

Functional Materials and Devices by Self-Assembly

Dmitri V. Talapin,^{1,2} Michael Engel³ and Paul Braun⁴⁻⁷

¹ Department of Chemistry, James Franck Institute, University of Chicago, Chicago, Illinois 60637, United States

² Center for Nanoscale Materials, Argonne National Laboratory, Argonne, Illinois 60439, United States

³ Institute for Multiscale Simulation, IZNF, Friedrich-Alexander University Erlangen-Nürnberg, 91058 Erlangen, Germany

⁴ Department of Materials Science and Engineering, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, United States

⁵ Department of Chemistry, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, United States

⁶ Materials Research Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, United States

⁷ Beckman Institute for Advanced Science and Technology, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, United States

Abstract

The field of self-assembly moved far beyond early work, where the focus was primarily the resultant beautiful two- and three-dimensional structures, to a focus on forming materials and devices with important properties either otherwise not available, or only available at great cost. Over the last few years, materials with unprecedented electronic, photonic, energy storage, and chemical separation functionalities were created with self-assembly, while at the same time the ability of the field to form even more complex structures in two and three dimensions has only continued to advance. Self-assembly crosscuts all areas of materials. Functional structures have now been realized in polymer, ceramic, metallic, and semiconducting systems, as well as composites containing multiple classes of materials. As the field of self-assembly continues to advance, the number of highly functional systems will only continue to grow and make increasingly greater impacts in both the consumer and industrial space.

Main text

For a century, the atom has been the building block of chemistry. Small atomic assemblies, aka molecules, remain the most fundamental and important concept in chemistry.¹ However, organized structures can form spontaneously not only from atoms but from various other types of building blocks. This process called “self-assembly” allows expanding and generalizing the concepts of bottom-up design and synthesis of structures, materials and devices. Self-assembly creates an opportunity to develop new paradigms for chemistry and material science, where various, typically nanometer sized, objects with precisely engineered sizes, shapes, compositions, and concomitant properties serve as “meta-atoms” or superatomic building blocks for hierarchically assembled materials and devices. Just as atoms combine to form molecules with dramatically different properties than the atomic constituents, self-assembly of “meta-atoms” can create “meta-molecules”, “meta-crystals” and so on. Ultimately, self-assembly should contribute to the development and manufacturing of materials and devices for real-world applications (Figure 1). This issue of MRS Bulletin discusses examples of the successful adaption of self-assembly principles to the needs of electronics,[REF] photonics,[REF] energy storage,[REF] chemical separations,[REF] and complex structure formation.[REF] Self-assembly also plays a central role in biological systems and living organisms. These strong conceptual ties between self-assembly and biology open a wide design space for bio-mimetic materials.

What is self-assembly good for? Self-assembly adds several unique features to our existing toolset of chemical and physical methods for synthesis and processing of functional materials. First, self-assembly allows making materials with structural features on the length scales of several nanometers, in not only two dimensions, but also in three dimensions, which is too large for traditional (atom-by-atom) chemical synthesis but too small to be efficiently approached by top-down techniques, such as photolithography (Figure 2a). Self-assembly is also particularly useful to synthesize hierarchically organized materials with structures independently engineered on different scales. For example, a variety of macromolecules containing two or more covalently bonded blocks of different polymers can be prepared by conventional chemical synthesis. These block-copolymers spontaneously self-assemble into ordered structures with ~10 nm features (Figure 2b). The type of self-assembling structure and feature size can be rationally engineered by

controlling the block size of individual molecules.² A similar hierarchical design is achieved for nanocrystal solids that can be engineered at the level of individual nanocrystals and then self-assembled into superlattices with the structure of glasses, crystalline solids or quasicrystals (Figure 1).³

Different approaches to classify self-assembly phenomena. Self-assembly is a unifying umbrella for a broad range of effects observed in different materials, and there are several excellent reviews discussing self-assembly on molecular, nano-, micro- and macroscopic length scales.²⁻⁶ Self-assembly is observed on hard condensed matter systems, such as epitaxial semiconductor quantum dots formed by strain-guided Stranski-Krastanov growth⁷ and template-direct eutectics.⁸ There are many examples of self-assembled soft-matter systems, with block-copolymers^{2, 5} and DNA origami⁹⁻¹⁰ as famous examples. Finally, the hybrid systems incorporating hard and soft components, such as colloidally synthesized inorganic nanocrystals with organic capping ligands,³ combine the advantages of hard and soft components within the same material.

