

1 **Detection of significant antiviral drug effects on**  
2 **COVID-19 with reasonable sample sizes in randomized**  
3 **controlled trials: a modeling study combined with**  
4 **clinical data**

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## Abstract

### Background

Development of an effective antiviral drug for COVID-19 is a global health priority. Although several candidate drugs have been identified through *in vitro* and *in vivo* models, consistent and compelling evidence from clinical studies is limited. The lack of evidence from clinical trials may stem in part from the imperfect design of the trials, which may fail to incorporate two critical factors: 1) heterogeneity in virus dynamics among patients and 2) timing of treatment initiation. However, it remains unclear how SARS-CoV-2 virus dynamic differs among patients and how clinical studies of antiviral drugs for COVID-19 have to be designed.

### Methods and Findings

To help understand the reasons behind inconsistent clinical trial findings, we performed a modelling study. We first analyzed longitudinal viral load data for SARS-CoV-2 without antiviral treatment by use of a within-host virus dynamics model. The fitted viral load was categorized into three different groups by a clustering approach. Comparison of the estimated parameters showed that the three distinct groups were characterized by different virus decay rates ( $p$ -value $<0.001$ ). The decay rates were 1.17  $d^{-1}$  (95% CI: 1.06 to 1.27  $d^{-1}$ ), 0.777  $d^{-1}$  (0.716 to 0.838  $d^{-1}$ ), and 0.450  $d^{-1}$  (0.378 to 0.522  $d^{-1}$ ) for the three groups, respectively. Such heterogeneity in virus dynamics could be a confounding variable if it is associated with treatment allocation in compassionate use programs (i.e., observational studies).

77 Subsequently, we mimicked randomized controlled trials of antivirals by  
78 simulation. An antiviral effect causing a 95% to 99% reduction in viral replication was  
79 added to the model. To be realistic, we assumed that randomization and treatment are  
80 initiated with some time lag after symptom onset. Using the duration of virus shedding  
81 as an outcome, the sample size to detect a statistically significant mean difference  
82 between the treatment and placebo groups (1:1 allocation) was 13,603 and 11,670  
83 (when the antiviral effect was 95% and 99%, respectively) per group if all patients are  
84 enrolled regardless of timing of randomization. The sample size was reduced to 584  
85 and 458 (when the antiviral effect was 95% and 99%, respectively) if only patients who  
86 are treated within 1 day of symptom onset are enrolled. We confirmed the sample size  
87 was similarly reduced when using cumulative viral load in log scale as an outcome.

88 We used a conventional virus dynamics model which does not fully reflect the  
89 detailed physiological processes of virus replication of SARS-CoV-2 and excluded viral  
90 load data under treatment to evaluate our model. Further investigation should find  
91 factors not incorporated in the model, which would yield more reliable sample size  
92 calculation.

## 93 **Conclusions**

94 In this study, we found large heterogeneity in virus dynamics among infected  
95 individuals, characterized by different virus decay rates, and the time of treatment  
96 initiation as important factors behind the inconsistent or null findings of clinical studies of  
97 the antiviral effect of treatments for SARS-CoV-2 infection. In clinical trials that have  
98 failed to identify effective antiviral drugs against SARS-CoV-2, there may be at least two  
99 reasons behind this: 1) randomization is not performed (i.e., observational studies), and

100 2) randomization and treatment initiation are delayed. For a statistically significant effect  
101 of antiviral drugs on COVID-19 to be observed a study's design should consider these  
102 two factors.

## 103 **Author Summary**

### 104 ■ Why was this study done?

- 105 • Most clinical studies of antiviral drugs for SARS-CoV-2 have failed to observe a  
106 statistically significant effect.
- 107 • The confounding factors leading to the failure of antiviral drug clinical trials and the  
108 suitable design for successful clinical trials of antiviral drugs against SARS-CoV-2  
109 are unknown.

### 110 ■ What did the researchers do and find?

- 111 • SARS-CoV-2 virus dynamics was quantified by fitting a virus dynamic model to  
112 longitudinal viral load data.
- 113 • Cluster analysis of the fitted viral loads revealed three distinct groups characterized  
114 by different virus decay rates, which could be a confounding factor in observational  
115 studies.
- 116 • Simulation mimicking randomized controlled trials demonstrated that sample size  
117 would be unreasonably large (>11,000 per group) if the timing of treatment initiation  
118 is not considered. The sample size is significantly reduced by including only patients  
119 enrolled early after symptom onset.

### 120 ■ What do these findings mean?

- 121 • Randomized controlled trials for antiviral drugs should recruit patients as early as  
122 possible after symptom onset or set inclusion criteria based on the time since  
123 symptom onset to observe statistically significant results.

124

- More precise models reflecting the features of SARS-CoV-2 infection may provide more reliable sample size estimates.

125

126

## 127 Introduction

128 Development of an effective antiviral drug for COVID-19 is a global health  
129 priority. Along with the development of new antiviral drugs, repurposing of existing drugs  
130 for COVID-19 treatment has accelerated [1]. Some antiviral drugs have shown high  
131 efficacy against severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) in both  
132 *in vitro* and *in vivo* models [2, 3]. A number of clinical studies such as compassionate  
133 use programs and clinical trials have been conducted or are underway to test the  
134 efficacy of FDA-approved drugs, such as lopinavir and ritonavir, chloroquine, favipiravir,  
135 and remdesivir [4-9]. Different drugs have different modes of action, but the majority of  
136 the candidate antiviral drugs for SARS-CoV-2 are expected to block virus replication.  
137 Lopinavir/ritonavir are HIV protease inhibitors, and remdesivir was originally developed  
138 to mitigate the replication of hepatitis C viruses (and considered potentially useful for  
139 Ebola virus). Other nucleoside analogues [10, 11] are also candidates for mitigating  
140 SARS-CoV-2 replication within the host.

141 However, the results from those clinical studies were often nonsignificant and  
142 sometimes inconsistent. This may be in part attributable to a nonrigorous study design,  
143 which masks the true efficacy of antivirals [12]. Clinical trial design usually takes months  
144 to formulate the study protocol (i.e., dose of drugs, clinical outcomes to be evaluated,  
145 sample size, assessment of safety), and requires collecting preliminary data. However,  
146 the urgent need to find effective antiviral treatments for COVID-19 may have led to  
147 rushed studies.

148 In compassionate use programs (i.e., observational studies), whether and when  
149 antiviral treatment is initiated is determined by health practitioners along with patients

150 and their next of kin. By the very nature of these studies, potential confounders, such as  
151 the patients' clinical characteristics and preexisting conditions, influence both treatment-  
152 control allocation and clinical outcomes. As a consequence, conclusions from the  
153 program could be biased even when all observable confounders are addressed in the  
154 analysis [13]. However, such programs are widely used for hypothesis building.  
155 Contrary to compassionate use programs, clinical trials, particularly randomized  
156 controlled trials, are considered robust against confounder effects and the most reliable  
157 study design. **Table S1** summarizes the current major clinical studies for antiviral  
158 treatment of SARS-CoV-2. Indeed, the results from these clinical studies have yielded  
159 null or inconsistent findings. For example, compassionate use of hydroxychloroquine  
160 was reported in many articles, but the findings were not consistent. Gautret et al.  
161 reported significant antiviral efficacy [14], whereas Geleris et al. could not replicate the  
162 result [15].

163 To help understand the mechanism behind the inconsistent findings, we  
164 parametrized the virus dynamics model which we previously developed [16-18] by using  
165 longitudinal viral load data extracted from clinical studies and further ran simulations  
166 adding antiviral effects to the model. Here, we demonstrate that at least two factors can  
167 mask the effects of antiviral drugs in clinical studies for COVID-19: 1) heterogeneity in  
168 virus dynamics among patients and 2) late timing of treatment initiation. We also  
169 propose a novel approach to the best of our knowledge to calculating the sample size  
170 (i.e., the required or minimum sample size needed to infer whether the antiviral drug is  
171 effective assuming the drug is truly effective) accounting for within-host virus dynamics.

## 172 **Methods**

### 173 **Study data**

174 The longitudinal viral load data examined in our study were extracted from the  
175 published studies of SARS-CoV-2: Young et al. [19], Zou et al. [20], Kim et al. [21], and  
176 Wölfel et al. [22]. For consistency, the viral load data measured from upper respiratory  
177 specimens were used. We excluded patients who received antiviral treatment and for  
178 whom data were measured on only 1 or 2 days (because one or two data points are not  
179 enough to estimate parameters). We converted cycle threshold (Ct) values to viral RNA  
180 copy number values, where these quantities are inversely proportional to each other  
181 [20]. In total, we use the data from 30 patients. To extract the data from the images in  
182 those papers, we used the software datathief III (version 1.5, Bas Tummings,  
183 [www.datathief.org](http://www.datathief.org)).

