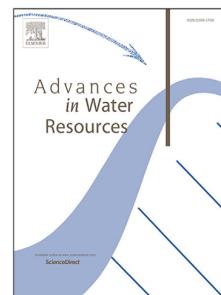


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A screening model for quantifying PFAS leaching in the vadose zone and mass discharge to groundwater

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Abstract

A growing body of site investigations have demonstrated that vadose zones serve as significant long-term sources of PFAS to groundwater. Quantifying PFAS leaching in the vadose zone and mass discharge to groundwater is therefore critical for characterizing, managing, and mitigating long-term contamination risks. Mathematical models representing the PFAS-specific transport and retention processes, including surfactant-induced flow, and rate-limited, nonlinear adsorption at solid–water and air–water interfaces, have been recently developed. While these advanced models provide fundamental insights into the primary processes controlling the long-term retention of PFAS, they are less suitable for screening-type applications due to significant computational cost and the requirement for detailed input parameters. To address this knowledge gap, we develop a simplified model by assuming steady-state infiltration and linear solid-phase and air–water interfacial adsorption; a two-domain model is used to represent kinetic solid-phase adsorption. We derive novel analytical solutions for the simplified model allowing for arbitrary initial conditions. The newly derived analytical solutions are then validated by application to miscible-displacement experiments under a wide range of conditions and by comparisons to a state-of-the-art comprehensive model under both experimental and field conditions applicable to PFAS-contamination sites. Overall, the simplified analytical model provides an efficient and accurate screening-type tool for quantifying long-term PFAS leaching in the vadose zone.

Keywords: per- and polyfluoroalkyl substances (PFAS), leaching, interfacial adsorption, analytical solution, rate-limited adsorption, unsaturated zone

¹ 1. Introduction

2 Per- and polyfluoroalkyl substances (PFAS) have become emerging contaminants of critical concern.
 3 Large-scale manufacturing and wide use of PFAS since the 1940s have led to their ubiquitous presence
 4 in the environment including surface water, soils, sediments, and groundwater. A growing body of site
 5 investigations have established that vadose zones are significant PFAS reservoirs that pose long-term threats
 6 for contaminating groundwater even several decades after the contamination events were stopped (Xiao et al.,

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7 2015; Weber et al., 2017; Dauchy et al., 2019; Høisæter et al., 2019; Anderson et al., 2019; Brusseau et al.,
8 2020; Adamson et al., 2020; Cáñez et al., 2021).

9 Most PFAS are surfactants with unique interfacial properties that distinguish their transport behaviors
10 from that of traditional non-surfactant contaminants. Laboratory measurements and analysis of surface
11 tension data (Brusseau, 2018, 2019; Silva et al., 2019; Schaefer et al., 2019a; Costanza et al., 2019, 2020; Silva
12 et al., 2021; Brusseau & Van Glubt, 2021) and miscible-displacement experiments under water-unsaturated
13 conditions (Lyu et al., 2018; Brusseau et al., 2019b; Lyu et al., 2020; Li et al., 2021; Brusseau et al., 2021)
14 have demonstrated that PFAS tend to accumulate at air–water interfaces in soils, which can greatly increase
15 retention in the vadose zone (e.g., Brusseau, 2018; Guo et al., 2020). Adsorption at the solid–water interfaces
16 resulting from hydrophobic and electrostatic interactions also enhances the retention of PFAS in soils (e.g.,
17 Higgins & Luthy, 2006; Barzen-Hanson et al., 2017; Xiao et al., 2019; Mejia-Avendaño et al., 2020; Wang
18 et al., 2021). Additional processes including volatilization, transformation of precursors, and uptake by biota
19 can add further complexities to the retention of some PFAS in the vadose zone (e.g., Sima & Jaffé, 2020;
20 Sharifan et al., 2021).

21 Mathematical models representing the complex retention and leaching processes of PFAS in soils are
22 critically needed for understanding long-term risks of vadose-zone PFAS as a source of contamination to
23 groundwater. Guo et al. (2020) reported a new mathematical model that accounts for a set of unique
24 transport behaviors of PFAS in the vadose zone, including nonlinear and rate-limited adsorption at solid–
25 water and air–water interfaces in the presence of transient variably saturated flow and surfactant-induced
26 flow. The mathematical model has been validated by application to water-unsaturated miscible-displacement
27 column experiments under a wide range of conditions (El Ouni et al., 2021; Brusseau et al., 2021; Zeng et al.,
28 2021) and applied to simulate long-term PFAS leaching at a model fire training area site (Guo et al., 2020;
29 Zeng et al., 2021). The simulated strong retention of PFAS in the shallow vadose zone is consistent with
30 many prior field observations (e.g., Anderson et al., 2019; Dauchy et al., 2019; Høisæter et al., 2019; Brusseau
31 et al., 2020). Shortly thereafter, a model similar to that of Guo et al. (2020) was independently reported
32 by Silva et al. (2020) where example simulations were presented in one- and two-dimensions (rate-limited
33 adsorption was not considered). More recently, Zeng & Guo (2021) extended the model formulations of Guo
34 et al. (2020) to three dimensions and examined the impact of surfactant-induced flow and preferential flow
35 on long-term PFAS leaching in heterogeneous vadose zones.

36 While the comprehensive models discussed above provide fundamental insights into the primary processes
37 controlling the long-term retention and leaching of PFAS in the vadose zone, their complexity and the asso-
38 ciated significant computational cost make them less suitable for practical screening-type application at field
39 contamination sites, such as for developing initial strategies for characterizing, managing, and mitigating
40 PFAS contamination risks based on limited site information. Screening-type analysis usually employs much
41 simpler analytical or semi-analytical models that are computationally efficient and do not need detailed
42 information for the input parameters and site conditions. Such simple models have been previously demon-

43 strated as useful screening tools for guiding remediation strategies and determining regulatory standards for
 44 non-PFAS contaminants. Examples include the EPA spreadsheet model for subsurface vapor intrusion (US-
 45 EPA, 2017) and REMChlor-MD for modeling long-term matrix diffusion of chlorinated solvent in aquifers
 46 (Falta et al., 2018). However, similar simple models for quantifying PFAS leaching in the vadose zone and
 47 mass discharge to groundwater are to date not available.

48 In the present work, we address this knowledge gap by developing a simplified model for PFAS retention
 49 and leaching in the vadose zone that allows for analytical solutions. Specifically, our model formulation
 50 assumes steady-state infiltration and simplifies the transport processes by linearizing the nonlinear terms for
 51 adsorption at the solid–water and air–water interfaces. Additionally, rate-limited adsorption at the solid–
 52 water interfaces is represented by a two-domain kinetic model. New analytical solutions derived for the
 53 simplified model are validated by application to miscible-displacement experiments for multiple PFAS under
 54 a wide range of conditions as well as via comparisons to simulations produced with a comprehensive numerical
 55 model under both experimental and field conditions. To the best of our knowledge, the analytical solutions
 56 presented here are the first for solute transport that account for the two-domain solid-phase kinetic adsorption
 57 and air–water interfacial adsorption. Finally, we present a workflow to demonstrate the application of the
 58 simplified models for analyzing long-term PFAS leaching in the vadose zone.

59 2. Mathematical model and simplifications

60 We present the mathematical model from simplifying both the variably saturated flow and PFAS transport
 61 processes represented in the model formulations of Guo et al. (2020).

62 2.1. Water flow

63 We consider water flow driven by steady-state infiltration in the vertical dimension of a homogeneous
 64 vadose zone. Water in the vadose zone is assumed unsaturated with a spatially uniform saturation, i.e.,
 65 $\frac{\partial h}{\partial z} = 0$ where h is the water pressure head, and the unsaturated water flow q (cm/s) is driven only by
 66 gravity. Assuming that z is positive downward, from Darcy's law $q = -K \frac{\partial h}{\partial z} (h - z)$, we obtain

$$q = K, \quad (1)$$

67 where K is the unsaturated hydraulic conductivity (cm/s), which can be approximated as an empirical
 68 function of the volumetric water content, θ (–). Here we present the widely used empirical function proposed
 69 by Mualem (1976) and van Genuchten (1980) as an example

$$K(\theta) = K_s S_{w,e}^\lambda \left[1 - \left(1 - S_{w,e}^{1/m} \right)^m \right]^2, \quad (2)$$

70 where K_s is the saturated conductivity (cm/s). $S_{w,e} = \frac{\theta - \theta_r}{\theta_s - \theta_r}$ is the effective water saturation (–), where
 71 θ_r and θ_s are the residual and saturated water contents (cm^3/cm^3), respectively. λ and m are empirical
 72 parameters. λ can vary for different soil media, though it is often set to 0.5 for simplicity. m is related to

73 the pore-size distribution of the soil media and can be determined by fitting the soil water characteristic
 74 function of van Genuchten (1980) to measured datasets. We note that alternative models for K , such as the
 75 equations proposed by Kosugi (1999), may also be employed. The Kosugi model was shown to match better
 76 the measured unsaturated water conductivity than Eq. (2) for some soil media.

77 *2.2. Transport of PFAS*

78 Transport of PFAS in the vertical dimension of a vadose zone may be described by an advection-dispersion
 79 equation coupled with solid-phase and air–water interfacial adsorption terms (e.g., Brusseau, 2020; Guo et al.,
 80 2020)

$$\frac{\partial(\theta C)}{\partial t} + \rho_b \frac{\partial C_s}{\partial t} + \frac{\partial C_{aw}}{\partial t} + \frac{\partial}{\partial z} (\theta v C) - \frac{\partial}{\partial z} \left(\theta D \frac{\partial C}{\partial z} \right) = 0, \quad (3)$$

81 where C is the aqueous concentration ($\mu\text{mol}/\text{cm}^3$). C_{aw} is the adsorption at air–water interfaces ($\mu\text{mol}/\text{cm}^3$).
 82 C_s is the solid-phase adsorption ($\mu\text{mol}/\text{cm}^3$). $v = q/\theta$ is the interstitial porewater velocity (cm/s). $D =$
 83 $\alpha_L v + \tau D_0$ is the dispersion coefficient (cm^2/s), where α_L is the longitudinal dispersivity (cm) and D_0 is the
 84 molecular diffusion coefficient in free water. The tortuosity τ can be approximated as $\tau = \frac{\theta^{7/3}}{\theta_s^2}$ (Millington
 85 & Quirk, 1961).