Given the breadth of self-assembly phenomena and materials systems, the classification of these effects can be approached from different angles. Thus, we distinguish equilibrium or *static* and non-equilibrium or *dynamic* self-assembly. In the former case, the ordered structures form when system spontaneously evolves toward the global or local minimum of free energy. The organized structures represent equilibrium states and, once formed, remain stable. The assembly process is controlled by the free energy landscape. This landscape can be modified, e.g., by applying external fields, temperature gradients, and other stimuli to drive assembly toward a particular outcome. These approaches often come under the name of “directed self-assembly”. In dynamic self-assembly, structures or patterns form away from equilibrium.¹¹ Such patterns require continuous energy input and disappear in the absence of an external drive. Oscillatory chemical reactions, e.g., the Belousov–Zhabotinsky reaction,¹² are simple examples of non-equilibrium self-assembly. The biological systems represent much more complex networks of dynamic assembly.

Generally, self-assembly is associated with noncovalent interactions, such as van der Waals forces, long-ranged electrostatic and magnetic interactions, hydrogen bonding, etc. These “weak” forces are favorable for reversible interactions between macromolecular or particle building units, where reversibility is required for healing incorrect bonds and growing ordered domains.¹³ From

the big-picture view, equilibrium self-assembly can be described using established theoretical frameworks of nucleation and growth.³ However, when the assembling blocks are larger than atoms and small molecules, the interactions can be much more complex than interatomic forces. Moreover, the interactions can be rationally engineered in terms of magnitude, range and specificity.

One can roughly define three categories of such interactions (Figure 3). In the first category, the local assembly rules are binary like-dislike type interactions, e.g., between hydrophobic and hydrophilic domains of a polymer backbone.⁵ Even these simple interactions, combined with precise control over size and shape of assembling units, can lead to very complex structures.

The next level of complexity and engineerability is achieved when the building blocks exhibit highly specific interactions with respect to each other. The best examples come from biology, with DNA being the most famous molecule capable to exchange information *via* local intermolecular interactions. In manmade materials, this concept laid the foundation for the field of DNA nanotechnology.¹⁴ Highly specific site recognition has been implemented in metal-organic frameworks,¹⁵ colloidal systems,¹⁶⁻¹⁷ and is widely used in drug development.

Finally, complex ordered structures can form spontaneously even in the absence of any local attractive or repulsive forces between assembling units. This case can be demonstrated using hard colloidal spheres that do not experience any interactions except bumping into each other. In a concentrated solution, these spheres spontaneously self-organize into long-range ordered domains.¹⁸ Counterintuitively, it is a system's entropy that organizes hard spheres into an *fcc* crystal.³ Very complex structures emerge when using non-spherical particles and when hard spheres of two different sizes are mixed together.¹⁹⁻²⁰

Theoretical and computational insights in self-assembly. Self-assembly processes of nanoscale building blocks are founded on statistical mechanics. Modeling is best accomplished with computer simulation. There are three closely related challenges: (i) handling a vast number of degrees of freedom, (ii) accurate representation of microscopic interactions, and (iii) following the evolution of the system for sufficiently long times. It is impossible to tackle all challenges at once,

which is why a range of strategies have been developed, each with strengths and weaknesses and each at different level of spatial and temporal coarse-graining resolution (Figure 4).

It is rarely necessary to include quantum mechanical effects explicitly in the modeling process to study self-assembly. But quantum effects can become relevant when analyzing physical and chemical properties of the final self-assembled material. *Ab initio* quantum chemistry methods can assist parametrization of coarser simulations with classical force fields, which foremost must reproduce van der Waals force accurately as those are often difficult to estimate and most crucial for self-assembly. All-atom simulations are best suited to resolve molecular processes where individual atoms are essential,²¹ like conformation changes, quantum dots, crystallization,²² or at interfaces. The number of atoms attainable in all-atom simulations reaches a practical limit already for systems containing only a small number of 10 nm nanoparticles. To go beyond, the number of degrees of freedom must be reduced.

