

Current Biology

Metabolic tradeoffs control biodiversity gradients through geological time

Highlights

- There is a non-monotonic relationship between climate and biodiversity through time
- Thermodynamics and physiology explain this temperature-biodiversity relationship
- Aerobic scope likely limits low-latitude biodiversity on geologic timescales
- Low-latitude ecosystems are particularly at risk under future climate projections

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In brief

Boag et al. demonstrate a non-monotonic relationship between temperature and diversity over the last 145 million years. By combining principles of thermodynamics and physiology, they derive a model that predicts this relationship. This suggests that low-latitude ecosystems are particularly vulnerable to future biodiversity loss in the near future.

Report

Metabolic tradeoffs control biodiversity gradients through geological time

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SUMMARY

The latitudinal gradient of increasing marine biodiversity from the poles to the tropics is one of the most conspicuous biological patterns in modern oceans.^{1–3} Low-latitude regions of the global ocean are often hotspots of animal biodiversity, yet they are set to be most critically affected by anthropogenic climate change.⁴ As ocean temperatures rise and deoxygenation proceeds in the coming centuries, the volume of aerobically viable habitat is predicted to decrease in these zones.^{5,6} In contrast to the slightly asymmetrical modern latitudinal biodiversity gradient,⁷ compilations of fossil occurrences indicate peaks in biodiversity may have existed much further away from the equator in the past, with transitions between climate states hypothesized to explain this trend.^{8–13} We combine a new compilation of fossil mollusc occurrences, paleotemperature proxies, and biogeographic data to reveal a non-monotonic relationship between temperature and diversity in the paleontological record over the last 145 million years. We derive a metabolic model that integrates the kinetic effects of temperature on biodiversity¹⁴ with the recently described Metabolic Index that calculates aerobic habitat availability based on the effect of temperature on hypoxia sensitivity.^{5,15,16} Although factors such as coastal habitat area and homeothermy are important,^{17,18} we find strong congruence between our metabolic model and our fossil and paleotemperature meta-analysis. We therefore suggest that the effects of ocean temperature on the aerobic scope of marine ectotherms is a primary driver of migrating biodiversity peaks through geologic time and will likely play a role in the restructuring of biodiversity under projected future climate scenarios.

RESULTS

Estimating temperature and biodiversity through time

In our analyses of temperature and biodiversity across the last 145 million years, we divided the globe into 24 equal-area latitudinal bins. We then calculated sea surface temperature and diversity for each of these latitudinal bins across ten time intervals that have been chosen based on the availability of temperature proxy data in the published literature with high-enough temporal and geographic resolution and broad-enough latitudinal spread: the Early Cretaceous (Berriasian to Barremian, 145–125 Ma), Campanian (83.6–72.1 Ma), Maastrichtian (72.1–66 Ma), Late Paleocene (59.2–56 Ma), Early Eocene (56–47.8 Ma), Middle Eocene (47.8–37.8 Ma), Early Oligocene (33.9–27.82 Ma), Late Miocene (Serravallian to Messinian, 13.82–5.333 Ma), Late Pliocene (3.333–2.58 Ma), and Modern. Although there is abundant temperature proxy data for earlier time periods, the data are often limited to very narrow latitudinal ranges. To determine the modern temperature gradient, we used objectively analyzed decadal averaged annual mean sea surface temperature data at one-degree grid resolution spanning 1955 to 2012 from the World Ocean Atlas 2013 V2.¹⁹ To estimate temperature for the nine geological time

periods, we obtained sea surface temperature estimates and associated paleolatitude estimates from previous compilations based on terrestrial and marine proxies.^{20–23} For each time interval, we fit a generalized additive spline model to the data using generalized cross validation. The model was then used to estimate the average sea surface temperature within each latitudinal bin.

For biodiversity estimates, we used genus-level mollusc occurrences. Molluscs are ideal ectotherms for such analyses due to their widespread geographic extent, abundance across marine ecosystems, and high preservation potential in the fossil record. We chose to estimate genus diversity for both the modern and our geologic time periods, as fossil specimens are very often not attributed to species. Although there has been debate as to whether genera should be used as proxies for species in the fossil record,²⁴ broad-scale geographic diversity patterns are often similar at both taxonomic levels.^{2,25} To calculate modern genus diversity, we downloaded mollusc occurrences from marine shelf environments (less than 200 m water depth) from the Global Biodiversity Information Facility (<https://www.gbif.org/occurrence/download/0135238-200613084148143>; summarized in Figure 1). To calculate genus diversity in the fossil record, we downloaded fossil mollusc occurrence data from the Paleobiology Database

