

# **Facile cross-linking polybenzimidazole with polycarboxylic acids to improve H<sub>2</sub>/CO<sub>2</sub> separation performance**

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## ABSTRACT

Polybenzimidazole (PBI) with a strong size-sieving ability exhibits attractive H<sub>2</sub>/CO<sub>2</sub> separation properties for blue H<sub>2</sub> production and CO<sub>2</sub> capture. Herein we report that PBI can be facilely cross-linked with polycarboxylic acids, oxalic acid (OA) and trans-aconitic acid (TaA), to improve its separation performance. The acids react with the amines on the PBI chains, decreasing free volume and increasing size-sieving ability. The acid doping increases H<sub>2</sub>/CO<sub>2</sub> selectivity from 12 to as high as 45 at 35 °C. The acid-doped samples demonstrate stable H<sub>2</sub>/CO<sub>2</sub> separation performance when challenged with simulated syngas containing water vapor at 150 °C, which surpasses state-of-the-art polymers and Robeson's upper bound for H<sub>2</sub>/CO<sub>2</sub> separation.

**Keywords:** polybenzimidazole; polycarboxylic acid; H<sub>2</sub>/CO<sub>2</sub> separation; cross-linking; membranes; carbon capture

## 1. INTRODUCTION

Pre-combustion CO<sub>2</sub> capture with H<sub>2</sub> production is a promising approach to eliminate the emission of CO<sub>2</sub> from large source points such as power plants, realizing a clean utilization of fossil fuels.<sup>1-5</sup> In this process, fuels are gasified to generate gas mixtures containing H<sub>2</sub> and CO, and the CO is further shifted to H<sub>2</sub> and CO<sub>2</sub>.<sup>6</sup> For H<sub>2</sub> to be used in a green manner, the CO<sub>2</sub> must be captured for utilization or sequestered. Membrane technology has been extensively explored for H<sub>2</sub>/CO<sub>2</sub> separation application due to its inherently high energy efficiency, small footprint, easy scale-up and low maintenance.<sup>4, 7-10</sup>

Gas transport through nonporous polymers usually follows the solution-diffusion mechanism, and gas permeability ( $P_A$ ) can be expressed as:<sup>9</sup>

$$P_A = S_A \times D_A \quad (1)$$

where  $S_A$  is gas solubility, and  $D_A$  is diffusion coefficient. Gas selectivity ( $\alpha_{A/B}$ ) is the ratio of their permeability (i.e.,  $\alpha_{A/B} = P_A/P_B$ ) and the combination of solubility selectivity ( $S_A/S_B$ ) and diffusivity selectivity ( $D_A/D_B$ ). For H<sub>2</sub>/CO<sub>2</sub> separation, the  $S_A/S_B$  is always less than 1 because H<sub>2</sub> is less condensable than CO<sub>2</sub>.<sup>8</sup> On the other hand, H<sub>2</sub> has a smaller molecular size (2.89 Å) than CO<sub>2</sub> (3.3 Å); therefore, membrane materials with a strong size-sieving ability is desirable to achieve high diffusivity selectivity, and thus high permeability selectivity.<sup>8</sup>

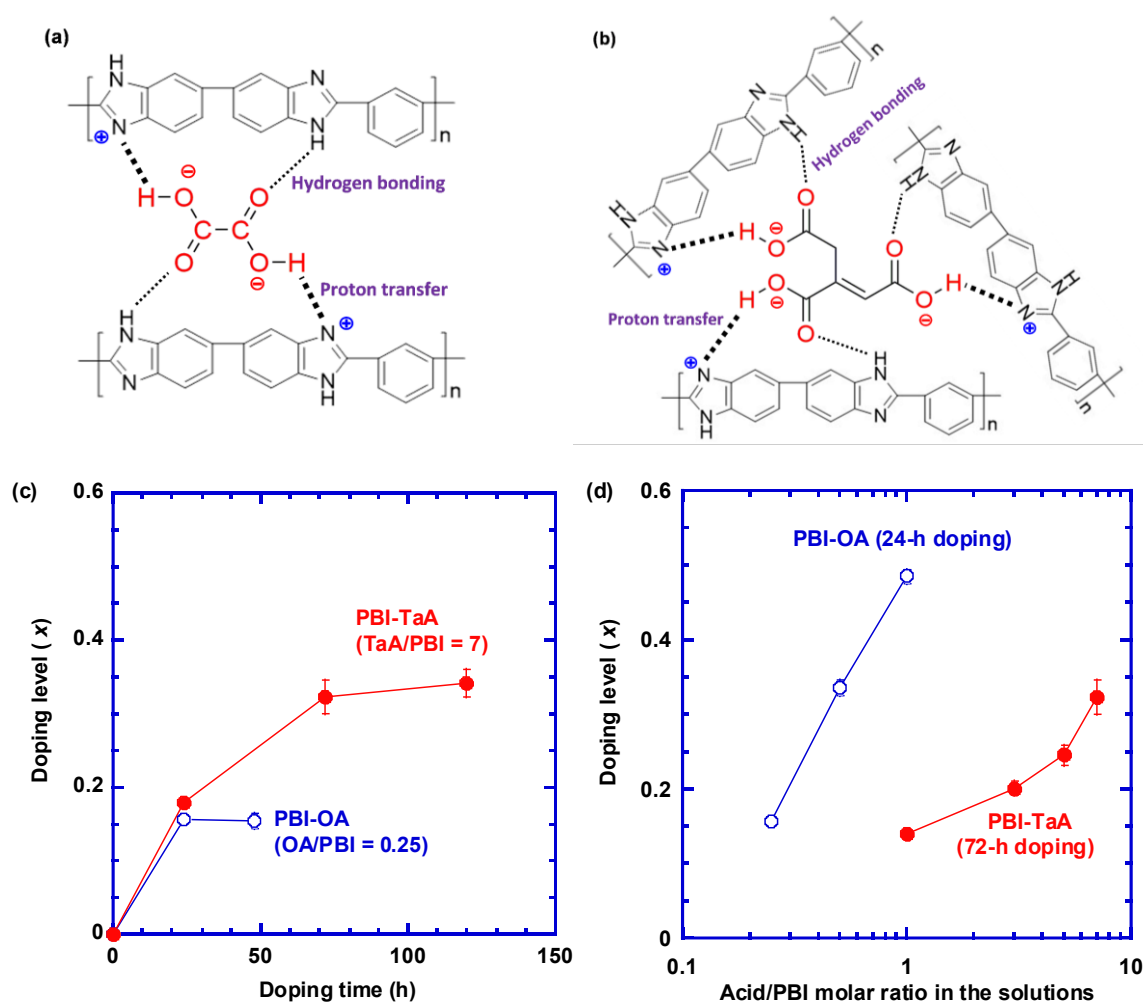
Industrial gas separation membranes are usually made of polymers, and polybenzimidazole (PBI) with a glass transition temperature of above 400 °C has emerged as a leading polymer for H<sub>2</sub>/CO<sub>2</sub> separation at high temperatures.<sup>8, 11-13</sup> Commercial *m*-PBI exhibited H<sub>2</sub> permeability of 27 Barrer (1 Barrer = 10<sup>-10</sup> cm<sup>3</sup> (STP) cm<sup>-2</sup> s<sup>-1</sup> cmHg<sup>-1</sup>) and H<sub>2</sub>/CO<sub>2</sub> selectivity of 16 at 150 °C.<sup>4</sup> PBI

was further cross-linked with terephthaloyl chloride (TCL),<sup>7</sup> 1,3,5-tris(bromomethyl)benzene (TBB),<sup>14</sup> and  $\alpha,\alpha'$ -dibromo-p-xylene (DBX)<sup>15</sup> to enhance the size-sieving ability and thus H<sub>2</sub>/CO<sub>2</sub> selectivity. For example, the cross-linking with TCL increased H<sub>2</sub>/CO<sub>2</sub> selectivity by almost 100% and retained 78% H<sub>2</sub> permeability at 150 °C.<sup>7</sup> For optimal performance, the cross-linkers should have multi-functional groups with high reactivity with PBI and low molecular weight to retain the PBI structure.<sup>16</sup>

Recently, we reported a facile cross-linking of PBI via proton transfer and hydrogen bonding using phosphoric acid (H<sub>3</sub>PO<sub>4</sub>) and sulfuric acid (H<sub>2</sub>SO<sub>4</sub>).<sup>4</sup> Increasing the acid doping level (defined as the molar ratio of the acid to PBI repeating units) resulted in a phenomenal increase in H<sub>2</sub>/CO<sub>2</sub> selectivity.<sup>4</sup> For instance, as the doping level approached 1, H<sub>2</sub>/CO<sub>2</sub> selectivity reached an unprecedented value of 140 at 150 °C. H<sub>3</sub>PO<sub>4</sub> has pK<sub>a1</sub>, pK<sub>a2</sub>, and pK<sub>a3</sub> values of 2.15, 7.20, and 12.3, respectively, suggesting that it has only one free proton. By contrast, H<sub>2</sub>SO<sub>4</sub> has two free protons (<1 for pK<sub>a1</sub> and 1.92 for pK<sub>a2</sub>) and stronger acidity than H<sub>3</sub>PO<sub>4</sub>. Interestingly, at a doping level of  $\approx$  0.24, H<sub>2</sub>SO<sub>4</sub> and H<sub>3</sub>PO<sub>4</sub> showed very similar H<sub>2</sub>/CO<sub>2</sub> separation properties, despite their difference in the free protons and pK<sub>a</sub> values.<sup>4</sup> Therefore, the understanding the effect of the number of free protons and acidity strength on the H<sub>2</sub>/CO<sub>2</sub> separation properties can be critical to designing high-performance membrane materials for this separation.

