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Natural statistics as inference principles of auditory tuning in biological and artificial midbrain networks

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1 **Manuscript Title Page**

2 **1. Manuscript Title (50 word maximum)**

3 Natural statistics as inference principles of auditory tuning in biological and artificial midbrain networks

4

5 **2. Abbreviated Title (50 character maximum)**

6 Auditory tuning in biological and artificial brain

7

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38

39

40 Natural statistics as inference principles of auditory tuning in biological and artificial midbrain networks

41

42 **Abstract**

43 Bats provide a powerful mammalian model to explore the neural representation of complex sounds, as
44 they rely on hearing to survive in their environment. The inferior colliculus (IC) is a central hub of the
45 auditory system that receives converging projections from the ascending pathway and descending
46 inputs from auditory cortex. In this work, we build an artificial neural network to replicate auditory
47 characteristics in IC neurons of the big brown bat. We first test the hypothesis that spectro-temporal
48 tuning of IC neurons is optimized to represent the natural statistics of conspecific vocalizations. We
49 estimate spectro-temporal receptive fields (STRF) of IC neurons and compare tuning characteristics to
50 statistics of bat calls. The results indicate that the FM tuning of IC neurons is matched with the statistics.
51 Then, we investigate this hypothesis on the network optimized to represent natural sound statistics and
52 to compare its output with biological responses. We also estimate biomimetic STRF's from the artificial
53 network and correlate their characteristics to those of biological neurons. Tuning properties of both
54 biological and artificial neurons reveal strong agreement along both spectral and temporal dimensions,
55 and suggest the presence of nonlinearity, sparsity and complexity constraints that underlie the neural
56 representation in the auditory midbrain. Additionally, the artificial neurons replicate IC neural activities
57 in discrimination of social calls, and provide simulated results for a noise robust discrimination. In this
58 way, the biomimetic network allows us to infer the neural mechanisms by which the bat's IC processes
59 natural sounds used to construct the auditory scene.

60

61 **Significance Statement**

62 Recent advances in machine learning have led to powerful mathematical mappings of complex data.
63 Applied to brain structures, artificial neural networks can be configured to explore principles underlying
64 neural encoding of complex stimuli. Bats use a rich repertoire of calls to communicate and navigate their
65 world, and the statistics underlying the calls appear to align with tuning selectivity of neurons. We show
66 that artificial neural network with a nonlinear, sparse and deep architecture trained on the statistics of
67 bat communication and echolocation calls results in a close match to neurons from bat's inferior
68 colliculus. This tuning optimized to yield an effective representation of spectro-temporal statistics of bat
69 calls appears to underlie strong selectivity and noise invariance in the inferior colliculus.

70

71 **1. Introduction**

72 Biological neural circuits are believed to provide an efficient code of the sensory world, which allow us
73 to process complex and dynamic stimulus information from our surroundings. Perception of an auditory
74 scene is created by neural activity filtered through several stages of feed-forward and feedback sensory
75 processing. Sound pressure of an acoustic signal is first transduced into a bio-electrical signal in the
76 cochlea. Subsequently, the bio-electrical signal is relayed through the auditory pathway. The inferior
77 colliculus (IC) is an auditory hub that receives ascending inputs from brainstem nuclei and sends

78 information through the thalamus to the auditory cortex, while it also receives descending inputs from
79 auditory cortex (Casseday et al., 2002). The IC encodes complex auditory features such as frequency
80 sweep rate (Williams and Fuzessery, 2010) and patterning (Gordon and O'Neill, 1998) that are necessary
81 for identification of complex auditory objects and therefore plays a key role in representing these
82 objects in a natural listening environment.

83 Echolocating bats build a representation of their surroundings by emitting ultrasonic vocalizations and
84 processing the features of returning echoes to compute the location and features of targets and
85 obstacles in the environment. Bats must rapidly process sonar echoes while concurrently parsing
86 environmental noise and calls emitted by conspecifics. In this complex and rapidly changing auditory
87 scene, the bat's brain efficiently encodes acoustic stimuli and allows the animal to accurately track prey,
88 avoid obstacles, and communicate with conspecifics while dynamically navigating a three-dimensional
89 environment. Humans and other animals face similar challenges in the course of their natural acoustic
90 behaviors. With the goal of elucidating principles underlying auditory scene analysis in the midbrain, we
91 examine the relationship between statistics of the rich acoustic repertoire of bat calls and neural
92 response patterns in the bat's IC to explore artificial networks tuned to map natural statistics in these
93 calls and identify emergent properties that match responses in the IC.

94 Here, we test the hypothesis that the bat's auditory midbrain is optimized to accurately represent the
95 natural statistics in the sounds and echoes that exist in the bat's environment (particularly social and
96 echolocation calls). Past research has suggested that the IC plays a major role in the representation and
97 mapping of communication sounds that give rise to specialized encoding of natural sounds along the
98 ascending auditory system (Aitkin et al., 1994; Suta et al., 2003). An earlier study in the Mexican free
99 tailed bat suggested a possible correspondence between tuning characteristics of individual IC neurons
100 and properties of natural calls from conspecific sounds (Andoni et al., 2007; Brimijoin and O'Neill 2005).
101 In the current study, we corroborate this relationship in a different species and further probe constraints
102 and implications of such optimal encoding of natural sounds on auditory signal processing in a complex
103 scene.

104 We recorded vocalizations from socially housed bats and analyzed the spectro-temporal statistics of
105 natural sounds (e.g. frequency modulation (FM) velocity, directionality). Using the database of collected
106 statistics, we built an artificial network, which projects sounds onto a latent space that efficiently
107 represents statistics of these natural sounds in a strategy of signal reconstruction (Smith and Lewicki,
108 2006). This computational model offers a biomimetic architecture whose main operation is to capture
109 the statistics of natural bat calls, without information about the function of biological neurons. We then
110 ask: Does the emergent tuning of this artificial network match properties of biological neurons in the big
111 brown bat inferior colliculus? To answer this question, we also recorded responses to sound stimuli,
112 spectro-temporal ripples, from individual neurons in the IC of big brown bats.

113 It is known that the spectro-temporal receptive fields (STRF's) suggest a reasonable linear-
114 approximation of neural responses as a transfer function from acoustic stimuli and those are usually
115 used to explore auditory characteristics of the neurons (Andoni et al., 2007; Depireux et al., 2001; Elhilali
116 et al., 2013). We extracted STRF's from IC and artificial neurons and calculated auditory characteristics
117 from these neural response functions (Kowalski et al., 1996; Poon and Yu, 2000). The spectro-temporal
118 tuning characteristics of biological neurons were then compared to both the statistics of natural calls as
119 well as emergent tuning of artificial neurons. By varying the configuration of the artificial network, we

120 employed the theoretical network as springboard to examine possible constraints on the configuration
121 of midbrain networks, and gauge the validity of the hypothesis linking biological encoding in the
122 mammalian midbrain to efficient representation of natural sound statistics. While various artificial
123 neural networks can be optimized to reconstruct an input sound from compressed feature on latent
124 space, finding an architecture that closely emulates the biological network provides insights into the
125 underlying functional role of certain brain nuclei. Here, we examine the relationship between the
126 optimal encoding of natural statistics in bat calls and its role in facilitating robust selectivity across sound
127 classes in the repertoire. The graphical abstract in Fig. 1 shows an overview of the approach taken in this
128 work.

