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# Layer and material-type dependent photoresponse in WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures

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#### Abstract

Transition metal dichalcogenide (TMD) heterostructures are promising for a variety of applications in photovoltaics and photosensing. Successfully exploiting these heterostructures will require an understanding of their layer-dependent electronic structures. However, there is no experimental data demonstrating the layer-number dependence of photovoltaic effects (PVEs) in vertical TMD heterojunctions. Here, by combining scanning electrochemical cell microscopy (SECCM) with optical probes, we report the first layer-dependence of photocurrents in WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures as well as in pristine WS<sub>2</sub> and WSe<sub>2</sub> layers. For WS<sub>2</sub>, we find that photocurrents increase with increasing layer thickness, whereas for WSe<sub>2</sub> the layer dependence is more complex and depends on both the layer number and applied bias ( $V_b$ ). We further find that photocurrents in the WSe<sub>2</sub>/WS<sub>2</sub> heterostructures exhibit anomalous layer and material-type dependent behaviors. Our results advance the understanding of photoresponse in atomically thin WSe<sub>2</sub>/WS<sub>2</sub> heterostructures and pave the way to novel nanoelectronic and optoelectronic devices.

#### 1. Introduction

Transition metal dichalcogenides (TMDs) (such as MoS<sub>2</sub>, MoSe<sub>2</sub>, WS<sub>2</sub>, and WSe<sub>2</sub>) are promising candidate materials for nanoelectronics and optoelectronics [1–13], owing to their strong light-matter interactions [1] and layer-dependent electronic structures [13, 14]. The ability to precisely fabricate vdW heterostructures [15] by assembling different TMD atomic layers provides a novel route to a wide variety of artificial semiconductor heterostructures and Moiré superlattices [16-18]. Furthermore, the thicknessdependent band gaps of thin TMD layers enable even more possibilities to create novel p-n junctions at the atomic scale for photodetection and energy-harvesting applications [19]. In the past few years, most efforts have been devoted to exploring the photoresponse in heterojunctions made of different TMD monolayers or their multilayers with random thicknesses, such as WSe<sub>2</sub>/MoS<sub>2</sub> [19, 20], black

phosphorene/MoS<sub>2</sub> [21, 22], MoTe<sub>2</sub>/MoS<sub>2</sub> [23, 24],  $WSe_2/SnS_2$  [25, 26]. On the other hand, for solar cell applications, it has been shown that the responsivity can be significantly enhanced in vertical heterojunctions consisting of TMD multilayers [19, 27]. However, due to the technical difficulties associated with the fabrication of top and bottom electrical contacts and the relatively low spatial resolution achievable with current laser-based techniques, little work has been performed to study the layer dependence of the photovoltaic effects (PVEs) in TMD-based heterojunctions, particularly along the vertical direction, thus far. To fully explore the potential of TMD-based vdW heterostructures for future energy-harvesting applications, studies of the layer-dependent photoresponse in TMD heterojunctions are highly desirable.

In this paper, we report the preparation of highquality, atomically thin layers of  $WS_2$  (intrinsic),  $WSe_2$  (p-type) and their vertical heterojunctions on conductive indium tin oxide (ITO) substrates. We employed a unique tool, scanning electrochemical cell microscopy (SECCM) [28–36] to study the PVEs of the prepared TMD layers along the out-of-plane direction. We systematically studied the layer-dependent PVEs of the pristine WS<sub>2</sub> and WSe<sub>2</sub> atomic layers as well as their heterostructures. In addition, we show the strong layer-dependent PL of the corresponding pristine WS<sub>2</sub> and WSe<sub>2</sub> atomic layers and their heterostructures. Our results indicate that the atomically thin WSe<sub>2</sub>/WS<sub>2</sub> heterostructures with type-II band alignment and distinct layer- and material type dependent photocurrent generation characteristics can be used to create novel nanoelectronic and optoelectronic devices.

#### 2. Results and discussion

#### 2.1. Layer-dependent PL and PVE of WS<sub>2</sub>

Figure 1(a) shows a representative optical image of the pristine WS<sub>2</sub> atomic layers prepared on an ITO substrate using the dry transfer technique [37] (see figure S1 available online at stacks.iop.org/2DM/9/015022/ mmedia). We first studied the layer-dependent PL of thin  $WS_2$  flakes (figure 1(a)) with thickness ranging from a monolayer (1L) to four layers (4L). Figure 1(b)shows the corresponding room-temperature PL maps of two WS<sub>2</sub> samples. We see that the monolayer portion of the WS<sub>2</sub> sample exhibits the strongest PL signal with a dramatic decrease in intensity as the thickness increases. This observation can be understood by the layer-dependent electronic structures of thin WS<sub>2</sub> layers, including (a) a transition from a direct (1L) to indirect (>1L) band gap; and (b) a reduced band gap as the sample thickness increases (see figure S2).