Herein we chose two polycarboxylic acids for PBI doping, namely oxalic acid (OA) and trans-aconitic acid (TaA), as shown in Fig. 1a,b. OA has two free protons with pK<sub>a1</sub> and pK<sub>a2</sub> values of 1.27 and 4.27, respectively,<sup>17</sup> and TaA has three protons with pK<sub>a1</sub>, pK<sub>a2</sub>, and pK<sub>a3</sub> values of 2.91, 4.33, and 6.16, respectively.<sup>18</sup> Both acids have similar structures and stronger

acidity than  $\text{H}_3\text{PO}_4$ . We systematically determine the effect of the acid doping on physical properties of PBI (such as density, thermal stability, and free volume) and gas transport properties (such as pure-gas sorption and pure- and mixed-gas permeability) at various temperatures. The samples with promising separation properties were further evaluated with simulated wet syngas mixtures for extended tests to demonstrate their promise for industrial  $\text{H}_2/\text{CO}_2$  separation.



**Fig. 1.** Cross-linking PBI by OA and TaA. Schematic illustration of (a) PBI-OA and (b) PBI-TaA. (c) Doping level as a function of the doping time. The molar ratio of the acid in the solution to the PBI repeating unit is 0.25 for OA and 7 for TaA. (d) Effect of the acid/PBI molar ratio in the doping solutions on the doping level at equilibrium.

## **2. EXPERIMENTAL SECTION**

### **2.1 Materials**

Celazole® PBI S10 solution was purchased from PBI Performance Products Inc. (Charlotte, NC). The solution contains  $\approx 9.5$  wt% PBI (with a molecular weight of 35 kDa) in N,N-dimethylacetamide (DMAc). OA, TaA, and methanol were procured from Sigma-Aldrich Corporation (St. Louis, MO). Gas cylinders of H<sub>2</sub>, CO<sub>2</sub>, and N<sub>2</sub> with ultrahigh purity were obtained from Airgas Inc. (Buffalo, NY).

### **2.2 Preparation of thin films**

PBI films were prepared by a solution casting method.<sup>4,7</sup> First,  $\sim 2$  mL of PBI S10 solution was filtered through a 0.45  $\mu\text{m}$  syringe filter (Thermo Fisher Scientific, Waltham, MA). Second, the filtered solution was cast on a glass plate using a casting knife (BYK-Gardner, Pompano Beach, FL). Third, the liquid film was dried overnight in a conventional oven at 60 °C under N<sub>2</sub> flow, followed by heating at 200 °C under vacuum for 48 h. Fourth, the dried film was peeled off the plate and then immersed in methanol at  $\approx 23$  °C for 24 h to remove the residual DMAc. Finally, the film was vacuum-dried at 100 °C for 12 h. The PBI film was determined to have a thickness of  $\approx 12$   $\mu\text{m}$ .

To prepare an acid-doped film, a PBI film ( $\sim 120$  mg) was first immersed in 100 mL methanol at  $\approx 23$  °C. Second, the desired amount of OA or TaA was added to the solution. The molar ratio of the acid in the solutions to the repeating units of the PBI film was varied from 0.25 to 1 for OA, and from 1 to 7 for TaA to achieve different doping levels. Doping time was set at 24 h for OA and 72 h for TaA to ensure that the acid was evenly distributed in the film at equilibrium.

Finally, the film was taken out of the solution and dried in the vacuum oven at 100 °C for 12 h.

The doping level ( $x$ ) was calculated using the following equation:

$$x = \frac{\Delta m / M_a}{m_0 / M_p} \quad (2)$$

where  $M_a$  is the molar mass of the acid (90 g mol<sup>-1</sup> for OA and 174 g mol<sup>-1</sup> for TaA), and  $M_p$  is the molar mass of the PBI repeating unit (308 g mol<sup>-1</sup>). The  $m_0$  is the mass of the dry sample before the acid doping, and  $\Delta m$  is the mass increase caused by the acid doping. The doped samples are denoted as PBI-OA<sub>x</sub> or PBI-TaA<sub>x</sub>, depending on the acid used.

### 2.3 Characterization of PBI-OA and PBI-TaA films

Attenuated total reflection—Fourier transform infrared spectroscopy (ATR-FTIR) was performed using a vertex 70 Burkert spectrometer (Bruker Scientific LLC, Billerica, MA). For each sample, 100 scans were performed in the range of 450-4000 cm<sup>-1</sup> at 4 cm<sup>-1</sup> resolution. Thermal properties of the samples were determined using an SDT Q600 thermogravimetric analyzer (TA Instruments, New Castle, DE) from  $\approx$  23 °C to 800 °C at a ramping rate of 10 °C/min under N<sub>2</sub> flow. The ramping rate of 10 °C/min is typical for the study of polymers, as used in other reports.<sup>4,</sup>

7, 14, 19

Wide-angle X-ray diffraction (WAXD) patterns were obtained using a Rigaku Ultima IV X-ray diffractometer (Rigaku Analytical Devices, Wilmington, MA) with the CuK $\alpha$  x-ray wavelength of 1.54 Å. The scanning has a 2 $\theta$  range of 5 – 45° and a rate of 1.0 °/min.

The sample density ( $\rho_M$ ) was determined using an analytical balance (Mettler-Toledo, Columbus, OH) based on the Archimedes' principle. The  $\rho_M$  can be calculated as followed:<sup>4, 7</sup>

$$\rho_M = \frac{m_A}{m_A - m_L} \rho_L \quad (3)$$

where  $m_A$  and  $m_L$  are the sample mass in air and an auxiliary liquid, respectively.  $\rho_L$  is the density of the auxiliary liquid (i.e., iso-octane with a density of 0.69 g/cm<sup>3</sup>).

Pure-gas permeability was determined at various pressures and temperatures via a constant-volume and variable-pressure system. The permeability was calculated using the following equation:<sup>4, 7</sup>

$$P_A = \frac{V_p \cdot l_m}{p_2 A_m R T} \left[ \left( \frac{dp_1}{dt} \right)_{ss} - \left( \frac{dp_1}{dt} \right)_{leak} \right] \quad (4)$$

where  $V_p$  is the downstream volume,  $l_m$  is the film thickness,  $A_m$  is the effective film area for gas transport,  $R$  is the gas constant, and  $T$  is the temperature. The  $(dp_1/dt)_{ss}$  and  $(dp_1/dt)_{leak}$  are the steady-state rate of pressure rise in the downstream volume at the feed pressure ( $p_2$ ) and under vacuum, respectively.

Mixed-gas permeability was determined using a constant-pressure and variable-volume apparatus with a sweep gas of N<sub>2</sub> on the permeate side and can be calculated using Eq. (5):<sup>4, 7</sup>

$$P_A = \frac{x_A \cdot Q_S \cdot l_m}{x_{sweep} \cdot A_m (p_{2,A} - p_{1,A})} \quad (5)$$

where  $Q_S$  is the flow rate of the sweep gas. The  $x_A$  and  $x_{sweep}$  are the mole fraction of gas component A and sweep gas in the sweep-out stream, respectively, which were measured using a 3000 Micro GC (Inficon Inc., Syracuse, NY). For the long-term stability testing, water vapor was introduced by flowing the feed gas through a water bubbler at 23 °C before entering the permeation cell. Since the permeation cell was at 150 °C, water condensation in the cell was not expected.

