graph neural network approaches (Velickovic et al. 2019; Xu et al. 2020) which model the mutual relations between local feature embeddings and a single global representation, we enrich the global semantics with the consideration of connected graph substructures (*e.g.*, the entire social relations of all users may consist of different connected subgraphs  $G'_u$ ). In particular, we first generate a fused graph-level representation  $\mathbf{f}_{G'_u}, \mathbf{f}_{G'_v} \in \mathbb{R}^d$  by applying the mean pooling over node-specific embeddings.

We design our neural mutual information estimator based on a discriminator  $\mathcal{D}(x, y)$  for node-graph pairwise relationships, to provide probability scores for sampled pairs. To be specific, we generate positive samples as  $(\mathbf{z}_{u_i}, \mathbf{f}_{G'_u})$ ,  $(\mathbf{z}_{v_j}, \mathbf{f}_{G'_v})$ , and negative samples as  $(\tilde{\mathbf{z}}_{u_i}, \mathbf{f}_{G'_u})$ ,  $(\tilde{\mathbf{z}}_{v_j}, \mathbf{f}_{G'_v})$ . Here,  $\tilde{\mathbf{z}}_{u_i}$  and  $\tilde{\mathbf{z}}_{v_j}$  are randomly picked with node shuffling to generate the misplaced node-graph pairwise relations.

Due to the rationality of cross-entropy in mutual information maximization (Wang et al. 2020), we define our noise-

contrastive knowledge-aware loss function  $\mathcal{L}_\beta$  as follows:

$$\begin{aligned} \mathcal{L}_\beta &= -\frac{\lambda_1}{N_{pos}^u + N_{neg}^u} \left( \sum_{i=1}^{N_{pos}^u} \tau(\mathbf{z}_{u_i}, \mathbf{f}_{G'_u}) \cdot \log \sigma(\mathbf{z}_{u_i} \cdot \mathbf{f}_{G'_u}) \right. \\ &\quad \left. + \sum_{i=1}^{N_{neg}^u} \tau(\tilde{\mathbf{z}}_{u_i}, \mathbf{f}_{G'_u}) \cdot \log [1 - \sigma(\tilde{\mathbf{z}}_{u_i} \cdot \mathbf{f}_{G'_u})] \right) \\ &\quad -\frac{\lambda_2}{N_{pos}^v + N_{neg}^v} \left( \sum_{i=1}^{N_{pos}^v} \tau(\mathbf{z}_{v_j}, \mathbf{f}_{G'_v}) \cdot \log \sigma(\mathbf{z}_{v_j} \cdot \mathbf{f}_{G'_v}) \right. \\ &\quad \left. + \sum_{i=1}^{N_{neg}^v} \tau(\tilde{\mathbf{z}}_{v_j}, \mathbf{f}_{G'_v}) \cdot \log [1 - \sigma(\tilde{\mathbf{z}}_{v_j} \cdot \mathbf{f}_{G'_v})] \right) \end{aligned} \quad (7)$$

where  $N_{pos}^u/N_{neg}^u$  and  $N_{pos}^v/N_{neg}^v$  denotes the number of positive and negative instances sampled over sub-graph  $G'_u$  and  $G'_v$ .  $\tau(\cdot)$  is an indicator function, *e.g.*,  $\tau(\mathbf{z}_{v_j}, \mathbf{f}_{G'_v}) = 1$  and  $\tau(\tilde{\mathbf{z}}_{v_j}, \mathbf{f}_{G'_v}) = 0$  corresponds to the positive and negative pair instances.  $\lambda_1$  and  $\lambda_2$  are balance parameters. We aim to minimize  $\mathcal{L}_\beta$  which is equivalent to maximize the mutual information, to jointly preserve the node-specific user/item characteristics and global graph-level dependencies.