### 184 **Mathematical model for virus dynamics without and with antiviral treatment**

185 SARS-CoV-2 virus dynamics without antiviral treatment is described by a  
186 mathematical model previously proposed in [23-25].  
187

$$188 \quad \frac{df(t)}{dt} = -\beta f(t)V(t), \quad (1)$$

$$189 \quad \frac{dV(t)}{dt} = \gamma f(t)V(t) - \delta V(t), \quad (2)$$

190 where  $f(t)$  is the relative fraction of uninfected target cells at time  $t$  to those at time 0  
191 and  $V(t)$  is the amount of virus at time  $t$ , respectively. Both  $f(t)$  and  $V(t)$  are in linear

192 scale. The parameters  $\beta$ ,  $\gamma$ , and  $\delta$  represent the rate constant for virus infection, the  
 193 maximum rate constant for viral replication, and the per capita death rate of virus-  
 194 producing cells, respectively. Note that  $\delta$  implicitly includes the effects of the immune  
 195 response in killing infected cells, e.g. by cytotoxic T lymphocytes. All viral load data  
 196 were fit using a nonlinear mixed-effect modelling approach, which estimates population  
 197 parameters while accounting for inter-individual variation in virus dynamics (see the next  
 198 section for detail). The day from symptom onset was used as a time scale (i.e.,  $t = 0$  at  
 199 symptom onset).

200 The virus dynamic model under antiviral treatment (which we assume blocks  
 201 virus replication) initiated at  $t^*$  days after symptom onset can be described based on the  
 202 above model as follows:

$$203 \quad \frac{df(t)}{dt} = -\beta f(t)V(t), \quad (3)$$

$$204 \quad \frac{dV(t)}{dt} = (1 - \varepsilon \times H(t))\gamma f(t)V(t) - \delta V(t), \quad (4)$$

205 where  $H(t)$  is a Heaviside function indicating off- and on-treatment, defined as  $H(t) = 0$   
 206 if  $t < t^*$  (i.e., before treatment initiation); otherwise  $H(t) = 1$ .  $\varepsilon$  is the fraction of virus  
 207 production inhibited by the therapy ( $0 < \varepsilon \leq 1$ ).  $\varepsilon = 1$  when the virus replication from the  
 208 infected cells is totally inhibited (i.e., the antiviral effect is 100%). We evaluated the  
 209 expected antiviral effect of the treatment on the outcomes (duration of virus shedding  
 210 and cumulative viral load measured on a log scale) under different inhibition rates ( $\varepsilon$ )  
 211 and initiation times ( $t^*$ ). The effect of drugs that blocking *de novo* infection can be  
 212 modeled by inhibiting both the  $\beta f(t)V(t)$  and  $\gamma f(t)V(t)$  terms and a drug promoting  
 213 cytotoxicity can be modeled by increasing  $\delta V(t)$ , as we discussed in [24]. Unfortunately,

214 because sufficient viral load data under antiviral drug therapy are not available yet, the  
215 antiviral effect ( $\varepsilon$ ) of drugs in preclinical development and in clinical trials are still  
216 unknown. Therefore, we chose to examine hypothetical examples of drugs with 50%,  
217 95%, or 99% efficacy. We used 50% and 99% efficacy to illustrate the difference in viral  
218 dynamics between patients with and without treatment (see section “**SARS-CoV-2 virus**  
219 **dynamics and antiviral effect**”), and 95% and 99% efficacy in “**Simulation mimicking**  
220 **a randomized controlled trial for antiviral drugs**”. Since clinical trials are performed  
221 only for drugs with sufficient efficacy (i.e., there is no reason to test drugs with weak  
222 efficacy), we believe this value range is reasonable.

223

#### 224 **Parameter estimation with the nonlinear mixed-effects model**

225 A nonlinear mixed-effects model was used to fit the viral dynamic model given by  
226 equations [Eq1] and [Eq2] to the longitudinal viral load data. The model included both a  
227 fixed effect (constant across patients) and a random effect (different between patients)  
228 in each parameter. Specifically, the parameter for patient  $k$ ,  $\vartheta_k (= \vartheta \times e^{\pi_k})$  is  
229 represented as a product of  $\vartheta$  (a fixed effect) and  $e^{\pi_k}$  (a random effect).  $\pi_k$  follows the  
230 normal distribution with mean 0 and standard deviation  $\Omega$ . Fixed effects and random  
231 effects were estimated using the stochastic approximation expectation-maximization  
232 algorithm and empirical Bayes’ method, respectively. The conditional distribution of the  
233 vector of individual parameters was estimated for each patient using the Metropolis-  
234 Hastings algorithm and was used to calculate the 95% predictive interval of the viral  
235 load curve in **Fig. 1**. The mixed model approach is becoming more common in  
236 longitudinal viral load data analysis [18, 26], because it can capture the heterogeneity in

237 virus dynamics, and parameter estimation is feasible even for those with limited data.  
238 Fitting was performed using MONOLIX 2019R2 ([www.lixoft.com](http://www.lixoft.com)) [27]. To account for  
239 data points under the detection limit (see the red dots in **Fig. S1**), the likelihood function  
240 reflected the likelihood that the data are in the censoring interval (0 to the detection  
241 limit) given parameter values with a right-truncated Gaussian distribution [28].

242

### 243 **Clustering of individual viral load dynamics**

244 As observed in **Fig. 1**, the virus dynamics has huge heterogeneity between  
245 patients. For some patients, viral load declines rapidly, but for others, it persists for  
246 almost 1 month. It is ideal if the longitudinal viral load data can be directly compared  
247 between patients; however, the data collection intervals are not the same between  
248 patients, and the data under the detection limit are not quantifiable. Therefore, we used  
249 the fitted viral load every day since symptom onset, which is available from the best fit  
250 curve, for comparison. The fitted daily viral load values of each patient were rescaled by  
251 their maximum values and log-transformed. Then, hierarchical clustering was performed  
252 on the rescaled-transformed fitted daily viral load using the linkage function with Ward's  
253 method [29] in SciPy [30]. Once multiple clusters are identified, estimated parameter  
254 distributions among the clusters were compared by ANOVA to assess the source of the  
255 difference in virus dynamics. Pairwise comparison was subsequently performed using  
256 Student's *t* test. The p-values of the pairwise Student's *t* test were adjusted by the  
257 Bonferroni correction.

258

## Simulation mimicking a randomized controlled trial for antiviral drugs

We mimicked randomized controlled trials using the model including the effects of an antiviral drug. The allocation ratio is assumed as 1:1 (control:treatment). A total of 20,000 parameter sets were randomly sampled from the estimated distributions of individual parameters. A longitudinal viral load time series for each individual was created based on their chosen parameter set. Note that for those in the treatment group, the antiviral effect ( $\varepsilon$ ) was assumed to be constant. For sensitivity analysis, we used two different values of  $\varepsilon$ , 95% and 99%. To obtain a realistic simulation, treatment was initiated following the distribution of time from symptom onset to hospitalization obtained from Bi et al.:  $\text{lognorm}(1.23, 0.79)$  (the mean is 4.64 days) [31], where the treatment was assumed to be initiated immediately after hospitalization. We also used a truncated distribution to mimic the randomized controlled trials including only patients recruited and treated early (within 0.5, 1, 2, 3, and 4 days after symptom onset).

We used two quantities as outcome measures: the duration of virus shedding from the onset of symptoms until the time the virus becomes undetectable ( $T_D$ ), and the log10-transformed cumulative viral load, i.e., the area under the curve (AUC) of viral load ( $\log_{10}(\text{AUC}): \log_{10} \int_0^{T_D} V(s) ds$ ). Many clinical studies have used the duration of viral shedding as a primary outcome (see **Table S1**) and previous theoretical studies have quantified the AUC. Both of the outcomes we use here are expected to be reduced under effective antiviral treatment.

From our simulations we obtained 10,000 outcomes for each group (duration of virus shedding and cumulative viral load). The sample size was computed for different

281 values of  $\varepsilon$  using the two-tailed Welch's  $t$  test with significance level and power as 0.05  
282 and 80%, respectively.

## Results

### Heterogeneity in SARS-CoV-2 virus dynamics

SARS-CoV-2 viral load data were analyzed using a mathematical model to quantify the heterogeneity in virus dynamics among patients and to examine the source of the heterogeneity. Longitudinal viral load data from 30 patients from different countries were fitted simultaneously using a nonlinear mixed-effects modelling approach. With the estimated parameters for each patient (listed in **Table S2**), viral loads since the time of symptom onset were fully reconstructed even when the viral load was missed or under the detection limit (**Fig.1** and **Fig.2A**). This reconstruction allowed us to quantitatively compare viral load dynamics between patients. The viral loads over time, which were reconstructed based on the mathematical model with the estimated parameters, were analyzed with a clustering approach (**Fig.2B**) and placed into three groups. Patient “China O” was detected as an outlier and was excluded from further analysis.