129

130 **2. Materials and Methods**

131 **2.1. Collection of Bat's vocalization**

132 **2.1.1. Animals**

133 Big brown bats (*Eptesicus fuscus*) were collected from an exclusion site under a state permit. All
134 experimental procedures were carried out in accordance with a protocol approved by an Institutional
135 Animal Care and Use Committee. A total of approximately 100 bats were housed in our Lab and used for
136 vocal data recordings, and four (2 male, 2 female) bats were used for neurophysiological data collection.

137

138 **2.1.2. Audio recordings for training the biomimetic network**

139 A bat call library was built from audio recordings of bats housed in a vivarium room where the
140 temperature is kept at 70-80 °F, and humidity is kept at 30-70 %. This room holds approximately 100
141 bats in groups of 1-6 separated in mesh cages. The recordings were made for two days using an Avisoft
142 CM16/CMPA ultrasonic microphone and the Avisoft-RECORDER software. Mono audio was recorded at a
143 sampling rate of 300 kHz.

144 Natural call recordings from big brown bats were processed to extract meaningful segments. An
145 energy-based signal activity detection was performed on the entire database to remove the silences
146 between calls and to split the recordings into segments containing bat calls (Park et al., 2014). As a
147 result, we constructed species specific databases containing 17,713 calls (about 10 min) for big brown
148 bats. This call database was used for training artificial networks. The data was divided into a training set
149 (15,000 randomly selected calls) to learn network parameters and test set (remaining 2,713 calls) for
150 verifying the network.

151

152 **2.1.3. Social calls for natural sound representation**

153 To investigate discriminability in the artificial network, we used a social call database that includes 26
154 audio clips for 8 different types of bat calls (Fig. 2). These types include six calls, as defined in (Wright et
155 al., 2013), specifically, Echolocation (Echo), Frequency Modulated Bout (FMB), Upward Frequency
156 Modulated (UFM), Long Frequency Modulated (LFM), Short Frequency Modulated (SFM), and Chevron-
157 Shaped (CS); in addition to two additional calls types, Long-Wave and Hook, which resemble a hook in
158 time-frequency space. All audio clips were up-sampled from 250 kHz to 300 kHz.

159

160 **2.2. Neurophysiological Inferior Colliculus data**

161 Recordings of neural responses from IC neurons were used to perform two separate analyses: (1)
162 characterize receptive field tuning of IC neurons; and (2) examine discriminability of IC neurons to
163 different con-specific calls. Methods for receptive field analysis are described next in section 2.2.4, while
164 data used for discriminability analysis are described in section 2.2.5.

165

166 **2.2.1. Receptive field recordings**

167 A head-post was adhered to the skull of bats for head fixation as described in (Macias et al., 2018). The
168 inferior colliculus was located using skull and brain landmarks and a surgical drill was used to make a ≤ 1
169 mm diameter craniotomy preserving dura. The neurophysiological recordings were performed in a
170 sound-attenuating and electrically shielded chamber (Industrial Acoustics Company, Inc.). Each bat was
171 restrained individually in a custom-made foam mold and the head was fixed by the head-post. Recording
172 sessions were carried out over 3 to 5 consecutive days, each one lasting no more than 4 hours. Water
173 was offered to the bats every 2 hours. No drugs were administered during recordings. During recordings
174 a silver wire for grounding was placed in between muscle and skull about 5mm rostral to the craniotomy
175 site. The 16-channel recording probe (Neuronexus A1x16-5mm-50-177-A16) was inserted into the brain
176 using a micromanipulator. The surface of the brain was registered as 0 μm for depth reference and the
177 probe was advanced in 10 μm steps using a hydraulic microdrive (Stoeling Co.). Recordings were taken
178 at least 100 μm apart. An OmniPlex D Neural Data Acquisition System recording system (Plexon, Inc.)
179 was used to obtain neural responses with 16-bit precision and 40 kHz sampling rate. A transistor-
180 transistor-logic (TTL) pulse for each stimulus presentation was generated with the National Instrument
181 card used for stimulus presentation and was recorded on channel 17 of the analog channels of the
182 acquisition system for synchronization of acoustic stimuli and neural recordings. The stimuli were
183 recorded on channel 18 of the acquisition system to corroborate synchronization.

184

185 **2.2.2. Moving ripple stimuli**

186 A set of ripple stimuli was generated to estimate STRFs of IC neurons (Kowalski et al., 1996; Depireux et
187 al. 2001; Andoni et al., 2007). Ripples are modulated noise stimuli that are dynamic both in time and
188 frequency. Each ripple can be described as

$$189 S(t, x) = 1 + \Delta A \times \sin(2\pi(\omega t + \Omega x) + \phi) \quad (1)$$

190 where t and x are indices for time and octave scaled frequency. ΔA and ϕ are amplitude and a phase,
191 respectively. And ω and Ω represent modulation rates along temporal (Hz) and spectral (cyc/oct) axes.
192 The temporal and spectral modulation parameters were varied from -176 - 176 Hz in steps of 32 Hz and
193 0.0 - 1.5 cyc/oct in steps of 0.15 cyc/oct spectrally (Fig. 3A). Each ripple spanned 6.66 octaves from 1.2
194 kHz to 121 kHz and was 300 ms in duration.

195

196 **2.2.3. Audio playbacks for neural recordings**

197 Extracellular recordings from the inferior colliculus of awake animals were taken while they passively
 198 listened to broadcast of either ripple stimuli, or pure tones at 70 dB. All stimuli were generated at a
 199 sampling rate of 250 kHz using a National Instruments card (PXIE 6358) and transmitted with a
 200 calibrated custom-made electrostatic ultrasonic loudspeaker connected to an audio amplifier (Krohn-
 201 Hite 7500). The loudspeaker was placed at 60 cm (for all ripple and pure tones stimuli) from the bat's
 202 ear. The frequency response of the loudspeaker was compensated by digitally filtering the playback
 203 stimuli with the inverse impulse response of the system as described in (Luo and Moss, 2017).

204 Frequency tuning curves were built by recording neural responses to pure tones of 5 ms duration (with
 205 0.5 ms ramping rise and fall). The tones ranged between 20 and 90 kHz (in 5 kHz steps) and the sound
 206 pressure levels ranged from 20 to 70 SPL (10 dB steps). At each recording site first, we played 20
 207 repetitions of the randomized ripple stimulus and then 15 repetitions of each of the randomized pure
 208 tones at a different SPL.

209

210 2.2.4. Analysis of neuronal responses

211 For the analysis of auditory tuning in response to ripple and pure tone stimuli, responses were sorted
 212 offline, then single units were detected using the program 'Wave_clus' (Quiroga et al., 2004). Each
 213 individual waveform was inspected and the acceptance threshold for clusters was less than 10% of
 214 spikes with < 3 ms inter-spike interval, consistent with the neuronal refractory period. Any sites that
 215 showed no response to ripple stimuli were excluded from the spike sorting and further analysis in line
 216 with procedures used in other studies (Poon and Yu, 2000; Escabi and Schreiner, 2002; Andoni et al.,
 217 2007). After spike sorting, the Euclidian distance error between the mean and variance of number of
 218 spikes across trials was computed. Units whose error is less than 1.0 were selected for further analysis,
 219 following a Poisson model of spike representation (Corrado et al., 2005; Schwartz et al., 2006). This
 220 analysis resulted in 108 single units used for the current study.