It is common to search for a good compromise between accuracy and simplicity in computational models. A united-atom ansatz (or similar levels of coarse-graining) is the method of choice if molecular flexibility is important. Groups of atoms or small parts of molecules are combined into simple spherical beads that interact over short distances. Mesophase formation of block-copolymers,²³ DNA hybridization and origami,²⁴ self-assembled monolayers,²⁵ and ligand shells²⁶⁻²⁷ have been successfully modeled in this way.

In the case of rigid macromolecular or nanoparticle building blocks it has proven most efficient to represent the complete building block by a single simulation particle. Particle shape effects (e.g., formation of liquid crystals and plastic crystals),²⁸ directional interactions (patchy particles),²⁹ and nanoparticle-self-assembly (often in close collaboration with experiment)³⁰⁻³¹ are best modeled at this level. Versatile toy models are hard particle models, which favor densest packing at high packing density, and the soft sphere models favor minimal internal surface area at low temperature.³ The combination of softness and anisotropic shape is mostly unexplored.

Finally, at the largest scale, where the individual particle effects can be ignored, phase field and other continuum models can describe phenomena at or above the mesoscale, like microphase separation and solidification, as well as connect to mechanical properties. Continuum methods often start from a semi-empirical free-energy functional.³²⁻³³ In practice, the level of coarse graining is chosen to best suit the scientific problem at hand. Coupling different levels of coarse

graining automatically or semi-automatically, as envisioned a few years ago, has proven cumbersome and inefficient, which is why it is at present rarely used.

The descriptive power of modeling advanced rapidly in recent years as a result of compute power increase, availability of easy-to-use general-purpose simulation toolkits (e.g., HOOMD-blue),³⁴ and improvements in algorithms and model assumptions. To date, the most successful applications of self-assembly simulations are structure prediction (local order, mesophases, crystallographic order) and resolving particle dynamics. Structure is well accessible via real space imaging (electron microscopy) and various scattering techniques. Dynamics is more difficult to access in experiment, which is why modeling can be particularly helpful.

Exciting and sometimes counterintuitive predictions were obtained from the analysis of emergent phenomena related to entropic ordering.³⁵ Many-body effects are increasingly appreciated with future potential for better insights, like the deformation of the ligand shell.³⁶⁻³⁷ While quantitative theoretical predictions remain difficult with room for future improvement, theory already routinely provides assistance for mechanistic understanding of self-assembly processes, helps improve simulation parameters, and inspires new research directions. In particular the rational (inverse) design of particles³⁸ and process conditions for desired materials properties has been developing into an exciting direction.

From new structures to new functions. The early research on self-assembly focused on understanding of the physical principles and new structures. Those fundamental studies have been motivated by the expectations for making practical materials and devices. Some of those hopes, such as self-assembling nano-robots and similar over-hyped claims did not deliver, at least as of today, but there are also impressive success stories. Here we discuss several examples of physical and chemical properties enabled by self-assembly of nano- and mesoscale building blocks.

Self-assembly allows combining dissimilar materials into one structure while enhancing the function beyond that of the building blocks. Nature efficiently utilized this concept in Pearl nacre (Figure 5a) composed of hard but brittle calcium carbonate platelets with a thickness of about half a micron. The platelets are separated by sheets of elastic biopolymers. Such combination of hard and elastic components makes nacre simultaneously strong and tough, which is quantified by the

simultaneous observation of large Young modulus and high Fracture toughness, respectively. This bio-inspired concept has been implemented in artificial nacre prepared using layer-by-layer assembly that approached mechanical properties of its natural counterparts.³⁹⁻⁴⁰ Achieving high mechanical strength of the artificial nacre required strong chemical bonding at the interface between inorganic platelets and binding polymer layers. This demonstrates an important point about properties of self-assembled materials which are determined not only by the properties of individual building blocks and their arrangements but on the properties of the interfaces responsible for connectivity of the components. The critical role of interfaces becomes the crosscutting theme in self-assembly of functional materials and devices.