To understand the source of the difference in virus dynamics between groups, we tested the differences in the estimated parameters (i.e.,  $\beta$ ,  $\gamma$ ,  $\delta$  and  $V(0)$ ) among the groups. Statistically significant between-group differences were found in the maximum rate constant for viral replication,  $\gamma$ , and in the death rate of virus-producing cells per day,  $\delta$  (**Fig.S1**). The differences in  $\gamma$  are related to the growth of viral load (a larger  $\gamma$  indicates more rapid growth); however, the difference in  $\gamma$  between groups was sufficiently small that its influence on virus dynamics especially after the viral load peak (or symptom onset) is negligible. The difference in  $\delta$  manifests in the speed of viral load decay; that is, a small value of  $\delta$  corresponds to a slow decay in viral load (**Fig.2B**).

306 Thus, we named the three groups as rapid, medium, and slow viral load decay groups  
307 (**Fig.3A**). The means of decay rates were  $1.17 \text{ d}^{-1}$  (95% CI:  $1.06$  to  $1.27 \text{ d}^{-1}$ ),  $0.777 \text{ d}^{-1}$   
308 ( $0.716$  to  $0.838 \text{ d}^{-1}$ ), and  $0.450 \text{ d}^{-1}$  ( $0.378$  to  $0.522 \text{ d}^{-1}$ ) for the three groups, respectively  
309 and the minimum and maximum of the decay rate for the three identified groups were  
310  $0.270 \text{ d}^{-1}$  to  $0.616 \text{ d}^{-1}$  (slow),  $0.700 \text{ d}^{-1}$  to  $0.914 \text{ d}^{-1}$  (medium), and  $0.993 \text{ d}^{-1}$  and  $1.30 \text{ d}^{-1}$   
311 (rapid). The border value of the decay rate between groups is defined as the mean of  
312 the highest value in the lower group and the lowest value in the higher group. Thus, the  
313 border value of the slow and medium groups was  $0.658 \text{ d}^{-1}$  [ $(0.616 + 0.700)/2$ ], and that  
314 of the medium and rapid groups was  $0.953 \text{ d}^{-1}$  [ $= (0.914 + 0.993)/2$ ].

315

### 316 **SARS-CoV-2 virus dynamics and antiviral effect**

317 Using our mathematical model and the estimated parameter distribution for each  
318 patient (**Table S3**), we conducted *in silico* experiments to determine the possible  
319 therapeutic response, measured in terms of virus dynamics, of drug treatments blocking  
320 virus replication. Clinical outcomes are known to be related to the timing of initiation of  
321 antiviral treatment in general and especially for influenza [24, 32-35], and the antiviral  
322 effects of a treatment are dependent on dose and the patients' immune system [36, 37].  
323 Thus, we studied several different scenarios in which we varied the time of treatment  
324 initiation (0.5 or 5 days from symptom onset, which were before and generally after the  
325 estimated peak viral load in our dataset) and the inhibition rate (99% or 50%). We  
326 resampled a total of 1,000 parameter sets from the estimated parameter distributions for  
327 this simulation and separated the individuals according to the value of the viral load  
328 decay rate (i.e., rapid,  $\delta > 0.953 \text{ d}^{-1}$ ; medium,  $0.658 \text{ d}^{-1} \leq \delta \leq 0.953 \text{ d}^{-1}$ , or slow,  $\delta <$

329 0.658 d<sup>-1</sup>). We found that early initiation of antiviral treatment with a high inhibition rate  
330 (i.e., 99%) immediately reduced the viral load after initiation (**Fig.2B** and **Fig.S3**).  
331 However, if the inhibition rate was low (i.e., 50%), the viral load kept increasing, and the  
332 viral load decay rate after the peak was slower or equivalent to that without treatment.  
333 This was because viral replication was not efficiently inhibited and thus it continued  
334 albeit with a lower rate even after treatment initiation and continued long after the peak.  
335 In contrast, virus dynamics was not much influenced if treatment was initiated after the  
336 peak regardless of the inhibition rate or the patient type (**Fig.3B** and **Fig.S2**), because  
337 the number of uninfected targeted cells remaining at this stage of infection is limited. It  
338 is intriguing that a weak antiviral effect was observed for patients with rapid decay even  
339 when the treatment was initiated after the peak. Because the virus is removed rapidly  
340 during the course of infection for patients with rapid decay, more uninfected cells remain  
341 compared with the other groups. Therefore, antiviral drugs can mitigate replication of  
342 the virus even when treatment is initiated after the peak to some extent. Note that these  
343 findings are not unique to SARS-CoV-2; similar findings for virus dynamics and antiviral  
344 effects have been suggested in other infectious diseases [17, 38].

345

### 346 **Observational studies for antiviral drugs cannot yield significant results owing to** 347 **heterogeneity in virus dynamics**

348 We explored why compassionate use programs do not yield significant findings  
349 when using the duration of virus shedding as an outcome. Duration of virus shedding is  
350 one of the most frequently used outcomes for assessing antiviral treatment for SARS-  
351 CoV-2 infection (**Table S1**) [4, 5, 7, 38]. The distribution of the duration of virus

352 shedding without treatment in the different virus decay groups is shown in **Fig.4A** and  
353 **Fig.S3A**. As can be expected from the difference in viral load dynamics, the duration of  
354 virus shedding without treatment is longer in the group with slow viral load decay: the  
355 averages in the groups with medium, rapid, and slow decay were 12.3 (SD: 1.06), 8.86  
356 (SD: 1.40), and 22.5 (SD: 8.15) days, respectively. As a sensitivity analysis we also  
357 computed and compared the cumulative viral load (area under the curve; AUC). We  
358 confirmed the same trend in the cumulative viral load in log scale (**Fig.S3B** and  
359 **Fig.S4A**). We further compared the outcomes under antiviral treatment (inhibition rate  
360 was set as 50% and 99%). Regardless of viral decay rate group, we consistently  
361 observed that both outcomes were improved by early treatment initiation (day 0.5) but  
362 not by late treatment initiation (day 5), as illustrated in **Fig.4B** and **Fig.S4B**.

363 If a patient possesses strong viral defenses, including immune-mediated  
364 defenses, the virus-producing cells are removed quickly, which corresponds to a shorter  
365 duration of virus production and rapid viral load decay. Indeed, the duration of virus  
366 shedding in respiratory samples has been associated with disease severity [39] and  
367 differs between symptomatic and asymptomatic cases [40]. Taken together, these  
368 findings suggest that both treatment allocation and clinical outcomes in compassionate  
369 use programs are associated with severity; thus, severity is a potential confounding  
370 variable. Further, there may be other confounding variables in the assessment of  
371 treatment efficacy in compassionate use programs; however, controlling all of them in  
372 the analysis is not possible. For example, heterogeneous immune responses, which are  
373 partially represented by the death rate of infected cells in the model, can confound the

374 inference. However, quantifying the immune response is difficult. We need to be careful  
375 when interpreting the results from compassionate use programs.

376

377 **Randomized controlled trials need to enroll patients early after symptom onset to**  
378 **observe significant antiviral effects**

379 In contrast to observational studies, randomized controlled trials may not be  
380 influenced by confounding variables and could provide valid inference. However, clinical  
381 trials for COVID-19 should consider the timing of treatment initiation in the design (i.e.,  
382 inclusion-exclusion criteria), because differences in outcomes are unlikely to be  
383 observed under late treatment initiation as we demonstrated in the previous section  
384 **(Fig.4B and Fig.S4B)**.

385 We computed the sample size needed to observe a statistically significant  
386 difference in outcomes with 80% power and a significance level of 0.05 assuming  
387 patients are randomly assigned and treated (with antiviral or placebo) immediately after  
388 hospitalization with different antiviral effect (95% and 99%) **(Fig.5A)** and with different  
389 inclusion and exclusion criteria for the timing of enrollment. We primarily used the  
390 duration of virus shedding as an outcome, but the results are qualitatively consistent for  
391 cumulative viral load as an outcome. The sample size is strongly dependent on the  
392 criterion of the timing of enrollment; that is, the sample size can be reduced if patients  
393 are enrolled early after symptom onset **(Table S4)**. The distribution of duration of virus  
394 shedding under the different criteria is shown in **Fig.5BC**. If patients are enrolled  
395 regardless of the time of treatment initiation, the sample sizes are 13,603 and 11,670  
396 per group when the inhibition rate is 95% and 99%, respectively, which is much larger

397 than the empirical sample size of the randomized controlled trials of antivirals for SARS-  
398 CoV-2 (**Table S1**). This large sample size is needed given that the treatment is initiated  
399 4.6 days after onset of symptoms on average, which is after the viral load peak. If we  
400 enroll only the patients treated within 1 day of the onset of symptoms, the sample size is  
401 reduced to 584 and 458 per group when inhibition rate is 95% and 99%, respectively.  
402 Note that antiviral drugs with a weaker inhibition rate will require larger sample sizes.  
403 The trend was similar when cumulative viral load in log scale was used as an outcome  
404 (**Table S4** and **Fig.S4CD**).

