

# Incremental Maintenance of ABAC Policies

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## ABSTRACT

Discovery of Attribute Based Access Control policies through mining has been studied extensively in the literature. However, current solutions assume that the rules are to be mined from a static data set of access permissions and that this process only needs to be done once. However, in real life, access policies are dynamic in nature and may change based on the situation. Simply utilizing the current approaches would necessitate that the mining algorithm be re-executed for every update in the permissions or user/object attributes, which would be significantly inefficient. In this paper, we propose to incrementally maintain ABAC policies by only updating the rules that may be affected due to any change in the underlying access permissions or attributes. A comprehensive experimental evaluation demonstrates that the proposed incremental approach is significantly more efficient than the conventional ABAC mining.

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## 1 INTRODUCTION

The flexibility, scalability, dynamic nature, portability and identity-less features of Attribute Based Access Control (ABAC) make it an attractive choice to be employed as a means to enforce access control in many traditional and emerging application domains [8]. Under ABAC, security policies (also called rules in this paper) are specified based on subject, object and environmental attribute conditions. However, a key problem in deploying ABAC is to precisely configure it for effective access control. The problem of automatically discovering the best set of minimum ABAC rules to configure the system using existing permissions of users on the resources is known as ABAC Policy Mining.

While the ABAC mining problem has been well studied in the literature, all the approaches assume the system to be static in nature. However, in reality, all systems change in due course of

time, which necessitates updating (or maintaining) the ABAC rules since the original rules may no longer be valid. Such maintenance requires *re-mining* of the ABAC policies that reflect the changes, which is often quite expensive and inefficient, especially when the number of users and objects is large and changes to the data are quite frequent.

In this paper, we propose an efficient alternative where ABAC policy maintenance can be performed in an incremental fashion whenever a change occurs. In particular, we consider the following changes ( $\Delta$ ). Note that other changes such as adding subjects and objects do not affect the ABAC policies.

- (1) Addition of a permission: This means granting access to a user on an object that did not previously exist.
- (2) Deletion of a permission: This means revoking a user's existing permission to access an object.
- (3) Addition of an attribute value: This means assigning a new attribute value to either a subject or an object that currently is not assigned.
- (4) Deletion of an attribute value: This means removing an existing attribute value assignment from a subject or an object.

Given the current set of ABAC policies and the set of changes  $\Delta$ , the two alternative approaches to discover the new set of ABAC policies have been depicted in Figure 1. More specifically:

- (1) *Redo ABAC Mining* is an intuitive method to discover new set of ABAC rules in which ABAC mining process is performed whenever there is a change.
- (2) *Incremental Maintenance* is an efficient means of handling changes and discovering new ABAC rules by taking into account only the part of the data that was affected by the change. However, this process requires us to first extract and maintain some intermediary data structures using which we obtain the new set of rules that cover the changes.

In this paper, we have employed the ABAC-SRM mining algorithm proposed by Talukdar et al. [20] as this is one of the fastest approaches thus far proposed. We have compared the efficiency of the above two approaches - the redo ABAC mining and the incremental maintenance. Since the data used to mine the policies in the latter case is significantly smaller than the former approach, is very efficient as shown in our experimental evaluation.

The rest of this paper is organized as follows. In Section 2, we review the preliminaries of ABAC definition and concepts, as well as the ABAC-SRM mining approach [20]. In Section 3, we discuss the types of changes and formalize the problem of incremental maintenance of ABAC policies. We also provide an overview of the approach to solve the problem. In Section 4 we present the proposed

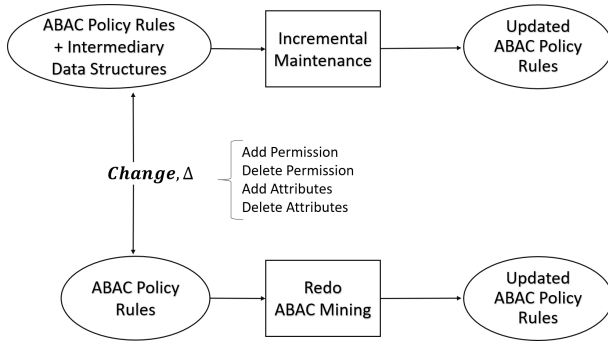
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**Figure 1: Alternative Approaches to Maintenance of ABAC Policies**

incremental maintenance approach with detailed algorithms. This includes a pre-processing phase to extract the necessary intermediate data structures and algorithms to handle the four types of changes mentioned above. In Section 5, we experimentally compare the cost of maintaining ABAC system using our proposed incremental maintenance approach versus employing the redoing ABAC mining approach. In Section 6 we discuss the related work and in Section 7, we present conclusions and future research.

## 2 PRELIMINARIES

In this section, we briefly review the attribute based access control model (ABAC) [9], and the ABAC mining approach from Talukdar et al. [20], called the ABAC-SRM. The notations of ABAC and ABAC Mining approach have been borrowed from [20].

### 2.1 ABAC

In an ABAC system, the authorization to perform an operation (e.g., read, write) is granted based on the attributes of the requesting user, requested object, and the environment in which a request is made. The ABAC policy rules are comprised of the attributes, which include user attribute conditions and object attribute conditions that determine granting of a permission to the user.

The basic components of an ABAC system are as follows:

**Users ( $U$ ):** Represents a set of authorized users/subjects.  $u_i$ , for  $1 \leq i \leq |U|$  denotes each member of this set.

**Objects ( $O$ ):** Represents a set of resources to be protected. Each member of this set is denoted as  $o_i$ , for  $1 \leq i \leq |O|$ .

**Environment ( $E$ ):** Represents a set of environment conditions, independent of users and objects. Each member of this set is denoted as  $e_i$ , for  $1 \leq i \leq |E|$ .

**$U_A$ :** Represents a set of user attribute names. Members of these sets are represented as  $ua_i$ , for  $1 \leq i \leq |U_A|$ . Each  $ua_i$  is associated with a set of possible values it can acquire. For instance, if a user attribute *Title* is associated with the values {Instructor, TA, Student}, then for every  $u \in U$ , value of the attribute *Title* can be either *Instructor*, *TA* or *Student*.

**$O_A$ :** Represents a set of object attribute names. Members of these sets are represented as  $oa_i$ , for  $1 \leq j \leq |O_A|$ . Each  $oa_i$  is associated with a set of possible values it can acquire. For instance, if an object folder with records of student has object attribute *Major* associated with a set of values {Computer Science, Electronics, Mechanical}, then

**Table 1:  $U_A$**

User ( $u$ )	Department = Computer Science ( $uc_1$ )	Title = Instructor ( $uc_2$ )	Department = Electronics ( $uc_3$ )	Title = TA ( $uc_4$ )
$u_1$	0	0	1	1
$u_2$	0	1	1	0
$u_3$	1	1	0	0
$u_4$	1	0	0	1

for every  $o \in O$ , value of the attribute *Major* can be either *Computer Science*, *Electronics* or *Mechanical*.

**$E_A$ :** Represents a set of environment attribute names. Members of these sets are represented as  $ea_i$ , for  $1 \leq i \leq |E_A|$ . Each  $ea_i$  is associated with a set of possible values it can acquire. For instance, if an environment attribute *Campus* is associated with a set of values {USA, UK, Australia}, then for every  $e \in E$ , value of the attribute *Campus* can be either *USA*, *UK* or *Australia*.

**$P$ :** A set consisting of all possible permissions/operations on objects allowed in a system. For example, if *read* and *write* are the only two possible operations on objects, then  $P = \{\text{read}, \text{write}\}$ . Each member of  $P$  is represented as  $p_i$ , for  $1 \leq i \leq |P|$ .

**$U_C$ :** Represents a set of all possible user attribute conditions denoted as  $uc_j$ , for  $1 \leq j \leq |U_C|$ . Members of this set are represented as equalities of the form  $n = c$ , where  $n$  is a user attribute name and  $c$  is either a constant or *any*. For instance if user attribute *Title* has possible values {Instructor, TA, Student} and user attribute *Department* has possible values as {Computer Science, Electronics, Mechanical}, then  $U_C$  will be a set comprising of {Title=Instructor, Title=TA, Title=Student, Title=Any, Department=Computer Science, Department=Electronics, Department=Mechanical, Department=Any}. Note here, that the condition  $n = \text{Any}$  does not have to be explicitly chosen. It is set only if at least one other condition for  $n$  is present.

**$O_C$ :** Represents a set of all possible object attribute conditions denoted as  $oc_k$ , for  $1 \leq k \leq |O_C|$ . Members of this set are represented as equalities of the form  $n = c$ , where  $n$  is an object attribute name and  $c$  is either a constant or *any*. For instance if object attribute *Major* has possible values {Computer Science, Electronics, Mechanical} and object attribute *RecordsOf* has possible values {Instructor, TA, Student, Staff}, then  $O_C$  will be a set comprising of {Major=Computer Science, Major=Electronics, Major=Mechanical, Major=Any, RecordOf=Instructor, RecordOf=Student, RecordOf=TA, RecordOf=Staff, RecordOf=Any}. For an attribute name  $n$ , if the value of  $c$  is *any*, then the attribute  $n$  is not relevant for making the corresponding access decision. Therefore, as above, the condition  $n = \text{Any}$  does not have to be explicitly chosen. It is set only if at least one other condition for  $n$  is present.