Gas sorption isotherms of the samples ( $\sim 80$  mg) with a thickness of  $\approx 12$   $\mu\text{m}$  were determined using a gravimetric sorption analyzer of IGA 001 (Hidden Isochema, Warrington, UK), at various pressures (i.e., 3.4 bar, 7.0 bar, and 10 bar) and temperatures (i.e., 35  $^{\circ}\text{C}$  and 150  $^{\circ}\text{C}$ ).  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$  sorption at each pressure reached equilibrium in  $\sim 10$  h and  $\sim 20$  h, respectively. The buoyancy effect was considered in the calculation of gas sorption.<sup>4, 7</sup>

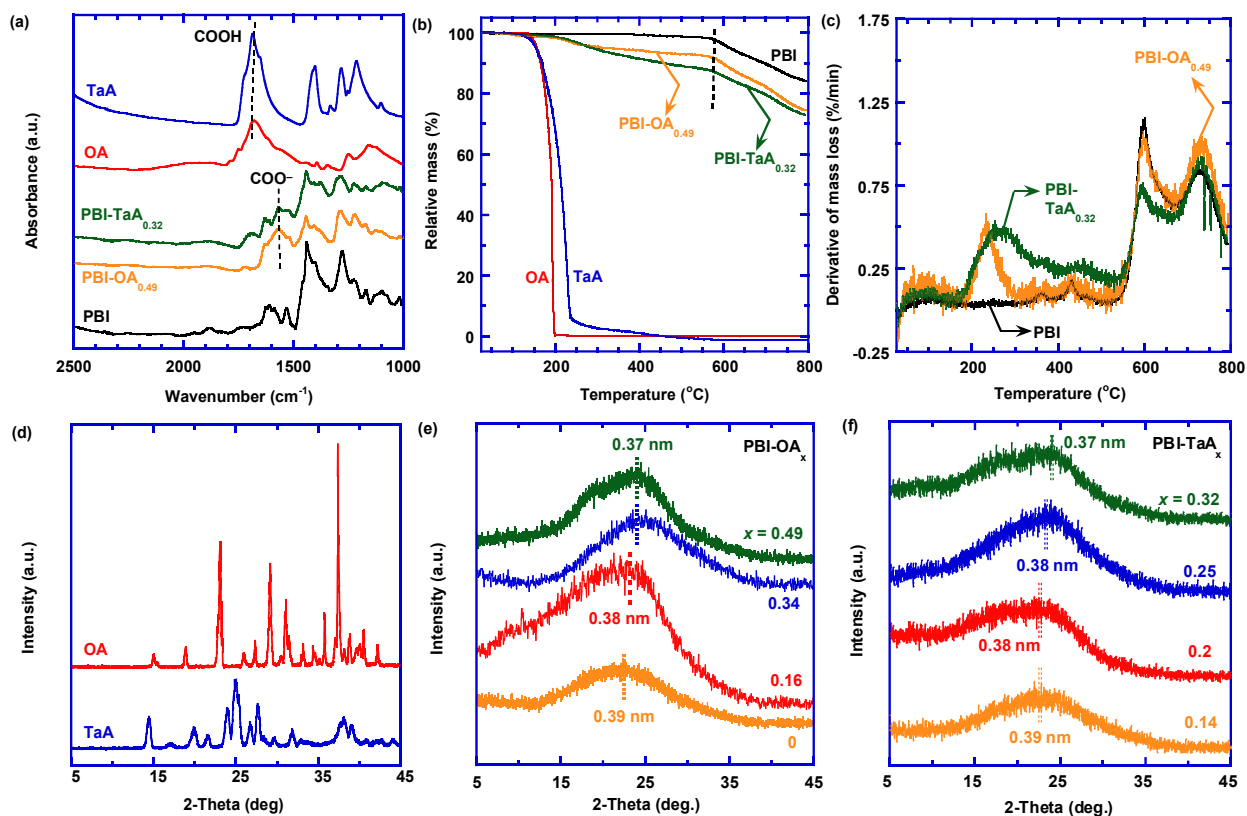
### 3. RESULTS AND DISCUSSION

#### 3.1 Effect of acid doping on physical properties

Fig. 1c displays the effect of the doping time on the acid doping level of  $\approx 12$   $\mu\text{m}$  thin PBI films. The doping level increases with increasing doping time and levels off after 24 h for PBI-OA and 72 h for PBI-TaA. The difference is consistent as TaA has a larger molecular size than OA, and thus requires a longer doping time before reaching equilibrium. Therefore, the doping time was set at 24 h for PBI-OA and 72 h for PBI-TaA to ensure even acid distribution in the films. Fig. 1d elucidates the method used to control the doping level of PBI films (i.e., changing the molar ratio of the acid to the PBI repeating units in the doping solutions). Increasing the acid amount increases the doping level. Due to the equilibrium for the acids between the solution and the PBI films, the doping level is lower than the molar ratio of the acid to the PBI repeating units in the solutions, particularly at high doping levels. Therefore, the maximal doping level obtained in this study was 0.32 for TaA and 0.49 for OA.

Fig. 2a displays the FTIR spectra of both PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub>, which exhibit a characteristic peak of  $\text{COO}^-$  at  $1550\text{ cm}^{-1}$ .<sup>20</sup> This suggests that the protons transfer from the

carboxylic acid (-COOH) groups to the amine groups on the PBI chains, thus confirming the acid-base reaction. PBI-TaA<sub>0.32</sub> shows a small characteristic peak of the unreacted -COOH groups at 1720 cm<sup>-1</sup>, presumably due to the high pK<sub>a3</sub> value and low acidity. The C=N stretching can be seen on PBI spectra at 1620 cm<sup>-1</sup> but shifts to 1630 cm<sup>-1</sup> for the acid-doped samples because of the hydrogen bonding.<sup>21, 22</sup> The N-H stretching of the imidazole rings on the PBI chains overlaps with the hydrogen bonding between the PBI and acid, and thus are not displayed in Fig. 2a.<sup>14</sup>



**Fig. 2.** Characterization of PBI, OA, TaA, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub>. (a) FTIR spectra; (b) TGA curves; (c) derivative thermogravimetric analysis (DTA) curves; WAXD patterns of (d) pure OA and TaA, (e) PBI-OA<sub>x</sub>, and (f) PBI-TaA<sub>x</sub>. The double dotted lines show the peaks and corresponding 2 $\theta$  values, which are used to calculate the *d*-spacing.

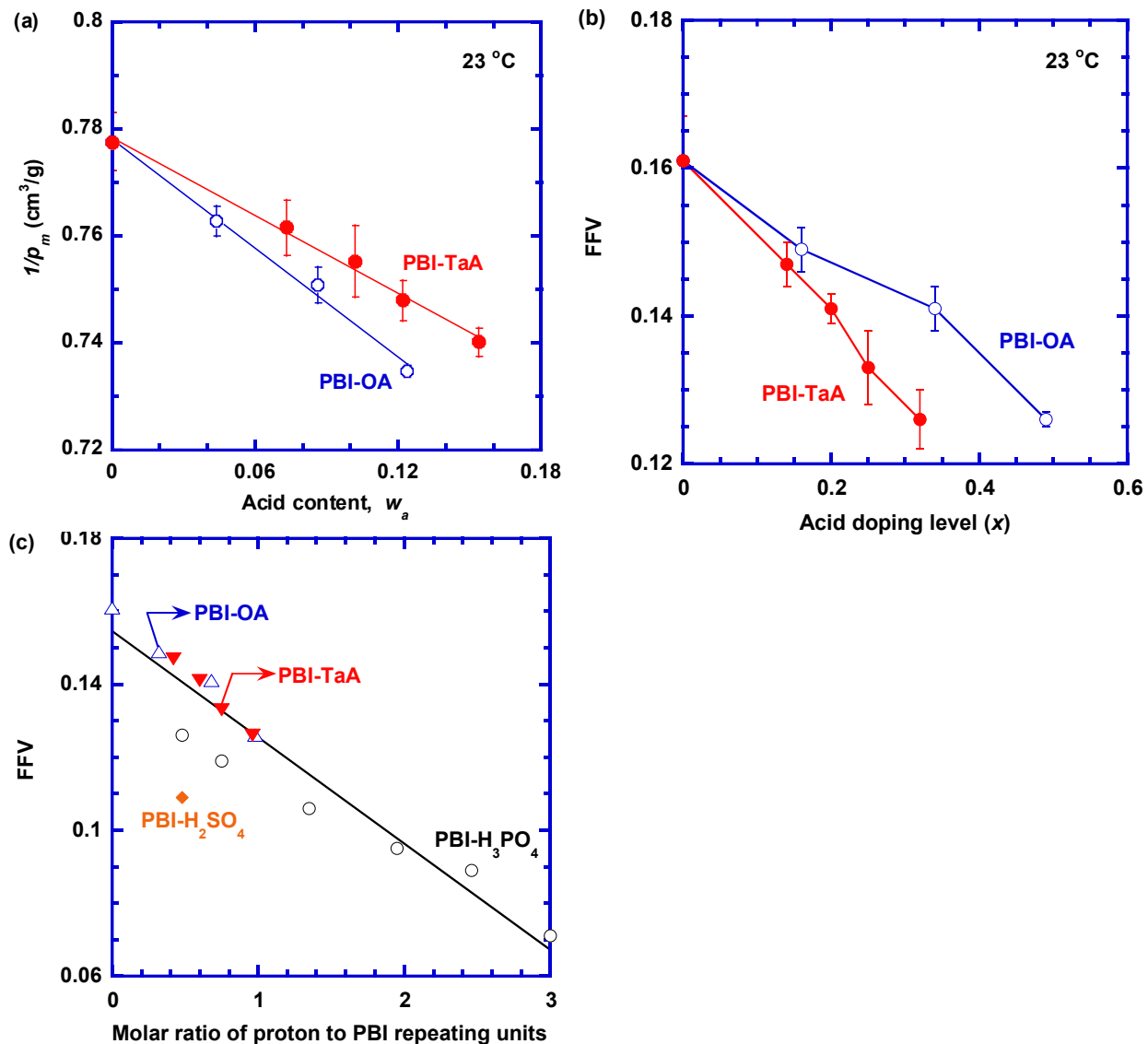
Fig. 2b,c compares the thermal stability of pure acids and two representative samples of PBI-OA and PBI-TaA. Both OA and TaA start to degrade at  $\sim 150$  °C. However, PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub> have degradation temperatures of  $\sim 230$  °C and  $\sim 260$  °C, respectively, indicating improved acid thermal stability when reacted with PBI. At 580 °C, PBI exhibits 2% mass loss, while PBI-OA<sub>0.49</sub> containing 12 wt% OA and PBI-TaA<sub>0.32</sub> containing 15 wt% TaA show a mass loss of 8.5 wt% and 13 wt%, respectively. The lower mass loss values than the acid content can be ascribed to the partial degradation of the acids. The DTA peaks above 580 °C are attributed to the degradation of the PBI backbones.<sup>7</sup>