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#### 406 **Timing of randomization of clinical studies of antiviral drugs for SARS-CoV-2**

407 To validate our findings from a practical perspective, we checked the clinical  
408 trials investigating antiviral efficacy registered in ClinicalTrials.gov. As of 22 May 2020,  
409 we identified 176 clinical trials with the search terms “antiviral” and “COVID.” Among  
410 them, 46 studies did not investigate the efficacy of antiviral drugs (the effect of anti-  
411 inflammatory drugs were investigated, for example), and 20 studies did not directly  
412 investigate the efficacy of antivirals (such as vaccine studies, safety studies). Among  
413 the remaining 110 studies investigating antiviral effect, including remdesivir, chloroquine,  
414 and lopinavir/ritonavir, only 17 studies (15%) explicitly stated the time from symptom  
415 onset in the inclusion or exclusion criteria. The average time from symptom onset to  
416 randomization was 7.2 days, which our findings suggest is too late to observe a  
417 statistically significant antiviral effect with a reasonable sample size.

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## Discussion

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We explored the mechanism behind the inconsistent or null findings of clinical studies of the antiviral effect of treatments for SARS-CoV-2 infection. By fitting a conventional virus dynamics model to the longitudinal viral load data from patients with COVID-19 (without antiviral treatment), we found that there is large heterogeneity in virus dynamics, as characterized by different virus decay rates. Such heterogeneity in virus dynamics could be a confounding factor in observational studies. Subsequently, a set of randomized controlled trials were mimicked by using a version of the model with an antiviral effect. We assumed that therapy was initiated as soon as a participant was hospitalized with COVID-19 symptoms. We used a reported distribution of time delays from symptom onset to hospitalization in China to make the simulation more realistic. When we included all patients in the trial regardless of the timing of randomization and treatment initiation (1:1 allocation for treatment:placebo), we found that more than 11,000 patients per group would need to be recruited. By including only patients hospitalized within 1 day since symptom onset, the sample size is reduced to about 450 per group. Thus, we conclude that clinical trials should consider the time of treatment initiation in the study design.

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In randomized controlled trials, the calculation of sample size has been performed directly by assuming specific distributions for outcomes with a prespecified effect size [41]. However, as we demonstrated, the antiviral effect is determined not only by dose and type of drug, but also by the timing of treatment initiation and the parameters that govern the virus dynamics. Further, the association between treatment initiation and the outcome (length of viral shedding) is nonlinear; thus, our mathematical

441 model-based approach can provide a more reliable sample size than a conventional  
442 effect size-based approach.

443 We used measurements related to viral load as outcomes in this study rather  
444 than mortality. Mortality is an important and ultimate clinical outcome at both the  
445 individual and the population level. However, that does not undermine the value of  
446 outcomes related to viral load (such as the duration of virus shedding), which have a  
447 different interpretation than clinical outcome. One thing that can be captured by viral  
448 load but not by clinical outcome is potential transmissibility. From a clinical viewpoint,  
449 each drug has its purpose of use. For example, immunosuppressive agents (e.g.,  
450 dexamethasone) are expected to reduce clinical symptoms and mortality. Meanwhile,  
451 the efficacy of antiviral drugs should be evaluated primarily by using viral load. In  
452 addition, the major objective of therapy depends on the severity of disease. Lifesaving is  
453 the most important for patients with severe illness. For mild cases, physicians attempt to  
454 prevent the condition and spread of infection from getting worse by using drugs with few  
455 adverse effects. A primary endpoint should be determined on the basis of the objectives  
456 and goals of clinical trials. As most COVID-19 patients have mild to moderate disease,  
457 the duration of viral shedding would be more appropriate than mortality as a primary  
458 outcome. Indeed, many studies have used the duration of viral shedding as an outcome  
459 **(Table S1)**.

460 Regarding the association between viral load and clinical outcomes such as  
461 mortality and clinical scores, it has been observed in a number of studies that a high  
462 viral load at diagnosis is associated with severe clinical outcomes [39, 42, 43] and  
463 increased risk of mortality [44]. The data we used in this study do not contain clinical

464 outcomes, thus we cannot correlate our results with clinical outcomes. However,  
465 assuming that the viral load at diagnosis is close to the viral load at symptom onset,  
466  $V(0)$ , we did not find a significant difference in  $V(0)$  between groups. The groups we  
467 identified were characterized by a difference in the death rate of virus-producing cells  
468 which was reflected in the virus decay rate. Combining our findings with those from the  
469 literature, disease severity might not be associated with a difference in overall viral  
470 dynamics. For prognosis purposes, we need to better understand when and which  
471 biomarkers including the viral load differentiate between severe and non-severe cases.

472 The strength and uniqueness of our approach is that we accounted for virus  
473 dynamics in the assessment of antiviral effects and sample size calculations. As far as  
474 we know, considering the timing of treatment initiation in a conventional approach to  
475 sample size calculation is challenging, especially because the outcome is nonlinearly  
476 dependent on the timing of treatment initiation. Even if it is technically possible, the data  
477 including the timing of treatment initiation would be limited or small. We used clinical  
478 data from SARS-CoV-2-infected patients for the simulation. Thus, our numerical results  
479 are realistic and directly interpretable for drug development for SARS-CoV-2. In other  
480 words, our approach is flexible and can be applied to other antiviral drugs for other  
481 diseases by replacing the dataset.

482 There are several limitations in our approach. First, our within-host virus  
483 dynamics model does not fully reflect the detailed physiological processes of virus  
484 replication of SARS-CoV-2. For example, our mathematical model assumed target cells  
485 are a homogeneous population (i.e., single-target cell compartment). The susceptibility  
486 of target cells for SARS-CoV-2 infection is, however, dependent on expression levels of

487 its receptor, angiotensin converting enzyme 2 (ACE2) [45], and therefore susceptibility  
488 to infection might be heterogeneous (i.e., multi-target cell compartments) even in the  
489 same organ. However, the virus dynamics of our model and that of a model with multi-  
490 target cell compartments may not differ substantially unless a large fraction of the total  
491 target cells in the modified model remain uninfected around peak viral load. Another  
492 modelling limitation is that possible immunomodulation induced by treatment was not  
493 modelled. That is, if anti-SARS-CoV-2 drugs induce immunomodulation as bystander  
494 effects, late initiation of treatments might still have the potential to reduce viral load,  
495 which is not reflected in our model [24]. We further compared the results of the model  
496 we used in this study with two other extended models, which have been used to  
497 describe virus dynamics of SARS-CoV-2 and other viruses, to check whether our model  
498 is appropriate: one included the effect of interferons produced by infected cells [46] and  
499 the other included the eclipse phase of infection [46, 47]. We fit these models to the  
500 data and used model selection theory to compare the models based on the Bayesian  
501 information criteria (BIC) and corrected Bayesian information criteria (BICc). BIC and  
502 BICc among the three models were comparable. In addition, given limited data (i.e.,  
503 only viral load data were available), we believe using a minimal model is appropriate at  
504 this stage of knowledge. At such time that further data and appropriate scientific  
505 information about infection dynamics becomes available, more complex models may be  
506 able to capture additional details of within-host viral dynamics. Second, we did not use  
507 viral load data under treatment to evaluate our model because such data were not  
508 sufficiently available. Estimating antiviral effects from such data and using that in the

509 sample size calculation would strengthen our approach, but we need to wait until such  
510 data are accumulated.

511 Future study should include development of a similar sample size calculation  
512 framework for different types of antiviral treatment. Although we focused on drugs  
513 inhibiting virus replication, there are different classes of drugs such as viral entry  
514 inhibitors (e.g., hydroxychloroquine and camostat) and immunomodulators (e.g.,  
515 interferon and the related agents) [48].

516 Along with vaccines, developing effective antiviral drugs is urgently needed. At  
517 present, most of the randomized controlled trials have failed to identify effective antiviral  
518 agents against SARS-CoV-2. However, this might not be because the antiviral drugs  
519 are not effective, but because of imperfect design of the clinical studies. The timing of  
520 treatment initiation and virus dynamics should be accounted for in the study design (i.e.,  
521 sample size and inclusion-exclusion criteria). We further believe our approach is  
522 informative for determining treatment strategy in clinical settings.