The bottom-up engineering of low-cost, large-area, flexible, and printable electronic and optoelectronic devices has seen tremendous development in the last decade.⁴¹ In many cases, self-assembly helped integrating active components; such as semiconductor quantum dots, carbon nanotubes and polymer molecules in the complete device structure. The active components of Li-ion batteries also consist of nano- and microscopic grains, with electrons hopping from grain to grain toward collecting electrodes. All these devices rely on efficient transport of charge carriers, electrons or ions, through self-assembled materials. The interfaces often introduce bottlenecks to charge transport and act as recombination sites that reduce carrier mobility and lifetime. The importance of interfacial engineering of self-assembled materials is therefore the key to achieving competitive device performance. For example, recent progress in charge transport through nanocrystal solids used for quantum dot LEDs, solar cells, and photodetectors can be linked to various developments of the interfacial chemistry (Figure 5b).⁴²⁻⁴³

The hierarchical organization of self-assembled materials has been utilized for templated synthesis and nanofabrication. For example, *fcc* superlattices self-assembled from spherical silica or poly(methyl methacrylate) particles with a diameter of hundreds nanometers to microns exhibit the properties of photonic crystals.⁴⁴ Photonic crystals can inhibit the propagation of light of certain colors (energies), creating a photonic band gap⁴⁵ (Figure 4c). However, the refractive indexes of SiO₂ and PMMA are insufficient to develop complete photonic bandgap, while high-index materials, such as TiO₂ or Si, could not be prepared as monodisperse spheres suitable for self-assembly into long-range ordered superlattices. In addition, the *fcc* structure does not exhibit a complete photonic bandgap. The solution was to use silica or PMMA superlattices as templates

for infilling ordered voids with TiO_2 or silicon precursors forming an inverse *fcc* structure, which can exhibit a complete photonic bandgap.⁴⁶⁻⁴⁷ Selective dissolution of the templates resulted in inverse opals that demonstrated photonic crystal behaviors useful for designing special mirrors, waveguides, and cavities.⁴⁸

The approach of using self-assembled structures as templates has been very successfully realized for block-copolymers where one of the blocks is made of PMMA. In ordered self-assembled structures, the PMMA phase can be selectively dissolved by mild acid treatment, leaving behind voids which can be used as lithographic masks in semiconductor device patterning,⁴⁹ or form uniform pores in a filtration membrane.⁵⁰

As an example of where self-assembly greatly enhances function one needs to look no further than self-healing materials. In these systems, self-assembly enables formation of large volumes of hierarchical and compartmentalized architectures with clever placements of materials. In one example, catalyst-containing self-assembled microcapsules and insoluble healing-agent droplets were dispersed in an epoxy matrix and coated on a substrate. Upon a damage event, microcapsules and phase-separated droplets of a healing-agent were ruptured, flowed into the damaged region, healed the damage, and prevented rusting of the underlying substrate (Figure 5c).⁵¹ In another example, a self-healing composite formed where the catalyst and healing agent was only placed in the regions of the structure where damage is expected.⁵² There remains considerable opportunity to use self-assembly to form increasingly sophisticated systems for self-healing including through the design of microcapsules and the use of self-assembly to place healing chemistries in the desired locations within a material.

From function to market. As discussed in the preceding sections, self-assembled structures can show not only unprecedented structural motifs on previously inaccessible length scales in both two and three dimensions, but importantly, also provide materials with unique physical and chemical properties. The key to the market is that these materials either compete favorably with any alternative technological solutions or provide important functionalities not available at any cost. Additionally, long-term stability and environmental concerns must be addressed for the successful adaption of self-assembled materials by the marketplace. At this relatively early stage, several examples of self-assembled materials and devices have been integrated in consumer products or

implemented in large-scale manufacturing processes and more are currently on a commercialization pathway. Epitaxial quantum dots are used as efficient single-photon emitters for quantum information technologies,⁵³ colloidal nanocrystals are employed in light-emitting devices,⁵⁴ including flat panel displays and infrared sensors.⁵⁵⁻⁵⁶ Block-copolymers are being extensively tested by leading microelectronics companies and have been included in the International Roadmap for Devices and Systems,⁵⁷ however, the extreme ultraviolet (EUV) lithography and other developments in this very fast-moving semiconductor industry poses high activation barrier for radically new technologies. One of the obstacles that complicates adaption of self-assembled materials by the nanoelectronics community is structural defects arising from small local variations in process parameters. Annealing defects in materials composed of large building blocks (polymer chains, nanocrystals, etc.) is slower compared to defects annealed in ordinary atomic and molecular crystals.⁵⁸ Likely, self-assembled materials will find an easier path to adoption in more defect-tolerant applications such as energy storage electrodes,⁵⁹ and self-healing coatings.⁵¹ Batteries present a particularly compelling application space given the significant gains in performance resulting from hierarchical assembly of electrode materials that enables optimized pathways for electron and ion flows.⁶⁰ Implementation of this strategy in a cost-effective way has resulted in successful commercialization of bottom-up engineered electrode materials by Sila Nanotechnologies and other companies.