86 The solid-phase adsorption C_s can be modeled by the nonlinear Freundlich isotherm (Higgins & Luthy,
 87 2006; Wei et al., 2017; Brusseau et al., 2019a; Van Glubt et al., 2020). The fitted exponent parameter in the
 88 Freundlich isotherm was reported to range from 0.75 to 1.1 for multiple PFAS in a wide range of soils and
 89 sediments (Higgins & Luthy, 2006; Guelfo & Higgins, 2013; Van Glubt et al., 2020). A recent study showed
 90 that the fitted exponent parameter ranged from 0.64 to 1.27 (median: 0.82 and mean: 0.85) for PFOS in
 91 114 tropical and temperate soils (Umeh et al., 2021). Because the present study focuses on formulating a
 92 simplified model for which analytical solutions can be derived, we assume that the solid-phase adsorption
 93 can be approximated by a linear isotherm. Kinetics associated with solid-phase adsorption were shown to
 94 be present in both batch and miscible-displacement experiments (Brusseau et al., 2019a; Guelfo et al., 2020;
 95 Schaefer et al., 2021; Zhou et al., 2021). Guelfo et al. (2020) and Schaefer et al. (2021) suggested that kinetic
 96 solid-phase adsorption is only present in real soils with organic carbon or clay content greater than 0. We
 97 use a two-domain model to represent kinetic solid-phase adsorption, i.e., $C_s = C_{s,1} + C_{s,2}$, where $C_{s,1}$ is the
 98 adsorbed concentration in the “instantaneous” sorption domain and $C_{s,2}$ is the adsorbed concentration in
 99 the kinetic sorption domain.

$$C_{s,1} = F_s K_d C, \quad (4)$$

$$\frac{dC_{s,2}}{dt} = \alpha_s [(1 - F_s) K_d C - C_{s,2}], \quad (5)$$

101 where K_d is the solid-phase adsorption coefficient (cm^3/g), F_s is the fraction of sorbent for which sorption
 102 is instantaneous, α_s is the first-order rate constant for kinetic sorption. Miscible-displacement experiments
 103 using soil-packed columns have demonstrated that the kinetics associated with air–water interfacial adsorp-
 104 tion is minimal under steady-state flow conditions (Brusseau, 2020; Brusseau et al., 2021). We thus assume

105 equilibrium air–water interfacial adsorption. The adsorption at air–water interfaces C_{aw} in Eq. (3) is the
 106 product of the surface excess Γ ($\mu\text{mol}/\text{cm}^2$) and the air–water interfacial area A_{aw} (cm^2/cm^3)

$$C_{aw} = \Gamma A_{aw}, \quad (6)$$

107 where the surface excess Γ is a function of the aqueous concentration, $\Gamma = K_{aw}C$. K_{aw} (cm^3/cm^2) is the
 108 air–water interfacial adsorption coefficient, which under the ideal dilute solution assumption (i.e., below the
 109 critical micelle concentration) can be computed based on the Gibbs equation (e.g., Kiss, 2001; Rosen &
 110 Kunjappu, 2012)

$$K_{aw} = \frac{\Gamma}{C} = -\frac{1}{\chi R_g T C} \left(\frac{\partial \sigma}{\partial \ln C} \right)_T, \quad (7)$$

111 where R_g is the universal gas constant (J/K/mol) and T is temperature (K). χ is a coefficient that equals
 112 to 1 for a nonionic PFAS or an ionic PFAS in the presence of a swamping amount of electrolyte, or 2 for
 113 an ionic PFAS with no swamping electrolyte. Surface tension σ for a solution with a single PFAS can be
 114 modeled by the Szyszkowski equation (e.g., Chang & Franses, 1995; Adamson & Gast, 1997)

$$\sigma = \sigma_0 \left[1 - b \ln \left(1 + \frac{C}{a} \right) \right], \quad (8)$$

115 where σ_0 is the surface tension of the aqueous solution with no dissolved PFAS (dyn/cm), and a ($\mu\text{mol}/\text{cm}^3$)
 116 and b (–) are fitting parameters to experimental data. Substituting Eq. (8) into Eq. (7) yields

$$K_{aw} = \frac{1}{\chi R_g T} \frac{\sigma_0 b}{a + C}, \quad (9)$$

117 Substituting Eqs. (4–6) to Eq. (3), we obtain a linear advection-dispersion equation (Eq. (10)) coupled
 118 with a two-domain kinetic solid-phase adsorption model (Eq. (5)).

$$\beta R \frac{\partial C}{\partial t} + \frac{\rho_b \alpha_s}{\theta} [(1 - F_s) K_d C - C_{s,2}] + \frac{\partial}{\partial z} (vC) - \frac{\partial}{\partial z} \left(D \frac{\partial C}{\partial z} \right) = 0, \quad (10)$$

119 where the retardation factor $R = 1 + R_s + R_{aw}$ and $\beta = (1 + F_s R_s + R_{aw}) / R$. $R_s = \rho_b K_d / \theta$ and $R_{aw} =$
 120 $K_{aw} A_{aw} / \theta$ represent the retardation from solid-phase and air–water interfacial adsorption, respectively.

121 For PFAS migration in the vadose zone, we consider the following initial and boundary conditions for
 122 Eqs. (10) and (5) assuming that PFAS are released to a semi-infinite vadose zone at a constant concentration
 123 C_0 for the time period $0 < t < t_0$.

$$C(z, 0) = C_i(z), \quad (11)$$

$$C_{s,2}(z, 0) = C_{s,2,i}(z), \quad (12)$$

$$\left(-D \frac{\partial C}{\partial z} + vC \right) |_{z=0} = \begin{cases} vC_0 & 0 < t \leq t_0 \\ 0 & t \geq t_0 \end{cases}, \quad (13)$$

$$\frac{\partial C}{\partial z} |_{z=+\infty} = 0. \quad (14)$$

127 where $C_i(z)$ and $C_{s,2,i}(z)$ are initial concentrations in the aqueous phase and in the kinetic sorption domain,
 128 respectively. Assuming equilibrium initially, $C_{s,2,i} = (1 - F_s) K_d C_i$.

129 We note that the air–water interfacial area (A_{aw}) in Eq. (6) in soils is comprised of two types including
 130 capillary interfaces associated with menisci between bulk air and water and film-related interfaces associated
 131 with wetting films surrounding grain surfaces, both of which are relevant for PFAS transport as demonstrated
 132 by prior miscible-displacement experiments (Lyu et al., 2018; Brusseau et al., 2019b; Lyu et al., 2020; Li
 133 et al., 2021; Brusseau et al., 2021; Brusseau & Guo, 2021). The combination of the two, i.e., the total air–
 134 water interfacial area, is considered in the present study. The total A_{aw} usually increases as S_w decreases.
 135 We approximate A_{aw} as a second degree polynomial function of water saturation S_w

$$A_{aw} = x_2 S_w^2 + x_1 S_w + x_0, \quad (15)$$

136 where x_2 , x_1 , and x_0 are parameters that can be determined by fitting to air–water interfacial area data
 137 measured by aqueous interfacial tracer methods. When measured A_{aw} based on aqueous interfacial tracer
 138 methods are not available, A_{aw} may be estimated using the thermodynamic-based approach (Leverett, 1941;
 139 Morrow, 1970; Bradford & Leij, 1997). The thermodynamic-based method is described in more detail in
 140 section 5 and employed for the soil media therein.

141 **3. Analytical solutions**

142 We derive new analytical solutions for Eqs. (10) and (5) subject to the initial and boundary conditions
 143 of Eqs. (11–14) using the Laplace transform. Similar derivation procedures were reported in the literature
 144 for solute transport in the presence of kinetic solid-phase adsorption with no air–water interfacial adsorption
 145 (Lindstrom & Narasimham, 1973; van Genuchten & Wagenet, 1989; Toride et al., 1993), we therefore only
 146 present the final form of the analytical solutions with the detailed and rather tedious derivation steps omitted.
 147 To the best of our knowledge, the analytical solution reported here is the first that accounts for the two-
 148 domain solid-phase kinetic adsorption and air–water interfacial adsorption.

149 For convenience, we define the following dimensionless variables and parameters $T = vt/L$, $T_0 = vt_0/L$,
 150 $Z = z/L$, $P = vL/D$, $\omega_s = \alpha_s (1 - \beta_s) (1 + R_s) L/v$, where L is an arbitrary distance from the land surface,
 151 which is taken as the depth of the vadose zone in the present study, and $\beta_s = (1 + F_s R_s)/(1 + R_s)$. ω_s is
 152 often referred to as the Damköhler number, which represents the ratio between the characteristic time scales
 153 of transport (i.e., advection in the present study) and reaction (i.e., kinetic solid-phase adsorption in the
 154 present study).

