

1 Modeled Three-Dimensional Currents and Eddies on an 2 Alongshore-Variable Barred Beach

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8 **Key Points:**

- 9 • Trends in SWASH-simulated nearshore circulation patterns and magnitudes on an
10 alongshore-variable barred beach are similar to observations
- 11 • Small length-scale eddies are intensified by wave directional spread, and large eddies
12 are enhanced by alongshore bathymetric variability
- 13 • Eddy length scales and low-frequency currents are weakly vertically-dependent in the
14 outer surf zone and depth-uniform in shallower water

15 **Abstract**

16 Circulation in the nearshore region, which is critical for material transport along the coast
 17 and between the surf zone and the inner shelf, includes strong vortical motions. The hori-
 18 zontal length scales and vertical structure associated with vortical motions are not well doc-
 19 umented on alongshore-variable beaches. Here, a three-dimensional phase-resolving numer-
 20 ical model, Simulating WAves till SHore (SWASH), is compared with surfzone waves and
 21 flows on a barred beach, and is used to investigate surfzone eddies. Model simulations with
 22 measured bathymetry reproduce trends in the mean surfzone circulation patterns, includ-
 23 ing alongshore currents and rip current circulation cells observed for offshore wave heights
 24 from 0.5 to 2.0 m and incident wave directions from 0 to 15° relative to shore normal. The
 25 length scales of simulated eddies, quantified using the alongshore wavenumber spectra of
 26 vertical vorticity, suggest that increasing wave directional spread intensifies small-scale ed-
 27 dies ($O(10)$ m). Simulations with bathymetric variability ranging from alongshore uniform
 28 to highly alongshore variable indicate that large-scale eddies ($O(100)$ m) may be enhanced
 29 by surfzone bathymetric variability, whereas small-scale eddies ($O(10)$ m) are less depen-
 30 dent on bathymetric variability. The simulated vertical dependence of the magnitude and
 31 mean length scale (centroid) of the alongshore wavenumber spectra of vertical vorticity and
 32 very low-frequency ($f \approx 0.005$ Hz) currents is weak in the outer surf zone, and decreases
 33 toward the shoreline. The vertical dependence in the simulations may be affected by the ver-
 34 tical structure of turbulence, mean shear, and bottom boundary layer dynamics.

35 **Plain Language Summary**

36 The nearshore region includes the surf zone, where waves break, and the inner shelf, which
 37 extends several km offshore from the surf zone. Within this region, currents transport con-
 38 taminants, sediments, and larvae along the coast and between the beach and the shelf. Nearshore
 39 eddies are rotational currents that fluctuate at timescales longer than individual waves and
 40 shorter than mean hourly currents, and are important to mixing and transport. Here, a three-
 41 dimensional numerical model simulates observed waves and flow patterns on a natural beach
 42 near Duck, NC with highly variable seafloor elevations (*e.g.*, bumps and holes). Estimates
 43 of the alongshore (parallel to the coastline) length of simulated eddies suggest that large ed-
 44 dies are enhanced by higher variability in the seafloor, whereas the intensity of small eddies
 45 increases when waves enter the surf zone with larger directional spread (from multiple direc-

46 tions). The structure and strength of nearshore eddies over the water column is shown to vary
 47 across the surf zone.

48 **1 Introduction**

49 The nearshore region consists of the surf zone, extending from the shoreline to the
 50 seaward limit of depth-induced wave breaking, and the inner shelf, a region with overlap-
 51 ping surface and bottom boundary layers on the continental shelf offshore of the surf zone
 52 [Lentz and Fewings, 2012]. Quantifying circulation dynamics and the transport of material
 53 (e.g., contaminants, sediments, and larvae) in the nearshore is critical given the concentration
 54 of recreational, commercial, and ecosystem resources in this region [Boehm *et al.*, 2017].
 55 Nearshore currents may dilute or concentrate pollutants and pathogens that cause gastroin-
 56 testinal infections and require beach closures [Stoner and Dorfman, 2007], and excess nu-
 57 trient supply from terrestrial runoff may lead to eutrophication in coastal zones, creating hy-
 58 poxic conditions that threaten benthic organisms and ecosystem health [Boehm *et al.*, 2016].
 59 In addition, species inhabiting the nearshore (e.g., intertidal invertebrate gametes) exploit
 60 cross-shore circulation for recruitment and settlement [Pineda *et al.*, 2007; Shanks *et al.*,
 61 2010]. A comprehensive understanding of nearshore dynamics is necessary to maintain pub-
 62 lic safety and reduce anthropogenic stresses on ecosystems.

63 Surfzone circulation is the result of complex interactions between surface waves, bathy-
 64 metric irregularities, and bottom boundary layer dynamics. Mean cross-shore velocities are
 65 characterized by a balance between radiation-stress gradients, barotropic-pressure gradients,
 66 and a weaker contribution from bottom stress, resulting in wave setup and an offshore near-
 67 bed return current [*i.e.*, ‘undertow’, Longuet-Higgins and Stewart, 1964; Bowen *et al.*, 1968;
 68 Stive and Wind, 1982; Raubenheimer *et al.*, 2001]. Wave-induced mean alongshore currents
 69 result from alongshore barotropic-pressure gradients [Apotsos *et al.*, 2008; Hansen *et al.*,
 70 2015] and cross-shore gradients of the off-diagonal component of the radiation-stress ten-
 71 sor [Longuet-Higgins, 1970; Feddersen *et al.*, 1998; Garcez-Faria *et al.*, 1998], primarily
 72 balanced by bottom stress [Visser, 1986; Simons *et al.*, 1992; Reniers *et al.*, 2004a]. Wave
 73 breaking over alongshore bathymetric variations drives rip currents and meandering along-
 74 shore currents, including cell-like circulation patterns [MacMahan *et al.*, 2006; Dalrymple
 75 *et al.*, 2011; Castelle *et al.*, 2016; Moulton *et al.*, 2017].

76 The vertical structure of surfzone currents depends on the forces associated with sur-
 77 face wave breaking, bottom friction, and interaction with the three-dimensional circulation
 78 [Putrevu *et al.*, 1995; MacMahan *et al.*, 2004], and is altered by the vertical distribution of
 79 turbulence in the water column, which depends on the breaking wave energy and bed rough-
 80 ness [Feddersen and Trowbridge, 2005; Feddersen, 2012; Henderson *et al.*, 2017]. Field and
 81 numerical modeling studies have investigated the vertical profile of undertow [Garcez-Faria
 82 *et al.*, 1998] and of mean alongshore currents [Garcez-Faria *et al.*, 2000; Reniers *et al.*,
 83 2004a]. However, the three-dimensional structure of surfzone velocities at timescales longer
 84 than those of wind waves (*e.g.*, surfzone eddies) and their implications for material exchange
 85 are not understood well.

86 Surfzone eddy activity contributes to dispersion and mixing, thus affecting the trans-
 87 port of material along the coast and between the surf zone and the inner shelf [Spydell and
 88 Feddersen, 2009; Clark *et al.*, 2010, 2011; Suanda and Feddersen, 2015]. Very low-frequency
 89 (VLF) vortical motions at timescales greater than 250 s (approximately $f < 0.004$ Hz, where
 90 f is frequency), longer than infragravity timescales ($0.004 < f < 0.040$ Hz), may be gener-
 91 ated by shear instabilities [Bowen and Holman, 1989; Oltman-Shay *et al.*, 1989; Allen *et al.*,
 92 1996] and wave-breaking induced vorticity [Peregrine, 1998; Haller *et al.*, 1999]. Shear in-
 93 stabilities in an obliquely incident wave-driven alongshore current have been observed with
 94 length scales up to several hundred meters [Oltman-Shay *et al.*, 1989]. Wave-group driven
 95 alongshore radiation stress gradients from alongshore wave-breaking variability may con-
 96 tribute to surfzone eddy generation with length scales on the order (O) of 100 m [Haller
 97 *et al.*, 1999; Reniers *et al.*, 2004b; Long and Özkan Haller, 2009]. As a result of alongshore
 98 gradients in wave dissipation, short-crested breaking waves generate vorticity with length
 99 scales $O(10)$ m [Peregrine, 1998; Clark *et al.*, 2012], which are hypothesized to coalesce to
 100 larger scales $O(100)$ m due to an inverse energy cascade [Kraichnan, 1967; Spydell and Fed-
 101 dersen, 2009; Boffetta and Ecke, 2012; Elgar and Raubenheimer, 2020]. The length scales
 102 associated with vortical motions generated by both shear instabilities and wave breaking have
 103 been explored for depth-integrated velocities on alongshore-uniform beaches [Spydell and
 104 Feddersen, 2009; Feddersen *et al.*, 2011; Feddersen, 2014; Kumar and Feddersen, 2017]
 105 and an alongshore-varying beach [O'Dea *et al.*, 2020], but have not been explored for depth-
 106 varying velocities on beaches with complex bathymetry.

107 Surfzone vortical motions, often assumed to be depth-uniform, usually have been mea-
 108 sured at a single elevation with a horizontally spaced sensor array. However, two recent stud-

109 ies on a barred beach measured low-frequency motions with vertically stacked electromag-
 110 netic current sensors [Lippmann *et al.*, 2016] and acoustic Doppler profilers [Henderson
 111 *et al.*, 2017]. These studies found that low-frequency cross- and alongshore velocities are
 112 weakly vertically dependent in the outer surf zone [Lippmann *et al.*, 2016; Henderson *et al.*,
 113 2017]. Analytic solutions based on bottom boundary layer theory include complex vertical
 114 structure of low-frequency motions in the presence of a horizontally sheared alongshore cur-
 115 rent [Lippmann and Bowen, 2016]. Although these studies have established that eddies in the
 116 outer surf zone have some vertical variability, further investigation is necessary to understand
 117 the vertical dependence of VLF currents for varying beach profiles and wave conditions.

118 Numerical modeling has been used to investigate the three-dimensionality of surf-
 119 zone vortical motions. Phase-averaged models, which simulate the evolution of the wave
 120 energy spectrum, are skillful at reproducing wave-induced dynamics, including rip-current
 121 circulation, alongshore currents, and wave setup [Reniers *et al.*, 2004a; Uchiyama *et al.*,
 122 2010; Kumar *et al.*, 2012]. Studies using three-dimensional phase-averaged model simula-
 123 tions indicate that vertical shear instabilities modify depth-dependent currents due to disper-
 124 sive mixing [Newberger and Allen, 2007a,b], and that VLF motions are excited on complex
 125 bathymetry [Uchiyama *et al.*, 2017]. However, the parameterizations of wave-induced vor-
 126 ticity associated with energy dissipation from short-crested wave breaking used in phase-
 127 averaged models have not been tested extensively.

128 Coupled ocean-circulation and phase-averaged wave models (*e.g.*, COAWST) simulate
 129 vertically varying surfzone circulation [Warner *et al.*, 2010; Kumar *et al.*, 2012], and can be
 130 one-way coupled with depth-averaged phase-resolving models (*e.g.*, funwaveC) to allow for
 131 the investigation of three-dimensional eddies resulting from bulk vorticity injection similar
 132 to that resulting from short-crested wave breaking [Kumar and Feddersen, 2017]. However,
 133 wave-forced rotational flows associated with eddies may be aliased as a result of smaller time
 134 steps in the phase-resolving simulations [Kumar and Feddersen, 2017]. In addition, two-way
 135 coupled wave-current interactions between three-dimensional eddies and propagating waves
 136 are not included.

137 Phase-resolving Boussinesq models (*e.g.*, FUNWAVE-TVD and funwaveC), which
 138 simulate individual wave propagation, have been used to study surfzone vorticity dynamics,
 139 including finite-crested wave-breaking eddy generation [Feddersen, 2014; Hally-Rosendahl
 140 and Feddersen, 2016]. These models are depth integrated, and thus do not resolve eddy

141 vertical variability. Three-dimensional phase-resolving non-hydrostatic numerical models,
 142 such as Simulating WAves til SHore (SWASH) and NHWAVE, contain the physics needed
 143 to simulate three-dimensional circulation and vorticity dynamics, including wave-forced
 144 eddy generation [Zijlema *et al.*, 2011; Derakhti *et al.*, 2016]. SWASH has been used to study
 145 nearshore wave breaking, infragravity wave dynamics, nonlinear infragravity-wave interac-
 146 tions, run-up oscillations, and nonlinear wave-dynamics [Rijnsdorp *et al.*, 2012, 2014; Smit
 147 *et al.*, 2013; Ruju *et al.*, 2014; Smit *et al.*, 2014; de Bakker *et al.*, 2016]. Although SWASH
 148 has skill simulating wave-induced flows measured in the laboratory, including the undertow
 149 profile and alongshore currents [Rijnsdorp *et al.*, 2017], the accuracy of SWASH-simulated
 150 surfzone circulation on an alongshore-variable beach has not been tested.

