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## A complete search for redshift $z \gtrsim 6.5$ quasars in the VIKING survey

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#### **ABSTRACT**

We present the results of a new, deeper, and complete search for high-redshift 6.5 < z < 9.3 quasars over 977 deg<sup>2</sup> of the VISTA Kilo-Degree Infrared Galaxy (VIKING) survey. This exploits a new list-driven data set providing photometry in all bands Z, Y, J, H, K<sub>s</sub>, for all sources detected by VIKING in J. We use the Bayesian model comparison (BMC) selection method of Mortlock et al., producing a ranked list of just 21 candidates. The sources ranked 1, 2, 3, and 5 are the four known z > 6.5quasars in this field. Additional observations of the other 17 candidates, primarily DESI Legacy Survey photometry and ESO FORS2 spectroscopy, confirm that none is a quasar. This is the first complete sample from the VIKING survey, and we provide the computed selection function. We include a detailed comparison of the BMC method against two other selection methods: colour cuts and minimum- $\chi^2$  SED fitting. We find that: (i) BMC produces eight times fewer false positives than colour cuts, while also reaching 0.3 mag deeper, (ii) the minimum- $\chi^2$  SED-fitting method is extremely efficient but reaches 0.7 mag less deep than the BMC method, and selects only one of the four known quasars. We show that BMC candidates, rejected because their photometric SEDs have high  $\chi^2$  values, include bright examples of galaxies with very strong [O III]  $\lambda\lambda4959,5007$  emission in the Y band, identified in fainter surveys by Matsuoka et al. This is a potential contaminant population in Euclid searches for faint z > 7 quasars, not previously accounted for, and that requires better characterization.

Key words: quasars: general.

## 1 INTRODUCTION

Quasars at redshift z > 6.5 are useful probes of early supermassive black hole growth and the epoch of reionisation. Since the discovery of the first such quasar (Mortlock et al. 2011), the current tally of z >6.5 quasars stands at almost 50, with discoveries made using a wide range of near-infrared (NIR) surveys (Venemans et al. 2013, 2015; Matsuoka et al. 2016, 2018a,b, 2019; Decarli et al. 2017; Koptelova et al. 2017; Tang et al. 2017; Reed et al. 2017, 2019; Wang et al. 2017, 2019; Songaila et al. 2018; Pons et al. 2019; Fan et al. 2019; Yang et al. 2019, 2020).

Discovering z > 6.5 quasars remains challenging, not least due to their space density, which declines strongly with increasing redshift. The decline of the number density of quasars brighter than a specific absolute magnitude  $M_{1450}$  is often parametrized as

$$\rho(z, < M_{1450}) = \rho(z_0, < M_{1450}) \ 10^{k(z-z_0)},\tag{1}$$

where  $z_0$  is an arbitrary reference redshift. A comprehensive measurement of the QLF at  $z \sim 6$  was made by Jiang et al. (2016), who used a complete sample of 47 SDSS quasars, 5.7 < z < 6.4, measuring a rapid fall in quasar number density over z = 5-6, with  $k=-0.72\pm0.11$ . For  $M_{1450}=-26$ , they measure  $\rho\sim$  $1 \,\mathrm{Gpc^{-3}}$  (comoving) at z = 6, corresponding to a surface density of approximately one object per 100 deg<sup>2</sup>.

In addition to the low numbers of quasars, selection of z > 6.5quasars is severely hampered by contamination from intervening populations: cool stars and brown dwarfs (henceforth MLTs); and compact early-type galaxies (ETGs) at intermediate redshifts ( $z \sim$ 1-2), misclassified at low signal-to-noise ratio (S/N) as of stellar morphology. These populations are far more abundant than, and have similar NIR colours to, the target quasars (e.g. Hewett et al. 2006). Consequently, colour-selected samples of candidates are dominated by contaminants, especially as quasar searches move to lower S/N to maximize the number of discoveries. Because of this many searches have stopped after identifying the more obvious bright quasars, and have not persisted to the point of following up all candidates to produce a complete sample with a computed selection function, i.e.

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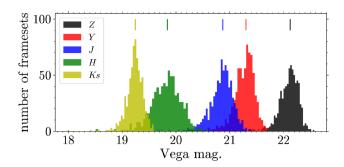
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<sup>&</sup>lt;sup>1</sup>A further known class of contaminant which we do not explicitly treat in this work is extreme FeLoBALs (e.g. Hall et al. 2002), where strong MgII absorption can produce a sharp continuum break. These are considerably less common than MLTs and ETGs, but more common than z > 6.5 quasars.



**Figure 1.** Distribution of  $5\sigma$  frameset depths in each VIKING band. The dashes indicate the median value for each filter.

the measured completeness as a function of absolute magnitude and redshift. The measurement by Wang et al. (2019) of the space density at z>6.5, using the DESI Legacy Survey (Dey et al. 2019) and Pan-STARRS (Chambers et al. 2016), is the only such analysis at these redshifts based on a complete sample. They measured  $k=-0.78\pm0.18$  between z=6 and 6.7, consistent with the rate of decline measured over 5< z<6.

The main purpose of the current paper is to use the VISTA Kilo-Degree Infrared Galaxy (VIKING) survey (Edge et al. 2013) to produce a complete sample of z > 6.5 quasars (high-redshift quasars, HZQs), with a computed selection function, that reaches fainter absolute magnitudes and higher redshifts than the survey of Wang et al. (2019). Improving and extending measurements of the quasar luminosity function (QLF) to fainter luminosities and higher redshifts is an important aim, as such studies will constrain models of the formation and growth of supermassive black holes at early times (e.g. Willott et al. 2010; Jiang et al. 2016), and are also important for designing future surveys for quasars at  $z \sim 7$  and beyond, such as for Euclid (Euclid Collaboration: Barnett et al. 2019). The VIKING survey has already been searched using colour cuts, yielding four HZQs (Venemans et al. 2013; Wang et al. 2017). To improve upon these previous searches, we exploit a new list-driven photometric catalogue, which provides aperture-corrected aperture photometry in all five available bands Z, Y, J, H, K<sub>s</sub> for every VIKING source detected in the J band (Cross et al. 2014). As explained in the next section, this data base has advantages for searches for HZQs.

To search the VIKING data base, we use an updated version of the Bayesian model comparison (BMC) technique developed by Mortlock et al. (2012). This method has been adapted for Subaru data by Matsuoka et al. (2016) and used in their SHELLOs surveys. The same method has been adapted by Pipien et al. (2018) and applied to CFHT data. In a previous paper (Euclid Collaboration: Barnett et al. 2019), we compared two different search methods, namely BMC and minimum- $\chi^2$  SED-fitting (e.g. Reed et al. 2017, applied to DES data). Using simulated data sets we showed that the BMC method is the more useful method as it reaches much deeper than the SED-fitting method, while still being highly efficient. A third search method is the use of simple colour cuts, as applied by Venemans et al. (2013) in their search of the VIKING survey. Although we do not use the candidate lists, for the sake of comparison of the efficiency and depth of the methods we also produce candidate lists using the SED-fitting and colour cuts methods. This extends the comparison of methods undertaken by Euclid Collaboration: Barnett et al. (2019), and has the advantage of using real data.

The paper is structured as follows. In Section 2, we give an overview of the VIKING survey, and the new list-driven data set. In Section 3, we describe the BMC selection method used for the

survey. We also detail the two other methods, SED fitting, and colour cuts, that are used in the comparison of techniques. We present the results from our BMC HZQ search in Section 4. We compute the selection functions for the BMC search and for the other two methods in Section 5. In Section 6, we test that the models of the contaminating populations are reasonable by creating a synthetic survey and comparing, for the three selection methods, the numbers of simulated candidates to the numbers of candidates found in the real data. We summarize in Section 7. All magnitudes and colours quoted are on the Vega system, the default for the VISTA telescope, unless otherwise stated. The AB conversions used in this work for Z, Y, J, H,  $K_{\rm s}$  are 0.524, 0.618, 0.937, 1.384, 1.839, respectively.<sup>2</sup>

Where required we have used cosmological parameters h=0.7,  $\Omega_{\rm M}=0.3,$  and  $\Omega_{\Lambda}=0.7.$ 

#### 2 VIKING SURVEY

VIKING is a medium-deep NIR survey covering  $\sim 1300\,\mathrm{deg}^2$  in five broad-band filters - Z, Y, J, H and  $K_\mathrm{s}$  - with the VISTA telescope. VIKING data sets are named by the release date. The list-driven photometry data base used here is based on the data set 20160406, which was the latest release at the time this project started. This contains a total of 835 framesets, and the majority have coverage in all filters. We use all the framesets that have, as a mimimum, observations in the Z, Y, J filters. This subset contains 782 framesets, and has a footprint covering a total area of 988.7  $\mathrm{deg}^2$ . This calculation accounts for overlaps between framesets, and the fact that detector 16 is not used. With later releases, the area has expanded to 1244.2  $\mathrm{deg}^2$ , but a list-driven data set does not currently exist of the additional area.

