

- 1 Assessing the accuracy of density-independent demographic models for predicting
- 2 species ranges
- 3
- 4 **Keywords:** demographic distribution model, density-dependence, invasion risk map, matrix
- 5 population model, range dynamics, range shifts, species distribution model

6 **Abstract:**

7 Accurately predicting species ranges is a primary goal of ecology. Demographic distribution  
8 models (DDMs), which correlate underlying vital rates (e.g. survival and reproduction) with  
9 environmental conditions, can potentially predict species ranges through time and space.  
10 However, tests of DDM accuracy across wide ranges of species' life histories are surprisingly  
11 lacking. Using simulations of 1.5 million hypothetical species' range dynamics, we evaluated  
12 when DDMs accurately predicted future ranges, to provide clear guidelines for the use of this  
13 emerging approach. We limited our study to deterministic demographic models ignoring density  
14 dependence, since these models are the most commonly used in the literature. We found that  
15 density-independent DDMs overpredicted extinction if populations were near carrying capacity  
16 in the locations where demographic data were available. However, DDMs accurately predicted  
17 species ranges if demographic data were limited to sites with mean initial abundance less than  
18 one half of carrying capacity. Additionally, the DDMs required demographic data from at least  
19 25 sites, over a short time-interval (<10 time-steps), as populations initially below carrying  
20 capacity can saturate in long-term studies. For species with demographic data from many low  
21 density sites, DDMs predicted occurrence more accurately than correlative species distribution  
22 models (SDMs) in locations where the species eventually persisted, but not where the species  
23 went extinct. These results were insensitive to differences in simulated dispersal, levels of  
24 environmental stochasticity, the effects of the environmental variables, and the functional forms  
25 of density dependence. Our findings suggest that deterministic, density-independent DDMs are  
26 appropriate for applications where locating all possible sites the species might occur in is  
27 prioritized over reducing false presence predictions in absent sites. This makes DDMs a

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**Deleted:** that ignore density dependence (1) accurately predict range dynamics for small, fast-growing populations, but (2) overpredict extinction for slow-growing populations, and (3) overpredict

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**Deleted:** . For fast-growing populations, demographic distribution models accurately predict occurrence as long as the population is at <65% of carrying capacity in the sites where the demographic data are collected. For slow-growing populations, DDMs greatly overpredict extinction

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53 promising tool for mapping invasion risk. However, demographic data are often collected at sites

54 where a species is abundant. Density-independent DDMs are inappropriate in this case.

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## 61 Introduction

62 Spatial projections of species occurrence and persistence are essential for developing ecological  
63 theory and improving environmental management (Guisan et al. 2013, Meyer et al. 2015,  
64 Briscoe et al. 2019). While scientists and environmental agencies commonly correlate static  
65 presence/absence data with environmental variables to project species ranges (Elith and  
66 Leathwick 2009, Guisan et al. 2013, Hijmans et al. 2017), the accuracy and utility of these  
67 projections have been criticized, especially when projecting distributions in time or to novel  
68 environments (Pearson and Dawson 2003, Thuiller et al. 2014, Zurell et al. 2016, Cabral et al.  
69 2017, Briscoe et al. 2019). Unfortunately, due to current, rapid, environmental change,  
70 projections in time and to novel environments are urgently needed (Ackerly et al. 2010).  
71 Demographic distribution models (DDMs), which model vital rates, such as survival,  
72 development, and reproduction, as functions of environmental variables, have been proposed as a  
73 promising alternative for generating these projections (Merow et al. 2014, 2017, Zurell et al.  
74 2016, Briscoe et al. 2019). DDMs are promising because they model the underlying mechanisms  
75 that drive occurrence (Normand et al. 2014, Cabral et al. 2017), mechanisms which may continue  
76 to hold in new environments. Yet the accuracy and limitations of DDMs are poorly understood.

77 The first step to building a DDM is regressing vital rates against environmental factors to  
78 determine trajectories of population size through time, which then may be projected into the  
79 future to predict species occurrence and abundance (Villellas et al. 2015, Ehrlén et al. 2016,  
80 Cabral et al. 2017, Csergő et al. 2017). This explicit focus on capturing how environmental  
81 variables on vital rates differs from other approaches using demographic models to to project  
82 species' ranges. For example, coupled niche-population models use stochastic demographic  
83 models to project range dynamics, but vital rates are typically fixed, with environmental effects

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84 captured by constraining potential habitat and carrying capacity based on modelled habitat  
 85 suitability (Keith et al. 2008, Fordham et al. 2013, 2018). Such approaches allow one to  
 86 explicitly project range dynamics with limited demographic data across sites, but their reliance  
 87 on occurrence data to model environmental constraints means that they can suffer from many of  
 88 the same drawbacks as correlative SDMs (Briscoe et al. 2019). Unfortunately, DDMs also have  
 89 important drawbacks. Even the simplest DDMs require population abundance data through time  
 90 (Buckley et al. 2010), or detailed demographic data tracking many individuals and their offspring  
 91 within a field season (Merow et al. 2014). In both cases, these data must be collected at multiple,  
 92 geographically, and climatically dissimilar sites, and classified by age, and/or size of  
 93 development (Caswell 2001, Needham et al. 2018). This requirement of spatial and temporal  
 94 replication is challenging in its own right. Therefore, DDMs typically ignore the effect of  
 95 intraspecific competition on survival or reproduction, despite tools for incorporating density-  
 96 dependence effects in demographic models (Cushing et al. 2002, Dahlgren et al. 2014, Teller et  
 97 al. 2016). To our knowledge, the vast majority of DDMs, parameterized with field data, to  
 98 project species ranges, ignore density-dependent effects (Buckley et al. 2010, Barbraud et al.  
 99 2011, Merow et al. 2014, 2017, Sheth and Angert 2018, Needham et al. 2018) but see (Pagel et  
 100 al. 2020) for an exception. Such density-independent DDMs predict occupancy by linking  
 101 environmental variables to long-term population growth rate,  $\lambda$ , through the variables' effects on  
 102 vital rates in matrix-population or integral-projection models (Buckley et al. 2010, Merow et al.  
 103 2014, 2017). The implicit logic is that if  $\lambda > 1$ , the local population is predicted to persist; if  $\lambda < 1$ ,  
 104 the population is predicted to go locally extinct in the long-term.

105 However, estimates of  $\lambda$  from density-independent demographic models do not  
 106 necessarily reflect long-term persistence if the population experiences density-dependent

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108 survival, development, and/or fecundity. If fecundity or survival are lower at high population  
109 densities due to, for example, competition for resources, populations can approach a long-term  
110 equilibrium abundance – which we will refer to as carrying capacity. It is likely that  
111 demographers often collect data where populations are abundant, *i.e.* close to carrying capacity  
112 (Quintana-Ascencio et al. 2018, Fournier et al. 2019). This is because large populations are  
113 easier to find and researchers often go where healthy populations are known to exist, not to  
114 fringe populations, likely to produce small datasets. However, in healthy populations near  
115 carrying capacity, there may be limited population growth, even if the site is highly suitable.  
116 Demographic models fit to data from these sites should produce  $\lambda \sim 1$ , and therefore, an estimate  
117 of  $\lambda < 1$  could simply reflect measurement error, disturbance, or temporary declines after  
118 populations exhausted their resources. In short, if demographic data are collected in field sites  
119 where the species is abundant, a density-independent DDM using these data could erroneously  
120 map prime habitat as uninhabitable. Therefore, it is no surprise that empirical studies often find  
121 estimates of  $\lambda$  uncorrelated or even negatively correlated with habitat suitability or species  
122 occurrence (Diez et al. 2014, Thuiller et al. 2014, Csörgő et al. 2017). In contrast, there are at  
123 least two cases of density-independent DDMs built from demographic data restricted to sites  
124 with small populations (e.g. an invasive species and species experiencing high levels  
125 disturbance). In these cases,  $\lambda$  successfully predicted species occurrence (Merow et al. 2014,  
126 2017).