523

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- 716

717 **Supporting information**

718 Supplementary Text

719 Figures S1-S4

720 Tables S1-S4

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## Figures

**Fig. 1. Observed and fitted viral load data for individual patients.** Viral loads were measured using nasal swabs (China), pharyngeal swabs (Germany), and nasopharyngeal swabs (Singapore and France) for hospitalized SARS-CoV-2-infected patients. Note that the detection limits of the PCR assay for SARS-CoV-2 were 68.0 copies/ml (Singapore and Korea) 15.3 copies/ml (China) and 33.3 copies/ml (Germany), respectively, and are shown as dotted horizontal lines. The closed dots and curves correspond to the observed and the estimated viral load for each patient using their individual parameters given in **Table S2**, respectively. Shaded regions correspond to 95% predictive intervals. Different colors of the dots and the lines (light blue, black, and pink) correspond to the three different types of patients characterized by rapid, medium, and slow viral load decay, respectively. The red dots represent the data at or under the detection limit regardless of the group. Patient IDs are the same as in the original papers if available.

**Fig. 2. Characterizing and clustering COVID-19 patients using viral load data.** (A) Schematic illustration for data fitting with a virus dynamics model. Longitudinal SARS-CoV-2 RNA load data (i.e., clinical data) were extracted from published papers. The data were analyzed by the mathematical model, and then virus dynamics parameters were estimated for each patient (i.e., characterizing). Daily viral load since symptom onset for each patient was simulated by running the model with the estimated parameters. (B) Clustering patients using daily viral load. Daily viral load obtained through simulation was used for clustering of the 30 patients. In the dendrogram, the height from the bottom to the point where two or more patients are joined indicates the

745 distance (i.e., dissimilarity) between patients. For example, “Singapore 11” and  
746 “Germany 2” are very close and those are far from “Singapore 6.” As a result, three  
747 different patient groups were identified and “China O” was detected as an outlier. The  
748 heatmap next to the dendrogram (“Virus dynamics parameters”) shows the estimated  
749 parameters and initial condition  $(\gamma, \beta, V(0), \delta)$  for each patient. Light blue and pink  
750 correspond to high and low values, respectively. Statistically significant between-group  
751 differences were found in the maximum rate constant for viral replication,  $\gamma$  (ANOVA p-  
752 value:  $3.61 \times 10^{-3}$ ), and the death rate of virus-producing cells,  $\delta$  (ANOVA p-value:  
753  $3.23 \times 10^{-13}$ ), moreover there were statistical differences between all pair groups for  $\delta$ .  
754 The death rate is highlighted by the dotted square. The right heatmap shows the daily  
755 viral load for each patient. Green and purple correspond to high and low values,  
756 respectively. “Group 1” maintained a high viral load for a longer period compared with  
757 the other groups.

758 **Fig. 3. Patient variability and difference in therapeutic response.** (A) Viral load  
759 trajectories since symptom onset for the three groups (black: medium decay group, light  
760 blue: rapid decay group, pink: slow decay group) obtained through simulation (without  
761 antiviral treatment). (B) Viral load trajectories since symptom onset for the three groups  
762 under antiviral treatment with different inhibition rates and different timing of treatment  
763 initiation. The left three panels are viral load trajectories when the treatment is initiated  
764 at 0.5 days (“Early initiation”) since symptom onset. The right three panels are viral load  
765 trajectories when treatment is initiated at 5 days (“Late initiation”) since symptom onset.  
766 Blue and red dotted lines correspond to the trajectories with 50% and 99% inhibition

767 rate, respectively. The bolded lines are the trajectory without treatment shown for  
768 comparison. The dotted horizontal lines are the detection limit (D.L.).

769 **Fig. 4. Duration of virus shedding in the three different groups.** (A) The relative  
770 density distributions of duration of virus shedding since symptom onset for the three  
771 groups (light pink: medium decay group, light blue: rapid decay group, pink: slow decay  
772 group) without treatment obtained through simulation. (B) The relative density  
773 distributions of duration of virus shedding since symptom onset for the three groups  
774 under antiviral treatment with different inhibition rates and different timing of treatment  
775 initiation. The left three panels are when antiviral treatment is initiated at 0.5 days  
776 (“Early initiation”) since symptom onset. The red dotted line corresponds to the  
777 distribution with a 99% inhibition rate. The distribution without treatment is shown in the  
778 back for comparison. The right three panels are when antiviral treatment is initiated at 5  
779 days (“Late initiation”) since symptom onset. The distributions are represented as  
780 ‘relative density’ to reflect different proportions of the three groups.

781 **Fig. 5. Simulation mimicking randomized controlled trial for anti-SARS-CoV-2.** (A)  
782 Schematic illustration for the simulation mimicking randomized controlled trials for  
783 antiviral drugs. 20,000 parameter sets were sampled from the estimated parameter  
784 distributions. The parameter sets were randomized into control (“No treatment”, 10,000  
785 individuals in total) or treatment (“Anti-SARS-CoV-2 treatment”, 10,000 individuals in  
786 total) groups. For the treatment group, the treatment is initiated randomly to reflect the  
787 delay of treatment initiation since symptom onset. We have also used a truncated  
788 distribution (red area) to mimic the randomized controlled trials including only patients  
789 recruited and treated early (“Early initiation”). Then the outcomes (duration of virus

790 shedding and the cumulative viral load in log scale) were calculated for each patient. (B)  
791 The distributions of duration of virus shedding for patients without and with treatment  
792 are shown in black and red curves, respectively. For antiviral treatment, a 99% inhibition  
793 rate of virus replication was assumed. The red dotted curve is when all patients are  
794 included regardless of the timing of recruitment and treatment initiation. The red dashed  
795 curve is the case when only patients recruited and treated within 0.5 days since  
796 symptom onset are included. (C) Means and standard deviation of the duration of virus  
797 shedding under different inclusion criteria (not treated, included regardless of the timing  
798 of recruitment and treatment initiation, early treatment initiation [within 0.5, 1, 2, 3, 4,  
799 days since symptom onset]) are shown.

## Supporting information for

### **Detection of significant antiviral drug effects on COVID-19 with reasonable sample sizes in randomized controlled trials: a modeling study combined with clinical data**