## Model Optimization

We define our loss  $\mathcal{L}$  which includes (i) multi-behavior user-item interaction encoding; (ii) knowledge-aware user-user and item-item inter-dependent relation learning. Particularly,  $\mathcal{L}$  integrates the pairwise BPR loss, which has been widely used in recommendation task (Wang et al. 2019c), with the mutual information maximization paradigm as:

$$\mathcal{L} = \sum_{(i, j^+, j^-) \in \mathcal{O}} -\ln \sigma(\hat{x}_{i, j^+} - \hat{x}_{i, j^-}) + \lambda \|\Theta\|^2 + \mathcal{L}_\beta \quad (8)$$

the pairwise training data is denoted as  $\mathcal{O} = \{(u, j^+, j^-) | (u, j^+) \in \mathcal{R}^+, (u, j^-) \in \mathcal{R}^-\}$  ( $\mathcal{R}^+$ ,  $\mathcal{R}^-$  denotes the observed and unobserved interactions, respectively).  $\Theta$  are trainable parameters,  $\sigma(\cdot)$ —sigmoid.  $\lambda$  controls the strength of  $L_2$  regularization for overfitting alleviation.

**Model Time Complexity Analysis.** Our model spends  $O(|E| \times d)$  for the message passing in handling all of the u-i, i-u and i-i relations, where  $|E|$  denotes the number of edges. Also,  $O((I + J \cdot K) \times d^2)$  computation is spent by the transformations. Typically, the first term is dominant due to information compression. In conclusion, KCGN is comparable in time efficiency compared to the most efficient GNN recommendation methods. Also, our model only utilize moderate memory to store node embeddings ( $O((I + J \cdot K) \times d)$ ), which is also similar to the existing methods.

## Evaluation

Experiments are performed from the following aspects:

- **RQ1:** Does *KCGN* consistently outperform other baseline in terms of recommendation accuracy?
- **RQ2:** How is the performance of *KCGN*'s variants with the combination of different relation encoders?
- **RQ3:** How is forecasting performance of compared methods *w.r.t* different interaction density degrees?

- **RQ4:** How do the representations benefit from the collectively encoding of global knowledge-aware cross-interactive patterns in social recommendation?
- **RQ5:** How do different hyper-parameter settings impact the performance of our *KCGN* framework?
- **RQ6:** How is the model efficiency of the *KCGN*?

## Experimental Settings

**Dataset.** Table 1 lists the statistics of three datasets.

**Epinions**<sup>1</sup>. This data records the user’s feedback over different items from a social network-based review system Epinions (Fan et al. 2019). Each explicit rating score (ranging from 1 to 5) is regarded as an individual type of interaction: negative, below average, neutral, above average, positive.

**Yelp**<sup>2</sup>. This data is collected from the Yelp platform, in which user-item interactions are differentiated with the same split rubric in Epinions. Furthermore, user’s social connections (with common interests) are contained in this data.

**E-Commerce** It is collected from a commercial e-commerce platform with different types of behaviors, *i.e.*, *page view*, *add-to-cart*, *add-to-favorite* and *purchase*. User’s relations are constructed with their co-interact patterns.

Table 1: Statistics of Experimented Datasets.

| Dataset                     | Epinions  | Yelp      | E-commerce |
|-----------------------------|-----------|-----------|------------|
| # of Users                  | 18,081    | 43,043    | 334,042    |
| # of Items                  | 251,722   | 66,576    | 195,940    |
| # of User-Item Interactions | 715,821   | 283,512   | 1,930,466  |
| Interaction Density Degree  | 0.0157%   | 0.0098%   | 0.0029%    |
| # of Social Ties            | 590,641   | 549,451   | 13,572,512 |
| Social Tie Density Degree   | 0.1806%   | 0.0296%   | 0.0121%    |
| # Item Relations            | 6,069,106 | 1,847,060 | 1,382,280  |

**Evaluation Protocols.** We adopt two widely used evaluation metrics for social recommendation tasks (Chen et al. 2019a): *Hit Ratio* ( $HR@k$ ) and *Normalized Discounted Cumulative Gain* ( $NDCG@k$ ). We follow the evaluation settings in (Chen et al. 2019b; Wu et al. 2019a) and employ the leave-one-out method for generating training and test data instances. To be consistent with (Sun et al. 2019), we associate each positive instance with 99 negative samples.

**Baselines.** We consider the following compared methods: **Probabilistic Matrix Factorization Method.**

- **PMF** (Mnih and *et al* 2008): it is a probabilistic approach with the matrix factorization for user/item factorization.

**Conventional Social Recommendation Methods.**

- **TrustMF** (Yang et al. 2016): this method incorporates the truth relationships between users into the matrix factorization architecture for user interaction embedding.

**Attentive Social Recommendation Techniques.**

- **SAMN** (Chen et al. 2019a): this model is a dual-stage attention network which learns the influences between the target user and his/her neighboring nodes.
- **EATNN** (Chen et al. 2019b): This transfer learning model is also on the basis of attention mechanism to jointly fuse information from user’s interactions and social signals.