The standard VIKING catalogues are formed by merging lists of objects detected in each filter. The subsequent list-driven photometry (Cross et al. 2014) is motivated by the fact that the majority of HZQs will be too faint in the Z band to be detected. This is a consequence of absorption by neutral hydrogen along the line of sight (Lynds 1971), that increases with redshift (Becker et al. 2001), so that by z = 6.5nearly all the flux blueward of Ly $\alpha$  has been absorbed (e.g. Barnett et al. 2017). Consequently, in the standard catalogues, the Z band will only provide a flux limit for HZQs. For such sources, a flux measurement provides much more information than an upper limit (Mortlock et al. 2012). Our new list-driven catalogue is produced by performing aperture photometry in each band at the position of every object that is detected in the VIKING J band, and applying an aperture correction appropriate for a point source. These are therefore total magnitudes. The aperture corrections are measured from bright stars in the same field. Further details of the creation of the list-driven catalogue will be provided in a forthcoming paper (Cross et al., in preparation; see also Ross & Cross 2020).

The photometric depths vary across the survey. The distributions of depths in the different bands are plotted in Fig. 1. Here, depth is quantified by the total magnitude of a point source that is detected at  $5\sigma$  in a 2 arcsec diameter aperture. The median  $5\sigma$  depths are (Z, Y, J, H,  $K_s$ ) = (22.1, 20.3, 20.9, 19.8, 19.2). These depths are some 1.5 mag deeper than the UKIDSS data used by Wang et al. (2019).

Regions close to bright stars are excised from the data set as we found that the VIKING photometry of sources is unreliable in these locations. We observe an excess of candidates near bright stars,

<sup>&</sup>lt;sup>2</sup>These conversions are provided on the Cambridge Astronomical Survey Unit (CASU) website (http://casu.ast.cam.ac.uk/surveys-projects/vista/technical/filter-set), and calculated following Hewett et al. (2006).

which are therefore clearly false positives. The size of the region affected increases with the brightness of the star. We used the 2MASS catalogue (Skrutskie et al. 2006) to quantify this, as the bright stars are saturated in VIKING. We drilled holes around stars brighter than J=11, with a radius R dependent on the 2MASS magnitude according to R=20 arcsec ( $11-J_{\rm 2MASS}$ ). There are  $4.3\times10^4$  bright stars with  $J_{\rm 2MASS}<11$  in the VIKING footprint and we remove 12.2 deg<sup>2</sup> from the survey, leaving an effective area of 976.5 deg<sup>2</sup>.

#### 3 HIGH REDSHIFT QUASAR SELECTION

In this section, we provide the details of our search for HZQs that uses the BMC method. In Section 3.3, we also list the details of the SED-fitting and colour cuts techniques that are used in our comparison of methods. The BMC and SED-fitting methods both require model colours of the contaminating populations. The BMC method additionally requires models of the surface density, as a function of apparent magnitude, of the contaminating populations and of the quasars. The populations modelled are the same as we used in the Euclid study (Euclid Collaboration: Barnett et al. 2019), but adapted specifically for VIKING data, taking into consideration the different filter transmission curves and image quality. The full details of the models of the populations (colours and surface densities of quasars and contaminants) are provided in the Appendix, Section B. Nevertheless, we begin this section with a very brief summary of the models, as this is needed as background for understanding the selection methods.

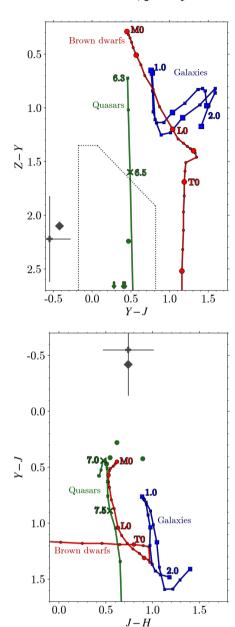
#### 3.1 Overview of population models

The colours of the three populations (quasars, MLTs, and ETGs), are plotted in Fig. 2, showing the Z-Y, Y-J and J-H colours. The colours of the four known VIKING HZQs are also shown. We have used the convention of blue-top-left, red-bottom-right in these plots, as used in Sandage (1965), the paper that initiated multicolour searches for quasars. At high S/N, the three populations are easily mutually distinguishable. At low S/N extreme outliers from the two contaminating populations, which outnumber quasars by orders of magnitude, can have the same observed colours as the target quasars.

The modelling of the colours of the quasar population utilizes nine different spectral types, which are combinations of three different continuum slopes and three emission-line strengths. The nine different types are used in the SED-fitting selection method, and are also used (with appropriate weights) in computing the selection functions for all the methods. However, the BMC selection method itself uses only a single quasar type (the typical SED). The significance of this choice is discussed when describing the BMC method (Section3.2.2). The modelled surface density of quasars uses the measured luminosity function at z=6, with a declining space density towards higher redshift.

The colours of MLT dwarfs, covering the spectral range M0 to T8, were determined from a combination of measured colours of sources classified by spectroscopy, as well as calculation of synthetic colours from spectra. We assume that the space density falls off exponentially with the height from the Galactic mid-plane, and the adopted space density of each spectral sub-type comes from recent wide-field surveys for these populations.

ETGs at intermediate redshift 1 < z < 2 have very red colours. The galaxy size is a strong function of luminosity so that fainter ETGs detected in VIKING are very compact and may be classified as stellar. Only very extreme outliers of this population can mimic the SEDs of HZQs, but the surface density of ETGs is more than



**Figure 2.** Colour–colour diagrams of relevant populations. Green tracks (crosses): HZQ model colours as a function of redshift, spacing  $\Delta z = 0.1$ . Red tracks (circles): model MLT colours for each spectral type. Blue tracks (squares): ETGs ( $z_f = 3$  and 10), spacing  $\Delta z = 0.1$ . Green circles are the known VIKING HZQs. The grey plus-sign indicates the emission-line galaxy VIK J1459–0321 (Section 4.1). The grey diamond indicates the average colours of the high- $\chi^2$  rejected candidates (Section 4.1). Upper panel: *ZYJ* colours. Selection criteria of the colour-cuts method are shown as black dotted lines. Three of the known HZQs have Z - Y > 3, and are indicated using arrows. Lower panel: *YJH* colours.

four orders of magnitudes higher than that of HZQs. Combined with the difficulty of modelling the star/galaxy boundary, this means that this is the most difficult population to model accurately.

A relevant question is whether or not to allow for intrinsic spread in the colours of the different populations. For the MLTs, Skrzypek et al. (2015) showed that intrinsic spread was accurately accounted for by applying a dispersion of 0.05 mag. in each band, added in quadrature to the photometric uncertainties. Therefore at very high S/N, brighter than any expected quasars, the colour tracks of the

MLTs are narrower than they should be. However, should there be any unusually bright quasars in the survey this is not a problem, since of course they will be very well separated from the contaminating populations. In the expected magnitude range of quasars in the survey J > 18.5, the photometric uncertainties dominate over the intrinsic spread. This means that the model for the MLTs adequately represents the population (adding 0.05 mag. in quadrature does not make a significant difference). A similar argument applies to the modelling of ETGs and quasars. For these there is some intrinsic spread in colour, of a discrete rather than a continuous nature. For the ETGs, we split the population by adopting two different formation redshifts z = 3 and 10. For the quasars, we have the nine different spectral types. Again these individual colour tracks do not overlap at very bright magnitudes, but at J > 18.5 all the sub-populations of, respectively, the quasars, and the ETGs, overlap because of the size of the photometric errors at these magnitudes. To confirm that additional intrinsic spread is not needed, we reran the selection functions for a case where additional intrinsic spread of 0.05 mag in each band was included, and found negligible difference.

#### 3.2 Candidate selection using BMC

#### 3.2.1 Initial cuts

To target HZQs, before applying the BMC algorithm we implement the following cuts:

- (i) S/N  $_J \ge 4$ . Given that our list-driven catalogue requires a J-band detection, very few sources are removed by this step. We do not have an equivalent requirement in Y, which means our sensitivity in redshift extends to  $z \sim 9.3$ . However, in a survey of the depth and area of VIKING the predicted yield is extremely small at such high redshift.
  - (ii) The particular field was observed in all three bands Z, Y, J.
- (iii) S/N  $\geq$  4 in one additional band Y, H or  $K_s$ . In practice, this ensures that a J-band detection corresponds to a real source.
  - (iv) S/N  $_Z$  < 4, or  $Z Y \ge 1.5$ .
- (v) -4 < MergedClassStat < 2. The parameter MergedClassStat (MCS) is a morphology statistic in VIKING, which we use to exclude identifiably extended sources.
- (vi) Not on detector 16. Flat-fielding is not accurate for this CCD due to a time-varying quantum efficiency and many detected sources are spurious. A flag is automatically applied to VIKING sources from this detector (Cross et al. 2012). The exclusion of detector 16 is accounted for in the quoted survey area and corresponds to a reduction in area of 6 per cent.

The cut in Z - Y colour was selected carefully to ensure that the selection function cuts off just below z = 6.5. The redshift cut is sensitive to the emission-line strength, since this affects the Z - Y colour. This sensitivity to line strength is accounted for in computing the selection function, by the weights adopted for the different quasar SEDs.

At this point the number of sources under consideration is  $3.6 \times 10^5$ . If the colour cut in item (iv) is not applied, the number of sources is  $8 \times 10^6$ .