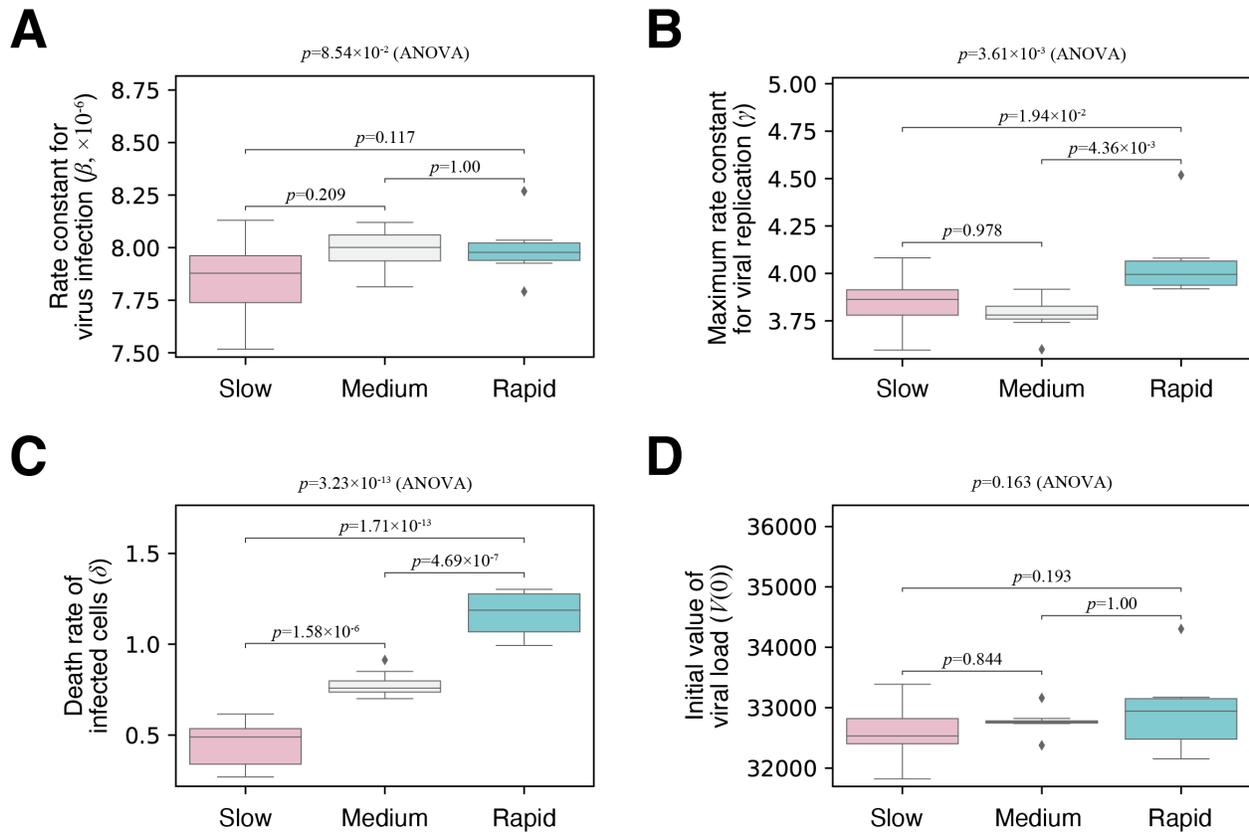
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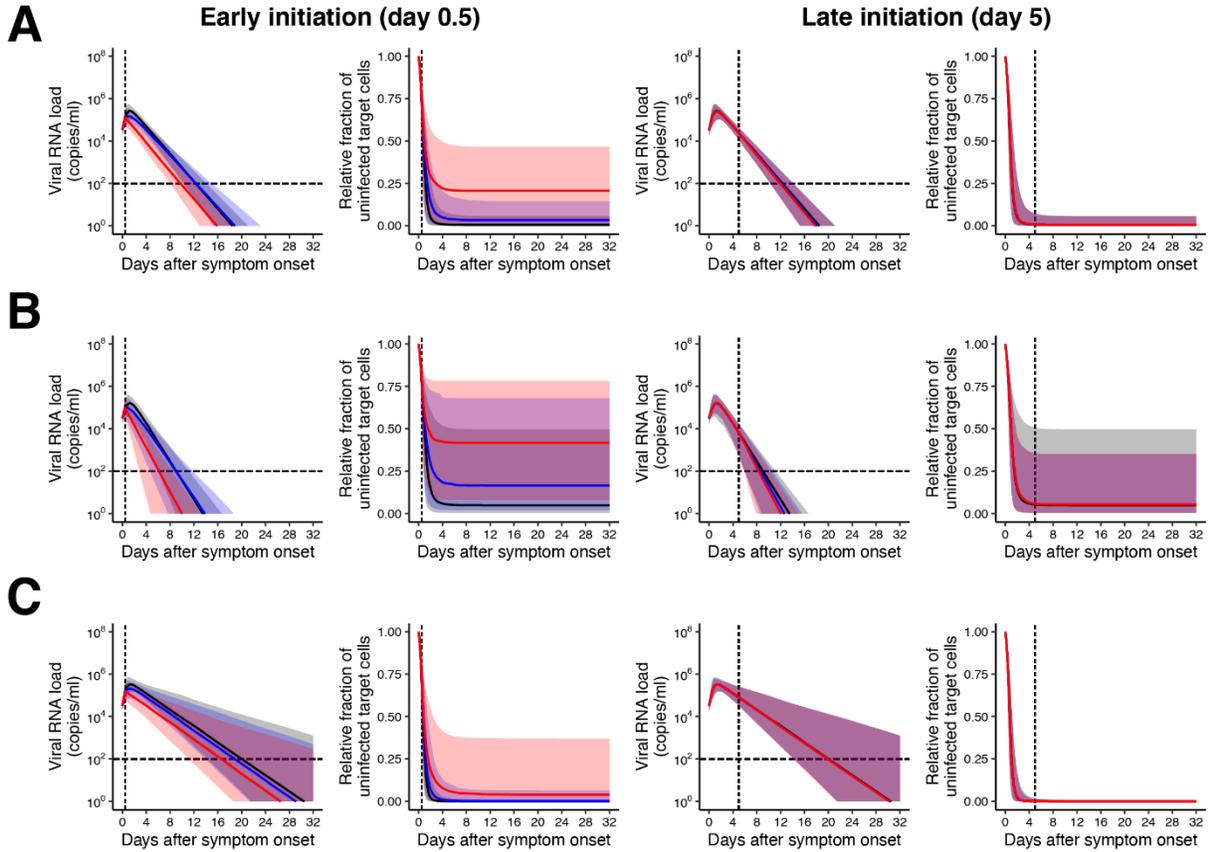
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Figs. S1 to S4