Similar analysis can be applied to many other application areas for self-assembled materials. In this analysis, it is important to realize that self-assembly is not a “silver bullet” but rather a useful addition to already existing technological toolsets. It is also important to realize that many elements of self-assembly, such as self-assembled monolayers as adhesion promotors, have existed in industrial practice for many years.⁶¹ In this capacity, it is only a matter of time until there is an increase in the numbers of materials and devices with self-assembled components in the market.

Future directions. Like any other field, self-assembly will continue developing with a combination of steady evolution and disruptive, revolutionary breakthroughs. On the evolutionary side, further improvements in the control of structural defects will be needed for wide utilization of self-assembly in the nanoelectronics and nanophotonics industries. We also expect the development of advanced computational models and tools with good predictive power for the

rational design of functional materials by self-assembly. Such tools will have to access systems with multiple types of building blocks and concurrent ordering processes, possibly programmable,⁶² networked,¹¹ or kept out of equilibrium by chemical fuel or external driving. Optimization of model and process parameters and automatic scans across parameter spaces will become more important. As in many other research fields, the powerful tools of machine learning and artificial intelligence are attractive choices.⁶³⁻⁶⁴ Success with these methods in self-assembly to date is still comparably slow and rare. But they already achieved significant attention in related areas of simulation, e.g., for the parameterization of interatomic potentials.⁶⁵⁻⁶⁶ In addition to these necessary improvements, we suggest watching out for two areas where truly transformative developments can be expected in the near future.

In the previous sections, we exclusively discussed equilibrium assembly where ordering is associated with the lowest energy state. However, equilibrium assembly represents just a subset of possible self-organization phenomena. All living systems, for example, rely on complex networks of non-equilibrium self-assembly. Our understanding of dynamic self-assembly is very much in its infancy and it is an area of active academic pursuit. Some exciting developments in the field of externally driven materials have been reported in recent years. One of the most intriguing aspects of active matter is that it does not obey the fundamental principles of closed systems, such as energy and momentum conservation.⁶⁷ This introduces new properties, such as odd elasticity⁶⁸ and odd viscosity,⁶⁹ and calls for different theoretical frameworks for describing and classifying non-equilibrium self-assembly phenomena. At this point, we can only speculate about what applications and technologies of non-equilibrium self-assembly will emerge once we develop a better understanding of its physical and chemical principles.

The second area of huge potential relates to the coupling strength of the components in self-assembled materials. In the case of weak coupling, all electronic states are localized on individual building blocks, and charge carriers and excitations can propagate only by hops between these localized states. As a result, optical or electronic properties of multicomponent and multifunctional assemblies are not too different from linear combinations of the properties of individual constituents. On the opposite side, strong electronic coupling brings materials to the realms of the quantum world with extended delocalized states, coherent transport phenomena, giant oscillator strengths, etc. For example, in crystalline semiconductors electrons are not localized on individual

atoms but freely move as Bloch waves. The wealth of quantum phenomena in condensed-matter systems has been traditionally associated using structurally coherent materials, such as single crystals and epitaxial heterostructures. In recent years, however, this paradigm has been challenged, and there is growing evidence that coherent transport can be approachable in structurally incoherent, non-epitaxial materials, namely organic semiconductors and nanocrystal solids, enabling delocalized electronic states and new regimes for charge, heat, and energy transport.⁷⁰⁻⁷⁴ The quality of self-assembled materials only recently approached levels needed to observe such effects. The time may be just right to launch systematic investigations and engineering of quantum phenomena in self-assembled materials.