These selection criteria are very broad, with the goal of maximizing the discovery space of HZQs. The only explicit colour cut is in item 4. It is common to apply a higher S/N threshold than we have in item 1. The very low S/N threshold applied is possible because the BMC method utilizes the photometric uncertainties in an optimal way. One z > 6.4 quasar in VIKING, listed with z = 6.51 by Chen et al. (2017), but revised to z = 6.44 by Decarli et al. (2018), lies

above, but close to the Z-Y cut. This indicates that the colour cut lies close to z=6.5. This source is also excluded by the colour cuts applied by Venemans et al. (2013), described below. Our cut on Z-Y is slightly redder than that used by Venemans et al. (2013), which we found helped reduce the number of false positives in our search with BMC.

As detailed below, for sources identified by the BMC method as candidate quasars, we apply an additional cut  $\chi^2_{min} < 11$ . The quantity  $\chi^2_{min}$  is the goodness of fit of the quasar model that provides the best fit to the photometry.

#### 3.2.2 BMC method

We use an extension of the BMC technique proposed by Mortlock et al. (2012). The extended method is additionally described in detail by Euclid Collaboration: Barnett et al. (2019), so we only recap the main points here.

The method works by determining a 'weight' for each population under consideration, with a population posterior probability given by the ratio of those weights. In our search for quasars, denoted q, where we have assumed two contaminating populations, MLTs, s, and ETGs, g, we define the probability that a source is a quasar,  $P_q$ , given photometric data d as

$$P_{q} \equiv p(q \mid d) = \frac{W_{q}(d)}{W_{q}(d) + W_{s}(d) + W_{g}(d)}.$$
 (2)

The individual weights for a population are calculated by combining all available photometric data for a source, with the surface density of the population, which serves as the prior. For a given source, a particular population weight measures the relative probability that the source would have the measured photometry in all bands, characterized by the model colours for that population, weighted by surface density as a function of apparent magnitude. Mortlock et al. (2012) applied the method to the case of two populations: quasars and M stars; here, we have extended the method to three populations. Additionally, the MLT population is now divided into a set of sub-populations, namely the individual spectral types from M0 to T8. This approach to the cool dwarf population is similar to that of Pipien et al. (2018), who developed models for each spectral type L0-T9 in a search for HZQs in the Canada-France High-z Quasar Survey in the NIR.

As noted above, for the search we only used one quasar type the 'typical' quasar defined by Euclid Collaboration: Barnett et al. (2019), with standard continuum slope and average line strength. But quasars have a range of spectral properties, so the search will be optimal if this range is represented in the search, i.e. like for the cool stars, we should divide the quasars into sub-populations. The optimal approach would have been to divide the quasars into the nine spectral types, with weights that characterise the relative numbers (see table 5 in Euclid Collaboration: Barnett et al. 2019). The use of only one quasar type was an unfortunate consequence of meeting the deadline for applying for 8-m spectroscopy of candidates, and then the candidate list was locked in. While this means that the search was not quite optimal, the consequences of this are not very significant. The selection function for the search we have undertaken has been correctly computed, i.e. we assume that the actual quasar population has a range of spectral types. The only consequence of the choice made is that the survey goes slightly less deep than the optimal search. Based on calculations presented in Euclid Collaboration: Barnett et al. (2019), we estimate that the optimal search would increase the yield by 20 per cent, i.e. possibly one more quasar would be found.

Explicitly, individual weights for each type,  $W_t(d)$ , are given by

$$W_{t}(\boldsymbol{d}) = \int \rho_{t}(\boldsymbol{\theta}_{t}) \ p(\boldsymbol{d} \mid \boldsymbol{\theta}_{t}, t) \ d\boldsymbol{\theta}_{t}, \tag{3}$$

where  $\theta_t$  is the set of parameters describing each population. The two terms in the integral in equation (3) are, respectively, the surface density function, and a Gaussian likelihood function based on model colours, which is written in terms of (linear) fluxes (as opposed to magnitudes).

The candidates are ranked on  $P_{\rm q}$ , and the candidate list is defined as all objects with  $P_{\rm q}$  larger than some threshold value. The chosen threshold value of  $P_{\rm q}$  effects a balance between contamination and completeness. A value  $P_{\rm q} > 0.1$  worked well for the UKIDSS LAS high-redshift quasar survey (Mortlock et al. 2012). However, we found the number of candidates rises steeply for VIKING as the threshold is lowered from  $P_{\rm q} = 0.15$  to 0.1, with only a small associated change in the simulated selection function, and hence the predicted quasar yield. The implication is that the lower  $P_{\rm q}$  threshold simply allows more contaminants into the sample, to no significant benefit. Therefore, in this work, we select candidates with  $P_{\rm q} > 0.15$ .

In the Appendix, Section A, we detail a slight modification to the selection procedure which we applied to sources which have both a primary and secondary entry in VIKING as a result of the VISTA observation strategy (i.e. the source is duplicated in the catalogue).

#### 3.3 Candidate selection using other methods

#### 3.3.1 SED fitting

The second method that we consider is minimum- $\chi^2$  SED fitting. Reed et al. (2017) applied such a method to a combination of DES, VHS, and WISE data, discovering eight bright ( $z_{AB}$  < 21.0) z > 6 quasars, including one source with z = 6.50. This method is applied to the same sample that the BMC method is applied to, i.e. after the initial cuts enumerated in Section 3.2.2. For the sake of making an explicit comparison, we have attempted to reproduce the methods of Reed et al. (2017) as closely as is possible, given the different data sets. It is likely that some improvements (in terms of contamination and completeness) could be made by making adjustments to the cuts in the parameter space they use. Nevertheless, we found that the chosen cuts were sensible when plotting the data in that parameter space. The method was also compared to BMC in Euclid Collaboration: Barnett et al. (2019), and in that study, we found that there was little scope for significantly improving the depth achieved by the method. For these reasons, although we have not attempted to optimize the SED-fitting method for the VIKING data set, we feel the comparison as presented provides a useful representation of the relative strengths and weaknesses of the method compared to BMC.

The method works by fitting the full range of contaminant model SEDs, and the nine quasar spectral types, to the measured fluxes of a source, minimizing the reduced  $\chi^2$  value,  $\chi^2_{red}$  i.e. the value of  $\chi^2$  divided by the number of degrees of freedom.<sup>3</sup> We calculate the  $\chi^2_{red}$  value for a given model SED m as follows:

$$\chi_{\text{red},m}^2 = \frac{1}{N_b - 2} \sum_{b}^{N_b} \left( \frac{\hat{f}_b - s_{\text{best}} f_{m,b}}{\hat{\sigma}_b} \right)^2,$$
(4)

 $^3When$  we use reduced  $\chi^2$  in this paper there is always an explicit subscript i.e.  $\chi^2_{red}$ 

where  $\hat{f}_b$  and  $\hat{\sigma}_b$  are the measured flux and its uncertainty in band b,  $f_{m,b}$  is the (unnormalized) model SED flux in band b, and  $s_{\text{best}}$  is the normalization that minimizes  $\chi^2$ . We have  $N_b-2$  degrees of freedom as there are two parameters under consideration: the normalization of a single model, and the particular model being fitted, selected from a range of models (e.g. Skrzypek et al. 2015). That is to say, for the quasars and ETGs the second parameter is redshift,  $\Delta z = 0.05$ , while for the MLT dwarfs, which form a continuous sequence, the second parameter is spectral type.

We use the model colours detailed in the Appendix, Section B, to produce quasar and contaminant SEDs, and fit them to the fluxes of each source, following equation (4). We keep the single best-fitting quasar (q) model and contaminant (c) model, with respective  $\chi^2_{\rm red}$  values  $\chi^2_{\rm red,q(best)}$  and  $\chi^2_{\rm red,c(best)}$ . Following Reed et al. (2017), we apply two cuts to the  $\chi^2_{\rm red}$  values to retain a source (see fig. 15 of that work). We firstly require  $\chi^2_{\rm red,c(best)} > 10$ , i.e. the data are a bad fit to all contaminant models. We additionally require the ratio  $\chi^2_{\rm red,c(best)}/\chi^2_{\rm red,q(best)} > 3$ , i.e. the data are fit substantially better by a quasar SED than any contaminant model.

#### 3.3.2 Colour cuts

The final method we use in this paper is the 'conservative' set of colour/magnitude cuts used to select quasars from 332 deg<sup>2</sup> of VIKING by Venemans et al. (2013). The selection criteria, transformed from the AB photometric system used by them to the Vega system used here, are the following:

- (i) Z Y > 1.35, or undetected in Z (VIKING).
- (ii)  $S/N_Z < 3$  or Z Y > 1.3 + 0.75(Y J).
- (iii) -0.2 < Y J < 0.8.
- (iv)  $0.7 < Y K_s < 2.5$ , or unmeasured in  $K_s$ .
- (v)  $\sigma_Y(VIKING) < 0.15$ . This requirement limits the search to redshifts z < 7.5, in contrast to the other two search methods used here
  - (vi) Not on detector 16.

A source must satisfy all criteria to be accepted. In their search, Venemans et al. (2013) also undertook their own aperture photometry on the images, and additionally applied the above cuts to the repeat photometry. Since we do not have access to their software, we use the list-driven photometry to emulate this process, i.e. we apply the cuts first to the standard VIKING photometry, then additionally to the list-driven photometry. In the first stage, we also apply the morphological cut pGalaxy < 0.95 used by Venemans et al. (2013).