<sup>1</sup><https://www.cse.msu.edu/~tangjili/datasetcode/truststudy.htm>

<sup>2</sup><https://www.yelp.com/dataset/download>

**Graph Neural Networks Social Recommender Systems.**

- **DiffNet** (Wu et al. 2019a): it is a deep influence propagation framework to model the social diffusion process.
- **GraphRec** (Fan et al. 2019): it aggregates the social relations between users via a graph neural architecture.
- **NGCF+S** (Wang et al. 2019c): we incorporate the social ties into the state-of-the-art graph-structured neural collaborative filtering model for joint message propagation.
- **DANSER** (Wu et al. 2019b): it is composed of two graph attention layers for capturing the social influence and homophily, respectively from both users and items.
- **LR-GCCF** (Chen et al. 2020b): it is a new graph-based collaborative filtering model based on graph convolutional network by removing non-linearities.

**Social Recommendation with Sequential Pattern.**

- **DGRec** (Song et al. 2019): it jointly models the dynamic user’s preference and the underlying social relations.

**Knowledge Graph-enhanced Recommendation.**

- **KGAT** (Wang et al. 2019b): it is a graph attentive message passing framework which utilize the knowledge graph to enhance the recommendation with side information.

**Implementation Details.** In our experiments, the *KCGN* framework is implemented with Pytorch and Adam optimizer is adopted for hyperparameter estimation. The training process is performed with the learning rate of  $1e^{-3}$ , and the batch size selected from [1024, 2048, 4096, 8192]. The embedding size is tuned from the range of [8, 16, 32, 64]. In our evaluations, we employ the early stopping for training termination when the performance degrades for 5 continuous epochs on the validation data.

## Overall Model Performance Comparison (RQ1)

Table 2 reports the results of *KCGN* and 10 baselines in predicting the overall click-through rate. It can be seen that *KCGN* consistently obtains the best performance across different recommendation scenarios in terms of two metrics, which justifies the effectiveness of our method in integrating user-user and item-item relations, with the multi-modal user-item interactive patterns.

Compared with traditional approaches, neural network based models usually achieve better performance, due to the modeling of high-level non-linearities during the feature interaction phase. Among various compared approaches, the GNN-based models outperforms the attentive social recommender systems, which ascertains the rationality of applying graph neural networks for high-order relations across users/items in a recursive way. Different from those GNN-based techniques, our framework integrates the social and knowledge-aware relations from global context via a mutual information encoding paradigm, and also captures behavior dynamics, which results in consistent better performance.

We further investigate the performance of our *KCGN* in making recommendations on the target type of interactions (*e.g.*, user’s purchase on E-commerce or positive feedback on Epinions and Yelp). The results are shown in Table 3. We can observe that *KCGN* still achieves significant improvement, with the careful consideration of dependencies

Table 2: Performance comparison of all methods in CTR prediction in terms of  $HR@10$  and  $NDCG@10$ .

| Data       | Metrics | PMF    | TrustMF | DiffNet | SAMN   | DGRec  | EATNN  | NGCF+S | KGAT   | GraphRec | DANSER | LR-GCCF | KCGN          |
|------------|---------|--------|---------|---------|--------|--------|--------|--------|--------|----------|--------|---------|---------------|
| Epinions   | HR      | 0.6197 | 0.6353  | 0.6323  | 0.6390 | 0.6268 | 0.6422 | 0.7071 | 0.6756 | 0.6865   | 0.6693 | 0.6779  | <b>0.7429</b> |
|            | NDCG    | 0.4105 | 0.4179  | 0.4160  | 0.4259 | 0.4127 | 0.4483 | 0.4980 | 0.4708 | 0.4786   | 0.4627 | 0.4783  | <b>0.5131</b> |
| Yelp       | HR      | 0.6986 | 0.7562  | 0.7853  | 0.7514 | 0.7662 | 0.7715 | 0.7813 | 0.7721 | 0.7605   | 0.7740 | 0.7692  | <b>0.8026</b> |
|            | NDCG    | 0.4609 | 0.4959  | 0.5126  | 0.4863 | 0.4954 | 0.5066 | 0.5232 | 0.5113 | 0.4943   | 0.5082 | 0.5189  | <b>0.5308</b> |
| E-Commerce | HR      | 0.6540 | 0.6742  | 0.7223  | 0.6767 | 0.6723 | 0.6837 | 0.6944 | 0.6891 | 0.6680   | 0.6703 | 0.6901  | <b>0.7353</b> |
|            | NDCG    | 0.4312 | 0.4527  | 0.5193  | 0.4614 | 0.4417 | 0.4569 | 0.4763 | 0.4735 | 0.4393   | 0.4437 | 0.4851  | <b>0.5296</b> |