221 **Neurophysiological STRFs:** At each recording site, ripple stimuli were repeated 10-20 times in a
 222 randomized order for each repetition. A PST histogram was calculated from the spike time sequence of
 223 each ripple; then histograms were folded into 32-point periods. The strength and phase of the response
 224 to each ripple were estimated directly from the fundamental component obtained by applying a 32-
 225 point Fast Fourier Transform (FFT) to the period histogram. Magnitude and phase responses to each
 226 ripple were combined together into a magnitude matrix $M(\Omega, \omega)$ and a phase matrix $\Phi(\Omega, \omega)$,
 227 respectively. To derive a Ripple Transfer Function (RTF), which is a representation of a STRF in the
 228 modulation domain, $M(\Omega, \omega)$ and $\Phi(\Omega, \omega)$ were expanded to four quadrants in the modulation domain
 229 spanning from -176 Hz and -1.5 cyc/oct to 176 Hz and 1.5 cyc/oct as $M_e(\Omega, \omega) = M_e^*(-\Omega, -\omega) =$
 230 $M(\Omega, \omega)$ and $\Phi_e(\Omega, \omega) = \Phi_e^*(-\Omega, -\omega) = \Phi(\Omega, \omega)$ based on a symmetric property around the origin
 231 (Depireux et al., 2001; Andoni et al., 2007). As a result, the RTF was formulated as

$$232 T(\Omega, \omega) = M_e(\Omega, \omega) e^{j\Phi_e(\Omega, \omega)} \quad (2)$$

233 where $j = \sqrt{-1}$. Finally, a STRF was obtained by performing 2D inverse FFT on the RTF as

$$234 STRF(x, t) = F_{t, -x}^{-1}[T(\Omega, \omega)] \quad (3)$$

235 where F^{-1} designates the 2D inverse FFT along each axis in the modulation domain.

236

237 2.2.5. Neural discriminability of con-specific calls

238 In order to examine selectivity of IC neurons to calls from the bat's natural repertoire, we re-used neural
239 data previously collected in an earlier study (Salles et al., 2020), where we collected neuronal responses
240 to Echolocation calls (Echo) versus Frequency-Modulated Bout (FMB) social calls. The study followed the
241 same methodology for data collection as described here. 'Wave_clus' was used to detect and classify
242 single units from the recordings. The spikes responding to either FMB or Echo were counted in windows
243 of 25 ms duration, starting 5ms after stimulus onset. Some units with an average of less than five spikes
244 over 20 times recordings were excluded because they were considered as a non-responsive unit to the
245 stimulus. Multi-unit activity was determined from inter-spike intervals with < 3ms that were inconsistent
246 with neuronal refractory period; and units with greater than 10% of spikes with < 3ms inter-spike
247 interval were excluded from analysis. As a result, total 575 units were finally obtained and their
248 responses are used in the present work to contrast neural discriminability between Echo and FMB calls
249 with artificial neurons.

250

251 2.3. Responses in artificial neurons

252 2.3.1. Artificial network front-end processing

253 To develop a biomimetic architecture, a biologically-inspired auditory spectrogram is used as input for
254 the network (Shamma, 1985a; Shamma, 1985b; Yang et al., 1992; Wang and Shamma, 1994). The
255 auditory spectrogram incorporates four processing stages that emulate peripheral processing in the
256 mammalian system: cochlear filtering, auditory-nerve transduction, hair cell responses, and lateral
257 inhibition (Chi et al., 2005). Briefly, an incoming acoustic waveform is analyzed along a bank of constant-
258 Q filters spanning a logarithmic scale. Then, each frequency channel undergoes a high-pass, nonlinear
259 compression and low-pass filtering followed by lateral inhibition across frequency, following the
260 implementation available in the NSL toolbox (Chi and Shamma, 2005) with the following settings: The
261 frame length was set to 0.2 ms without overlap, and each octave was represented with 24 channels (i.e.
262 128 channels over 5.33 octaves). Octave-scaled center-frequencies were represented as $f_c = 440 \times$
263 $2^{((c-32)/24+\gamma)}$ where f_c is a center frequency of the c^{th} channel, and γ is a constant factor of octave
264 shift ($\gamma = 4.38$). Inputs to the artificial network were sampled as square patches of the spectrogram
265 spanning 128 frequency channels (i.e. 5.33 octaves) and 160 time-samples (i.e. 32 ms).

266

267 2.3.2. Structure of artificial network

268 An artificial neuron, i.e. node mimicking a biological neuron, is mathematically modelled by a linear
269 combination of pre-node outputs and a non-linear activation function. An artificial network is
270 constructed by connecting a large number of nodes to each other. Using nonlinear activation functions
271 enables the network to perform nonlinear computations on feedforward propagation. For this study, we
272 favored a generative architecture using an autoencoder composed of an encoder, which compresses
273 original data into a compact code; and a decoder, which reconstructs the original signal from that code
274 (Baldi, 2012; Doersch, 2016). The intuition is to directly test our hypothesis that the network would infer

275 a statistical model of the training dataset of natural calls, and if successful should allow a faithful
 276 reconstruction of the inputs.

277 The proposed architecture is shown in Fig. 4. First an encoder stage E is composed of convolutional
 278 layers, pooling layers, and a fully connected layer. A latent vector represents compressed features
 279 learned from the input data. A decoder stage D composed of reverse operations using transposed
 280 convolutions, reconstructs the input features from a latent vector. A sampling stage, interposed
 281 between the encoder and decoder, emulates neural activity yielding sparse binary activations.

282 Using the same general building block composed of convolution and pooling layers, this study
 283 investigates various configurations of the network by varying: (1) *depth*, which is the number of blocks.
 284 In Fig. 4, the black-flow shows a double stacking structure as an example. A deeper network can be
 285 constructed by stacking more blocks, on the other hand, a shallow network can be created by removing
 286 a block; (2) *nonlinearity*, by varying the slope of nonlinear activation function employed; and (3) *sparsity*,
 287 by controlling the density of sampling in the latent space.

288 The encoder architecture E follows a convolutional neural network (CNN) framework in order to reduce
 289 the number of trainable parameters, hence controlling for over-fitting issues and generalizability to
 290 unseen data (Dietterich, 1995). The convolutional layers compute output feature maps using 2D
 291 convolutions between input feature maps and several filters as

$$292 \quad I_o^l[f, t, k] = \sum_{\xi, \tau, m} I_i^l[\xi, \tau, m] f^l[\xi - f, \tau - t, m, k] \quad (4)$$

293 where f, t, l, k and m are indices for spectral, temporal, layer, channel of output feature map, and
 294 channel of input feature map respectively. I_i , I_o , and f^l are feature maps for input and output, and
 295 convolutional filter applied in the l^{th} layer, respectively. Multi-scale filters are employed in each
 296 convolutional layer to balance broad span (in time and frequency) vs. localized analyses. Then, output
 297 feature maps concatenate filter outputs using multi-sized filters (Fig. 5A) (Szegedy et al., 2015). Specifics
 298 of both filter composition and dimensions of intermediate feature maps are summarized in Table 1.
 299 Neural activation by an acoustic feature is emulated by applying a nonlinear function after convolution
 300 as

$$301 \quad I_a^l[f, t, k] = \max(I_o^l[f, t, k], \alpha \times I_o^l[f, t, k]) \quad (5)$$

302 where α is a constant within an interval $[0, 1]$ (Maas et al., 2013). Next, pooling layers compress the
 303 output from the previous convolutional layer by extracting a maximum among some values enclosed by
 304 a non-overlapping window (i.e. max-pooling) I^l (Scherer et al., 2010). As a result, the width and height
 305 of the output are reduced by half. At the top of the encoder, a fully connected layer is applied for
 306 mapping into a latent space, which involves natural statistics requiring to reconstruct original input, as
 307 $v_c = W_l^T \times \text{flatten}(I^L)$ where I^L is a feature map in the last pooling layer, W is weight matrix in the
 308 fully connected layer, and $\text{flatten}(\cdot)$ is a reshape function from a 3D tensor to a vector.