155 The analytical solutions for the aqueous concentration $C(Z, T)$ and adsorbed concentration at the kinetic
 156 sorption domain $C_{s,2}(Z, T)$ can be considered as the sum of the solution for the boundary value problem
 157 (BVP) and the solution for the initial value problem (IVP), i.e., $C(Z, T) = C^{BVP}(Z, T) + C^{IVP}(Z, T)$ and
 158 $C_{s,2}(Z, T) = C_{s,2}^{BVP}(Z, T) + C_{s,2}^{IVP}(Z, T)$. The solutions for the boundary value problem are

$$C^{BVP}(Z, T) = \begin{cases} C_0 A(Z, T), & 0 < T \leq T_0 \\ C_0 A(Z, T) - C_0 A(Z, T - T_0), & T > T_0 \end{cases} \quad (16)$$

$$C_{s,2}^{BVP}(Z,T) = \begin{cases} C_0(1-F_s)K_d B(Z,T), & 0 < T \leq T_0 \\ C_0(1-F_s)K_d B(Z,T) - C_0(1-F_s)K_d B(Z,T-T_0), & T > T_0 \end{cases} \quad (17)$$

159 where

$$A(Z,T) = \int_0^T g(Z,\tau) J(a_1, b_1) d\tau, \quad (18)$$

$$B(Z,T) = \int_0^T g(Z,\tau) [1 - J(b_1, a_1)] d\tau, \quad (19)$$

$$J(a_1, b_1) = 1 - e^{-b_1} \int_0^{a_1} e^{-\lambda} I_0[2\sqrt{b_1\lambda}] d\lambda, \quad (20)$$

$$a_1 = \frac{\omega_s \tau}{\beta R}, \quad (21)$$

$$b_1 = \frac{\omega_s (T - \tau)}{(1 - \beta_s)(1 + R_s)}, \quad (22)$$

$$g(Z,\tau) = \left(\frac{P}{\pi \beta R \tau} \right)^{1/2} e^{-\left[\frac{P(\beta R Z - \tau)^2}{4\beta R \tau} \right]} - \frac{P}{2\beta R} e^{PZ} \operatorname{erfc} \left[\left(\frac{P}{4\beta R \tau} \right)^{1/2} (\beta R Z + \tau) \right]. \quad (23)$$

160 In addition to the volume-averaged resident concentration $C(Z,T)$ (i.e., mass of solute per unit volume
161 of fluid), the flux-averaged concentration (i.e., mass of solute per unit volume of fluid passing through a
162 given cross-section) may also be of interest when simulating the breakthrough concentrations for miscible-
163 displacement experiments (Kreft & Zuber, 1978; van Genuchten & Parker, 1984). For flux-averaged concen-
164 tration, $g(Z,\tau)$ is given by

$$g(Z,\tau) = \frac{Z}{\tau} \left(\frac{P\beta R}{4\pi\tau} \right)^{1/2} e^{-\left[\frac{P(\beta R Z - \tau)^2}{4\beta R \tau} \right]}. \quad (24)$$

165 The Goldstein's J function in Eq. (20) can be approximated in various ways as summarized by van
166 Genuchten (1981). In the present study, we employ the approximation based on the modified Bessel function
167 given by Lindstrom & Stone (1974).

168 The solutions for the initial value problem are

$$C^{IVP}(Z,T) = e^{-\frac{\omega_s T(1-F_s)R_s}{(1-\beta_s)(1+R_s)\beta R}} G(Z,T) + \frac{\omega_s}{(1-\beta_s)(1+R_s)} \int_0^T H(T,\tau) G(Z,\tau) d\tau, \quad (25)$$

169 where

$$G(Z,T) = \int_0^{+\infty} C_i(\xi) \left\{ \frac{e^{-\frac{P\beta R}{4T}(Z-\xi-T/\beta/R)^2} + e^{-\xi P - \frac{P\beta R}{4T}(Z+\xi-T/\beta/R)^2}}{2\sqrt{\frac{\pi T}{\beta R P}}} - \frac{P}{2} e^{PZ} \operatorname{erfc} \left(\frac{Z+\xi+T/\beta/R}{2\sqrt{\frac{T}{\beta R P}}} \right) \right\} d\xi, \quad (26)$$

170

$$H(T, \tau) = \frac{R_s (1 - F_s)}{\beta R} e^{-\frac{\omega_s (T - \tau)}{(1 - \beta_s)(1 + R_s)} - \frac{\omega_s \tau (1 - F_s) R_s}{(1 - \beta_s)(1 + R_s) \beta R}} \\ \left\{ I_0 \left[\frac{2\omega_s}{(1 - \beta_s)(1 + R_s)} \sqrt{\frac{R_s (1 - F_s) (T - \tau) \tau}{\beta R}} \right] + \frac{\tau I_1 \left[\frac{2\omega_s}{(1 - \beta_s)(1 + R_s)} \sqrt{\frac{R_s (1 - F_s) (T - \tau) \tau}{\beta R}} \right]}{\sqrt{R_s (1 - F_s) (T - \tau) \tau / \beta R}} \right\}. \quad (27)$$

$$C_{s,2}^{IVP}(Z, T) = C_{s,2,i}(Z) e^{-\frac{\omega_s T}{(1 - \beta_s)(1 + R_s)}} + \frac{\omega_s}{(1 - \beta_s)(1 + R_s)} \int_0^T (1 - F_s) K_d G(Z, \tau) H_{s,2}(T, \tau) d\tau, \quad (28)$$

171 where

$$H_{s,2}(T, \tau) = e^{-\frac{\omega_s (T - \tau)}{(1 - \beta_s)(1 + R_s)} - \frac{\omega_s \tau (1 - F_s) R_s}{(1 - \beta_s)(1 + R_s) \beta R}} \\ \left\{ I_0 \left[\frac{2\omega_s}{(1 - \beta_s)(1 + R_s)} \sqrt{\frac{R_s (1 - F_s) (T - \tau) \tau}{\beta R}} \right] + \sqrt{\frac{R_s (1 - F_s) (T - \tau)}{\beta R \tau}} I_1 \left[\frac{2\omega_s}{(1 - \beta_s)(1 + R_s)} \sqrt{\frac{R_s (1 - F_s) (T - \tau) \tau}{\beta R}} \right] \right\}. \quad (29)$$

172 We make two comments on the analytical solutions presented above. 1) The analytical solutions can be
 173 greatly simplified when kinetic solid-phase adsorption is not considered. In that case, $F_s = 1$, $C_{s,2} = 0$,
 174 $J(a_1, b_1) = 1$, and $A(Z, T)$ can be integrated analytically. The analytical solution for this special case with
 175 no kinetic solid-phase adsorption is presented in the Appendix. 2) The simplified model in section 2 is
 176 more general than the analytical solutions presented in section 3 because the transport equation (Eq. (10))
 177 can involve spatial heterogeneities. For example, the solid-phase adsorption coefficient K_d can be a depth-
 178 dependent function to reflect the change of sorption capacities along depth, e.g., decrease of organic carbon
 179 content along the soil profile. Additionally, the more general Freundlich nonlinear adsorption model can also
 180 be used for representing solid-phase adsorption. However, the presence of nonlinearities and heterogeneities
 181 would prevent the transport equation from being solved analytically.

182 4. Model validation and evaluation

183 We validate the simplified analytical model by simulating breakthrough curves measured in multiple
 184 miscible-displacement experiments reported in the literature and by conducting simulations of PFAS leaching
 185 in the vadose zone at a model fire training area site under field-relevant conditions. The analytical-based
 186 simulations are in both cases compared to numerical solutions of the full-process model of Guo et al. (2020).

187 4.1. Simulating miscible-displacement experiments

188 We simulate three sets of PFAS unsaturated miscible-displacement experiments reported in the literature.
 189 All of the experiments were conducted using columns packed with a commercially available natural quartz
 190 sand (UNIMIN Corp.) referred to as Accusand, which has a mean grain diameter of 0.35 mm and a total

191 organic carbon content of 0.04%. Aggregated data for the air–water interfacial area under a wide range
 192 of water saturations for Accusand were summarized in Jiang et al. (2020). The air–water interfacial area
 193 measured by aqueous interfacial tracer methods was fitted to a second degree polynomial function of water
 194 saturation (Eq. (15); $x_2 = 548.54$, $x_1 = -1182.5$, $x_0 = 633.96$) by Guo et al. (2020), and is employed here
 195 for simulating the experiments.

196 The first set of experiments were conducted for PFOA at three different input concentrations (0.01, 0.1,
 197 and 1 mg/L), but only the arrival fronts of the breakthrough curves were measured (Lyu et al., 2018). The
 198 second set of experiments was conducted for PFOS at an input concentration of 0.1 mg/L (Brusseau et al.,
 199 2021). The third set of experiments was conducted for hexafluoropropylene oxide dimer acid (HFPO-DA,
 200 also known as GenX) at an input concentration of 10 mg/L (Yan et al., 2020). Full breakthrough curves
 201 were measured for both the second and third sets of experiments. The water saturation of the sand column
 202 was 0.68, 0.68, and 0.64 for the three sets of experiments, respectively.

203 All of the miscible-displacement experiments were conducted using a background electrolyte solution of
 204 0.01 M NaCl solution. The surface tension of the NaCl solution with no PFAS is $\sigma_0 = 71.4$ dyn/cm. The
 205 Szyskowski parameters for the five PFAS in the NaCl solution are: PFBA ($a = 4702.6$ mg/L, $b = 0.19$),
 206 PFHxA ($a = 502.1$ mg/L, $b = 0.17$), PFOA ($a = 78.6$ mg/L, $b = 0.2$), PFOS ($a = 5$ mg/L, $b = 0.1$), GenX
 207 ($a = 109$ mg/L, $b = 0.1$). The hydraulic parameters of the sand were measured in the lab and were reported
 208 in Guo et al. (2020). The solid-phase adsorption parameters were determined from transport experiments
 209 conducted under water-saturated conditions. It is important to point out that all of the parameters are
 210 determined independently with no fitting or calibration, thus the model simulations are predictions of the
 211 experiments and comparisons between the simulations and measurements represent a direct validation test
 212 of the model.

213 The experimental data and the simulations from both the simplified analytical model and the full-
 214 process numerical model are presented in Figure 1. The flux-averaged concentration at the outlet is used
 215 in the analytical solution. The results show that the predictions from both the analytical and numerical
 216 models agree well with the experimental data. The case that sees some deviation is PFOA with an input
 217 concentration of 0.1 mg/L in the first set of experiments. This may be caused by variability in the kinetics of
 218 the solid-phase adsorption among the three columns in this set of experiments—the kinetic parameters were
 219 determined from one of the columns under saturated condition and then employed for all three columns.
 220 The comparisons in the semi-log plots (d-f) are generally consistent with those in the arithmetic plots
 221 (a-c). The low concentration data points at approximately 0.2 pore volume for PFOA (d) and 17 pore
 222 volumes for GenX (f) are near the detection limit of the analytical method and hence may not be accurate.
 223 Some deviation between the model simulations and the experimental data is observed for the two data
 224 points at approximately 12 and 13 pore volumes for GenX. This deviation indicates that there may be
 225 nonideal adsorption kinetics that are not captured by the two-domain kinetic sorption model employed in
 226 the simulations. According to the data and analysis presented in Brusseau et al. (2019a), this long tailing

227 behavior observed for GenX is most likely caused by nonideal adsorption at the solid surfaces. We would
 228 like to point out that Guelfo et al. (2020)—using a similar sand but with a total organic carbon content
 229 of 0—concluded that the solid-phase adsorption is not rate limited under the conditions examined in their
 230 experiments.