PVEs of the same samples were interrogated at room temperature (figure 1(a)) using SECCM (see figure 1(c)). In these studies, an electrochemical probe was constructed by filling a small (200–500 nm terminal diameter) conical probe with an aqueous electrolyte solution containing 100 mM NaI and 10 mM I<sub>2</sub>. The inclusion of I<sup>-</sup> and I<sub>2</sub> species creates a defined electrochemical potential within the probe based on the following reaction ( $E^0 = 0.536$  V vs. standard hydrogen electrode = -5.0 eV vs. vacuum):

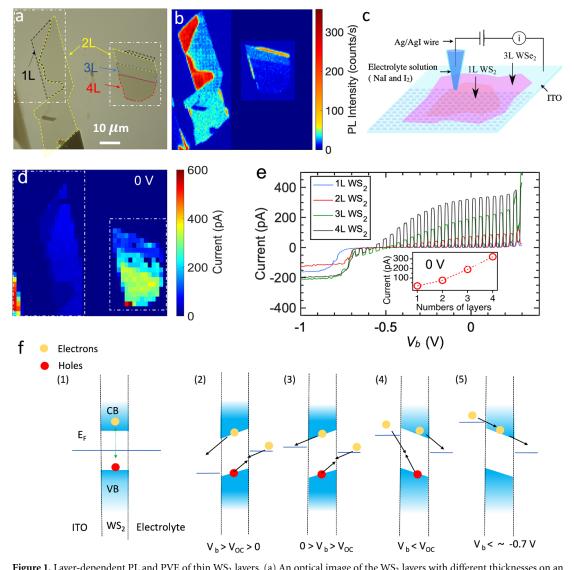
$$I_3^- + 2e^- \rightleftharpoons 3I^-$$

This probe was brought into contact with the sample, creating a miniaturized contact area between the sample and electrolyte solution. The effective area is defined by the size of the liquid meniscus which extends from the probe tip, which is typically ~1.5 times the physical dimensions of the probe. The tip diameter ranges from 200 to 500 nm, thus the corresponding effective area is between  $7.1 \times 10^{-14}$  and  $4.4 \times 10^{-13}$  m<sup>2</sup>. The field within the sample can be controlled by applying a bias ( $V_b$ ) between the ITO substrate and the electrochemical probe. Carriers driven to the sample-electrolyte interface can cross

the interface by driving the above electrochemical reaction, resulting in a measurable current. In effect, the electrochemical probe in SECCM can behave as a reconfigurable, conformal contact with a work function effectively set by the electrolyte species. This approach has been recently applied to great effect in the study of photovoltaic processes in thick TMD layers [38–41]. It should also be noted that these SECCM measurements are non-destructive, which was confirmed through Raman analyses (see figure S3) carried out before and after PVE measurements and further supported by the high stability of photoelectrochemical solar cells made from these materials [42, 43].

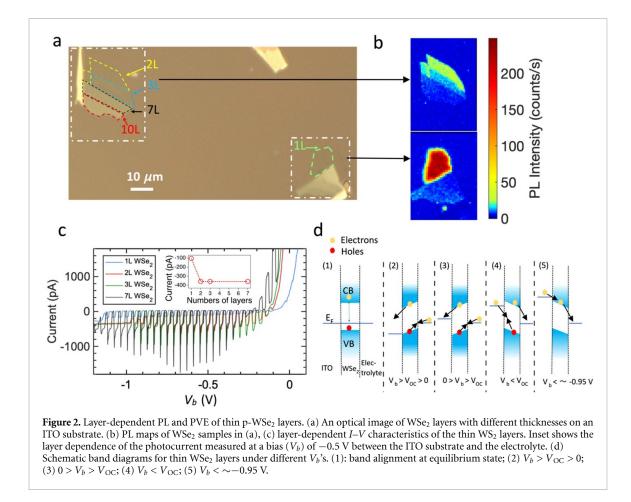
PVEs in the TMD samples were investigated by obtaining a series of I-V curves with the probe in contact with an array of points spanning the structure of interest. During I-V measurements, samples were illuminated through the ITO substrate with a chopped broadband light source. Representative photocurrent maps obtained at  $V_b = 0$  V for pristine WS<sub>2</sub> samples are shown in figure 1(d). In contrast to the PL results (figure 1(b)), the photocurrent of WS<sub>2</sub> increases with the increasing thickness (figure 1(d)). We further plotted the representative *I–V* curves taken from different regions of the WS<sub>2</sub> sample (figure 1(a)). As shown in figure 1(e), three essential features can be observed when  $V_b$  is larger than the open-circuit voltage  $(V_{OC})$ , including (a) the photocurrent with negligible dark current can be observed in all the layers; (b) the photocurrent gradually saturates as  $V_b$  increases to a higher value, indicating a clear photodiode behavior; and (c) the photocurrent ( $V_b = 0$  V) increases with an increasing number of layers (inset of figure 1(e)), showing a strong layer-dependent photocurrent consistent with the mapping results shown in figure 1(d). On the other hand, when  $V_b$  is  $\langle V_{OC}$ , we only observed an apparent dark current in all the layers that quickly saturates. Such saturation is due to the diffusion-limited transport of  $I_3^-$  species to the interface. Meanwhile, we observed a small negative photocurrent when  $V_b$  is slightly smaller than  $V_{\rm OC}$  that was quickly suppressed by the appearance of a dark current. Furthermore, important merits for photovoltaic devices, the corresponding open-circuit voltage V<sub>OC</sub> and short-circuit current ISC were extracted as listed in table S1. We find that  $I_{SC}$  decreases as the thickness of WS<sub>2</sub> decreases. Although the highest  $V_{\rm OC}$  was observed in the monolayer  $WS_2$ , no clear layer-dependence of the  $V_{OC}$  can be identified.