**$\Pi$ :** Represents a set of access rules called the rule base of the ABAC system. Each member of this set is denoted as  $r_i$ , for  $1 \leq i \leq |\Pi|$ . A rule  $r$  in ABAC is of the form  $\langle uc, oc, p \rangle$ .

If a user makes a request to access an object, the rule base is searched for any rule through which the user can gain access. If such a rule exists, then the access is granted, otherwise it is denied.

For the sake of simplicity, in this paper, we assume the environment condition to be *any*.

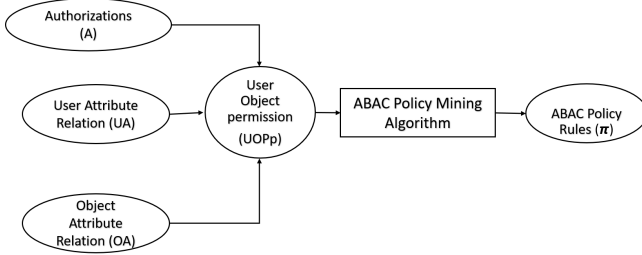
**$U_A$ :** User attribute relation  $U_A \subseteq U \times U_C$  is a many-to-many mapping of users and user attribute conditions. We use a  $m \times n$  binary

**Table 2: OA**

Object (o)	Major =Electronics (oc <sub>1</sub> )	Major =Computer Science (oc <sub>2</sub> )	Recordof =Student (oc <sub>3</sub> )
o <sub>1</sub>	1	0	1
o <sub>2</sub>	0	1	1

**Table 3:  $\Pi$** 

Rule ID	Rule
1	uc <sub>3</sub> , oc <sub>1</sub>
2	uc <sub>1</sub> , oc <sub>2</sub>

**Figure 2: ABAC Mining Process**

matrix to represent  $UA$ , where  $UA[i,j]=1$ , if user  $u_i$  satisfies an attribute condition  $uc_j$ . An example is shown in Table 1 where user  $u_1$  is a  $TA$  whose department is *Electronics*.

$OA$ : Object attribute relation,  $OA \subseteq O \times OC$  is a many-to-many mapping of objects and the set of all attributes conditions, where an  $m \times n$  binary matrix represents  $OA$ .  $OA[i,j]=1$  if an object  $o_i$  satisfies an object attribute condition  $oc_j$ . Table 2 shows an example where object  $o_1$  is the *recordof Student* in *Electronics Major*.

## 2.2 ABAC Mining

$A$ : An authorization  $a$  is of the form of  $\langle u, o, p \rangle$  and represents user  $u \in U$ , object  $o \in O$ , and permission  $p \in P$ , respectively, where  $a$  denotes that a user  $u$  is allowed to perform an operation  $p$  on an object  $o$ . We use  $p.a$  as the permission associated with  $a$ . We denote the set of all authorizations as  $A$ . For each permissions  $p_i \in P$ , we define  $A_{p_i} \subset A$  such that for every  $a \in A_{p_i}$ ,  $p.a = p_i$ . For example, if  $P = \{\text{read}, \text{write}\}$ , we have  $A_{\text{read}}$  and  $A_{\text{write}}$  such that  $A_{\text{read}} \cup A_{\text{write}} = A$ .

Given  $A$ , we construct a table  $UOP_p$  for each permission type  $p$  (read, write etc.). The columns of this matrix are all possible user attribute conditions and object attribute conditions of users and objects in  $A$ , respectively, a column for  $p$  and column for *Row Id*. There is a row in  $UOP_p$  for each user object pair. For each row, if the user attribute condition (object attribute condition) is true for a user (object), the corresponding cell is filled with 1, otherwise with 0. If there exists a  $a = \langle u, o, p \rangle$ , we insert a 1 in the  $p$  column of that  $u - o$ . For the remaining rows, the  $p$  column is 0. Given  $P = \{p_1, p_2, \dots, p_n\}$ ,  $UOP = \cup_{i=1}^n UOP_{p_i}$ .

$UOP_p$ : User Object Permission Matrix  $UOP_p$ , is a  $M \times N$  matrix, where  $M = |U| \times |O|$  comprising of a row for each user-object pair, and  $N = |UC| + |OC| + 1$ , comprising of a column for each object

attribute condition, a column for each user attribute condition, and a column for the permission  $p$  and a column for *Row Id*. For the  $UA$  in table 1,  $OA$  in table 2 and  $A$  in table 4a, table 4b shows the  $UOP_{\text{read}}$  constructed.

**ABAC Mining:** Given the set of authorizations  $A$ , the set of user attribute conditions ( $UC$ ), the set of object attribute conditions ( $OC$ ), ABAC Mining discovers minimum set of access rules  $\Pi$  such that there exists a rule  $r \in \Pi$  where  $u$  is allowed to perform  $p$  on  $o$  iff  $a = \langle u, o, p \rangle \in A$ . Table 3 shows the rules  $\Pi$  corresponding to the  $UOP_{\text{read}}$  in table 4b.

In this work, to find out  $\Pi$ , the ABAC-SRM Mining algorithm has been used. This algorithm finds minimum possible ABAC rules through subset enumeration. It is being used in the form of the following function:  $\text{ABAC-SRM}(\text{Perm1Rules}, \text{Perm0Rules}, \text{SpecificRules})$ , where  $\text{Perm1Rules}$  are the Permission One rows,  $\text{Perm0Rules}$  are Permission Zero rows and  $\text{SpecificRules}$  are current ABAC rules. This function evaluates the ABAC rules  $\Pi$  and returns them.

## 3 INCREMENTAL MAINTENANCE PROBLEM

In this section, we define the problem of maintenance of ABAC policies in an incremental fashion, and discuss the basic idea behind our proposed approach.

### 3.1 Types of Changes

$\Delta$ : Represents a set of possible changes allowed in an ABAC system. Each member is denoted as  $\Delta_i$  for  $1 \leq i \leq |\Delta|$ . The change  $\Delta$  could be to authorization set ( $A$ ) or User Attribute Relation ( $UA$ ) or Object Attribute Relation ( $OA$ ) in ABAC, and makes the current rules  $\Pi$  invalid. Types of changes,  $\Delta$  are:

- (1) Addition of an Access Permission ( $\Delta_{ap}$ ): This means authorizing a user access to an object which previously didn't exist.  $\Delta_{ap} : A \leftarrow A \cup a$ , where  $a = \langle m\_user, m\_object, p \rangle$ . This will lead to the permission column of a row in  $UOP$  corresponding to user  $m\_user$  and object  $m\_object$  to be changed from 0 to 1.
- (2) Deletion of an Access Permission ( $\Delta_{dp}$ ): This means removing a user's existing access to an object. This will lead to the permission column of a row in  $UOP$  to be changed from 1 to 0.  $\Delta_{dp} : A \leftarrow A \setminus a$  where  $a = \langle m\_user, m\_object, p \rangle$ . This will lead to the permission column of a row in  $UOP$  corresponding to user  $m\_user$  and object  $m\_object$  to be changed from 1 to 0.
- (3) Addition of an Attribute value ( $\Delta_{aa}$ ): This means assigning a user/object an attribute value which previously it did not have, i.e.,  $\Delta_{aa} : UA[i,j] \leftarrow 1$  where user  $m\_user$  satisfies user attribute condition  $uc_j$ . This will lead to the attribute condition being 1 for all of the user's/object's rows in the  $UOP$ .
- (4) Deletion of an Attribute value ( $\Delta_{da}$ ): This means removing an existing attribute value of a user/object, i.e.,  $\Delta_{da} : UA[i,j] \leftarrow 0$ , where user  $m\_user$  does not satisfy user attribute condition  $uc_j$ . This will lead to the attribute condition being 0 for all of the user's/object's rows in the  $UOP$ .