231 It is interesting that the analytical solutions are almost identical to the numerical solutions from the
 232 full-process model for all of the experiments. This implies that the additional processes included in the
 233 full-process model have a minimal impact on PFAS transport under the specific conditions employed in the
 234 experiments, i.e., relatively low input concentrations. These observations are consistent with the results
 235 reported in Brusseau et al. (2021), which concluded that surfactant-induced flow and nonlinearity in air-
 236 water interfacial adsorption are insignificant when the input concentration is sufficiently below the critical
 237 reference concentration (i.e., the concentration corresponding to 2.5% of reduction in surface tension). Given
 238 that the simulations are predictions with no parameter fitting, the excellent agreement with the experimental
 239 data and the full-process numerical model demonstrates the validity of the simplified analytical model for
 240 representing the transport processes of PFAS in water-unsaturated miscible-displacement experiments.

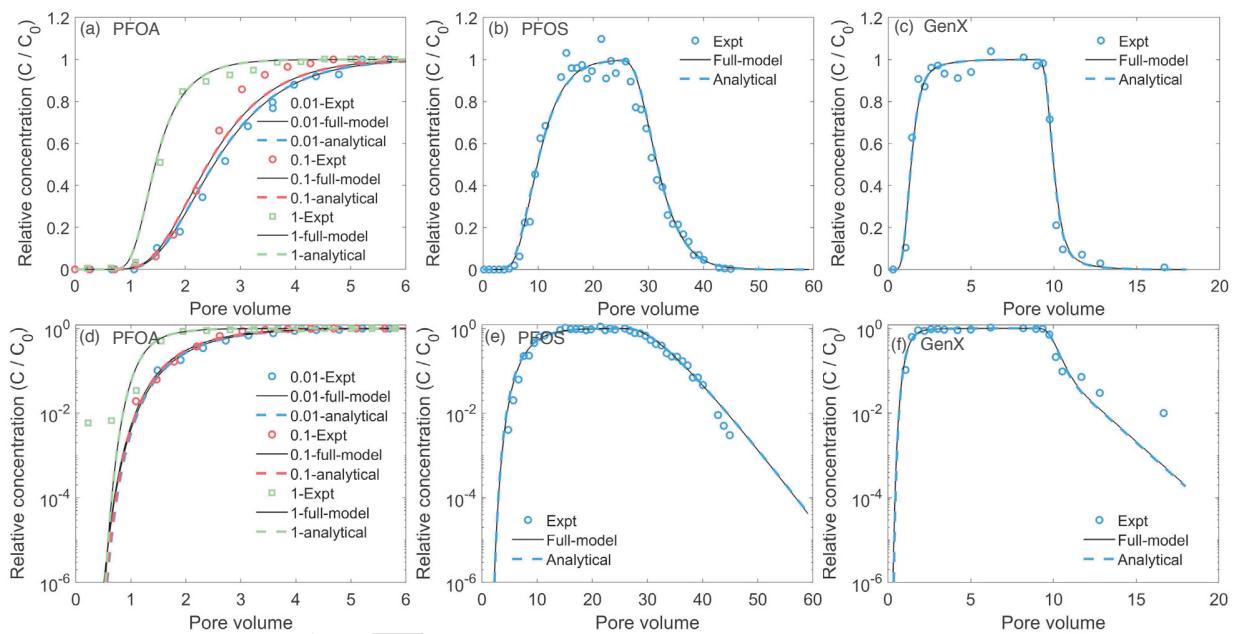


Figure 1: Comparisons of the breakthrough curves simulated by the simplified analytical model (dashed lines) and full-process numerical model (solid lines), and measured (symbols) from the miscible-displacement experiments under water-unsaturated conditions. (a), (b), and (c) correspond to the three sets of miscible-displacement experiments described in section 4.1, respectively. (d), (e), and (f) are the semi-log version of the plots.

241 4.2. Simulating PFAS retention and leaching at a model AFFF-impacted fire training area site

242 We further evaluate the simplified analytical model by comparing it to the full-process numerical model
 243 for simulating long-term retention and leaching of PFAS in the vadose zone under field-relevant conditions.

244 We consider a model aqueous film-forming foam (AFFF)-impacted fire training area site with a 30-year
 245 contamination period (PFAS are being released to the vadose zone due to regular fire training activities)
 246 and a 50-year post-contamination period (fire training activities are stopped and no additional PFAS are
 247 being released to the vadose zone). A 4-m deep vadose zone is assumed homogeneous and is composed of
 248 one of two porous media (Accusand and Vinton soil) for which extensive prior laboratory measurements
 249 are available. The detailed hydraulic and transport parameters for Accusand and Vinton soil were reported
 250 in Guo et al. (2020). We consider four representative PFAS including two short-chain compounds (PFPeA
 251 and PFHxS) and two long-chain compounds (PFOA and PFOS). As suggested by Guo et al. (2020) based
 252 on standard practices at fire training area sites, the fire training is assumed to occur every ten days with
 253 each training lasting for 30 mins leading to a total infiltration of 0.0458 cm of diluted AFFF solution per
 254 training session. PFAS composition in AFFF varies among different products and in different years (Houtz
 255 et al., 2013). Here we adopt the composition reported in Høisæter et al. (2019) for a commercial AFFF.
 256 With a 1:100 dilution, the concentrations for PFPeA, PFHxS, PFOA, and PFOS are 0.23, 7.1, 0.9, and 100
 257 mg/L, respectively. The surface tension data for the PFAS measured in synthetic groundwater are used to
 258 determine the Szyskowski parameters, which are presented together with other PFAS in section 5 (Table
 259 2). Similar to the simulations reported in Guo et al. (2020), rainfall and evapotranspiration data at 30-min
 260 resolution from a site in Arizona (AZ) and a site New Jersey (NJ) downloaded from the AmeriFlux database
 261 (URL: <https://ameriflux.lbl.gov/>) are used to represent semiarid and humid regions, respectively.

262 Both models consider a one-dimensional domain along the vertical dimension of the vadose zone. The
 263 numerical model employs a uniform grid ($\Delta z=1$ cm). Free drainage (i.e., normal gradient of capillary
 264 pressure is zero) and zero dispersion (i.e., advective flux only) are assumed at the bottom boundary. The
 265 full-process model accounts for surfactant-induced flow, rate-limited and nonlinear solid-phase adsorption,
 266 and rate-limited and nonlinear air–water interfacial adsorption (Guo et al., 2020). The coupled Richards'
 267 equation and nonlinear advection-dispersion equation are solved in a fully implicit numerical framework by
 268 Newton-Raphson iterations. Further details about the model setup and numerical algorithms for the full-
 269 process model can be found in Guo et al. (2020). For the simplified analytical model, we need to make three
 270 simplifications to represent the field conditions. 1) Since the analytical solution can only represent steady-
 271 state infiltration, we take the average annual net infiltration rate computed from the numerical simulations
 272 and convert it to steady-state infiltration. 2) We also need to compute the average PFAS infiltration and
 273 convert it to steady-state infiltration during the active-contamination period. 3) Finally, the nonlinear
 274 solid-phase adsorption and air–water interfacial adsorption both need to be linearized; the linear solid-phase
 275 adsorption coefficients $K_d = K_f C_{rep}^{N-1}$ are computed at representative concentration values (see Table 1),
 276 while the constant air–water interfacial adsorption coefficient K_{aw} is computed at $C = 0$ mg/L for simplicity.

277 Comparisons between the simulations from the simplified analytical model and the full-process numerical
 278 model are presented in Figures 2 and 3. Despite the various assumptions employed by the analytical model,
 279 the simplified analytical model agrees well with the full-process numerical model for the simulated retention

Soil media	PFAS	K_f (mg/kg)/(mg/L) ^N	N	C_{rep} mg/L	K_d cm ³ /g	F_s —	α_s 1/hour
Accusand	PFPeA	0.0211	0.87	0.005	0.0420	0.4	5.9
	PFHxS	0.0213	0.81	0.15	0.0305	0.1	3.1
	PFOA	0.1	0.87	0.016	0.1712	0.4	5.9
	PFOS	0.15	0.81	1	0.15	0.1	3.1
Vinton	PFPeA	0.122	0.87	0.005	0.2429	0.16	0.9
	PFHxS	0.156	0.77	0.15	0.2413	0.16	0.9
	PFOA	0.58	0.87	0.016	0.9929	0.16	0.9
	PFOS	1.11	0.77	1	1.11	0.16	0.9

Table 1: Parameters for the solid-phase adsorption of four PFAS (PFPeA, PFHxS, PFOA, and PFOS) in Accusand and Vinton soil. C_{rep} is the representative concentration at which the nonlinear Freundlich isotherm is linearized to a linear isotherm ($K_d = K_f C_{rep}^{N-1}$) for the simplified analytical model.

(i.e., mass remaining in the vadose zone) and cumulative mass discharge to groundwater (Figure 2) as well as the time-dependent spatial profiles of PFAS concentrations in the vadose zone (Figure 3). The exception is PFOS, where the simplified analytical model substantially underestimates the leaching compared to the full-process numerical model.

The underestimated leaching observed for PFOS may be attributed to two of the assumptions made in the simplified analytical model: 1) steady-state infiltration and 2) linear air–water interfacial adsorption. While transient variably saturated flow due to time-dependent rainfall infiltration does not substantially change water saturation at deeper locations in the vadose zone, it leads to significant changes in the water saturation near the land surface. The increases in water saturation during rainfall events destroy air–water interfaces and reduce air–water interfacial adsorption, which then leads to accelerated leaching of PFAS. This phenomenon has a more significant impact on the leaching of PFOS because it is more strongly retained in soils and stays in the shallow vadose zone for a longer period of time. A close inspection also reveals that the impact of transient infiltration has a greater impact during the active contamination period because transient infiltration dynamically redistributes the released PFAS near the land surface. This is not accounted for in the simplified analytical model so its simulated concentration profiles deviate from those simulated by the full-process model during the active contamination period ($t \leq 30$ years), especially near the land surface. Concomitantly, the release concentration of PFOS (100 mg/L) is the highest among the four PFAS, which leads to stronger nonlinear air–water interfacial adsorption. Therefore, using the maximum $K_{aw} = 0.048$ cm³/cm² (i.e., $C = 0$ mg/L) in the analytical solution underestimates leaching of PFOS in the vadose zone.