To understand the I-V characteristics and photocurrent of the thin WS<sub>2</sub> layers, we applied band structure analysis based on metal-semiconductor junction physics. In the WS<sub>2</sub> device, two junctions are formed at the ITO/WS<sub>2</sub> and WS<sub>2</sub>/electrolyte interfaces. Band offsets at these interfaces depend on the work function of the ITO and the electrochemical potential of the I<sub>3</sub><sup>-</sup>/I<sup>-</sup> redox couple. Simplified band



**Figure 1.** Layer-dependent PL and PVE of thin WS<sub>2</sub> layers. (a) An optical image of the WS<sub>2</sub> layers with different thicknesses on an ITO substrate. PL (b) map of the sample in (a), (c) schematic of the SECCM measurements. (d) Photocurrent map of the WS<sub>2</sub> samples in (a), (e) layer-dependent *I*–V characteristics of WS<sub>2</sub>. Inset is the layer dependence of the photocurrent measured at a bias ( $V_b$ ) of 0 V applied between the ITO substrate and the electrolyte. (f) Schematic band diagrams of WS<sub>2</sub> under different  $V_b$ 's. (1) Band alignment at equilibrium state; (2)  $V_b > V_{OC} > 0$ ; (3)  $0 > V_b > V_{OC}$ ; (4)  $V_b < V_{OC}$ ; (5)  $V_b < \sim -0.7$  V.

diagrams of the device structure at different  $V_b$ 's are shown in figure 1(f). At the equilibrium state, the Fermi level  $E_F$  is located near the middle of the band gap of WS<sub>2</sub> due to its intrinsic nature. Under optical excitation, electrons in the valence band (VB) can be excited to the conduction band (CB) where electronhole pairs (EHPs) are generated, contributing to the photocurrent. When  $V_b > V_{OC} > 0$ , as shown in diagram (2) of figure 1(f), the energy bands of WS<sub>2</sub> near the ITO side is lowered. Under illumination, holes generated in the WS<sub>2</sub> layer flow towards the electrolyte interface, driving the oxidation of I<sup>-</sup>. Meanwhile, the excited electrons in the CB of WS<sub>2</sub> are driven towards the ITO substrate, resulting in a positive photocurrent. Negligible dark current is expected since hole injection from ITO into the VB is unfavorable. When  $0 > V_b > V_{OC}$ , as shown in diagram (3) of figure 1(f), the Fermi level of ITO is lifted up to slightly higher than that of the electrolyte. However, a positive photocurrent is still expected because of the unchanged energy band bending in WS<sub>2</sub> induced by the generated EHPs. On the other hand, when  $V_b$  is  $\langle V_{OC}$  (diagram (4) of figure 1(f)), the Fermi level of ITO is further lifted up to a point still lower than the CB of WS<sub>2</sub>. Under illumination, the energy bands of WS<sub>2</sub> will be bent in the opposite direction. Thus, the excited electrons in CB of WS<sub>2</sub> are driven to the electrolyte and electrons in ITO recombine with holes in VB of WS<sub>2</sub>, resulting in a negative photocurrent as observed in figure 1(e). When a more negative  $V_b$  is applied (about -0.7 V, diagram (5) of figure 1(f) the Fermi level  $E_F$  of ITO is now higher than the CB of WS<sub>2</sub> and electrons can directly transfer from the ITO substrate to the electrolyte through the CB of WS<sub>2</sub>, resulting in an apparent dark current and a negligible photocurrent, consistent with



our experimental observations (figure 1(e)). We note that the layer dependence of PVEs for the thin WS<sub>2</sub> layers is different from previously reported results of MoS<sub>2</sub> [44] even though both samples have a similar layer-dependent PL behavior. In our case, the enhanced photocurrent in thicker WS<sub>2</sub> samples is mainly due to the reduced band gaps as well as the increased light absorption in thicker samples. When a white light source is applied the narrower the band gap results in a wider range of absorbed photon energies. Thus, more EHPs can be generated in thicker layers resulting in a higher photocurrent. We note that, since a laser source was used in the studies of previous MoS<sub>2</sub> samples [44], a direct comparison between the two experiments may not be straightforward.