We assume that during the addition and deletion of permission changes, the user/object attribute values remain the same. Similarly,

(a) Authorizations (A)			(b) UOP <sub>Read</sub>									
User <i>u</i>	Object <i>o</i>	Permission <i>p<sub>i</sub></i>	Row Id	User - Object <i>u - o</i>	Department =Computer Science ( <i>uc</i> <sub>1</sub> )	Title= Instructor ( <i>uc</i> <sub>2</sub> )	Department= Electronics ( <i>uc</i> <sub>3</sub> )	Title= TA ( <i>uc</i> <sub>4</sub> )	Major =Electronics ( <i>oc</i> <sub>1</sub> )	Major =Computer Science ( <i>oc</i> <sub>2</sub> )	RecordOf =Student ( <i>oc</i> <sub>3</sub> )	<i>p</i> <sub>1</sub> = <i>Read</i>
<i>u</i> <sub>1</sub>	<i>o</i> <sub>1</sub>	<i>p</i> <sub>1</sub>	1	<i>u</i> <sub>1</sub> <i>o</i> <sub>1</sub>	0	0	1	1	1	0	1	1
<i>u</i> <sub>2</sub>	<i>o</i> <sub>1</sub>	<i>p</i> <sub>1</sub>	2	<i>u</i> <sub>2</sub> <i>o</i> <sub>1</sub>	0	1	1	0	1	0	1	1
<i>u</i> <sub>2</sub>	<i>o</i> <sub>1</sub>	<i>p</i> <sub>2</sub>	3	<i>u</i> <sub>3</sub> <i>o</i> <sub>1</sub>	1	1	0	0	1	0	1	0
<i>u</i> <sub>3</sub>	<i>o</i> <sub>2</sub>	<i>p</i> <sub>1</sub>	4	<i>u</i> <sub>4</sub> <i>o</i> <sub>1</sub>	1	0	0	1	1	0	1	0
<i>u</i> <sub>3</sub>	<i>o</i> <sub>2</sub>	<i>p</i> <sub>2</sub>	5	<i>u</i> <sub>1</sub> <i>o</i> <sub>2</sub>	0	0	1	1	0	1	1	0
<i>u</i> <sub>4</sub>	<i>o</i> <sub>2</sub>	<i>p</i> <sub>1</sub>	6	<i>u</i> <sub>2</sub> <i>o</i> <sub>2</sub>	0	1	1	0	0	1	1	0
			7	<i>u</i> <sub>3</sub> <i>o</i> <sub>2</sub>	1	1	0	0	0	1	1	1
			8	<i>u</i> <sub>4</sub> <i>o</i> <sub>2</sub>	1	0	0	1	0	1	1	1

Table 4: The set of Authorizations and the corresponding  $UOP_{Read}$ 

we assume that during the addition and deletion of attribute values, the permissions of users on objects remain unchanged. We would also like to note that addition/deletion of environment attributes will be handled similar to user/object attributes.

**DEFINITION 1 (INCREMENTAL ABAC POLICY MAINTENANCE).** *Given a set of ABAC rules  $\Pi$  that encapsulate the original access policy, and the change  $\Delta$ , the Incremental ABAC Maintenance Problem aims to discover a set of rules  $\Pi'$  that encapsulates the new access policy derived by applying the changes  $\Delta$  more efficiently than re-mining the new policy.*

### 3.2 Overview of the approach

The concept behind performing incremental mining is that whenever a change occurs, it impacts only a particular row in the  $UOP$  or a small set of rows in the  $UOP$ . We only need to work on that part of the  $UOP$  to update the ABAC rules. Intuitively, we need to replace a few rows in the  $UOP$  with new ones which have the change incorporated in them. We can have two types of rows in  $UOP$  that can be added or deleted from the  $UOP$ :

- (1) Rows with value of Permission column as 1, called Permission One Rows.
- (2) Rows with value of Permission column as 0, called Permission Zero Rows.

For example, in Table 5, the Permission One Rows are [3,5,6,8] and Permission Zero Rows are [1,2,4,7,9]. For every type of change, we delete the Permission Zero and Permission One rows impacted and add the modified/changed Permission Zero and Permission One rows back to the data set (or data structures that we maintain for efficient updation). Our approach to incremental ABAC maintenance is based on the above concept.

## 4 INCREMENTAL MAINTENANCE APPROACH

In this section, we describe in detail our proposed approach to perform the incremental maintenance of ABAC policies. We first discuss the steps performed during the pre-processing phase and then discuss the incremental maintenance algorithms for the four change types.

### 4.1 Pre-Processing

The incremental ABAC maintenance approach is based on the idea that we maintain certain intermediary data structures on which we can operate to find out the new set of ABAC rules  $\Pi'$ . Specifically, given the set of ABAC rules  $\Pi$  (i.e., the original policy) and the  $UOP$  derived from the policy, we maintain the following data structures:

- (1) **ZeroRowIds**: The Row Ids of Permission Zero Rows in the  $UOP$ .
- (2) **ZeroRules**: This is a minimum set of Permission Zero Rows which covers all the Permission Zero rows, such that each Zero row is a subset of atleast one rule in **ZeroRules**.
- (3) **ZeroRowCoverage**: This is a list of size  $|\text{ZeroRules}|$  where each element is a set that gives the Row Ids in the  $UOP$  of the Permission Zero rows that are a subset of the corresponding **ZeroRule** (i.e., it provides a mapping of the **ZeroRules** to the Rows Ids of the Permission Zero rows covered by the corresponding rule in **ZeroRules**).
- (4) **ZeroRuleIds**: The Row Ids in the  $UOP$  of the **ZeroRules** rows.
- (5) **OneRowIds**: The Row Ids in the  $UOP$  of the Permission One Rows.
- (6) **OneRowCoverage**: This is a list of size  $|\Pi|$  where each element is a set that gives the Row Ids in the  $UOP$  of the Permission One rows that are a super set of the corresponding ABAC rule in  $\Pi$  (i.e., it provides a mapping of the  $\Pi$  to the Row Ids of the Permission One Rows authorized by the corresponding ABAC rule in  $\Pi$ ).

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#### Algorithm 1 Pre-Processing Steps

---

**Require:** Dataset  $D = UOP$

**Require:**  $\Pi$

- 1:  $\text{ZeroRowIds} \leftarrow$  Row Ids of Permission Zero Rows
  - 2:  $\text{ZeroRules} \leftarrow \text{findZeroRules}(\text{ZeroRowIds})$
  - 3:  $\text{ZeroRowCoverage} \leftarrow \text{CoverageCalc}(\text{ZeroRowIds}, \text{ZeroRules}, 0)$
  - 4:  $\text{ZeroRuleIds} \leftarrow$  Row Ids of **ZeroRules**
  - 5:  $\text{OneRowIds} \leftarrow$  Row Ids of Permission One Rows
  - 6:  $\text{OneRowCoverage} \leftarrow \text{CoverageCalc}(\text{OneRowIds}, \Pi, 1)$
- 

We will denote the entire set of the above data structures by  $I$ . Algorithm 1 gives the specific steps to construct these, and utilizes

**Algorithm 2** findZeroRules(ZeroRowIds)

---

```

1: ZeroRules, ZeroRowList  $\leftarrow \phi$ 
2: ZeroRowList  $\leftarrow$  List of set of attribute conditions of Ids in
   ZeroRowIds
3: Sort ZeroRowList in descending order based on the number of
   attributes in each row
4: for each row in ZeroRowList do
5:   if  $\nexists$  rule  $\in$  ZeroRules such that row  $\subseteq$  rule then
6:     ZeroRules  $\leftarrow$  ZeroRules  $\cup$  row
7:   end if
8: end for
9: return ZeroRules

```

---

**Algorithm 3** CoverageCalc(RowIds, Rules, type)

---

```

1: coverage  $\leftarrow \{\phi, \dots, \phi\}$ 
2: for each rule in Rules do
3:   for each Id in RowIds do
4:     if (type==0 and attributes conditions of Id  $\subseteq$  rule) OR
       (type==1 and rule  $\subseteq$  attributes conditions of Id) then
5:       coverage[rule]  $\leftarrow$  coverage[rule]  $\cup$  Id
6:     end if
7:   end for
8: end for
9: return coverage

```

---

two helper functions: i) findZeroRules (Algorithm 2) and ii) CoverageCalc (Algorithm 3). findZeroRules takes as input ZeroRowIds and returns the minimum set of Permission Zero Rows that encapsulate all the Zero rows such that each Zero row is a subset of atleast one ZeroRule. This is done by sorting the Zero Rows in descending order based on the number of attribute conditions in each row and then by adding each row that is not already covered by some rule to the ZeroRules.

The CoverageCalc function is used to find OneRowCoverage and ZeroRowCoverage. CoverageCalc takes as input the OneRowIds or ZeroRowIds,  $\Pi$  or ZeroRules and type as 1 for OneRowCoverage and 0 for ZeroRowCoverage. It returns the corresponding list of sets called coverage in Line 9 (OneRowCoverage or ZeroRowCoverage depending on the type). This is accomplished by simply iterating over each rule and each row provided as input and checking if the rule is a subset (superset) of the role if the ZeroRowCoverage (correspondingly, OneRowCoverage) is requested.