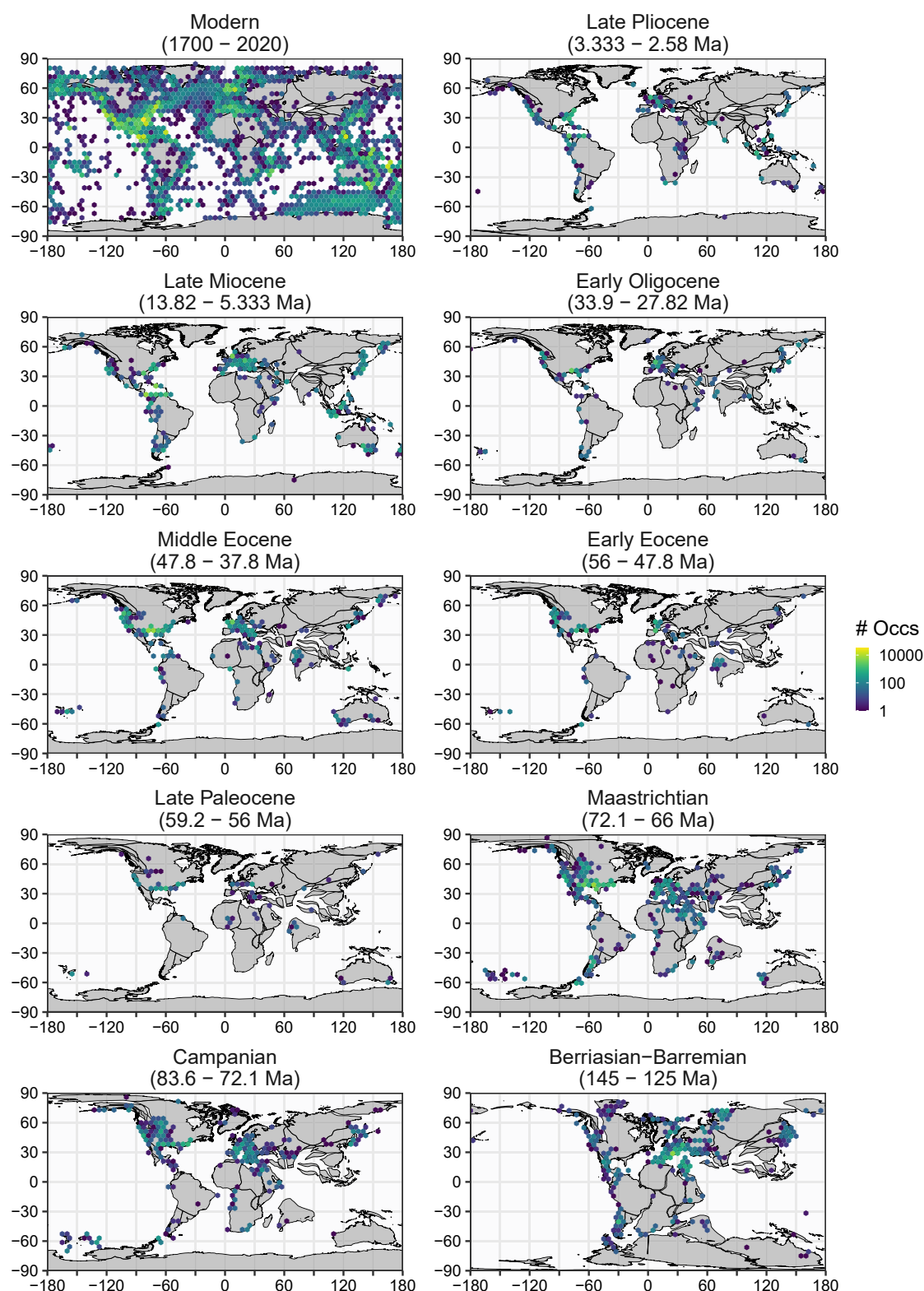


Figure 1. Density of raw mollusc occurrences plotted by time interval

Occurrences are binned within 5-degree by 5-degree hexagons for visualization purposes. Paleogeographic reconstructions are taken from GPlates.²⁶ See [Figures S1A and S1B](#) for a summary of occurrence distributions by latitude and temperature at the meta-analysis level.

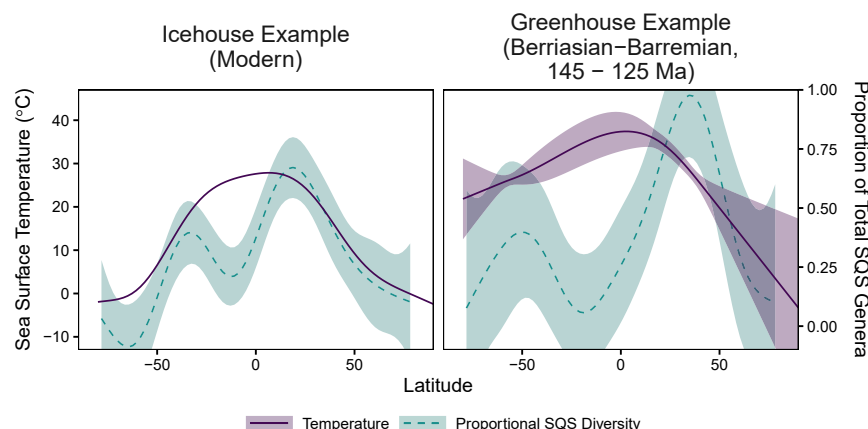


Figure 2. Examples of biodiversity and temperature gradients during cold periods and hot periods

Colored envelopes indicate 95% regression confidence intervals (approximately zero for modern temperature regression). During cold periods (e.g., Modern, maximum average annual temperature is $\sim 28^{\circ}\text{C}$, purple solid line), biodiversity (green dashed lines) peaks at low latitudes, but the biodiversity peak migrates to much higher latitudes during hot periods (e.g., Early Cretaceous, maximum average annual temperature is $\sim 37^{\circ}\text{C}$). In the greenhouse period, the diversity trough near the equator is further depressed, particularly relative to the diversity peak. See Figure S1C for more details and other time periods. Note that the regressions fit to the diversity data are for illustrative purposes only; we did not interpolate diversity data for any analyses.

