

Characterizing TES power noise for future single optical-phonon and infrared-photon detectors ^{EP}

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ABSTRACT

In this letter, we present the performance of a $100\ \mu\text{m} \times 400\ \mu\text{m} \times 40\ \text{nm}$ W Transition-Edge Sensor with a critical temperature of 40 mK. This device has a noise equivalent power of $1.5 \times 10^{-18}\ \text{W}/\sqrt{\text{Hz}}$, in a bandwidth of 2.6 kHz, indicating a resolution for Dirac delta energy depositions of $40 \pm 5\ \text{meV}$ (rms). The performance demonstrated by this device is a critical step toward developing a $\mathcal{O}(100)$ meV threshold athermal phonon detector for low-mass dark matter searches.

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As dark matter (DM) direct detection experiments probe lower masses, there is an increasing demand for sensors with excellent energy sensitivity. Several athermal phonon sensitive detector designs have been proposed using superconductors¹ or novel polar crystals^{2–5} as the detection medium. Additionally, experiments that use single infrared (IR) sensitive photonic sensors to read out low band gap scintillators or multi-layer optical haloscopes for both axion and dark photon DM have also been proposed.⁶

Each of these designs would ultimately require sensitivity to single optical-phonons or IR-photons, corresponding to energy thresholds of $\mathcal{O}(100)$ meV.^{1–3,6} Coherent neutrino scattering experiments have recently made progress using DM detector technology and are also interested in cryogenic detectors with very low thresholds.⁷ Transition-Edge Sensor (TES) based detector concepts have been successfully applied in DM searches,^{8–10} as well as IR and optical photon sensors.¹¹ The same concepts can also be used

in these new applications, as the necessary energy sensitivities can theoretically be achieved.^{1,2}

The energy resolution of a calorimeter can be estimated with an optimum filter (OF)^{12,13} from

$$\sigma_E^2 = \left[\varepsilon^2 \int_0^\infty \frac{d\omega}{2\pi} \frac{4|p(\omega)|^2}{S_P(\omega)} \right]^{-1}, \quad (1)$$

where $S_P(\omega)$ is the total (one-sided) power-referred noise spectrum, ε is the total phonon collection efficiency, and $p(\omega)$ is power-referred pulse shape defined as $p(\omega) = 1/(1 + j\omega\tau_{ph})$, with τ_{ph} the athermal phonon collection time of the detector. The resolution for a TES-based calorimeter is minimized when the noise is dominated by the intrinsic thermal fluctuation noise (TFN) between the TES and the bath.¹⁴ This noise can be written as

$$S_P(\omega) \approx 4k_B T_c^2 GF(T_c, T_B)(1 + \omega^2 \tau_c^2), \quad (2)$$

where k_B is the Boltzmann constant, T_c is the superconducting (SC) critical temperature, T_B is the temperature of the bath, G is the dominant thermal conductivity between the TES and the bath, and $F(T_c, T_B) \approx 1/2$ is a scale factor accounting for the nonequilibrium nature of the thermal conductance. The effective time constant¹⁵ in the strong electrothermal feedback zero inductance limit (also neglecting small effects from the resistance terms and the current sensitivity) can be approximated as $\tau \approx C\sqrt{2n}/(G\alpha)$, where α is the dimensionless temperature sensitivity, C is the heat capacity, and n is the thermal conduction power law exponent. Under this scenario, the integral in Eq. (1) becomes

$$\sigma_E^2 \approx \frac{1}{\varepsilon^2} 4k_B T_c^2 G F(T_c, T_B) (\tau_{ph} + \tau_-). \quad (3)$$