Fig. 2d displays WAXD patterns of pure OA and TaA at  $\approx 23$  °C, and the sharp peaks indicate that they are crystalline. By contrast, these sharp peaks disappear in the patterns of the acid-doped PBIs (cf. Fig. 2e,f), suggesting that the reaction with PBI causes structure modification of the acids, from crystalline to amorphous in PBI films. PBI has a characteristic peak at  $22.5^\circ$ , corresponding to a  $d$ -spacing (represents the average inter-segmental distance between polymer chains) of 0.39 nm according to Bragg's equation.<sup>23</sup> By contrast, PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub> show the  $d$ -spacing of 0.37 nm, confirming the tightened structure by acid doping. Fig. S1 shows that increasing temperature increases the  $d$ -spacing.

Fig. S2a shows that the density of the acid-doped PBI ( $\rho_m$ ) increases with increasing acid doping level. To elucidate the reaction between the acids and PBI, the  $\rho_m$  is described using an additive model:<sup>24</sup>

$$\frac{1}{\rho_m} = \frac{\omega_p}{\rho_p} + \frac{\omega_a}{\rho_a} = \frac{1}{\rho_p} + \left( \frac{1}{\rho_a} - \frac{1}{\rho_p} \right) \omega_a \quad (6)$$

where  $\omega$  is the weight fraction, and the subscripts of  $p$  and  $a$  represent the PBI and amorphous acid, respectively. This model assumes that the density of PBI and amorphous acid are independent of the composition. While this model might not depict the physical presentation of the acid-doped PBI, there is no reported way to obtain the  $\rho_p$  and  $\rho_a$  values, which are also needed for the analysis of the free volume. Fig. 3a also shows that the  $\rho_m$  data can be satisfactorily modeled with the  $\rho_a$  value of 2.27 g/cm<sup>3</sup> for OA and 1.87 g/cm<sup>3</sup> for TaA, which are higher than the pure acid densities (1.90 g/cm<sup>3</sup> for OA and 1.70 g/cm<sup>3</sup> for TaA), though the pure acids are crystalline. While the crystalline phase of most materials exhibits higher density than their amorphous phase, several polymers were reported with higher density for the amorphous phase than the crystalline phase, such as poly(4-methyl-1-pentene) (PMP)<sup>25</sup> and poly(2,6-dimethyl-1,4-phenylene)oxide (PPO).<sup>26</sup> Nevertheless, the preparation of amorphous acids and their density measurement is beyond the scope of this study.



**Fig. 3.** Effect of the acid doping on  $\rho_m$  and  $FFV$  of the acid-doped PBIs at  $\approx 23$  °C. (a) Modeling of the density using Eq. (6). (b)  $FFV$  of PBI-OA and PBI-TaA. (c) Correlation between  $FFV$  and the molar ratio of the proton to PBI repeating units. The data of PBI-H<sub>3</sub>PO<sub>4</sub> and PBI-H<sub>2</sub>SO<sub>4</sub> in (c) are from the literature.<sup>4</sup>

The free volume of a polymer is an important parameter to determine its gas diffusivity.<sup>27</sup> However, polymers are often nonporous, and the free volume cannot be directly measured using low-temperature gas adsorption measurement and Brunauer–Emmett–Teller (BET) theory. For example, PBI shows negligible porosity and surface to volume ratio in the BET measurement.<sup>28</sup>

Instead, fractional free volume (*FFV*) of the polymers is often used as an indicator of the free volume and can be estimated from the density using the following equation:<sup>4, 27</sup>

$$FFV = \frac{V - V_0}{V} = \frac{V - 1.3V_w}{V} \quad (7)$$

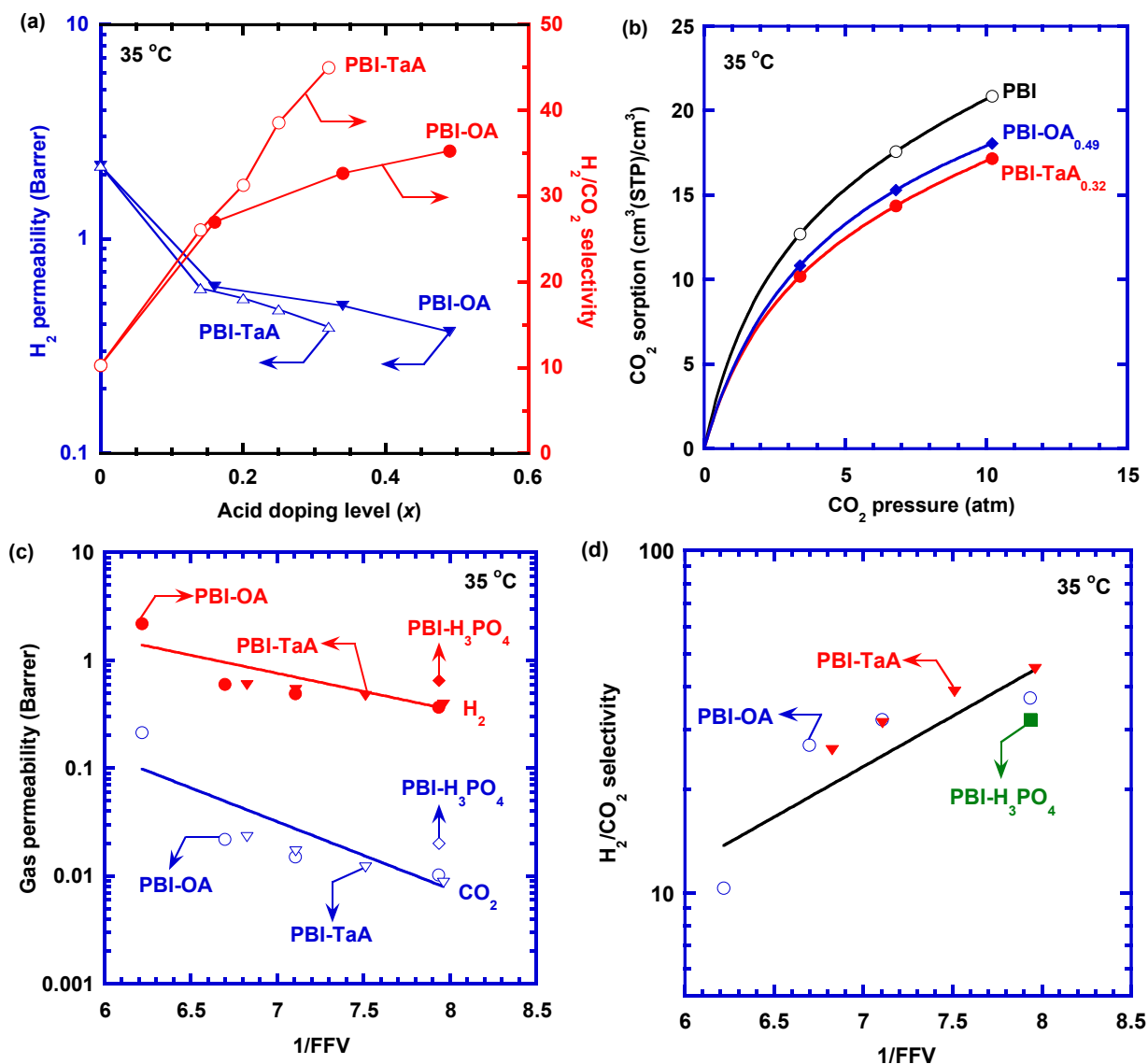
where  $V$  and  $V_0$  are the specific volume and occupied volume, respectively.  $V_0$  equals to 1.3 times of the Van der Waals volume ( $V_w$ ), which can be estimated by the group contribution method (cf. Table S1). Fig. 3b shows that *FFV* decreases with increasing  $x$ , which is consistent with the  $d$ -spacing results and thus confirms the tightened structure by acid doping. The *FFV* of PBI-TaA decreases at a faster rate than that of the PBI-OA because TaA has more carboxylic acid groups and renders a higher cross-linking density than OA. The *FFV* values at 150 °C were also estimated and decrease with increasing acid doping level (cf. Fig. S2b).

Fig. 3c displays the correlation between the *FFV* and the molar ratio of the proton to the PBI repeating units in PBI-OA, PBI-TaA, PBI-H<sub>3</sub>PO<sub>4</sub>, and PBI-H<sub>2</sub>SO<sub>4</sub>.<sup>4</sup> There seems to be a linear relationship, indicating that the amount of acid groups determines the polymer chains compactness instead of the acidity.