151 Here, SWASH is used to simulate three-dimensional wave propagation and circulation
 152 on a beach with complex alongshore-varying bathymetry. The field experiment and model
 153 setup are described in section 2, and the results comparing the observed with the simulated
 154 wave statistics and circulation patterns are presented in section 3. Additionally, the relative
 155 roles of alongshore bathymetric variability and directional spread in the horizontal and depth
 156 variability of length scales of the simulated eddies, and of the vertical structure of VLF hori-
 157 zontal velocities, are presented in section 3. The physical processes influencing the horizon-
 158 tal and depth variability of surfzone eddies and VLF currents are discussed in section 4. The
 159 results are summarized in section 5.

160 2 Methods

161 2.1 Field Experiment

162 Field observations were collected on an alongshore-inhomogeneous barred beach near
 163 Duck, North Carolina at the United States Army Corps of Engineers Field Research Facility
 164 (FRF, <http://frf.usace.army.mil/frf.shtml>) as part of the BathyDuck-2015 Experiment, a large
 165 effort to evaluate and improve the estimation of surfzone bathymetry [Smith *et al.*, 2017].
 166 Instruments included offshore wave sensors in water depths (h) of 11 ($x, y = 1295, 978$ m,
 167 positive offshore and to the north, respectively) and 6 m ($x, y = 606, 937$ m) and an array of
 168 colocated pressure sensors and acoustic Doppler velocimeters (ADVs) in the surf zone, sam-
 169 pled at 2 Hz (Figure 1a,b). Two cross-shore transects of four colocated ADVs and pressure
 sensors were deployed from $-3.5 < z < -1.5$ m (positive upward and referenced to the
 NAVD88 datum, approximately local mean sea level), initially positioned 0.5 to 1.0 m above

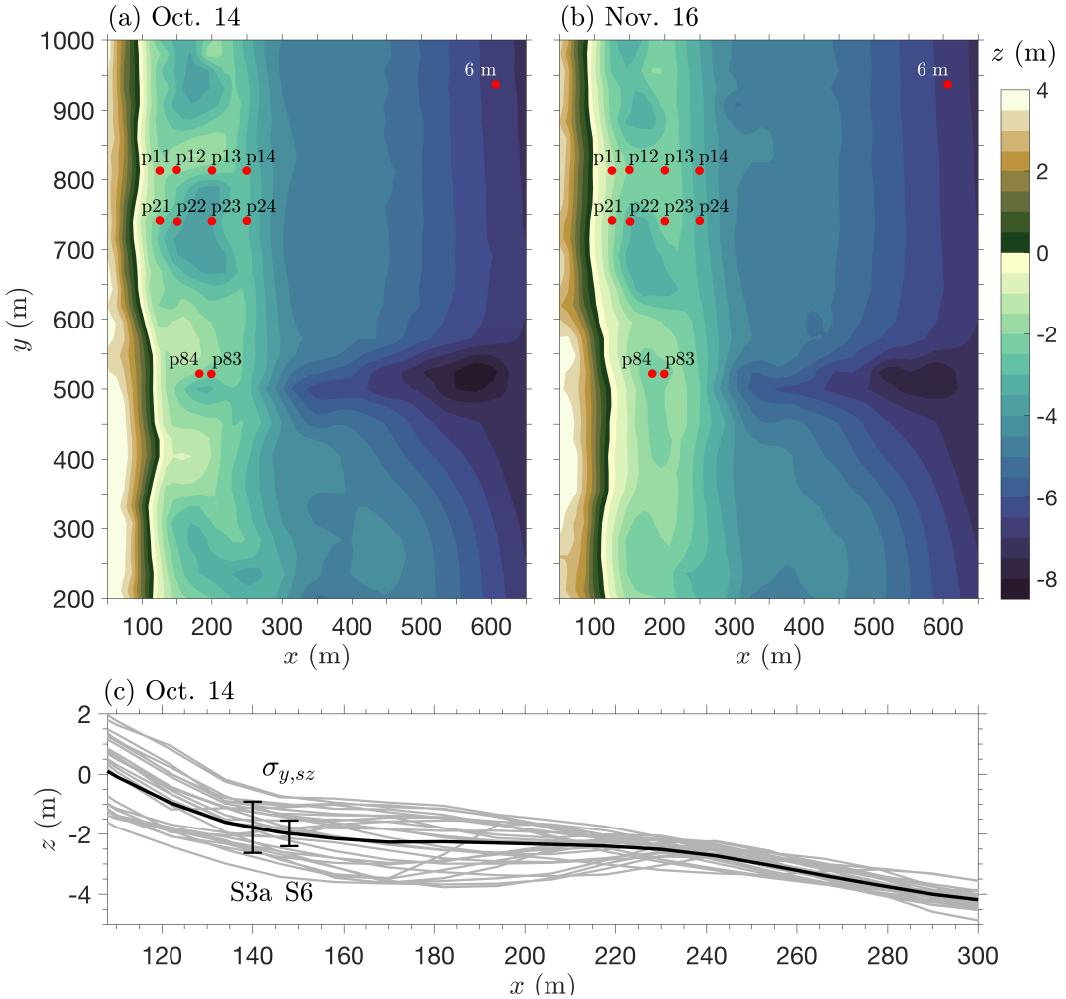
180 the bed, and separated by approximately 125 m in the cross-shore and 75 m in the alongshore
 181 (Figure 1, red circles, $y = 741$ and 813 m). Two additional sensors were deployed south of
 182 these arrays near the FRF pier ($y = 521$ m). Occasionally, current meter data were omitted
 183 when sensors were out of the water (low tide) or buried (accretion).

184 Bathymetric surveys were performed on Oct. 14 and Nov. 16, 2015 with the Lighter
 185 Amphibious Resupply Cargo (LARC) vehicle using a single-beam acoustic sonar and RTK
 186 GPS (Figure 1). The survey data were smoothed to an 8-m cross-shore by 45-m alongshore
 187 gridded bathymetry with estimated root-mean-square vertical elevation errors of approx-
 188 imately 0.05 m, attributed to sampling and interpolation errors [Plant *et al.*, 2002; Smith
 189 *et al.*, 2017]. The surveys covered 1200-m in the alongshore ($y = -100$ – 1100 m) and spanned
 190 from the beach to $h \approx 9$ m ($x = 50$ – 950 m).

191 Between the most offshore position of the shoreline ($x = 135$ m) and the bar crest
 192 ($x = 235$ m), the Oct. 14 bathymetry has a maximum surfzone alongshore standard devi-
 193 ation ($\sigma_{y,sz}$) of 0.86 m (Figure 1c, left vertical bar, S3a) located in the trough region. The
 194 nondimensional metric of bathymetric nonuniformity, the spatially averaged and normalized
 195 squared difference between the measured depth ($h(x, y)$) and the alongshore-averaged cross-
 196 shore depth ($\bar{h}(x)$) [Ruessink *et al.*, 2001] is defined as:

$$\chi^2 = \frac{1}{L_x L_y} \int_{x_0}^{x_{sz}} \int_{y_{south}}^{y_{north}} \left(\frac{h(x, y) - \bar{h}(x)}{\bar{h}(x)} \right)^2 dy dx \quad (1)$$

197 where L_x and L_y are the cross-shore and alongshore length where χ^2 is evaluated. χ^2 com-
 198 puted from $x = 134$ m (the farthest offshore extent where $h = 0$ m, x_0) to $x = 260$ m (the edge
 199 of the surf zone for the simulations with the largest wave simulation, x_{sz}) and $-100 \geq y \geq$
 200 1100 m is 0.099. On Oct. 14 (Nov. 16), the average shoreline position was approximately x
 201 = 108 m (110 m), and a single bar was located near $x = 235$ m (215 m) with an alongshore-
 202 variable trough near $x = 175$ m (170 m). In both bathymetric surveys, the morphology in-
 203 cludes bar-trough patterns (*e.g.*, Figure 1a: $y = 600$ – 750 m, Figure 1b: $y = 550$ – 700 m), vari-
 204 able terraces (*e.g.*, Figure 1a: $y = 750$ – 825 m, Figure 1b: $y = 700$ – 800 m), and a scoured
 205 channel under the FRF pier (Figure 1a,b: $y = 500$ m). Between Oct. 14 and Nov. 16, there
 206 was on average about a 10 m shoreward migration of the bar crest at $y = 600$ – 1100 m and a
 207 southward migration of some bathymetric features, such as the depression from $y = 600$ – 750
 208 m on Oct. 14, which may have migrated to $y = 550$ – 700 by Nov. 16 (Figure 1a,b).



162 **Figure 1.** Locations of colocated ADVs and pressure gauges (red symbols) and bathymetry (z , color
 163 contours, scale on the right) measured on (a) Oct. 14, 2015 and (b) Nov. 16, 2015 versus cross- (x) and along-
 164 shore (y) coordinates. Bathymetry from Oct. and Nov. have alongshore-varying sandbar-trough and terrace
 165 systems interrupted by channels. The deep channel at around $y = 500$ m is formed from scour near the FRF
 166 pier. (c) Vertical elevation (z) versus cross-shore coordinate (x) for profiles every 45 m in the alongshore
 167 (S3a, gray curves) and the alongshore-averaged profile (S7, black curve) for Oct 14. The alongshore standard
 168 deviation of the bathymetry ($\sigma_{y,sz}$) in the surf zone is denoted with vertical bars for simulations S3a and S6
 169 (Tables 1, 2).

209 ADV measurements were quality controlled [Elgar *et al.*, 2005] and used to compute
 210 hourly bulk current and wave parameters, reported as the average of six 512-second data col-
 211 lections each hour. A frequency-dependent correction for depth using linear wave theory was
 212 applied to nearshore pressure measurements to estimate sea-surface elevation statistics [Guza
 213 and Thornton, 1980]. Significant wave heights (H_s , 4 times the standard deviation of sea-
 214 surface elevation fluctuations for $0.05 < f < 0.30$ Hz) have an estimated error $< 5\%$. The
 215 energy-weighted wave angles (θ) and directional spread (σ_θ) were computed for the same
 216 frequency range using directional moments [Kuik *et al.*, 1988], and have an estimated er-
 217 ror of 5° owing to compass inaccuracies. Incident waves from counter-clockwise (from the
 218 north-east) and clockwise (from the south-east) of shore-normal are reported as $\theta > 0^\circ$ and
 219 $\theta < 0^\circ$, respectively. The range of the mean water level ($\langle \eta \rangle$, including tides, surge, and
 220 other large-scale water-level fluctuations) measured by a NOAA tide gauge ($h = 6$ m, $x, y =$
 221 582, 509 m) varied from -0.6 to 1.0 m. In 11-m water depth, H_s ranged from 0.3 to 2.0 m, θ
 222 varied from -45° to 50° , σ_θ was between 25° to 40° , and the peak wave periods (T_p) ranged
 223 from 4 to 12 s. In 2-m water depth, wave heights were depth limited, and thus varied tidally,
 224 wave directions usually were close to shore-normal, and directional spreads decreased rela-
 225 tive to offshore waves. The maximum hourly-average current speeds at a nearshore sensor at
 226 $h \approx 2$ m ($x, y = 150, 740$ m), was approximately 0.5 m/s (0.6 m/s) in the cross-shore (along-
 227 shore) when $H_s > 1.5$ m.

228 2.2 Numerical Modeling Testing Framework

229 Nearshore circulation and wave propagation were simulated using Simulating WAves
 230 till SHore (SWASH), a three-dimensional open source non-hydrostatic wave-flow model [Zi-
 231 jlema *et al.*, 2011]. SWASH solves the nonlinear shallow water equations including non-
 232 hydrostatic pressure, and conserves temperature, salinity, and suspended sediment [Zijlema
 233 and Stelling, 2005]. The second-order finite difference approximations (in time and space)
 234 in SWASH improve the computational efficiency, while correcting for frequency dispersion
 235 through the addition of more vertical layers. The steepening wave front is resolved in sim-
 236 ulations with sufficient vertical resolution and regarded as a jump-discontinuity in the flow
 237 variables (free surface, velocities). Conservation of momentum is enforced across the dis-
 238 continuity, which enables an energy dissipation rate similar to a hydraulic jump [Smit *et al.*,
 239 2013]. The hydrostatic front approximation that initiates wave breaking based on thresholds
 240 also is used in case the vertical gradients are not resolved adequately. Vertical mixing is ap-

proximated using a $k - \epsilon$ model, where k is the turbulent kinetic energy per unit mass and ϵ is the dissipation rate of turbulent kinetic energy per unit mass [Launder and Spalding, 1983]. The sensitivity to other approaches for vertical mixing is not explored here [Rijnsdorp *et al.*, 2017, see Appendix A for further details about the model].

SWASH was run on a 2-m-resolution horizontal grid spanning 1500 m alongshore and 900 m cross-shore from the shoreline to $h = 9$ m water depth with 5 vertical layers. Simulations were run with the observed bathymetry interpolated to the model grid with the still water level set to the hour-averaged observed ($h = 6$ m) water elevation ($\langle \eta \rangle$). To allow for north and south periodic boundary conditions, the domain was extended an additional 124 m alongshore on the northern and southern boundaries, converging exponentially to an alongshore-averaged bathymetry. All simulations were conducted for 2 hours with an initial time step of 0.04 seconds and a cycle length (repeated length of the time series realization) of 1 hr. After 1 hr of model spin up, 1-Hz output for the second hour is used for analysis. Further information about the numerical approach and model settings are provided in Appendix A.