309 In the middle stage, a binary code vector v_b is generated by performing a Bernoulli sampling process. A
 310 sigmoid function is applied to the latent vector to calculate prior probabilities. Thus, the output of the
 311 middle stage is represented as $v_b = \text{Bernoulli}(\sigma(v_c))$ where $\sigma(\cdot)$ is a sigmoid function.

312 The decoder D is composed of a fully connected layer and transposed convolution layers. In the fully
 313 connected layer, a latent vector is expanded into an initial space as $\hat{v} = W_l \times v_b$, and the vector \hat{v} is

314 reshaped to a 3D tensor as a set of initial feature maps as $\hat{l}^l = \text{reshape}(\hat{v})$. From initial feature maps, a
 315 transposed convolution using multi-scale filters is sequentially performed until the output has the same
 316 dimensions as the input patch (Shelhamer et al., 2017; Radford et al., 2015). Convolutional filters used in
 317 the encoder are applied for transposed convolution after transposing input channel from output
 318 channel dimension as $\hat{f}^l[f, t, k, m]$. A transposed convolution using multi-scale filters is performed in
 319 three steps (Fig. 5B). First, the input feature map \hat{l}^l is split into submaps, $[\hat{l}_1^l, \hat{l}_2^l, \dots, \hat{l}_N^l]$, as many as the
 320 number of filters. Second, transposed convolution is individually performed for each pair of submap and
 321 filter. Finally, a set of output feature maps is obtained by averaging the results of the second step.

322

323 2.3.3. Training artificial network

324 The network was trained using the cost function:

$$325 \quad L = \frac{1}{2} \sum_n [(x_n - D(E(x_n)))^2 + \lambda(\rho - \sum_i \sigma(v_{c_i}))^2] \quad (6)$$

326 where x_n is an input patch with respect to the n^{th} index, $E(\cdot)$ represents an encoder function while
 327 $D(\cdot)$ is for a decoder, and ρ means the average number of active nodes. The first term represents the
 328 mean square error between an input patch and its reconstruction by the autoencoder. The sparse
 329 constraint prevents overfitting as well as emulates sparsity of active neurons in the brain. Let Y be a
 330 random variable representing the number of active nodes by the Bernoulli process. Then, the
 331 distribution known as the Poisson binomial distribution is denoted as

$$332 \quad \Pr(Y = \rho) = \sum_A [\prod_{i \in A} \sigma(v_{c_i}) \prod_{j \in A^c} (1 - \sigma(v_{c_j}))] \quad (7)$$

333 where A is a set whose elements are possible combination for choosing ρ nodes from N nodes. This
 334 distribution can be approximated by $\text{Binomial}(N, \mu/N)$ where $\mu = \sum_i \sigma(v_{c_i})$ (Choi and Xia, 2002). The
 335 network training was implemented using TensorFlow (Abadi et al., 2016). AdamOptimization was
 336 applied for an optimizer with $1.0e-4$ learning rate. And, λ was set to $1.0e-4$. For more details,
 337 readers can find the implementation on <http://www.github.com/JHU-LCAP/BioSonar-IC-model/>.

338 Comparisons between the biological neurons and artificial neurons were performed to infer the
 339 network configuration that best matches the characteristics of IC neurons (as explained next). The best
 340 configuration composed of a triple stacking network, a parameter of nonlinearity $\alpha = 0.2$ in (5), and 10%
 341 sparsity constraint in (6).

342

343 2.3.4. Biomimetic STRFs

344 Once trained, the network was interrogated following the same procedure as biological neurons. The
 345 same ripple stimuli were given as input to the network and activity of the nodes before applying the
 346 sigmoid activation and the Bernoulli sampling, v_c in Fig. 4 was characterized. Each ripple was
 347 transformed into an auditory spectrogram (as described earlier). A sequence of input patches for each
 348 ripple were then composed by applying a sliding window (window length: 160 frames) in every 2 ms
 349 (sliding step: 10 frames) (Fig. 3B). Input patches in the sequence were consecutively fed into the pre-
 350 trained encoder, then a latent vector v_c was obtained every 2 ms. The same procedure for extracting

351 biological STRF's was followed (See, Section 2.2.4). To find the magnitude m and phase ϕ of the
 352 responses, we performed a 32-point Fast Fourier Transform (FFT) and derived the magnitude and
 353 unwrapped phase of the fundamental component (Fig. 3C). By repeating this procedure for all ripples,
 354 the magnitude and phase were collected in a matrix $M(\Omega, \omega)$ and a $\Phi(\Omega, \omega)$, respectively (Fig. 3D).
 355 These modulation responses were then converted into time-frequency STRF profiles by performing a 2D
 356 inverse FFT on the RTF (Fig. 6). Note that, in this study, all network architectures employed a total 100
 357 artificial neurons (spanning a 100-dimensional latent space) so that 100-biomimetic STRFs were used for
 358 analysis.

359

360 **2.4. Analysis of auditory characteristics**

361 **2.4.1. Natural statistics and Auditory characteristics**

362 *Frequency Modulation (FM) velocity (statistics of bat calls):* To characterize conspecific vocalizations, we
 363 calculated FM velocities of each call segment in our database. Since moving ripples were used as bases
 364 components of the Fourier modulation domain (Singh and Theunissen, 2003), we derived auditory
 365 spectrograms of each call, then performed a 2D FFT after mean subtraction to remove constant
 366 components. $T_c(\Omega, \omega) = F_{f,t}[S(f, t) - \bar{S}]$ where $F_{f,t}[\cdot]$ is the 2D FFT, S is an auditory spectrogram of a
 367 bat call, and \bar{S} is its mean over the time and frequency axes. A velocity line was estimated by performing
 368 a line fitting on the magnitude of 2D FFT result. Finally, the FM velocity of a bat call was acquired by
 369 calculating the slope of the velocity line.

370 *Best Velocity (BV):* We defined a best velocity as the center of mass with respect to response power in a
 371 magnitude plot. To estimate the center of mass, we performed a Gaussian surface fitting on the 1st
 372 quadrant of magnitude plot. After normalization as $\bar{M}_e = M_e / [\sum_{\Omega, \omega} M_e \Delta \Omega \Delta \omega]$ where $\Delta \omega$ and $\Delta \Omega$ are
 373 respectively step size of temporal and spectral modulation rate, the fitting was performed to estimate
 374 mean vector and covariance matrix, by minimizing a square mean error function as
 375 $Err = \frac{1}{2} \sum_{\Omega, \omega} (ln(\bar{M}_e) - ln(G_{\mu, \Sigma}))^2$, where $G_{\mu, \Sigma}$ is a Gaussian distribution with mean vector μ and
 376 covariance matrix Σ . By performing the Least Square Error (LSE) estimator iteratively (Kay, 1993), we
 377 derived the Gaussian mean vector and covariance matrix. Best Velocity was defined as the slope of the
 378 mean vector (Fig. 7).