To further illustrate the influence of the two assumptions discussed above and to explore ways to improve the prediction of the simplified analytical model, we conduct two sets of additional simulations for PFOS using the simplified analytical model. The first set of simulations uses $K_{aw} = 0.038$ cm³/cm² corresponding to a

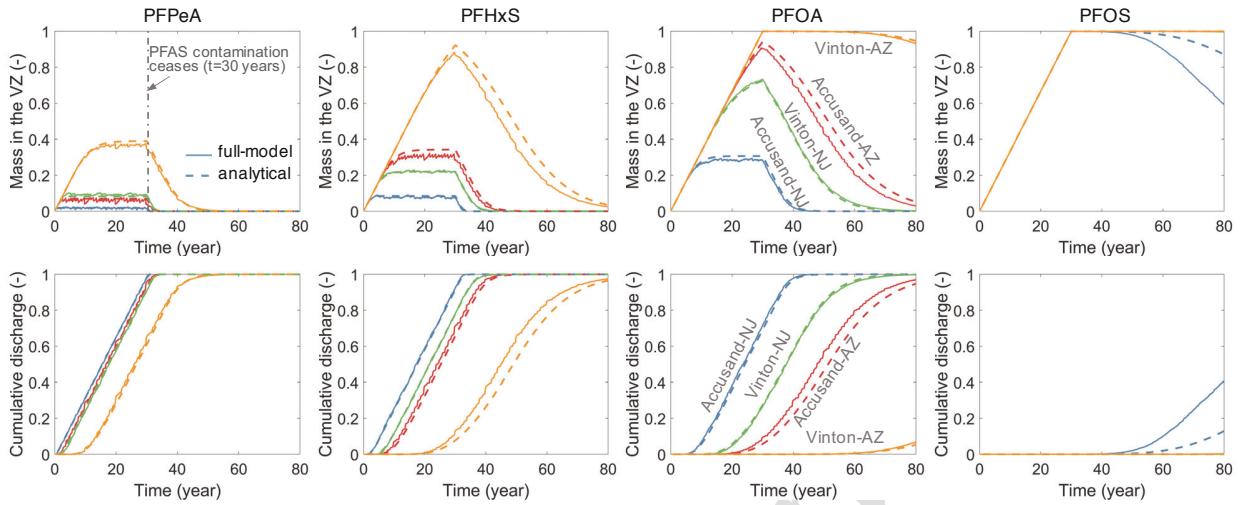


Figure 2: Comparisons between the simplified analytical model and the full-process numerical model for the simulated PFAS mass retained in the vadose zone (row 1) and the cumulative mass discharge to groundwater (row 2) over time. The four columns correspond to the four PFAS (PFPeA, PFHxS, PFOA, PFOS). Both the mass in the vadose zone and cumulative mass discharge are normalized by the total mass released to the vadose zone during the active-contamination period.

representative aqueous concentration in the vadose zone ($C_{rep} = 1 \text{ mg/L}$). The representative concentration is estimated from the original simulated plume (i.e., assuming maximum K_{aw}). Note that the representative aqueous concentration in the vadose zone is substantially lower than the release concentration (100 mg/L) for PFOS. This is because the majority of the PFOS is adsorbed at the solid–water and air–water interfaces, leaving only a small fraction in the aqueous phase. The second set of simulations—in addition to using K_{aw} at a representative concentration—uses the solution of the full-process numerical model at $t=30$ years as the initial condition and only focuses on simulating post contamination. Comparisons between the two additional simulations with the original simulations are presented in Figure 4. The scenario for Accusand and NJ climate is used as an example. The results show that using the representative K_{aw} leads to greater leaching and a better agreement with the full-process numerical model (see the first two rows of Figure 4). The post-contamination simulation that uses the 30-year solution of the full-process numerical model as the initial condition further improves the prediction of the simplified analytical model. The above results and analysis demonstrate that the deviations observed for PFOS in Figures 2 and 3 are indeed in part caused by the steady-state infiltration and linear air–water interfacial assumptions employed in the original simulations. Furthermore, the simplified analytical model can be improved by using a representative aqueous concentration to compute K_{aw} , and when simulating post contamination, which would be the case for most of the legacy contamination sites.

We point out that the PFAS contamination scenarios considered here—AFFF-impacted fire training area sites—are among the PFAS source zones with the highest concentrations as demonstrated by many prior field investigations (e.g., Anderson et al., 2019; Brusseau et al., 2020). PFAS concentrations at other

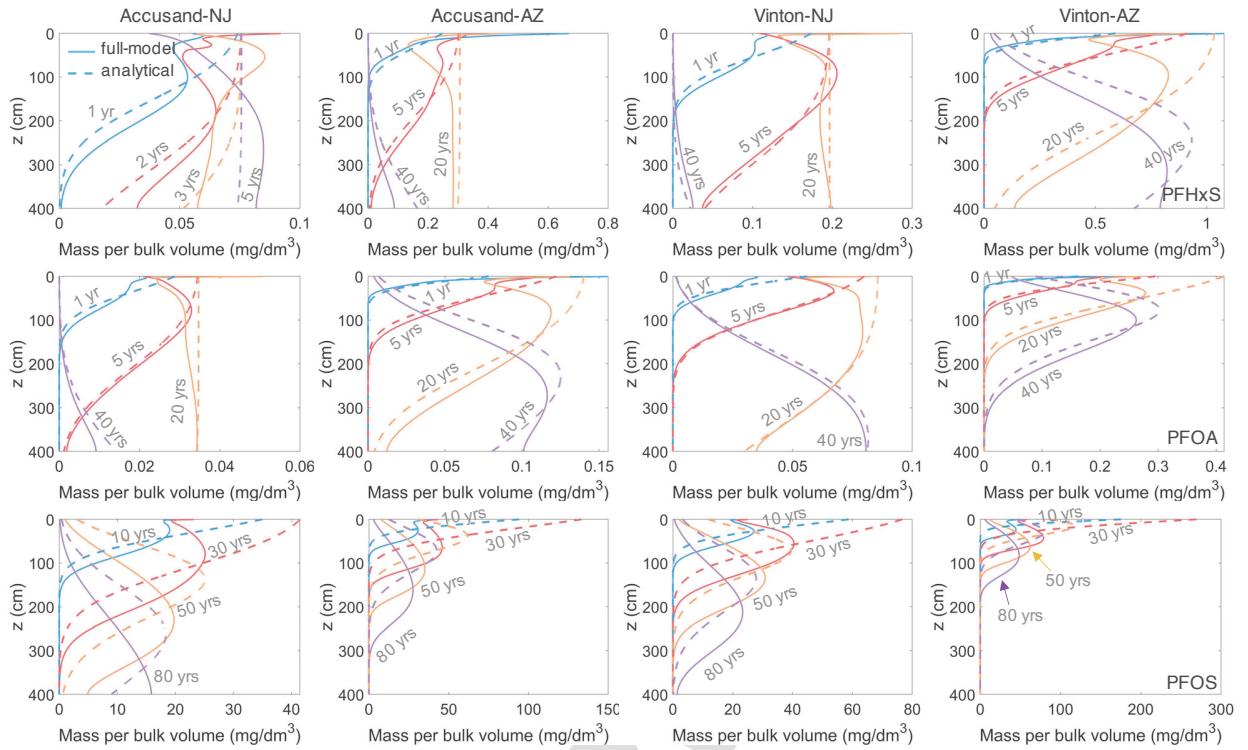


Figure 3: Comparisons between the simplified analytical model and the full-process numerical model for the simulated time-dependent spatial concentration profiles of PFAS. The mass concentration per bulk volume of soil media represents the combination of PFAS dissolved in the aqueous phase, and adsorbed at the solid–water and air–water interfaces. The three rows correspond to the three PFAS (PFHxS, PFOA, and PFOS). The results for PFPeA are not shown because most of the PFPeA mass is discharged to groundwater shortly after the contamination stops at $t = 30$ years. The four columns denote the four different scenarios, i.e., soil media (Accusand and Vinton soil) and climatic conditions (“AZ” denotes Arizona and “NJ” denotes New Jersey).

322 source zones including agricultural lands that receive PFAS-contaminated biosolids and irrigation water and
 323 wastewater treatment plant sites are often several orders of magnitude lower (e.g., Brusseau et al., 2020).
 324 Therefore, it is expected that the linear air–water interfacial adsorption employed in the simplified analytical
 325 model would be more appropriate for other source zones compared to the simulations presented here for the
 326 AFFF-impacted fire training area sites.

327 Finally, we note that there is an ongoing debate as to whether the air–water interfacial adsorption can
 328 be considered linear at lower concentrations (Schaefer et al., 2019a; Arshadi et al., 2020; Schaefer et al.,
 329 2020), i.e., whether Eq. (9) or another equation that represents Freundlich adsorption should be used to
 330 compute the air–water interfacial coefficient. Some additional data and analyses were recently added to this
 331 discussion. Brusseau (2021) reported that the air–water interfacial adsorption of two hydrocarbon surfactants
 332 (SDS and SDBS) determined by Eq. (9) matches with the air–water interfacial adsorption measured directly
 333 by neutron reflectometry for concentrations down to lower than 10^{-5} M. In another study, Brusseau et al.

334 (2021) employed miscible-displacement data of PFOA at a concentration of $C = 1 \mu\text{g/L}$ and showed that the
 335 air–water interfacial coefficient computed from the experimental breakthrough curve matches well with that
 336 determined by Eq. (9). Nevertheless, further research and data are needed to test the potential nonlinearity
 337 of air–water interfacial adsorption at lower concentrations for a wider range of PFAS and under a broader
 338 range of conditions.