The model was forced uniformly along the offshore boundary by a model-generated JONSWAP spectrum based on the observed offshore bulk wave parameters (H_s , T_p , θ , and σ_θ in $h = 11$ m) and a peakedness parameter (γ_J) calibrated to match the observed spectra ($\gamma_J = 1.4 - 1.9$). Errors introduced by applying forcing from an 11-m depth measurement at the 9-m depth model domain boundary are estimated to be small, with refraction resulting in differences of less than 1° in direction and less than 0.01 m in wave height. Bulk wave and current statistics from model simulations with bathymetry derived from the Oct. 14 survey (Figure 1a) are compared with observations for three directionally spread wave conditions (Table 1). Two of the simulations (S1 and S2, observed conditions on Oct 20 10:00 and 15:00 Eastern Daylight Time (EDT)) were selected to compare oblique with shore-normal waves during lower-energy conditions. The third simulation (S3a, observed conditions on Oct 28 00:00 EDT) has higher-energy, normally incident waves. Additionally, the sensitivity of the simulated nearshore circulation to bathymetry is investigated by repeating the third simulation (S3a) with bathymetry observed on Nov. 16 (S3b, Figure 1b). The surfzone width (L_{sz}) for each simulation is the distance from the alongshore-averaged shoreline position (x_{sl} , set by the mean water elevation) to the outer edge of the surf zone (x_{sz} , beginning of breaker zone), defined as the cross-shore location with the maximum cross-shore gradient in the alongshore-averaged significant wave height, $d\langle H_s \rangle_y / dx$ (Table 1).

274 The numerical framework and stability of SWASH impacted the selection of the test
 275 cases. For conditions with highly oblique, directionally spread waves ($\theta > 20^\circ, \sigma_\theta > 30^\circ$),
 276 unrealistic alongshore banding of H_s resulted from interference of the limited directional
 277 components that could be included in the domain geometry. Additionally, SWASH became
 278 unstable in the swash zone for moderate-energy oblique waves conditions ($\theta > 20^\circ, H_s > 1$
 279 m). Simulations were forced with a JONSWAP spectrum generated with the bulk wave pa-
 280 rameters, and thus time periods with bi-modal wave spectra, including from Oct. 14 10:00 to
 281 Oct. 17 23:00 EDT, were not simulated. The stability was compromised and computational
 282 time substantially increased when the number of vertical layers was doubled.

283 **Table 1.** Simulated test cases forced with observed conditions, including hour-average mean water elevation
 284 ($\langle \eta \rangle$) and offshore ($h = 11$ m) significant wave height (H_s), peak wave period (T_p), incident wave angle
 285 ($\theta = 0^\circ$ is shore-normal, $\theta < 0^\circ$ indicates waves from the southeast), directional spread (σ_θ), and the JON-
 286 SWAP gamma parameter (γ_J). Model bathymetry for each simulation was derived from surveys on Oct. 14
 287 or Nov. 16. The surfzone width (L_{sz}) is the distance between the shoreline (x_{sl} , where alongshore-averaged
 288 water depth, $\langle h \rangle_y = 0$) and the beginning of wave breaking (x_{sz}).

Sim.	Time of Obs. (EDT)	Bathymetry	$\langle \eta \rangle$ (m)	H_s (m)	T_p (s)	θ ($^\circ$)	σ_θ ($^\circ$)	γ_J	L_{sz}
S1	Oct. 20 10:00	Oct. 14	-0.03	0.62	7.8	-3.4	30.8	1.9	70
S2	Oct. 20 15:00	Oct. 14	0.13	0.51	8.8	-15.0	29.5	1.8	58
S3a	Oct. 28 00:00	Oct. 14	-0.32	1.95	7.1	-2.1	28.6	1.4	146
S3b	Oct. 28 00:00	Nov. 16	-0.32	1.95	7.1	-2.1	28.6	1.4	134

289 2.3 Vorticity Wavenumber Spectra Analysis

290 The alongshore length scales of surfzone eddies are quantified with the hour average
 291 of 1-Hz alongshore wavenumber spectra of vertical vorticity (with the spatial mean removed)
 292 over the second hour of a simulation (3600 - 7200 s). The alongshore wavenumber spectra
 293 were computed from depth-averaged vertical vorticity ($S_{\omega\omega}$) and from vertical vorticity at
 294 individual elevations ($S_{\omega\omega}(z)$), for alongshore eddy length scales $L \geq 4$ m ($k/2\pi \leq 0.25$
 295 m^{-1} , where k is the wavenumber) at each cross-shore grid location (2-m resolution). Ver-
 296 tical vorticity was estimated from gridded velocity components using a central-difference

297 approach [Patankar, 1980], where vorticity at individual vertical layers was computed from
 298 horizontal velocities at time-evolving terrain-following sigma layers interpolated to a grid
 299 of fixed elevations. To estimate phase-averaged vorticity, a 60-s moving average is applied
 300 to the vertical vorticity prior to computing the wavenumber spectra of vertical vorticity at 1
 301 Hz. The averaging is applied prior to, rather than following, the discrete vorticity estimate to
 302 remove apparent instantaneous wave-induced vorticity that is an artifact of the discretization.

303 Wavenumber spectra were computed for the energetic shore-normal waves (S3a) over
 304 the observed alongshore-variable bathymetry (measured Oct. 14, Figure 1a,c, $\sigma_{y,sz} = 0.86$
 305 m) and for four additional simulations (Table 2) with the same forcing as in S3a (Table 1),
 306 but with altered alongshore bathymetric variability and wave directional spread. The sen-
 307 sitivity of eddy length scales to the incident wave field (*e.g.*, short-crested wave breaking)
 308 is investigated with two simulations with the observed Oct. 14 bathymetry and with half of
 309 the observed (S4, $\sigma_\theta = 14.3^\circ$) and zero (S5) offshore directional spread. The influence of
 310 alongshore bathymetric variability on the distribution of eddy length scales is addressed with
 311 two simulations (S6, S7) with the observed offshore directional spread ($\sigma_\theta = 28.6^\circ$) and
 312 reduced alongshore bathymetric variability. S6 has bathymetry with half of the observed
 313 alongshore variability ($\sigma_{y,sz} = 0.43$ m, bathymetric features decreased by half the observed
 314 amplitude about the alongshore mean bathymetry, Figure 1c, right vertical bar), and S7 has
 315 alongshore-uniform bathymetry set to the alongshore-average of the observed bathymetric
 316 profiles ($\sigma_{y,sz} = 0$ m, Figure 1c, thick black curve).

317 **Table 2.** Simulations for the eddy length-scale analysis with the corresponding alongshore bathymetry stan-
 318 dard deviation in the surf zone ($\sigma_{y,sz}$), and the offshore directional spread (σ_θ). All other model parameters
 319 for each run are consistent with those for S3a (Table 1).

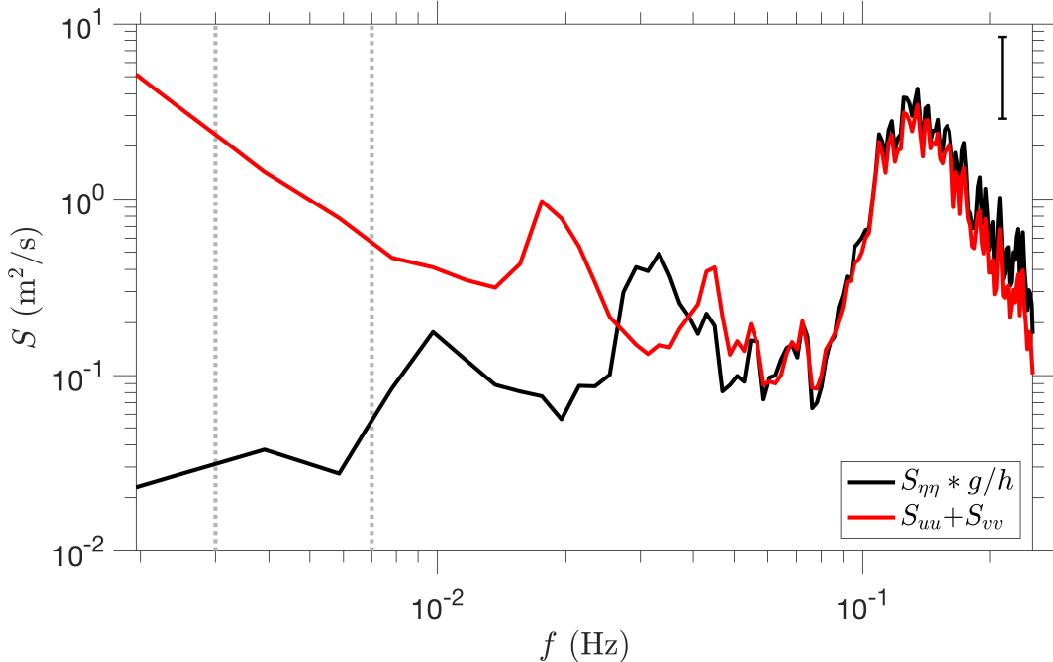
Sim. No.	$\sigma_{y,sz}$ (m)	σ_θ ($^\circ$)
S3a	0.86	28.6
S4	0.86	14.3
S5	0.86	0
S6	0.43	28.6
S7	0	28.6

320 **2.4 Very Low-Frequency Velocity Analysis**

321 The very low-frequency (VLF) surfzone currents, defined here as currents in the band
 322 $0.003 < f < 0.007$ Hz, were computed with 1-Hz time series along several cross-shore
 323 transects of the three-dimensional SWASH simulations. Similar to the vorticity estimates at
 324 specific elevations, horizontal velocities at sigma layers were interpolated to a fixed vertical
 325 grid spanning from near the mean sea-surface to near the bed. Velocities defined as ‘near-
 326 surface’ are at the grid point closest to one half of the alongshore-averaged significant wave
 327 height below the mean sea-surface elevation. Velocities defined as ‘near-bottom’ are at the
 328 grid point closest to 0.03 m above the bed, typically outside of a surface-gravity wave bot-
 329 tom boundary layer. Temporal velocity spectral analyses were performed using a Hanning
 330 window period of 512 s with an overlap period of 256 s for a 1-hr cross- (u) and alongshore
 331 (v) velocity 1-Hz time series, yielding a $\Delta f = 0.002$ Hz with the lowest bin centered at
 332 $f = 0.002$ Hz and 28 DOF. To test the confidence in VLF statistics over the last hour of the
 333 2-hr simulation, simulation S3a and S7 (Table 2) were run for a longer time period (4 hrs with
 334 84 DOF). The statistics from the last hour of the 2-hr simulation (3600 - 7200 s) were simi-
 335 lar to statistics from the last 3 hrs of the 4-hr simulation (3600 - 14400 s), justifying that the
 336 results are statistically significant for the shorter simulation. When converted to equivalent
 337 velocity using the linear finite-depth dispersion relationship, sea-surface elevation spectral
 338 levels ($S_{\eta\eta} * g/h$ where g is gravitational acceleration and h is mean water depth) within the
 339 VLF band are 1 to 2 orders of magnitude lower than the velocity spectral levels ($S_{uu} + S_{vv}$,
 340 e.g., modeled at $x, y = 132, 740$ m in Figure 2, dashed lines indicate the VLF band), indicat-
 341 ing that VLF motions are rotational rather than directly forced by sea, swell, or infragravity
 342 waves [Lippmann *et al.*, 1999; MacMahan *et al.*, 2010; Elgar *et al.*, 2019]. The observed and
 343 modeled velocity spectral levels at $x, y = 132, 740$ m are similar for infragravity and VLF
 344 motions (within the 95% confidence interval).

345 The VLF spectral densities (S_{uu}, S_{vv}) are computed as the sum of the frequency bins
 346 centered at $f = 0.004$ and 0.006 Hz. The squared coherence of the VLF velocity (λ_u^2, λ_v^2)
 347 and the phase relative to the near-surface VLF velocity (ϕ_u, ϕ_v , positive and negative phase
 348 indicate leading and lagging surface velocities) are computed as the energy weighted aver-
 349 age over the $f = 0.004$ and 0.006 Hz bins [Hannan, 1970; Priestely, 1981]. To represent
 350 the relative variability of VLF velocities over the water column, $(u_{rms} - u_{0,rms})/u_{0,rms}$ and
 351 $(v_{rms} - v_{0,rms})/v_{0,rms}$, the normalized difference between the root mean square (rms) over
 352 time of filtered VLF velocities (u_{rms}, v_{rms}) and the near-surface velocity ($u_{0,rms}, v_{0,rms}$),

353 was computed from the band-passed $0.003 < f < 0.007$ Hz) velocities [PL64 filter, *Rosenfeld*, 1983], where greater and less than 0 indicates more and less VLF velocity variance at
 354 depth relative to near the surface, respectively.
 355



356 **Figure 2.** Sea-surface elevation spectral density converted to equivalent velocity ($S_{\eta\eta} * g/h$, black) and
 357 the sum of the depth-averaged cross- and alongshore spectral densities (S_{uu}, S_{vv} , red) in the surf zone (x, y
 358 = 132, 740 m) versus frequency (f). Vortical motion is the dominant energy in the VLF band (between the
 359 vertical dashed lines). The vertical bar indicates the 95% confidence interval for 28 DOF.