### 3.2 Effect of the acid doping on gas transport properties

Fig. 4a presents pure-gas H<sub>2</sub> permeability and H<sub>2</sub>/CO<sub>2</sub> selectivity at 35 °C as a function of the acid doping level. Increasing  $x$  decreases membrane gas permeability (cf. Fig. S3), which is consistent with the decreased  $d$ -spacing and *FFV*. H<sub>2</sub>/CO<sub>2</sub> selectivity increases dramatically with increasing  $x$  values due to the increased size-sieving ability, and thus H<sub>2</sub>/CO<sub>2</sub> diffusivity selectivity. At the same  $x$  values, PBI-TaA exhibits higher H<sub>2</sub>/CO<sub>2</sub> selectivity than PBI-OA due to the higher

cross-linking density in PBI-TaA. The PBI-TaA<sub>0.32</sub> exhibits H<sub>2</sub>/CO<sub>2</sub> selectivity as high as 45 at 35 °C.



**Fig. 4.** Pure-gas transport properties in PBI-OA and PBI-TaA at 35 °C. (a) H<sub>2</sub> permeability and H<sub>2</sub>/CO<sub>2</sub> selectivity as a function of the acid doping level. (b) CO<sub>2</sub> sorption isotherms. (c) H<sub>2</sub> (filled symbols) and CO<sub>2</sub> (open symbols) permeability and (d) H<sub>2</sub>/CO<sub>2</sub> selectivity as a function of 1/FFV. The curves in (b) are the best fits of the dual-mode sorption model (cf. Eq. 8). The lines in (c) and (d) are the best fits of the free volume model (Eq. 9).

Gas permeability can be decoupled to gas solubility and diffusivity. Fig. 4b compares CO<sub>2</sub>

sorption isotherms of PBI, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub> at 35 °C. Gas sorption ( $C_A$ , cm<sup>3</sup>(STP)/cm<sup>3</sup>) at a constant pressure ( $p_A$ , atm) for glassy polymers is often described using the dual-mode sorption model:<sup>29, 30</sup>

$$C_A = k_D p_A + \frac{C'_H b p_A}{1 + b p_A} \quad (8)$$

where  $k_D$  is Henry's constant,  $C'_H$  is Langmuir sorption capacity, and  $b$  is the affinity parameter. The PBI's CO<sub>2</sub> sorption in this study is slightly lower than those reported in the literature, presumably due to the different processing conditions.<sup>4, 7, 31, 32</sup> The sorption isotherms can be satisfactorily described using this model with the values of the adjustable parameters recorded in Table S2.

PBI-TaA<sub>0.32</sub> and PBI-OA<sub>0.49</sub> show almost the same CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub> sorption (cf. Fig. 4b and S4), which is slightly lower than PBI due to the lower *FFV* in the doped PBIs. These results suggest that the acid loading or chemical environment has a negligible effect on the gas sorption. By contrast, PBI-TaA<sub>0.32</sub> and PBI-OA<sub>0.49</sub> show CO<sub>2</sub> permeability of 0.0087 and 0.0090 Barrer, respectively (cf. Fig. S3). These values are ~95% lower than that of PBI (0.21 Barrer), indicating that the acid doping mainly affects gas diffusivity. Therefore, pure-gas permeability can be correlated with *FFV* using the free volume model:<sup>27</sup>

$$P_A = A_p \exp\left(-\frac{B_p}{FFV}\right) \quad (9)$$

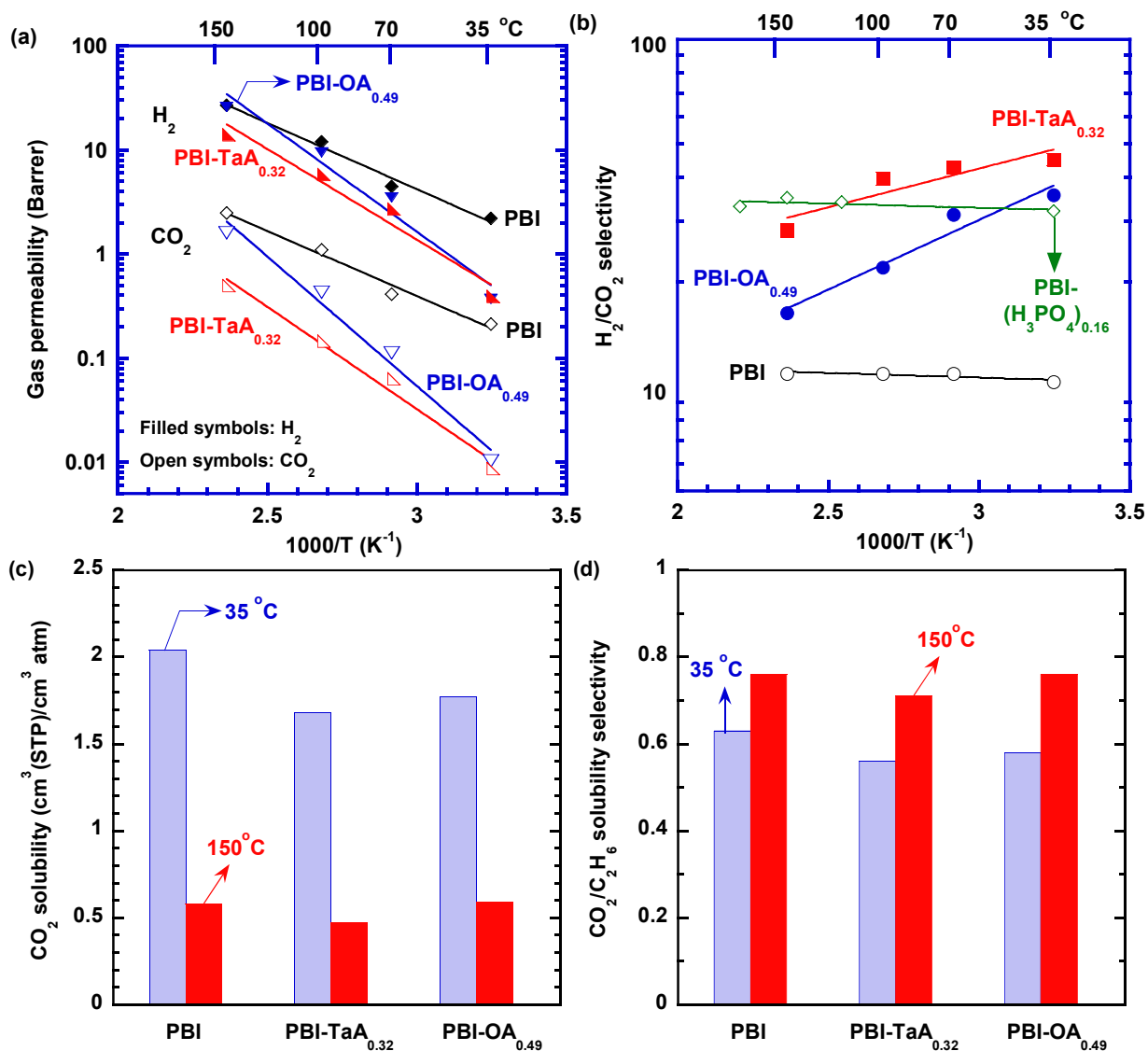
where  $A_p$  is a pre-exponential factor, and  $B_p$  is a constant that increases with increasing penetrant molecular size.

Fig. 4c shows that both H<sub>2</sub> and CO<sub>2</sub> permeability of PBI-OA, PBI-TaA, and PBI-H<sub>3</sub>PO<sub>4</sub> can be fitted with Eq. (9) with a  $B_p$  value of 0.90 for H<sub>2</sub> and 1.7 for CO<sub>2</sub>. The lower  $B_p$  value of H<sub>2</sub> is consistent with its smaller molecular size than CO<sub>2</sub>. Fig. 4d shows that the H<sub>2</sub>/CO<sub>2</sub> selectivity also correlates well with the free volume model, validating that the gas transport in these samples still follows the solution-diffusion mechanism. Both PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub> exhibit higher H<sub>2</sub>/CO<sub>2</sub> selectivity than PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub> at 35 °C, presumably because of their higher molar ratios of the protons to PBI repeating units and thus higher cross-linking density.

PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub> were chosen to investigate the effect of temperature on H<sub>2</sub>/CO<sub>2</sub> separation properties due to their high H<sub>2</sub>/CO<sub>2</sub> selectivity and similar content of the carboxylic acid groups, and the results are shown in Fig. 5a,b. The results for other acid-doped PBIs are reported in Table S3. The pure-gas permeability can be correlated with the temperature using the Arrhenius equation:

$$P_A = P_{A,0} \exp\left(\frac{-E_{P,A}}{RT}\right) \quad (10)$$

where  $P_{A,0}$  is a pre-exponential factor, and  $E_{P,A}$  is the activation energy for gas permeation. As shown in Fig. 5a, both H<sub>2</sub> and CO<sub>2</sub> permeability can be satisfactorily fitted with the parameters recorded in Table S4. The acid doping of PBI increases the  $E_{P,A}$  value due to the increased size-sieving ability. For example,  $E_{P,A}$  for H<sub>2</sub> is 24 kJ/mol for PBI, 33 kJ/mol for PBI-TaA<sub>0.32</sub>, and 40 kJ/mol for PBI-OA<sub>0.49</sub>, and  $E_{P,A}$  for CO<sub>2</sub> is 24 kJ/mol for PBI, 36 kJ/mol for PBI-TaA<sub>0.32</sub>, and 48 kJ/mol for PBI-OA<sub>0.49</sub>.