Table 3: Prediction results for like/purchase behaviors on three datasets in terms of  $HR@10$  and  $NDCG@10$ .

| Data     | Metrics | DiffNet | SAMN   | DGRec  | EATNN  | NGCF+S | KGAT   | GraphRec | DANSER | KCGN          |
|----------|---------|---------|--------|--------|--------|--------|--------|----------|--------|---------------|
| Epinions | HR      | 0.6283  | 0.6387 | 0.6251 | 0.6686 | 0.7008 | 0.6851 | 0.6782   | 0.6535 | <b>0.7459</b> |
|          | NDCG    | 0.4113  | 0.4217 | 0.4093 | 0.4543 | 0.4855 | 0.4808 | 0.4653   | 0.4449 | <b>0.5196</b> |
| Yelp     | HR      | 0.8098  | 0.7872 | 0.8087 | 0.8007 | 0.8102 | 0.7911 | 0.7815   | 0.7900 | <b>0.8396</b> |
|          | NDCG    | 0.5422  | 0.5258 | 0.5348 | 0.5315 | 0.5469 | 0.5300 | 0.5209   | 0.5331 | <b>0.5739</b> |
| E-Cmrc.  | HR      | 0.8948  | 0.8912 | 0.9008 | 0.8774 | 0.9077 | 0.8864 | 0.8493   | 0.8724 | <b>0.9115</b> |
|          | NDCG    | 0.6733  | 0.6602 | 0.6598 | 0.6510 | 0.6984 | 0.6534 | 0.6279   | 0.6497 | <b>0.7106</b> |

among different types of user-item interactions. While the baseline KGAT proposes to incorporate the auxiliary knowledge graph, it fails to explicitly differentiate type-specific behavioral patterns.

We further present the performance of click behavior prediction with different top- $K$  ranked items in Table 4. From the results, it is obvious that *KCGN* outperforms all baselines with different top- $K$  values, which demonstrate its robust ranking performance.

Table 4: Ranking performance evaluation on Yelp dataset with varying Top- $K$  value in terms of  $HR@K$  and  $NDCG@K$

| Model       | @5            |               | @10           |               | @15           |               |
|-------------|---------------|---------------|---------------|---------------|---------------|---------------|
|             | HR            | NDCG          | HR            | NDCG          | HR            | NDCG          |
| DiffNet     | 0.6311        | 0.4622        | 0.7853        | 0.5126        | 0.8628        | 0.5329        |
| SAMN        | 0.5995        | 0.4363        | 0.7514        | 0.4863        | 0.8271        | 0.5050        |
| DGRec       | 0.6114        | 0.4445        | 0.7662        | 0.4954        | 0.8399        | 0.5141        |
| EATNN       | 0.6258        | 0.4552        | 0.7715        | 0.5066        | 0.8411        | 0.5250        |
| NGCF+S      | 0.6428        | 0.4697        | 0.7813        | 0.5232        | 0.8525        | 0.5370        |
| KGAT        | 0.6398        | 0.4674        | 0.7721        | 0.5113        | 0.8541        | 0.5329        |
| GraphRec    | 0.6233        | 0.45044       | 0.7605        | 0.4943        | 0.8342        | 0.5137        |
| DANSER      | 0.6304        | 0.4624        | 0.7740        | 0.5082        | 0.8356        | 0.5245        |
| <i>KCGN</i> | <b>0.6594</b> | <b>0.4876</b> | <b>0.8026</b> | <b>0.5308</b> | <b>0.8682</b> | <b>0.5424</b> |

### Impact of Different Relation Encoders (RQ2)

We next perform experiments to evaluate the impact of the incorporation of multi-typed user-item interactions, user-wise relations, item-wise dependencies, and the temporal context, with the following five contrast variants of *KCGN*.