360 3 Results

361 3.1 Observed and Modeled Nearshore Conditions

362 The capability of SWASH to simulate surfzone circulation on a natural beach is tested
 363 by comparing modeled with the observed hourly bulk wave and current statistics. At the
 364 model offshore boundary ($h = 11$ m) for simulations with Oct. 14 bathymetry (S1, S2, S3a,
 365 Table 1) the alongshore-averaged $S_{\eta\eta}$ is similar to the observed sea-surface elevation spec-
 366 tra ($S_{\eta\eta}$, Figure 3, black curves). The observed and modeled $S_{\eta\eta}$ also are similar at $h = 6$
 367 m (Figure 3, red curves), with slightly lower energy in the modeled spectra at the peak fre-
 368 quency for lower-energy waves (S1, S2). The differences between the observed and modeled
 369 spectra at $h = 6$ m may be associated with differences in the observed and modeled off-

shore spectrum and boundary conditions (Figure 3, black curves), including the assumption of uniform wave forcing along the offshore boundary, and inaccuracy in modeled physics (e.g., wave transformation, wave-wave interactions, and other nonlinear processes).

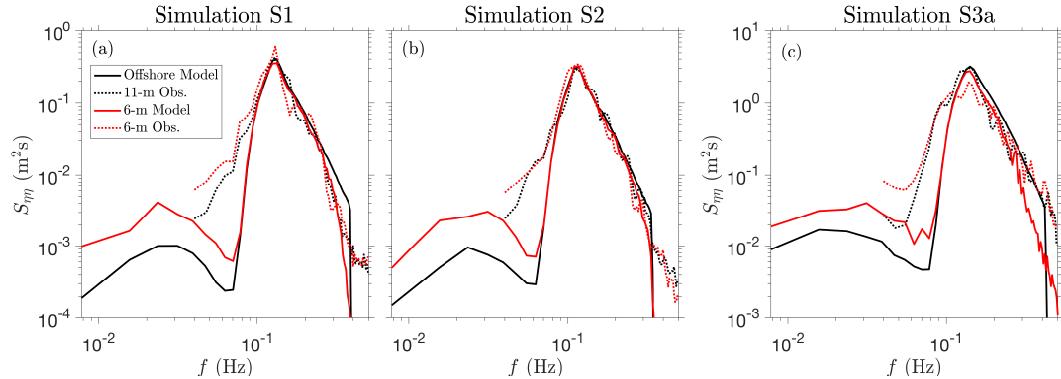


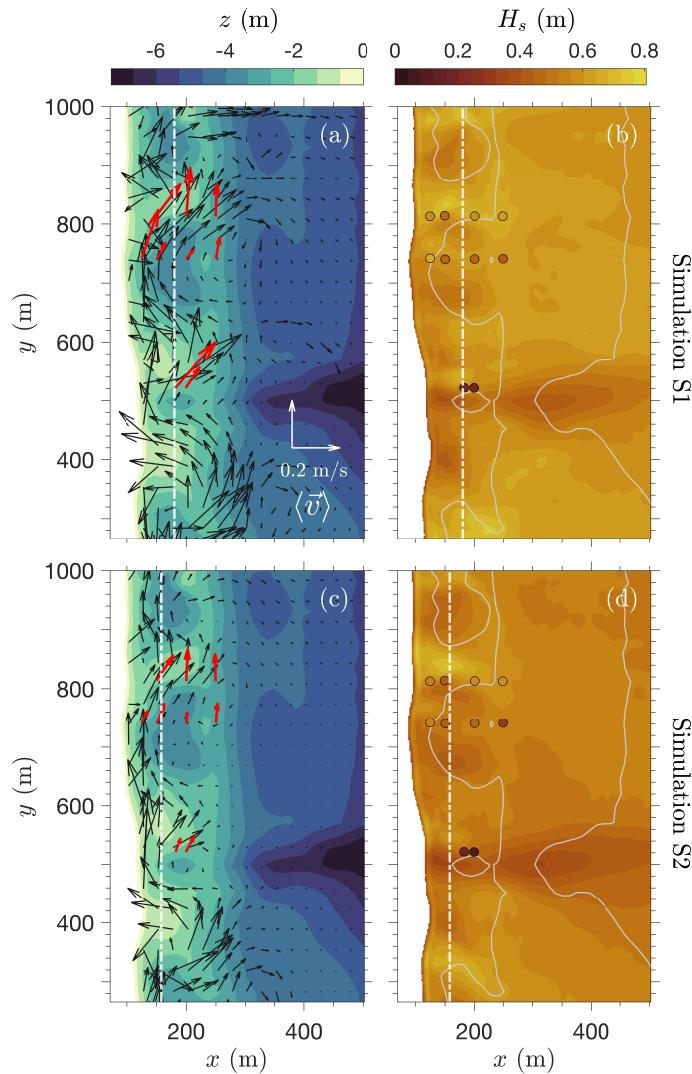
Figure 3. Sea-surface elevation spectral densities ($S_{\eta\eta}$) versus frequency (f) for alongshore-averaged model spectra at the offshore boundary (solid-black curves), observed spectra in 11-m depth (dashed-black curves), and simulated (solid-red curves) and observed (dashed-red curves) spectra in 6-m depth for simulations (a) S1, (b) S2, and (c) S3a. There are 48 DOF in the spectra.

The modeled and observed H_s for simulations with Oct. 14 bathymetry (S1, S2, S3a) have similar patterns, including a reduction in H_s from depth-limited breaking in the surf zone (Figure 4b,d, 5b, x_{sz} : white dashed lines) and smaller H_s near the pier due to wave refraction (around $y = 500$ m). Although the model simulates the observed cross-shore pattern of H_s , the modeled H_s is larger than observed (RMSE = 0.28 m, bias = 0.23 m, Figure 4b,d, 5b, colors in circles are darker than in the surrounding area). The positive bias of the modeled H_s is smaller if the stations near the pier (p84 and p85), where large changes in bathymetry may occur, are not included in the comparison (RMSE=0.21 m, bias = 0.18 m). The similar patterns and positive bias of modeled H_s relative to observations is shown along the cross-shore transect at $y = 741$ m (along stations p21-24, Figure 6a), where the modeled statistics are alongshore-averaged over 90 m ($696 \leq y \leq 786$ m, Figure 6, solid curves). A simulation with higher spatial resolution (1-m) performed for the same conditions as S1 resulted in similar errors between the modeled and observed wave height and velocities. Errors in H_s are larger than results from 3D simulations with small alongshore bathymetric variability [Rijnsdorp *et al.*, 2015], whereas the absolute biases are similar to 2-layer simulations at this field site [Gomes *et al.*, 2016]. The wave breaking parameters, α and β (Appendix A) were set to standard values from the literature and were not tuned to this dataset. Although

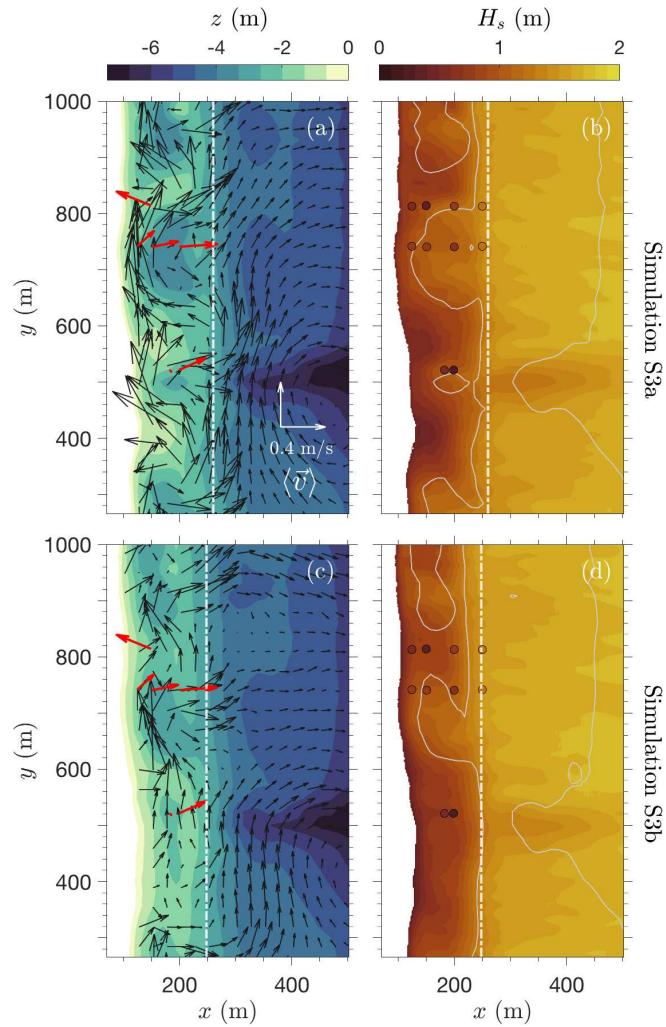
394 dissipation due to wave breaking may be improved with higher resolution simulations, in-
 395 creasing the number of vertical layers leads to instabilities. Due to the bathymetric uncer-
 396 tainty and a focus on understanding circulation dynamics rather than accurate hindcasting,
 397 tuning of the vertical resolution to minimize errors between the observed and modeled H_s
 398 was not investigated here.

399 The observed and simulated hour-averaged velocities include strong offshore-directed
 400 cross-shore velocities, $\langle u \rangle$, as part of bathymetric rip-current circulation cells, and along-
 401 shore velocities, $\langle v \rangle$, that meander around prominent bathymetric features with weaker $\langle v \rangle$ in
 402 the center of circulation cells (e.g., $y = 741$ m, Figure 4a,c, 5a). The modeled depth-averaged
 403 velocities are on average higher than the observed velocities (bias = 0.04 m/s), but almost
 404 always are within the alongshore range (Figure 6, shaded regions, comparisons with depth-
 405 varying velocities at the instrument elevations are similar). For small shore-normal wave
 406 conditions (S1), the modeled and observed velocities have similar magnitudes with small
 407 differences that may be owing to localized bathymetric variability not resolved by the sur-
 408 veys or to migration of bathymetric features after the Oct. 14 survey (Figure 6b,c). For the
 409 moderate-energy shore-normal wave condition (S3a), the strongest modeled $\langle u \rangle$ appear to
 410 be shifted in the positive alongshore direction relative to the observations (Figure 5a), which
 411 may be due to migration of bathymetric features resulting from strong alongshore currents
 412 between Oct. 14 and Oct. 28.

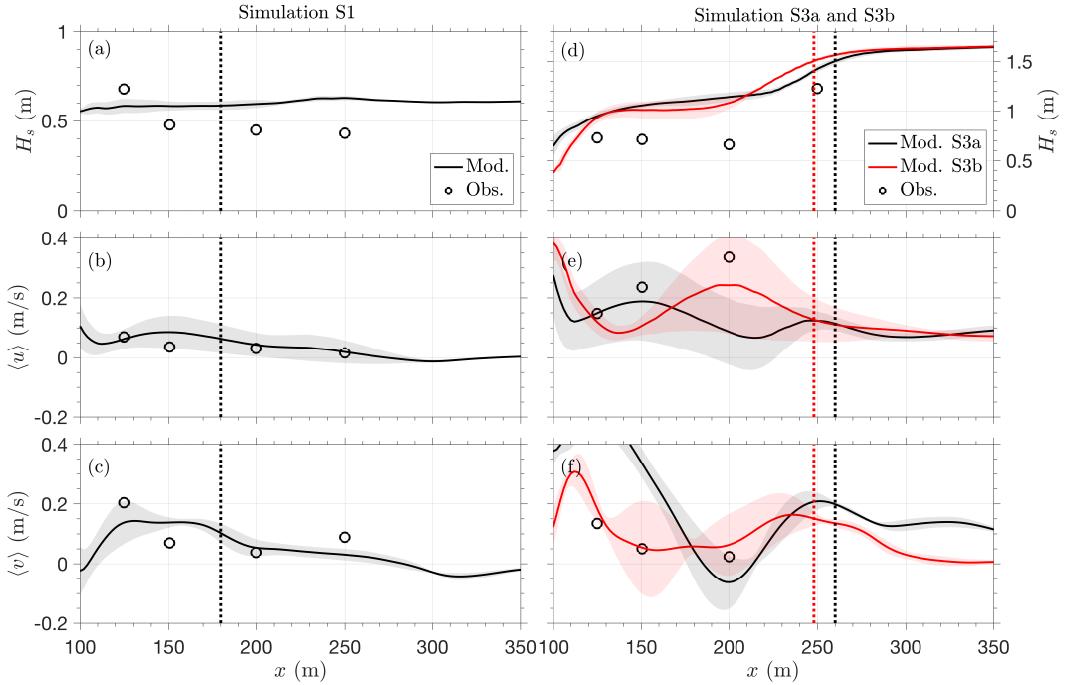
413 To determine the sensitivity of the H_s and hour-averaged velocity spatial patterns to
 414 bathymetric variability, an additional simulation was conducted with bathymetry from Nov.
 415 16 and the moderate-energy shore-normal wave conditions observed on Oct. 28 (S3b, same
 416 wave conditions as S3a). Oct 28 is approximately halfway between the dates of two bathymetry
 417 surveys (Figure 1a,b). The modeled $S_{\eta\eta}$ at $h = 6$ m is not sensitive to the survey bathymetry,
 418 but surfzone H_s are smaller in S3b than in S3a, and thus are more similar to observations
 419 (S3a: bias = 0.40 m, S3b: bias = 0.23 m, Figure 6d, compare black with red curves). In S3b,
 420 the position of the modeled circulation features, including the strong offshore-directed ve-
 421 locities, is similar to that of the observations, leading to smaller errors in a point-to-point
 422 comparison (S3a: RMSE = 0.30 m/s, S3b: RMSE = 0.13 m/s, Figure 6e,f).