(<https://paleobiodb.org>; summarized in Figure 1). For each time interval, we binned the occurrences within our 24 latitudinal bins using modern latitude or paleolatitude estimates.²⁶ Despite known geographic sampling biases in the fossil record,^{27,28} there is high specimen coverage across all temperatures and latitudes of interest, regardless of binning resolution (Figures S1A and S1B). Then, we used shareholder quorum subsampling (SQS)²⁹ with a quorum of 0.25 and 100 trials to estimate the generic diversity within each bin. We use this diversity metric to account for uneven preservation and sampling of specimens.^{30,31} We show that this specific quorum level (0.25) most effectively accounts for the possible correlation of sampling and diversity, as high diversity can be estimated even with small numbers of specimens (Figure S2A). For each time interval, we also estimated the global generic diversity using SQS with a quorum of 0.25 on the entire occurrence dataset. We divided our latitudinal bin diversity estimates by their respective global diversity estimates to standardize them across time intervals to proportional diversity.

To assess the relationship between temperature and proportional generic diversity since the Cretaceous, we fit nine different regression models to the data: linear; linear with one to four breakpoints; quadratic; cubic; quartic; and a generalized additive spline (GAM). We then compared their fit to the data using the corrected Akaike information criterion (ΔAICc and AICc weights).³² To address potential concerns regarding SQS or sampling biases, we repeated this model fitting approach using alternative diversity estimation methods and several sampling cutoffs (STAR Methods).

Climate and migration of biodiversity peaks

In total, we had occurrence data for 198 latitude bins across the nine geologic time intervals (Late Pliocene, 20; Late Miocene, 21; Early Oligocene, 17; Middle Eocene, 20; Early Eocene, 15; Late Paleocene, 13; Maastrichtian, 22; Campanian, 22; Berriasian-Barremian, 24) and for the Modern (24 bins). The temperature estimates for these bins range from -2°C to 37°C (271 to 310 K), and the proportional diversity estimates range from 1% to 84%. In time intervals with maximum temperatures below $\sim 27^{\circ}\text{C}$ (300 K; e.g., Modern, Late Pliocene, and Late Miocene), diversity tends to peak at low latitudes (Figures 2 and S1C; note that the regressions fit to the diversity data are for illustrative purposes only; we did not interpolate diversity data for any analyses). This matches

trends observed in many other Modern clades.^{2,3} However, time intervals with maximum temperatures greater than $\sim 27^{\circ}\text{C}$ (300 K) (e.g., Early Eocene, Late Paleocene, and Berriasian-Barremian) tend to exhibit more dramatic decreases in diversity near the equator, with peaks in diversity at higher latitudes (Figures 2 and S1C).^{8,10} Although, in general, these latitudinal diversity gradient reconstructions vary between different climate regimes, they also have variation that is likely caused by biases, such as limited sampling. The true diversity patterns may also be impacted by biotic or abiotic factors, such as lack of shallow shelf area, nutrient availability, and biotic interactions. To address these potential sources of variation between time intervals, here, we combine all these latitudinal gradients within our meta-analysis framework to investigate the direct effects of temperature on biodiversity, rather than comparing relative temperature differences reflected by latitude across different climate regimes (Figures 3, S1A, and S1B). Low-diversity estimates occur across the entire temperature range of our meta-analysis but are most pronounced at the extremes. However, high-diversity estimates ($>50\%$) almost exclusively occur in the middle of the temperature range, a trend that is robust to sampling intensity (STAR Methods). Combined, this results in a diversity-temperature relationship that peaks at moderate temperatures (15°C – 25°C) and decreases outside of this range.

Our model fitting approach resulted in essentially no support for a simple linear regression to summarize the relationship between proportional diversity and temperature (Table S1), regardless of diversity metric or sampling cutoff (Figure S2B). For the main analysis described above, the model with the best relative fit is a linear regression with a single breakpoint at 18.3°C (291.4 K; ± 3.2), with a slope of 0.12 for temperatures below this breakpoint and a slope of -0.03 for temperatures above it (Figure 3). The breakpoint temperature is robust to sampling, diversity metric, and binning method (STAR Methods; Figure S3A). Furthermore, the regression slope for lower temperatures is similarly robust and indistinguishable from the empirical estimate of Roy et al.¹ based on marine prosobranch gastropods and the theoretical range proposed by Gillooly and Allen³³ using the metabolic theory of ecology (STAR Methods; Figure S3B). Other models with substantial support ($<2 \Delta\text{AICc}$) include linear regressions with two or three breakpoints and a generalized additive spline. These four models together account for more than 85% of the AICc weight (Table S1).