127       Given the mixed success of initial attempts to predict species ranges using density-  
128 independent demographic models, we set out to determine general guidelines for when these  
129 models can predict species occupancy accurately. We achieved this by simulating range dynamic  
130 data, and observers sampling the data to build DDMs. We then compared DDM predictions

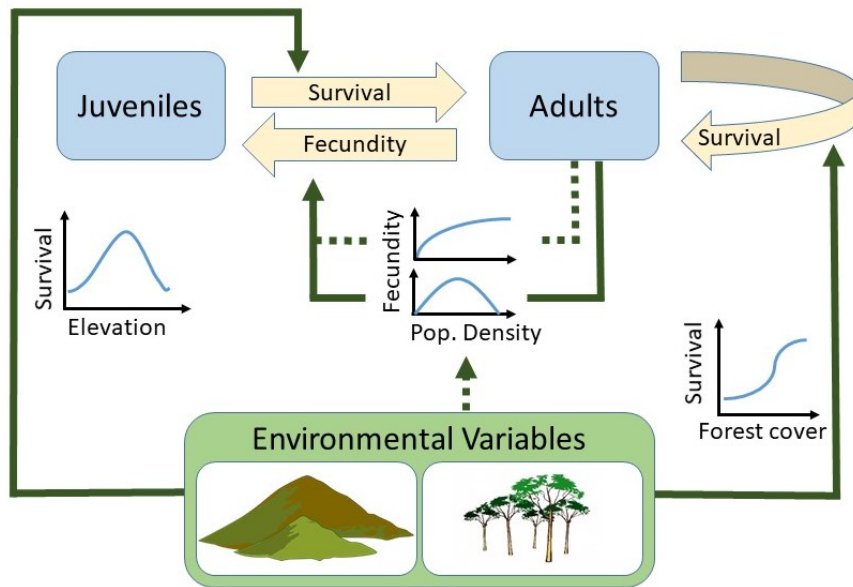
131 against long term occupancy, assessed DDM accuracy, and correlated DDM accuracy with  
132 various species and population characteristics. Finally, we compared DDM predictions to  
133 predictions from standard correlative species distribution models (SDMs). In face of limited data  
134 available to validate predictions of species range dynamics, our simulated approach provides a  
135 tool for assessing DDM accuracy. Our computational framework has many advantages over  
136 traditional validation and sensitivity analyses using real-world data, including: increased  
137 repeatability, transparency, sample sizes, and control over environmental and historical factors  
138 (Zurell et al. 2010) – all of which help improve the generality of the results.

## 139 Material and methods

140 Our study involved three separate processes: (1) simulating population dynamics for hypothetical  
141 species using a stochastic, negative density-dependent, spatially-explicit, stage-structured  
142 population model with two life stages (juvenile, adult) and juvenile dispersal (see Fig 1 for a  
143 graphical description of the model); (2) simulating sampling by field workers conducting  
144 demographic surveys across a subset of the species' habitat; and (3) fitting demographic  
145 distribution models, computed from the sampled field data. To determine the characteristics of  
146 species that can successfully be modeled using demographic distribution models, we simulated  
147 the range dynamics of 1.5 million hypothetical species that differed in their maximum survival  
148 rates at each life stage, maximum fecundity at low densities, maximum carrying capacity,  
149 response to environmental variables, stochastic variability in survival, initial population  
150 densities, and proportion of the population that disperses at each time step. We then determined  
151 if we could draw general conclusions about the species for which DDMs made accurate vs.  
152 inaccurate predictions of species occurrence.

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**Fig 1.** A graphical depiction of the simulation model. Solid dark arrows represent the effects of environmental variables and population density on vital rates (thick yellow arrows) in the baseline scenario. Dashed arrows are for effects absent in the baseline scenario, but which are tested in the sensitivity analysis. Blue curves show the assumed functional relationships between the variables. Note that both elevation and forest cover affect survival in both life stages, but repeated arrows are omitted to improve readability. For the beverton-Holt and logistic fecundity curves, the fecundity axis is total offspring (this is rescaled to expected per-capita offspring in the model description).

168

## 169 Simulated population dynamics - survival

170 We simulated population dynamics using a simple stochastic model. The probability of survival  
171 for an individual in life stage  $s$  and site  $i$ ,  $\varphi(i, s)$ , was a function of life stage, and environmental  
172 conditions,

$$\varphi(i, s) = \frac{\psi_s e^{u(i, s)}}{1 + e^{u(i, s)}}, \quad (\text{eqn. 1})$$

$$u(i, s) = \sum_{j=1}^{n_e} (\alpha_{1,s,j} x_{i,j} + \alpha_{2,s,j} x_{i,j}^2) + \alpha_0 + \epsilon_{i,s,t}. \quad (\text{eqn. 2})$$

173 In the above equations,  $x_{i,j}$  is the value of environmental variable  $j$  in site  $i$ , ( $j = 1, \dots, n_e$ ), where  
174  $n_e$  is the number of environmental variables. The parameter  $\psi_s$  is the maximum expected  
175 survival probability in life stage  $s$ . The functional form in (eqn. 1) maps linear and quadratic  
176 combinations of the environmental variables,  $u$ , to survival, so that survival is always bounded  
177 between 0 and  $\psi_s$ . The coefficient  $\alpha_{1,s,j}$ , is the linear trend between the link to survival, of life  
178 stage  $s$ , and the environmental variable  $j$ , whereas  $\alpha_{2,s,j}$  is the quadratic trend. If the quadratic  
179 coefficient is negative,  $\alpha_{2,s,j} < 0$ , survival is maximized at intermediate values of environmental  
180 variable  $j$ , along its gradient, to resemble first principles of the Hutchinsonian niche concept  
181 (Holt 2009). Whereas, if  $\alpha_{1,s,j} > 0$ , and  $\alpha_{2,s,j} = 0$ , then increases in environmental variable  $j$   
182 strictly increase survival. Spatial and temporal variation in survival during life stage  $s$ , not  
183 attributable to the environmental variables,  $x_{i,j}$  is given by,  $\epsilon_{i,s,t}$ , a random variable with zero  
184 expectation. The intercept,  $\alpha_0$ , is set to zero throughout the paper with no loss of generality.

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## 186 Simulated population dynamics - fecundity

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191 As standard in ecological modeling and environmental management (Quinn II and Deriso 1999),  
 192 we incorporated density-dependence in simulated fecundity. We considered two of the most  
 193 widely used types of negative density-dependence in the literature. The first was logistic  
 194 fecundity, where the expected number of juvenile offspring was determined by the logistic model  
 195 (May 1974). This represented scramble competition, where population sizes above carrying  
 196 capacity cause declines in total viable offspring. The second was Beverton-Holt (aka. reciprocal  
 197 yield) density dependence (Shinozaki and Kira 1956, Beverton and Holt 2012). This represented  
 198 contest competition, decreasing per-capita fecundity, but increasing total fecundity, with respect  
 199 to population size. Both of these fecundity functions were parameterized with the variables  $f_{max}$   
 200 and  $k_i$ , per capita fecundity at low adult abundance and adult carrying capacity in site  $i$ ,  
 201 respectively. We refer to the fecundity function in site  $i$  as  $f_i(n)$ , where  $n$  is the number of adults  
 202 in the given site and time. Note, however, that we did not consider Allee effects and use density-  
 203 dependence synonymously with strict negative density dependence. For details on the functional  
 204 forms and parameterization of these standard ecological models, see appendix A.

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## 206 **Simulation algorithm**

207 We considered a population with two life stages, juvenile ( $s = 0$ ) and adult ( $s = 1$ ), and assumed  
 208 juveniles became adults after one time step or died in that period of time. Therefore,  $\varphi(i, 0)$  was  
 209 the probability of a juvenile in site  $i$  transitioning to an adult and,  $1 - \varphi(i, 0)$  was the associated  
 210 mortality probability. The unit of each time step was one iteration of the demographic model,  
 211 often thought of as one year (Salguero-Gómez et al. 2016). However, for generality, we do not  
 212 specify the time unit since the species are hypothetical.

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216 Note that a deterministic version of this simulation, without dispersal, is equivalent to  
 217 simulating a standard matrix population model governed by the density-dependent Lefkovitch  
 218 matrix (Caswell 2001),

$$\begin{bmatrix} 0 & f_i(n) \\ \varphi(i, 0) & \varphi(i, 1) \end{bmatrix}, \quad (\text{eqn. 3})$$

219  
 220  
 221 where,  $f_i(n)$  is per-capita adult fecundity, and with survival probabilities  $\varphi(i, 0)$  and  $\varphi(i, 1)$ ,  
 222 determined by eqn 1. Therefore, one can predict the persistence of the population (in an  
 223 analogous deterministic scenario) by the leading eigenvalue of the linearized system at the  
 224 extinction equilibrium, e.g. the eigenvalue of,

$$\begin{bmatrix} 0 & f_{max} \\ \varphi(i, 0) & \varphi(i, 1) \end{bmatrix}, \quad (\text{eqn. 4})$$

225  
 226 which yields an expected long-term population growth rate, at low population densities, in site,  $i$ ,  
 227

$$\lambda_i = \frac{1}{2} \left( \varphi(i, 1) + \sqrt{\varphi(i, 1)^2 + 4f_{max}\varphi(i, 0)} \right). \quad (\text{eqn. 5})$$

228  
 229 If  $\lambda_i < 1$ , a population in site  $i$  will eventually go extinct without dispersal from other sites or a  
 230 series of random favorable years; similarly, if  $\lambda_i > 1$ , the population will persist in the absence  
 231 of random fluctuations.