423 **Figure 4.** Observed (left: red arrows, right: filled circles) and modeled (left: black arrows, right: color
 424 contours) (a,c) hour-averaged depth-averaged velocity, $\langle \vec{v} \rangle$ and (b,d) significant wave height, H_s for small
 425 shore-normal (S1, a,b) and oblique (S2, c,d) wave conditions. Bathymetry (left: color contours, right: grey
 426 contour curves at 2.5 and 5.0 m depths) and the approximate outer edge of the surf zone (x_{sz} , all panels:
 427 dashed white lines) are shown. Sensor measurements that were removed during quality control are not in-
 428 cluded here.



429 **Figure 5.** Observed (left: red arrows, right: filled circles) and modeled (left: black arrows, right: color
 430 contours) (a,c) hour-averaged depth-averaged velocity, $\langle \vec{v} \rangle$ and (b,d) significant wave height, H_s for moderate-
 431 energy shore-normal wave conditions on Oct. 28 with Oct. 14 (S3a, a,b) and Nov. 16 (S3b, c,d) bathymetry.
 432 Bathymetry (left: color contours, right: grey contour curves at 2.5 and 5.0 m depth) and the approximate outer
 433 edge of the surf zone (x_{sz} , all panels: dashed white lines) are shown. The $\langle \vec{v} \rangle$ scale (left) and H_s colorbar
 434 (right) span approximately twice the range of those in Figure 4.



435 **Figure 6.** (a,d) Observed (circles) and modeled (curves) significant wave height, H_s and (b,e) 1-hr mean
 436 cross-shore, $\langle u \rangle$ and (c,f) alongshore $\langle v \rangle$ velocities along the cross-shore transect at $y = 741$ m (Figure 1) for
 437 simulations S1 (left), S3a (right, black), and S3b (right, red). Model results are represented as the cross-shore
 438 profiles of 90 m alongshore-averaged (curves) and standard deviation (shaded areas) of wave and current
 439 statistics. The black (S1, S3a) and red (S3b) dashed vertical lines are the alongshore-averaged outer edge of
 440 the surf zone, x_{suz} .

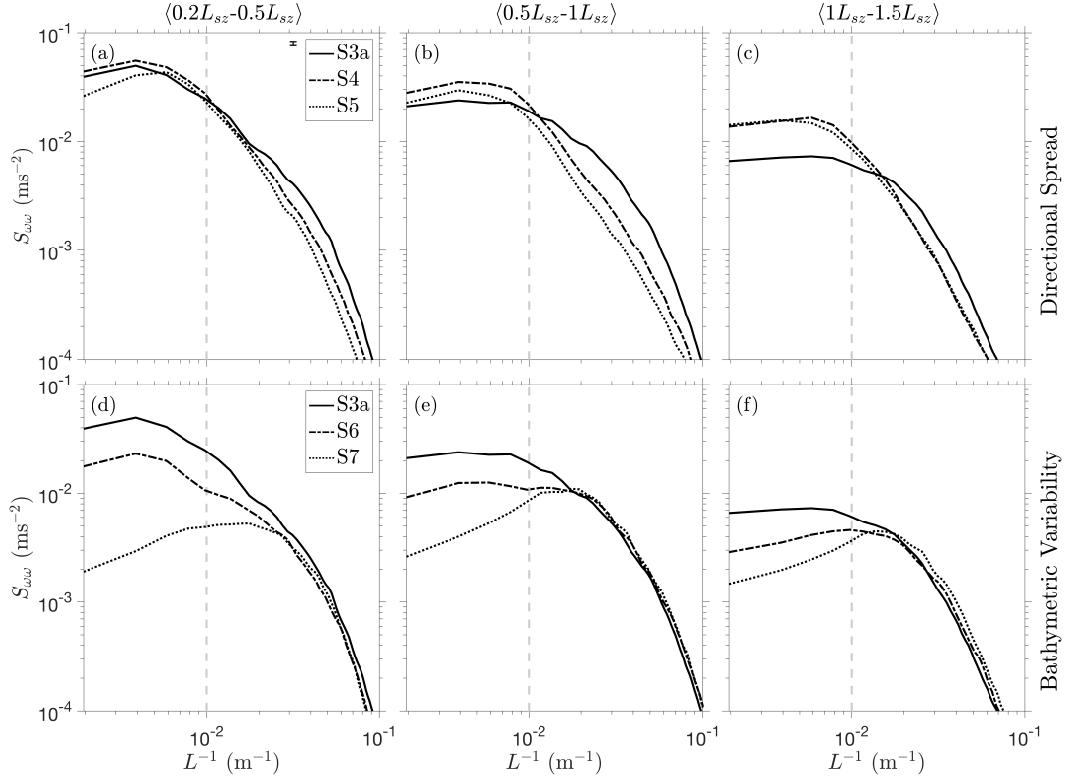
441 **3.2 Vorticity Wavenumber Spectra**

442 The cross-shore and vertical variability of eddy length scales on alongshore-variable
 443 bathymetry is not known. Here, the alongshore wavenumber spectra of the modeled vertical
 444 vorticity is considered for shore-normal waves ($H_s = 2$ m) with different directional spreads
 445 (S3a, S4, S5) and alongshore bathymetric variability (S3a, S6, S7, Table 2). The cross-shore
 446 coordinate is normalized by the surfzone width, L_{sz} (Table 1), where $L_{sz} = x_{sz} - x_{sl}$, where
 447 x_{sz} is the position of the outer edge of the surf zone, and x_{sl} is the alongshore-mean position
 448 of the still-water shoreline. Swashzone dynamics, including strong runup and backwash ve-
 449 locities, along an alongshore-varying shoreline may dominate the vorticity field near and in
 450 the swash zone ($0L_{sz} < x - x_{sl} < 0.2L_{sz}$) and are not shown here, where the focus is on the
 451 inner ($0.2L_{sz} < x - x_{sl} < 0.5L_{sz}$) and outer surf zones ($0.5L_{sz} < x - x_{sl} < 1.0L_{sz}$), and just
 452 offshore of the surf zone ($1.0L_{sz} < x - x_{sl} < 1.5L_{sz}$).

463 **3.2.1 Cross-Shore Variability of the Alongshore Wavenumber Spectra of Vorticity**

464 For simulations conducted with observed Oct. 14 bathymetry ($\sigma_{y,sz} = 0.86$ m) and dif-
 465 ferent offshore directional spreads (S3a, S4, S5), the magnitude of $S_{\omega\omega}$ is largest at large
 466 length scales ($L > 100$ m) and is insensitive to directional spread in the inner surf zone
 467 (Figure 7a). In contrast, in the outer surf zone and immediately outside the surf zone, $S_{\omega\omega}$
 468 has more variance at large length scales for simulations with less directional spread (Figure
 469 7b,c). The magnitude of $S_{\omega\omega}$ at small length scales ($\mathcal{O}(10)$ m), hypothesized to be associated
 470 with injection of vorticity from finite-crested breaking waves, is highest for the largest wave
 471 directional spread (S3a) at all cross-shore positions (Figure 7, top row). For the simulation
 472 with the largest directional spread (S3a, $\sigma_\theta = 28.6^\circ$), the magnitude of $S_{\omega\omega}$ at $L < 85$ m
 473 in the outer surf zone, where wave breaking is strong, is larger than the magnitude in the in-
 474 ner surf zone and just offshore of the surf zone (Figure 7, top row, compare solid curves at
 475 $L^{-1} > 10^{-2}$ m $^{-1}$).

476 For simulations with observed offshore directional spread ($\sigma_\theta = 28.6^\circ$) and differing
 477 alongshore bathymetric variability (S3a, S6, S7, Table 2), the variance of vorticity fluctua-
 478 tions at large length scales ($L > 100$ m) increases with increasing alongshore bathymetric
 479 variability (Figure 7, bottom row). The largest sensitivity to bathymetry of the $S_{\omega\omega}$ magni-
 480 tude at large length scales occurred in the inner surf zone (Figure 7d), where deep trough and
 481 terrace bathymetric features are present. In contrast, the variance of small length-scale eddies



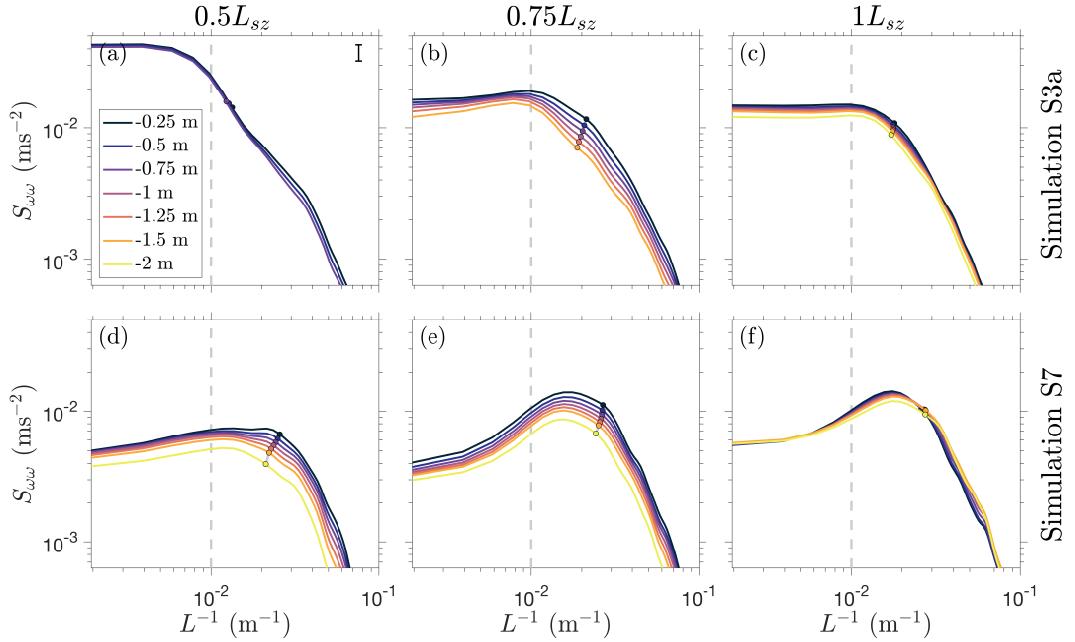
453 **Figure 7.** Cross-shore average of the alongshore wavenumber spectra of vorticity ($S_{\omega\omega}$) versus the inverse
 454 alongshore length scale (wavenumber divided by 2π , $L^{-1} = k_y/2\pi$), vertical dashed grey lines at $L = 100$ m)
 455 for (a,d) the inner surf zone ($0.2L_{sz} < x - x_{sl} < 0.5L_{sz}$), (b,e) the outer surf zone ($0.5L_{sz} < x - x_{sl} < 1.0L_{sz}$),
 456 and (c,f) just offshore of the surfzone edge ($1.0L_{sz} < x - x_{sl} < 1.5L_{sz}$) for (a-c) simulations with observed
 457 bathymetry and forced with large directional spread ($S3a$, $\sigma_\theta = 28.6^\circ$, solid curves), half the directional
 458 spread ($S4$, $\sigma_\theta = 14.3^\circ$, dot-dashed curves), and no directional spread ($S5$, $\sigma_\theta = 0^\circ$, dotted curves), and
 459 for (d-f) simulations with directionally spread waves ($\sigma_\theta = 28.6^\circ$) and observed Oct. 15 bathymetry ($S3a$,
 460 $\sigma_{y,sz} = 0.86$ m, solid curves), half the observed alongshore bathymetric variability ($S6$, $\sigma_{y,sz} = 0.43$ m,
 461 dot-dashed curves), and alongshore-averaged bathymetry ($S7$, $\sigma_{y,sz} = 0$ m, dotted curves). The vertical bar in
 462 (a) indicates the 95% confidence interval for 3540 DOF.

482 ($\mathcal{O}(10)$ m) is similar and relatively independent of alongshore bathymetric variability (Figure
 483 7d-f).