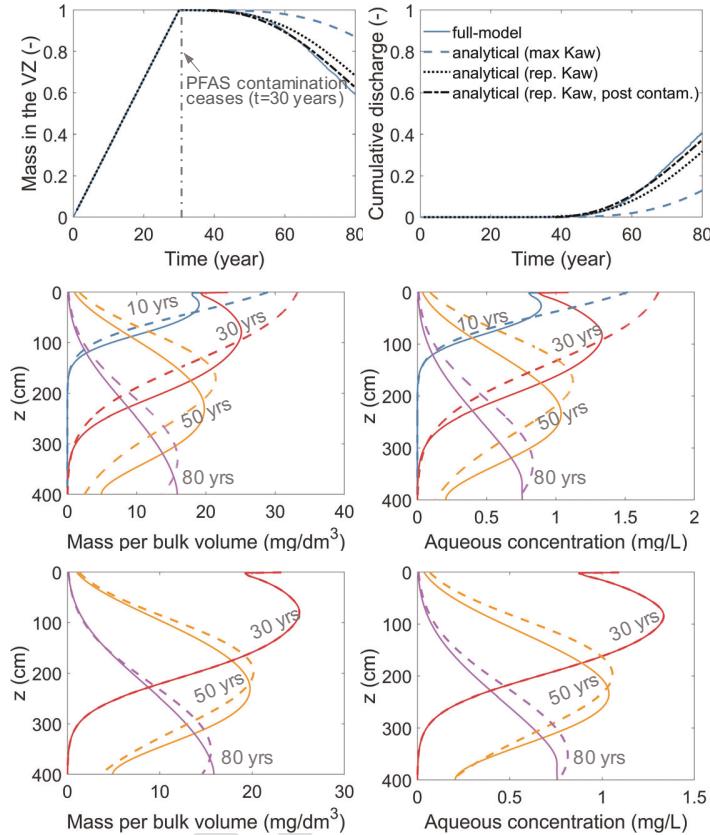


Figure 4: Simulated long-term retention and leaching of PFOS in the vadose zone using the simplified analytical model with different initial conditions and air–water interfacial adsorption coefficients. The PFOS mass retained in the vadose zone and the cumulative mass discharge to groundwater are shown in the first row, both of which are normalized by the total mass of PFOS released to the vadose zone during the active-contamination period. The spatial profiles of PFOS concentration are presented in the second row (the simulation using K_{aw} at C_{rep}) and third row (the simulation using K_{aw} at C_{rep} and only considers post contamination). The mass concentration per bulk volume of soil media represents the combination of PFOS dissolved in the aqueous phase, and adsorbed at the solid–water and air–water interfaces. All of the simulations are for the scenario of Accusand under NJ climate.

339 **5. Demonstration of model application**

340 We present a workflow to demonstrate how to employ the simplified analytical model as a screening
 341 tool for analyzing PFAS retention and leaching at field contamination sites. We take a model AFFF-
 342 impacted fire training area site as an example for the demonstration. Suppose we are interested in quantifying

343 the leaching of nine representative PFAS varying in headgroups and chain lengths (six PFCAs and three
 344 perfluoroalkanesulfonic acids (PFSAs)) in a homogeneous vadose zone represented by six soils. The annual
 345 net water recharge rate is assumed 30 cm. Similar to the scenarios considered in section 4.2, we consider an
 346 active contamination period of 30 years followed by 50 years of post contamination.

PFAS	<i>a</i> mg/L	<i>b</i> –	<i>M</i> g/mol	<i>D</i> ₀ (×10 ⁻⁶) cm ² /s	Concentration mg/L
PFPeA	3168.6	0.22	264.05	12	0.23
PFHxA	1350.42	0.21	314.05	7.8	0.75
PFHpA	345.86	0.22	364.06	9.3	0.3
PFOA	62.11	0.19	414.07	4.9	0.9
PFNA	5.11	0.16	464.08	2.93	0.0031
PFDA	3.7	0.17	514.08	2.27	0.0015
PFBS	2400.8	0.15	300.1	11	1.4
PFHxS	160.05	0.14	400.12	4.5	7.1
PFOS	3.65	0.12	500.13	5.4	100

Table 2: Parameters for PFAS including Szyskowski parameters for surface tension, molecular weight, molecular diffusion coefficients, and the release concentrations in the diluted AFFF solution. The surface tension parameters for the PFCAs and PFSAs were reported in Silva et al. (2019) and Silva et al. (2021), respectively. The molecular diffusion coefficients were reported in Schaefer et al. (2019b). The PFAS concentrations in the diluted AFFF solution are estimated from a commercial AFFF product reported in Høisæter et al. (2019). Note that the release concentrations need to be converted to C_0 in Eq. (13) assuming steady-state infiltration based on the net recharge rate.

347 For the nine PFAS, the Szyskowski parameters for the surface tension in synthetic groundwater (Silva
 348 et al., 2019, 2021), molecular weights, and the release concentrations from a diluted AFFF solution (Høisæter
 349 et al., 2019) are provided in Table 2. The six soils include sand (soil 1), sandy loam (soil 2), two loams (soils
 350 3&4), sandy clay (soil 5), and a sandy clay loam (soil 6). For the present study, the solid-phase adsorption
 351 coefficients for the six soils were measured for the nine PFAS (Nguyen et al., 2020) and are summarized in
 352 Table 3. If no measured solid-phase adsorption coefficients are available, they may be estimated using the so-
 353 called distributed-sorption models that represent the contribution of individual soil constituents (soil organic
 354 carbon, clay minerals, metal oxides) to the total sorption. The distributed-sorption models can implicitly
 355 represent the different potential sorption mechanisms such as hydrophobic and electrostatic interactions and
 356 have been developed and applied for quantifying the solid-phase adsorption of PFOA and PFOS in soil
 357 media (Higgins & Luthy, 2007; Knight et al., 2019; Wang et al., 2021). The hydraulic parameters for the
 358 six soils are not available and are estimated (see Table 4) using the Rosetta pedotransfer model (Zhang &
 359 Schaap, 2017) based on soil texture and bulk density reported in Nguyen et al. (2020). No measurements of
 360 air–water interfacial area are available for the soils. One approach is to employ the thermodynamic-based
 361 method to estimate the air–water interfacial area as a function of water saturation (Leverett, 1941; Morrow,

PFAS	K_d (cm ³ /g)					
	soil 1	soil 2	soil 3	soil 4	soil 5	soil 6
PFPeA	0.04	0.44	0.2	0.15	0.24	0.35
PFHxA	0.05	0.52	0.21	0.17	0.24	0.35
PFHpA	0.3	1.41	0.47	0.46	0.5	0.61
PFOA	0.53	2.84	1.42	0.64	0.81	0.68
PFNA	1.27	10.69	1.77	2	1.31	1.57
PFDA	7.53	45.75	7.96	12.3	16.87	0.86
PFBS	0.05	0.5	0.2	0.17	0.25	0.36
PFHxS	0.28	2.12	0.39	0.45	0.4	0.69
PFOS	3.22	34.3	3.52	4.18	3.15	3.45

Table 3: Solid-phase adsorption coefficients for the nine PFAS in the six soils obtained from Nguyen et al. (2020). The textures for the six soils are sand, sandy loam, two loams, sandy clay, and sandy clay loam, respectively.

362 1970; Bradford & Leij, 1997). The thermodynamic-based method assumes that the mechanical work done for
 363 fluid–fluid displacement is fully converted to surface energy (i.e., generating air–water interfaces). As a result,
 364 the air–water interfacial area can be estimated by computing the area under the capillary pressure–water
 365 saturation curve as

$$A_{aw} = \frac{\phi}{\sigma} \int_{S_w}^1 p_c(S_w) dS_w, \quad (30)$$

366 where ϕ is the porosity of the soil, σ is the surface tension, and p_c is the capillary pressure. Prior studies
 367 have shown that the thermodynamic-based method significantly underestimates the air–water interfacial area
 368 compared to that measured by aqueous interfacial tracers (Jiang et al., 2020), but the latter was suggested
 369 to be more relevant for PFAS transport in the vadose zone (Brusseau & Guo, 2021). Here, we employ a
 370 scaling method to correct the estimated air–water interfacial area estimated from the thermodynamic-based
 371 method. We take the Vinton soil introduced in section 4.2 to compute the ratio between the A_{aw} estimated
 372 from the thermodynamic-based method and the measured A_{aw} by aqueous interfacial tracer. The ratio
 373 varies from 3.89 to 4.41 for the entire saturation range. As an approximation, the mean ratio 4.15 is applied
 374 to correct the air–water interfacial area for the six soils. When computing the thermodynamic-based A_{aw} ,
 375 the surface tension σ in Equation (30) is taken as the surface tension with no dissolved PFAS.

376 The simulated PFAS retention in the vadose zone is presented in Figure 5 for the nine PFAS in the
 377 six soils. The results clearly demonstrate that the retention of PFAS vary strongly with different chain
 378 lengths and functional groups. For both PFCAs and PFSAs, the longer-chain PFAS are much more strongly
 379 retained in the vadose zone than their shorter-chain counterparts, which is consistent with the increasing
 380 solid-phase and air–water interfacial adsorption for longer-chain PFAS. While variations in the retention of
 381 a given PFAS exist among the six soils, the difference between the soils is not significant except for soil 2,

soil	K_s cm/day	θ_s cm ³ /cm ³	θ_r cm ³ /cm ³	ρ_b g/cm ³	α cm ⁻¹	n —	α_L cm
soil 1	482.7	0.363	0.054	1.58	0.03133	2.72	24.39
soil 2	211.1	0.570	0.097	0.82	0.01291	1.38	24.39
soil 3	6.1	0.361	0.079	1.59	0.01072	1.362	24.39
soil 4	10.1	0.384	0.079	1.47	0.00893	1.411	24.39
soil 5	8.2	0.383	0.111	1.66	0.01364	1.238	24.39
soil 6	16.2	0.371	0.090	1.59	0.01095	1.327	24.39

Table 4: Hydraulic and transport parameters for the six soils employed in section 5. The textures for the six soils are sand, sandy loam, two loams, sandy clay, and sandy clay loam, respectively. The hydraulic parameters including K_s , θ_s , θ_r , α , and n are estimated by the Rosetta pedotransfer model (Zhang & Schaap, 2017) based on soil texture and bulk density reported in Nguyen et al. (2020). The dispersion coefficient α_L is approximated using the empirical model of Xu & Eckstein (1995) where the dependence of α_L on water saturation is not considered.