Conclusions

Two decades of active research on self-assembly has delivered materials with unprecedented nanoscale structures in both two and three dimensions. In early work, the focus was primarily the nanostructure of the self-assembled materials, however, now, as commercialization interests have been increasing, the focus is increasing on the physical and chemical properties of these structures, and proof-of-concept devices. The current state of the field, as covered in this MRS Bulletin issue, strongly suggests that self-assembly is making significant strides toward application in nanoelectronics,[REF] photonics,[REF] energy storage,[REF] chemical separations,[REF] and as a path to form complex structures.[REF]. We suggest that deep understanding of self-assembly phenomena will pave the way for modular design of materials with many levels of functionality, hierarchical organization, and compartmentalization on a scale not previously harnessed in manmade materials.

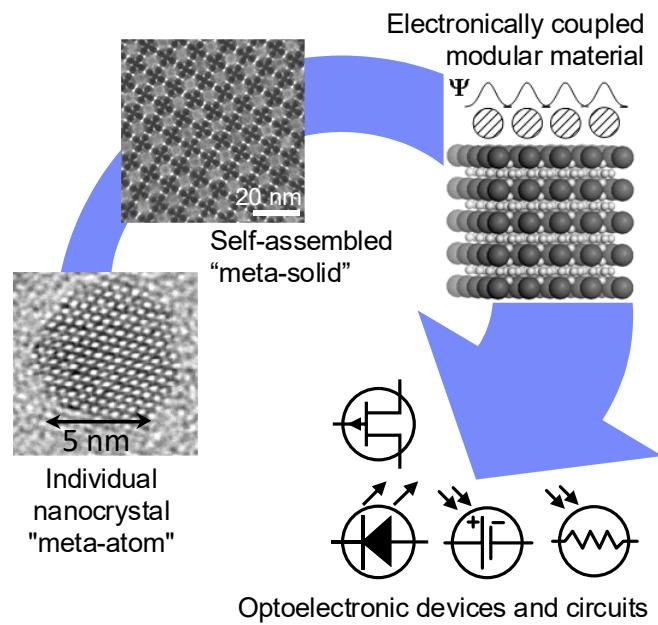


Figure 1. Self-assembly enables the transition from precisely engineered nanoscale building blocks or “meta-atoms” to macroscopic functional materials used for devices and other applications.