#### 4 RESULTS: z > 6.5 QUASAR CANDIDATES

We present the BMC candidate list, and the results of follow-up observations, in Section 4.1. We did not discover any new quasars; however, the four known quasars in the VIKING area are easily recovered. In Section 4.2, we outline the candidate lists produced using the other two methods. As noted above these are only for the purposes of comparing the efficiency and depth of the three different selection methods.

#### 4.1 Results from BMC

Applying our first cuts to the full VIKING survey (Section 3.2), we have an initial sample of  $3.6 \times 10^5$  sources, to which we apply the BMC method. This produced an initial list of 349 candidates satisfying  $P_q > 0.15$ . All candidates were then checked on the

**Table 1.** VIKING HZQ candidates from the BMC method. Follow-up imaging (g or r) and spectroscopic (FORS2/FIRE) observations are listed in the final column. Here, 'Legacy' means the DESI Legacy Survey. The asterisked probabilities were calculated on the basis of combining primary and secondary VIKING photometry for those sources (see Appendix Section A). The quantity  $\chi_{\min}^2$  has three degrees of freedom.

	α	δ	$P_{\mathrm{q}}$	$\chi^2_{\rm min}$	Zbest	notes
Known HZQs	01:09:53.12	-30:47:26.3	0.97	0.6	7.00	z = 6.8, Venemans et al. (2013)
	03:05:16.91	-31:50:55.9	1.00*	2.1	6.55	z = 6.6, Venemans et al. (2013)
	10:48:19.08	-01:09:40.2	1.00	4.5	6.60	z = 6.6, Wang et al. (2017)
	23:48:33.33	-30:54:10.2	1.00*	2.3	7.00	z = 6.9, Venemans et al. (2013)
Candidates	00:03:51.28	-31:24:00.2	0.21	1.9	6.65	FORS2
	00:27:57.62	-30:02:19.7	0.20	1.9	6.45	Legacy r
	00:45:39.65	-34:28:02.3	0.17	0.1	7.45	FORS2
	00:58:42.88	-28:52:06.1	0.42	3.3	6.50	Legacy r
	01:00:23.22	-28:55:36.5	0.19	1.5	6.55	Legacy r
	01:21:51.96	-28:00:18.4	0.99	5.8	6.40	Legacy r
	01:40:12.32	-27:54:04.7	0.17	1.3	6.50	Legacy r
	01:46:30.52	-30:11:51.0	0.63	0.4	7.40	FORS2
	02:19:41.29	-27:25:33.8	0.38	5.9	7.00	Legacy r, FORS2
	03:13:16.83	-30:59:20.9	0.77*	6.9	6.45	Legacy r
	08:59:02.86	-01:36:02.5	0.25	2.4	6.45	Legacy r
	12:05:47.13	+01:52:54.3	0.37*	2.1	6.50	Legacy r
	14:08:11.22	-02:44:39.3	0.29	1.6	6.60	FIRE
	22:02:09.61	-28:19:51.0	0.27	1.1	7.50	FORS2
	22:25:11.17	-27:23:29.6	0.16	3.6	6.45	Pan-STARRS r
	22:39:54.55	-27:12:18.1	0.64	1.6	6.45	ATLAS $r$
	23:24:17.94	-30:12:12.3	0.52	5.4	6.45	KiDS r
Rejects	01:13:32.06	-30:08:45.6	0.91	18.4	6.50	Legacy r
$11 < \chi^2_{\min} < 40$	01:27:59.05	-33:02:57.1	0.31	25.1	6.45	Legacy r
XIIIII	02:16:04.31	-32:58:58.7	0.39	31.4	7.00	FORS2; Fig. 4
	02:16:23.37	-32:07:40.4	0.99	32.3	6.55	FORS2
	11:48:27.75	+02:53:51.8	0.53	19.8	6.45	Legacy r
	12:25:39.61	+ 02:31:27.8	0.47	14.4	6.45	Legacy r
	12:45:09.26	-01:40:23.3	0.62	27.4	6.50	ATLAS $g$
	12:51:50.09	+ 02:50:16.2	0.98	35.0	6.40	Legacy r
	14:45:21.04	+02:00:58.4	0.99	36.3	7.00	Legacy r
	14:59:14.63	-03:21:29.1	0.20	22.0	6.50	Legacy r, FORS2; ELG, Fig. 5
	23:04:16.06	-34:52:30.8	0.20	24.2	6.45	ATLAS g

VIKING images. The majority were eliminated as obvious spurious images arising from, e.g. detector flaws, diffraction spikes, and satellite trails, and only 42 real sources remained. At this stage, we were left with a number of candidates that have SEDs very different to the SEDs of quasars. For each candidate, we determined the best-fitting quasar SED, by min- $\chi^2$ , using all nine quasar types, with redshifts over the range 6 < z < 10. For sources with measurements in all five bands  $ZYJHK_s$ , this fit has three degrees of freedom, so we rejected all candidates with  $\chi^2_{min} > 11$ . For three degrees of freedom, this cut corresponds to a 1 per cent probability, i.e., in principle, we include 99 per cent of quasars with this cut. We removed 21 sources in this way, leaving 21 candidates. The nature of the sources eliminated by this cut is discussed later in this section.<sup>4</sup>

At this stage, we checked the photometry of the remaining sources in the ALLWISE data base [this combines WISE (Wright et al. 2010) with NEOWISE (Mainzer et al. 2011)], since late T dwarfs would appear bright in the W2 band. Many of the candidates are undetected in ALLWISE, and no sources were eliminated in this way. ALLWISE is of limited utility for searches for HZQs at the depth of VIKING. The final list of 21 candidates is provided in Table 1. We also list

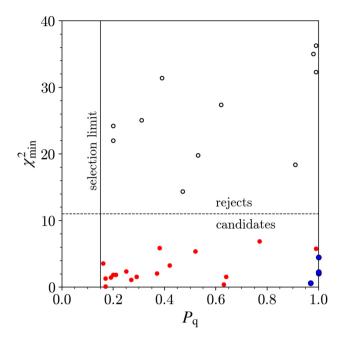
the 11 rejected sources with  $11 < \chi^2_{\rm min} < 40$  (10 rejected sources have  $\chi^2_{\rm min} > 40$  and are not considered further). The table lists the coordinates (IRCS, truncated, according to IAU convention), the value of  $P_{\rm q}$ , the value of  $\chi^2_{\rm min}$ , and  $z_{\rm best}$ , the redshift of the best-fitting quasar SED. Ranking the candidates by  $P_{\rm q}$ , the four known HZQs are ranked numbers 1, 2, 3, 5.

The 21 candidates as well as the 11 rejected sources with  $11 < \chi^2_{\rm min} < 40$  are plotted in Fig. 3. The number of candidates increases extremely rapidly below the selection cut  $P_{\rm q} = 0.15$  (see Mortlock et al. 2012, fig. 11, for an illuminating plot on this point). It is noticeable that the distribution of  $\chi^2_{\rm min}$  for the blue and red points is sensible for three degrees of freedom, 5 but that there is an excess of sources with bad fits, with  $\chi^2_{\rm min} > 11$ .

Since we want a complete sample we must confirm whether or not any of the remaining 17 candidates is a quasar. At redshifts, z > 6.5, flux shortward of the quasar Ly $\alpha$  emission line is almost completely absorbed, with at most some residual transmission redward of Ly $\beta$  which lies at  $\lambda > 770$  nm (see, e.g. Barnett et al. 2017, for recent measurements). Therefore, if a candidate is a HZQ, there will be a negligible flux in the g and r photometric bands, which lie blueward of  $\lambda 700$  nm. (We therefore ignore the possibility of gravitational

<sup>&</sup>lt;sup>4</sup>The use of  $\chi^2$  at this stage is to measure the goodness of fit. This is distinct from the use of  $\chi^2$  in the SED-fitting method, where it is employed for model comparison.

<sup>&</sup>lt;sup>5</sup>For the 21 blue and red points,  $\chi^2_{min}$  has mean 2.7 and standard deviation 1.9. The expected values, for a larger sample, are 3 and 2.4, respectively.



**Figure 3.** Plot of  $\chi^2_{\min}$  against  $P_q$  for the 21 candidates, and the 11 rejected sources with  $11 < \chi^2_{\min} < 40$ . The four larger blue circles (two overlap) are the four quasars and the red circles are the 17 candidates subsequently shown to not be quasars.

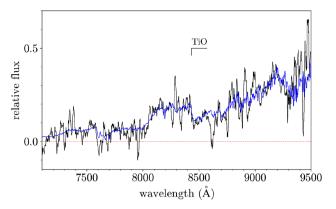
lensing by an intervening galaxy that magnifies the quasar image(s) and directly contributes optical flux, see Fan et al. 2019.) We matched our candidates to imaging data from the DESI Legacy Survey, the VST ATLAS survey (Shanks et al. 2015), the Kilo-Degree Survey (KiDS, de Jong et al. 2017), and Pan-STARRS, and eliminated any candidates clearly detected in either of these bands.<sup>6</sup> The images (survey and photometric band) used to eliminate any candidate are listed in the final column of Table 1.