232  
 233 The full stochastic simulation, including dispersal, involved four steps. We:

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1. Drew the number of surviving juveniles that became adults in the next time step, in each site, from a binomial distribution with the number of trials equal to the number of juveniles in the previous time step and probability of survival,  $\varphi(i, 0)$ ;
2. Drew the number of surviving adults in each site, from a binomial distribution with the number of trials equal to the number of adults in the previous time step and probability of survival,  $\varphi(i, 1)$ ;
3. Drew the number of new juveniles from a Poisson distribution with expectation  $f_i(n)n$  [See Appendix A for details about the fecundity function  $f_i(n)$ ]
4. Randomly selected a fraction of new juveniles (offspring in step 3),  $p_d$ , to disperse, where each dispersing individual has an equal probability of landing in each site.
5. Updated the total number of adults to equal the surviving adults plus the surviving juveniles (new adults), and updated the total number of juveniles as the new juveniles from reproduction, accounting for offspring entering and exiting the site, due to dispersal.

## Simulation scenarios

The main goal of the study was to test how different species varying in survival rates, fecundity, dispersal, responses to environmental variables, stochasticity, and initial abundance affect the accuracy of demographic distribution model (DDM) predictions. We first calculated DDM performance for a baseline scenario, with logistic fecundity, and parameters set to values in Table 1. We then performed a sensitivity analysis, where we simulated the population dynamics and fit distribution models under 1,000 random combinations of parameter values, each under the two different density-dependent fecundity functions, [three correlation structures](#)

between fecundity and survival, and three different ways of distributing initial population density in space, each containing approximately 50 different density distributions. This created 1.5 million experiments, each over 4,915 sites and two age-classes (over 145-billion time series).

In both the baseline and the sensitivity analysis, we simulated population dynamics of hypothetical species over 4,195, 10 km<sup>2</sup>, sites in Switzerland, affected by elevation,  $x_{i,1}$ , and forest cover,  $x_{i,2}$  (Fig. S1ab), standardized to zero mean and unit standard deviation (Kéry et al. 2017). We let  $\epsilon_{i,s,t}$  be independently, identically, normally distributed with mean 0 and standard deviation,  $\sigma$ . Site-specific carrying capacity,  $k_i$ , was set to maximum abundance,  $k_{max}$ , times the proportion of the site covered by forest. In sites with  $k_i < 5$ , we set carrying capacity to zero, to represent too little habitat for a persistent, long-term population. We set initial abundances in sites where the species would persist in the absence of stochasticity (sites with  $\lambda_i > 1$ ) to specified proportions of carrying capacity. We randomly selected 5% of sites where forest cover was high enough to yield carrying capacity above 10 individuals, but where survival was too low to maintain a long term viable population (sites with  $\lambda_i < 1$ ) and set their initial adult abundances to 10 individuals, to represent invaded sink populations. There were 200 time-steps in the simulations.

For the sensitivity analysis (see Table 1), maximum adult and juvenile survival,  $\psi_1$  and  $\psi_0$ , were assigned random values uniformly drawn between 0.01 and 0.99. This wide range includes slow-growing, long-lived species and fast-growing, short-lived species. The linear effect of forest cover on survival,  $\alpha_{1,s,1}$ , was randomly drawn from a uniform distribution from 0 to 3. To produce ecologically sensible, yet wide ranges for the effect of elevation on survival, we drew the quadratic elevation effect,  $\alpha_{2,s,1}$ , from a uniform distribution from -3 to 0, and then also drew a preferred elevation,  $v$ , uniformly over the entire elevation range in the data, and chose the

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287 linear elevation effect to maximize survival at this preferred elevation, namely,  $\alpha_{1,s,1} =$   
 288  $-2v\alpha_{2,s,1}$ . A quadratic factor of zero represented species that could survive across all observed  
 289 elevations equally, whereas -3 was for species that could only tolerate a narrow range of  
 290 elevations.

291 We considered three scenarios for maximum viable offspring at low population densities,  
 292  $f_{max}$ , (1) positively correlated with survival, (2) negatively correlated with survival, and (3) fixed  
 293 across sites. For the fixed case, in each of the 1,000 parameter sets,  $f_{max}$  was randomly drawn  
 294 from a uniform distribution ranging between the lowest possible number such that the species  
 295 would be expected to persist in at least 5% of sites (i.e.  $\lambda_i > 1$ ), and the largest possible number  
 296 for which carrying capacity was guaranteed to be a stable equilibrium at the most favorable site,  
 297 given  $\psi_1$ ,  $\psi_0$ , and the effects of environmental variables (which were drawn first). The last  
 298 constraint simply eliminated the possibility of chaotic and unstable, periodic dynamics, and was  
 299 determined through standard linear stability analysis (Strogatz 1994) techniques (see Appendix  
 300 B). In the correlated case,  $f_{max}$  was different at each site according to the environmental variables  
 301 at that site. This was achieved by drawing a number between the maximum and minimum values  
 302 for  $f_{max}$  described above, for each site, using a beta distribution, with beta distribution parameters  
 303 as a function of environmental variables. This made  $f_{max}$  more likely to be high in sites with high  
 304 survival, and low in sites with low survival (see the section “environmentally driven fecundity  
 305 scenarios” in Appendix B for details). The negatively correlated scenario was achieved similarly  
 306 (Appendix B).

307 The standard deviations of environmental stochasticity and the dispersal proportion were  
 308 uniformly randomly generated on (0, 0.5) and (0, 0.05), respectively, to represent wide ranges for  
 309 the types of species an ecologist would consider fitting a deterministic demographic model

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without dispersal. Maximum carrying capacity across all sites,  $k_{\max}$ , was also uniformly distributed.

We considered three different scenarios for how initial population sizes were distributed through space: (1) fixed initial abundances at all sites where the species was expected to persist were varied factorially with each parameter combination, using 51 values between 5% and 135% of local carrying capacity; (2) initial abundance set at 25, 50 and 75% of the carrying capacity in a fixed proportion of sites and carrying capacity in the other sites (varied across all possible proportions); and (3) uniformly distributed abundance, with 46 mean values [from 52.5%, corresponding to a lower bound of 5%, to 100% of carrying capacity].

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324 **Table 1.** A list of parameters used in the species range dynamics [baseline](#) simulations ([third](#)  
325 [column](#)), which are perturbed in the sensitivity analysis ([fourth column](#)) to test the generality of  
326 results for different types of hypothetical species.

Parameter	Description	Baseline Value	Range tested
$\psi_0$	Maximum juvenile survival	0.5	0.01 – 0.99
$\psi_1$	Maximum adult survival	0.5	0.01 – 0.99
$\alpha_{1,s,1}$	Linear forest cover effect of stage $s$ survival	0.5	0 – 3
$\alpha_{1,s,2}$	Linear elevation effect on stage $s$ survival	0.5	-5 – 23*
$\alpha_{2,s,2}$	Quadratic elevation effect on stage $s$ survival	-0.5	-3 – 0
$p_d$	Dispersal proportion per time step	0.01	0 – 0.05
$\sigma$	Standard deviation of environmental stochastic effect on survival	0.25	0 – 0.5
$f_{max}$	Fecundity at zero density, i.e. maximum fecundity [surviving offspring / adult]	4	0.1 – 250
$k_{max}$	Maximum carrying capacity (at a site with 100% forest cover) [number of adults]	1,000	500 – 1,000

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327 \*chosen to maximize survival at a uniform randomly chosen preferred elevation, over all  
328 possible elevations in the data, given a random quadratic elevation effect, drawn from the range  
329 in the row below.  
330

### Simulated field sampling

We assumed that simulated population dynamics represented the true population, and sampled from this population by simulating a demographer using common field-sampling methods (Zurell et al. 2010). Sampling occurred for ten time-steps from the start of the simulation with dispersal turned off, to simplify the analysis and mimic a situation where the researcher can account for the origin of individuals in the site. The virtual ecologist randomly chose  $n_s$  sites where the species was present at the beginning of the simulation and then counted the number of surviving juveniles (new adults), surviving adults, and new juveniles, at each sampled site, over ten time-steps. While this is a standard approach (Lavine et al. 2002), an alternative, but more laborious and computationally expensive, approach, would model individual organisms, and track a sampled subset of these individuals. Tracking individuals is advantageous if one wants to quantify individual variability in demographic processes, but this was not a focus of our study. Also, considering we were analyzing nearly five-billion time series, computational efficiency was required to make sure results were general across species. We set  $n_s = 200$  sites, representing a highly optimistic, but realistic sample size. For example, previously, DDMs have used 138 sites (Merow et al. 2014). We selected a high value because the purpose of the study was to identify species for which DDMs could generate useful predictions given high-quality data, but we also tested DDM accuracy for scenarios with 50, 30, 25 and 20 sampled sites. We set the length of demographic surveys to two years, but we also tested survey lengths of three, five, 10 and 20 years.