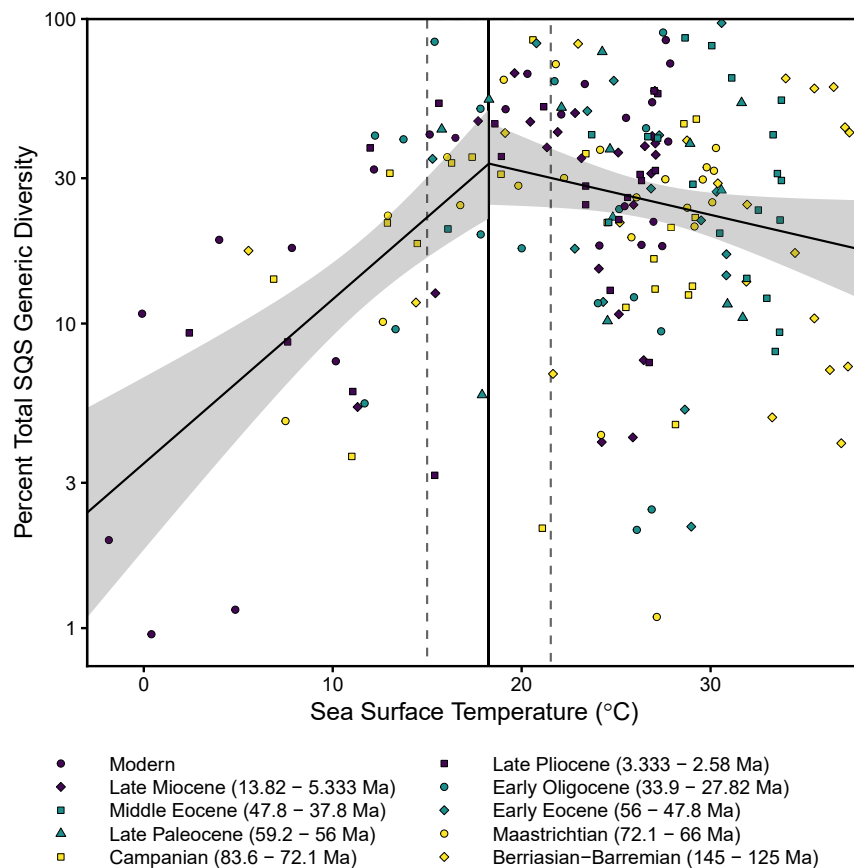


Figure 3. Estimated percent generic diversity and reconstructed temperature across the modern and nine geologic time intervals

Each point represents percent generic diversity in an equal-area latitudinal band from a given time interval, with sea surface temperature for each band determined from proxy data. The independent variable of temperature is therefore explicitly illustrated as a predictor of species diversity across all geological intervals at once. The solid vertical line indicates the best-fitting linear regression breakpoint, with the dotted vertical lines representing $\pm 1.96\sigma$. The black curve represents the best-fitting breakpoint regression, with the gray region representing the 95% confidence interval. See [Figures S2 and S3](#) for sensitivity analysis results.

A_o and E_o are species-specific physiological traits. A_o is the inverse of a species' hypoxic threshold (i.e., the minimum pO_2 at which resting metabolism can be sustained), and E_o is the temperature dependency of A_o . ϕ_{crit} is the ratio of the energy required to sustain key ecological activities versus resting metabolism. ϕ_{crit} is estimated based on the biogeographic distribution of taxa for which A_o and E_o are known. T_{ref} is a reference temperature of 15°C, and pO_2 is the partial pressure of oxygen in seawater.

We use a Monte Carlo approach to generate uncertainty-bounded predictions of diversity-temperature relationships in marine ectotherms.

Temperature-driven metabolic tradeoffs

We developed a novel metabolic model that combines the kinetic relationship between temperature and biodiversity^{14,33} and the predicted impact of temperature-dependent hypoxia on aerobic niche availability.^{5,15} Specifically, we propose that the change in total taxonomic richness (S_{tot} ; Equation 1) per unit temperature (T) is the sum of changes in richness predicted by the temperature dependence of biochemical kinetics (S_{kinet}) and the temperature dependence of aerobic habitat viability (S_{aerob}):

$$\frac{d \ln(S_{tot})}{dT} = \frac{d \ln(S_{kinet})}{dT} + \frac{d \ln(S_{aerob})}{dT} \quad (\text{Equation 1})$$

Our expression for S_{kinet} is borrowed directly from Allen et al.¹⁴ (Equation 2), where E is the activation energy of metabolism, k_B is the Boltzmann constant, and C_1 is a temperature-independent constant:

$$\ln(S_{kinet}) = \left(\frac{-E}{1000 k_B} \right) \left(\frac{1000}{T} \right) + C_1 \quad (\text{Equation 2})$$

S_{aerob} is defined based on the Metabolic Index, a method developed to quantify the extent of viable aerobic habitat for marine ectotherms (Equation 3):

$$S_{aerob} = \sum A_o \frac{pO_2}{\exp \left[\frac{-E_o}{k_B} \left(\frac{1}{T} - \frac{1}{T_{ref}} \right) \right]} > \phi_{crit} \quad (\text{Equation 3})$$

E (Equation 2), the slope of the linear relationship defining $\frac{d \ln(S_{kinet})}{dT} \left(\frac{1000}{T} \right)$ in Allen et al.,¹⁴ is parameterized by a uniform distribution describing updated calculations and associated uncertainty for the activation energy of metabolism.³³ A_o , E_o , and ϕ_{crit} are all individually parameterized using probability density functions that describe the physiological responses of 61 different marine ectotherm species (described in Penn et al.¹⁵ and [Table S2](#)). pO_2 is parameterized by a uniform distribution defined by the 5th and 95th percentiles of observed modern sea surface values.³⁴ Initial $\ln(S_{tot})$ values are defined based on our best fit model and associated uncertainty presented in [Figure 3](#), calibrating the relative predicted changes in biodiversity with temperature from our model to observed data. We specifically highlight how the temperature sensitivity of hypoxic thresholds (E_o ; Equation 3) relates to predicted biodiversity-temperature relationships. We therefore solve our model at E_o values corresponding to the mean, mean $\pm 0.5\sigma$, and mean $\pm 1\sigma$ of the normal distribution ([Table S2](#)) to produce the analyses presented in [Figure 4](#). See [STAR Methods](#) for further details of Monte Carlo approach and methods for solving differential equations. We additionally present distributions of modeled annual mean equatorial sea surface temperature (summarizing spatial variation) from the HadGEM2-ES Earth system model³⁵ for preindustrial climate (based upon the year 1860) and Representative/Extended Concentration Pathways 4.5 and 8.5^{36,37} for the years 2100 and 2299, to aid comparison between our results and future projected sea surface temperatures ([Figure 4](#)).