If the energy of an incident particle is absorbed directly by the TES, that is, $\tau_{ph} = 0$ and $\varepsilon = 1$, then the energy variance in Eq. (3) becomes

$$\sigma_E^2 \approx k_B T_c^2 \frac{C}{\alpha} \sqrt{\frac{n}{2}}. \quad (4)$$

For a metal in the low-temperature regime, the heat capacity scales with the volume of the TES (V_{TES}) and the temperature as $C(T) \propto V_{TES} T$, suggesting

$$\sigma_E^2 \propto V_{TES} T_c^3. \quad (5)$$

However, if operated as an athermal phonon sensor, specifically a quasiparticle-trap-assisted electrothermal-feedback transition-edge sensor (QET),¹⁶ the energy sensitivity dependence on T_c becomes even more important. The energy resolution is minimized when athermal phonons bounce in the crystal for times long compared to the characteristic time scale of the TES sensor (i.e., $\tau_- < \tau_{ph}$),^{1,13,17} as long as the surface athermal phonon down-conversion rate is negligible.¹⁸ In this case, the thermal conductance term is not canceled from Eq. (3). For low- T_c W films, the thermal conductance is dominated by electron-phonon decoupling, thus scaling as $G \propto V_{TES} T_c^{n-1}$ with $n = 5$, as confirmed by measurement described later in this letter. This implies that the baseline energy variance of the detector scales with the critical temperature as $\sigma_E^2 \propto T_c^6$, suggesting that a low- T_c device is ideal for single optical-phonon sensitivity.

A set of 4 W TESs were fabricated on a 525 μm thick $1 \times 1 \text{ cm}^2$ Si substrate (“chip”). The smallest of the TESs was 25 $\mu\text{m} \times 100 \mu\text{m}$

$\times 40 \text{ nm}$. Each subsequent TES increased in area by a factor of four, keeping an aspect ratio of 1:4 (width:length), which implies all the TESs have the same normal resistance (R_N). The TES mask design can be seen in the left panel of Fig. 1. Two sets of these chips were made, one with TESs of $T_c = 40 \text{ mK}$ and the other with TESs of $T_c = 68 \text{ mK}$. This letter focuses on the measurement and characterization of the low- T_c 100 $\mu\text{m} \times 400 \mu\text{m} \times 40 \text{ nm}$ TES (hereby referred to as simply “the TES”), but also presents characterization data from these other devices to elucidate scalings with T_c and volume. The utility of such devices for applications of photon detectors and athermal phonon sensors are also discussed.

The voltage-biased TES was studied at the SLAC National Accelerator Laboratory in a dilution refrigerator at a bath temperature of 15 mK. The Si chip was mounted to a copper plate with GE 7031 varnish. The current through the TES was measured with a custom DC Superconducting Quantum Interference Device (SQUID) array system with a noise floor of $\sim 4 \text{ pA}/\sqrt{\text{Hz}}$, fabricated for the SuperCDMS experiment, with a measured lower bound on the bandwidth of greater than 250 kHz. The SQUID array was read out by an amplifier similar to the one in Ref. 19.

Multiple measures were put in place to mitigate electromagnetic interference (EMI). Pi-filters with a cutoff frequency of 10 MHz were placed on all input and output lines to the refrigerator. Ferrite cable-chokes were placed around the signal readout cabling at 300 K, and the 4 K and 1 K cans were filled with broadband microwave-absorptive foam to suppress radio frequency (RF) radiation onto TESs. The outer vacuum chamber of the dilution refrigerator was surrounded by a high-permeability metal shield to suppress magnetic fields. These measures were the result of a systematic search of the system’s susceptibility to environmental noise, and they lowered the measured electrical noise by roughly an order of magnitude. Despite these efforts, an unknown parasitic noise source remained, which inhibited the smallest two low- T_c TESs from going through their SC transition.

To characterize the TES, IV sweeps were taken at various bath temperatures by measuring TES quiescent current (I_0) as a function of bias current (I_{Bias}),²⁰ with complex admittance data taken at each point in the IV curve.^{13,21} Data were also taken simultaneously with the largest low- T_c TES (TES2) on the same Si chip, biased at an operating resistance (R_0) of $\sim 40\%R_N$, in order to attempt to quantify the amount of remaining excess noise that coupled coherently to both