#### 2.2. Layer-dependent PL and PVE of p-type WSe<sub>2</sub>

We performed similar PL and PVE measurements on thin p-type WSe<sub>2</sub> layers. Figure 2(b) shows the representative PL maps taken from two samples (marked by two white rectangles in figure 2(a)) with different thicknesses. Similar to WS<sub>2</sub>, the PL signal decreases as the thickness of WSe<sub>2</sub> increases because both WS<sub>2</sub> and WSe<sub>2</sub> feature a similar layer-dependent direct to indirect energy gap transition (see figure S4). Figure 2(c) shows the *I*–*V* characteristics of the WSe<sub>2</sub> samples taken from different locations with different thicknesses (figure 2(a)). The layer-dependent photocurrent in p-type WSe<sub>2</sub> is more complex in contrast to WS<sub>2</sub>. For instance, among the WSe<sub>2</sub> flakes, the thin ( $\leq$ 4L) and thick flakes ( $\geq$ 7L) show very different photovoltaic behaviors as shown in figures 2(c)and S5. For thicker flakes ( $\geq$ 7L), both the photocurrent and dark currents can be observed when  $V_b$  is  $>V_{OC}$  while the dark current remains high in the thinner layers, where the photocurrent is missing. When  $V_b$  is  $< V_{OC}$ , the photocurrent was detected in all the measured WSe<sub>2</sub> layers and is insensitive to the applied  $V_b$  whereas the dark current vanishes. Furthermore, when a more negative  $V_b$  is applied (<-0.9 V), an apparent dark current with a negligible photocurrent was detected in the thin layers (figures 2(c) and S5). We have depicted the photocurrent (at  $V_b = -0.5$  V) as a function of the number of WSe2 layers in the inset of figure 2(c) where the photocurrents of the measured layers greater than a monolayer are very close to 350 pA. Another prominent feature is the spikes in the *I*–*V* curves measured in 2, 3 and 7L samples. These spikes appear instantly when the light is on and then decay quickly. Such a feature is mainly due to charge recombination/trapping at the interface [45]. We note that in this study only the steady-state photocurrent is considered. We further analyzed the layerdependences of both the  $V_{\text{OC}}$  and  $I_{\text{SC}}$  of the WSe<sub>2</sub> as listed in table S1, where both the  $V_{OC}$  and  $I_{SC}$  of WSe<sub>2</sub> decrease as the thickness decreases.

To qualitatively understand the PVE of p-type WSe<sub>2</sub>, we consider the simplified band diagram of p-type WSe<sub>2</sub> devices at different  $V_b$ 's, as shown in figure 2(d). At the equilibrium state (diagram (1) of figure 2(d)), the  $E_F$  is close to the VB of WSe<sub>2</sub> due to its p-type nature. When  $V_b > V_{OC} > 0$  (diagram (2) of figure 2(d)), a significant dark current can flow through the devices (ITO /WSe<sub>2</sub>/electrolyte) through the VB of WSe<sub>2</sub> consistent with our experimental observations as shown in figure 2(c). Under illumination, the generated EHPs further enhance the overall current resulting in a photocurrent. We note that the photocurrent is only detected in thick layers (see figures 2(c) and S5). When  $0 > V_b > V_{OC}$  (diagram (3) of figure 2(d), the band bending in WSe<sub>2</sub> still predicts a positive photocurrent but minimal dark current. We note that the positive photocurrent was only observed in our thick samples and an obvious dark current was observed in all the measured layers. Such a contradiction requires further study. When  $V_b < V_{\rm OC}$ , as shown in diagram (4) of figure 2(d), the energy bands of the WSe2 near the ITO interface are lifted up. In this case, no dark current is expected due to the energy barriers for both charge carriers at the interfaces while the photo-generated electrons in the CB of the WSe<sub>2</sub> can flow into the electrolyte contributing to a negative photocurrent that is consistent with our experimental observations. When the  $V_b$  is more negative (about -0.95 V as shown in diagram (5) of figure 2(d)) the Fermi level of the ITO is now above the CB edge of WSe2. Therefore, electrons from ITO can directly travel to the electrolyte resulting in a significant dark current as observed in our thin samples (figures 2(d) and S5).

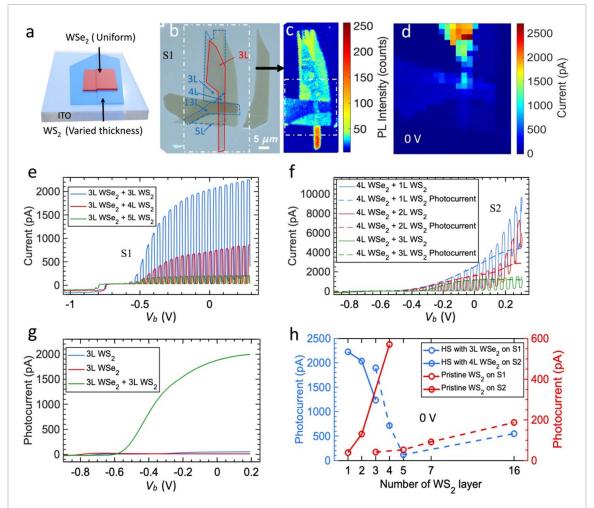
## 2.3. Layer-dependent PL and PVE of WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures

We further studied the layer-dependent PL and PVE of the WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures. Figure 3(a) shows a schematic of a WSe<sub>2</sub>/WS<sub>2</sub> heterostructure (type-I) where a uniform WSe<sub>2</sub> layer sits on a WS<sub>2</sub> flake with different thicknesses at different locations. The optical image of an actual device (S1, with a 3L WSe<sub>2</sub> and a WS<sub>2</sub> flake containing 3, 4, 5, and 13L) is shown in figure 3(b) where different vertical heterojunctions can be formed. With such a configuration, measurements on all the formed heterojunctions can be performed under the same conditions, offering a direct way to compare their performance. Figures 3(c) and (d) show a PL map taken from the white rectangle region in figure 3(b)and a photocurrent map measured from the square region highlighted in figure 3(c) at  $V_b = 0$  V, respectively. One can see that the PL signal is suppressed in all the heterojunction areas whereas the photocurrent is significantly enhanced. For instance, the photocurrent of a WSe2 (3L)/WS2 (3L) heterostructure (figure 3(g), measured at  $V_b = 0.15$  V) has been enhanced by about 30 times compared to those from