484 **3.2.2 Vertical Variability of the Alongshore Wavenumber Spectra of Vorticity**

485 The cross-shore variability of eddy length scales has been investigated with models
 486 that account for the generation of eddies from short-crested wave breaking [Kumar and Fed-
 487 dersen, 2017; O'Dea *et al.*, 2020]. However, the vertical variability of eddy length scales
 488 is not known and has not been investigated using a three-dimensional phase-resolving model.
 489 Here, the alongshore wavenumber spectra of vertical vorticity at different elevations ($S_{\omega\omega}(z)$,
 490 computed with interpolated horizontal velocities, Section 2.3) are used to investigate the
 491 vertical variability of eddy length scales in the surf zone for shore-normal waves with Oct.
 492 14 observed (S3a, Figure 8a-c) and alongshore-averaged (S7, Figure 8d-f) bathymetry. The
 493 magnitude of $S_{\omega\omega}(z)$ at large length scales ($L > 100$ m) is larger at all depths for the alongshore-
 494 varying (S3a) than for the alongshore-uniform (S7) bathymetry (compare Figure 8a-c with
 495 Figure 8d-f), consistent with the wavenumber spectra computed from the depth-averaged ve-
 496 locities ($S_{\omega\omega}$, Figure 7).

505 The magnitude of $S_{\omega\omega}(z)$ is nearly depth uniform outside of (not shown) and at the
 506 outer edge (Figure 8c,f) of the surf zone, and decays slightly with decreasing vertical eleva-
 507 tions, primarily for small length-scale eddies, in the outer surf zone in both examples (Figure
 508 8b,e) and in the inner surf zone for the alongshore uniform bathymetry (Figure 8d). The ver-
 509 tical dependence of $S_{\omega\omega}(z)$ in the inner surf zone for the alongshore-variable bathymetry
 510 is not evaluated here due to the inability to resolve $S_{\omega\omega}(z)$ at elevations that are below the
 511 seafloor at some alongshore locations (*e.g.*, $z < -0.75$ m at $0.5L_{sz}$, Figure 8a). For the
 512 alongshore-variable bathymetry simulation (S3a), the vorticity variance (the area under
 513 $S_{\omega\omega}(z)$) for small eddy length scales ($L < 100$ m) decays by 36% over 1 m in the water col-
 514 umn in the outer surf zone (Figure 8b), whereas the vorticity variance for small length scales
 515 decreases by less than 15% over 2 m in the water column at the outer edge of the surf zone
 516 (Figure 8c). In the inner and outer surf zone for the alongshore-uniform bathymetry simula-
 517 tion (S7), the vorticity variance from near the surface ($z = -0.25$ m) to the lowest resolved
 518 elevation in the water column decays by $\geq 45\%$ for small eddy length scales and $> 25\%$ for
 519 large eddy length scales (Figure 8d,e).

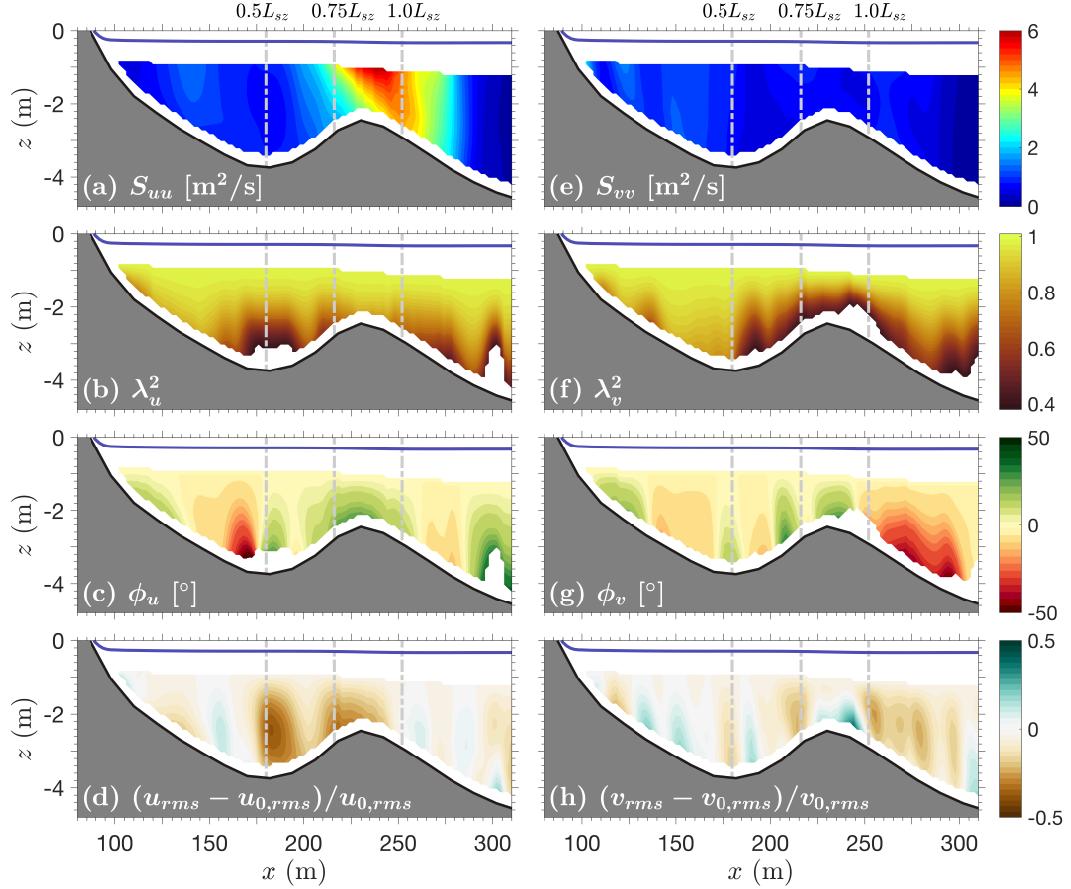


497 **Figure 8.** The alongshore wavenumber spectral density of vorticity ($S_{\omega\omega}(z)$) versus the inverse along-
 498 shore length scale (wavenumber divided by 2π , $L^{-1} = k_y/2\pi$), vertical dashed grey line at $L = 100$ m) for
 499 normalized cross-shore positions (a,d) in the inner surf zone ($x - x_{sl} = 0.5L_{sz}$), (b,e) the outer surf zone
 500 ($x - x_{sl} = 0.75L_{sz}$) and (c,f) the outer edge of the surf zone ($x - x_{sl} = 1.0L_{sz}$). At each location, the col-
 501 ored curves (legend inset, lighter curves nearer to the seafloor) are the spectra at 0.25 to 2 m below the mean
 502 sea-surface elevation for (a-c) observed bathymetry (S3a) and (d-f) alongshore-uniform bathymetry (S7). The
 503 circles (colored by elevation) are at the mean eddy length scale, \bar{L} (centroid). The vertical bar (a) indicates the
 504 95% confidence interval for 354 DOF.

Furthermore, the mean eddy length scale, \bar{L} ($= \bar{k}_y/2\pi$, energy-weighted average length scale, the centroid of the spectrum, Figure 8 circles) of $S_{\omega\omega}(z)$ increases with decreasing vertical elevations in the surf zone for nearly all simulations (wavenumber decreases with decreasing vertical elevations, Figure 8b,d,e) and decreases or remains approximately the same over the vertical near the surfzone edge (Figure 8c,f) and just offshore of the surf zone (not shown). For the simulation with the observed bathymetry (S3a), \bar{L} near-surface is ~ 46 m and increases to ~ 53 m over 1.25 m in the water column in the outer surf zone (Figure 8b). Similarly, for the alongshore-uniform bathymetry simulation (S7), \bar{L} is ~ 39 m near the surface and increases to ~ 45 m over 1.5 m in the water column in the inner surf zone (Figure 8d).

3.3 Vertical Structure of Very Low-Frequency Motion

Field observations suggest there may be vertically varying structure of low-frequency eddies in the outer surf zone, but less variation in shallower depths [Lippmann *et al.*, 2016; Henderson *et al.*, 2017]. Here, the very low-frequency (VLF, $0.003 < f < 0.007$, Section 2.3, Figure 2) velocities from the simulation with moderate-energy shore-normal waves and Oct. 14 observed bathymetry (S3a, Figure 1) vary along the barred cross-shore profile ($y = 741$ m) and vertically in the outer surf zone (Figure 9). In the outer surf zone, the change in simulated cross-shore (alongshore) VLF velocities are up to 0.14 m/s (0.12 m/s) over the water column (not shown). The VLF velocity spectral density varies in the cross-shore, with the highest cross-shore VLF spectral density near the bar crest at $x = 220 - 240$ m (Figure 9a) and the highest alongshore VLF spectral density near the shoreline at $x < 100$ m (Figure 9e). The cross- and alongshore spectral densities are similar in magnitude at all locations, except near the bar crest where the cross-shore spectral density is much greater than the alongshore spectral density (Figure 9a,e). The coherence of VLF velocities at different elevations in the water column with those near the surface decreases with distance below the surface, including near the wave breaking region (around the bar crest, $x = 200 - 270$ m, Figure 9b,f). The VLF phase relative to the phase at the surface changes sign in the cross-shore (Figure 9c,g), indicating that near-bottom velocities alternate between leading and lagging surface velocities. The root-mean-squared (rms) VLF cross-shore velocities decrease with depth in the trough and near the bar crest ($x = 175 - 190$ and $x = 220 - 240$ m, Figure 9d), indicating more variable VLF velocities near the surface onshore of the onset of wave breaking.



530 **Figure 9.** Cross-shore transect for the simulation S3a at $y = 741$ m of the (a-d) cross- and (e-h) along-
 531 shore VLF velocity spectral density (a: S_{uu} , e: S_{vv}), squared coherence (b: λ_u^2 , f: λ_v^2), phase shift (c:
 532 ϕ_u , g: ϕ_v), and the normalized root-mean-squared (rms) difference (d: $(u_{rms} - u_{0,rms})/u_{0,rms}$, h:
 533 $(v_{rms} - v_{0,rms})/v_{0,rms}$) where negative (positive) indicates less (more) variability compared with the
 534 surface, with the mean sea-surface elevation (blue) and surfzone regions (dashed grey lines). Values are not
 535 shown for coherence squared and phase when the coherence is less than the 95% significance level.

557 The rms VLF alongshore velocities have relatively small vertical dependence onshore and
 558 offshore of the bar (Figure 9h).

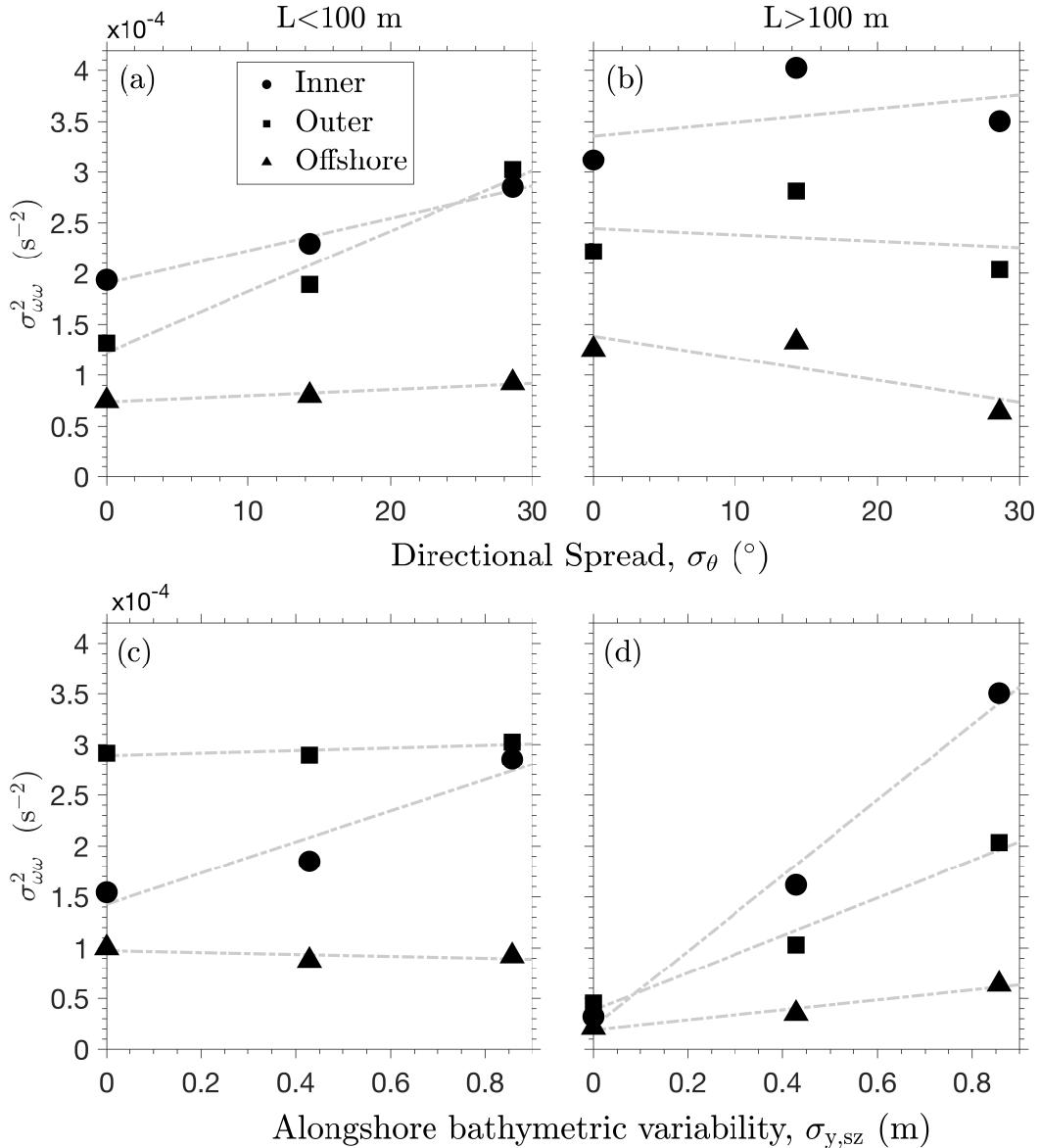
559 Cross-shore transects at other regions of the S3a domain (*e.g.*, the terraced beach pro-
 560 file at $y \approx 850$ m, Figure 1) have similar vertical dependence in the outer surf zone (*e.g.*, $0.75L_{sz}$),
 561 as do VLF velocities with alongshore-uniform bathymetry (S7 simulation, not shown), sug-
 562 gesting that there is vertical variation of VLF velocities in the outer surf zone, with decreas-
 563 ing vertical dependence toward the shore for both the simulated alongshore-uniform and
 564 alongshore-varying bathymetry.