379 *Orientation (Ori):* To characterize velocity selectivity, we defined orientation as the angle between a
 380 line connecting the origin to the center of mass and a dominant eigenvector of the Gaussian covariance
 381 matrix. Note that the dominant eigenvector indicates the dominant direction of magnitude spread at
 382 the center of mass (Fig. 7) (Andoni et al., 2007).

383 *Inseparability (Ins):* Singular value decomposition (SVD) is applied to each STRF for calculating
 384 inseparability (Depireux et al., 2001). This approach decomposes the STRF into a linear combination of
 385 rank-1 matrices; in other words, $STRF = \sum_i \lambda_i \mathbf{u}_i \mathbf{v}_i^H$, where \mathbf{u}_i and \mathbf{v}_i are respectively left- and right-
 386 eigenvectors (column vector) corresponding to a singular value λ_i , and H means Hermitian transpose
 387 (Strang, 2009). Based on this definition, a STRF is called separable if the STRF can be approximated by
 388 summation of just a few matrices otherwise it is inseparable. We measured inseparability of a STRF
 389 calculated as $Ins = 1 - \lambda_1^2 / \sum_i \lambda_i^2$, where $\lambda_1 \geq \lambda_2 \geq \lambda_3 \geq \dots$. Note that the inseparability is bounded
 390 within the interval $[0, 1]$ where the Ins is equal to 0 for separable STRFs otherwise it goes to 1.

391 *Direction Selectivity Index (DSI):* To investigate direction selectivity of STRF's, we compared total power
 392 in the 1st and the 2nd quadrant of the RTF. If a STRF favors downward-moving ripples, total power in
 393 the 1st quadrant of magnitude plot is larger than the other since the 1st quadrant is composed of
 394 responses evoked by downward-sweeping ripples. From this perspective, a DSI was defined as
 395 $DSI = (P_2 - P_1)/(P_2 + P_1)$ where P_i is a power in the i^{th} quadrant of RTF, and it is calculated by
 396 $P_i = \sum_{(\Omega, \omega) \in Q_i} |T(\Omega, \omega)|$ where Q_i means the i^{th} quadrant. Since the power on each quadrant is a non-
 397 negative value, the DSI is bounded within the interval [-1,1] where downward/upward selectivity is
 398 represented to negative/positive DSI while 0 represents no selectivity in the direction. DSI for natural
 399 vocalizations was derived using the Fourier representation described to derive FM velocity.

400 *Best Frequency (BF):* To investigate frequency selectivity of STRFs, we defined a BF as the frequency of
 401 the maximum peak of absolute STRF, $|STRF|$ over the entire time and frequency spans. Best frequency
 402 (spectral peak) of natural calls was computed by finding the peak frequency of the average spectrum.

403

404 2.4.2. A bootstrap for statistical comparison}

405 We performed a bootstrap analysis to evaluate similarity between distributions of characteristics (e.g.
 406 FM velocity, BV) comparing natural calls, IC neurons, and artificial neurons. The procedure selects
 407 random 30 samples from natural calls in each iteration with replacement. For IC neurons, random
 408 samples from each of the 4 bats are used in each iteration to maintain a balanced representation across
 409 bats. In case of artificial neurons, we trained 10 independent-networks (using different initialization
 410 procedures) and combined the neurons from each network into a complete set that was then sampled
 411 during the bootstrap procedure. For each comparison and each bootstrap repetition, the distance
 412 between means was noted. 1000 repetitions were used to generate a distribution of mean distances
 413 $d_{(\mu, \sigma)}$ where μ and σ are the mean and standard deviation. The *p*-value for accepting null hypothesis
 414 was calculated as $p = 1 - 2 \int_0^{|\varepsilon|} d_{(0, \sigma)}(x) dx$ where $d_{(0, \sigma)}$ is a zero-mean Gaussian distribution with
 415 same variance σ , and ε was a real number satisfying $d_{(0, \sigma)}(\varepsilon) = d_{(\mu, \sigma)}(\varepsilon)$.

416

417 2.5. Natural sound representation with artificial neurons

418 2.5.1. Analysis of response selectivity in artificial neurons

419 We explored response selectivity to bat calls in biomimetic neurons. To replicate the study performed
 420 on IC neurons (Salles et al., 2020), FMB and Echo calls in the sound database were used to measure
 421 responses on artificial neurons. Each audio clip was fed into the network after converting to auditory
 422 spectrogram (See, Section 2.3.1), then we obtained activation probabilities for 100-nodes due to the
 423 stimulus as $\sigma(v_c)$ in Fig. 4. We averaged the activation probabilities over the same type of calls, and
 424 placed the results for 100-nodes onto a 2D scatter plot. Since the IC neurons are categorized into 3-
 425 groups such FMB selective, Echo selective, and Non-selective (Salles et al., 2020), we performed k-
 426 means clustering ($k=3$) on the principal axis by the principal component analysis (PCA).

427

428 2.5.2. Social call representation with artificial neurons

429 We explored bat's call representation with the biomimetic network. In order to perform stochastic
430 analysis, we made 10-copies for each audio clip in the natural sound database (See. Section 2.1.3) by a
431 data augmentation based on temporal shift so that 260 audio clips were ready for the response analysis
432 on artificial network. After converting the audio clips for 8 types of bat call to auditory spectrogram (See,
433 Section 2.3.1), the spectrograms were fed into the network to obtain the network's responses, the ν_c in
434 Fig. 4. Then, we estimated the Gaussian distributions for the responses to each call type, and measured
435 a distance between two distributions by using the Jensen-Shannon divergence (JSD) as $JSD(P\|Q) =$
436 $(KLD(P\|M) + KLD(Q\|M))/2$ where P and Q represent two target distributions, KLD is the Kullback-
437 Leibler divergence (KLD), and $M = (P + Q)/2$ (Endres and Schindelin, 2003). Unlike the KLD, the JSD is
438 bounded within the interval $[0,1]$ where 0 means that two distributions are equal. Finally, we quantified
439 a discriminability across the classes by averaging JSDs of all cases choosing 2 of 8. In evaluation, we
440 calculated the averaging JSDs with 10-models for each configuration that were trained on different
441 initial values and summarized the mean and standard deviation of the 10 results. Additionally, we
442 explored the noise effect on the sound representation with simulated audios produced by adding
443 Gaussian random noise to each of the 260 audio clips depending on signal to noise ratio (SNR).

444 To compare with neural data, we performed this analysis between FMB and Echo responses. In the
445 same manner, we calculated JSD based on the networks. We adopted neural data used in the previous
446 study (Salles et al., 2020). Among 575 neurons, we chose 351 neurons which were recorded with same
447 version of stimuli, and constructed 351-dimensional vector to represent response pattern across the
448 neurons by concatenating the number of spikes on each neuron. Once the vector is projected onto 100
449 dimensional space based on PCA, we estimated Gaussian distributions for FMB and Echo responses.
450 Then, we calculated JSD between the distributions.