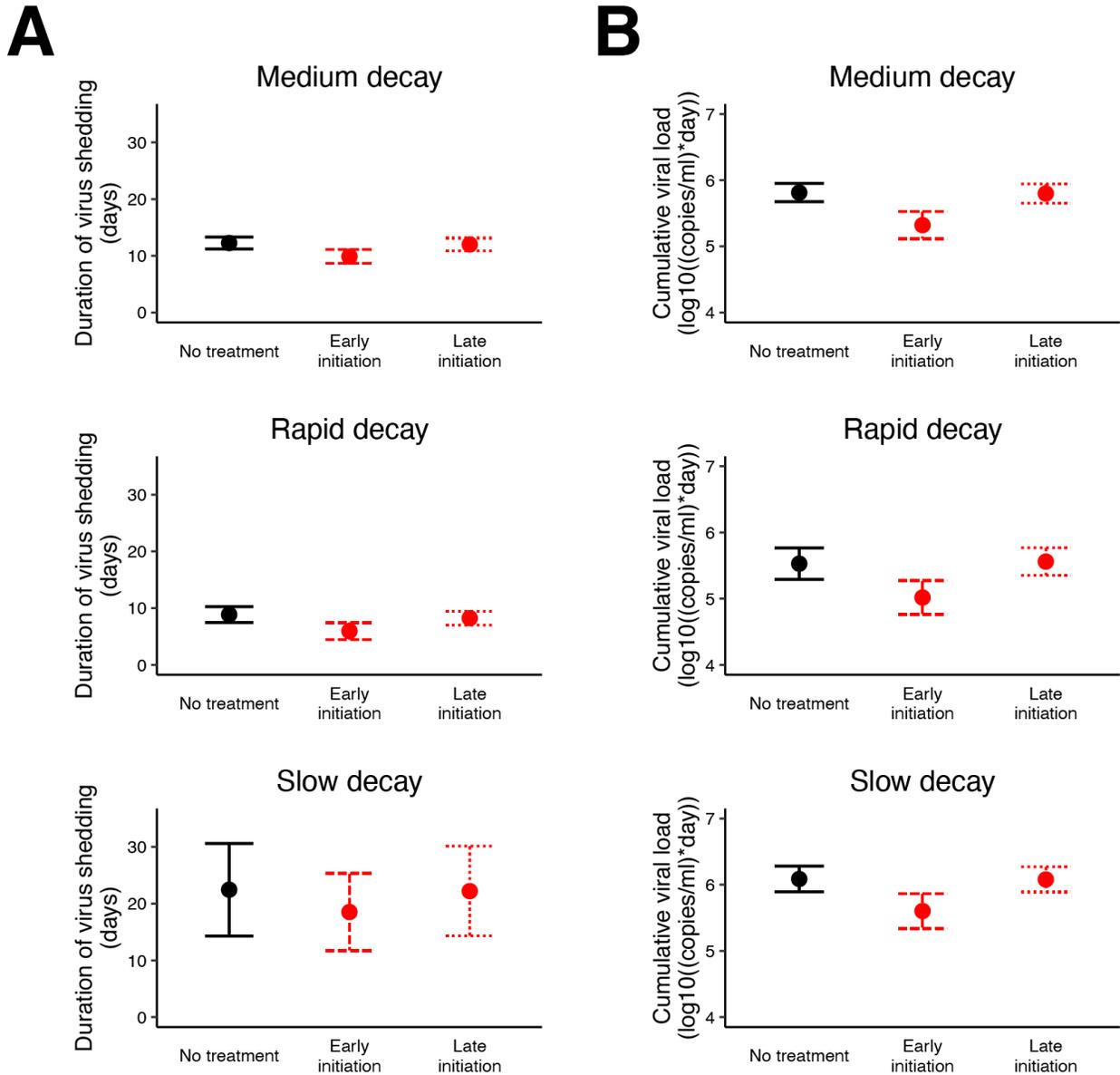
Tables S1 to S4



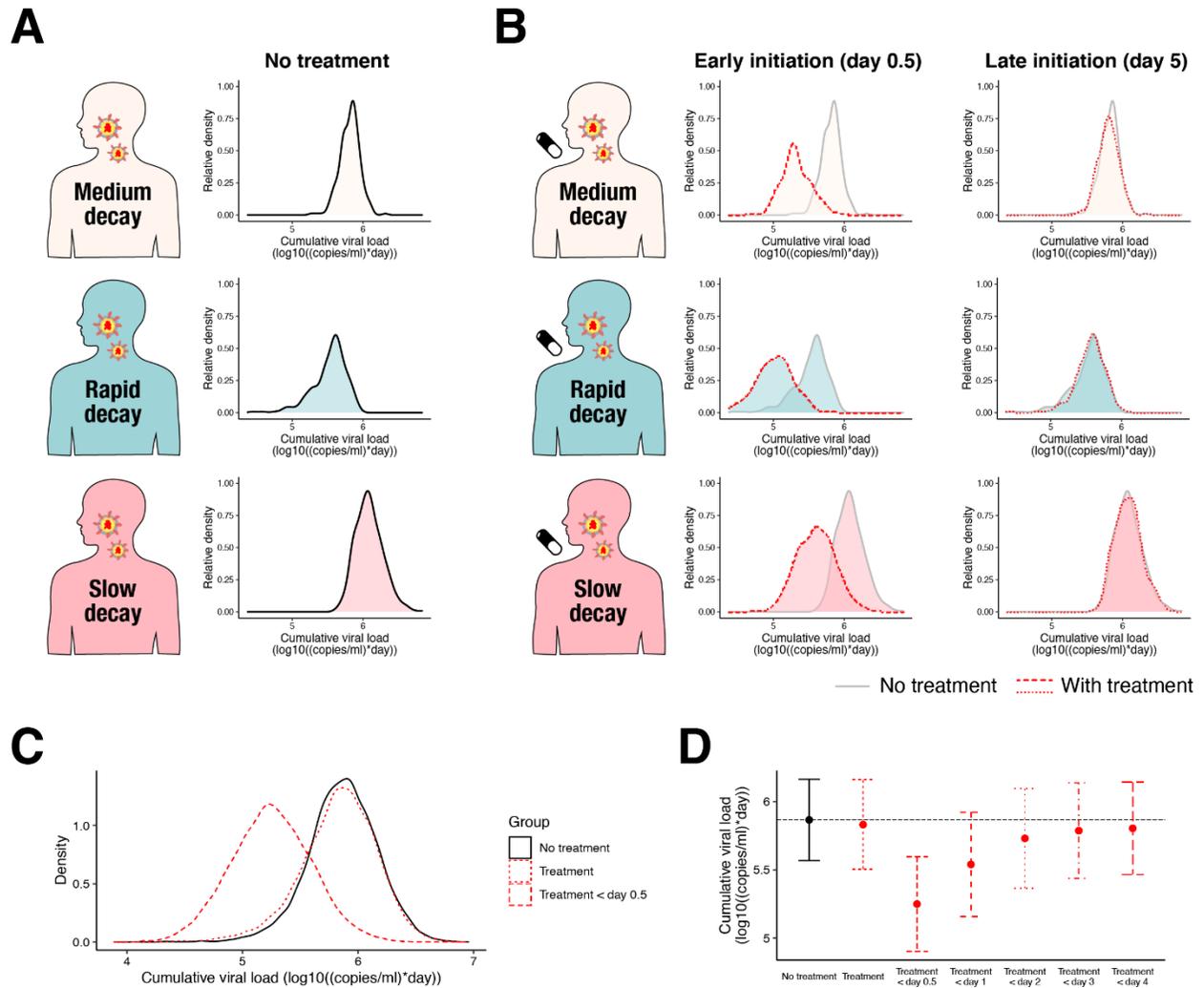
**Fig. S1. Estimated parameters of the mathematical model in the three different viral load decay groups.** Boxplots of estimates of (A) the rate constant for virus infection,  $\beta$ ; (B) the maximum rate constant for viral replication,  $\gamma$ ; (C) the death rate of virus-producing cells,  $\delta$ ; and (D) viral load at symptom onset,  $V(0)$ , respectively. Estimated parameter distributions between the three groups with different viral load dynamics (slow, medium, and rapid viral load decay groups) were compared by ANOVA. Pairwise comparison was subsequently performed using Student's  $t$  test. The  $p$ -values of the pairwise Student's  $t$  test were adjusted by the Bonferroni correction.



**Fig. S2. Expected virus dynamics under an antiviral treatment blocking viral replication.** The antiviral treatment was assumed to be initiated after 0.5 or 5 days (named early and late initiations, respectively) from symptom onset with 99% and 50% inhibition rates (named high and low antiviral effects, respectively) for patients with (A) medium, (B) rapid, and (C) slow viral load decay. Left and right panels in each group show the viral loads,  $V(t)$ , and the relative fraction of uninfected target cells,  $f(t)$ . The black and colored solid lines correspond to the mean of the values without and with the therapies (red: high, blue: low antiviral effects), respectively. The shadowed regions correspond to the 95% predictive intervals.



**Fig. S3. Distribution of duration of virus shedding and cumulative viral load.** (A) Duration of virus shedding and (B) cumulative viral load of SARS-CoV-2 for different types of patients (medium, rapid, and slow decay) with and without treatment. 'Early initiation' and 'Late initiation' means the early and the late treatment initiation (0.5 or 5 days after symptom onset). The dots and error bars represent the mean and the standard deviation.



**Fig. S4. Cumulative viral load in the three different groups.** (A) The relative density distributions of cumulative viral load for the three groups (light pink: medium decay group, light blue: rapid decay group, pink: slow decay group) without treatment obtained through simulation. (B) The relative density distributions of cumulative viral load (in log scale) for the three groups under antiviral treatment with different inhibition rate and different timing of treatment initiation. The left three panels are when antiviral treatment is initiated at 0.5 days (“Early initiation”) since symptom onset. The red dotted line corresponds to the distribution with 99% inhibition rate. The distribution without treatment is shown in the back for comparison. The right three panels are when antiviral treatment is initiated at 5 days (“Late initiation”) since symptom onset. The distributions are represented as ‘relative density’ to reflect different proportions of the three groups. (C) The distributions of cumulative viral load for patients without and with treatment are shown in black and red curves, respectively. The red dotted curve is when all patients are included regardless of the timing of recruiting and treatment initiation. The red dashed curve is the case for patients who were recruited and who received treatment

within 0.5 days since symptom onset only. (D) Means and standard deviation of the cumulative viral load under different inclusion criteria (not treated, included regardless of the timing of recruiting and treatment initiation, early treatment initiation [within 0.5, 1, 2, 3, 4 days since symptom onset]) are shown.

**Table S1. Summary of clinical trials for antiviral drugs for SARS-CoV-2:** The current major clinical studies for antiviral treatment of SARS-CoV-2 were investigated and their information were summarized on 22 May 2020.

Treatment	Study design <sup>\$</sup>	Timing of initiation since onset (days)	Sample size (control/treatment)	Primary outcome*	Effective <sup>#</sup>	Reference	Peer-reviewed
Lopinavir/ritonavir	RCT	13 (IQR: 11-16)	99/100	1	No	(1)	Yes
Remdesivir	RCT	10 (IQR: 9-12)	79/158	1	No	(2)	Yes
Remdesivir	RCT	9 (IQR: 6-12)	521/538	1	Yes	(3)	Yes
Hydroxychloroquine	RCT	Not reported	31/31	1	Yes	(4)	No
Hydroxychloroquine	RCT	16.6 (SD: 10.5)	75/75	2	No	(5)	Yes
Lopinavir/ritonavir	RCT	3.5 (IQR: 2-6)	17/34	2	No	(6)	No
Arbidol	RCT	6 (IQR: 2-8)	17/35	2	No	(6)	No
Remdesivir	OS	12 (IQR: 9-15)	53	1,3	-	(7)	Yes
Hydroxychloroquine	OS	4.1 (SD: 2.6)	16/20	2	Yes	(8)	Yes
Hydroxychloroquine	OS	Not reported	565/811	1,3	No	(9)	Yes
Hydroxychloroquine and azithromycin	OS	4.9 (SD: 3.6)	80	1,2	-	(10)	Yes
Meplazumab	OS	Not reported	11/17	2	Yes	(11)	No

<sup>\$</sup> RCT: randomized control trial, OS: observational study

\* 1. Clinical improvement/recovery, 2. Duration of virus shedding, 3. Mortality.

<sup>#</sup> Whether the primary outcome is statistically significantly different between control and treatment group. ‘-’ denotes no statistical test was performed because it is a single-arm study (i.e., no control group).

**Table S2. Estimated parameters for each patient (mode and 95% credible intervals):** The conditional modes of the individual parameters for each patient were estimated as Empirical Bayes Estimates and summarized. The patient type was based on the three groups identified by hierarchical clustering of the reconstructed daily viral load data.