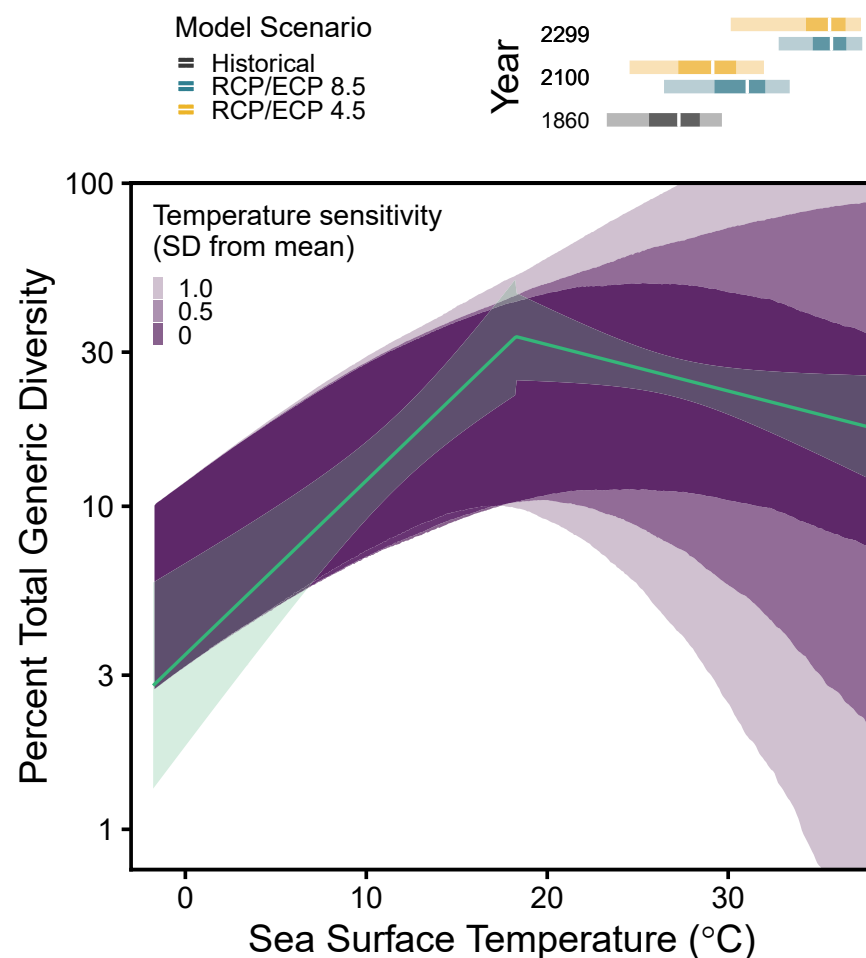


Figure 4. Combined metabolic model describing predicted relationships between biodiversity and temperature

The dark purple envelope describes 2 SD estimates of diversity for mean E_o (temperature sensitivity of hypoxic threshold). Lighter purple envelopes illustrate the increased uncertainty of predicted diversity with 0.5 and 1 SD from mean temperature sensitivity. Green line shows the observed relationship between percent generic diversity and temperature as summarized in Figure 3. Above the model, we illustrate the distributions of monthly equatorial sea-surface temperatures predicted for the years 2100 and 2299 under Representative and Extended Concentration Pathways (RCP/ECP) 4.5 and 8.5, relative to historical model temperatures for 1860 from the HadGEM2-ES model. Vertical white lines represent median values across the global surface ocean, darker bars represent interquartile ranges of spatial temperature variation, and lighter bars represent 5th and 95th percentiles. See Figure S4 for results of sensitivity analysis using temperature sensitivity of individual mollusc species.

DISCUSSION

Although this study evaluates marine biodiversity from the late Mesozoic through Cenozoic, the principles laid out here may also serve as a framework for interpreting the role of climate change and physiology in driving biodiversity trends deeper into the Phanerozoic. For example, combined Earth system and ecophysiological modeling of the

Our combined metabolic model predicts the first-order relationship between temperature and marine biodiversity that we observe in our analyses of primary data (Figure 4). The model supports an approximately exponential increase in proportional biodiversity below 20°C–25°C, in agreement with the metabolic theory of ecology.¹⁴ At higher temperatures, aerobic limitation becomes a dominant control and predicted biodiversity begins to decline with increasing temperature, matching well with our observations from the fossil record (Figure 4). At extreme temperature sensitivities, our model can accommodate both a continuous monotonic increase in diversity, as predicted by the metabolic theory of ecology,¹⁴ and a precipitous drop, as predicted by the Metabolic Index,^{5,15,16} but both of these scenarios are unlikely, given the modern distributions of temperature sensitivities.^{15,16} Of the 61 marine ectotherms used to construct the probability density functions defining the E_o , A_o , and ϕ_{crit} distributions used in the Monte Carlo model, 7 are molluscs. However, we propose (as previous authors have)¹⁵ that the improved sampling density of modern physiological responses that we gain from including non-molluscan taxa improves the accuracy of our model relative to using molluscan data alone. We further demonstrate that we can capture the full range of temperature-diversity relationships shown in Figure 3 using the individual mollusc E_o values from the Penn et al.¹⁵ dataset (Figure S4).

Permian-Triassic extinction suggests temperature-dependent hypoxia tolerance predicts the latitudinal loss of biodiversity observed across the boundary.¹⁵ Furthermore, the flattened overall biodiversity gradient in the early Triassic³⁸ can be linked to persistently higher sea surface temperatures (>30°C–40°C) than those in the modern equatorial ocean,^{39–41} as well as the potentially compounding effects of widespread ocean deoxygenation.^{15,42} Expanding studies like these to wider intervals of the geologic record has exciting potential but in many cases would require the generation of considerably more geochemical data (and potentially more paleontological data).