- *KCGN-M*: *KCGN* without modeling multi-behavioral patterns and only with singular-type interactions.
- *KCGN-U*: *KCGN* without the social relation encoder for capturing the social signals in the recommendation.
- *KCGN-I*: *KCGN* without the external knowledge to characterize the item semantic relatedness.
- *KCGN-UI*: *KCGN* without both the user- and item-wise relation encoders and remove the coupled mutual information paradigms in the joint learning framework.
- *KCGN-T*: *KCGN* without the temporal context encoding.

Figure 3 shows the comparison results of different variants. We can see that the joint model *KCGN* achieves the best performance. As such, it is necessary to build a

joint framework to simultaneously capture social dimension (users’ social influence), item dimension (knowledge-aware inter-item relations), multi-behavior interactions, and time-aware user’s interest, for making recommendations. In addition, *KCGN-UI* performs worse than *KCGN-U* and *KCGN-I*, which again confirms the efficacy of our designed heterogeneous relation aggregation functions.

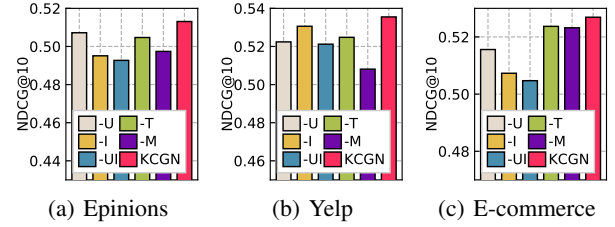


Figure 3: Ablation studies for different sub-modules of *KCGN* framework, in terms of  $HR@10$  and  $NDCG@10$ .

### Performance over Sparsity Distributions (RQ3)

One key motivation to exploit social- and knowledge-aware side information is to alleviate the sparsity issue, which limits the model robustness. Hence, we further evaluate our *KCGN* for both inactive and active users. In particular, we partition the target users into four sparsity levels in terms of their interaction densities. Figure 4 presents the evaluation results on different user groups on Yelp and E-Commerce data in terms of  $NDCG@10$ . We can observe that *KCGN* outperforms representative baselines in most cases, especially on sparse user groups. This suggests that incorporating both user and side knowledge as their external relations, empowers the representations of inactive users through our recursive information aggregation architecture.

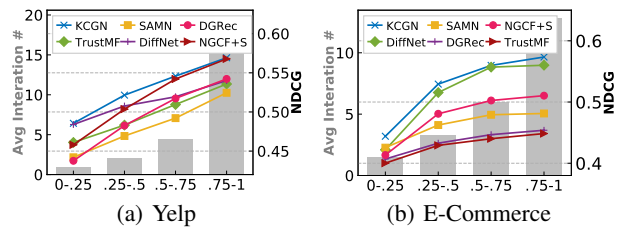


Figure 4: Performance of *KCGN* and baselines over users with different sparsity from Yelp and E-Commerce data.

### Qualitative Analyses of *KCGN* (RQ4)

We illustrate how our social-aware multi-typed relation encoding schema benefit the ability of embedding user’s preference into the latent learning space. In particular, we sample several users and their four- and five-star rated items

from Yelp dataset, and further visualize the corresponding user/item embeddings learned by NGCF+S and our KCGN (as shown in Figure 5). From the results, we can notice that: i) the visualized embeddings could well preserve the relationships between users and their interacted items with a clustering phenomenon (represented with the same color); ii) *KCGN* could provide a better separation for different users and their interacted items (*e.g.*, 9 v.s. 323, and 0 v.s. 341). Hence, the above observations verify the superior representation learning ability of *KCGN* through the encoding function which maps the social and behavioral interaction units into effective latent space.

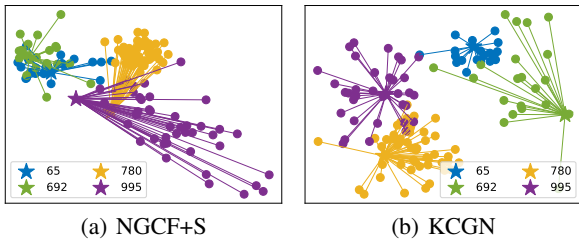


Figure 5: Visualized embeddings for users (stars) and their 4- or 5-rated item (circles), learned by *KCGN* and *NGCF+S*.