its constituents (3L WS<sub>2</sub> and 3L WSe<sub>2</sub>). Such an enhancement is mainly due to enhanced charge transfer and exciton dissociation in the heterojunction<sup>19</sup>. Figures 3(e) and (f) show the representative I-V characteristics taken from samples S1 and S2, respectively. Two distinct features can be found from the layerdependent *I*–*V* characteristics: (a) a significant dark current was observed in the 1L and 2L WS<sub>2</sub> (sample S2) while the dark current is absent from all other combinations when WS<sub>2</sub> is thicker than 2L. This is mainly due to a lower tunneling barrier in the junction with a thinner WS<sub>2</sub> layer compared with a thicker WS<sub>2</sub> layer; and (b) the photocurrent can only be observed when a  $V_b$  is larger than  $V_{OC}$  and decreases with the increasing thickness of  $WS_2$ . In figure 3(h) we summarized the layer-dependence of the photocurrents measured from both the constituent WS<sub>2</sub> (red right axis) and the heterostructure (blue left axis) regions from the two samples (S1 and S2).

One can see that, consistent with the data shown in figure 1(d), the photocurrent measured from pristine WS<sub>2</sub> layers increases as its thickness increases. However, in the junction region, the photocurrent first decreases with the increasing thickness of WS<sub>2</sub> and then slightly increases as the thickness of WS<sub>2</sub> reaches a threshold value. In addition, we compared the layer dependences of the  $V_{OC}$  and  $I_{SC}$  (table S1) of the heterostructures. In the same device, the  $V_{\rm OC}$ stays unchanged as the thickness of the constituent WS<sub>2</sub> layer varies. We note that a slightly higher value of  $V_{OC}$  was observed in the 4L WSe<sub>2</sub>/3L WS<sub>2</sub>. The slight difference between different devices on different substrates may be due to the environmental effects and different measurement conditions. It is also noted that the short circuit current decreases as the thickness of the WS<sub>2</sub> layer increases.

To further study the role of the WSe<sub>2</sub> layer in the PL and PVE of the WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures, we fabricated a type-II heterostructure consisting of a WS<sub>2</sub> bottom layer with a fixed thickness and a WSe<sub>2</sub> top flake with different thicknesses at different locations (figure 4(a)). Figure 4(b) shows the optical image of such a WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructure. The corresponding room-temperature PL map is shown figure 4(c), where the PL intensity is reduced in the heterojunction region. We note that, although the PL signal is still obvious in the junction regions of 1L (and 2L) WSe<sub>2</sub>/4L WS<sub>2</sub>, its intensity is already much lower than those taken from the pristine 1L and 2L WSe<sub>2</sub>. Figure 4(d) shows the short circuit photocurrent map obtained from the sample shown in figure 4(b). One can see that the highest photocurrent was detected in the 4L WSe2/4L WS2 location. To analyze the layer-dependent PVE, the characteristic I-V curves taken from different locations of the device (figure 4(b)) are shown in figure 4(e). We further summarized the corresponding photocurrent  $(V_b = 0 \text{ V})$  as a function of the number of WSe<sub>2</sub> layers in figure 4(f). The photocurrents observed in all the

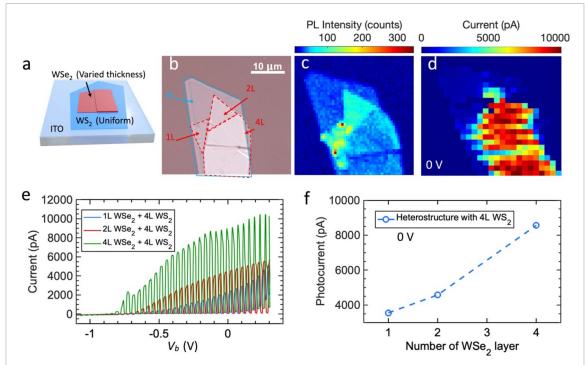


**Figure 3.** Layer-dependent PL and PVE of WSe<sub>2</sub> /WS<sub>2</sub> heterostructures with a fixed thickness of WSe<sub>2</sub>. (a) Schematic of a vertically stacked WSe<sub>2</sub>/WS<sub>2</sub> heterostructure with different thicknesses of WS<sub>2</sub> and a fixed thickness of WSe<sub>2</sub> on an ITO substrate. (b) An optical image of a WSe<sub>2</sub>/WS<sub>2</sub> heterostructure (sample 1, *S1*). The contours of the 3, 4, 5 and 13L of WS<sub>2</sub> are highlighted by the blue dashed lines. The contour of the 3L WSe<sub>2</sub> is highlighted by the red lines. (c) A PL map of *S1* taken from the box in (b). (d) A photocurrent map of *S1* taken from the region highlighted by the white box in (c) at  $V_b = 0$  V. Layer-dependent *I*-V characteristics of samples *S1* (e) and *S2* (f). The dashed lines in (f) represent the pure photocurrents taken from different locations of *S2*. (g) Photocurrents taken from different regions of a WSe<sub>2</sub> (3L) /WS<sub>2</sub> (3L) heterostructure, where the photocurrent has been enhanced by more than 30 times (at  $V_b = 0.15$  V) in the WSe<sub>2</sub> (3L)/WS<sub>2</sub> (3L) junction region comparing with that of the pristine 3L WS<sub>2</sub> or WSe<sub>2</sub>. (h) Photocurrent measured at  $V_b = 0$  V as a function of the number of WS<sub>2</sub> layers in the WSe<sub>2</sub> /WS<sub>2</sub> heterostructures (right axis) and of the pristine WS<sub>2</sub> layers (left axis).