### Distribution models

354 The demographic distribution model (DDM) assumed that the population dynamics in site  $i$  were  
 355 governed by a two-stage matrix population model. While a variety of density-independent  
 356 demographic models have been used to build DDMs in the literature, including integral  
 357 projection models (Merow et al. 2014, 2017) and matrix population models (Buckley et al.  
 358 2010), we chose a matrix approach for both the simulation and fitted DDM because it is the  
 359 simplest and most computationally efficient model that maintains the essential demographic  
 360 features of structured population dynamics. The fitted model was,

$$N_{i,t+1} = A_i N_{i,t};$$

(eqn. 6)

$$A_i = \begin{bmatrix} 0 & f(x_{i,1}, x_{i,2}) \\ \phi_0(x_{i,1}, x_{i,2}) & \phi_1(x_{i,1}, x_{i,2}) \end{bmatrix},$$

361 where  $A_i$  is a transition matrix for site  $i$ , and  $f(x_{i,1}, x_{i,2})$ ,  $\phi_0(x_{i,1}, x_{i,2})$ , and  $\phi_1(x_{i,1}, x_{i,2})$  are the  
 362 estimated fecundity, juvenile and adult survival in site  $i$ , respectively. Note these are functions of  
 363 the two environmental variables in site  $i$ ,  $x_{i,1}$ , and  $x_{i,2}$ . The estimation of  $f(x_{i,1}, x_{i,2})$ ,  
 364  $\phi_0(x_{i,1}, x_{i,2})$ , and  $\phi_1(x_{i,1}, x_{i,2})$  was performed using a statistical model. From the simulated field  
 365 sampling of demographic data, we computed the observed per-capita fecundity, number of  
 366 surviving adults, and juveniles over the sampling period. These quantities were uniquely  
 367 determined because we turned off dispersal during the period of demographic sampling. This  
 368 procedure created a vector of observed juveniles survived, adults survived, and fecundity, each  
 369 with the number of entries equal to the number of sites. The functions  $\phi_0$ ,  $\phi_1$ , and  $f$ , were then  
 370 estimated using generalized additive models, function 'gam' in R (Wood 2017). The generalized

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382 additive models assumed binomially distributed counts of surviving adults and juveniles and  
 383 Poisson distributed total offspring with a rate parameter equal to an estimated parameter, based  
 384 on environmental predictors, times the number of adults at the site. The estimated parameter was  
 385 therefore expected per-capita fecundity. We restricted total offspring predictions to the range of  
 386 observed values to avoid issues extrapolating beyond the data, as is common in distribution  
 387 modelling (Stohlgren et al. 2011, Owens et al. 2013).

388 The DDMs predicted a unique matrix,  $A_i$ , for every site based on the environmental  
 389 variables at that site. We used the predicted  $A_i$  to calculate the long-term population growth rate,  
 390  $\lambda_i$ , by computing  $A_i$ 's leading eigenvalue. Following standard practice for DDMs (Merow et al.  
 391 2014, 2017), we interpreted  $\lambda_i$  as a measure of persistence, where  $\lambda_i < 1$  predicted eventual  
 392 extinction and  $\lambda_i > 1$  predicted long-term persistence at a given site. We then compared the  
 393 predicted  $\lambda_i$  values to the presence of the species, 200-time steps after demographic sampling, to  
 394 determine whether DDM predictions of persistence were correlated with long-term persistence at  
 395 a site. Note that, throughout the paper, we refer to  $\lambda_i$  as long-term population growth rate from  
 396 the fitted DDM, whereas  $\lambda_i$  is the expected population growth rate from a deterministic version  
 397 of the true model used to simulate the data.

398 We also compared how accurately the DDMs predicted occupancy in comparison to  
 399 correlative species distribution models (SDMs). SDMs were generalized additive models,  
 400 predicting the probability of species' presence given presence/absence data and environmental  
 401 variable values, at the  $n_s$  sampled sites, at the end of demographic sampling. In cases where the  
 402 generalized additive models did not converge (less than 0.1 percent of scenarios), for both the  
 403 DDM and SDM, we used generalized linear models with similarly distributed error. To calculate

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- Deleted: Survival data was coerced between 0.0001 and 0.9999 instead of zero and one to prevent division by zero or taking the log of zero in the logit transformation
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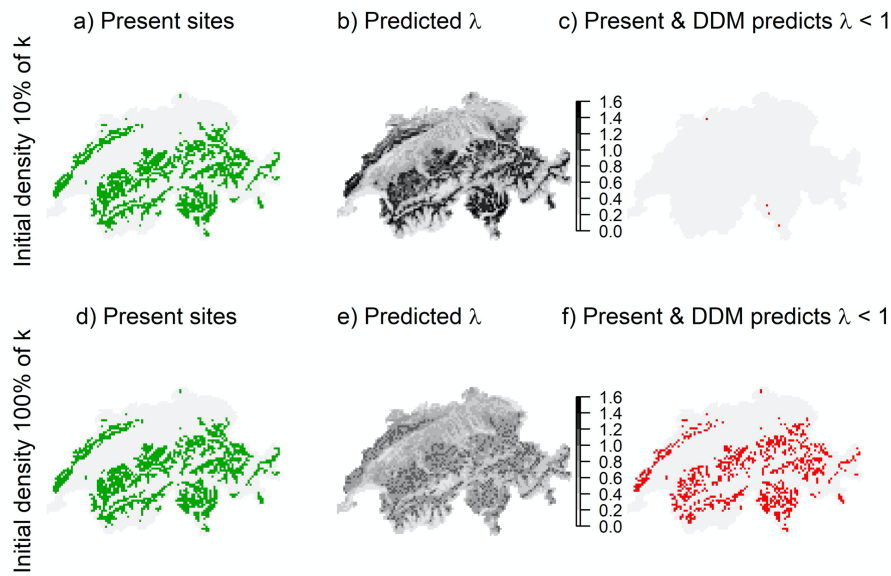
419 the prediction accuracy of the SDM we considered sites to be predicted present when the  
420 modeled probability of presence was greater than 0.5.  
421

## Results

For the baseline scenario, with all parameters set to intermediate values, and initial population sizes in each site set to 10% of local carrying capacity, the DDM performed well. For 95.1% of the 3,518 sites where the population went extinct (light grey in Fig. 2a), the DDM predicted  $\lambda_i < 1$  (Fig. 2b). For the 1,397 sites where the species was present at the end of the simulation (green in Fig. 2a), the DDM predicted  $\lambda_i > 1$  in 99.7% of these sites. The lack of red pixels in Fig. 2c denotes the 0.3% of present sites where the DDM incorrectly predicted  $\lambda_i < 1$ .

In the same baseline scenario, but with initial populations at carrying capacity during the start of demographic sampling, the DDM over-predicted extinction (Fig. 2 d-f). For the 1,415 sites where the species was present at the end of the simulation, the DDM predicted  $\lambda_i > 1$  at only 39.0% of the sites. On the other hand, out of the 3,500 sites where the population went extinct (light grey in Fig. 2d), the DDM correctly predicted  $\lambda_i < 1$ , 97.3% of the time (Fig. 2d). This means the DDM predicted the status of absent sites well regardless of population density at demographically sampled sites.

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**Fig. 2.** Maps of occupancy and predicted population growth rate,  $\lambda$ , from the Demographic Distribution Model (DDM) of a virtual species in Switzerland, given demographic data sampled from sites with low (top row) and high (bottom row) population densities, showing an over prediction of extinction when demographic data come from locations at carrying capacity. (a, d) Map of occupancy at the end of the simulation, (b, e) predicted population growth rate  $\lambda$  from the DDM, and (c, f) sites where present populations at the end of the simulation are incorrectly predicted by the DDM to be absent. The initial population sizes at sampled sites were at 10% of carrying capacity in row 1 (a-c) and at 100% of carrying capacity in row 2 (d-f), for the baseline parameterization. When demographic samples were conducted at sites where the populations were at 10% of carrying capacity, the DDM correctly predicted all present sites as present, whereas the DDM only correctly predicted 56.1% of present sites when demographic sampling occurred at carrying capacity.