382 which has the strongest retention due to its much stronger solid-phase adsorption. The similar retention is
 383 in part caused by the same net recharge rate (30 cm per year) employed for all of the six soils. At field
 384 sites, the net recharge rate will likely change with different soils in the vadose zone as a result of different
 385 surface evaporation rates due to different water retention capacities. For example, this was the case for the
 386 Accusand and Vinton soil employed in section 4.2, where their net recharge rates differ by almost 2 times.
 387 This also implies that it is critical to obtain a more accurate estimate of the net recharge rate for improved
 388 prediction of PFAS retention and leaching in the vadose zone when applying the simplified analytical model.

389 Another way to analyze the strength of retention is to compare the retardation factors among different
 390 PFAS and soils. Note that because parameters for kinetic solid-phase adsorption are not available, kinetic
 391 solid-phase adsorption is not accounted for in these simulations. The computed retardation factors are
 392 presented in Figure 6, from which we can make the following observations. Consistent with the retention
 393 behavior shown in Figure 5, the retardation factors increase with chain length for the same soil. The
 394 retardation factors for the short-chain PFAS (PFPeA, PFHxA, PFHpA, and PFBS) are smaller than 10
 395 for all soils except for PFHpA in soil 1 (sand) that has a retardation factor of 11.1. Comparisons among
 396 the soils reveal that for the longer-chain PFAS, the retardation factors for soil 1 (sand) and soil 2 (sandy
 397 loam) are greater than the other finer-grain soils. The reason for this rather counterintuitive observation
 398 is that, for a given infiltration rate, the finer-grain soils have a much higher water saturation that leads
 399 to a much smaller air–water interfacial area. This then leads to reduced air–water interfacial adsorption
 400 and total retention of PFAS in the vadose zone comprised of finer-grain soils. Overall, the above workflow
 401 and analyses demonstrate that the simplified analytical model provides a computationally efficient means to
 402 quantify PFAS leaching in the vadose zone and mass discharge to groundwater.

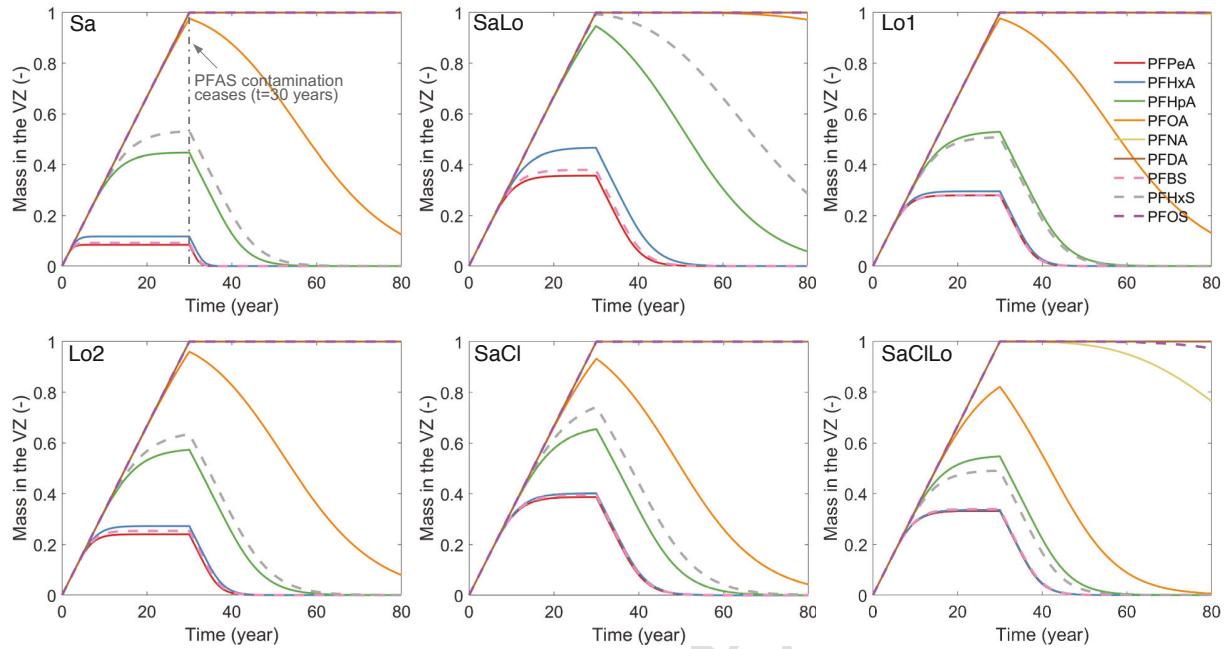


Figure 5: Simulated retention of nine PFAS (six PFCAs and three PFSAs) in a homogenous vadose zone represented by six soils. The soil textures are: sand (Sa), sandy loam (SaLo), two loams (Lo1 and Lo2), sandy clay (SaCl), and sandy clay loam (SaClLo). The solid and dashed lines denote PFCAs and PFSAs, respectively.

403 6. Summary and conclusion

404 We present a simplified model for quantifying PFAS leaching in the vadose zone and mass discharge to
 405 groundwater. The model assumes steady-state infiltration and linear solid-phase and air–water interfacial
 406 adsorption. Rate-limited solid-phase adsorption is represented by a two-domain kinetic model. Air–water
 407 interfacial adsorption is assumed instantaneous (i.e., equilibrium). New analytical solutions for the simplified
 408 model are derived that allow for arbitrary initial conditions. These analytical solutions are the first that
 409 account for the two-domain solid-phase kinetic adsorption and air–water interfacial adsorption for solute
 410 transport. While the model formulation involves a number of simplifications, predicted simulations using the
 411 analytical solution agree well with a wide range of sand-packed miscible-displacement experiments for PFAS
 412 under water-unsaturated conditions. For these experiments, the analytical solution is almost identical to the
 413 solution from a numerical model that accounts for a set of comprehensive PFAS-specific transport processes,
 414 including surfactant-induced flow and rate-limited and nonlinear adsorption at the solid–water and air–water
 415 interfaces. These comparisons demonstrate the validity of the simplified model and the analytical solution
 416 for representing the PFAS-specific transport processes under laboratory conditions. The simplified model
 417 is then compared to the full-process numerical model for simulating long-term PFAS leaching at a model
 418 AFFF-impacted fire training area site. Despite that several processes and conditions are not represented in
 419 the simplified model, e.g., surfactant-induced flow, time-dependent infiltration and evapotranspiration, and

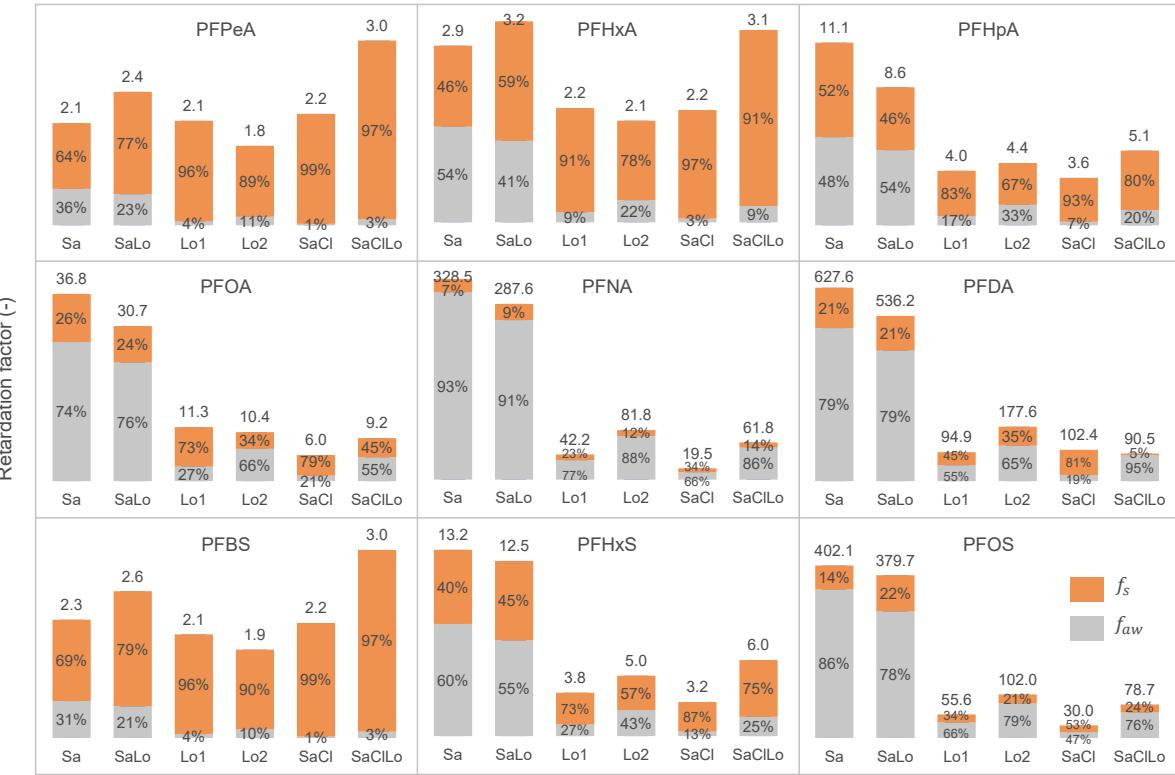


Figure 6: Simulated retardation factors for the nine PFAS in a homogeneous vadose zone represented by six soils. The soil textures are: sand (Sa), sandy loam (SaLo), two loams (Lo1 and Lo2), sandy clay (SaCl), and sandy clay loam (SaClLo). The number at the top of each bar is the total retardation factor R . The orange and gray portions of the bar denote, respectively, the fraction contributed by solid-phase adsorption ($f_s = R_s / (R - 1)$) and the fraction contributed by air-water interfacial adsorption ($f_{aw} = R_{aw} / (R - 1)$).

nonlinearity in the solid–water and air–water interfacial adsorption, close agreement is observed between the simplified analytical and full-process numerical models in their simulated long-term retention of PFAS in the vadose zone and mass discharge to groundwater.