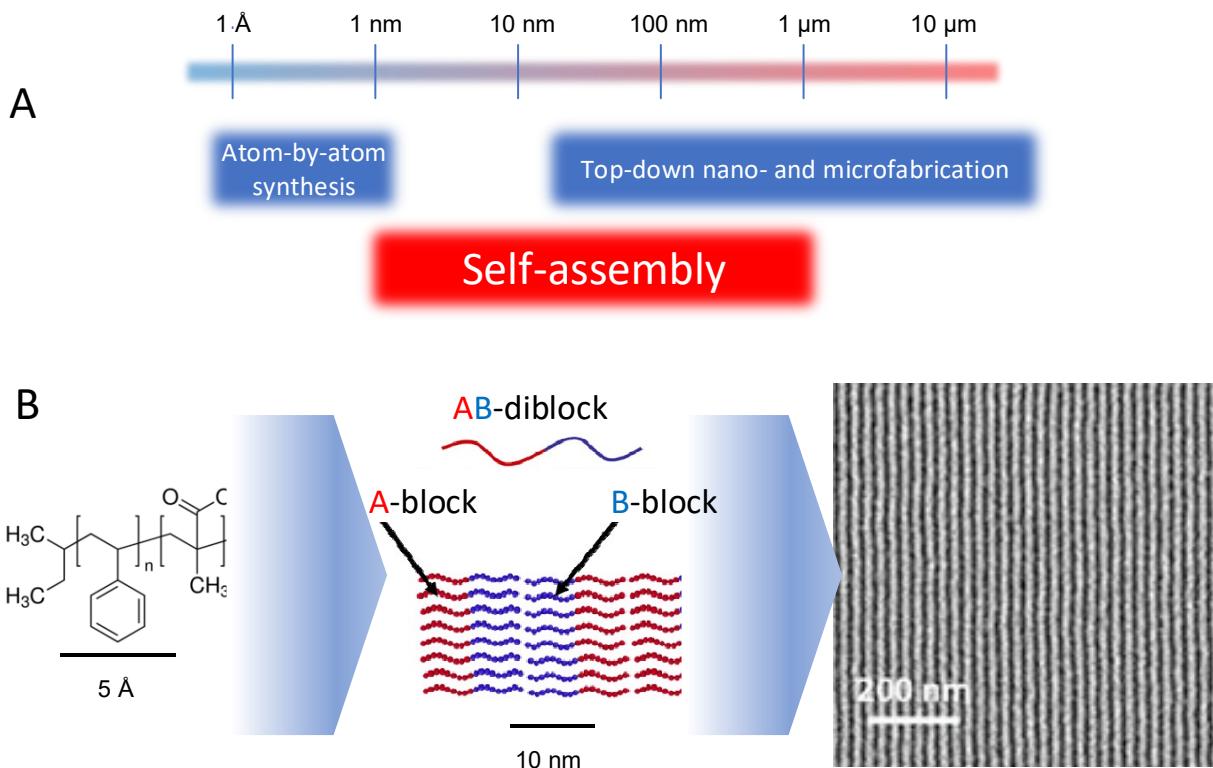


Figure 2. **(A)** Self-assembly allows organizing matter on length scales not achievable for traditional chemical synthesis and top-down nanofabrication techniques such as photolithography, imprint lithography, and even e-beam lithography. **(B)** The hierarchical nature of the materials synthesized by self-assembly: diblock copolymer chains self-organize in the lamella stacks driven by the repulsive interactions between the polymer blocks. One of the blocks can be selectively dissolved and the obtained template can be used to fabricate semiconductor nanoelectronic circuits on a length scale hardly achievable for traditional top-down photolithographic patterning. Panel 3 adapted with permission from Reference 75.

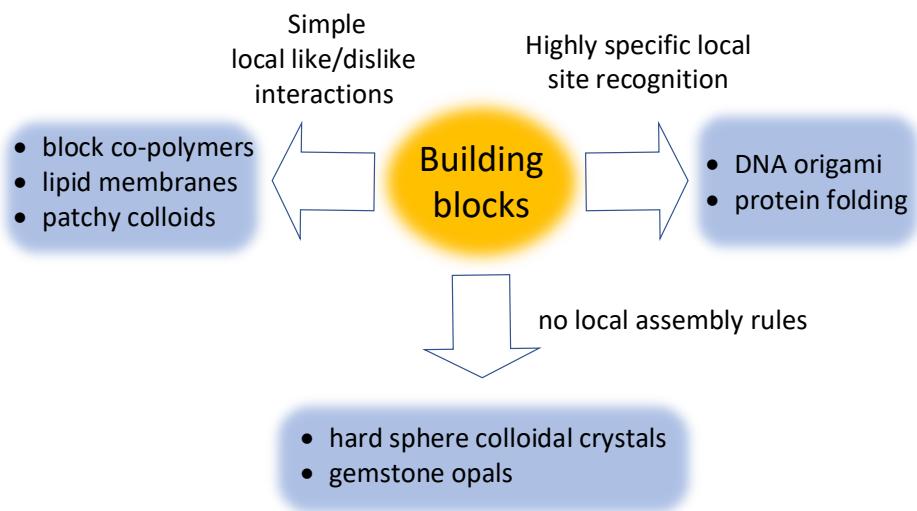


Figure 3. Classifications of interactions between building blocks utilized in self-assembly of functional materials.