**Fig. 5.** Effect of temperature on pure-gas transport properties of PBI, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub>. (a) H<sub>2</sub> and CO<sub>2</sub> permeability; (b) H<sub>2</sub>/CO<sub>2</sub> selectivity; (c) CO<sub>2</sub> solubility and (d) CO<sub>2</sub>/C<sub>2</sub>H<sub>6</sub> solubility selectivity at 10 bar. The lines in (a) and (b) are the best fits of the Arrhenius equation.

Fig. 5b compares the effect of the temperature on pure-gas H<sub>2</sub>/CO<sub>2</sub> selectivity for PBI, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub>. PBI-TaA<sub>0.32</sub> exhibits the highest H<sub>2</sub>/CO<sub>2</sub> selectivity among PBI, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub> at all studied temperatures and higher than PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub> at 100 °C and below. Both PBI and PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub> exhibit the selectivity independence of temperature

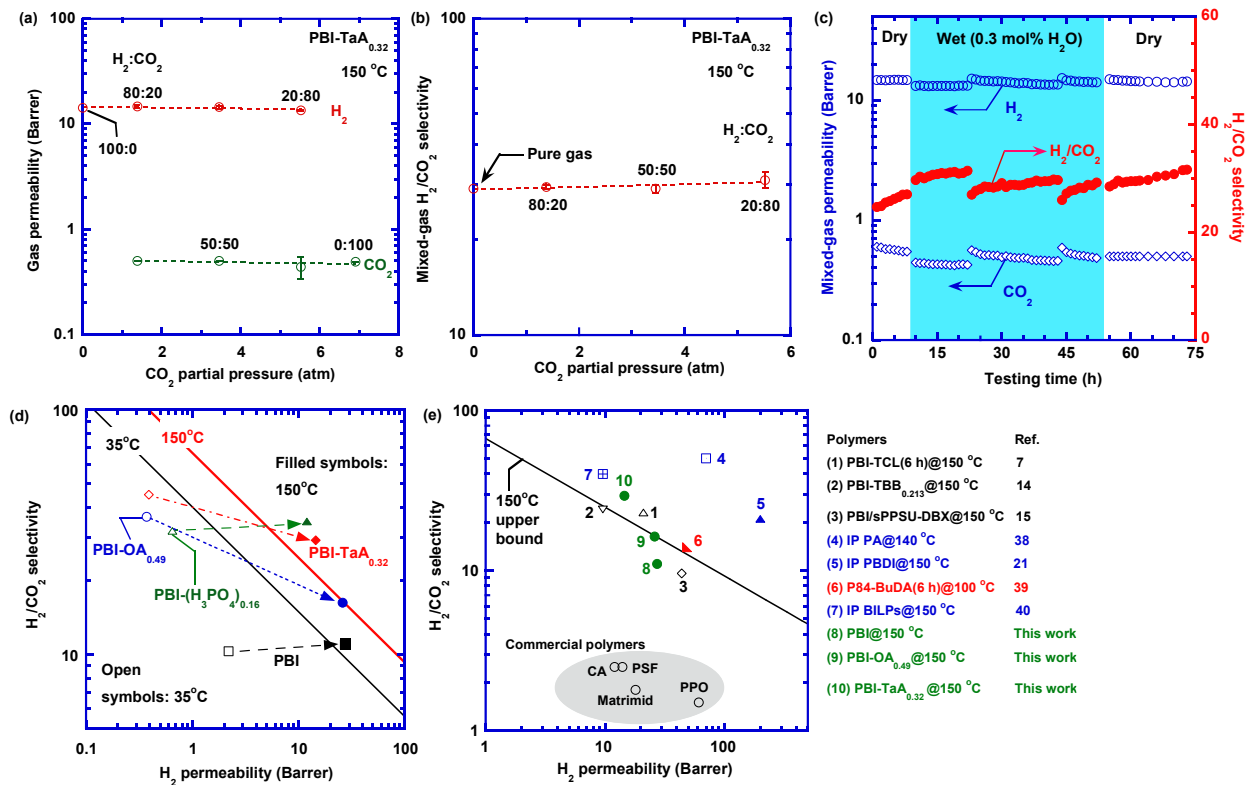
(consistent with the similar  $E_{P,A}$  values for H<sub>2</sub> and CO<sub>2</sub>), while the selectivity of PBI-OA<sub>0.49</sub> and PBI-TaA<sub>0.32</sub> decreases with increasing temperature (consistent with the lower  $E_{P,A}$  values for H<sub>2</sub> than CO<sub>2</sub>). For example, H<sub>2</sub>/CO<sub>2</sub> selectivity of PBI-OA<sub>0.49</sub> decreases from 40 to 18 as the temperature increases from 35 °C to 150 °C. The strong size-sieving ability derived from the cross-linking between PBI and OA or TaA appears to be weakened at elevated temperatures, as the hydrogen-bonded –NH becomes free at high temperature.<sup>33-35</sup> By contrast, the unchanged selectivity in PBI and PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub> suggests that the hydrogen bonding between PBI chains or between PBI and H<sub>3</sub>PO<sub>4</sub> remains strong up to 200 °C.

Fig. 5c,d presents the effect of temperature on CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub> solubility at 10 bar in PBI, PBI-TaA<sub>0.32</sub>, and PBI-OA<sub>0.49</sub>. H<sub>2</sub> sorption is too low to measure, and C<sub>2</sub>H<sub>6</sub> can serve as a surrogate for H<sub>2</sub> since both do not have polar or quadrupole moment to exhibit specific interactions with the polymers.<sup>4, 30, 35, 36</sup> Additionally, CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub> have a similar critical temperature (304.1 K and 305.3 K, respectively), and thus similar condensability. All samples show CO<sub>2</sub>/C<sub>2</sub>H<sub>6</sub> solubility selectivity less than 1, indicating no specific interaction between CO<sub>2</sub> and the acid-doped PBIs, despite the amine groups of PBI. Increasing the temperature decreases gas solubility (cf. Fig. S4) and slightly increases CO<sub>2</sub>/C<sub>2</sub>H<sub>6</sub> solubility selectivity. The acid doping slightly decreases the gas solubility and has a negligible effect on CO<sub>2</sub>/C<sub>2</sub>H<sub>6</sub> solubility selectivity, validating that the acid doping mainly affects gas diffusivity.

### 3.3 Superior H<sub>2</sub>/CO<sub>2</sub> separation performance of the acid-doped PBIs

PBI-TaA<sub>0.32</sub> shows the highest H<sub>2</sub>/CO<sub>2</sub> selectivity among the OA or TaA doped PBIs studied, and therefore, it was selected for further tests with three gas mixtures with H<sub>2</sub>:CO<sub>2</sub> molar ratio of

20:80, 50:50, and 80:20 at 7.9 bar and 150 °C. Fig. 6a shows that mixed-gas permeability is independent of CO<sub>2</sub> feed partial pressure and almost the same as the pure-gas permeability, indicating the absence of plasticization due to the low CO<sub>2</sub> sorption at high temperatures.<sup>37</sup> Fig. 6b shows the mixed-gas H<sub>2</sub>/CO<sub>2</sub> selectivity of ~30, which is also independent of the CO<sub>2</sub> feed partial pressure.



**Fig. 6.** Superior H<sub>2</sub>/CO<sub>2</sub> separation performance of PBI-TaA<sub>0.32</sub>. Effect of the feed CO<sub>2</sub> partial pressure on (a) mixed-gas H<sub>2</sub> and CO<sub>2</sub> permeability and (b) H<sub>2</sub>/CO<sub>2</sub> selectivity at 7.9 bar and 150 °C. (c) Long-term stability in dry-wet-dry conditions with H<sub>2</sub>/CO<sub>2</sub> of 50:50 at 7.9 bar and 150 °C for 90 h. (d) Pure-gas H<sub>2</sub>/CO<sub>2</sub> separation performance of PBI, PBI-OA, PBI-TaA, PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub>,<sup>4</sup> and PBI-(H<sub>2</sub>SO<sub>4</sub>)<sub>0.24</sub><sup>4</sup> at 35 °C and 150 °C benchmarking with Robeson's 2008 upper bounds. (e) Comparison between the cross-linked PBIs and commercial polymers: PBI-TCL(6 h),<sup>7</sup> PBI-TBB<sub>0.213</sub>,<sup>14</sup> PBI/sPPSU-DBX,<sup>15</sup> IP PA,<sup>38</sup> IP PBDI,<sup>21</sup> P84-BuDA(6 h),<sup>39</sup> and IP BILPs.<sup>40</sup>

Typical coal-derived syngas contains H<sub>2</sub>, CO<sub>2</sub>, water vapor, and other minor components

(such as H<sub>2</sub>S and CO) after the water-gas shift reaction. Fig. 6c presents the effect of water vapor on H<sub>2</sub>/CO<sub>2</sub> separation performance and long-term stability at 150 °C. The sample was first evaluated with a dry gas mixture of 50 % H<sub>2</sub> and 50 % CO<sub>2</sub> for 8 h. Then 0.3 mol% water vapor was introduced, and the test lasted for 43 h before the feed gas was switched back to the dry condition. Although H<sub>2</sub> permeability shows fluctuation with the wet gas, it remains at ~ 15 Barrer, and H<sub>2</sub>/CO<sub>2</sub> selectivity remained at ~ 30. The breaks were caused by the baking of the GC columns to remove residual water, which slightly changed the composition measurement. Both gas permeability and selectivity remain the same after switching back to the dry gas, indicating that PBI-TaA<sub>0.32</sub> is stable and has the potential for high-temperature H<sub>2</sub>/CO<sub>2</sub> separation.