565 4 Discussion

566 4.1 Cross-Shore Variability of Vorticity Wavenumber Spectra

567 The length scales of horizontal eddies and their dependence on the incident wave forc-
 568 ing, coupled with the role of surfzone bathymetry, is a focus of recent studies [Feddersen,
 569 2014; Kumar and Feddersen, 2017; O'Dea *et al.*, 2020]. Here, for simulations with varying
 570 offshore directional spread (σ_θ) on an alongshore inhomogeneous bathymetry, the vorticity
 571 variance, $\sigma_{\omega\omega}^2$ (the area under alongshore wavenumber spectra of depth-averaged vertical
 572 vorticity separated for inverse length scales (wavenumbers divided by 2π , $L^{-1} = k_y/2\pi$)
 573 on either side of 0.01 m^{-1} , $S_{\omega\omega}$, in Figure 7) at small length scales ($L < 100$ m) increases
 574 with directional spread in all cross-shore regions (Figure 10a, circles, squares, triangles, and
 575 linear fit with slopes = 3.2, 6.0, and $0.6 \times 10^{-6} \text{ m}^{-1}\text{s}^{-2}$, respectively), consistent with re-
 576 sults from previous modeling studies using a depth-integrated wave-resolving Boussinesq
 577 model with alongshore-uniform bathymetry [Spydell and Feddersen, 2009; Suanda and Fed-
 578 dersen, 2015] and alongshore-variable bathymetry [O'Dea *et al.*, 2020]. Multiple surfzone
 579 processes may contribute to the vorticity variance at small length scales, including gener-
 580 ation by directionally spread short-crested breaking waves (*e.g.*, $\sigma_\theta = 28.6^\circ$ in S3a). The
 581 small length-scale ($O(10)$ m) vorticity injected during wave breaking may be transferred to
 582 longer length scales through an inverse cascade [Bühler and Jacobson, 2001; Boffetta and
 583 Ecke, 2012; Feddersen, 2014; Elgar *et al.*, 2019; Elgar and Raubenheimer, 2020] or dissi-
 584 pated through bottom friction.

590 In contrast to small length scales, the dependence of large length-scale ($L > 100$ m)
 591 vorticity variance on directional spread differs by region within the surf zone, possibly ow-
 592 ing to eddy coalescence and pulsations in mean circulation patterns. In the inner surf zone,



585 **Figure 10.** Vorticity variance, $\sigma_{\omega\omega}^2$ versus (a,b) directional spread, σ_θ (S3a, S4, S5) and (c,d) the stand-
 586 dard deviation of surfzone bathymetric variability, $\sigma_{y,sz}$ (S3a, S6, S7) for (a,c) small ($L < 100$ m) and (b,d)
 587 large ($L > 100$ m) eddy length scales for the inner (circles, $0.2L_{sz} < x - x_{sl} < 0.5L_{sz}$), outer (squares,
 588 $0.5L_{sz} < x - x_{sl} < 1.0L_{sz}$), and offshore (triangles, $1.0L_{sz} < x - x_{sl} < 1.5L_{sz}$) of the surf zone. Linear
 589 least-squares fits are given by the dashed-grey lines.

593 vorticity variance at large length scales are small and weakly increase with directional spread
 594 (Figure 10b, circles and linear fit with slope = $1.3 \times 10^{-6} \text{ m}^{-1}\text{s}^{-2}$), possibly as a result of
 595 the enhancement of the coalescence of small length-scale eddies generated by short-crested
 596 wave breaking in the highly variable inner surf zone [Bühler and Jacobson, 2001; Spydell
 597 and Feddersen, 2009; Clark *et al.*, 2012] or fluctuations of strong inner surf zone circula-
 598 tion patterns (Figure 5a). In contrast, in the outer surf zone and just offshore of the surf zone,
 599 the vorticity variance at large length scales decreases with directional spread (Figure 10b,
 600 squares, triangles, and linear fit with slope = $-0.6 \times 10^{-6} \text{ m}^{-1}\text{s}^{-2}$ and $-2.2 \times 10^{-6} \text{ m}^{-1}\text{s}^{-2}$,
 601 respectively), which may result from fluctuations of strong mean circulation features that
 602 extend farther offshore for simulations with variable bathymetry and less directional spread
 603 [O'Dea *et al.*, 2020].

604 For simulations with a range of alongshore bathymetric variability (the maximum
 605 alongshore standard deviation of the seafloor elevation, $\sigma_{y,sz}$), the vorticity variance at small
 606 length scales ($L < 100 \text{ m}$) is independent of bathymetric variability in the outer surf zone
 607 and just offshore of the surf zone (Figure 10c, triangles, squares, and linear fits with slopes
 608 = -0.2 and $-0.1 \times 10^{-4} \text{ m}^{-1}\text{s}^{-2}$, respectively), suggesting that small length-scale eddy
 609 generation is primarily a function of the incident wave field, rather than the surfzone bathy-
 610 metric variability. However, in the inner surf zone, higher variance of medium length-scale
 611 ($L = 80 - 100 \text{ m}$) eddies is present in the simulation with observed bathymetry ($\sigma_{y,sz} = 0.86$
 612 m) than in simulations with less alongshore variability (Figure 7d, 10c). The source of this
 613 additional variance is unknown, but may be related to instabilities of the mean circulation,
 614 which tend to have moderate to long length scales associated with the bathymetric variability
 615 [Tabeling *et al.*, 1990; Akkermans *et al.*, 2008; Geiman and Kirby, 2013].

616 In contrast to the vorticity variance at small length scales, which is not strongly de-
 617 pending on bathymetry, the eddy variance at large length scales ($L > 100 \text{ m}$) increases with
 618 alongshore bathymetric variability in all regions, particularly in the inner surf zone (Figure
 619 10d, circles and linear fit with slope = $5.0 \times 10^{-4} \text{ m}^{-1}\text{s}^{-2}$). There is a weaker increase in eddy
 620 variance with bathymetric variability in the outer surf zone and offshore of the surf zone
 621 (Figure 10d, squares, triangles, and linear fit with slopes = 2.5 and $0.7 \times 10^{-4} \text{ m}^{-1}\text{s}^{-2}$, re-
 622 spectively). The role of bathymetric variability in controlling surfzone vorticity at large spa-
 623 tial scales, shown here as a function of the cross-shore position in the surf zone and degree
 624 of alongshore bathymetric variability, is consistent with previous findings that compared the

625 average variance across the entire surf zone for alongshore-uniform and alongshore-variable
 626 bathymetry [O'Dea *et al.*, 2020].

627 The correlation of large-scale eddies with alongshore bathymetric variability, in con-
 628 trast to no correlation with directional spread, suggests that bathymetric variability influ-
 629 ences large-scale low-frequency fluctuations in the surf zone, possibly owing to enhanced
 630 eddy interaction and coalescence in depressions or troughs (Figure 1a) [Bühler and Jacob-
 631 son, 2001]. In addition, the highly variable observed bathymetry modulates wave breaking
 632 patterns, driving meandering mean currents (Figure 5a), which may pulsate at low frequen-
 633 cies and may shed large eddies [MacMahan *et al.*, 2004; Reniers *et al.*, 2007]. Eddy kinetic
 634 energy is intensified in the surf zone in simulations with bathymetric variability [Uchiyama
 635 *et al.*, 2017; O'Dea *et al.*, 2020]. Elevated eddy kinetic energy also is present outside of the
 636 surf zone, where oscillations in bathymetrically driven circulation patterns [*e.g.*, rip current
 637 jets, Smith and Largier, 1995; Haller and Dalrymple, 2001] or ejections of surfzone eddies
 638 [Feddersen, 2014] may result in higher variance at large eddy length scales.

639 4.2 Vertical Variability of the Vorticity Wavenumber Spectra

640 Although previous studies have quantified surfzone eddy variability with alongshore
 641 arrays of electromagnetic current meters at one elevation in the water column [Oltman-Shay
 642 *et al.*, 1989; Noyes *et al.*, 2004], the depth variability of eddies in the surf zone has been in-
 643 vestigated in only a few studies, and no previous numerical modeling experiments have in-
 644 vestigated the vertical variability of vortical motion with a fully three-dimensional phase-
 645 resolving model. Simulations with phase-averaged models have shown vertical structure of
 646 shear instabilities [Newberger and Allen, 2007a,b] and the effect of vortex tilting on the sur-
 647 fzone vorticity budget [Uchiyama *et al.*, 2017]. However, these models do not include wave-
 648 forced eddy generation, which is an important source of eddy energy and may influence the
 649 vertical structure of eddies [Zhao *et al.*, 2003; Newberger and Allen, 2007a].

650 Here, the energy levels of the alongshore wavenumber spectra of the simulated vertical
 651 vorticity decrease slightly from the surface to the seafloor, particularly for small length-scale
 652 eddies, and the mean eddy length scales (centroids of the spectra) increase (Figure 8, circles)
 653 in some locations in the nearshore for all simulations, indicating that eddies may exhibit ele-
 654 vation dependence for beaches with uniform or alongshore-varying bathymetry. The change
 655 in magnitude and mean length scale of $S_{\omega\omega}(z)$ with location within the water column may

656 be related to length-scale dependent attenuation and the combined effects of bottom bound-
 657 ary layer dynamics, vertical mixing, and the vertical distribution of shear instabilities [Zhao
 658 *et al.*, 2003; Boffetta and Ecke, 2012; Lippmann and Bowen, 2016], which could result in
 659 depth variation of eddy stretching and tilting, as seen in three-dimensional phase-averaged
 660 ROMS simulations [Uchiyama *et al.*, 2017]. The vertical dependence of $S_{\omega\omega}(z)$ may be sen-
 661 sitive to changes in the vertical eddy viscosity [Lippmann and Bowen, 2016] and the incorpo-
 662 ration of wave breaking related turbulence production [Feddersen and Trowbridge, 2005].

663 Simulations with alongshore-uniform bathymetry exhibit vertical variation at all length
 664 scales, whereas simulations with alongshore-variable bathymetry only have vertical vari-
 665 ation in the outer surf zone (compare Figure 8a-c with Figure 8d-f), indicating that bathy-
 666 metric variability may play a role in reducing the vertical dependence of large length-scale
 667 eddies. Although there is some vertical variation of eddies at all length-scales on alongshore
 668 uniform beaches (Figure 8d,e), on beaches with alongshore varying bathymetry the verti-
 669 cal dependence at small length scales decreases somewhat in the outer surf zone (Figure 8b)
 670 and is negligible in the inner and outer edge of the surf zone (Figure 8a,c). Thus, whereas
 671 small length-scale eddies may exhibit vertical dependence in the outer surf zone on beaches
 672 with large alongshore variability, larger length-scale eddies may be nearly depth-uniform on
 673 alongshore variable bathymetry.

674 4.3 Vertical Structure of Very Low-Frequency Motion

675 The three-dimensionality of very low-frequency (VLF) currents, which may impact
 676 material exchange and dispersion, is not well documented. Similar to the small number of
 677 observations of VLF motion vertical structure [Lippmann *et al.*, 2016; Henderson *et al.*,
 678 2017], VLF motion simulated with SWASH varies in the vertical near the bar crest (Figure
 679 9). Cross-shore energy density decays with depth, with over an 60% drop in squared co-
 680 herence over the water column, and with large phase shifts near the bottom (up to 50°) rel-
 681 ative to near-surface velocities [Lippmann *et al.*, 2016]. Simulated VLF velocities have weak
 682 vertical dependence of VLF motions near the outer edge of the surf zone with little vertical
 683 variation in shallower depths, broadly consistent with observations [Lippmann *et al.*, 2016;
 684 Henderson *et al.*, 2017].