449 To summarize, in the baseline scenario, DDMs predicted present sites accurately if initial  
450 density during sampling was close to zero, and inaccurately for initial density at carrying  
451 capacity. However, for what initial density in sampled sites, between 10% and 100% of carrying  
452 capacity, do predictions cease to be accurate at present sites? To identify the critical population  
453 density to achieve a specified target percentage of correctly predicted present sites, we ran the  
454 above simulation with initial densities of 5% to 135% of carrying capacity (Fig. 3) and computed  
455 the proportion of present sites where the DDM predicted  $\lambda_i > 1$  for each initial density (black dots  
456 in Fig. 3). The black dots in Fig. 3 formed a clear monotonic decreasing pattern, and we fit a  
457 smooth curve to these data (curve in Fig. 3, see Appendix C for details on curve fitting methods).  
458 We then computed the critical population abundance as the intersection of this curve with the  
459 specified target prediction accuracy (Fig. 3). A critical initial population size of 94.2% of  
460 carrying capacity was required to achieve a prediction accuracy of 80% in present sites (circle in  
461 Fig. 3). The critical population abundance needed to correctly predict 90% of present sites was  
462 90.1% of carrying capacity (square in Fig. 3). Unlike true presence predictions, correctly  
463 predicting absent sites was not strongly related to population density, which we discuss further in  
464 the results of the sensitivity analysis.  
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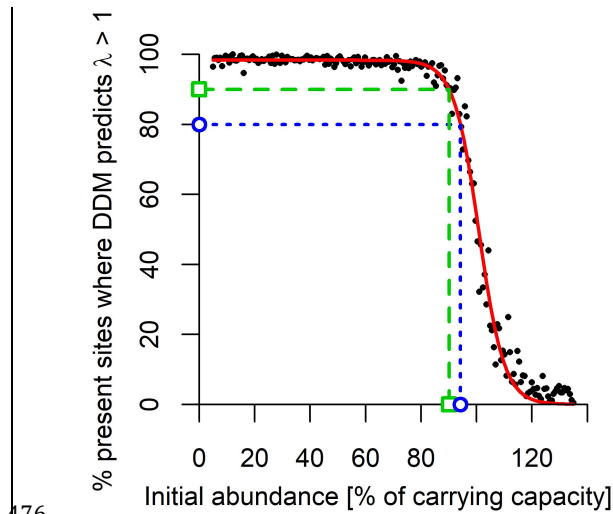
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477 **Fig. 3.** The probability that the DDM correctly predicted species' presence [at present sites](#)  
 478 declined as population size, relative to carrying capacity, increased at sampled sites. Each black  
 479 dot is the proportion of occupied sites at the end of a single simulation where the DDM predicted  
 480  $\lambda_i > 1$ , given an initial population size, during demographic sampling, specified by the x-axis. The  
 481 red line is a fitted smooth monotonic curve to these data. The green square and blue circle on the  
 482 x-axis are the critical initial population sizes (90.1%, and 94.2% of carrying capacity,  
 483 respectively) required, during demographic sampling, to achieve a 90% and 80% [chance](#) of  
 484 correctly predicting occupied sites at the end of the simulation. All parameters were set to their  
 485 baseline, and the fecundity function was logistic. Absent sites were always predicted absent by  
 486 the DDM with 96-100% accuracy regardless of initial population abundance in sampled sites and  
 487 hence are not displayed here.

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490 To demonstrate that Fig. 3 was not an artefact of the baseline parameterization chosen, we  
 491 then proceeded to calculate the critical population abundance, as in Fig. 3, for every parameter  
 492 combination, fecundity function, and correlation scenario in the sensitivity analysis. We set the  
 493 true presence accuracy threshold equal to 80% accuracy, a round number close to the 79%  
 494 prediction accuracy reported from past empirical DDMs (Merow et al. 2014). A histogram of  
 495 critical population abundances across all parameter combinations tested, under both fecundity  
 496 functions and all three correlation scenarios, shows that high critical initial population sizes (80-  
 497 95% of carrying capacity) at demographically sampled sites were the most common (Fig. 4).  
 498 This means that DDMs predicted presence accurately even when abundances at sampled sites  
 499 were intermediate rather than small. However, in the fixed fecundity scenario, when maximum  
 500 fecundity was not spatially correlated with survival, the DDMs did not accurately predict  
 501 occupancy at present sites for a few parameter combinations, even when sites had small  
 502 population sizes during sampling (small leftmost bar in the middle column of Fig. 4).  
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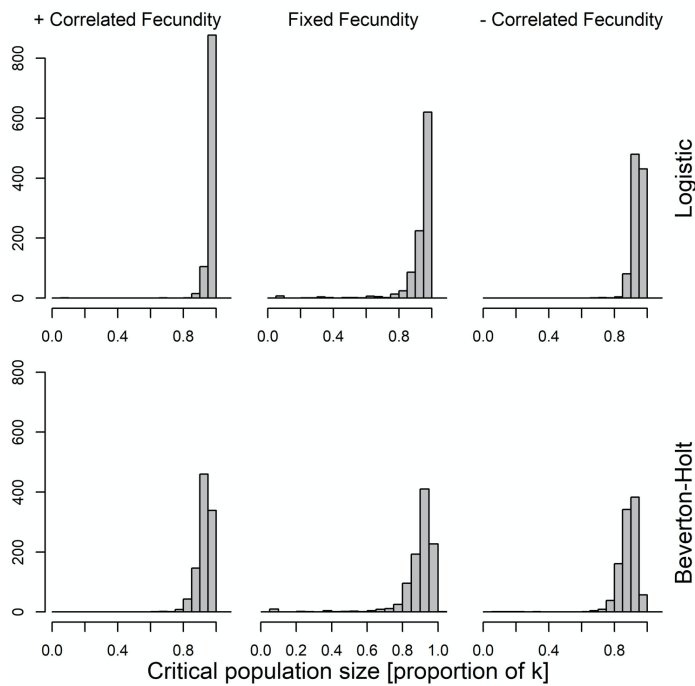
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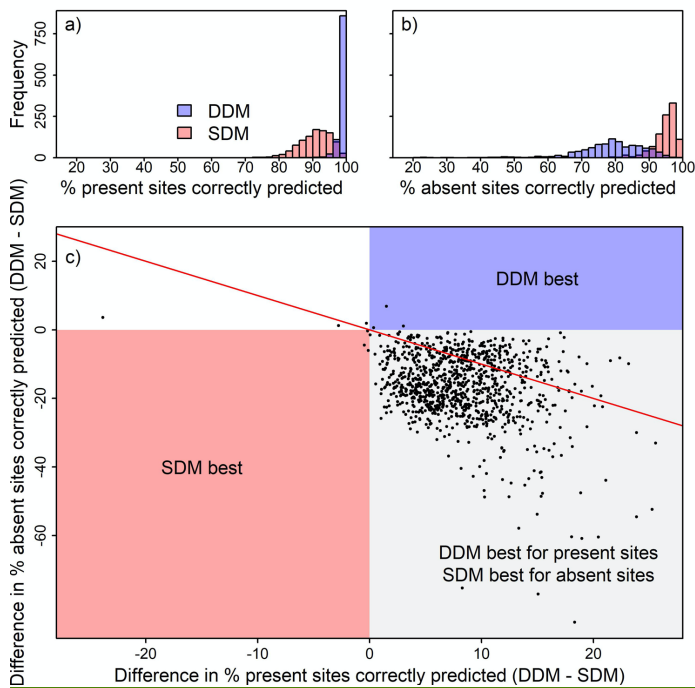


**Fig. 4.** Histogram of critical population size at the start of demographic sampling required for the DDM to achieve 80% prediction accuracy at present sites, across 1,000 randomly drawn parameter combinations. Critical population density [initial abundance as a proportion of carrying capacity] was typically between 0.75 - 0.95. The top and bottom rows are for Logistic and Beverton-Holt negative density-dependent fecundity functions. Maximum fecundity, at low population densities, is positively and negatively correlated with survival in the left and right columns. In the middle column, maximum fecundity is fixed across the landscape. As long as both survival and fecundity were correlated with environmental variables, DDMs achieved an 80% prediction accuracy in nearly all simulations. Note that critical population size means the population must be at or lower than this population size, to achieve the accuracy threshold.