451

452 3. Results

453 3.1. Database of natural big-brown bat calls

454 Acoustic recordings of bat calls emitted while socially housed in the laboratory yielded a data set of
455 natural calls containing a wide range of vocalization types. Fig. 8 shows the time-frequency
456 representation of several types of vocalizations in the database. The bat vocalizations include isolated
457 (non-overlapping) calls representing communication (Fig. 8A-C) or echolocating (Fig. 8D-G) sounds as
458 well as overlapping calls from two distinct bats (Fig. 8G-H). Best Velocity (BV) values reflect the broad
459 range of FM energies in these social communication calls (BV = 18 oct/s, 43 oct/s and 140 oct/s for Fig.
460 8A, B and C respectively). Echolocation calls show even higher FM energies with shorter signals (BV =
461 274 oct/s and 333 oct/s for Fig. 8D and E respectively). In Fig. 8G and H, we note presence of multiple
462 calls though the statistics derived from that segment are largely influenced by the dominant call (BV =
463 381 oct/s and 410 oct/s for Fig. 8G and H respectively). The natural complexity in the animal's auditory
464 environment was maintained in this study and no supervised curation of this data set was performed
465 beyond removal of silence segments (see *Methods*). We also note presence of ambient background in all
466 recordings as a result of the cage environment and recording setup used to collect this data.

467

468 3.2. Auditory characteristics of biological STRF's

469 To explore auditory characteristics of big brown bat midbrain, we calculated STRF's from neural
470 recordings of IC neurons. Fig. 9A highlights examples from 6 neurons, revealing a downward sweep
471 selectivity, with excitation and inhibition represented as red and blue areas, respectively. The best
472 frequency (BF) is also shown as red dashed line indicating the maximum peak, positive or negative, of
473 the STRF. We evaluated auditory characteristics across all neural recordings with respect to BV, DSI
474 (direction selectivity), orientation, and inseparability (Fig. 10, yellow histograms). Using a bootstrap
475 procedure, we compared the auditory characteristics of IC neurons to properties of natural calls (Fig. 10,
476 gray background regions for standard deviation). The analysis revealed that the distribution of BVs in IC
477 neurons is statistically equivalent to that of natural calls ($\mu=-1.63$, $\sigma=17.13$, $p\text{-value}=0.9622$, Fig. 10A). A
478 match was also observed for direction selectivity $\mu=-0.01$, $\sigma=0.03$, $p\text{-value}=0.8789$, Fig. 10B). This result
479 is consistent with the hypothesis that IC neurons have consistent tuning to the statistics of conspecific
480 vocalizations (Andoni et al., 2007). We noted that the majority of IC neurons (93.6%) favored downward
481 sweeps (Fig. 10B) (Gittelman et al., 2009) while their orientation is centered around 0 deg. Most IC
482 neurons yield higher than rank-one STRF's (average inseparability index 0.49 ± 0.09).

483 The distribution of frequency tuning (BF) of IC neurons tended to fall between 10 and 30 kHz.
484 Particularly, BF's of 87% of neurons are below 30 kHz (Fig. 11B). In contrast, spectral peaks observed in
485 the vocalization database revealed a higher spectral peak (37.17 ± 5.62) as shown in Fig. 11A. This
486 profile is likely driven by the strength of the first harmonic component in vocalization which tends to be
487 stronger than other components. As seen from the examples in Fig. 8, most vocalizations contain
488 multiple harmonic peaks with higher energy in the first component resulting in a difference between the
489 BF of IC neurons and spectral peaks of the calls database ($\mu=-12.58$, $\sigma=1.82$, $p\text{-value}=0$).

490

491 **3.3. Auditory characteristics of artificial STRF's**

492 Using natural calls, an artificial network was trained to best represent the statistics of the vocalization.
493 Characteristics of model neurons were analyzed in the same way as biological neurons using spectro-
494 temporal receptive fields. The distribution of model characteristics is shown in Fig. 10, overlaid in blue.
495 Compared to natural calls, model neurons reveal a statistically matching distribution with respect to BV
496 (bootstrap $\mu=-2.62$, $\sigma=19.85$, $p\text{-value}=0.9473$) and DSI (bootstrap $\mu=-0.005$, $\sigma=0.01$, $p\text{-value}=0.9382$).
497 Model neurons also match the spectral peak of natural calls (bootstrap $\mu=-0.49$, $\sigma=4.75$, $p\text{-value}=0.9592$,
498 Fig. 11C). These results are not surprising given that the model was trained to mimic the statistics of
499 these calls. Still, the model was not specifically configured to match specific directionality or velocity
500 patterns but rather represent the time-frequency profile of the calls as a whole.

501 In parallel, the comparison between model and biological neurons reveal remarkable agreement. A
502 bootstrap procedure was performed to compare all auditory characteristics of these STRF's, and results
503 are shown in inset panels in Fig. 10. We note that characteristics of biomimetic neurons match the
504 properties of IC neurons including BVs ($\mu=2.92$, $\sigma=16.61$, $p\text{-value}=0.9300$), DSI ($\mu=0.01$, $\sigma=0.07$, $p\text{-value}=0.9358$),
505 orientation ($\mu=1.34$, $\sigma=3.26$, $p\text{-value}=0.8370$), and inseparability ($\mu=-0.02$, $\sigma=0.04$, $p\text{-value}=0.8079$). The BFs of artificial neurons are statistically different from IC neurons (bootstrap $\mu=12.10$,
506 $\sigma=4.44$, $p\text{-value}=0.1731$), even though there is substantial overlap at the range of 0-40 kHz. The BFs of
507 artificial neurons are more broadly distributed over the entire frequency range with about 14% of
508 artificial neurons having high BF (above 60 kHz) (Ferragamo et al., 1997).

510

511 **3.4. Architecture of the biomimetic network**

512 While results reported so far focus on the 'best' biomimetic network, we also investigated how changing
513 the architecture of the model affects the tuning parameters of artificial neurons. We systematically
514 varied the model in terms of structural complexity (the number of stacking blocks), sparsity of the latent
515 space and non-linearity of the activation function. Fig. 12A shows the mean and standard deviation of
516 characteristics of model neurons across 10-network validations for each pair of complexity and sparsity
517 ($\alpha = 0.2$). The mean FM velocities and orientation in the natural calls database are represented by a
518 black line on each panel; while the grey regions represent 95% confidence intervals for each mean. The
519 results show that a very shallow model (mono-stacking) results in a greatly biased negative orientation,
520 as well slower BV estimates. By increasing the model depth, there is an increased match between the
521 model's spectro-temporal configuration (represented by BV and orientation) and that of natural
522 statistics. Furthermore, extremely low or high sparsity values also result in over or under-estimating
523 statistics of natural calls; with 10% sparsity results in a great match with average statistics of the natural
524 calls.

525 Using the triple stacking network with 10% sparsity, we investigated the effect of the model non-
526 linearity on the same auditory characteristics of model neurons (Fig. 12B). Setting the non-linearity
527 parameter to 1.0 results in a fully linear processing which clearly produces in a mismatch between the
528 model and call characteristics. By increasing the degree of non-linearity (decreasing alpha), we note a
529 closer match between the two.

530 It should be noted that across all the different configurations of the model, all architectures were able
531 to converge (i.e. minimize the reconstruction error between the spectrogram of a given call sound and
532 its reconstruction using the model's latent space). Fig. 12C shows the average reconstruction error over
533 the 10 models for each parameter set. While all models successfully converge to reconstruct natural
534 calls and encode statistics of in the database, only a few configurations result in a reasonable match to
535 the spectro-temporal characteristics of model neurons. As a matter of fact, the model was not
536 constrained to match these properties in its latent space; it is merely trained to represent the call
537 spectrograms as faithfully as possible. This requirement has multiple plausible solutions, and only
538 certain configurations result in a close match with velocity and orientation characteristics of natural calls.