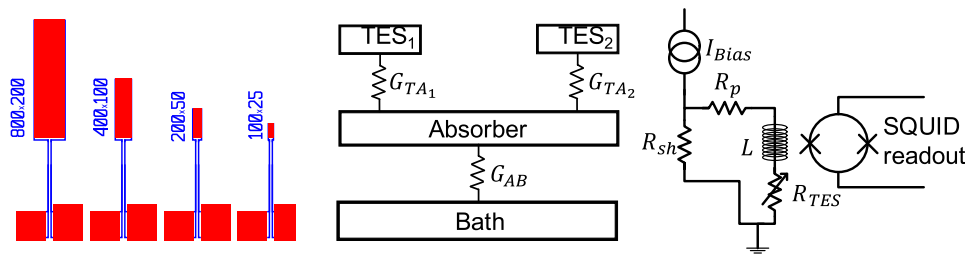


FIG. 1. Left: TES mask design. The W is shown in red, while the blue represents Al bias rails. The Al connects to the left and right sides of the TES. Middle: Thermal model for experimental setup. For simplicity, only two TESs are shown in the model. Right: Electrical circuit. R_{sh} is a shunt resistor that turns the current source (I_{Bias}) into a voltage bias. Any parasitic resistance on the shunt side of the bias circuit is absorbed into the value used for R_{sh} in this analysis. R_p is the parasitic resistance on the TES side of the bias circuit. L is the inductance in the TES line. R_{TES} is the TES resistance, which takes on a value of R_0 when in transition and takes on a value of R_N when its temperature is above T_c .

TABLE I. Various calculated parameters of the TES. R_{\square} or "R-square" is the sheet resistance of the W film.

R_{sh} (m Ω)	R_p (m Ω)	R_N (m Ω)	R_{\square} (Ω)	P_0 (fW)	G_{AB} (nJ/K)	G_{TA} (pJ/K)	T_c (mK)	T_B (mK)	T_{ℓ} (mK)	n
5.0 ± 0.5	5.8 ± 0.6	640 ± 65	2.56 ± 0.26	31 ± 2	1.6 ± 0.1	4.0 ± 0.4	40 ± 1	15 ± 1	37 ± 2	5

TES channels. From the IV sweep at each temperature, both the DC offset from the SQUID and any systematic offset in I_{Bias} were corrected for using the normal and SC regions of the data. After this correction, the parasitic resistance in the TES circuit (R_p), the normal state resistance, the TES resistance in transition, and the quiescent bias power (P_0) were calculated (see the right panel of Fig. 1 for the circuit diagram).

Since the Si chip contained multiple TESs, the thermal conductance between the chip and the bath (G_{AB}) was measured by using one as a heater and one as a thermometer. The knowledge of G_{AB} allowed us to infer the temperature of the Si chip (T_A) from a measurement of T_B . See the middle panel of Fig. 1 for the thermal diagram of the setup. Measuring P_0 as a function of temperature from the IV sweeps, the thermal conductance between the TES and the Si substrate (G_{TA}), T_c , and n were fit to a power law,²² confirming our $n = 5$ assumption. We measured that G_{AB} was roughly three orders of magnitude larger than G_{TA} , meaning that T_A was effectively equal to T_B , and the system could be modeled as a single thermal conductance between the TES and the bath. The characteristics of the TES system from the IV data are shown in Table I.

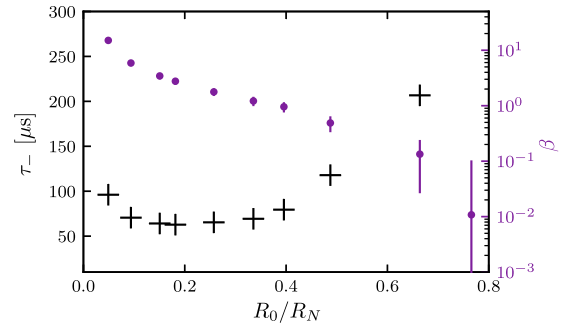
For each point in transition, a maximum likelihood fit of the complex admittance was done using the standard small-signal current response of a TES,¹⁴

$$Z(\omega) \equiv R_{sh} + R_p + j\omega L + Z_{TES}(\omega),$$

$$Z_{TES}(\omega) \equiv R_0(1 + \beta) + \frac{R_0 \mathcal{L}}{1 - \mathcal{L}} \frac{2 + \beta}{1 + j\omega \frac{\tau}{1 - \mathcal{L}}}. \quad (6)$$

In this fit, L , R_0 , R_p , R_{sh} ,²³ β , τ , and \mathcal{L} are all free parameters. L is the inductance in the TES bias circuit, β is the dimensionless current sensitivity, τ is the natural thermal time constant, and \mathcal{L} is the loop gain. We include the estimates from the IV data of R_0 , R_p , and R_{sh} as priors in the fit. Additionally, we include a prior on L , measured from the SC complex admittance data. The TES response times can also be measured from the complex admittance data, defined as the rise and fall times of the TES response from a delta function impulse (τ_+ and τ_- , respectively).¹⁴ Best fit values of β and τ_- are shown in Fig. 2, while a typical complex impedance curve can be seen in Fig. 3.