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In the case where populations were at 50% of carrying capacity at the start of demographic sampling DDMs had higher prediction accuracy at present sites than correlative species distribution models (SDMs) in both the correlated (Fig. 5a) and negatively correlated (Fig. S2a) fecundity scenarios. However, SDMs predicted locations where the population was absent more accurately (Fig. 5b and S2b). The trade-off in improved accuracy at present and absent sites for DDMs and SDMs, respectively, occurred in over 98 percent of the simulations (points in the lower-right, grey region in Fig 5c and S2c). SDMs improved total accuracy over DDMs more frequently if survival was correlated with fecundity (more points below the 1-1 line in Fig 5c). However, the DDM improved overall accuracy if survival and fecundity were negatively correlated (more points above the 1-1 line in Fig S2c). In the negatively correlated fecundity scenario, the accuracy of both methods declined compared to the correlated scenario (see more left bars in the histograms in Figs S2ab than 5ab). However, the relative improvement of DDMs over SDMs was due to major decreases in SDM accuracy at present sites under negatively correlated fecundity (see the leftward shift of pink bars in Fig S2a compared to Fig 5a).

**Deleted:** DDM prediction accuracy at present sites was correlated with the long-term population growth rate of the species at low densities,  $\lambda_i$ , in sites where the species occurred. In Fig. 3cd, critical population abundance was usually 65-95% of carrying capacity, as long as the median of  $\lambda_i$  in present sites was greater than 1.15 (Fig. 3cd). For slow-growing species, median  $\lambda_i$  less than 1.1, DDMs were likely to over-predict extinction, even if demographic data was sampled at sites well below carrying capacity (left-most points in Fig. 3cd). No other parameters in the simulation strongly correlated with the critical population abundance at sampled sites (Fig. S3). These results were robust to the length of demographic sampling (see Fig. S4 – S9) but were even more pronounced when reducing the sampling period from 10 to six timesteps (Fig. S4-S6).<sup>†</sup> SDMs accurately predicted occupancy, and there was no strong trend between SDM prediction accuracy and population growth rate (first column in Fig. 4). Instead, SDM prediction accuracy, at present sites, was influenced by the number of present sites at the end of the simulation (shading in Fig. 4a). The two outliers (light, lower-left points in Fig. 4a), were the only two simulation runs where the species persisted in less than 5% of sites.<sup>†</sup> Alternatively, DDM presence prediction accuracy was much more strongly correlated with population growth rate. DDMs over-predicted extinction for slow-growing populations, even when the initial density was at 5% of carrying capacity in sampled sites (Fig. 4b). For fast growing-populations, the DDM more frequently over-predicted presence at absent sites (Fig. 4d). For the SDM, the opposite was true, there was a slight tendency to over-predict absence at present sites for faster-growing species.



**Fig. 5.** DDM and SDM prediction accuracy at (a) present and (b) absent sites, and (c) difference in prediction accuracy between SDMs and DDMs at present sites (horizontal axis) and absent sites (vertical axis), given initial densities at 50% of carrying capacity. Positive values indicate that DDMs have higher prediction accuracy. In (c) each point corresponds to a single randomly sampled parameter set. Almost all points fall in the lower right quadrant, corresponding to parameter sets where DDMs more accurately predicted present sites, and SDMs more accurately predicted absent sites. Points above the red one-to-one line correspond to parameter sets where a DDM's improved prediction accuracy at present sites is higher than the DDM's decreased prediction accuracy at absent sites. Fecundity was logistic, and positively correlated with survival.

585 All of the results discussed thus far assumed that populations were at a specified density,  
 586 relative to carrying capacity, at all sites used to build the DDM. If only a portion of sites started  
 587 at a specified density, perturbed below carrying capacity, while others started at carrying  
 588 capacity, predictions worsened (Fig S3, S4). For example, if fecundity was logistic, 25 – 61  
 589 percent of sites supplying demographic data needed to be perturbed from carrying capacity in  
 590 order to achieve 80 percent prediction accuracy in 90 percent of the simulations (Fig S3) across  
 591 the three fecundity correlation structures and three perturbation magnitudes tested. The results  
 592 were qualitatively similar for Beverton-Holt fecundity, but with a higher proportion of sites that  
 593 needed to be perturbed (34-75% of sites) to achieve the same accuracy. (Compare Fig S3a-c to  
 594 Figs. S4a-c). In the case where initial population size was uniformly distributed at each site, 80  
 595 percent prediction accuracy was achieved if mean initial densities exceeded 71% of carrying  
 596 capacity, across all scenarios (Fig S4).  
 597 In general, given 200 sampled sites, across all scenarios, if mean initial abundance,  
 598 averaged across sites, was 70% of carrying capacity or less, a density-independent DDM  
 599 predicted present sites with at least 80% accuracy, in at least 90% of the simulations (Fig S3-S6  
 600 and 6a). However, demographic data from fewer than 200 sites, meant more sites had to be  
 601 perturbed below carrying capacity during demographic sampling to achieve a desired DDM  
 602 prediction accuracy. For example, for logistic fecundity, positively correlated with survival, and  
 603 populations at 50% of carrying capacity in perturbed sites, the DDM required 25, 61, and 87% of  
 604 sites to be perturbed below carrying capacity, given 200, 50, and 30 sampled sites, respectively  
 605 (Fig. 6a-c). Even if all populations were at 50% of carrying capacity during the start of  
 606 demographic sampling, it was impossible to guarantee 80% accuracy in 90% of the simulations,  
 607 if there were 25 sampled sites or fewer (Fig. 6de). Additionally, DDMs built with long-term

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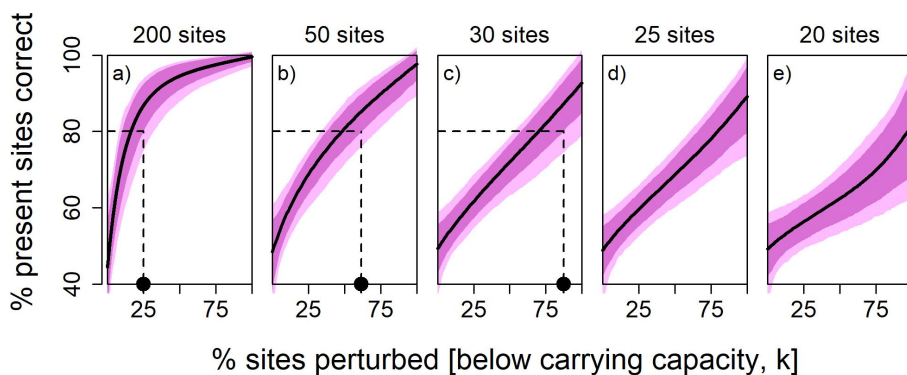
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monitoring data (e.g. 10 time-steps or greater) provided less accurate predictions (right column of Fig S6) despite increased sample sizes, because sampled populations frequently saturated at carrying capacity during data collection.



**Fig. 6.** Percent of present sites correctly predicted by the DDM as a function of the percentage of sites perturbed 50% below carrying capacity given data from (a) 200, (b) 50, (c) 30, (d) 25, and (e) 20, sites respectively. Dark and light shaded regions are 80 and 95% confidence intervals, respectively. Black circles are the critical percentage of sites that must be perturbed below carrying capacity during demographic sampling to achieve 80% prediction accuracy or higher at present sites in 90% of the simulations. As the number of sampled sites decreases, a higher percentage of sites need to be below carrying capacity to achieve the desired accuracy. If there were 25 sampled sites, or fewer, it was not possible to achieve 80% prediction accuracy, in 90% of the simulations (d, e). Fecundity was logistic, and maximum fecundity was positively correlated with survival.

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## 668 Discussion

669 Using 1.5 million simulations of hypothetical species' range-dynamics, we evaluated when  
 670 deterministic, density-independent, demographic distribution models (DDMs) accurately  
 671 predicted species' distributions. While DDM predictions were biased towards species absence in  
 672 simulations where data used to build the DDM came from sites with populations near carrying  
 673 capacity, our comprehensive simulations support the following generality: if mean initial  
 674 population size is less than 50% of carrying capacity, averaged across >25 sites, where  
 675 demographic data is available, a density-independent DDM will predict present sites accurately.  
 676 When this condition was satisfied, DDMs outperformed correlative species distribution models  
 677 (SDMs) at accurately predicting present sites, but, not absent sites. Our results suggest that  
 678 density-independent DDMs may be useful for predicting species ranges for some taxa and  
 679 applications (Briscoe et al. 2019), despite obvious limitations (Ellner et al. 2016). Often species'  
 680 have multiple locations available for sampling with populations well below carrying capacity  
 681 (Haak 2000, Williams et al. 2011), and there are 11 species of plants and animals with matrix  
 682 population models built from data at >25 sites, already available in the global, open-access  
 683 databases COMPADRE and COMADRE (Salguero-Gómez et al. 2015, 2016).