685 Here, the simulated VLF motion exhibits vertical dependence in the outer surf zone,
 686 (e.g., immediately onshore of the bar crest, $0.75L_{sz}$, Figures 8b, 9), with decreasing vertical

687 dependence toward the inner surf zone. Furthermore, simulated VLF velocities are eleva-
 688 tion dependent for the terraced profile of S3a at $y \approx 850$ m (not shown), and for alongshore
 689 uniform bathymetry (S7, not shown). A theoretical model for eddy vertical dependence for a
 690 scenario with a depth-uniform alongshore mean current, constant eddy viscosity, no incorpo-
 691 ration of surface sheer stresses from wave breaking, and varying bottom friction [Lippmann
 692 and Bowen, 2016] suggests the vertical structure of eddies in the surf zone may result from
 693 instabilities and bottom boundary layer dynamics. These solutions, which include bottom
 694 friction and linearized lateral momentum advection, suggest that eddy vertical structure may
 695 depend on vertical mixing, eddy scales, and the magnitude of shear in a mean alongshore
 696 current, but do not address shear in the cross-shore current or the role of variability in wave
 697 forcing in a phase-resolved framework.

698 The analyses here build on previous studies to investigate surfzone eddy dynamics
 699 by examining the alongshore length scales at lower frequencies than surface gravity waves
 700 [Spydell and Feddersen, 2009; O'Dea *et al.*, 2020] and cross-shore profiles of VLF flows
 701 ($0.003 < f < 0.007$ Hz) [Lippmann *et al.*, 2016; Henderson *et al.*, 2017]. The vertical de-
 702 pendence of $S_{\omega\omega}(z)$ and VLF horizontal velocities is largest in the outer surf zone ($0.75L_{sz}$,
 703 Figures 8b,e, 9), and decreases toward the shoreline. Near $0.5L_{sz}$, the coherence with near-
 704 surface cross-shore flows decreases toward the seafloor (Figure 9b), whereas it was not pos-
 705 sible to fully assess the vertical dependence of the alongshore eddy length scales at $0.5L_{sz}$
 706 for the alongshore variable bathymetry because the varying water depths preclude computing
 707 $S_{\omega\omega}(k)$ for $z < 0.75$ m. The vertical dependence of $S_{\omega\omega}(k)$ and VLF velocities may be
 708 influenced by vertical eddy viscosity, bottom drag, and absence of breaking-wave-generated
 709 turbulence in SWASH simulations. Although simulations suggest that low-frequency mo-
 710 tions are primarily two-dimensional with some vertical structure, additional observational
 711 and numerical studies are necessary to understand the complex three-dimensional structure
 712 of VLF velocities in the surf zone, including the sensitivity of VLF velocities to wave condi-
 713 tions and surfzone bathymetries, and the implications for cross-shore exchange.

714 5 Conclusions

715 Simulations with a three-dimensional phase-resolving model (SWASH) reproduce
 716 the observed trends in wave transformation and the spatial patterns and magnitudes of the
 717 mean alongshore currents and meandering circulation on a barred beach with alongshore-
 718 inhomogeneous bathymetry. However, circulation features were sometimes shifted spatially

719 relative to the observations, and the simulated significant wave height was overestimated in
 720 the surf zone. The simulated surfzone circulation was sensitive to the bathymetry, which
 721 evolved during the field study.

722 The modeled dynamics include the horizontal and vertically-dependent structure of
 723 vortical motion in the surf zone. The alongshore eddy length scales were quantified using
 724 the alongshore wavenumber spectra of depth-averaged vorticity for simulations with differ-
 725 ent wave directional spreads and alongshore bathymetric variability. The variance of small
 726 length-scale eddies ($O(10)$ m) increases with directional spread and is independent of along-
 727 shore bathymetric variability in the outer surf zone and just offshore of the surf zone, sug-
 728 gesting that vortical motion with short alongshore length scales may be related to the inci-
 729 dent wave field, and in particular to forcing by short-crested wave breaking, consistent with
 730 previous findings [Spydell and Feddersen, 2009; Suanda and Feddersen, 2015]. The vari-
 731 ance of large length-scale eddies ($O(100)$ m) increases with alongshore bathymetric variabil-
 732 ity, indicating that alongshore bathymetric variability may intensify the formation of large
 733 length-scale eddies, in agreement with Boussinesq simulations with variability bathymetry
 734 [O'Dea *et al.*, 2020]. The variance of large length-scale eddies decreases with increasing di-
 735 rectional spread in the outer surf zone and just offshore of the surf zone, suggesting that the
 736 relationship between directional spread and large length-scale eddies is not well understood,
 737 but may be related to instabilities in the stronger mean circulation in cases with less direc-
 738 tional spread.

739 Modeled eddy length scales and low-frequency horizontal velocities were primarily
 740 two-dimensional with weak dependence on elevation in the outer surf zone, and occasionally
 741 in the inner surf zone for both uniform and alongshore-variable bathymetry. The magnitude
 742 of the alongshore wavenumber spectra of vorticity decreased, specifically at small length
 743 scales, and the mean length scale (spectral centroid) increased between the surface and the
 744 seafloor within the surf zone, whereas the vertical variation at the edge of the surf zone and
 745 just outside of the surf zone was small. The horizontal and vertical structures of very low-
 746 frequency (VLF) motions have complex patterns, including large drops in coherence and
 747 changes in phase between near-surface and subsurface flows. The vertical dependence of
 748 VLF velocities decreases from the outer surf zone toward the shoreline, broadly consistent
 749 with previous field studies [Lippmann *et al.*, 2016; Henderson *et al.*, 2017]. Further inves-
 750 tigation is necessary to understand the complex three-dimensional vertical and horizontal
 751 variability of low-frequency motions in the surf zone.

752 **Acknowledgments**

753 We thank the staff of the USACE Field Research Facility, Duck, NC and of the PVLAB at the
 754 Woods Hole Oceanographic Institution for helping deploy, maintain, and recover sensors, for
 755 providing data from long-term sensors, and for bathymetric surveys. Also, we thank Pieter
 756 Smit for assistance with the model setup, and Jim Thomson, Falk Fedderson, and other re-
 757 viewers for useful comments on the manuscript. Support was provided by the University of
 758 Washington Royalty Research Fund, the National Science Foundation, the Office of Naval
 759 Research, a National Defense Science and Engineering Graduate Fellowship, a Vannevar
 760 Bush Faculty Fellowship, the United States Army Corps of Engineers, the United States
 761 Coastal Research Program, Sea Grant, and the WHOI Investment in Science Program.

762 **6 Data Availability Statement**

763 Nearshore ADV data used in this study are available at Zenodo-url-in-prep (data archiv-
 764 ing on Zenodo is underway; for review, the data is uploaded temporarily as Supporting Infor-
 765 mation) and bathymetry, water levels, and offshore wave data are provided by the USACE
 766 at <https://frfdataportal.erdc.dren.mil/>. Model configuration files, MATLAB
 767 processing codes, and model output used to produce figures in this paper are available at
 768 <https://doi.org/10.5281/zenodo.4141219>.

769 **7 Appendix**

770 **A: Model description**

771 Simulating WAves till SHore (SWASH) is based on an explicit, second-order finite
 772 difference method for horizontally staggered grids, and conserves mass and momentum at
 773 discrete levels for an incompressible fluid with a constant density, which enables an efficient
 774 scheme to simulate individual wave propagation and breaking with high spatio-temporal res-
 775 olution [Zijlema and Stelling, 2005; Zijlema *et al.*, 2011]. The momentum equations are

$$\frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p_h + p_{nh}}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} - g \delta_{i3} \quad (\text{A.1})$$

776 and

$$\frac{\partial u_j}{\partial x_j} = 0 \quad (\text{A.2})$$

777 where x and u are the position and velocity in a Cartesian coordinate system ($i, j = 1, 2, 3$).

778 Here, t is time, ρ is density, g is gravitational acceleration, τ_{ij} are turbulent stresses, and p_h
 779 (p_{nh}) is hydrostatic, $\rho g z$ (non-hydrostatic, $\rho g(\eta - z)$) pressure components. The time evolu-

780 tion of the surface elevation is determined by continuity,

$$\frac{\partial \eta}{\partial t} + \frac{\partial}{\partial x_i} \int_{-h}^{\eta} u_i dz = 0 \quad (\text{A.3})$$

781 where h is the stationary bottom boundary, η is the moving free-surface, and z is the vertical
 782 coordinate ($x_i=3$). The surface and bottom kinematic boundary layers constrain particle
 783 motion, providing the constraints at the fixed bottom,

$$w|_{z=-h} = -u_i \frac{\partial h}{\partial x_i} \quad (\text{A.4})$$

784 and the free-surface,

$$w|_{z=\eta} = \frac{\partial \eta}{\partial t} + u_i \frac{\partial \eta}{\partial x_i} \quad (\text{A.5})$$

785 where w is the vertical velocity ($u_i=3$) and there is a constant pressure ($p_h = p_{nh} = 0$) and
 786 no surface stresses at the free-surface. The bottom boundary shear stress, τ_b is based on a
 787 quadratic friction law, with the drag coefficient, c_f determined from the Manning-Strickler
 788 formulation such that

$$c_f = 0.015(k/h)^{1/3} \quad (\text{A.6})$$

789 where k is the Nikuradse roughness height, set as 1 mm, within the range of values used in
 790 previous studies at this cite [Hsu *et al.*, 2006].

791 The turbulent stresses are obtained from a turbulent viscosity approximation ($\tau_{xx} =$
 792 $\nu_h \frac{\partial u}{\partial x}$, where ν_h is the horizontal eddy viscosity and $\tau_{xz} = \nu_v \frac{\partial u}{\partial z}$, where ν_v is the vertical
 793 eddy viscosity) [Smit *et al.*, 2013; Rijnsdorp *et al.*, 2017]. The horizontal eddy viscosity is
 794 approximated with the Smagorinsky model with a Smagorinsky constant of 0.1 [Smagorinsky,
 795 1963], and vertical mixing is approximated using the $k - \epsilon$ model, with k the turbulent
 796 kinetic energy per unit mass and ϵ the dissipation rate of turbulent kinetic energy per unit
 797 mass [Launder and Spalding, 1983]. The vertical eddy viscosity allows for diffusion of this
 798 stress into the water column, including coupling between vertical layers, and also increases
 799 numerical stability [Smit *et al.*, 2013]. A 10^{-3} m²/s background eddy viscosity was speci-
 800 fied to account for unresolved vertical mixing, enhancing stability in the model. This value is
 801 small compared with the vertical viscosity computed by the standard $k - \epsilon$ model. Although
 802 the breaking-induced turbulence is not directly implemented in SWASH, model simulations
 803 have shown that the turbulent kinetic energy below spilling breakers is well predicted [Rijns-
 804 dorp *et al.*, 2017].

805 The simulation stability was improved further by discretization with flux-limited (shock-
 806 resolving) vertical advective terms indicated with the first-order upwind scheme. At points
 807 where velocity is computed, the water depths are approximated with the Monotonic Upstream-
 808 centered Scheme for Conservation Laws limiter (MUSCL), a finite volume method that im-
 809 proves numerical accuracy. Non-hydrostatic pressure gradients in the vertical momentum
 810 equations are approximated with the Keller-box scheme [Lam and Simpson, 1976]. Explicit
 811 time integration is performed using a specified Courant number between 0.05 and 0.30, and
 812 the vertical time integration uses the implicit Euler Scheme.

813 SWASH simulates wave breaking using a hydrostatic front approximation, similar to
 814 disabling dispersive terms in the Boussinesq equations [Tissier *et al.*, 2012; Tonelli and Petti,
 815 2010], by prescribing a hydrostatic pressure distribution in the model around the discontinu-
 816 ity of a breaking wave. The turbulent wave-front is regarded as a sub-grid flow feature where
 817 the vertical accelerations are not resolved and the non-hydrostatic pressure is set to zero. The
 818 hydrostatic front approximation is initiated when local surface steepness exceeds a fraction of
 819 the shallow water celerity,

$$\frac{\partial \eta}{\partial x} > \alpha \sqrt{gh} \quad (\text{A.7})$$

820 where α is a parameterized value. The spatial persistence of wave breaking is achieved by
 821 labeling a mesh-point for hydrostatic computation if the neighboring grid point has been la-
 822 belled for hydrostatic computation and the local steepness exceeds a fraction of the shallow
 823 water celerity (Equation A.7) where the parameterized value is replaced with a coefficient
 824 β . In all simulations, wave breaking is controlled with a threshold parameter for initiation
 825 of wave breaking at a mesh-point, $\alpha = 0.6$ [Lynett Patrick J., 2006] and for the neighboring
 826 mesh-points, $\beta = 0.3$. This approach, combined with the conservation of momentum, leads
 827 to appropriate levels of energy dissipation on the front face of a breaking wave [Peregrine,
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