We obtained spectra to confirm the nature of the remaining five objects. One of these, VIK J140811.2–024439.4, was observed using Magellan FIRE in June 2017. The other four candidates were observed with the ESO FORS2 instrument between 2018 November 11 and 2019 March 18, as well as one additional source VIK J021941.3–272533.8 that was only later detected in a r image. None of the six spectra displays the continuum break or Ly $\alpha$  emission-line characteristic of HZQs. Instead, all display continua strongly rising towards longer wavelengths, characteristic of L and T dwarfs. They are similar to the spectrum of the source VIK J021604.3–325858.7, plotted in Fig. 4, that is discussed in the next section. Accordingly, these sources were also eliminated. In this way all 17 candidates were eliminated, meaning no new quasars were discovered. By this means, the four previously known quasars now form a complete sample.

## 4.1.1 The nature of $\chi^2_{min} > 11$ sources

A number of candidates have acceptable values of  $P_q > 0.15$  but the best-fitting quasar model is a very bad fit, with  $\chi^2_{min} > 11$ . This is not a shortcoming of the BMC method *per se*. From the range of

<sup>6</sup>In principle, this additional optical photometry could have been incorporated into the BMC calculation. However, for our search insufficient optical data were available at the time the candidate list was finalized. In any case, matching once we have a shortlist is considerably less work than matching complete catalogues before starting the search.

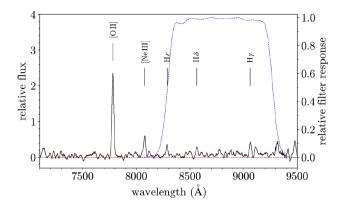


**Figure 4.** FORS2 spectrum of VIK J0216–3258, which we identify as a late M or early L dwarf. The spectrum has been flux calibrated relatively, and smoothed. Overplotted in blue is the scaled spectrum of the L0 standard 2MASS J0345 + 2540 from Kirkpatrick et al. (1999).

models (i.e, quasars and contaminants), the BMC method optimally selects the model that best explains the data. A bad fit of the best model suggests that the object is not a member of any of the three populations considered, and may indicate the presence of another contaminating population. The BMC method itself does not measure the goodness of fit, which is why we assess the goodness of fit using  $\chi^2$ .

In Table 1, we list the objects with  $11 < \chi^2_{min} < 40$ . To investigate the nature of this population, we again matched the sources to the deep optical surveys previously cited. Most are detected in the r band, and these are considered further below. Two sources were not detected in g or r and we obtained spectra of these. Their spectra are similar to the spectra of the red objects discussed in the preceding section. The spectrum of the source J021604.3–325858.7, J = 20.1, is plotted in Fig. 4. The wavelength of the sharp dip near the centre of the spectrum matches to the 8432 Å band head of TiO. The overall shape of the spectrum, the TiO absorption, and the dip near 9300 Å identified as H<sub>2</sub>O, are characteristic of a source near the M/L boundary, and as shown in the figure the spectrum is satisfactorily fit by the L0 standard. The reason for the large value of  $\chi^2_{min}$  is not clear, but conceivably this source and the other one undetected in optical imaging are subdwarfs, but this cannot be confirmed without much longer integrations.

We also targeted a source detected in r with one of the smallest values of  $\chi^2_{min}$  in this group. The spectrum of this source, VIK J145914.6-032129.11 (VIK J1459-0321), is plotted in Fig. 5. It is an emission-line galaxy (ELG) with z = 1.087. The colours of this source are plotted in Fig. 2, where it can be seen that the object is very blue in Y - J. Given the redshift of the source, the emission lines H $\beta$  and [O III]  $\lambda\lambda 4959,5007$  lie in the Y band, but off the red end of the spectrum plotted in Fig. 5. From the spectrum, it is clear that the Balmer lines are weak, so the very blue Y - J colour must be caused by very strong [O III] λλ4959,5007 emission. The strength of the high-ionization [Ne III] line compared to the Balmer lines suggests this object is likely to be an AGN. Also plotted in Fig. 2 are the average colours, and scatter, of the nine sources in the high- $\chi^2_{min}$  reject category that are visible in g or r. These are consistent with the colours of VIK J1459–0321, suggesting that they may all be ELGs at similar redshifts. While these objects are easily distinguished from quasars, by their high  $\chi^2_{min}$  values, similar sources with somewhat weaker emission lines might have less blue Y - Jcolours, and so smaller values of  $\chi^2_{min}$ . It is possible that some of the



**Figure 5.** FORS2 spectrum of VIK J1459–0321, a z = 1.087 ELG. The spectrum has been flux calibrated relatively, and smoothed. The (relative) transmission profile of the *Z* filter is plotted as the blue dashed line, showing that the strong [O II] line lies outside the filter.

actual candidates, i.e. objects with  $\chi^2_{\min} < 11$ , detected on r, are also ELGs.

This population of ELGs, with very strong [O III] λλ4959,5007 emission, is discussed in the literature (e.g. Atek et al. 2011; Hayashi et al. 2018), and has been noted as a contaminant in the very deep Subaru surveys for HZQs by Matsuoka et al. (2019). It appears we are seeing the bright tip of this population in VIKING. As described in the Euclid paper, we made an explicit search of the deep COSMOS data (Laigle et al. 2016) for an additional contaminating population, failing to find any such sources over the 1.5 deg<sup>2</sup> of the COSMOS field, but the area covered was evidently too small to capture this population. The Euclid wide survey will cover an area 10 000 times larger. Therefore, further analysis and better characterization of this ELG population are needed, to feed into HZQ selection with Euclid. It may be that the much better imaging quality of *Euclid* compared to VIKING will allow the ELG population to be eliminated from quasar searches as extended sources, or that the complementary ground-based optical imaging data will be deep enough to detect these sources, in r or i, and so eliminate them in that way.

A further known contaminant in z > 6.5 quasar surveys are FeLoBALs (Hall et al. 2002), although none of the objects for which we obtained a spectrum in this work is an example. FeLoBALs are best eliminated by deep photometry in the optical bands, and it is conceivable that some of our objects detected in r fall into this category.

## 4.2 Candidate lists from other methods

We applied the SED-fitting criteria to the same initial sample of  $3.6 \times 10^5$  sources as in Section 4.1. After checking the VIKING images of all candidates, we were left with only two candidates, of which one is the z=6.9 quasar listed in Table 1, and the other is one of the BMC candidates, which we excluded on the basis of a DESI Legacy Survey detection. The other three known quasars are excluded as the photometry is well-enough fit by a contaminant model. This implies that the SED-fitting method is very efficient, but only picks out the most obvious sources. In our analysis for *Euclid* (Euclid Collaboration: Barnett et al. 2019), we investigated whether tuning the selection parameters for SED fitting could improve the completeness. However, in that work, we found relaxing the cuts slightly resulted in a threefold increase in contamination, for only a 10 per cent increase in the predicted number of quasars found. We concluded that it was difficult to improve the depth significantly

without the number of candidates rapidly rising. In their more recent search, Reed et al. (2019) used different SED-fitting criteria compared to Reed et al. (2017), extending the region of parameter space searched. However, because they have not obtained spectra of all candidates a quantitative comparison of the two selection methods is not possible. In the newer search, they found three new HZQs. Two of these satisfy the selection criteria of Reed et al. (2017), while the third lies outside but very close to the cut  $\chi^2_{\rm red,c(best)}/\chi^2_{\rm red,c(best)} > 3$ .

Using the colour cuts, and after checking all candidates in the VIKING images, we are left with a total of 199 good HZQ candidates. We recover the four known quasars as well as five BMC candidates listed in Table 1 (all of which have detections in the r band). We find a further 124 candidates which are not selected by the BMC algorithm because  $P_{\rm q} < 0.15$ . Finally, there are 66 additional candidates which were not checked using BMC, as they lie bluer than the Z-Y cut applied to produce the initial sample used in the BMC method. The surface density of the 199 candidates, from 977 deg², is  $0.20\,{\rm deg}^{-2}$ . Venemans et al. (2013), selected 43 candidates from  $332\,{\rm deg}^2$ , or  $0.13\,{\rm deg}^{-2}$ , so our methods are reproducing theirs reasonably closely.

Considering the colour range in common, the BMC method produces 17 false positives. Colour cuts produce 129 candidates in addition to the known quasars. Considering the high probabilities of the confirmed quasars it can be assumed that nearly all the 129 candidates are false positives, so on this basis we find colour cuts produce eight times as many false positives as the BMC method.

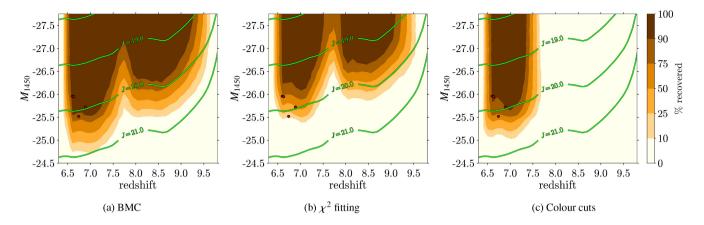
#### **5 SELECTION FUNCTIONS**

In this section, we compute the quasar selection functions for the three selection methods, i.e. we compute the probability that a quasar of given absolute magnitude and redshift and spectral type, would be selected by each method. We start with a grid in luminosity/redshift space, over which we simulate large numbers of quasars. Although the selection algorithm employs only a single quasar spectral type, one with typical properties, quasars, in reality, have a range of emission-line strengths, and continuum slopes. We employ nine different spectral types, corresponding to all combinations of three different line strengths and three continuum slopes. Further details of the models are provided in Euclid Collaboration: Barnett et al. (2019). We measure the detection probability over the full range of spectral types. The final selection function weights the detection probabilities by the assumed fractions of the different spectral types (table 5 in Euclid Collaboration: Barnett et al. 2019).