### Parameter Sensitivity Study (RQ5)

**Impact of # Recursive Graph Layers.** Figure 6 shows the experimental results with different number of embedding propagation layers over user-item interaction graph. We can observe that increasing the depth of *KCGN* could boost the performance, *i.e.*, *KCGN-2* performs better than *KCGN-0* (without the graph structure) and *KCGN-1* (only consider 1-hop neighbors). The performance improvement lies in the effective modeling of high-order collaborative effects across users and items. *KCGN* with 3 graph layers performs worse than *KCGN-2*, suggests that exploring higher-level relations may involve noise.

**Impact of Embedding Dimension.** We notice that the accuracy is initially improved with larger embedding size due to the stronger representation ability. However, the performance degrades with the further increase of dimensionality, which indicates the overfitting phenomenon.

### Model Efficiency Study (RQ6)

We finally investigate the computation cost of our *KCGN* when competing with state-of-the-art baselines. We perform experiments on a single NVIDIA GeForce GTX2080 Ti GPU. For fair comparison, the evaluation is conducted with the released code of baselines and we further optimize the implementations of data retrieval process for all baselines with efficient strategies (*e.g.*, sparse matrix storage). As shown in Table 5, we can observe that *KCGN* achieves competitive time efficiency (measured by running time of each epoch) when compared with neural social recommendation methods. It is worthwhile pointing out that methods with

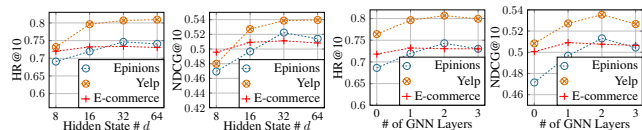


Figure 6: Hyper-parameter study of *KCGN*

Table 5: Model scalability study with running time (s).

| Data     | DiffNet | DGRec | SAMN | EATNN | NGCF+S | KGAT  | GraphRec | <i>KCGN</i> |
|----------|---------|-------|------|-------|--------|-------|----------|-------------|
| Epinions | 4.2     | 4.4   | 4.7  | 10.7  | 12.6   | 60.5  | 328.8    | 17.5        |
| Yelp     | 1.7     | 2.6   | 8.9  | 13.5  | 3.2    | 20.9  | 94.5     | 3.7         |
| E-Cmrc.  | 70.5    | 82.5  | 78.3 | 152.7 | 149.4  | 342.8 | 2400     | 70.2        |

stacking multiple graph attention layers is time-consuming, due to their pairwise attentive weights calculations for social or knowledge graph information aggregation.

## Related Work

**Social-aware Recommender Systems.** Deep learning has been revolutionizing recommender systems and many neural network models have been proposed for social recommendation scenario (Yin et al. 2019). For example, attention mechanisms are introduced to learn the influences between users, such as SAMN (Chen et al. 2019a) and EATNN (Chen et al. 2019b). It is worth mentioning that several recent efforts explore the GNNs for incorporating social relations into the user-item interaction encoding (Wu et al. 2019b; Fan et al. 2019; Wu et al. 2019a; Xu et al. 2020). Different from these methods, *KCGN* focus on fuse the heterogeneous relations from different modalities (social, item knowledge and temporal), to boost the recommendation performance.

**Graph Methods for Recommendation.** Many recent efforts have been devoted to exploring insights from GNNs for modeling collaborative signals in recommender systems. For example, inspired by the graph convolutional operations, PinSage (Ying et al. 2018) and NGCF (Wang et al. 2019c) aims to aggregate high-hop neighboring feature information over the user-item interaction graph. Several subsequent extensions have been developed to revisit the graph-based CF effects, such as LightGCN (He et al. 2020), LR-GCCF (Chen et al. 2020b) and KHGT (Xia et al. 2021). Motivated by these works, we propose a new knowledge-aware graph neural architecture for social recommendation.

## Conclusion

In this paper, we propose *KCGN*, an end-to-end framework that naturally incorporates knowledge-aware item dependency into the social recommender systems. *KCGN* unifies the user-user and item-item relation structure learning with a coupled graph neural network under a mutual information-based neural estimator. To handle the dynamic user-item interaction heterogeneity, we design a relation-aware graph encoder to empower *KCGN* to maintain dedicated representations of multiplex behavioral signals with the incorporation of temporal information. Through extensive experiments on real-world datasets, we demonstrate that *KCGN* achieves substantial gains over state-of-the-art baselines.

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