**EXAMPLE 1.** Consider the UOP given in Table 5. The existing ABAC rules in the system are :  $[(uc_3, oc_2), (uc_1, uc_2, oc_1)]$ . By performing the **Pre-processing Steps**, we get:

ZeroRowIds = [1, 2, 4, 7, 9]

ZeroRules =  $[(uc_1, uc_2, oc_2, oc_3), (uc_2, oc_1, oc_2), (uc_1, uc_3, oc_1)]$

ZeroRowCoverage = [(7, 9), (1, 4), (2)]

ZeroRuleIds = [9, 4, 2]

OneRowIds = [3, 5, 6, 8]

OneRowCoverage = [(3, 6), (5, 8)]

**Table 5: Illustrative example: UOP**

Row Id	<i>u - o</i>	<i>uc</i> <sub>1</sub>	<i>uc</i> <sub>2</sub>	<i>uc</i> <sub>3</sub>	<i>oc</i> <sub>1</sub>	<i>oc</i> <sub>2</sub>	<i>oc</i> <sub>3</sub>	<i>p</i>
1	<i>u</i> <sub>1</sub> <i>o</i> <sub>1</sub>	0	1	0	1	0	0	0
2	<i>u</i> <sub>2</sub> <i>o</i> <sub>1</sub>	1	0	1	1	0	0	0
3	<i>u</i> <sub>3</sub> <i>o</i> <sub>1</sub>	1	1	0	1	0	0	1
4	<i>u</i> <sub>1</sub> <i>o</i> <sub>2</sub>	0	1	0	1	1	0	0
5	<i>u</i> <sub>2</sub> <i>o</i> <sub>2</sub>	1	0	1	1	1	0	1
6	<i>u</i> <sub>3</sub> <i>o</i> <sub>2</sub>	1	1	0	1	1	0	1
7	<i>u</i> <sub>1</sub> <i>o</i> <sub>3</sub>	0	1	0	0	1	1	0
8	<i>u</i> <sub>2</sub> <i>o</i> <sub>3</sub>	1	0	1	0	1	1	1
9	<i>u</i> <sub>3</sub> <i>o</i> <sub>3</sub>	1	1	0	0	1	1	0

**Algorithm 4** AddPermission(*D*,  $\Pi$ , *m\_user*, *m\_object*, *I*)

---

```

1: m_rowid  $\leftarrow$  Row Id of m_user and m_object in the UOP
2: m_row  $\leftarrow$  attribute condition set of m_row
3: Delete_Perm0Rows ([m_rowid])
4: Add_Perm1Rows ([m_row],[m_rowid])

```

---

**4.2 Handling Add Permission**

Algorithm 4 gives the procedure to grant *m\_user* the permission to access *m\_object*. This is done by removing the corresponding row from the list of permission zero rows and adding to the list of permission one rows. Two helper functions are used to accomplish this: i) Delete\_Perm0Rows (Algorithm 5) and ii) Add\_Perm1Rows (Algorithm 6).

**Algorithm 5** Delete\_Perm0Rows(*del0rowsIds*)

---

```

1: R_ZeroRules, R_RuleIds  $\leftarrow \phi$ 
2: for each Id  $\in$  del0rowsIds do
3:   ZeroRowIds  $\leftarrow$  ZeroRowIds  $\setminus$  Id
4:   for each cover  $\in$  ZeroRowCoverage do
5:     if Id  $\subseteq$  cover then
6:       if Id  $\in$  ZeroRuleIds then
7:         R_ZeroRules  $\leftarrow$  R_ZeroRules  $\cup$  findZeroRules
           (cover  $\setminus$  Id)
8:         R_RuleIds  $\leftarrow$  R_RuleIds  $\cup$  Index of cover
9:       else
10:        cover  $\leftarrow$  cover  $\setminus$  Id
11:      end if
12:    end if
13:  end for
14: end for
15: Delete rules in ZeroRules at row numbers in R_RuleIds
16: Delete covers in ZeroRowCoverage at row numbers in
   R_RuleIds
17: R_ZeroRowCoverage  $\leftarrow$  CoverageCalc(ZeroRowIds, R_ZeroRules, 0)
18: ZeroRules  $\leftarrow$  ZeroRules  $\cup$  R_ZeroRules
19: ZeroRowCoverage  $\leftarrow$  ZeroRowCoverage  $\cup$ 
   R_ZeroRowCoverage
20: ZeroRuleIds  $\leftarrow$  findZeroRuleRows (ZeroRules)

```

---

**Delete\_Perm0Rows** (*del0rowsIds*) Algorithm 5 gives the specific steps for removing a permission. First, we remove the row from

the permission zero rows (Line 3). Now, we update the intermediary data structures. First we update the *ZeroRowCoverage* mapping. If the permission row to be removed is a rule in *ZeroRules* then we need to recompute the rule by removing it from the set of zero permission rows covered by that rule (lines 7-8). Of course, if this is the only zero permission row represented by that rule, then it is eliminated altogether. Otherwise the permission row is removed from the cover of every rule in *ZeroRules* it belongs to (line 10). Lines 15-20 update the *ZeroRules*, *ZeroRuleIds*, and the *ZeroRowCoverage* by first removing the appropriate rules and affected covers, and then adding in the additional rules prior calculated (at line 7) and recalculating the cover corresponding to those rules (line 17).

**Add\_Perm1Rows(add1rows, add1rowsIds):** Algorithm 6 gives the specific steps for adding a permission one row. This function adds the rows given in *add1rows* to the ABAC system and re-mines the policy. To do this, the ABAC-SRM function is used, but instead of passing in the entire *UOP*, only the *ZeroRules*, *add1rows* and  $\Pi$  are used since they encapsulate the entire *UOP*, and therefore the mining is much more efficient, as confirmed by the experimental evaluation. We then update the *OneRowIds* and the *OneRowCoverage* using CoverageCalc (Algorithm 3).

**EXAMPLE 2 (ADD PERMISSION:  $u_3$  GETS ACCESS  $o_3$ ).** Granting  $u_3$  access to  $o_3$ , means we have to make the permission in RowId 9 equal to 1. This effectively means we have to delete the Permission Zero, Row Id 9 from the *UOP* and add a Permission One row with the same attribute conditions. Therefore, Algorithm 4 calls Delete\_Perm0Rows with [9] and Add\_Perm1Rows with argument  $((uc_1, uc_2, oc_2, oc_3), [9])$ , obtaining the output given below:  
 $m\_row = (uc_1, uc_2, oc_2, oc_3)$ ,  $m\_rowid = 9$

**Delete\_Perm0Rows([9])**

*ZeroRowIds* = [1,2,4,7]

*ZeroRules* =  $((uc_2, oc_1, oc_2), (uc_1, uc_3, oc_1), (uc_2, oc_2, oc_3))$

*ZeroRowCoverage* = [(1,4),(2),(7)]

*ZeroRuleIds* = [4,2,7]

**Add\_Perm1Rows([(uc<sub>1</sub>,uc<sub>2</sub>,oc<sub>2</sub>,oc<sub>3</sub>)],[9])**

$\Pi = ((uc_3, oc_2), (uc_1, uc_2))$

*OneRowIds* = [3,5,6,8,9]

*OneRowCoverage* = [(5,8),(3,6,9)]

### 4.3 Handling Delete Permission

Algorithm 7 gives the specific steps to revoke  $m\_user$ 's permission to access  $m\_object$ . This is done by removing the corresponding row from the list of permission one rows and adding to the list of permission zero rows. Two helper functions are used to accomplish this: i) Delete\_Perm1Rows (Algorithm 8) and ii) Add\_Perm0Rows (Algorithm 9).

**Delete\_Perm1Rows (del1rowsIds):** Algorithm 8 gives the specific steps to delete permission one rows from the ABAC system. Note that whenever a permission one row is deleted, some

---

#### Algorithm 7 DeletePermission( $D, \Pi, m\_user, m\_object$ )

---

```

1:  $m\_rowid \leftarrow$  Row Id of  $m\_user$  and  $m\_object$  in the UOP
2:  $m\_row \leftarrow$  Attribute condition set of  $m\_rowid$ 
3: Delete_Perm1Rows ([ $m\_rowid$ ])
4: Add_Perm0Rows ([ $m\_row$ ],[ $m\_rowid$ ])

```

---



---

#### Algorithm 8 Delete\_Perm1Rows (del1rowsIds)

---

```

1:  $ridinvalid, minerowids, minerows \leftarrow \phi$ 
2:  $ridinvalid \leftarrow$  Indices of covers in OneRowCoverage having any  $Id$  from del1rowsIds
3: for  $r$  in ridinvalid do
4:    $minerowids \leftarrow minerowids \cup (cover \text{ of } OneRowCoverage \text{ at } r \setminus del1rowsIds)$ 
5: end for
6: Delete rules in  $\Pi$  and covers in OneRowCoverage at row numbers in ridinvalid
7:  $minerows \leftarrow$  List of attribute condition sets of rows in minerowids
8:  $\Pi \leftarrow$  AbacMining (minerows, ZeroRules,  $\Pi$ )
9: OneRowIds  $\leftarrow OneRowIds \setminus del1rowsIds$ 
10: OneRowCoverage  $\leftarrow$  CoverageCalc (OneRowIds,  $\Pi$ , 1)