In deep time, peaks in latitudinal biodiversity broadly correspond with climate state;¹⁰ however, these patterns may also be impacted by other factors, such as continental shelf area⁴³ and continental configuration.^{44,45} Also, there are inherent biases associated with reconstructing these patterns of biodiversity from the fossil record, including anthropogenic search intensity and geographic sampling,⁴⁶ taxonomic classification,⁴⁷ animals with hard parts preserving better than soft-bodied groups,⁴⁸ and time averaging of assemblages as they enter the fossil record.⁴⁹ Furthermore, when reconstructing paleotemperatures, marine and terrestrial environments may record slightly different temperature histories, proxy data are unlikely to have sufficient resolution to examine the impact of seasonality, and individual

paleotemperature proxies have system-specific uncertainties (e.g., the $\delta^{18}\text{O}$ proxy may be impacted by assumptions regarding seawater isotope values and diagenetic alteration).^{50,51} Despite these possible sources of uncertainty, our use of comprehensive paleontological data and spatially extensive paleotemperature proxy data within a meta-analysis framework has revealed a strong connection between temperature and diversity through Earth history.

Looking toward future climate projections, increases in greenhouse gas concentrations leading to a global mean warming of $\sim 0.75^\circ\text{C}$ to 2.75°C by the end of the 21st century (Representative Concentration Pathways 2.6–8.5; Figure 4)³⁶ will likely result in continued dissolved oxygen loss and up to 6°C warming of the upper tropical ocean by 2300 (Extended Concentration Pathway 8.5; Figure 4).³⁷ These changes will place many tropical species with already limited acclimation potential⁵² at temperature and oxygen conditions that are beyond their aerobic thresholds.⁵³ At an ecosystem scale, this loss of aerobic scope will likely affect biodiversity through disruption of complete life cycles, including predator-prey dynamics, ontogeny, and reproduction, in addition to fragmentation of suitable physiological habitats via poleward migration to extratropical latitudes ($>35^\circ$).^{5,54–56} Other factors, such as declines in primary production, ocean acidification, overfishing, and dead zone expansion, are also expected to exacerbate the effects of warming and deoxygenation.^{57–60} Given the expected impacts of these stressors, it remains a critical unanswered question whether the loss of tropical marine biodiversity will be recovered in the coming centuries by long-term acclimation and physiological adaptation.^{60,61}

Our paleotemperature data compilation reveals that models of upper ocean temperatures for 2300 predict similar thermal maxima as those measured during hyperthermal events in the geological record, such as the Paleocene-Eocene Thermal Maximum and Early and Latest Cretaceous (Figures 4 and S1C). Furthermore, fossil latitudinal biodiversity gradients of molluscs from the past 145 million years show that, over geological timescales, warmer-than-modern ocean climates with sea surface temperatures above 24°C – 27°C result in the permanent extirpation of species richness from tropical latitudes proportional to absolute seawater temperature. Our model results demonstrate that temperature-driven loss of aerobic scope explains this pattern (Figure 4). Of course, many other factors are also expected to negatively impact habitat viability during hyperthermal events, such as physical changes to coral reef habitats (e.g., the impacts of reef accumulation rates and structural complexity on total habitat area and volume),^{62,63} however, our results demonstrate that metabolism alone can account for a significant portion of the observed trends. Given the geological timescale of these patterns (millions of years), this suggests that physiological adaptation of marine ectothermic animals is insufficient to allow the repopulation of tropical latitudes during hyperthermal intervals.⁵⁶ These findings suggest that contemporary emissions-driven warming will likely result in a comparable loss of biodiversity in the tropical ocean as ecosystems increasingly suffer from the chronic impacts of warming in the coming centuries, a trend that may have already begun.¹²

STAR★METHODS

Detailed methods are provided in the online version of this paper and include the following:

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SUPPLEMENTAL INFORMATION

Supplemental information can be found online at <https://doi.org/10.1016/j.cub.2021.04.021>.

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AUTHOR CONTRIBUTIONS

T.H.B. conceived of the project, and all authors designed the research approach. W.G. performed the diversity and temperature analyses with input from T.H.B. and R.G.S. R.G.S. performed the metabolic modeling analyses with input from T.H.B. and W.G. All authors wrote and edited the manuscript.

DECLARATION OF INTERESTS

The authors declare no competing interests.

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STAR★METHODS

KEY RESOURCES TABLE

REAGENT or RESOURCE	SOURCE	IDENTIFIER
Deposited data		
Paleobiology Database	https://paleobiodb.org	https://github.com/willgearty/biogradients/blob/v1.0.0/PBDBdata.RData (Paleobiology Database download as described in text - accessed December 2020)
Global Biodiversity Information Facility	https://www.gbif.org	https://www.gbif.org/occurrence/download/0135238-200613084148143 (Global Biodiversity Information Facility download as described in text - accessed December 2020)
HadGEM2-ES	Centre for Environmental Data Analysis (https://data.ceda.ac.uk)	https://data.ceda.ac.uk/badc/cmip5/data/cmip5/output1/MOHC/HadGEM2-ES
Deposited data	This paper	https://github.com/willgearty/biogradients
Software and algorithms		
R computing environment	http://www.r-project.org/ ; R Development Core Team ⁶⁴	v4.0.3
Deposited code	This paper	https://github.com/willgearty/biogradients
rgbif package in R	Chamberlain et al. ⁶⁵	v3.4.0
plyr package in R	Wickham ⁶⁶	v1.0.2
dplyr package in R	Wickham et al. ⁶⁷	v1.0.2
raster package in R	Hijmans et al. ⁶⁸	v3.4-5
paleoMap package in R	https://github.com/willgearty/paleoMap	Accessed December 2020
dispeRse package in R	https://github.com/laurasoul/dispeRse	Accessed December 2020
mgcv package in R	Wood ⁶⁹	v1.8-33
segmented package in R	Muggeo ⁷⁰	v1.3-1
AICcmodavg package in R	Mazerolle ⁷¹	v2.3-1
deeptime package in R	https://github.com/willgearty/deeptime ; Gearty ⁷²	v0.5.2
ggplot2 package in R	Wickham ⁷³	v3.3.2
viridis package in R	Garnier ⁷⁴	v0.5.1
broom package in R	Robinson et al. ⁷⁵	v0.7.3
Hmisc package in R	Harrell ⁷⁶	v4.4-2
MASS package in R	Venables and Ripley ⁷⁷	v7.3-53
rworldmap package in R	South ⁷⁸	v1.3-6
geosphere package in R	Hijmans ⁷⁹	v1.5-10
deSolve package in R	Soetaert et al. ⁸⁰	v1.27.1
ncdf4 package in R	Pierce ⁸¹	v1.17
RNetCDF package in R	Michna and Woods ⁸²	V2.4-2