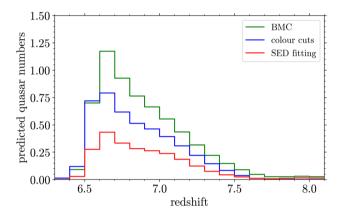
We produce realistic list-driven fluxes for these sources using our model colours (Appendix, Section B1), and add Gaussian noise based on the distribution of frameset depths in each band (Fig. 1). We additionally simulate the process of detection in the J band, which determines whether a real source will appear in the list-driven catalogue. The way the detection process is modelled is described in the Appendix, Section C. This is relevant for the BMC method, which reaches very deep.

We determine the final quasar selection functions by recording the fraction of simulated HZQs that pass the selection criteria for each method, considering every step in the selection process, i.e. following the procedures detailed in Section 3. The three selection functions are plotted in Fig. 6.

There is a sharp cut-off in sensitivity to quasars below z=6.5 for all three methods. Colour cuts are insensitive to quasars at  $z\gtrsim 7.6$ , beyond which the Ly $\alpha$  break is sufficiently redshifted that HZQs become too faint in the Y band to be selected. By contrast, there is no Y-band S/N requirement for the other two methods (a source with a 4  $\sigma$  flux measurement in any of YHKs will be accepted), and



**Figure 6.** Selection functions for the three different selection methods. Circles indicate the four published VIKING HZQs (Venemans et al. 2013; Wang et al. 2017). Contours of constant apparent magnitude, computed using *k*-corrections determined for an average quasar SED, are indicated in green.



**Figure 7.** Predicted HZQ yield as a function of redshift for each selection method, produced by multiplying the selection functions in Fig. 6 by the Jiang et al. (2016) QLF, evolved beyond z = 6 using k = -0.78.

quasars could in principle be recovered up to  $z \sim 9.3$ . For the BMC and SED-fitting methods, there is a noticeable decline in selection efficiency over the redshift interval 7.5 < z < 8.0. Over this redshift range, HZQs fainter than  $J \sim 19$  begin to be misclassified as MLTs, as a result of the very similar colours of the two populations.

Over the redshift range in common to the three methods, the BMC method reaches deepest, followed by colour cuts, and then SED fitting. To quantify the relative performance of the three HZQ selection methods, we integrate the QLF over the quasar selection functions in Fig. 6, to determine a 'predicted yield' of HZQs using each method. We use the Jiang et al. (2016) QLF measured at z=6, and evolve it in redshift using the value k=-0.78 measured by Wang et al. (2019), assuming this value applies at all redshifts z>6. We plot the predicted numbers in redshift bins in Fig. 7. The total counts are 6.4, 2.4, 4.4 for the BMC-, SED-fitting, and colour cuts methods. Although the BMC and SED-fitting methods have sensitivity to z>8 quasars, in practice, this is not of great interest as the predicted numbers are negligible for the assumed luminosity function evolution. The tally of four detected quasars using BMC is effectively a  $-1\sigma$  deviation from the predicted counts.<sup>7</sup> The

implication of the results is that the rate of decline of the luminosity function with redshift is slightly steeper than found by Wang et al. (2019). In a future paper we will combine our data set with that of Wang et al. (2019), to carry out a full analysis of the redshift evolution at z > 7.

To quantify the relative depths of the three selection methods, we consider the redshift range 6.6 < z < 7.0. We sum the predicted counts over this redshift range for each method. We then similarly integrate the evolving luminosity function, assuming 100 per cent completeness, to find the depth that matches the counts for each method. The effective depths of the BMC-, SED-fitting, and colour cuts methods are respectively  $M_{1450} = -25.0, -25.7, -25.3$ . This implies that the BMC method reaches 0.3 mag. deeper than colour cuts, and 0.7 mag. deeper than SED fitting.

#### 6 CONTAMINANT SIMULATIONS

As a test of the modelling process, and therefore of the reliability of the selection functions, we created a synthetic survey using the population modelling and selection apparatus already described. We ran our selection methods on the synthetic survey and compared the numbers of synthetic candidates to the numbers of actual candidates. Our models for the contaminants specify the surface density as a function of apparent magnitude and colour. The synthetic survey accounts for the varying depths across the VIKING survey by simulating sources for every frameset. We simulate sources down to one magnitude fainter than the 5  $\sigma$  limit of each frameset in order to correctly model the possibility that faint sources are scattered by flux errors to brighter than the detection limit. For both contaminating populations, we use the model colours to determine true fluxes in each band, and then add Gaussian noise based on the frameset depth. We discard sources that are not detected in the J band, and in the case of ETGs, we reject sources on the basis of the morphology cut (Appendix Section B3). The resulting synthetic survey contains  $\sim 1.5 \times 10^6$  MLTs, and  $\sim 4 \times 10^5$  ETGs (the large majority having been removed by the morphology cut). We gauge the predicted contamination by applying our selection methods to this sample.

For the BMC method, we predict contamination by 29 sources, as compared to the 17 contaminants found (effectively a  $-2\sigma$  fluctuation), and for SED fitting we predict one contaminant which

(Marshall et al. 1983). The log likelihood of the VIKING sample is consistent with the resulting distribution.

 $<sup>^7</sup>$ To further check the consistency of the BMC selection function and VIKING HZQ sample, we draw  $1 \times 10^5$  fake quasar samples from the product of the selection function and the QLF. We calculate the log likelihood of each

matches the one found. These numbers are in very close agreement, providing confidence in the models used and therefore in the accuracy of the computed selection functions. However, we note that our idealized simulations do not incorporate the possible ELG population discussed in Section 4.1, and that at present it is unclear what fraction of the contaminants are ELGs.

We cannot fully simulate the colour cuts method using simulations. Recall (Section 3.3.2) that Venemans et al. (2013) required an object to meet their selection criteria both in the catalogue data and in their own repeat photometry. While we could emulate this in the candidate selection, we cannot do this in the simulation. Because of this, the simulation is expected to overestimate the number of candidates. In the actual data we selected 199 candidates using colour cuts. Applying the colour-cut criteria to the simulations, we select 472 HZQ candidates. There is a discrepancy of a factor of 2.4. Although we predicted an excess, this difference is substantial. Nevertheless, the context of this estimate is that over the parameter space searched, ETGs outnumber HZQs by a factor larger than 10<sup>4</sup>. So here we are attempting to model only the extreme tail of the ETG distribution. Coupled with the complication of accurately modelling the MCS cut we consider this a satisfactory prediction of the number of contaminants. We conclude that these results again indicate the models are providing a good representation of the contaminant populations.

We have shown in this section that we have a good understand of the dominant contaminating populations. This implies that the selection algorithm is nearly optimal.

#### 7 CONCLUSIONS

In this paper, we have presented a search for redshift 6.5 < z < 9.3 quasars over  $977 \, \mathrm{deg^2}$  of the VIKING survey. We have exploited a new list-driven data set, which provides fluxes and uncertainties for all *J*-detected VIKING sources, in all available photometric bands *Z*, *Y*, *J*, *H*,  $K_s$ . We searched the data base using a modification of the BMC method of Mortlock et al. (2012), and produced a sample of 21 candidate quasars z > 6.5. This candidate list includes the four previously discovered z > 6.5 quasars in this field.

We have followed up the additional 17 candidates and confirmed that none are quasars. The sample and the selection criteria define a complete sample and allow us to compute the survey selection function for VIKING for the first time. The survey reaches some 1.5 mag deeper than the sample of Wang et al. (2019), the only other complete sample at these redshifts. Previous searches of VIKING (Venemans et al. 2013, 2015) covered a smaller area, were not as deep, and were incomplete in that they did not follow-up all candidates.

We also undertook a comparison of three different selection methods, BMC-, SED-fitting, and colour cuts. We found that the BMC method is the best. It reaches 0.3 mag deeper than the colour cuts method, while the number of false positives is a factor of eight smaller. The BMC method reaches 0.7 mag deeper than the SED-fitting method, which only finds one of the four known quasars in this field.

We find evidence for a population of emission-line galaxies with strong [O III]  $\lambda\lambda4959,5007$  emission that are brighter examples of similar sources found in deeper quasar surveys near z=6. Such objects could potentially contaminate future surveys for HZQs with *Euclid*, and therefore need to be better characterized.

In a forthcoming publication, we will use the new complete sample and associated selection function to refine the estimated rate of decline in quasar space density over the interval of 6 < z < 7.5.

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#### DATA AVAILABILITY

This work is based on the VIKING data release VIKINGv20160406 available as part of the VISTA Science Archive (http://horus.roe.ac.u k/vsa/index.html). A version of the BMC code is publicly available at http://github.com/rhysrb/Pq\_server. Raw ESO follow-up data can be accessed via http://archive.eso.org/cms.html as part of programme 0102.A-0848(A). Derived data products generated in this research will be shared on reasonable request to the corresponding author.