```

---



---

#### Algorithm 9 Add\_Perm0Rows(add0rows, add0rowsIds)

---

```

1:  $ridinvalid, minerowids, minerows \leftarrow \phi$ 
2:  $ridinvalid \leftarrow$  Indices of rules in  $\Pi$  that are subset of any row from add0rows
3:  $minerowids \leftarrow$  row Ids covering all ridinvalid (from OneRowCoverage)
4:  $minerows \leftarrow$  List of attribute condition sets of rows in minerowids
5:  $\Pi \leftarrow \Pi \setminus ridinvalid$ 
6: Delete cover in OneRowCoverage at all numbers in ridinvalid
7: for row in add0rows do
8:   for  $zrule$  in ZeroRules do
9:     if  $zrule \subset row$  then
10:       replace  $zrule$  with row
11:     else if  $row \not\subset zrule$  then
12:        $ZeroRules \leftarrow ZeroRules \cup row$ 
13:     end if
14:   end for
15: end for
16: ZeroRowIds  $\leftarrow ZeroRowIds \cup add0rowsIds$ 
17: Update ZeroRuleIds, ZeroRowCoverage
18:  $\Pi \leftarrow$  ABAC-SRM(minerows, ZeroRules,  $\Pi$ )

```

---

ABAC rules become invalid. These rules are found in Line 2, using *OneRowCoverage*. Every  $Id$  in *del1rowsIds* is checked in every cover of *OneRowCoverage*. If an  $Id$  is in a cover, the index of the cover is added to *ridinvalid*. The numbers in *ridinvalid* signify that those rules in  $\Pi$  have become invalid. Next, in Lines 3 - 5, for all  $r$  in *ridinvalid*, *minerowids* is evaluated, which is *cover* at  $r$  (in *OneRowCoverage*) after the *del1rowsIds* are deleted from it. The  $\Pi$  and covers in *OneRowCoverage* are deleted at row numbers in *ridinvalid* in Line 6.

---

#### Algorithm 6 Add\_Perm1Rows(add1rows, add1rowsIds):

---

```

1:  $\Pi \leftarrow$  ABAC-SRM (add1rows, ZeroRules,  $\Pi$ )
2: OneRowIds  $\leftarrow OneRowIds \cup add1rowsIds$ 
3: OneRowCoverage  $\leftarrow$  CoverageCalc(OneRowIds,  $\Pi$ , 1)

```

---

The list of attribute conditions of the rows in *minerowids* is put in *minerows* in Line 7. In Line 8, *rowsleftattributes* are then used to mine new  $\Pi$  using the algorithm ABAC-SRM. In Lines 9 - 10, *OneRowIds* are updated by removing the *del1rowIds* from them and *OneRowCoverage* is also updated by using *CoverageCalc* function in Algorithm 3.

**Add\_Perm0Rows(*add0rows*, *add0rowsIds*):** Algorithm 9 gives the specific steps to add permission zero rows. It adds the *add0rows* to the ABAC system. When permission zero rows are added, some rule in  $\Pi$  may become invalid. If an ABAC rule is subset of a Permission Zero row, the rule becomes invalid. In Line 2, we find any such rules that become invalid. For each *row* in *add0rows*, and for all  $\Pi$ , if any *rule* in  $\Pi$  is a subset of any *row* in *add0rows*, index of that *rule* is added to *ridinvalid*. In Line 3, for all rules in *ridinvalid*, the row Ids in *OneRowCoverage* are added to *minerowids* and in Line 4, the attribute conditions of all rows in row Ids of *minerowids* are made into list and added to *minerows*. Next, in Line 5 and 6, at the row numbers in *ridinvalid*, we delete the  $\Pi$  and *covers* in *OneRowCoverage*. In Lines, 7-15, we update the *ZeroRules* by adding the *add0rows*. If a rule in *ZeroRules* is a subset of a row in *add0rows*, then the rule is replaced with the row in *add0rows*; the row in *add0rows* is added to *ZeroRules* if it is not subset of any rule in *ZeroRules*. In Line 16, the *add0rowsIds* are added to *ZeroRowIds*. Also in Line 17, *ZeroRuleIds* and *ZeroRowCoverage* are updated. Finally, in Line 18,  $\Pi$  are updated using the ABAC-SRM mining algorithm. As earlier, the mining is much more efficient in practice since it only utilizes the *ZeroRules* and the  $\Pi$  as opposed to the entire *UOP*.

**EXAMPLE 3 (REMOVING  $u_2$ 's ACCESS TO  $o_3$ ).** This means we have to make the permission in RowId 8 equal to 0. This effectively means we have to delete the Permission One, Row Id 8 from the *UOP* and add a Permission Zero row with same attributes conditions. Therefore, Algorithm 7 calls *Delete\_Perm1Rows* with [8] and *Add\_Perm0Rows* with  $[(uc_1, uc_3, oc_2, oc_3), [8]]$ , obtaining the output given below:

$m\_row = (uc_1, uc_3, oc_2, oc_3)$ ,  $m\_rowid = 8$

**Delete\_Perm1Rows([8])**

$\Pi = [(uc_1, uc_2, oc_1), (uc_3, oc_2)]$

$OneRowIds = [3, 5, 6]$

$OneRowCoverage = [(3, 6), (5)]$

**Add\_Perm0Rows([(uc<sub>1</sub>, uc<sub>3</sub>, oc<sub>2</sub>, oc<sub>3</sub>), [8]])**

$ZeroRules = [(uc_1, uc_2, oc_2, oc_3), (uc_2, oc_1, oc_2), (uc_1, uc_3, oc_1), (uc_1, uc_3, oc_2, oc_3)]$

$ZeroRuleRows = [9, 4, 2, 8]$

$ZeroRowIds = [1, 2, 4, 7, 9, 8]$

$\Pi = [(uc_1, uc_2, oc_1), (uc_3, oc_1, oc_2)]$

$OneRowCoverage = [(3, 6), (5)]$

$ZeroRowCoverage = [(7, 9), (1, 4), (2), (8)]$

#### 4.4 Handling Add Attribute Value

Algorithm 10 gives the specific steps to add the attribute value *m\_attribute* to user *m\_user*. This is done in four steps: i) we extract all permission zero rows and permission one rows for *m\_user* and the corresponding attribute sets (lines 1-4); ii) we remove the corresponding rows from the permission zero and permission one rows; iii) we update the attributes sets; iv) we insert the updated rows into

the permission zero rows and permission one rows. To ensure that the intermediary data structures are consistently maintained, the four prior defined functions i) *Delete\_Perm0Rows* (Algorithm 5); ii) *Delete\_Perm1Rows* (Algorithm 8); iii) *Add\_Perm0Rows* (Algorithm 9) and iv) *Add\_Perm1Rows* (Algorithm 6) are used to accomplish this. Note that an attribute value can also be added to an object in exactly the same way.

---

#### Algorithm 10 AddAttribute(*D*, $\Pi$ , *m\_user*, *m\_attribute*)

---

- 1:  $m\_rowids1 \leftarrow$  List of Row Ids of Permission One Rows of *m\_user* in the *UOP*
  - 2:  $m\_rowids0 \leftarrow$  List of Row Ids of Permission Zero Rows of *m\_user* in the *UOP*
  - 3:  $m\_rows1 \leftarrow$  List of attribute condition sets of all rows in *m\_rowids1*
  - 4:  $m\_rows0 \leftarrow$  List of attribute condition sets of all rows in *m\_rowids0*
  - 5: *Delete\_Perm0Rows* (*m\_rowids0*)
  - 6: *Delete\_Perm1Rows* (*m\_rowids1*)
  - 7: Add the *m\_attribute* to the *m\_rows0* and *m\_rows1*
  - 8: *Add\_Perm0Rows* (*m\_rows0*, *m\_rowids0*)
  - 9: *Add\_Perm1Rows* (*m\_rows1*, *m\_rowids1*)
- 

**EXAMPLE 4 (ADD ATTRIBUTE VALUE:  $u_1$  GETS  $uc_3$ ).** Adding attribute condition  $uc_3$  to user  $u_1$ , requires removing all the rows of user  $u_1$ , i.e. Row Ids 1, 4 and 7. Then we have to add the attribute condition  $uc_3$  to the attribute condition set of these rows and add them back to the data set. Therefore, Algorithm 10 calls *Delete\_Perm0Rows* with [1, 4, 7], *Delete\_Perm1Rows* with  $\phi$ , *Add\_Perm0Rows* with  $[(uc_2, uc_3, oc_1), (uc_2, uc_3, oc_1, oc_2), (uc_2, uc_3, oc_2, oc_3)], [1, 4, 7]$  and *Add\_Perm1Rows* with  $(\phi, \phi)$  obtaining the output given below:

$m\_rowids0 = [1, 4, 7]$ ,  $m\_rowids1 = \phi$

$m\_rows0 = [(uc_2, oc_1), (uc_2, oc_1, oc_2), (uc_2, oc_2, oc_3)]$ ,  $m\_rows1 = \phi$