Practically, the analytical solution provides a simple approach for estimating PFAS retention and leaching in the vadose zone and mass discharge to groundwater at PFAS-contamination sites. This screening-type tool allows stakeholders and practitioners to develop quantitative guidance for characterizing, managing, and mitigating the long-term risks of PFAS contamination. In particular, because the simplified model can be solved analytically, 1000s of simulations can be easily conducted for a given problem using a wide range of input parameters. These simulations can be used to quantify the uncertainty propagated from the input parameters to the final predictions and also to gain critical insights into the primary parameters or factors that control the long-term risks of PFAS contamination at sites. In addition to the computationally-focused analyses, this screening-type tool can also be combined with direct measurements of soil porewater concentrations proposed in a recent perspective by Anderson (2021) for quantifying soil-to-groundwater mass

433 discharge and providing remedial guidance at PFAS-contamination sites.

434 The simplified model is nevertheless limited by the imposed assumptions. We point out the limitations
 435 and propose strategies that may be employed to partially address these limitations when applying the model
 436 to analyze practical problems. For example, the analytical solution is unable to simulate PFAS leaching in
 437 the presence of spatial heterogeneities such as soil layering that can lead to both heterogeneous hydraulic
 438 and sorption properties (Zeng & Guo, 2021). The impact of heterogeneities may be indirectly accounted for
 439 by conducting a range of simulations using different soil types relevant to a specific site. These simulations
 440 can be used to provide upper and lower bounds for the estimates of PFAS leaching and mass discharge.
 441 Similarly, since the analytical solution is derived under steady-state infiltration, it cannot represent the
 442 impact of dynamic infiltration on PFAS leaching. However, the simulation results presented in section 4.2
 443 show that the simulated PFAS leaching by assuming steady-state flow agrees well with those generated by
 444 the full-process numerical model that accounts for highly dynamic infiltration rates from real rainfall data
 445 at a 30-min temporal resolution. While only homogeneous vadose zones are considered in section 4.2, a
 446 prior study by Russo & Fiori (2008) suggested that assuming steady-state flow is sufficient for predicting
 447 solute transport even in heterogeneous vadose zones (a non-surfactant solute in the absence of complex
 448 retention processes was considered therein), provided that the groundwater table is located at sufficiently
 449 large distance from the land surface. Nonetheless, when dynamic infiltration does influence PFAS leaching,
 450 as a practical approach, one may examine the impact of varying infiltration rates by comparing results from
 451 a range of simulations that cover the common or possible ranges in infiltration rates.

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 455 (P42 ES4940). The analytical solutions presented in this paper have been implemented into a computer code
 456 that is available from the corresponding author (B. Guo) upon reasonable request.

457 Appendix: Special case of the analytical solution (equilibrium adsorption)

458 When the solid-phase adsorption can be assumed equilibrium, i.e., $F_s = 1$ and $C_{s,2} = 0$, Eq. (10) reduces
 459 to the standard advection-dispersion equation with a constant retardation factor representing retention from
 460 equilibrium solid-water and air-water interfacial adsorption. Here, we present the analytical solution for
 461 this special case. The solution for the boundary value problem is available in the literature as summarized
 462 in van Genuchten & Alves (1982)

$$463 C^{BVP}(Z, T) = \begin{cases} C_0 A(Z, T), & 0 < T \leq T_0 \\ C_0 A(Z, T) - C_0 A(Z, T - T_0). & T > T_0 \end{cases} \quad (31)$$

463 where $A(Z, T) = \frac{1}{2} \operatorname{erfc} \left[\frac{RZ-T}{2(TR/P)^{1/2}} \right] + \left(\frac{TP}{\pi R} \right)^{1/2} e^{-\frac{(RZ-T)^2}{4TR/P}} - \frac{1}{2} \left(1 + PZ + \frac{PT}{R} \right) e^{PZ} \operatorname{erfc} \left(\frac{RZ+T}{2(TR/P)^{1/2}} \right)$.

464 The solution for the initial value problem with an arbitrary initial condition has the following form
 465 (Lindstrom & Narasimham, 1973)

$$C^{IVP}(Z, T) = \int_0^\infty C_i(\xi) \left[\frac{e^{-(RZ-R\xi-T)^2/(4TR/P)} + e^{(-P\xi-(RZ+R\xi-T)^2/(4TR/P))/(2\sqrt{\pi T/P/R})}}{2\sqrt{\pi T/(PR)}} - \frac{P}{2} e^{PZ} \operatorname{erfc} \left(\frac{RZ+R\xi+T}{2\sqrt{TR/P}} \right) \right] d\xi. \quad (32)$$

466 $C(Z, T) = C^{BVP}(Z, T) + C^{IVP}(Z, T)$ then gives the full solution for the special case with equilibrium
 467 solid–water and air–water interfacial adsorption.

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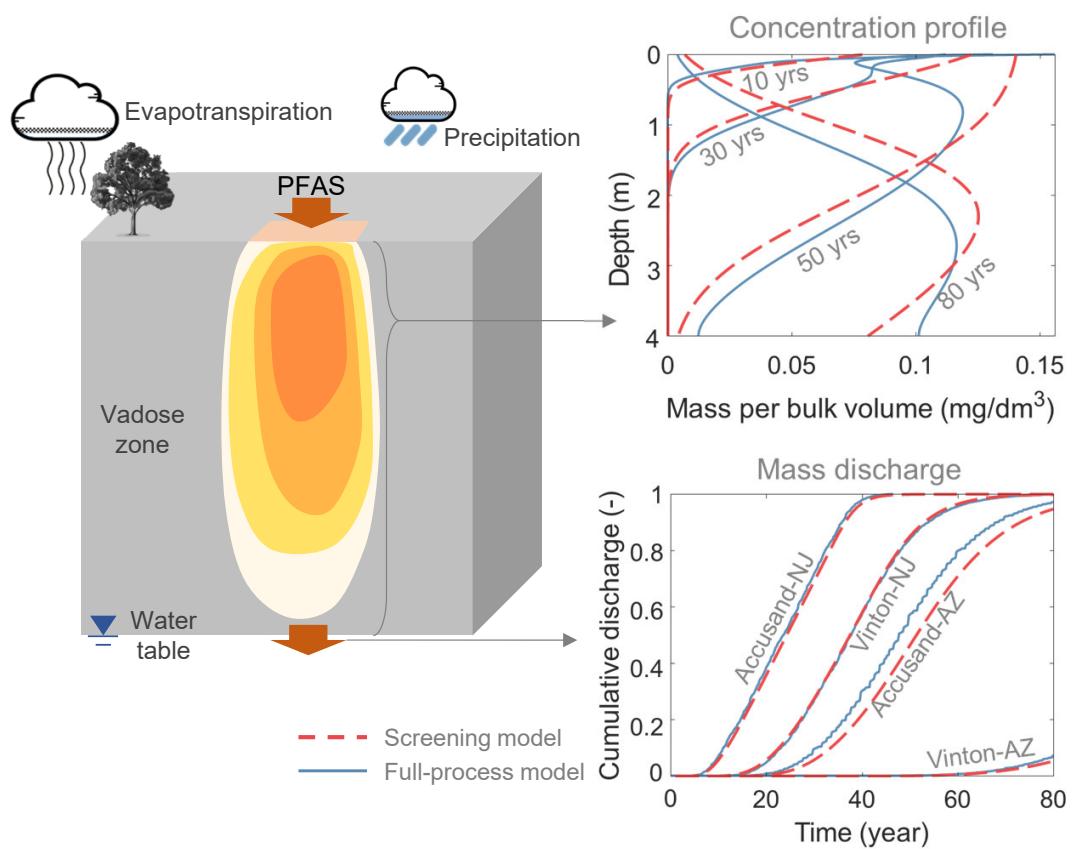
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Highlights

- We develop a simplified mathematical model representing the PFAS-specific transport and retention processes
- New analytical solutions are derived for the simplified model allowing for arbitrary initial conditions
- Validations by miscible-displacement experiments and comparisons to a full-process model are presented
- The analytical solution provides an efficient and accurate screening-type tool for quantifying vadose-zone PFAS leaching

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Screening model vs. Full-process model



Author Statement

Bo Guo – Conceptualization, Methodology, Investigation, Software, Data Curation, Formal analysis, Visualization, Writing – Original Draft.

Jicai Zeng – Data Curation, Visualization, Writing – Review & Editing.

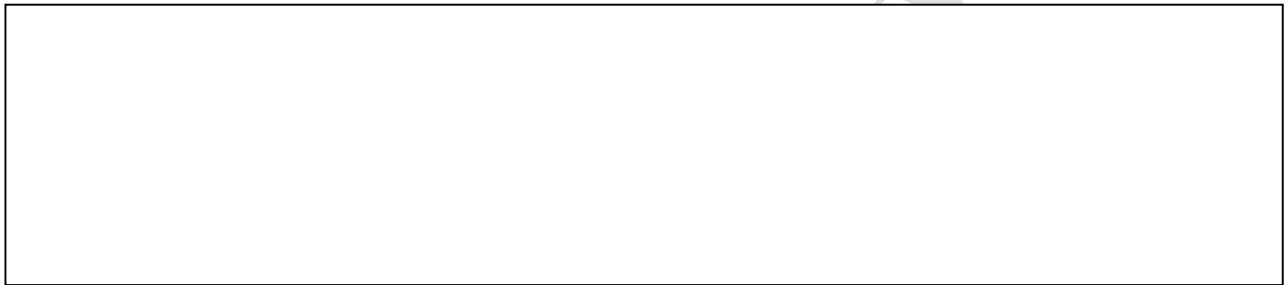
Mark L. Brusseau – Data Curation, Formal analysis, Writing – Review & Editing.

Yonggen Zhang – Data Curation, Writing – Review & Editing.

Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

A large, empty rectangular box with a thin black border, intended for authors to declare any potential competing interests.