539

540 **3.5. Natural call representation with the biomimetic network**

541 So far, the results suggest that a deep nonlinear architecture with high sparsity to achieve an optimal
542 representation of the statistics of natural bat vocalizations is capable to replicate auditory characteristics
543 of the bat's midbrain. We next examined the implications of this mapping to facilitate discrimination of
544 the large variety in the call repertoire. A study revealed that tuning characteristics of bat IC neurons
545 differentially encode different sound categories in the bat vocalizations, specifically echolocation calls
546 and food-claiming FMB (frequency-modulated bout) social calls (Salles et al., 2020). We examined
547 whether the artificial network, trained simply to emulate natural statistics in the bat repertoire (without
548 knowledge of different sound classes) also yields distinct activations of these different groups. Fig. 13A
549 top replicates the response selectivity of biological IC neurons, showing a scatter plot of average

550 activation probabilities for each neuron in response to FMB calls (x-axis) vs. Echolocation (echo) calls (y-axis),
551 projected on the principal axis by PCA. The figure inset shows the original neural responses before
552 data projection. Fig. 13B-D depict a similar analysis of call selectivity for the mono, double and triple
553 artificial network, respectively. Note that each panel from B to D was produced by one network of 10-
554 models for example. The top panels show a scatter. Across the 3 network configurations, we note that
555 the mono stacking model induces mostly non-selective activation across its neural population (Fig. 13B)
556 while the double stacking model yields biased responses in favor of Echo calls (Fig. 13C). The triple
557 stacking model reveals a more balanced activation from Echolocation and FMB social call types (Fig. 13D)
558 that closely matches biological selectivity.

559 We extend the analysis of call selectivity in the artificial network to other classes of calls in the bat
560 repertoire. We evaluated discriminability across 8 types of calls using the Jensen-Shannon divergences
561 (JSDs) (Endres and Schindelin, 2003). Fig. 14 shows the results for various network depths, linearity and
562 sparsity for the calls in the database (clean) as well as with additional simulated additive noise with
563 decreasing signal-to-noise (SNR) ratios. The triple stacking model (with high sparsity and nonlinear
564 activation) produces the most discriminable responses, as well as more robust discrimination even in
565 presence of noise. Shallower architectures are clearly affected by presence of resulting in reduced
566 discriminability. Linear activations and low sparsity appear to also affect discriminability and robustness
567 to noise albeit not at the same rate. These results suggest that the optimal representation of call
568 statistics likely plays a role in facilitating the identification of different sound classes even in presence of
569 noise. Similarly, a study with guinea pigs has shown the robust discrimination in the responses to
570 communication sounds (Souffi et al., 2020). Such hypothesis aligns with earlier reports (Chechik et al.,
571 2006) but remains to be validated in the IC of the big brown bat. As reference, we computed JSD for the
572 two echo and FMB call classes (Fig. 14) for both artificial and biological neurons. Both measures reveal a
573 close agreement and high discriminability that far surpasses selectivity from shallower architectures.

574

575 **4. Discussion**

576 **The biomimetic artificial network provides a nonlinear response model of neural selectivity**

577 To examine the tuning of auditory neurons, each cell can be considered as a system with a mapping
578 function F that represents a relation between stimulus s and neural response r i.e. $r = F(s)$. While
579 characterizing the full system function may be theoretically or experimentally nearly impossible,
580 linearized models using STRF are often used to build a computational response model as $r(t) =$
581 $\int s(t, f) * h(t, f) df$ where t and f is respectively time and frequency index, $s(t, f)$ is spectro-temporal
582 representation for a stimulus, $*$ is a convolution operator, and $h(t, f)$ represents a spectro-temporal
583 receptive fields (STRF's) (Depireux et al., 2001; Elhilali et al., 2013; Machens et al., 2004; Fritz et al.,
584 2003). This model is often applied with reasonable success to predict neural responses to other sound
585 classes including conspecific vocalizations or other natural sounds. Although the linear model is a
586 reasonable approximation for mimicking neural responses in the brain, it is limited in its ability to inform
587 nonlinear transformations that are usually observed in between stimulus and response (Escabi and
588 Schreiner, 2002; Theunissen et al., 2000). One of the main advantages of including nonlinear activations
589 in a feed-forward propagation in the proposed neural network is that it implicitly incorporates the
590 effects of these nonlinear mappings in the propagation of activity throughout the network. Still, we are
591 able to evaluate the linearized portion of the response (via STRF's of artificial neurons) without explicitly

592 incorporating the nonlinear terms in the STRF model itself. This black-box approach to incorporate
593 complexities of neural mapping via deep neural networks opens the possibility to more intricate
594 readouts of the representation of artificial networks. We anticipate that such biomimetic artificial
595 network can be used to build a system mimicking the bat's ability for object shape recognition using its
596 bio-sonar.

597

598 **Midbrain responses are optimized to represent the statistics of natural calls in a bat's soundscape**

599 In this study, we explored the hypothesis that the bat's IC neurons are tuned to represent the FM
600 velocity and spectro-temporal structure of conspecific vocalizations. Evidence in support of this Sender-
601 Receiver matching has been previously reported in the pallid bat (Fuzessery, et al., 2006) and Mexican
602 free-tailed bat (Andoni et al., 2007), as well as other species such as zebra finches (Woolley et al., 2005)
603 (also see (Woolley and Portfors, 2013). Here, we report similar findings in the big brown bat, and
604 establish a close correspondence between acoustic characteristics of natural calls and tuning of spectro-
605 temporal receptive fields of IC neurons of the big brown bat. Going beyond this relationship, an artificial
606 network trained independently on these natural calls reveals tuning properties that not only conform
607 with spectro-temporal features of the calls (which they were trained on), but also unveils IC-like tuning
608 structure and complexity (e.g. separability) that the model was not specifically trained on (Fig. 10). This
609 result hints that the midbrain architecture gives rise to tuning configurations that leverage the spectro-
610 temporal richness of the bat's repertoire to not only represent these features with high fidelity but also
611 enable selective responses to discriminate between classes of natural calls.

612 The artificial network used in the current study shows that the neural encoding of an incoming stimulus
613 gives rise to a response across neural populations that enables it to faithfully reconstruct this stimulus,
614 revealing a high fidelity mapping without loss of information. While not explicitly happening in the brain,
615 this stimulus reconstruction from the internal latent space is the basis for training the artificial network
616 which yields emergent tuning that matches the biology. It is important to note that tuning properties of
617 artificial neurons were derived using moving ripples which invoke the principle of signal decomposition
618 by separating each conspecific call into a sum of ripples with different orientations, rates and phases, in
619 line with the Fourier theory of signal representation. While the network was never trained on these
620 ripples, its response to each ripple spectral motion pattern both in terms of magnitude and phase (both
621 needed for STRF reconstruction) suggest a quantitative correspondence with the downward-sweeping
622 signals that are prominent in the bat repertoire. It is also important to note that not all known coding
623 properties of the bat midbrain are represented in STRFs (Brimijoin and O'Neill, 2010) and that future
624 steps to test time varying response properties (such as an adaptation) would further validate the ability
625 of this network to replicate the biology of the bat IC (Lesica and Grothe, 2008; Rabinowitz et al., 2013;
626 Lohse et al., 2020).