**Delete\_Perm0Rows([1, 4, 7])**

$ZeroRowIds = [2, 9]$

$ZeroRules = [(uc_1, uc_2, oc_2, oc_3), (uc_1, uc_3, oc_1)]$

$ZeroRowCoverage = [(9), (2)]$

$ZeroRuleIds = [2, 9]$

**Delete\_Perm1Rows( $\phi$ )**

**Add\_Perm0Rows([(uc<sub>2</sub>, uc<sub>3</sub>, oc<sub>1</sub>), (uc<sub>2</sub>, uc<sub>3</sub>, oc<sub>1</sub>, oc<sub>2</sub>), (uc<sub>2</sub>, uc<sub>3</sub>, oc<sub>2</sub>, oc<sub>3</sub>), [1, 4, 7])**

$ZeroRules = [(uc_1, uc_2, oc_2, oc_3), (uc_1, uc_3, oc_1), (uc_2, uc_3, oc_1, oc_2), (uc_2, uc_3, oc_2, oc_3)]$

$ZeroRowIds = [2, 9, 1, 4, 7]$

$ZeroRuleIds = [9, 2, 4, 7]$

$\Pi = (uc_1, uc_2, oc_1)(uc_1, uc_3, oc_3)$

$ZeroRowCoverage = [(9), (2), (4, 1), (7)]$

$OneRowCoverage = [(3, 6), (5, 8)]$

**Add\_Perm1Rows( $\phi, \phi$ )**

#### 4.5 Handling Delete Attribute Value

Algorithm 11 gives the specific steps to remove attribute value *m\_attribute* from user *m\_user*. This works exactly the same as Algorithm 10, except that in line 7, we delete *m\_attribute* from

the permission zero and permission one rows for  $m\_user$ , before updating all the intermediary data structures.

---

**Algorithm 11** DeleteAttribute( $D, \Pi, m\_user, m\_attribute$ )

---

- 1:  $m\_rowids1 \leftarrow$  List of Row Ids of Permission One Rows of  $m\_user$  in the UOP
  - 2:  $m\_rowids0 \leftarrow$  List of Row Ids of Permission Zero Rows of  $m\_user$  in the UOP
  - 3:  $m\_rows1 \leftarrow$  List of attribute condition sets of all rows in  $m\_rowids1$
  - 4:  $m\_rows0 \leftarrow$  List of attribute condition sets of all rows in  $m\_rowids0$
  - 5: Delete\_Perm0Rows( $m\_rowids0$ )
  - 6: Delete\_Perm1Rows( $m\_rowids1$ )
  - 7: Delete the  $m\_attribute$  from the  $m\_rows0$  and  $m\_rows1$
  - 8: Add\_Perm0Rows( $m\_rows0, m\_rowids0$ )
  - 9: Add\_Perm1Rows( $m\_rows1, m\_rowids1$ )
- 

EXAMPLE 5 (DELETE ATTRIBUTE VALUE:  $u_2$  LOSES  $uc_1$ ). Removing attribute condition  $uc_1$  from user  $u_2$  requires removing all the rows of user  $u_2$ , i.e. Row Ids 2, 5 and 8. Then we have to remove the attribute condition  $uc_1$  from the attribute condition set of these rows and add them back to the dataset. Therefore, Algorithm 11 calls Delete\_Perm0Rows with [2], Delete\_Perm1Rows with [5, 8], Add\_Perm0Rows with  $[(uc_3, oc_1)]$ , [2] and Add\_Perm1Rows with  $[(uc_3, oc_1, oc_2), (uc_3, oc_2, oc_3)], [5, 8]$  obtaining the output given below:

$m\_rowids1 = [5, 8], m\_rowids0 = [2]$

$m\_rows1 = [(uc_1, uc_3, oc_1, oc_2), (uc_1, uc_3, oc_2, oc_3)]$

$m\_rows0 = [(uc_1, uc_3, oc_1)]$

**Delete\_Perm0Rows([2])**

ZeroRules =  $(uc_1, uc_2, oc_2, oc_3), (uc_2, oc_1, oc_2)$

ZeroRowCoverage =  $[(7, 9), (1, 4)]$

ZeroRuleIds = [9, 4]

**Delete\_Perm1Rows([5, 8])**

$\Pi = [(uc_1, oc_1)]$

OneRowIds = [3, 6]

OneRowCoverage = [(3, 6)]

**Add\_Perm0Rows([(uc\_3, oc\_1)], [2])**

ZeroRules =  $[(uc_1, uc_2, oc_2, oc_3), (uc_2, oc_1, oc_2), (uc_3, oc_1)]$

ZeroRowIds = [1, 4, 7, 9, 2]

ZeroRuleIds = [9, 4, 2]

$\Pi = [(uc_1, oc_1)]$

OneRowCoverage = [(3, 6)]

ZeroRowCoverage =  $[(7, 9), (1, 4), (2)]$

**Add\_Perm1Rows([(uc\_3, oc\_1, oc\_2), (uc\_3, oc\_2, oc\_3)], [5, 8])**

$\Pi = [(uc_1, oc_1), (uc_3, oc_2)]$

OneRowIds = [3, 6, 5, 8]

OneRowCoverage = [(3, 6), (5, 8)]

## 5 EXPERIMENTAL EVALUATION

We carried out detailed experiments to study the effectiveness of the proposed approach in a wide variety of settings, and to understand the effect of different factors. There are no real datasets available that capture the incremental change in ABAC policies. So we ran

Parameter	Default Value
Users	40
Objects	60
User Attributes	60
Object Attributes	60
Rules	40

**Table 6: Default values of Parameters**

experiments on synthetic datasets and controlled the degree of changes and examined the effect of each parameter independently.

We have used the synthetic dataset generator introduced by Talukdar et al. in [20] to create ABAC policies. The input data set for the four ABAC maintenance algorithms and ABAC Mining (using ABAC-SRM) are the same.

ABAC Maintenance algorithms for each type of change were implemented considering a single modification at a time and without putting constraints to perform a fair comparison with ABAC-SRM algorithm. The ABAC Maintenance algorithms can handle multiple permissions and constraints.

For each set of parameter values, synthetic data was created. The default values for the various parameters are given in Table 6. In each experiment, we vary one parameter of interest while the rest are set to the default values given in Table 6.

ABAC rules were mined from the dataset using the ABAC-SRM algorithm. While using the proposed ABAC Maintenance algorithm, pre-processing steps were carried out and recorded as Pre-Processing Time. Further, for every change type (four ABAC Maintenance Algorithms: Add Permission, Delete Permission, Add Attribute value, Delete Attribute value), a random possible input (user and object or user and attribute value) is identified and both ABAC Maintenance and ABAC-SRM algorithms are used to accommodate the change. For all four change types, this process was repeated for 20 random possible inputs on a data set. For Add attribute value and Delete attribute value, we have performed experiments for addition and deletion of attribute in users. The results will be similar for object attributes and environment attributes.

Our objective is to compare the difference in time taken by the two approaches for different types of changes. Therefore, we observed: (I) the time taken for redoing the ABAC Mining from scratch; (II) the time taken for pre-processing to generate the intermediary data structures; and (III) the time taken for incrementally updating the policy as well as the intermediary data structures.

Note that without incremental maintenance, the time required for any change is given by (I). If incremental maintenance is used, then the time given by (II) is a one-time cost, while the time given by (III) is incurred for each change. From the figures, it is observed that for all the cases, ABAC Maintenance (III) is more efficient than ABAC-SRM (I). In fact, ABAC Maintenance (III) with the Pre-processing steps (II) also performs better than ABAC-SRM (I).

Figure 3 gives the average running time for adding a permission. Figure 3a shows the time taken when the User-Object Count is varied. It can be observed that the time taken for mining, pre-processing and incremental update all increase linearly. However, the overall time taken by the incremental approach is significantly less. Figure 3b shows the time taken when the rule count is varied.