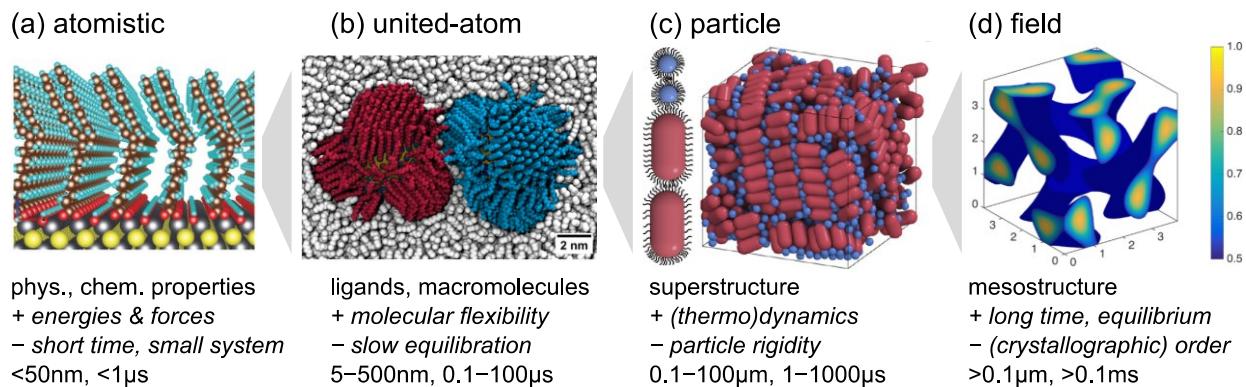


Figure 4. Theoretical and computational modeling strategies for self-assembled functional materials at the nanoscale. (a) Oleic acid molecules on the PbS(111) surface. Adapted with permission from Reference 76. © 2014 AAAS. (b) Gold nanoparticles coated with 1-hexadecanethiol and dispersed in decane. Adapted with permission from Reference 27. © 2018 American Chemical Society. (c) Self-assembled AB₂ binary spherocylinder-sphere superlattice. Adapted with permission from Reference 77. © 2013 American Chemical Society. (d) Free energy density of the block polymer gyroid phase (Ia³d) computed with the self-consistent field method. A typical type of application, a main strength (+) and a main weakness (−) are listed. The level of coarse-graining (characteristic length and time scale, given at the bottom) increases from the left to the right. Adapted with permission from Reference 33. © 2016 American Chemical Society.

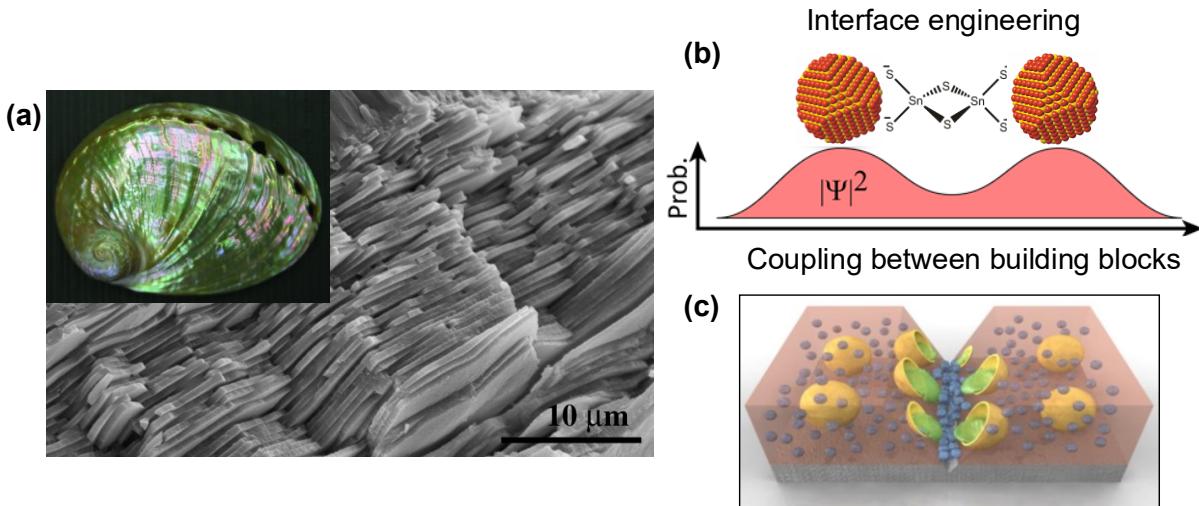


Figure 5. **(A)** SEM micrograph of a fracture surface of nacre, showing the layered structure. Some calcite is visible in the upper half. Inset, image of a polished abalone shell. SEM adapted with permission from Reference 78. © 2003 John Wiley and Sons. Abalone shell image in inset adapted with permission from Reference 79. © 2004 OSA Publishing. **(B)** Interface engineering is critical for efficient couplings of semiconducting, plasmonic, magnetic, or other self-assembled functional building blocks. **(C)** Self-healing polymer coating formed from self-assembled catalyst containing capsules and phase-separated healing agent droplets dispersed in an epoxy matrix. Upon a damage event, catalyst and healing agent are released into the damage region, healing the damage.⁵¹

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