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# APPENDIX A: PRIMARY AND SECONDARY OBSERVATIONS IN VIKING

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The basic VISTA survey area is, as described by Cross et al. (2012), a 'tile' (which we have also referred to as a frameset in this work), formed of six individual exposures labelled 'pawprints'. These pawprints are offset such that a single tile is at least doubly exposed, with the exception of a narrow strip at the top and bottom of the tile, which is imaged just once. These strips overlap with adjacent tiles, allowing the minimum survey depth to be achieved by ensuring the full VIKING area is imaged at least twice. A consequence of this observation strategy is that duplicate entries appear in the table. After source merging is complete, a process known as seaming takes place, which identifies and flags duplicates, using the PriOrSec (POS) property.

Where a VIKING source is duplicated, the 'better' entry as determined on the basis of the proximity to the optical axis of the camera, is labelled as the primary using the POS flag, and the other entry labelled the secondary. Our list-driven catalogue contains  $4.3 \times 10^7$  entries, of which 18 per cent are labelled as secondary.

This proportion corresponds closely to the area of a tile that is singly imaged (Cross et al. 2012).

Given that such a large proportion of VIKING sources are duplicated, in our search for HZQs using the BMC method, we applied slightly different criteria to these doubly observed sources to avoid missing any interesting candidates. If either of the primary or secondary observations of a doubly observed source satisfied  $P_{\rm q} > 0.1$ , we averaged the primary and secondary photometry using inverse variance weighting, and assessed its selection again, this time applying the  $P_{\rm q} > 0.15$  threshold. Two known quasars (for which both the primary and secondary entries satisfied  $P_{\rm q} > 0.15$  anyway) and two of the new candidates, indicated in Table 1, were selected in this way.

We also assessed the impact of primaries/secondaries on our BMC HZQ selection function. The flux errors of the VIKING secondaries are typically somewhat worse than the primary flux errors, up to a level of 30 per cent. For each HZQ that we simulate (representing primaries), we therefore produce a second set of photometry drawn from flux distributions with the uncertainties enhanced by 30 per cent (secondaries). Again, if either the primary or secondary HZQ entry was selected using the relaxed criteria, we produced a third set of photometry for each HZQ, by averaging the primary and secondary photometry using inverse variance weighting. We find, for a simulated HZQ, selection using the combined photometry matches selection using only primary data very closely. We conclude that the presence of a secondary does not typically allow the selection of a source that is not otherwise selected, nor does it prevent the selection of a HZQ that is selected on the basis of its primary.

#### APPENDIX B: POPULATION MODELLING

Here, we summarize the surface density terms and model colours which are used in the selection methods described in Section 3. We present the models for quasars in Section B1, for MLTs in Section B2, and for ETGs in Section B3. The population models are determined following the same procedures detailed in Euclid Collaboration: Barnett et al. (2019), allowing for the differences between the *Euclid* and VIKING filters, and the different image quality, which is relevant to modelling the ETGs. In order not to repeat too much material between the two papers, the presentation is briefer in the current paper, but we draw attention to aspects of the population models that differ from the *Euclid* work. The model colours are shown in Fig. 2. As a reminder, in this paper magnitudes are quoted on the Vega system, whereas in Euclid Collaboration: Barnett et al. (2019) they are on the AB system.

### **B1 Quasars**

The parameters  $\theta$  for the quasars are absolute magnitude and redshift. For the VIKING analysis, we adopt the single power law QLF used by Mortlock et al. (2012), since we do not probe significantly fainter than the 'knee' of the luminosity function (Jiang et al. 2016; Matsuoka et al. 2018). The redshift evolution of this QLF uses k=-0.47: We have not adopted the stronger values since we started selecting VIKING quasar candidates before Jiang et al. (2016) or Wang et al. (2019) were published. While using a weaker evolution for the quasar weight will boost the resulting values of  $P_{\rm q}$ , the relative probabilistic ranking of VIKING sources will be almost unchanged; even using a more strongly evolving QLF, we could select almost exactly the same list of candidates by adjusting the  $P_{\rm q}$  threshold.

The nine quasar SEDs comprise combinations of three different continuum slopes and three different emission-line strengths, and

### 1674 R. Barnett et al.

the details are provided in section 5.6 of Euclid Collaboration: Barnett et al. (2019). As was the case in Euclid Collaboration: Barnett et al. (2019), we use symphot to directly measure the quasar k-corrections and colours used in the SED-fitting and BMC techniques, from updated versions of the model spectra from Hewett et al. (2006) and Maddox et al. (2008). We use the version of the model with 'standard' continuum slope and emission-line strength in the selection. For our simulated sources, we assume that all flux blueward of Ly $\alpha$  is absorbed, except that we include a near zone of radius 3 Mpc (proper). Our quasar selection functions are not sensitive to the exact choice of the near-zone size within the range 1-5 Mpc.

#### **B2 MLT dwarfs**

The total MLT weight is determined by summing individual subweights, computed for each spectral type M0-T8. We therefore require the full range of VIKING ZYJHK<sub>s</sub> colours for each spectral type. Skrzypek et al. (2015), Skrzypek, Warren & Faherty (2016) provide UKIDSS YJHK colours for types M7-T8. The UKIDSS YJH filters are a close match to VISTA; however, there is no match in those works for the VISTA Z and  $K_s$  bands, so Z - Y and H  $-K_s$  must be determined separately for M7-T8. We additionally require the full set of VIKING colours for M0 – M6. To proceed, we select a bright subsample  $(S/N_i > 50)$  from the spectroscopic M dwarf catalogue presented by West et al. (2011). We determine average Z-Y and  $H-K_s$  colours for all M dwarfs by matching the M dwarf sample to VIKING. We additionally match the M dwarf sample to UKIDSS and measure median rizYJH SDSS/UKIDSS colours for M0-M5. These are required for the M0-M5 absolute magnitudes, as detailed further below.

For the L and T dwarf  $H - K_s$  colour, we make use of the corrections provided by Stephens & Leggett (2004), which allow conversions between the MKO filter set used by UKIDSS, and other photometric systems. We find the DENIS K band provides a close match to the VIKING  $K_s$  filter, allowing us to approximate  $H - K_s$  for L and T types. Finally, we determine Z - Y colours for L and T dwarfs by fitting a polynomial to the sources presented by Hewett et al. (2006). We present the full set of VIKING  $ZYJHK_s$  colours in Table B1.

The dwarf star surface density term requires number densities and absolute magnitudes for each spectral type. We use the the Galactic plane number densities presented in Euclid Collaboration: Barnett et al. (2019). Dupuy & Liu (2012) provide MKO *J*-band absolute magnitudes for spectral types M6–T8. For M0–M5 we use the relationship between i-z and  $M_r$  from Bochanski et al. (2010). We correct to the Vega system using the offsets provided by Hewett et al. (2006), and then use the colours determined above to convert  $M_r$  to  $M_J$ . As in Euclid Collaboration: Barnett et al. (2019), we have assumed MLT number density varies as  $\rho = \rho_0 \, \mathrm{e}^{-Z/Z_s}$ , where  $\rho_0$  is the number density of any spectral type M0–T8 at the Galactic central plane, Z is the vertical distance from the plane, and  $Z_s$  is the scale height, assumed to be 300 pc. The small offset of the Sun from the Galactic plane is disregarded.

#### **B3** Early-type galaxies

Over the redshift range z = 1-2, ETGs have red NIR colours, which can resemble the colours of HZQs at low S/N. In previous works, which have focused on the brightest candidates, this source of contamination has been mitigated by taking a cut on a morphological statistic (e.g. Mortlock et al. 2012; Venemans et al. 2013). However,

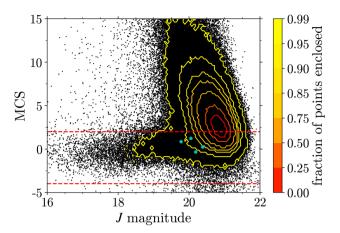
Table B1. MLT density and model colour data for VIKING.

SpT	$\rho_0  (\mathrm{pc}^{-3})$	$M_J$	Z-Y	Y - J	J-H	$H-K_{\rm s}$
M0	$2.4 \times 10^{-3}$	5.69	0.29	0.45	0.62	0.19
M1	$2.7 \times 10^{-3}$	6.24	0.32	0.47	0.60	0.22
M2	$4.4 \times 10^{-3}$	6.85	0.35	0.49	0.58	0.23
M3	$7.8 \times 10^{-3}$	7.38	0.39	0.51	0.55	0.24
M4	$1.0 \times 10^{-2}$	7.96	0.44	0.53	0.54	0.26
M5	$1.1 \times 10^{-2}$	8.56	0.51	0.57	0.53	0.29
M6	$7.8 \times 10^{-3}$	9.86	0.60	0.63	0.53	0.31
M7	$2.2 \times 10^{-3}$	10.65	0.70	0.68	0.54	0.34
M8	$1.7 \times 10^{-3}$	11.06	0.83	0.79	0.56	0.38
M9	$1.1 \times 10^{-3}$	11.31	0.99	0.87	0.59	0.42
L0	$6.7 \times 10^{-4}$	11.52	1.20	1.04	0.63	0.53
L1	$4.3 \times 10^{-4}$	11.78	1.29	1.11	0.67	0.55
L2	$3.8 \times 10^{-4}$	12.11	1.33	1.18	0.73	0.59
L3	$3.6 \times 10^{-4}$	12.51	1.36	1.23	0.79	0.62
L4	$5.3 \times 10^{-4}$	12.95	1.38	1.27	0.86	0.66
L5	$4.1 \times 10^{-4}$	13.40	1.40	1.31	0.91	0.68
L6	$2.2 \times 10^{-4}$	13.82	1.42	1.33	0.96	0.70
L7	$6.3 \times 10^{-4}$	14.17	1.46	1.35	0.97	0.70
L8	$3.9 \times 10^{-4}$	14.42	1.51	1.21	0.96	0.68
L9	$4.8 \times 10^{-4}$	14.56	1.59	1.20	0.90	0.63
T0	$6.3 \times 10^{-4}$	14.60	1.69	1.19	0.80	0.55
T1	$6.4 \times 10^{-4}$	14.55	1.82	1.19	0.65	0.45
T2	$3.6 \times 10^{-4}$	14.45	1.97	1.18	0.46	0.33
T3	$3.6 \times 10^{-4}$	14.35	2.14	1.18	0.25	0.19
T4	$5.6 \times 10^{-4}$	14.32	2.32	1.17	0.02	0.06
T5	$7.1 \times 10^{-4}$	14.44	2.52	1.16	-0.19	-0.05
T6	$2.1 \times 10^{-4}$	14.78	2.72	1.16	-0.35	-0.12
T7	$2.1 \times 10^{-3}$	15.42	2.92	1.15	-0.43	-0.11
T8	$7.5 \times 10^{-4}$	16.42	3.10	1.15	-0.36	0.01