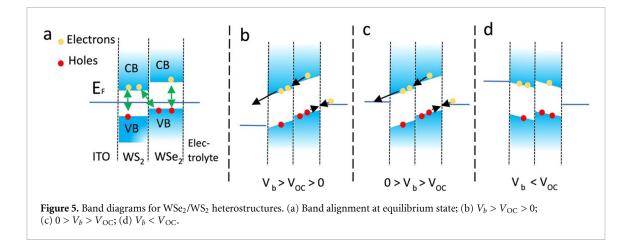
junctions increase as the thickness of the WSe<sub>2</sub> layers increases (figures 4(e) and (f)). We note that such a layer-dependent photocurrent is drastically different from that of WS<sub>2</sub> in the vertical heterostructures (figure 3(h)). In addition, we find that  $V_{OC}$  increases as the thickness of WSe<sub>2</sub> increases while the  $V_{OC}$  stayed unchanged as the thickness of WS<sub>2</sub> varies (table S1). The corresponding  $I_{SC}$  increases as the thickness of WSe<sub>2</sub> increases.

To explain the PVE observed in these WSe<sub>2</sub>/WS<sub>2</sub> vertical heterostructures, we investigated the band diagram of ITO/WSe<sub>2</sub>/WS<sub>2</sub>/electrolyte junctions under different  $V_b$ 's as shown in figure 5. Figure 5(a) shows the heterostructure at equilibrium. The band alignment between WS<sub>2</sub> and WSe<sub>2</sub> is known as type-II [46] that is consistent with our density functional theory (DFT) calculations (see figure S6). Under illumination, in addition to creating intralayer

excitons within WSe2 and WS2, interlayer excitons can also be generated by exciting electrons from VB of WSe<sub>2</sub> to CB of WS<sub>2</sub>. When the  $V_b$  is greater than  $V_{\rm OC}$  and less than 0 V, as shown in the figure 5(b), the energy bands of the heterostructure near the ITO side are tilted down. Thus, under illumination, both intralayer and interlayer excitons can be generated in the vertical WSe<sub>2</sub>/WS<sub>2</sub> heterostructures. Owing to the positive bias, the electrons from the electrolyte can recombine with the holes in the VBs of both WS<sub>2</sub> and WSe<sub>2</sub>; meanwhile the photoexcited electrons in the CBs can travel to the ITO substrate resulting in a positive photocurrent. When  $0 \text{ V} > V_b > V_{\text{OC}}$ , as shown in figure 5(c), the Fermi level of the ITO is lifted up while the energy bands of the heterojunction are still bent in the same way as that of  $V_b > V_{OC} > 0$ . Thus, similar electron and hole transfer processes are expected. In the case of  $V_b < V_{OC}$ , the band bending



**Figure 4.** Layer-dependent PL and PVE of WSe<sub>2</sub>/WS<sub>2</sub> heterostructures with a fixed thickness of WS<sub>2</sub>. (a) Schematic of a WSe<sub>2</sub>/WS<sub>2</sub> heterostructure with different thicknesses of WSe<sub>2</sub> and a fixed thickness of WS<sub>2</sub> on an ITO substrate. (b) An optical image of a WSe<sub>2</sub>/WS<sub>2</sub> heterostructure. The contours of the top WSe<sub>2</sub> and bottom WS<sub>2</sub> are highlighted by the dashed green and blue lines, respectively. PL (c) and photocurrent (d) maps (at  $V_b = 0$  V) of the sample in (b), (e) layer-dependent *I*–V characteristics of the sample in (b), (f) photocurrent (at  $V_b = 0$  V) as a function of the number of WSe<sub>2</sub> layers in the WSe<sub>2</sub>/WS<sub>2</sub> heterostructure.



in the heterojunction is now changed to the opposite direction as shown in figure 5(d). Owing to the energy barrier at the WSe<sub>2</sub>/WS<sub>2</sub> interface, no charge carriers can flow across the entire junction, resulting in zero photo and dark currents. We note that all these expectations are consistent with our experimental observations.

We have demonstrated that the PL signal is significantly suppressed in the WSe<sub>2</sub>/WS<sub>2</sub> vertical heterojunctions (figures 3, 4 and S7). To understand this phenomenon, we now focus on the simplest heterostructure of 1L WSe<sub>2</sub>/1L WS<sub>2</sub> (figure S7). The PL signal is quenched in the junction region but retains a high intensity in the pristine WSe<sub>2</sub> and WS<sub>2</sub> areas since both of them feature a direct band gap. We also performed a band structure calculation of the 1L WSe<sub>2</sub>/1L WS<sub>2</sub> heterojunction where an indirect band gap (figure S7(c)) is expected after considering the inter-layer interaction between the two constituents. Thus, we can conclude that, similar to multilayer WS<sub>2</sub> and WSe<sub>2</sub> samples, the mechanism of the suppressed PL in the WSe<sub>2</sub>/WS<sub>2</sub> heterojunctions is mainly due to the transition from a direct to indirect band gap.