684 One particularly important application of density-independent DDMs is invasive species  
 685 risk mapping (Merow et al. 2017), an application where traditional SDM approaches have been  
 686 criticized (Liu et al. 2020). Our work confirms that this is potentially an appropriate use of  
 687 DDMs because invasive species, at the start of an invasion, are typically well below carrying  
 688 capacity (Ramula et al. 2008, Davis 2009, Burns et al. 2013). Additionally, because successful  
 689 invaders often invade multiple locations across wide geographic ranges, they are also species for  
 690 which demographic data replicated across geographically distant and climatically dissimilar sites

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703 can be collected (Marshall 2016). Our simulations suggest more than 25 such sites are required  
 704 for accurate predictions. While this will be feasible for many invasive species (Merow et al.  
 705 2017), DDMs will not be useful for mapping invasion risk for species already abundant  
 706 throughout their entire invaded ranges or those whose populations start small but quickly saturate  
 707 to carrying capacity during demographic data collection.  
 708 DDMs may also be appropriate for predicting threatened species ranges, because  
 709 threatened populations are often at low densities (IUCN 2012). Since DDMs tie these predictions  
 710 to mechanisms of decline and growth, they may provide insight into which management actions  
 711 will maximize species persistence (Briscoe et al. 2019). However, our results identify a key  
 712 limitation of using DDMs for threatened species management. While DDMs accurately predicted  
 713 presence at sites where the species persisted, correlative species distribution models SDMs  
 714 outperformed DDMs at sites where the species was absent in over 95 percent of the simulations.  
 715 Therefore, our results suggest that DDMs may be more appropriate for applications where  
 716 identifying present sites correctly is more important than identifying absent sites. For example, in  
 717 invasion risk mapping, predicting a local invasion at a site where an invasion fails to occur is  
 718 a more tolerable error than missing the location of a future invasion. In this case, present site  
 719 predictions are more important and a DDM will be appropriate, if demographic data from low  
 720 density sites are available. In contrast, a manager looking for a site to release a threatened  
 721 species, to establish a new population (often called a species “translocation”), would not want to  
 722 select a site where the species will go extinct. Therefore, when identifying translocation sites,  
 723 predicting absences accurately is very important, and DDMs may be inappropriate. Our DDMs  
 724 possibly overpredicted presence in sites where the species went extinct because they were  
 725 deterministic and therefore did not predict extinctions caused by demographic stochasticity.

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Deleted: and reducing threats via conservation actions, such as habitat restoration (Garnett et al. 2019), removal of invasive predators or competitors (Legge et al. 2011, Kanowski et al. 2018, Prior et al. 2018), and harvest bans (Belcher and Jr. 2002, Fukuda et al. 2011), have led to high population growth rates during the recovery of several threatened populations

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744 Applications for which correct predictions in unsuitable habitat are more important than  
745 predictions in suitable habitat, therefore, require a stochastic DDM, or a coupled niche-  
746 population model, to account for demographic stochasticity explicitly (Keith et al. 2008,  
747 Fordham et al. 2013), or an SDM, which can account for extinctions from demographic  
748 stochasticity implicitly.

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the location of a futureThis provides another reason why  
DDMs are a promising tool for invasion risk mapping.

749 Perhaps the biggest obstacle for wide-scale use of density-independent DDMs is that, for  
750 many species, demographic data are sampled primarily at sites where the species is already  
751 abundant (Quintana-Ascencio et al. 2018, Fournier et al. 2019). Field ecologists do not typically  
752 risk designing randomized, labor-intensive, demographic studies at sites where populations are  
753 so small that the ecologists may not even find individuals to sample. However, there is a small  
754 subset of the demography literature focused on populations at the edge of species ranges, where  
755 population density is often small (Sexton et al. 2009, Eckhart et al. 2011, Pironon et al. 2017).  
756 Our results show that demographic data from such low-density sites are highly valuable for  
757 building accurate density-independent DDMs.

758 There are three major caveats behind our approach to identifying guidelines for when to  
759 use density-independent DDMs. First, we simulated range dynamics using a simple model with  
760 several underlying assumptions, such as common pool dispersal, random/fixed initial population  
761 densities across sites, density dependence in fecundity, and demographic rates influenced by life  
762 stages rather than continuous traits (Easterling et al. 2000). Second, we assumed no systematic  
763 environmental change (e.g. climate change or deforestation). Lastly, the DDM used a model that  
764 closely matched the stochastic model employed to simulate the data. Some of these choices may  
765 have affected the relative performance of DDMs vs. SDMs. For example, DDM performance  
766 may have improved, relative to SDMs, if we included systematic, environmental change,

770 allowing estimated vital rates to change through time with environmental drivers (Evans et al.  
771 2016). And the relative accuracy of DDMs might have declined if the DDM model did not  
772 closely match the simulation model. However, the main result of our paper, that density-  
773 independent DDMs will only be useful when demographic data are collected from areas where  
774 populations are below carrying capacity is likely robust to all of these caveats.

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775 For modelers who wish to predict species ranges using process-explicit models for

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776 species with data collected from populations near carrying capacity, one option is to model

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777 density dependence explicitly. Simulation studies have found that models including carrying-

778 capacity (Pagel and Schurr 2012, Schurr et al. 2012) can outperform density-independent

779 methods when predicting species occurrence (Zurell et al. 2016). And there are a few examples

780 of empirically-driven density-dependent demographic models (Vanderwel et al. 2013, García-

781 Callejas et al. 2016, Pagel et al. 2020). These models, which incorporate density dependence

782 explicitly are likely required to predict transient dynamics and project species abundances (rather

783 than just presence absence). Unfortunately, fitting density-dependent models requires, not only

784 data at multiple sites, across multiple environmental conditions, and tracking multiple life stages,

785 but also requires replication across populations at different densities. This may be impractical to

786 obtain in many scenarios. Here, we have demonstrated that ignoring density dependence when

787 predicting species ranges from demographic models is a practical first step and likely appropriate

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788 in several situations.

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797 **References**

- 798 Ackerly, D. D. et al. 2010. The geography of climate change: implications for conservation  
799 biogeography. - *Divers. Distrib.* 16: 476–487.
- 800 Barbraud, C. et al. 2011. Contrasted demographic responses facing future climate change in  
801 Southern Ocean seabirds. - *J. Anim. Ecol.* 80: 89–100.
- 802 Beverton, R. J. H. and Holt, S. J. 2012. On the Dynamics of Exploited Fish Populations.
- 803 Briscoe, N. J. et al. 2019. Forecasting species range dynamics with process-explicit models:  
804 matching methods to applications. - *Ecol. Lett.* 22: 1940–1956.
- 805 Buckley, L. B. et al. 2010. Can mechanism inform species' distribution models? - *Ecol. Lett.* 13:  
806 1041–1054.
- 807 Burns, J. H. et al. 2013. Greater sexual reproduction contributes to differences in demography of  
808 invasive plants and their noninvasive relatives. - *Ecology* 94: 995–1004.
- 809 Cabral, J. S. et al. 2017. Mechanistic simulation models in macroecology and biogeography:  
810 state-of-art and prospects. - *Ecography (Cop.)*. 40: 267–280.
- 811 Caswell, H. 2001. Matrix population models : construction, analysis, and interpretation. - Sinauer  
812 Associates.
- 813 Csergő, A. M. et al. 2017. Less favourable climates constrain demographic strategies in plants (J  
814 Gurevitch, Ed.). - *Ecol. Lett.* 20: 969–980.
- 815 Cushing, J. M. et al. 2002. Chaos in ecology : experimental nonlinear dynamics. - Academic  
816 Pres.
- 817 Dahlgren, J. P. et al. 2014. Local environment and density-dependent feedbacks determine  
818 population growth in a forest herb. - *Oecologia* 176: 1023–1032.
- 819 Davis, M. A. 2009. Invasion Biology. - Oxford University Press.