The normal-state noise was used to estimate the SQUID and amplifier noise, once the Johnson noise component of the TES at R_N was subtracted out. The effective load resistance temperature²⁴ was estimated from the SC noise spectrum, resulting in $T_{\ell} \approx 37$ mK, which was used to estimate the Johnson noise from R_{sh} and R_p . The TFN and TES Johnson noise components of the system were calculated as defined in the standard small-signal noise model,¹⁴ using the complex admittance fit parameters. The measured power spectral density (PSD), referenced to TES current, of the device in transition was converted into the noise equivalent power (NEP) with the

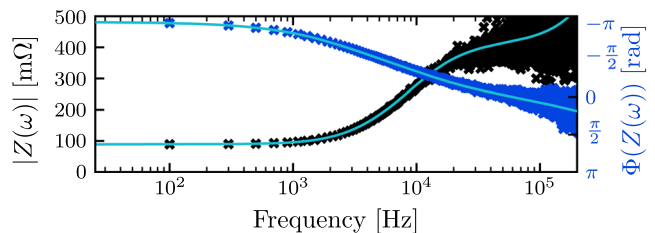
**FIG. 2.** Fitted values for β (purple dots) and effective electrothermal TES response time τ_- (black crosses) as a function of TES resistance.

power-to-current transfer function,¹⁴

$$\frac{\partial I}{\partial P}(\omega) = \left[I_0 \left(1 - \frac{1}{\mathcal{L}} \right) \left(1 + j\omega \frac{\tau}{1 - \mathcal{L}} \right) Z(\omega) \right]^{-1}, \quad (7)$$

where $Z(\omega)$ is defined in Eq. (6). A comparison of the noise model to the derived NEP for a typical operating point in transition is shown in Fig. 4.

From the derived NEP, the energy resolution of a Dirac delta impulse of energy directly into the TES was estimated using Eq. (1), with $\varepsilon = 1$ and $\tau_{ph} = 0$. It can be seen in the upper panel of Fig. 5 that when the TES is operated at less than $\sim 15\% R_N$, the estimated resolution of the collected energy is $\sigma_E = 40 \pm 5$ meV. At this point in the transition, the sensor has an NEP of 1.5×10^{-18} W/ $\sqrt{\text{Hz}}$ in a bandwidth of 2.6 kHz. This resolution represents the lower limit of the performance of this sensor given the measured noise, operated as either a photon or an athermal phonon sensor. In the case of the athermal phonon sensor, there would be an additional efficiency factor based on the design of the detector.

**FIG. 3.** A typical complex impedance curve for the TES in transition for $R_0 \approx 15\% R_N$. The measured magnitude and the phase of the complex impedance are shown in black and blue, respectively. In cyan, the complex impedance derived from the maximum likelihood fitting routine is shown.

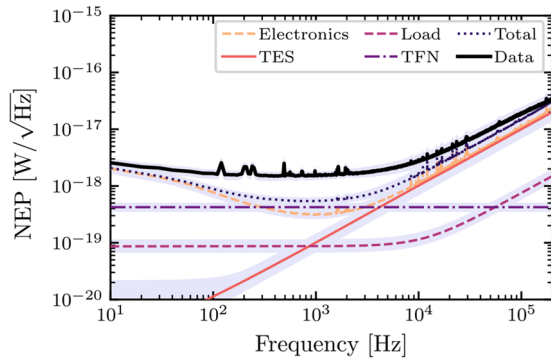


FIG. 4. Modeled noise components: TES Johnson noise (orange solid), load resistor Johnson noise (red dashed), electronics noise (yellow dashed), thermal fluctuation noise (purple alternating dashes and dots), and total modeled noise (purple dots) compared with the derived NEP (black solid). The noise model and NEP are shown for $R_0 \approx 15\%R_N$. The shaded regions represent the 95% confidence intervals.