size and stellar mass for the ETG population are strongly correlated (van der Wel et al. 2014), suggesting faint ETGs at these redshifts will be very compact, and classified as point sources by VIKING. We illustrate this point in Fig. B1, which shows the behaviour of the MCS statistic as a function of J magnitude for our initial sample of red sources, before applying the cut on MCS (see Sect 3.2). At bright magnitudes ( $J\lesssim19$ ), there are two distinct populations: point sources, with MCS  $\simeq0$ , and extended sources at much higher values. However, at fainter magnitudes, the two populations become merged, i.e. morphology is no longer a good discriminator. We therefore have to incorporate the ETG population as a contaminant.

The MCS statistic measures the similarity of the radial surface brightness profile to the profile of stars, and is normalized such that at any magnitude the distribution for point sources is Gaussian with standard deviation unity. As can be seen, at faint magnitudes the Gaussian distribution becomes more difficult to discern, and so to normalise correctly. However, this is successfully achieved by fitting to the negative part of the distribution. The fact that for each of the four quasars MCS lies within the range -2 to +2 is an indication that the normalization works well in the regime of high galaxy surface density.

We firstly derive a model for the surface density and colours of ETGs as a function of redshift and J magnitude. We then account for the magnitude dependence of the MCS parameter. As in Euclid Collaboration: Barnett et al. (2019), we make use of the COSMOS/UltraVISTA sources presented by Laigle et al. (2016) to derive the model. Euclid Collaboration: Barnett et al. (2019) found that quiescent objects in the COSMOS catalogue have a large range of formation redshifts ( $z_f$ ), and approximated the catalogue as two separate populations, with a fraction 0.8 having  $z_f = 3$ , and a fraction



**Figure B1.** MCS statistic as a function of J magnitude. Black points mark the sources in our VIKING sample, where we have not taken a cut on MCS. The blue circles are the four HZQs. The red dashed lines indicate our cut to eliminate bright ellipticals.

0.2 having  $z_f = 10$ . We use colours computed for both formation redshifts, from the evolutionary models of Bruzual & Charlot (2003).

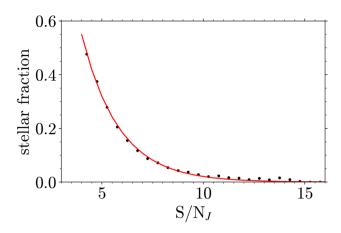
To produce a surface density model that can be applied to VIKING, we first fit a surface density model to 2".0 aperture COSMOS data. We then require corrections to convert COSMOS aperture magnitudes to VIKING APERMAG3 magnitudes. The COSMOS/UltraVISTA area does not overlap with VIKING; however, there is overlap with the UKIDSS LAS, and the UKIDSS and VIKING data are similar in terms of image quality and the data-processing pipeline. We find 195 COSMOS sources are detected in the K band in the LAS, allowing us to compare the 2'.0 aperture magnitudes between the LAS and COSMOS. The UKIDSS APERMAG3 photometry corresponds to the flux in a 2".0 aperture, that is then aperture corrected to total flux using the aperture correction for a point source. Therefore, the aperture correction has to be subtracted to get the LAS flux in the 2".0 aperture. After doing this we find the UKIDSS fluxes agree with the COSMOS fluxes almost exactly, on average. On this basis, we use the following relation between the 2".0 aperture J-band AB COSMOS magnitudes  $J_{corr}$  and VIKING Vega APERMAG3 Jmagnitudes:  $J_{corr} = J + 1.147$ . This equation incorporates both the AB correction and the point source aperture correction.

The surface density function in terms of  $J_{\rm corr}$  and source redshift is determined from a maximum-likelihood fit. The functional form of this function in units of  ${\rm mag}^{-1} {\rm deg}^{-2}$  per unit redshift is

$$\Sigma(J_{\text{corr}}, z) = \alpha \exp \left\{ -\frac{1}{2} \left[ \frac{J_{\text{corr}} - (J_0 + b z)}{\sigma} \right]^2 \right\} \exp \left[ -\left( \frac{z - 0.8}{z_0} \right) \right], \quad (B1)$$

where we find the best-fitting parameters to be  $(\alpha, \sigma, J_0, b, z_0) = (7697, 0.883, 20.467, 1.462, 0.429)$ . We assume the same function is applicable to ETGs with either formation redshift, and scale the resulting weights by 0.8 for  $z_f = 3$  and 0.2 for  $z_f = 10$  to reflect the distribution of  $z_f$  values seen in the COSMOS data.

The surface density function and the model colours provide a complete description of the ETG population, with the exception that only objects satisfying the cut -4 < MCS < 2 will appear in the sample. We therefore need to quantify the magnitude dependence of this cut on MCS. We wish to evaluate the fraction of ETGs that satisfy the MCS cut. From the counts of red sources as a function of S/N we can tally separately stellar sources, with -4 < MCS < 2, and extended sources. We can subtract the counts of MLTs from the stellar counts using the density model for these sources. Then we are left with galaxy counts only as a function of S/N, separated into



**Figure B2.** Measured fraction of ETGs classified as stellar as a function of  $S/N_J$ . The red curve shows the exponential fit, equation (B2).

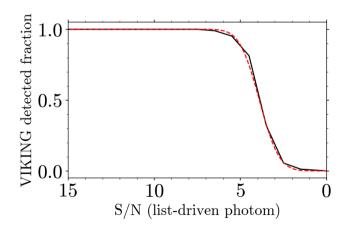
galaxies classified as stellar and galaxies classified as extended. The proportion of galaxies classified as stellar as a function of S/N in the J band is plotted in Fig. B2. The resulting function is well fit by an exponential of the form

stellar fraction = 
$$a \cdot \exp(-b \cdot S/N_I)$$
, (B2)

where we find the best fit to be (a, b) = (4.837, 0.544). The full galaxy prior is formed by multiplying equations (B1) and (B2).

## APPENDIX C: SIMULATING DETECTION IN THE J BAND

Our list-driven sample starts with the list of objects detected in the original VIKING catalogue which have S/N > 4 in an aperture of diameter 2".0. For a source in the J band that has a given S/N in the aperture, we want to know the probability that it would have been detected, i.e. would have made it into the VIKING catalogue. We cannot measure this in the J band itself since we do not have measurements of the sources not in the VIKING catalogue. However, whether or not a source in, say, the Y band measured at a particular S/N gets into the VIKING catalogue does not depend on what happens in the J band. So we can gauge the detection probability in any chosen band starting with any catalogue of real sources detected in some other band, and then measuring them in the chosen band.



**Figure C1.** VIKING completeness as a function of S/N in any band. Results from the Y, H, and  $K_s$  bands have been averaged. The red dashed line plots the cumulative Gaussian function that we fit to the data.

## 1676 R. Barnett et al.

We start by matching a sample of sources classified as stellar in the deeper VISTA Deep Extragalactic Observations survey (VIDEO; Jarvis et al. 2013) survey to our list-driven catalogue. This simply ensures that the objects are real, since they are found in both catalogues. Then in, e.g. the Y band, we evaluate the fraction of sources that are detected in Y in VIKING (i.e. appear in the original VIKING catalogue) as a function of S/N in the aperture in that band. The results averaged over the Y, H, and  $K_s$  bands are plotted in Fig. C1.

To be clear, this says that if an object has the given S/N in the aperture on any frame, then the probability that it will appear in the original VIKING catalogue is given by the function

plotted. This is the function needed to quantify detection in the J band for modelling the selection functions (Section 5), and for creating the synthetic catalogue (Section 6). We fit a Gaussian cumulative distribution function (CDF; i.e. the error function) to this curve. The (50, 68, 95) per cent quantiles are found to lie at at S/N = (3.9, 4.8, 5.7). Each source that we simulate is then detected or rejected with a probability set by this CDF, leaving us with sources that would be present in the VIKING list-driven catalogue.

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