From our studies of the layer dependent PVE of the  $WSe_2/WS_2$  heterostructure and its constituents, we noticed two anomalous behaviors for the  $WSe_2/WS_2$  heterostructures: (a) the photocurrents in pure  $WS_2$  flakes increase with increasing  $WS_2$  thicknesses, whereas an opposite dependence of the

photocurrent on WS<sub>2</sub> layers was observed in the WSe<sub>2</sub>/WS<sub>2</sub> heterostructure; and (b) the photocurrent in pristine WSe2 is largely thickness-independent while the photocurrent in WSe2/WS2 heterostructures would increase with the increasing thickness of WSe<sub>2</sub>. To address these anomalies, we propose a possible explanation based on the calculated band structures of the WSe<sub>2</sub>/WS<sub>2</sub> heterostructures (figure S6). We find that the conduction band minimum (CBM) of WSe<sub>2</sub> moves to a higher energy and the CBM of WS<sub>2</sub> remains almost unchanged. With addition of 1L WS<sub>2</sub> onto the 1L WS<sub>2</sub>/2L WSe<sub>2</sub> heterostructure, a larger band gap is expected in the WSe<sub>2</sub> side. Therefore, in the 2L WSe<sub>2</sub>/2L WS<sub>2</sub> heterostructures, the energy range of the intra-band absorption spectrum of the WSe<sub>2</sub> layer is narrowed and fewer EHPs can be generated under white light illumination. On the other hand, when a WSe<sub>2</sub> monolayer is added to the 2LWS<sub>2</sub>/1LWSe<sub>2</sub> heterostructure, both CBMs of WS<sub>2</sub> and WSe<sub>2</sub> are lowered. The corresponding energy ranges of the intra- and inter-band absorption spectra in the 2L WSe<sub>2</sub>/2L WS<sub>2</sub> heterostructure can be expanded resulting in photocurrent enhancements, consistent with our experimental observations.

#### 3. Conclusion

In summary, we have fabricated high-quality WS<sub>2</sub> and WSe2 atomic layers and their vertical heterojunctions on ITO substrates and explored their layer-dependent photoresponses (including PVE and PL). In particular, we found that the photocurrent increases with the increasing thickness of the pristine WS<sub>2</sub> while the photocurrent in WSe<sub>2</sub> is largely independent on the sample thickness. For the vertical heterojunctions, we observed anomalous behavior of the layer-dependent photocurrents. For instance, the photocurrent decreases with increasing WS<sub>2</sub> thickness while an opposite layer dependence for the WSe<sub>2</sub> layer was observed. For the layer-dependent PL signals, we observed consistent results in all the samples meaning that the PL intensity is largely reduced as the band gap changes from direct to indirect. Our study provides a new understanding of 2D semiconductors and their heterostructures and paves new ways to optimize the performance of 2D-semiconductorsbased photodetectors for possible energy-harvesting applications.

#### 4. Methods

#### 4.1. Materials and chemicals

NaI (Sigma Aldrich,  $\geq$ 99%) and I<sub>2</sub> (Mallinckrodt, U.S.P grade) were obtained from the indicated sources and used without further purification. Ag wire (Alfa-Aesar, 0.25 mm, 99.99%) was employed as the counter electrode for probe fabrication, and stored in an aqueous solution containing 100 mM NaI and 10 mM I<sub>2</sub> when not in use. ITO-coated cover

glass slides (22 × 22 mm, #1.5, 30–60  $\Omega$  sq., Structure Probe Inc (SPI)) were employed as sample substrates. Bulk WS<sub>2</sub> and WSe<sub>2</sub> crystals with dopant densities of ~3 × 10<sup>14</sup> cm<sup>-3</sup> and ~2 × 10<sup>17</sup> cm<sup>-3</sup>, respectively, were prepared via vapor transport methods [42, 43, 47]. The compositions of WS<sub>2</sub> and WSe<sub>2</sub> were confirmed by the energy-dispersive x-ray spectroscopy, as shown in figure S8.

#### 4.2. Device fabrication

WSe<sub>2</sub> and WS<sub>2</sub> flakes were exfoliated on SiO<sub>2</sub> ( $\sim$ 285 nm)/Si substrates. The WSe<sub>2</sub> and WS<sub>2</sub> layers with different thicknesses were first selected based on their optical contracts and then identified by atomic force microscopy. The targeting WSe<sub>2</sub> or WS<sub>2</sub> thin layers were picked up using a polyvinyl alcohol coated Polydimethylsiloxane stamp and then transferred onto ITO substrates using a dry-transfer method. The WSe<sub>2</sub>/WS<sub>2</sub> heterostructures were fabricated using the same dry-transfer method. We note that all the transfer processes were carried out inside a gloves box with both the H<sub>2</sub>O and O<sub>2</sub> levels below 0.1 ppm. A detailed illustration of the transfer process can be found in figure S1. The samples were annealed in a vacuum (<5 mTorr) at 230 °C for 3 h.