627

628 **A deep architecture with sparsity is best suited to model the statistics of natural calls**

629 Varying the architecture of the network led to different latent spaces to represent the characteristics of
630 the database of natural calls. Specifically, changing the complexity of the network (in terms of depth),
631 sparsity and nonlinearity converged on different solutions for representing conspecific sounds. Under all

632 configurations, the networks were able to reconstruct the input spectrogram with minimal error
633 indicating that its latent space is sufficiently informative about the statistics in the training database (Fig.
634 12C). Nonetheless, only a specific configuration with high sparsity, nonlinearity and sufficient depth is
635 able to replicate biological tuning properties, giving insights into coding principles underlying
636 configuration of IC networks probed in this study. Naturally, while this investigation cannot rule out
637 other configurations that would also reveal a strong match to biology, it can eliminate parameters that
638 converge on solutions that are far from the biology (e.g. shallow networks, linear models). It is worth
639 noting that we were unable to train a quadruple stacking network to represent statistics in the database
640 so we are unable to comment on the extend to which an even deeper network may correlate with
641 biological tuning. The output of a 4th block could be missing spectro-temporal features due to over-
642 compression. This is an issue that could be explored using large input patches or modifying the pooling step.

643

644 **Tuning to conspecific natural sounds may underlie selective and robust encoding of auditory objects**

645 We note that directional selectivity to FM sweeps in biological and artificial neurons, results in high
646 discriminability between different classes of calls. Specifically, these results support the notion that by
647 having neural sub-population tuned to different subsets of spectro-temporal statistics, the network is
648 able to encode and differentially respond to different vocalizations and social or echolocation calls. This
649 discriminability is enhanced in the triple sparse and nonlinear network that best matches biological
650 tuning and much reduced in other network configurations despite the fact that these other models were
651 also successfully trained to represent the same natural statistics in the bat call repertoire. This variability
652 may stem from correlated behavior across the neural population which was previously shown to play an
653 important role in enhanced discriminability of vocalizations in the auditory midbrain (Schneider and
654 Woolley, 2010). This encoding selectivity remains fairly stable in presence of stationary ambient noise
655 suggesting that the high dimensional mapping encoding incoming natural calls results in a noise
656 invariant representation that is believed to start emerging at the level of the inferior colliculus and
657 further strengthen in auditory cortex (see, Willmore et al., 2014).

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783 **Figures and Tables**

784 Fig. 1 Overview of study foci. A database of natural calls from a colony of big brown bats is collected and
785 analyzed for its auditory characteristics. Shown in the figure is a distribution of FM velocities. Right:
786 Tuning characteristics of biological neurons from the big brown bat inferior colliculus are derived using
787 Spectro-Temporal Receptive Field (STRF) method, and properties of biological neurons are derived (e.g.
788 best velocity, BV). Shown in the figure is a brain slice identifying the location of the IC in the big brown
789 bat (from Salles et al., 2020). Left: Computational models with various configurations are examined and
790 emergent tuning properties of artificial networks are derived to compare against statistics of natural
791 calls as well as biological neurons.

792

793 Fig. 2 Example spectrograms of 8 bat calls in social call database. **A**, Echolocation (Echo). **B**, Frequency
794 modulated bout (FMB). **C**, Upward frequency modulated (UFM). **D**, Long frequency modulated (LFM). **E**,
795 Short frequency modulated (SFM). **F**, Chevron shaped (CS). **G**, Hook. **H**, Long-wave.}

796

797 Fig. 3 Ripple transfer function extraction. **A**, A subset of ripple stimuli. **B**, Input patch sequence
798 configuration from a ripple stimulus to a code vector for characterizing the network. **C**, Examples of
799 responses on each node (each element of the code vector), and definition of magnitude m and phase ϕ
800 in a ripple response. **D**, Magnitude and phase plots on one of nodes.}

801

802 Fig. 4 Convolutional layered autoencoder structure for biomimetic network. The flow denoted in black
803 shows a double stacking structure as a standard example. Based on this structure, a deeper structure
804 can be constructed by stacking more modules, on the other hand, a shallow structure is created by
805 removing a module on the top of the standard example.

806

807 Fig. 5 Operations using multi-scale filters. **A**, convolution using multi-scale filters. **B**, transposed
808 convolution using multi-scale filters.

809

810 Fig. 6 STRF calculation. **A**, expanded magnitude and phase matrices which are matching to Fig. 2D. **B**, 2-
811 Dimensional (above) and 3-Dimensional (bottom) representation of the STRF that is obtained by
812 performing 64 by 64 interpolation and Gaussian smoothing sequentially. In 2D representation, red area
813 represents excitation regions while blue represents inhibition regions.

814

815 Fig. 7 Descriptions for best velocity and orientation. **A**, magnitude plot. **B**, the result of Gaussian surface
816 fitting. The red ellipse represents Gaussian mean vector μ (center) and covariance matrix Σ (rotation),
817 the best velocity is defined by a slope of Gaussian mean vector and the orientation error is defined by an
818 angle difference between mean vector and covariance rotation.

819

820 Fig. 8 Example spectrograms of several types of calls monophonic cases for social communication (A-C),
821 echolocation (D-F), and polyphonic cases (G-H). Note the differences in frequency content, duration, and
822 sweep velocity. Note that peak frequency is represented onto each panel as the black dashed line.

823

824 Fig. 9 Examples for biological STRF and biomimetic STRF. **A**, biological STRFs obtained from bat's IC
825 neuron. **B**, biomimetic STRFs obtained from a triple stacking network with 10% sparsity. Note that red
826 and blue area show excitation and inhibition regions, respectively.

827

828 Fig. 10 Histogram of biological and biomimetic STRFs according to auditory characteristics. **A**, Best
829 velocity. **B**, Direction selectivity index. **C**, Orientation (The zero-mean is marked as the red line). **D**,
830 Inseparability.

831

832 Fig. 11 Analysis of best frequency in dataset, IC neurons, and artificial neurons. **A**, histogram of peak
833 frequencies in natural calls, the background grey line represents averaging spectrum envelop of natural
834 calls. **B**, BFs on IC neurons. **C**, BFs on artificial neurons.

835

836 Fig. 12 Best velocity and Orientation of biomimetic STRF's depending on network's configuration. **A**, for
837 the number of stacking modules and sparsity (0.2 lReLU). **B**, for nonlinearity (Triple stacking model with
838 10% sparsity). **C**, average reconstruction error over the 10 networks for each parameter set, blue and
839 red dashed lines are mean of the errors for all configurations at the beginning of training and the end of
840 the training, respectively.

841

842 Fig. 13 Selectivity to FMB vs. Echolocation call for; **A**, IC neurons (Salles et al., 2020), spike frequency was
843 calculated by dividing the number of spikes by total number of spikes starting 5 ms after stimulus onset.
844 The horizontal axis on the bottom was circularly shifted with zero-centered non-selective neurons. **B**,
845 mono-stacking model. **C**, double-stacking model. **D**, triple-stacking model.}

846

847 Fig. 14 Natural sound representation by biomimetic network in different SNR conditions

848

849 Table 1. Description of network parameters, midlevel feature maps, and input.

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