Fig. 6d compares pure-gas H<sub>2</sub>/CO<sub>2</sub> separation performance of acid-doped PBIs, including PBI-OA<sub>0.49</sub>, PBI-TaA<sub>0.32</sub>, and PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>x</sub>, at 35 °C and 150 °C in Robeson's plot.<sup>4, 7, 41</sup> For the acid doped PBIs, the separation performance at 35 °C approaches the upper bound. By contrast, at 150 °C the acid-doped PBIs exhibit the separation properties above the upper bound. PBI-TaA<sub>0.32</sub> shows the H<sub>2</sub>/CO<sub>2</sub> separation properties similar to the PBI-(H<sub>3</sub>PO<sub>4</sub>)<sub>0.16</sub>.

Fig. 6e compares H<sub>2</sub>/CO<sub>2</sub> separation performance of PBI-TaA<sub>0.32</sub> and PBI-OA<sub>0.49</sub> at 150 °C with commercial membrane polymers, including polysulfone (PSF),<sup>42</sup> cellulose acetate (CA),<sup>43</sup> Matrimid,<sup>44, 45</sup> and poly(p-phenylene oxide) (PPO).<sup>46</sup> Commercial membrane polymers do not have good H<sub>2</sub>/CO<sub>2</sub> selectivity due to the lack of size-sieving ability. Highly cross-linked polyamides (PA) and poly(p-phenylene benzobisimidazole) (PBDI) via interfacial polymerization (IP) show excellent H<sub>2</sub>/CO<sub>2</sub> separation performance.<sup>21, 38</sup> Nevertheless, both PBI-TaA<sub>0.32</sub> and PBI-OA<sub>0.49</sub> show a good combination of high H<sub>2</sub> permeability and high H<sub>2</sub>/CO<sub>2</sub> selectivity.

## 4. Conclusions

We demonstrate that PBI can be effectively cross-linked by doping with polycarboxylic acids of OA and TaA to improve H<sub>2</sub>/CO<sub>2</sub> separation performance at elevated temperatures. The concentration of protons in the PBI films, instead of the acidity strength, plays an important role in influencing the separation properties. Increasing the proton content in PBI decreases the *d*-spacing and *FFV* and thus gas permeability and increases the size-sieving ability and thus H<sub>2</sub>/CO<sub>2</sub> selectivity. TaA has more acid groups than OA and is more effective in cross-linking PBI. The acid doping has a negligible effect on gas solubility, and its effect on gas permeability can be satisfactorily described using the free volume model. Increasing the temperature increases gas permeability and slightly decreases H<sub>2</sub>/CO<sub>2</sub> selectivity. PBI-TaA<sub>0.32</sub> exhibits superior and stable H<sub>2</sub>/CO<sub>2</sub> separation performance when challenged with wet gas mixtures, which surpasses Robeson's upper bound at 150 °C, indicating its promise for industrial H<sub>2</sub> purification and CO<sub>2</sub> capture.

## ASSOCIATED CONTENT

### Supporting Information.

WAXD patterns of PBI and PBI-OA<sub>0.49</sub> at varied temperatures; *FFV* calculation; pure-gas CO<sub>2</sub> permeability of PBI-OA and PBI-TaA at 35 °C; parameters of the dual-mode sorption model for CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub> sorption; and activation energy values for H<sub>2</sub> and CO<sub>2</sub> permeation in PBI, PBI-OA<sub>0.49</sub>, and PBI-TaA<sub>0.32</sub>.

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### **Notes**

The authors declare no competing financial interest.

### **Author Contributions**

The manuscript was written through the contributions of all authors. All authors have given approval to the final version of the manuscript.

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## **REFERENCES**

1. Dakhchoune, M.; Villalobos, L. F.; Semino, R.; Liu, L. M.; Rezaei, M.; Schouwink, P.; Avalos, C. E.; Baade, P.; Wood, V.; Han, Y.; Ceriotti, M.; Agrawal, K. V., Gas-Sieving Zeolitic Membranes Fabricated by Condensation of Precursor Nanosheets, *Nat. Mater.* **2020**, in press.
2. Lin, H.; Van Wagner, E.; Freeman, B. D.; Toy, L. G.; Gupta, R. P., Plasticization-Enhanced Hydrogen Purification Using Polymeric Membranes, *Science* **2006**, *311* (5761), 639-642.
3. Merkel, T. C.; Zhou, M. J.; Baker, R. W., Carbon Dioxide Capture with Membranes at an IGCC Power Plant, *J. Membr. Sci.* **2012**, *389*, 441-450.
4. Zhu, L.; Swihart, M.; Lin, H., Unprecedented Size-Sieving Ability in Polybenzimidazole Doped with Polyprotic Acids for Membrane H<sub>2</sub>/CO<sub>2</sub> Separation, *Energy Environ. Sci.* **2018**, *11* (1), 94-100.
5. Bui, M.; Adjiman, C. S.; Bardow, A.; Anthony, E. J.; Boston, A.; Brown, S.; Fennell, P. S.; Fuss, S.; Galindo, A.; Hackett, L. A., Carbon Capture and Storage (CCS): The Way Forward, *Energy Environ. Sci.* **2018**, *11* (5), 1062-1176.
6. Luo, S.; Zhang, Q.; Zhu, L.; Lin, H.; Kazanowska, B. A.; Doherty, C. M.; Hill, A. J.; Gao, P.; Guo, R., Highly Selective and Permeable Microporous Polymer Membranes for Hydrogen Purification and CO<sub>2</sub> Removal from Natural Gas, *Chem. Mater.* **2018**, *30* (15), 5322-5332.
7. Zhu, L.; Swihart, M.; Lin, H., Tightening Polybenzimidazole (PBI) Nanostructure via Chemical Cross-Linking for Membrane H<sub>2</sub>/CO<sub>2</sub> Separation, *J. Mater. Chem. A* **2017**, *5* (37), 19914-19923.
8. Hu, L.; Pal, S.; Nguyen, H.; Bui, V.; Lin, H., Molecularly Engineering Polymeric Membranes for H<sub>2</sub>/CO<sub>2</sub> Separation at 100–300 °C, *J. Polym. Sci.* **2020**, *58* (18), 2467-2481.
9. Park, H.; Kamcev, J.; Robeson, L. M.; Elimelech, M.; Freeman, B. D., Maximizing the Right Stuff: The Trade-off Between Membrane Permeability and Selectivity, *Science* **2017**, *356* (6343), eaab0530.
10. Koros, W. J.; Zhang, C., Materials for Next-Generation Molecularly Selective Synthetic Membranes, *Nat. Mater.* **2017**, *16* (3), 289-297.
11. Stevens, K. A.; Moon, J. D.; Borjigin, H.; Liu, R.; Joseph, R. M.; Riffle, J. S.; Freeman, B. D., Influence of Temperature on Gas Transport Properties of Tetraaminodiphenylsulfone (TADPS) Based Polybenzimidazoles, *J. Membr. Sci.* **2020**, *593*, 117427.
12. Singh, R. P.; Li, X.; Dudeck, K. W.; Benicewicz, B. C.; Berchtold, K. A., Polybenzimidazole Based Random Copolymers Containing Hexafluoroisopropylidene Functional Groups for Gas Separations at Elevated Temperatures, *Polymer* **2017**, *119*, 134-141.
13. Zhu, L.; Yin, D.; Qin, Y.; Konda, S.; Zhang, S.; Zhu, A.; Liu, S.; Xu, T.; Swihart, M. T.; Lin, H., Sorption-Enhanced Mixed Matrix Membranes with Facilitated Hydrogen Transport for Hydrogen Purification and CO<sub>2</sub> Capture, *Adv. Funct. Mater.* **2019**, *29* (36), 1904357.
14. Naderi, A.; Tashvigh, A. A.; Chung, T. S., H<sub>2</sub>/CO<sub>2</sub> Separation Enhancement via Chemical Modification of Polybenzimidazole Nanostructure, *J. Membr. Sci.* **2019**, *572*, 343-349.
15. Naderi, A.; Chung, T. S.; Weber, M.; Maletzko, C., High Performance Dual-Layer Hollow Fiber Membrane of Sulfonated Polyphenylsulfone/Polybenzimidazole for Hydrogen Purification, *J. Membr. Sci.* **2019**, *591*, 117292.
16. Zhu, L.; Omid, M.; Lin, H., Manipulating Polyimide Nanostructures via Crosslinking for

Membrane Gas Separation. In *Membranes for Gas Separations*, Carreon, M. A., Ed. World Scientific: 2017; Vol. 1, pp 243-270.