#### 4.3. Probe fabrication

Pipet-based electrochemical probes were fabricated from quartz capillaries (1.2 mm outer diameter, 0.9 mm inner diameter, Sutter) using a laser-based pipet puller (Sutter P-2000). Probes were fabricated using a two-line program: Heat = 750, Fil = 4, Vel = 30, Delay = 135, Pull = 80/Heat = 685, Fil = 3, Vel = 30, Delay = 135, Pull = 150. These probes were filled with an aqueous electrolyte solution containing 100 mM NaI and 10 mM I<sub>2</sub>, and a AgI-coated Ag wire was inserted into the back of the pipet, completing the electrochemical probe. The Ag/AgI wire provided a well-defined reference potential in the electrolyte corresponding to the AgI +  $e^- \rightarrow Ag + I^-$  couple, and all data presented herein is referenced vs this potential.

#### 4.4. PL measurements

For PL mapping, samples were mounted on a 2axis piezoelectric stage (PI P546.2C7) of an inverted optical microscope. The sample was illuminated with a pulsed laser source (485 nm, FWHM  $\approx$  110 ps, Picoquant) focused through a microscope objective (100×, NA = 0.9). PL from a localized region of the sample was collected using the same objective and directed through a non-polarizing beam splitter. One beam was directed onto the slit of a spectrometercharge coupled device (CCD) combination (Andor SR-303i-B, Newton EMCCD) and the other onto an avalanche photodiode micro photon devices (MPD) connected to a TCSPC system (Picoquant Picoharp 300). All instrumentation was controlled through custom LabVIEW software. For the PL spectra acquisition, a Horiba confocal Raman microscope with 532 nm laser excitation was employed.

#### 4.5. SECCM measurements

Samples were mounted on ceramic slides and placed on the stage of an inverted optical microscope. Electrical contact to the sample was made using Cu tape. The electrochemical probe was mounted to a three-axis piezoelectric stage (PI P-611.3S). A patchclamp style amplifier (Dagan CHEM-CLAMP) was employed to provide electrical bias between the sample and Ag/AgI counter electrode (ground). The sample was placed under intermittent (50 Hz) broadband illumination (50 W cm<sup>-2</sup>, Energetiq LDLS) and the electrochemical probe was lowered towards the sample, while a potential difference of -0.5 V was applied to the substrate and the current flowing in the system was monitored. Probe-sample contact was identified by a sudden current spike. Once the contact was established, probe movement was stopped and a triangular potential waveform (2000 mV  $s^{-1}$ ) was applied while the resulting currents were recorded. Upon completion of the waveform, the probe was retracted and moved laterally, where this procedure was repeated. Measurements were taken across a rectangular array of points and current data were recorded as a three-dimensional array. All instrumentation was controlled through custom LabVIEW software and a National Instruments DAQ interface (cDAQ-9174). Photocurrent images and voltammograms at specific points were generated from the raw data via custom python scripts.

#### 4.6. Raman spectroscopy

The Raman spectra were acquired under ambient conditions by a Horiba confocal Raman microscope with a 532 nm laser excitation. A 2400 grooves  $mm^{-1}$  grating was used to achieve a spectral resolution of below 1.4 cm<sup>-1</sup>.

#### 4.7. DFT calculations

The electronic structures of the WSe<sub>2</sub> and WS<sub>2</sub> layers were calculated using a plane wave implementation of DFT in Quantum Espresso [48–50]. We engaged the 2 H stacking in multilayer cases as it is found to be the most stable structure. The lattice constants used in the calculations are consistent with experimental data [51]. A vacuum of at least 20 Å was used along the z-direction to minimize the interaction among the periodic images. Projected augmented wave (PAW) potentials were used to selfconsistently solve the electronic structure with a kpoint mesh of  $12 \times 12 \times 1$ . The cut-off energies for the plane-wave basis states were 60 Ry. The Per-Burke-Ernzerhof (PBE) approximation was used for the exchange-correlation function. The weak van der Waals interaction was included by using a dispersion correction based on Grimme's DFT-D2 method [52, 53].

The WSe<sub>2</sub> /WS<sub>2</sub> heterostructures were constructed with 2H stacking as shown in figures S7(a) and (b). The distance d between  $WSe_2$  and  $WS_2$ which is defined as the distance between neighboring W atom's planes as shown in figure S6(a), was determined by geometry optimization as listed in figure S6(c). The other lattice constants of the heterostructures were kept identical with that of WS<sub>2</sub>. The geometry was optimized using the Broyden-Fletcher-Goldfarb-Shenno minimization technique, with a threshold of the converged structure of energy change per atom smaller than  $1.6 \times 10^{-4}$  Ry/atom. The vacuum spacer (larger than 15 Å) was used for all the heterostructures. PAW potentials were used to self-consistently solve the electronic structure with a k-point mesh of 12  $\times$  12  $\times$  1. The cut-off energy for the plane-wave basis states was 80 Ry. PBE approximation was used for the exchangecorrelation functional. The weak van der Waals interaction was included by a dispersion correction based on the Grimme's DFT-D2 method. We calculated the orbital projected band structures using the Quantum espresso and Wannier90 [54, 55]. We note that the spin-orbital interaction was not included in all calculations.

#### Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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