It is evident from Fig. 4 that the NEP is elevated from the theoretical expectation across the full frequency spectrum. We split the excess noise into two categories. Noise that scales with the complex admittance and is present when the TES is biased in its normal or SC state, we call “voltage-coupled,” e.g., inductively coupled electromagnetic signals (EMF). Noise that is only seen when the TES is in transition is referred to as “power-coupled,” e.g., IR photons radiating onto the device. The excess voltage-coupled noise (S_{SC^*}) can be modeled by scaling the SC power spectral density (PSD) by the complex admittance transfer function when the TES is in transition via Eq. (8). This modeled noise can then be subtracted from the transition state PSD in quadrature,

$$S_{SC^*}(\omega) = S_{SC}(\omega) \frac{|[Z(\omega)]_{R_0}|^2}{|[Z(\omega)]_{R_0 \rightarrow 0}|^2}. \quad (8)$$

We expect power-coupled noise from an environmental origin to couple coherently to each TES on the same Si chip, though we have seen evidence of power-coupled noise generated by the

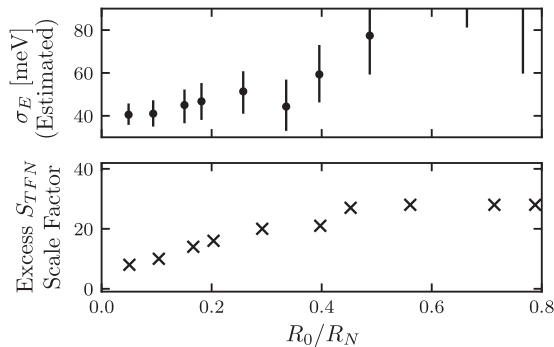


FIG. 5. Upper: Estimated energy resolution (from data) throughout the SC transition. Lower: Scale factor needed to increase S_{TFN} to make the noise model match the measured PSD.

Ethernet chip on our warm electronics to have significantly different couplings to different electronic channels. Because we acquired data simultaneously on TES2, we can determine the correlated and uncorrelated components of the noise by using the cross spectral density (CSD).^{21,25} The scaled SC noise PSD and the correlated part of the CSD are plotted with the measured PSD in Fig. 6 for $R_0 \approx 15\%R_N$. The two noise sources can explain the peaks in the noise spectrum but cannot explain the overall elevated noise level.

To investigate the hypothesis of the excess noise being explained by IR photons radiating onto the TES structure, we modeled this system by multiplying the TFN by a scalar in order to make the total noise model match the NEP. This scale factor is shown in the lower panel of Fig. 5. The fact that this scale factor monotonically increases with R_0 implies that this mechanism is not a dominant source of excess noise, as it should be independent of the TES operational bias point.

We ruled out the possibility of the excess noise being due to multiple thermal poles,^{26,27} as none of these models were able to explain the observed noise spectra. This is also evident by noting the lack of additional poles in the complex impedance in Fig. 3.

The fact that the two smallest low- T_c TESs (the most sensitive to parasitic power noise) were not able to go through their SC

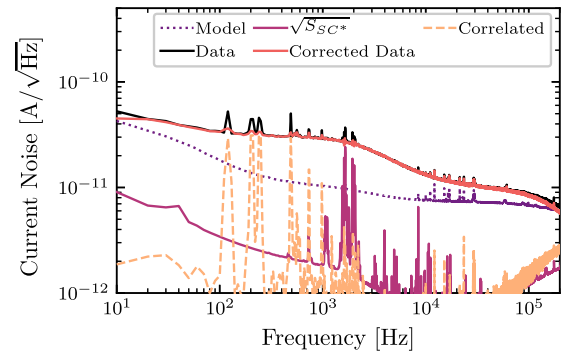


FIG. 6. Measured noise (black solid), modeled voltage-coupled noise (purple solid), correlated noise (yellow dashed), measured noise with voltage-coupled and correlated components subtracted (orange solid), and theoretical noise model (purple dots) shown for $R_0 \approx 15\%R_N$. The environmental noise model explains the peaks in the measured spectrum, but there is still a discrepancy between the environmental-noise-corrected data and the noise model.