17. Gelb, R. I., Conductometric Determination of pKa Values. Oxalic and Squaric Acids, *Anal. Chem.* **1971**, 43 (8), 1110-1113.
18. Pfindt, L.; Dražić, B.; Popović, G.; Drakulić, B.; Vitnik, Z.; Juranić, I., Determination of All pKa Values of Some Di-and Tri-Carboxylic Unsaturated and Epoxy Acids and Their Polylinear Correlation with the Carboxylic Group Atomic Charges, *J. Chem. Res.* **2003**, 2003 (5), 247-248.
19. Qiu, W.; Chen, C.-C.; Kincer, M. R.; Koros, W. J., Thermal analysis and Its Application in Evaluation of Fluorinated Polyimide Membranes for Gas Separation, *Polymer* **2011**, 52 (18), 4073-4082.
20. Chithambaram, V.; Das, S. J.; Krishnan, S.; Ahamed, M. B.; Nambi, R. A., Growth and Characterization of Urea-oxalic Acid Crystals by Solution Growth Technique, *EPJ Appl. Phys.* **2013**, 64 (2), 55-62.
21. Shan, M.; Liu, X.; Wang, X.; Liu, Z.; Iziyi, H.; Ganapathy, S.; Gascon, J.; Kapteijn, F., Novel High Performance Poly(p-Phenylene Benzobisimidazole) (PBDI) Membranes Fabricated by Interfacial Polymerization for H<sub>2</sub> Separation, *J. Mater. Chem. A* **2019**, 7 (15), 8929-8937.
22. Han, S. H.; Lee, J. E.; Lee, K. J.; Park, H. B.; Lee, Y. M., Highly Gas Permeable and Microporous Polybenzimidazole Membrane by Thermal Rearrangement, *J. Membr. Sci.* **2010**, 357 (1-2), 143-151.
23. Hu, L.; Liu, J.; Zhu, L.; Hou, X.; Huang, L.; Lin, H.; Cheng, J., Highly Permeable Mixed Matrix Materials Comprising ZIF-8 Nanoparticles in Rubbery Amorphous Poly(ethylene oxide) for CO<sub>2</sub> Capture, *Sep. Purif. Technol.* **2018**, 205, 58-65.
24. Huang, L.; Liu, J.; Lin, H., Thermally Stable, Homogeneous Blends of Cross-Linked Poly(ethylene oxide) and Crown Ethers with Enhanced CO<sub>2</sub> Permeability, *J. Membr. Sci.* **2020**, 610, 118253.
25. Puleo, A. C.; Paul, D. R.; Wong, P. K., Gas Sorption and Transport In Semicrystalline Poly(4-methyl-1-pentene), *Polymer* **1989**, 30 (7), 1357-1366.
26. Golla, M.; Nagendra, B.; Rizzo, P.; Daniel, C.; de Ballesteros, O. R.; Guerra, G., Polymorphism of Poly(2,6-dimethyl-1,4-phenylene)oxide in Axially Stretched Films, *Macromolecules* **2020**, 53 (6), 2287-2294.
27. Park, J.; Paul, D. R., Correlation and Prediction of Gas Permeability in Glassy Polymer Membrane Materials via A Modified Free Volume Based Group Contribution Method, *J. Membr. Sci.* **1997**, 125 (1), 23-39.
28. Omidvar, M.; Nguyen, H.; Huang, L.; Doherty, C. M.; Hill, A. J.; Stafford, C. M.; Feng, X. S.; Swihart, M. T.; Lin, H., Unexpectedly Strong Size-Sieving Ability in Carbonized Polybenzimidazole for Membrane H<sub>2</sub>/CO<sub>2</sub> Separation, *ACS Appl. Mater. Interfaces* **2019**, 11 (50), 47365-47372.
29. Maeda, Y.; Paul, D., Effect of Antiplasticization on Gas Sorption and Transport. I. Polysulfone, *J. Polym. Sci., Part B: Polym. Phys.* **1987**, 25 (5), 957-980.
30. Smith, Z. P.; Tiwari, R. R.; Murphy, T. M.; Sanders, D. F.; Gleason, K. L.; Paul, D. R.; Freeman, B. D., Hydrogen Sorption in Polymers for Membrane Applications, *Polymer* **2013**, 54

(12), 3026-3037.

31. Miller, M. B.; Chen, D.; Luebke, D. R.; Johnson, J. K.; Enick, R. M., Critical Assessment of CO<sub>2</sub> Solubility in Volatile Solvents at 298.15 K, *J. Chem. Eng. Data* **2011**, *56* (4), 1565-1572.
32. Yang, M.; Han, Y.; Zou, E.; Chen, W.; Peng, X.; Dong, B.; Sun, C.; Liu, B.; Chen, G., Separation of IGCC Syngas by Using ZIF-8/Dimethylacetamide Slurry with High CO<sub>2</sub> Sorption Capacity and Sorption Speed but Low Sorption Heat, *Energy* **2020**, *201*, 117605.
33. Skrovanek, D. J.; Howe, S. E.; Painter, P. C.; Coleman, M. M., Hydrogen Bonding in Polymers: Infrared Temperature Studies of an Amorphous Polyamide, *Macromolecules* **1985**, *18* (9), 1676-1683.
34. Moskala, E. J.; Howe, S. E.; Painter, P. C.; Coleman, M. M., On the Role of Intermolecular Hydrogen Bonding in Miscible Polymer Blends, *Macromolecules* **1984**, *17* (9), 1671-1678.
35. Kelman, S.; Lin, H.; Sanders, E. S.; Freeman, B. D., CO<sub>2</sub>/C<sub>2</sub>H<sub>6</sub> Separation Using Solubility Selective Membranes, *J. Membr. Sci.* **2007**, *305* (1-2), 57-68.
36. Liu, J.; Zhang, S.; Jiang, D.-e.; Doherty, C. M.; Hill, A. J.; Cheng, C.; Park, H. B.; Lin, H., Highly Polar but Amorphous Polymers with Robust Membrane CO<sub>2</sub>/N<sub>2</sub> Separation Performance, *Joule* **2019**, *3* (8), 1881-1894.
37. Coleman, M.; Koros, W., Conditioning of Fluorine-Containing Polyimides. 2. Effect of Conditioning Protocol at 8 Volume Dilation on Gas-Transport Properties, *Macromolecules* **1999**, *32* (9), 3106-3113.
38. Ali, Z.; Pacheco, F.; Litwiller, E.; Wang, Y.; Han, Y.; Pinnau, I., Ultra-Selective Defect-Free Interfacially Polymerized Molecular Sieve Thin-Film Composite Membranes for H<sub>2</sub> Purification, *J. Mater. Chem. A* **2018**, *6* (1), 30-35.
39. Omidvar, M.; Stafford, C. M.; Lin, H., Thermally Stable Cross-Linked P84 with Superior Membrane H<sub>2</sub>/CO<sub>2</sub> Separation Properties at 100 °C, *J. Membr. Sci.* **2019**, *575*, 118-125.
40. Shan, M.; Liu, X.; Wang, X.; Yarulina, I.; Seoane, B.; Kapteijn, F.; Gascon, J., Facile Manufacture of Porous Organic Framework Membranes for Precombustion CO<sub>2</sub> Capture, *Sci. Adv.* **2018**, *4* (9), eaau1698.
41. Robeson, L. M., The Upper Bound Revisited, *J. Membr. Sci.* **2008**, *320* (1-2), 390-400.
42. Aitken, C. L.; Koros, W. J.; Paul, D. R., Effect of Structural Symmetry on Gas-Transport Properties of Polysulfones, *Macromolecules* **1992**, *25* (13), 3424-3434.
43. Puleo, A. C.; Paul, D. R.; Kelley, S. S., The Effect of Degree of Acetylation on Gas Sorption and Transport Behavior in Cellulose Acetate, *J. Membr. Sci.* **1989**, *47* (3), 301-332.
44. Vu, D.; Koros, W. J.; Miller, S. J., Mixed Matrix Membranes Using Carbon Molecular Sieves - I. Preparation and Experimental Results, *J. Membr. Sci.* **2003**, *211* (2), 311-334.
45. Zhang, Y.; Musseman, I. H.; Ferraris, J. P.; Balkus, K. J., Gas Permeability Properties of Matrimid (R) Membranes Containing the Metal-Organic Framework Cu-BPY-HFS, *J. Membr. Sci.* **2008**, *313* (1-2), 170-181.
46. Koros, W.; Fleming, G.; Jordan, S.; Kim, T.; Hoehn, H., Polymeric Membrane Materials for Solution-Diffusion Based Permeation Separations, *Prog. Polym. Sci.* **1988**, *13* (4), 339-401.

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