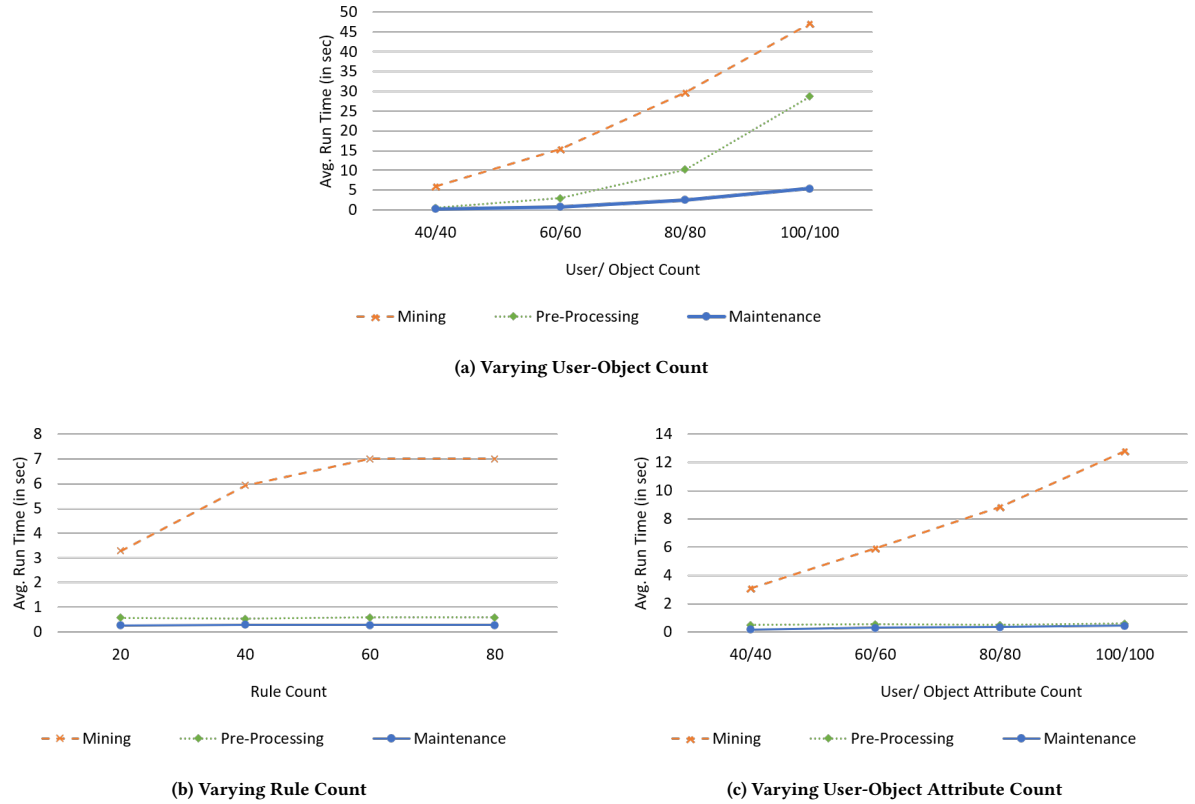


Figure 3: Running Time for Add Permission

Here, it can be observed that the time taken by the incremental approach is independent of the number of rules, whereas the time taken for mining increases, though it plateaus after about 60 rules. The overall time taken by the incremental approach is again significantly less. Finally, Figure 3c shows the results when the user-object attribute count is varied. Here, it is observed that the time taken by the incremental approach is again independent of the number of attribute values, whereas the time required for mining increases linearly with it. Figures 4, 5, and 6 give the average running time for deleting a permission, adding an attribute value, and deleting an attribute value respectively. The behavior in all three cases is very similar to that in Figure 3.

#### Quality of the results:

We also looked at the rules generated by our incremental approach and compared them to the rules obtained directly through mining. The experiments show that over the course of all 960 runs, in 598 of the cases, the rules generated are *exactly the same*, and only in 362 cases are the results different. Furthermore, even in those 362 cases, the number of rules generated by our incremental approach is no more than 3% more than the number of rules obtained directly through mining. This clearly shows that the quality of the results obtained through the incremental approach is very close to that obtained through mining.

## 6 RELATED WORK

To the best of our knowledge, maintenance of ABAC policies has been studied for the first time in this paper. Hence, there are no previous work directly related to this problem. However, there are works in field of ABAC Mining, incremental FD mining and incremental maintenance of databases, which are discussed below. **ABAC Mining:** The standard for ABAC model can be found in [9]. ABAC Mining has been studied by many researchers. Xu et al. [23] are the first to propose an approach for ABAC Mining. Their approach iterates over tuples in the user-permission relation and constructs candidate rules. Then it generalizes the candidate rule to cover additional tuples by using merging techniques. Medvet et al. [16] have proposed an evolutionary approach that is separate and conquer algorithm, where at every iteration, a new rule is generated and the set of access requests is reduced to a smaller size. The efficiency of this approach is not very different when compared to that in [23]. Mocanu et al. [17] have proposed a deep learning model (Restricted Boltzmann Machines) trained on logs to generate candidate rules. Their system is still under development. Iyer et al. [10] have presented an approach to mine ABAC policies having both positive and negative authorization rules. The approach is based on the rule mining algorithm called PRISM. Gautam et al. [7] have discussed a constrained policy mining algorithm that generates a set of ABAC rules, such that the total weight of all the rules in the mined policy is minimum and no individual rule

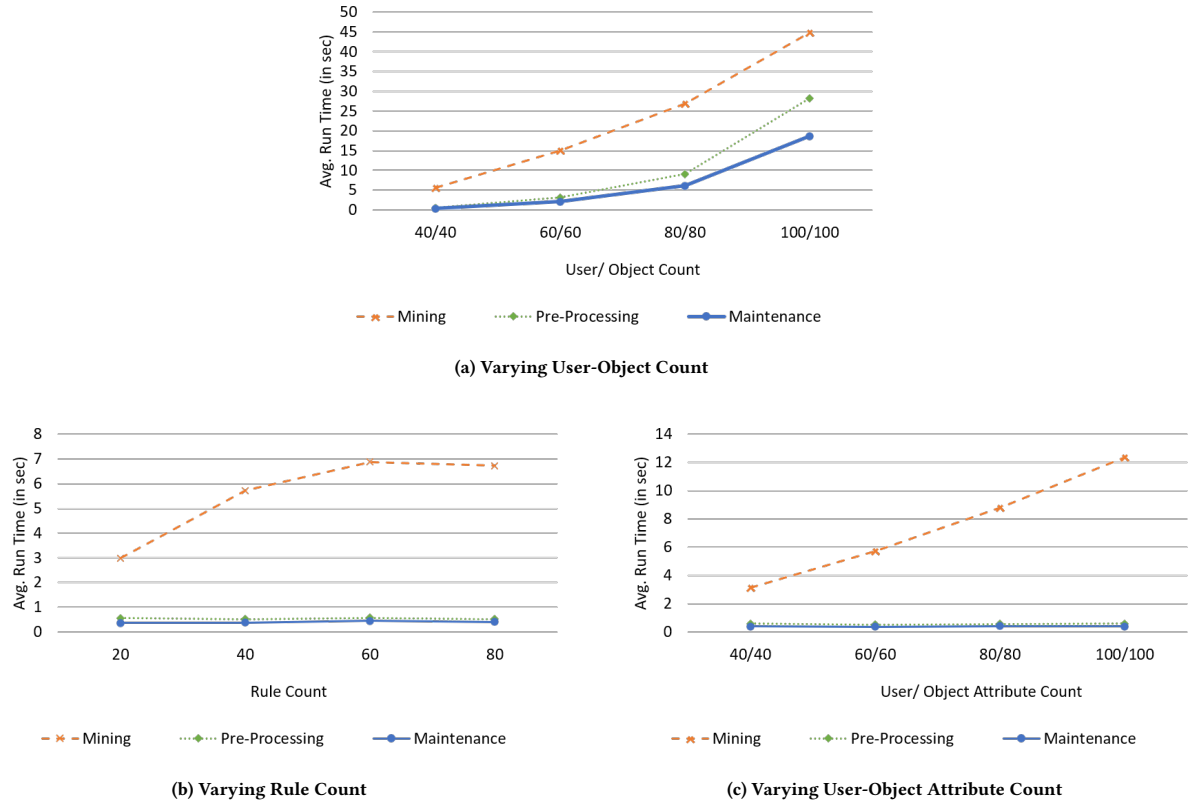


Figure 4: Running Time for Delete Permission

can have weight greater than a pre-specified constraint. Cotrini et al. [5] have proposed an algorithm for mining ABAC rules from sparse access logs. The algorithm, called Rhapsody, is built upon subgroup discovery algorithm called APRIORI-SD.

Karimi and Joshi [13] have proposed an approach to apply clustering algorithms over the decision examples to predict rules. Karimi et al. [14] have also proposed an unsupervised learning-based technique for detecting patterns in a set of access records and extracting ABAC policy rules from these patterns. They have presented two algorithms, rule pruning and policy refinement that improve quality of mined policy. The latter is useful in ABAC policy maintenance. Bertino et al. [12] have proposed an approach, called Polisma, for learning ABAC policies. It combines data mining, statistical, and machine learning techniques, with potential context information obtained from external sources to learn a better model. Iyer et al. [11] have proposed an algorithm for mining ReBAC policies, and an approach to mine graph transition policies. Gupta et al. [8] have proposed dynamic groups with attribute-based access control model for smart cars ecosystem.

Talukdar et al. [20] have used a subset enumeration approach to discover the ABAC rules in a bottom-up fashion. In this paper, we have chosen to develop our incremental maintenance approach on the ABAC-SRM mining algorithm proposed by [20] as they have shown that they take an order of magnitude less time than [23]. Also, both the algorithms ([20] and [23]) discover almost the same

number of rules; whereas [20] has better WSC [18] of the rules than [23]. It is to be noted that the mining approaches in [20] and [23] do not consider unrepresented attribute value combinations [2] as these do not exist in the current authorization set. Better mining algorithms will need to be devised to tackle this issue. However, with respect to maintenance, if an existing user is authorized access to an object with attribute values from unrepresented set, the incremental mining approach can handle this in terms of updating the policy by deleting the previous attribute and adding the new attribute to the user/object. We require the maintenance algorithm to be as fast as possible and to the best of our knowledge, the time results of this algorithm are one of the best. While all the above approaches focus on mining of ABAC policies, none of them attempt to perform incremental maintenance of the policies when changes occur. The idea in [20] is that ABAC rules are nothing but a set of Functional Dependencies. Based on this premise, we have performed a review of incremental FD mining algorithms which also inspired us to develop and implement our approach.