RESOURCE AVAILABILITY

Lead contact

Further information and requests for resources should be directed to and will be fulfilled by the Lead Contact, Thomas Boag (thomas.boag@yale.edu)

Materials availability

This study did not generate any reagents or other materials.

Data and code availability

All data and code generated during this study are deposited in the GitHub repository <https://github.com/willgearty/biogradients>.

EXPERIMENTAL MODEL AND SUBJECT DETAILS

This study used fossil occurrence data from the Paleobiology Database (<https://paleobiodb.org>) and modern biogeographic occurrence data from the Global Biodiversity Information Facility (<https://www.gbif.org>). No new occurrence data was collected for this study and no physical experiments were conducted.

METHOD DETAILS

Sampling Coverage

To visually assess the sampling coverage of our fossil mollusc occurrence dataset, we plotted the density of occurrences within each time interval (Figure 1). The paleolatitude and paleolongitude coordinates of each occurrence were estimated using the GPlates rotation model.²⁶ Points were binned within 5-degree by 5-degree hexagons. Some intervals have notable sampling geographic biases, such as a lack of sampling in the Indopacific before the Miocene and limited Southern Hemisphere sampling in several intervals.

To visually assess whether this was a concern at the meta-analysis level, we used the combined modern and fossil mollusc occurrence dataset to calculate the number of occurrences within equal-area latitude bins (12, 24, 45, 90, or 180 bins). We then plotted these occurrence sums (which represent fossil preservation and sampling intensity) against both the bins' mean latitude/paleolatitude (Figure S1A) and mean estimated temperature/paleotemperature (Figure S1B). Despite sampling biases within individual intervals (see above), at the meta-analysis level there is high specimen coverage across all temperatures and paleolatitudes.

Diversity Sensitivity Analyses

Alternative Methodologies

To demonstrate that the observed diversity pattern throughout the geologic record is robust to the methodology used to estimate diversity, we performed additional analyses that cover a wide spectrum of alternative methodologies. We split the occurrence data into a varying number of latitudinal bins (12, 24, 45, 90, and 180 bins), either based on equal areas (each bin has an identical surface area) or equal width (each bin has an equal latitudinal width). We then used these binned occurrences to estimate genus diversity in one of three ways: 1) rangethrough, in which taxa are assumed to occur at all points between their northernmost and southernmost occurrences, then diversity is estimated as in the raw occurrences method; 2) raw occurrences, in which diversity is estimated purely based on the raw number of unique genera that occur in a latitudinal bin; 3) shareholder quorum subsampling (SQS; Locarnini et al.¹⁹), in which genera are drawn from the occurrences in a given bin until a given "quorum" of the population is achieved based on the frequencies of the genera. We tested quorum values of 0.25, 0.5, and 0.75. For all quorum levels we performed 100 trials. We also tested the inclusion and exclusion of modern data and the use of raw diversity estimates versus proportional diversity estimates (each value is divided by the total generic diversity estimated using the same methodology). Altogether, this resulted in 200 different combined occurrence binning and diversity estimation methodologies. The results of these alternative methodologies were used for several of the following sensitivity analyses.

Sampling Effect on Diversity Estimation

To visually assess whether sampling intensity influenced diversity estimation, we plotted our latitudinal bin diversity estimates from all of the alternative sensitivity methodologies (see above) against the number of specimens/occurrences within the latitudinal bins (Figure S2A). The raw and rangethrough methods suffer from high correlation between diversity estimates and sampling intensity. SQS remedies this to varying degrees at different quorum levels. The 0.25 quorum level allows for high and low diversity estimates across nearly the entire sampling intensity spectrum (30+ specimens). While there are some modern biodiversity hotspots that are notably under-sampled in the fossil record (e.g., the Coral Triangle in the western Pacific Ocean, Figure 1, which was a tectonically active region for most of the time interval studied and has been historically under-sampled by paleontologists), these analyses demonstrate that we have good sampling across sea-surface temperatures. Geographic sampling biases therefore do not appear to have biased our sampling of the relationship we are principally interested in, i.e., that between marine biodiversity and environmental temperature.