820 Diez, J. M. et al. 2014. Probabilistic and spatially variable niches inferred from demography (E  
 821 Jongejans, Ed.). - J. Ecol. 102: 544–554.  
 822 Easterling, M. R. et al. 2000. Size-Specific Sensitivity: Applying a New Structured Population  
 823 Model. - Ecology 81: 694–708.  
 824 Eckhart, V. M. et al. 2011. The geography of demography: long-term demographic studies and  
 825 species distribution models reveal a species border limited by adaptation. - Am. Nat. 178  
 826 Suppl 1: S26–43.  
 827 Ehrlén, J. et al. 2016. Advancing environmentally explicit structured population models of plants  
 828 (A Griffith, Ed.). - J. Ecol. 104: 292–305.  
 829 Elith, J. and Leathwick, J. R. 2009. Species Distribution Models: Ecological Explanation and  
 830 Prediction Across Space and Time. - Annu. Rev. Ecol. Evol. Syst. 40: 677–697.  
 831 Ellner, S. P. et al. 2016. Density Dependence. - In: Data-driven Modelling of Structured  
 832 Populations. Springer, Cham, pp. 111–138.  
 833 Evans, M. E. K. et al. 2016. Towards Process-based Range Modeling of Many Species. - Trends  
 834 Ecol. Evol. 31: 860–871.  
 835 Fordham, D. A. et al. 2013. Tools for integrating range change, extinction risk and climate  
 836 change information into conservation management. - Ecography (Cop.). 36: 956–964.  
 837 Fordham, D. A. et al. 2018. How complex should models be? Comparing correlative and  
 838 mechanistic range dynamics models. - Glob. Chang. Biol. 24: 1357–1370.  
 839 Fournier, A. M. V. et al. 2019. Site-selection bias and apparent population declines in long-term  
 840 studies. - Conserv. Biol. 33: 1370–1379.  
 841 García-Callejas, D. et al. 2016. Projecting the distribution and abundance of Mediterranean tree  
 842 species under climate change: a demographic approach. - J. Plant Ecol. 10: rtw081.

843 Guisan, A. et al. 2013. Predicting species distributions for conservation decisions (H Arita, Ed.).  
844 - Ecol. Lett. 16: 1424–1435.

845 Haak, C. 2000. The concept of equilibrium in population ecology.

846 Hijmans, R. J. et al. 2017. dismo: Species distribution modeling.: 1–68.

847 Holt, R. D. 2009. Bringing the Hutchinsonian niche into the 21st century: ecological and  
848 evolutionary perspectives. - Proc. Natl. Acad. Sci. U. S. A. 106 Suppl 2: 19659–65.

849 IUCN 2012. IUCN Red List Categories and Criteria. - IUCN.

850 Keith, D. A. et al. 2008. Predicting extinction risks under climate change: coupling stochastic  
851 population models with dynamic bioclimatic habitat models. - Biol. Lett. 4: 560–563.

852 Kéry, M. et al. 2017. AHMbook: Functions and Data for the Book “Applied Hierarchical  
853 Modeling in Ecology.”

854 Lavine, M. et al. 2002. Statistical modeling of seedling mortality. - J. Agric. Biol. Environ. Stat.  
855 7: 21–41.

856 Liu, C. et al. 2020. Species distribution models have limited spatial transferability for invasive  
857 species (C Bertelsmeier, Ed.). - Ecol. Lett.: ele.13577.

858 Marshall, G. 2016. Individual performance and population dynamics of *Plantago lanceolata* in  
859 Southeast Queensland.

860 May, R. M. 1974. Biological Populations with Nonoverlapping Generations: Stable Points,  
861 Stable Cycles, and Chaos. - Science (80-. ). 186: 645–647.

862 Merow, C. et al. 2014. On using integral projection models to generate demographically driven  
863 predictions of species’ distributions: development and validation using sparse data. -  
864 Ecography (Cop.). 37: 1167–1183.

865 Merow, C. et al. 2017. Climate change both facilitates and inhibits invasive plant ranges in New

866 England. - Proc. Natl. Acad. Sci. U. S. A.: 201609633.  
 867 Meyer, C. et al. 2015. Global priorities for an effective information basis of biodiversity  
 868 distributions. - Nat. Commun. 6: 8221.  
 869 Needham, J. et al. 2018. Inferring forest fate from demographic data: from vital rates to  
 870 population dynamic models. - Proc. R. Soc. B Biol. Sci. 285: 20172050.  
 871 Normand, S. et al. 2014. Demography as the basis for understanding and predicting range  
 872 dynamics. - Ecography (Cop.). 37: 1149–1154.  
 873 Owens, H. L. et al. 2013. Constraints on interpretation of ecological niche models by limited  
 874 environmental ranges on calibration areas. - Ecol. Modell. in press.  
 875 Pagel, J. and Schurr, F. M. 2012. Forecasting species ranges by statistical estimation of  
 876 ecological niches and spatial population dynamics. - Glob. Ecol. Biogeogr. 21: 293–304.  
 877 Pagel, J. et al. 2020. Mismatches between demographic niches and geographic distributions are  
 878 strongest in poorly dispersed and highly persistent plant species. - Proc. Natl. Acad. Sci. U.  
 879 S. A. 117: 3663–3669.  
 880 Pearson, R. G. and Dawson, T. P. 2003. Predicting the impacts of climate change on the  
 881 distribution of species: are bioclimate envelope models useful? - Glob. Ecol. Biogeogr. 12:  
 882 361–371.  
 883 Pironon, S. et al. 2017. Geographic variation in genetic and demographic performance: new  
 884 insights from an old biogeographical paradigm. - Biol. Rev. 92: 1877–1909.  
 885 Quinn II, T. J. and Deriso, R. B. 1999. Quantitative fish dynamics. - Oxford University Press.  
 886 Quintana-Ascencio, P. F. et al. 2018. Predicting landscape-level distribution and abundance:  
 887 Integrating demography, fire, elevation and landscape habitat configuration (S Zhou, Ed.). -  
 888 J. Ecol. 106: 2395–2408.

889 Ramula, S. et al. 2008. General guidelines for invasive plant management based on comparative  
 890 demography of invasive and native plant populations. - J. Appl. Ecol. 45: 1124–1133.  
 891 Salguero-Gómez, R. et al. 2015. The compadre Plant Matrix Database: An open online  
 892 repository for plant demography. - J. Ecol. 103: 202–218.  
 893 Salguero-Gómez, R. et al. 2016. COMADRE: A global data base of animal demography. - J.  
 894 Anim. Ecol. 85: 371–384.  
 895 Schurr, F. M. et al. 2012. How to understand species' niches and range dynamics: a demographic  
 896 research agenda for biogeography. - J. Biogeogr. 39: 2146–2162.  
 897 Sexton, J. P. et al. 2009. Evolution and Ecology of Species Range Limits. - Annu. Rev. Ecol.  
 898 Evol. Syst. 40: 415–436.  
 899 Sheth, S. N. and Angert, A. L. 2018. Demographic compensation does not rescue populations at  
 900 a trailing range edge. - Proc. Natl. Acad. Sci. U. S. A. 115: 2413–2418.  
 901 Shinozaki, K. and Kira, T. 1956. Intraspecific competition among higher plants. VII. Logistic  
 902 theory of the C-D effect. - J. Inst. Polytech. Osaka Cy.: 35–72.  
 903 Stohlgren, T. J. et al. 2011. Bounding species distribution models. - Curr. Zool. 57  
 904 Strogatz, S. H. 1994. Nonlinear Dynamics and Chaos. - CRC press.  
 905 Teller, B. J. et al. 2016. Linking demography with drivers: climate and competition (J Metcalf,  
 906 Ed.). - Methods Ecol. Evol. 7: 171–183.  
 907 Thuiller, W. et al. 2014. Does probability of occurrence relate to population dynamics? -  
 908 Ecography (Cop.). 37: 1155–1166.  
 909 Vanderwel, M. C. et al. 2013. Climate-related variation in mortality and recruitment determine  
 910 regional forest-type distributions. - Glob. Ecol. Biogeogr. 22: 1192–1203.  
 911 Villellas, J. et al. 2015. Demographic compensation among populations: what is it, how does it

912        arise and what are its implications? (J Hille Ris Lambers, Ed.). - Ecol. Lett. 18: 1139–1152.  
913 Williams, J. L. et al. 2011. Distance to stable stage distribution in plant populations and  
914        implications for near-term population projections. - J. Ecol. 99: 1171–1178.  
915 Wood, S. N. 2017. Generalized additive models: An introduction with R, second edition. - CRC  
916        Press.  
917 Zurell, D. et al. 2010. The virtual ecologist approach: simulating data and observers. - Oikos 119:  
918        622–635.  
919 Zurell, D. et al. 2016. Benchmarking novel approaches for modelling species' range dynamics. -  
920        Glob. Chang. Biol. 22: 2651–2664.  
921