Patient ID	$\gamma$ (day <sup>-1</sup> )	$\beta$ ((RNA copies/ml) <sup>-1</sup> day <sup>-1</sup> )	$\delta$ (day <sup>-1</sup> )	$V(0)$ (RNA copies/ml)	Patient type
<b>Germany</b>					
1	3.74 (2.25 – 5.99)	8.12 (5.48 – 11.2)× 10 <sup>-6</sup>	0.75 (0.68 – 0.93)	3.32 (1.84 – 5.70)× 10 <sup>4</sup>	Medium
2	4.05 (2.81 – 5.97)	7.79 (5.95 – 10.2)× 10 <sup>-6</sup>	1.08 (0.88 – 1.34)	3.23 (1.71 – 4.66)× 10 <sup>4</sup>	Rapid
3	3.92 (1.89 – 6.35)	8.27 (6.08 – 10.9)× 10 <sup>-6</sup>	1.30 (1.07 – 2.06)	3.43 (1.89 – 5.44)× 10 <sup>4</sup>	Rapid
4	4.08 (2.80 – 6.05)	7.93 (6.07 – 10.3)× 10 <sup>-6</sup>	1.27 (0.99 – 1.92)	3.31 (2.07 – 6.37)× 10 <sup>4</sup>	Rapid
7	3.92 (2.45 – 5.36)	7.81 (5.82 – 11.2)× 10 <sup>-7</sup>	0.91 (0.80 – 1.29)	3.28 (1.65 – 5.27)× 10 <sup>4</sup>	Medium
8	3.77 (2.34 – 5.64)	8.04 (5.57 – 10.9)× 10 <sup>-6</sup>	0.75 (0.67 – 0.84)	3.28 (1.95 – 5.82)× 10 <sup>4</sup>	Medium
10	3.90 (2.59 – 5.85)	7.74 (5.60 – 11.4)× 10 <sup>-7</sup>	0.49 (0.46 – 0.55)	3.18 (1.75 – 6.22)× 10 <sup>4</sup>	Slow
14	4.06 (2.97 – 6.17)	7.95 (5.89 – 11.1)× 10 <sup>-6</sup>	1.28 (1.02 – 1.75)	3.28 (1.95 – 5.82)× 10 <sup>4</sup>	Rapid
<b>Korea</b>					
13	3.93 (2.39 – 6.18)	8.02 (5.89 – 10.4)× 10 <sup>-6</sup>	0.99 (0.79 – 1.36)	3.31 (1.58 – 5.97)× 10 <sup>4</sup>	Rapid
15	3.91 (2.13 – 6.10)	7.83 (5.80 – 11.1)× 10 <sup>-7</sup>	0.78 (0.55 – 0.93)	3.24 (1.94 – 6.09)× 10 <sup>4</sup>	Medium
<b>Singapore</b>					
2	3.78 (2.47 – 6.02)	7.96 (6.15 – 10.6)× 10 <sup>-6</sup>	0.61 (0.51 – 0.68)	3.26 (1.83 – 5.90)× 10 <sup>4</sup>	Slow
3	4.00 (2.75 – 6.36)	7.74 (5.77 – 10.4)× 10 <sup>-6</sup>	0.33 (0.24 – 0.38)	3.26 (1.93 – 5.62)× 10 <sup>4</sup>	Slow
4	3.83 (2.24 – 6.46)	7.88 (6.00 – 10.5)× 10 <sup>-6</sup>	0.62 (0.47 – 0.69)	3.25 (1.82 – 5.46)× 10 <sup>4</sup>	Slow
6	3.86 (2.42 – 6.43)	7.93 (5.47 – 11.0)× 10 <sup>-6</sup>	0.37 (0.26 – 0.43)	3.28 (2.01 – 6.64)× 10 <sup>4</sup>	Slow
8	3.76 (2.45 – 5.87)	8.04 (6.01 – 10.3)× 10 <sup>-6</sup>	0.41 (0.35 – 0.45)	3.34 (1.63 – 6.28)× 10 <sup>4</sup>	Slow
9	3.60 (2.39 – 4.94)	8.13 (6.00 – 10.5)× 10 <sup>-6</sup>	0.27 (0.22 – 0.31)	3.28 (1.61 – 5.53)× 10 <sup>4</sup>	Slow
11	3.94 (2.35 – 6.19)	8.04 (6.58 – 11.2)× 10 <sup>-6</sup>	1.14 (0.90 – 1.76)	3.32 (1.74 – 6.53)× 10 <sup>4</sup>	Rapid
12	3.77 (2.05 – 5.98)	8.02 (5.79 – 11.3)× 10 <sup>-6</sup>	0.70 (0.59 – 0.84)	3.28 (1.85 – 6.41)× 10 <sup>4</sup>	Medium
14	4.03 (2.21 – 7.06)	7.52 (5.47 – 10.6)× 10 <sup>-6</sup>	0.56 (0.45 – 0.66)	3.22 (1.90 – 6.19)× 10 <sup>4</sup>	Slow
16	3.85 (2.20 – 6.35)	7.88 (6.04 – 11.6)× 10 <sup>-6</sup>	0.46 (0.30 – 0.63)	3.25 (1.64 – 5.59)× 10 <sup>4</sup>	Slow
17	3.60 (2.19 – 5.76)	8.11 (5.79 – 10.6)× 10 <sup>-6</sup>	0.85 (0.57 – 1.25)	3.28 (1.71 – 5.70)× 10 <sup>4</sup>	Medium
18	3.63 (1.82 – 6.45)	8.07 (6.23 – 11.3)× 10 <sup>-6</sup>	0.34 (0.26 – 0.38)	3.28 (1.91 – 6.14)× 10 <sup>4</sup>	Slow
<b>China</b>					

C	3.80 (2.21 – 6.36)	7.97 (6.12 – 10.5)× 10 <sup>-6</sup>	0.77 (0.33 – 1.18)	3.27 (1.73 – 5.77)× 10 <sup>4</sup>	Medium
D	3.91 (2.13 – 6.44)	7.80 (5.76 – 11.0)× 10 <sup>-6</sup>	0.53 (0.22 – 1.14)	3.19 (1.98 – 6.06)× 10 <sup>4</sup>	Slow
E	3.79 (1.97 – 5.66)	7.98 (6.00 – 11.4)× 10 <sup>-6</sup>	0.70 (0.35 – 0.97)	3.27(1.60 – 5.48)× 10 <sup>4</sup>	Medium
H	4.52 (2.42 – 5.88)	8.01 (5.84 – 10.9)× 10 <sup>-6</sup>	1.23 (0.57 – 2.10)	3.22 (2.01 – 5.52)× 10 <sup>4</sup>	Rapid
I	4.08 (2.40 – 6.74)	7.67 (5.34 – 10.1)× 10 <sup>-6</sup>	0.30 (0.16 – 0.43)	3.25 (1.38 – 5.87)× 10 <sup>4</sup>	Slow
L	3.89 (2.30 – 5.82)	7.82 (5.78 – 10.4)× 10 <sup>-6</sup>	0.54 (0.21 – 0.94)	3.24 (1.80 – 6.09)× 10 <sup>4</sup>	Slow
O	5.62 (2.70 – 7.00)	8.70 (6.20 – 11.4)× 10 <sup>-6</sup>	2.29 (1.36 – 4.26)	3.64 (2.18 – 7.07)× 10 <sup>4</sup>	Outlier
T	3.94 (2.38 – 5.96)	7.94 (5.66 – 10.5)× 10 <sup>-6</sup>	1.02 (0.68 – 1.72)	3.25 (1.77 – 6.08)× 10 <sup>4</sup>	Rapid

**Table S3. Description of variables, parameters, and estimated parameter values:** The fixed effect and random effect for each parameter were estimated by a non-linear mixed effect model and the estimates and standard errors were summarized.

Variables or parameters	Description	Unit	$\vartheta$ : Fixed effect (SE)*	$\Omega$ : SD of random effect (SE)*
$f(t)$	Relative fraction of uninfected target cells at time $t$ to those at time 0	Unitless (fraction)	---	---
$V(t)$	Amount of virus at time $t$	RNA copies/ml	---	---
$\beta$	Rate constant for virus infection	(RNA copies/ml) <sup>-1</sup> day <sup>-1</sup>	$7.95 \times 10^{-6}$ ( $1.49 \times 10^{-6}$ )	0.16 (0.24)
$\gamma$	Maximum rate constant for viral replication	Day <sup>-1</sup>	3.80 (1.95)	0.27 (0.28)
$\delta$	Death rate of virus-producing cells	Day <sup>-1</sup>	0.68 (0.09)	0.56 (0.09)
$V(0)$	Amount of virus at time 0 (symptom onset)	RNA copies/ml	$3.27 \times 10^4$ ( $1.04 \times 10^4$ )	0.32 (0.25)

\* The parameter for patient  $k$ ,  $\vartheta_i (= \vartheta \times e^{\pi_k})$  is represented as a product of  $\vartheta$  (a fixed effect) and  $e^{\pi_k}$  (a random effect).  $\pi_k$  follows the normal distribution with mean 0 and standard deviation  $\Omega$ .

**Table S4. Sample size (per group) under different inclusion criteria**

Outcome	Inhibition rate	All patients (no inclusion criteria)	Patients treated within "X days" from the onset of symptoms				
			0.5 days	1 days	2 days	3 days	4 days
Duration of virus shedding	95%	13603	249	584	1717	4556	3200
	99%	11670	166	458	1462	3837	2840
Cumulative viral load	95%	2811	12	40	209	583	915
	99%	2554	11	37	192	533	836

## Reference and Notes

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