# Stochastic FDTD Modeling of Propagation Loss due to Random Surface Roughness in Sidewalls of Optical Interconnects

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Abstract—The dielectric waveguide (WG) is a building block of high-speed and high-bandwidtl opto-electronic interconnect networks that operate i quency regime. At the interface of Si/SiO2 dielectr with width above  $w=2.5~\mu\mathrm{m}$  and anisotropic surfa transverse electric (TE) mode surface wave pro experience a loss of approximately  $\alpha = 2$  dB/ propagation losses increase rapidly to near  $\alpha$ as the width decreases to w = 500 nm, due interaction of surface waves and sidewall surfa that exhibits random distribution inherent to the n process. Previous works have developed analyti for computing propagation loss in a single dielect exhibiting random roughness. More recent works r dB/cm noting the non-trivial estimation errors in 1 retical formulations which relied on planar approx highlight the discrepancy in planar approximation Volume Current Method.

A challenge that remains in the path of design optical interconnects is the dearth of efficient tic computational electromagnetic (CEM) models tightly coupled optical dielectric waveguides that characterize propagation loss due to random surface roughness in waveguide sidewalls. Through a series of theoretical and numerical experiments developed in the method of finite-difference time-domain (FDTD), we aim to develop stochastic CEM models to quantify propagation loss and facilitate signal & power integrity modeling & simulation of arbitrary configurations of multiple tightly-coupled waveguides, and to gain further insights into loss mechanisms due to random surface roughness in optical interconnects.

### I. INTRODUCTION

A challenge in the path of designing nanoscale optical interconnects is the dearth of accurate and efficient 3-D computational electromagnetic models [1]. The state-of-the-art work by [2] reports  $\alpha=0.4$  dB/cm and highlights the nontrivial estimation errors in previous theoretical formulation [3], [4] which rely on planar approximations. The work by [2] highlights the discrepancy in planar approximations vs. the 3-D Volume Current Method (VCM) [5]–[7] which was initially developed to model symmetric structures embedded in a uniform dielectric constant.

In this paper, we verify the FDTD simulation space by correlating against known analytic solutions for wave impedance  $Z_w$  from [8]. Additionally, we replicate data from [9] for propagation loss due to surface roughness in dielectric waveguide

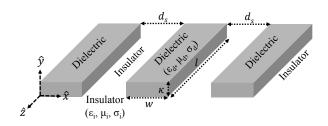


Fig. 1. Three parallel dielectric waveguides, where  $d_s$  is the edge-to-edge distance between two adjacent waveguides.

#### II. FORMULATION

# A. 2-D Analytic Approximation of $Z_w$

The 2-D models of the dielectric waveguide developed by [8], [10] assume a transverse electric (TE) mode of propagation along the waveguide length (i.e.,  $TE^z$  mode, transverse electric to  $\hat{z}$ ), and x-invariance along the waveguide width (i.e.,  $\frac{\partial}{\partial x} \Rightarrow 0$ ) which implies an infinite width for the waveguide.

Looking from free-space insulator down towards the dielectric slab, the TE mode surface wave impedance  $Z_w^{-y0}$  may be defined by (1), and obtained by solving two non-linear equations (2) simultaneously [8].

$$Z_w^{-y0} = E_x^{0+} / H_z^{0+} = -j \frac{\omega \mu_0}{\alpha_{y0}},$$
 (1)

where, the angular frequency  $\omega=2\pi f$  (rad/s), the cyclic frequency f (Hz),  $\jmath=\sqrt{-1},\,\alpha_{y0}$  is the attenuation constant in free-space along  $\hat{y}$ , and  $\{E_x^{0+},H_z^{0+}\}$  are the incident {electric, magnetic} field vector components along  $\{\hat{x},\,\hat{z}\}$ ; respectively.

$$(\mu_0/\mu_d)(\beta_{yd}h)\tan(\beta_{yd}h) = \alpha_{y0}h,$$
  
 $(\alpha_{y0}h)^2 + (\beta_{yd}h)^2 = a^2,$  (2)

where,  $a = \omega h \sqrt{\mu_0 \epsilon_0 (\mu_{r_d} \epsilon_{r_d} - 1)}$ , and  $\beta_{yd}$  is the phase constant in dielectric along  $\hat{y}$ .

The above model is inadequate for evaluating effects of finite width on propagation loss due to wall surface roughness; however, it serves its purpose here to verify our 2-D/3-D FDTD models via correlation of surface wave impedance  $Z_w$  in ideal waveguides; as shown in Fig. 2.

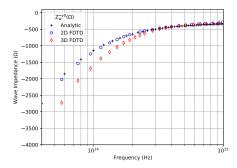


Fig. 2. Correlation of wave impedance across 2-D analytic, 2-D FDTD, and 3-D FDTD.

## B. 2-D Analytic Model of Propagation Loss due to Surface Roughness

Assuming surface roughness f(z) exhibits an exponential distribution, the auto-correlation function  $R(u) = \sigma^2 e^{-|u|/L_c}$ , where  $\sigma$  is the mean squared deviation of the roughness, and L is the correlation length. Figure 3 depicts random surface

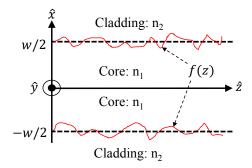


Fig. 3. Depiction of surface roughness f(z) on waveguide walls, along waveguide length 2l [3].

Figure 4 depicts the propagation loss as a function of waveguide width, assuming infinite height.  $\alpha_0$  shows the results from Fig. 2 in [9],  $\alpha_1$  is based on  $\beta$  from [11] based on the solution of (2), and  $\alpha_2$  is based on  $\beta$  from the *effective index method* [12]. The  $1/d^2$  curve is shown as reference for comparing losses. Figure 5 depicts the propagation loss as a function of both  $\sigma$  and  $L_c$ . The contours are in dB/cm and match Fig. 4 in [9].

## III. CONCLUSION

Our 2-D/3-D FDTD models of ideal dielectric waveguides in the THz regime were validated by correlation against analytic solutions. We also replicated estimates of propagation loss, due to random surface roughness, based on 2-D planar

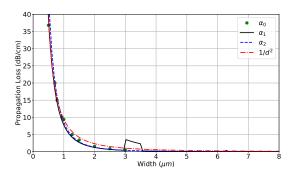


Fig. 4. Attenuation coefficient  $\alpha$  vs. waveguide width.

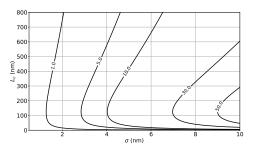


Fig. 5.  $\alpha$  vs.  $L_c$  and  $\sigma$ .

approximations developed by previous investigators. Currently, work is in-progress to compute the propagation loss via 2-D/3-D FDTD for comparison against previously published data from experimental measurements and numerical simulations.

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