HadGEM2-ES Model Results

Past and projected future climate model results are illustrated in Figure 4 to contextualize the relevance of our analyses for future climate change scenarios. We downloaded HadGEM2-ES results from the Centre for Environmental Data Analysis (<https://data.ceda.ac.uk/badc/cmip5/data/cmip5/output1/MOHC/HadGEM2-ES>). For the equatorial temperature distributions presented in Figure 4, we downloaded monthly sea water potential temperature data spanning the years 1860 (Historical model), 2100 (Representative Concentration Pathway, RCP 4.5 and 8.5³⁶) and 2299 (Extended Concentration Pathway, ECP 4.5 and 8.5³⁷). For each model scenario in each model year targeted, we computed 5th, 25th, 50th, 75th and 95th percentiles of monthly mean seawater potential temperature for 0-10 m water depth across the central equatorial cells (0.34 to -0.34 degrees latitude).

QUANTIFICATION AND STATISTICAL ANALYSIS

Diversity Sensitivity Analyses

Breakpoint Bootstrap

To assess the robustness of the breakpoint estimation to data outliers, we performed a bootstrap analysis. Each bootstrap consisted of sampling a new set of 198 latitudinal bins from the original compilation with replacement. We made 1000 of these bootstrap

datasets and performed a single breakpoint linear regression on each one. We then calculated a weighted mean and standard deviation for the 1000 breakpoint estimates using $1/\sigma^2$ as the weights for the breakpoint estimates. This mean (17.6°C , $290.7\text{K} \pm 3.4$) is not significantly different from the breakpoint of the original analysis (18.3°C , $291.5\text{K} \pm 3.3$).

Model Fitting

To assess the relationship between temperature and proportional generic diversity since the Cretaceous, we fit nine different regression models to the data: linear, linear with one to four breakpoints, quadratic, cubic, quartic, and a generalized additive spline (GAM). We repeated this process 100 times to account for the randomness associated with the bootstrap algorithm used in the breakpoint regression. We then compared the model fits using the corrected Akaike Information Criterion (ΔAICc and AICc weights).³² To address potential concerns regarding SQS or sampling biases, we repeated this entire model fitting approach using a subset of the alternative methods described above (all analyses used 24 equal-area bins) across three levels of sampling cutoffs (30, 50, and 200 specimens within each bin) (Figure S2B). This approach resulted in essentially no support for a simple linear regression to summarize the relationship between proportional diversity and temperature, regardless of diversity metric or sampling cutoff.

Diversity-Temperature Relationship Sensitivity

Once we had estimated genus diversity for each of alternative methodologies described above, we performed a breakpoint linear regression on the diversity~temperature data. The estimated breakpoint is robust to binning and diversity estimation methodologies (Figure S3A). We then extracted the slope of the diversity~temperature relationship for temperatures below the estimated breakpoint, which is also robust to the sensitivity analyses, especially when modern data is included (Figure S3B). Additionally, most slope estimates overlap with the estimate from Roy et al.¹ and the theoretical value from Gillooly and Allen³³ (Figure S3B).

Combined Metabolic Model

We employ a Monte Carlo approach to model diversity-temperature relationships as described in Equations 1, 2, and 3. The distributions used to parameterize the variables in our combined metabolic model are defined in Table S2. $\frac{d \ln(S_{\text{kinet}})}{d(1000/T)}$ is defined by a linear relationship, as in Allen et al.¹⁴ We sample a uniform distribution of E_o values 100 times to incorporate uncertainty in the precise slope of this relationship³³ (Table S2). Changes in $\ln(S_{\text{Aerob}})$ with temperature are defined by the interaction of multiple parameters that are individually described by probability density functions¹⁵ (Table S2). In this study, we focus on how the temperature-sensitivity of hypoxic thresholds (E_o , Equation 3) relates to predicted biodiversity-temperature relationships, defined by a normal distribution as in Penn et al.¹⁵ (Table S2). We solve our model at E_o values corresponding to the mean, mean $\pm 0.5\sigma$ and mean $\pm 1\sigma$ of this normal distribution to produce the analyses presented in Figure 4. A_o and ϕ_{crit} are defined by log-normal distributions as in Penn et al.¹⁵ (Table S2), each sampled 10,000 times. pO_2 is parameterized using a uniform distribution based on modern observations,^{19,34} again sampled 10,000 times. The same 10,000 A_o , ϕ_{crit} , and pO_2 values are used in each E_o iteration of our Monte Carlo analyses for consistency. These 10,000 samples are combined to represent a total possible genus pool in our model space, the temperature-sensitivity of which changes with each E_o percentile. $\frac{d \ln(S_{\text{Aerob}})}{d(1000/T)}$ is computed separately for each E_o percentile using discretization to maximize accuracy, despite the complex non-linear relationships, in the same dimensional space as Allen et al.¹⁴ The distribution of initial values for the differential model is defined based on the best fit model of generic diversity and temperature presented in Figure 3 at the lowest modeled temperature (-1.71°C , 271.44K), and the 95% confidence intervals of the entire general additive model. Specifically, the mean 95% confidence interval of the segmented linear regression model is used to define the standard deviation of a normal distribution intended to represent approximately the same level of uncertainty illustrated in Figure 3. The intercept of the plotted metabolic model analyses was adjusted to minimize the residual sum of squares between the median metabolic model values (median of distribution at median E_o) and the best fit model presented in Figure 3. 100 initial values were randomly subsampled from this normal distribution and are applied in each E_o iteration of our Monte Carlo analysis. We note that the E_o , A_o , and ϕ_{crit} distributions from Penn et al.¹⁵ are derived from a range of animal phyla, whereas our biodiversity data compilation (Figure 3) is based on molluscs only. We propose (as previous authors have¹⁵) that the improved sampling density of modern physiological responses that we gain from including non-molluscan taxa improves the accuracy of our model relative to using mollusc data alone. We also show that we can capture the full range of temperature-diversity relationships shown in Figure 3 using the individual mollusc E_o values from the Penn et al.¹⁵ dataset (Figure S4).