TABLE II. Energy resolution estimates for 68 mK T_c TESs compared to the 40 mK T_c TES described in this work.

T_c (mK)	TES dimensions ($\mu\text{m} \times \mu\text{m} \times \text{nm}$)	σ_E (meV) estimated	σ_E^a (meV) predicted using Eq. (5)
40	$100 \times 400 \times 40$	40 ± 5	N/A
68	$50 \times 200 \times 40$	44 ± 5	44 ± 5
68	$100 \times 400 \times 40$	104 ± 10	89 ± 11

^aThe resolution expected from a hypothetical device (with the same physical properties) by scaling the resolution of the low- T_c TES (σ_1) using Eq. (5), i.e., $\sigma_x = \sigma_1 \sqrt{V_x T_{c,x}^3 / V_1 T_{c,1}^3}$.

TABLE III. Performance of state-of-the-art TES single photon calorimeters/bolometers.

TES	T_c (mK)	V_{TES} (μm^3)	σ_E (meV)	$\frac{\sigma_E}{\sqrt{V_{\text{TES}}}} \left[\frac{\text{meV}}{\mu\text{m}^{3/2}} \right]$	Method
W ²⁸	125	21.88	120	25.7	Measured
Ti ²⁹	50	0.13	47	128.2	Measured
MoCu ³⁰	110.6	2000	295.4	6.6	Estimated ^a
TiAu ³¹	106	90	48	16	Measured
TiAu ³²	90	202.5	~23	1.6	Estimated ^a
W (this)	40	1600	40	1	Estimated

^aThe energy resolution is estimated with Eq. (1) from the given NEP and sensor bandwidth.

transition, suggests that a nonnegligible amount of the excess noise is environmental in origin. However, given the previous discussion, this leaves open the possibility that some of this excess noise is intrinsic to the TESs.

We compare the estimated energy resolution of the TES to the high- T_c TESs, using the same analysis techniques, in Table II. The high- T_c TESs also observed a similar amount of excess noise. Despite the elevated noise seen on both sets of TESs, the resolution scaling with volume and T_c from Eq. (5) still approximately holds. We note that we do not compare the energy resolutions using the expected scaling relation for athermal phonon sensors because of its dependence on both the substrate material and the QET geometry.

With an estimated energy resolution of 40 ± 5 meV (rms), this device has comparable energy sensitivity to world leading optical and near-IR TESs but with a volume that is much larger due to its low- T_c (see Table III). It has immediate use as a photon detector in optical haloscope applications.⁶ Furthermore, its large volume suggests that significant improvements in sensitivity can be made in short order; a $20 \mu\text{m} \times 20 \mu\text{m} \times 40 \text{ nm}$ TES made from the same W film would be expected to have 4 meV (rms) sensitivity, provided that we can reduce the observed excess noise and the volume scaling in Eq. (5) continues to hold.

For athermal phonon sensor applications,^{1–5} the expected resolution is also impacted by the athermal phonon collection efficiency, which is typically $>20\%$ in modern designs.³³ Thus, small-volume crystal detectors ($\sim 1 \text{ cm}^3$) should be able to achieve sub-eV triggered energy thresholds. Though such devices could not achieve the ultimate goal of single optical-phonon sensitivity, they could achieve the intermediate goal of sensitivity to single ionization excitations in semiconductors without E-field amplification mechanisms,^{9,34} which have historically correlated with spurious dark counts. A decrease in TES volume and T_c , along with concomitant improvements in environmental noise mitigation and the use of crystals with very low athermal phonon surface down-conversion, would additionally be necessary to achieve optical phonon sensitivity. As we expect the energy variance to go as T_c^6 in this application, the benefit of lower T_c should be significant.

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DATA AVAILABILITY

The main findings of this letter can be replicated from the presented data, but the full data that support the findings of this study are available from the corresponding author upon reasonable request.

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- ²⁰We use the term “IV” even though we are applying a bias current, as the voltage and current are related by the shunt resistor: $V_{\text{Bias}} = I_{\text{Bias}} R_{\text{sh}}$.
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