**Incremental FD Mining:** Caruccio et al. [1] represent FDs in a bit-vector. Their approach employs an upward and downward search strategy, and updates the set of Functional Dependencies on addition of new tuples to the database. Wang et al. [21] have proposed to add new set of tuples to the database based on concept of tuple partitions and the monotonicity of the Functional Dependencies and avoid re-scanning of the database. In [22], Wang et al. have

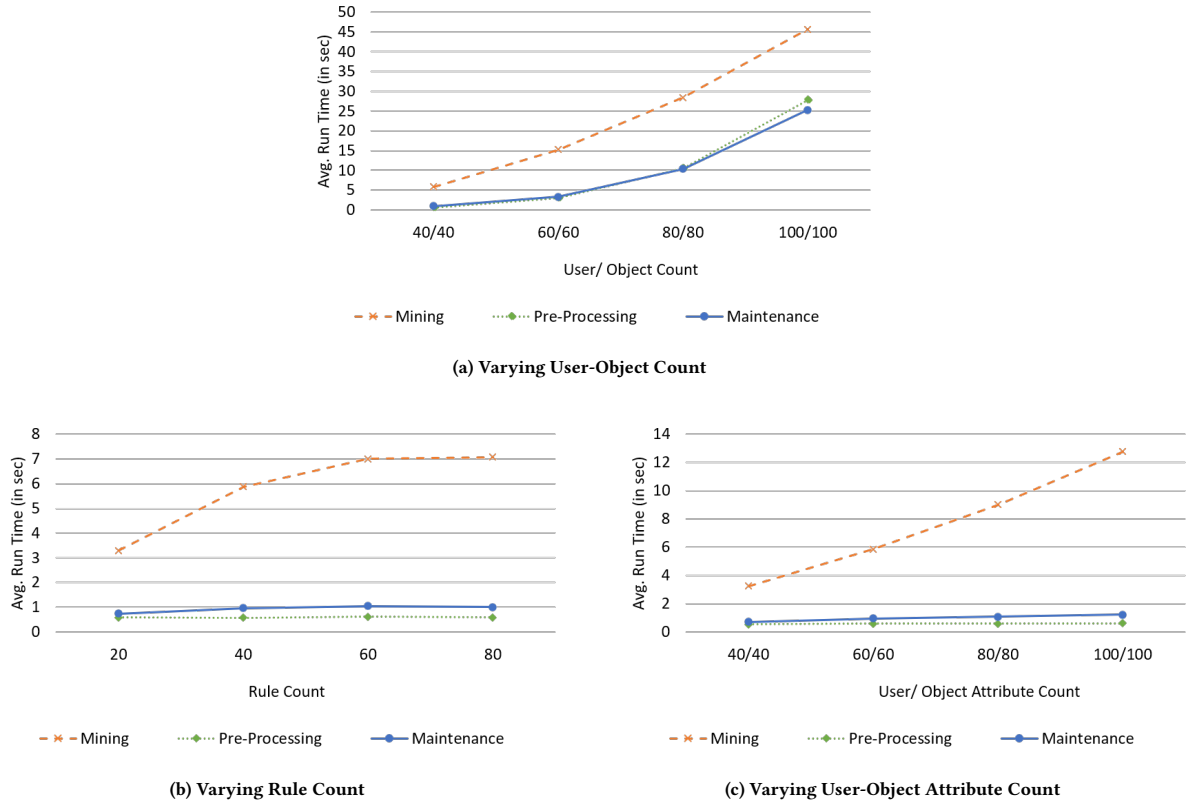


Figure 5: Running Time for Add Attribute Value

also given a Functional Dependency maintenance algorithm which deals with tuple deletion. Also, Gasmi et al. [6] have proposed an algorithm to maintain the canonical Functional Dependencies incrementally when a new tuple is appended to the original database. Our approach is mostly inspired by the work of Schirmer et al.'s DynFD [19]. They maintain Functional Dependencies for a dynamic dataset using a bottom up and top down approach, and indices to evolve the Functional Dependencies. For a batch of operations, insert, update and delete of data, the algorithm adapts its validation data structures, and a positive and negative cover of Functional Dependencies.

**Incremental Maintenance in Databases:** Besides the above, incremental maintenance has been studied extensively in data bases. Cheung et al. [3] use incremental updating technique to update the association rules in large databases whenever new transactions are added to the database. Also in [4], Cheung et al. have proposed algorithms for frequent pattern mining in a database and to allow mining in a single pass over the database as well as insertion or deletion of transactions in an efficient manner.

Lin et al. [15] have proposed an efficient incremental algorithm for transaction insertion. The algorithm reduces computations without candidate generation and is based on the utility-list structures.

## 7 CONCLUSIONS AND FUTURE WORK

In this paper, we have examined the problem of maintenance of ABAC policies in an incremental fashion. We have formalized this problem and proposed an efficient algorithm to maintain ABAC policies considering four types of changes. We have experimentally evaluated the performance of the proposed algorithm and showed that it takes significantly less time to perform a change when compared to redoing ABAC mining from scratch.

In the future, we plan to develop an approach that would allow batching of changes and optimally switch between incremental maintenance and re-mining. We plan to study the consistency and scalability aspects of this approach. We would also like to implement the algorithm for negative authorizations and by adding noise. Also, we plan to implement the ABAC maintenance approach when there are constraints such as mutual exclusion, preconditions, obligations, SoD, attribute-attribute conditions, etc.

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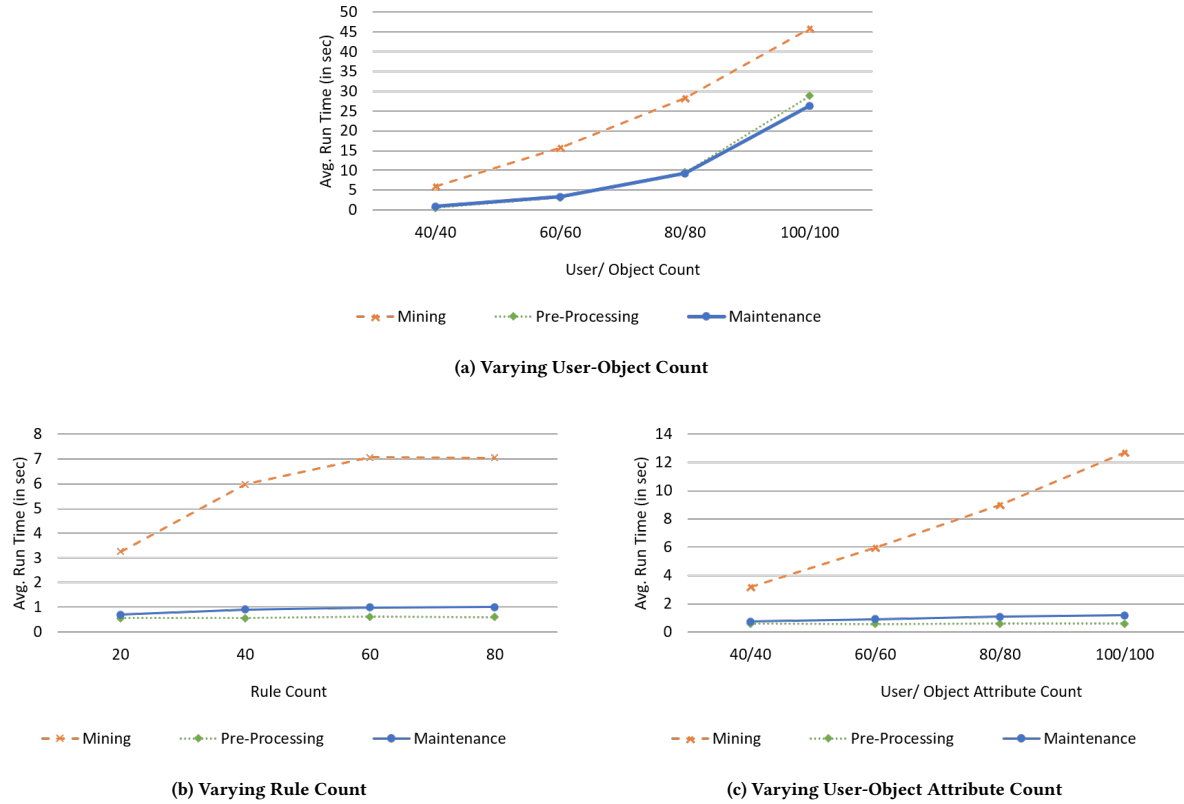


Figure 6: Running Time for Delete Attribute Value

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