

Reinforcement Learning-based Hierarchical Seed Scheduling for Greybox Fuzzing

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Abstract—Coverage metrics play an essential role in greybox fuzzing. Recent work has shown that fine-grained coverage metrics could allow a fuzzer to detect bugs that cannot be covered by traditional edge coverage. However, fine-grained coverage metrics will also select more seeds, which cannot be efficiently scheduled by existing algorithms. This work addresses this problem by introducing a new concept of multi-level coverage metric and the corresponding reinforcement-learning-based hierarchical scheduler. Evaluation of our prototype on DARPA CGC showed that our approach outperforms AFL and AFLFAST significantly: it can detect 20% more bugs, achieve higher coverage on 83 out of 180 challenges, and achieve the same coverage on 60 challenges. More importantly, it can detect the same number of bugs and achieve the same coverage faster. On FuzzBench, our approach achieves higher coverage than AFL++ (Qemu) on 10 out of 20 projects.

I. INTRODUCTION

Greybox fuzzing is a state-of-the-art testing technique that has been widely adopted by the industry and has successfully found tens of thousands of vulnerabilities in widely used software. For example, the OSS-Fuzz [20] project has found more than 10,000 bugs in popular open-sourced projects like OpenSSL since its launch in December 2016.

As shown in Figure 1, greybox fuzzing can be modeled as a genetic process where new inputs are generated through mutation and crossover/splice. The generated inputs are selected according to a fitness function. Selected inputs are then added back to the seed pool for future mutation. Unlike natural evolution, due to the limited processing capability, only a few inputs from the seed pool will be scheduled to generate the next batch of inputs. For example, a single fuzzer instance can only schedule one seed at a time.

The most common fitness function used by off-the-shelf fuzzers like American Fuzzy Lop (AFL) [55] is edge coverage, i.e., inputs that cover new branch(es) will be added to the seed pool, as its goal is to achieve higher edge coverage of the code. While most fuzzers are coverage-guided (i.e., use new coverage as the fitness function), recent research has shown that the genetic process can also be used to discover

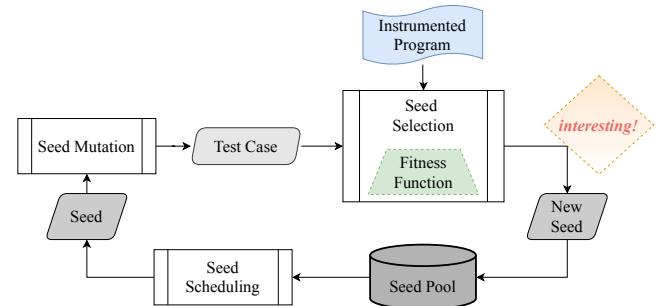


Fig. 1: Overview of greybox fuzzing

a diversity of program properties by using a variety of fitness functions [26], [32], [34].

An important property of a fitness function (e.g., a coverage metric) is its ability to preserve intermediate waypoints [32]. To better illustrate this, consider flipping a magic number check $a = 0xdeadbeef$ as an example. If a fuzzer only considers edge coverage, then the probability of generating the correct a with random mutations is 2^{32} . However, if the fuzzer can preserve important waypoints, e.g., by breaking the 32-bit magic number into four 8-bit number [25], then solving this checking will be much more efficient since the answer can be generated from a sequence as $0xef$, $0xbeef$, $0xadbeef$, and $0xdeadbeef$. This check can also be solved faster by understanding distances between current value of a and the target value [12]–[14], [18], [42]. More importantly, recent research has shown that many program states *cannot* be reached without saving critical waypoints [30], [45].

Wang et al. [45] formalize the ability to preserve intermediate waypoints as the *sensitivity* of a coverage metric. Conceptually, a more sensitive metric would lead to more program states (e.g., code coverage). However, the empirical evaluation of [45] shows that this is not always the case. The reason is that, a more sensitive coverage metric will select more seeds, which could cause seed explosion and exceed the fuzzer's ability to schedule. As a result, many seeds may never be scheduled or be scheduled without enough time/power to make a breakthrough [9].

In this work, we aim to address the seed explosion problem with a *hierarchical scheduler*. Specifically, fuzzing can be modeled as a multi-armed bandit (MAB) problem [49], where the scheduler needs to balance between *exploration* and *exploitation*. With a more sensitive coverage metric like branch distance, exploitation can be considered as focusing on solving a hard branch (e.g., magic number check), and exploration can

be considered as exercising an entirely different function. Our crucial observation is that when a coverage metric C_j is more sensitive than C_i , we can use C_j to save all the intermediate waypoints without losing the ability to discover more program states; but at the same time, we can use C_i to cluster seeds into a representative node and schedule at node level to achieve better exploration. More specifically, the scheduler will choose a node first, and then choose a seed in that node. Based on this observation, we propose to organize the seed pool as a multi-level tree where leaf nodes are real seeds and internal nodes are less sensitive coverage measurements. The closer a node is to the leaf, the more sensitive the corresponding coverage measurement is. Then we can utilize the existing MAB algorithms to further balance between exploitation and exploration.

To validate our idea, we implemented two prototypes: one AFL-HIER based on AFL and the other AFL++-HIER based on AFL++. We performed extensive evaluation on the DARPA Cyber Grand Challenge (CGC) dataset [10] and Google FuzzBench [21] benchmarks. Compared to AFLFAST [9], AFL-HIER can find more bugs in CGC (77 vs. 61). AFL-HIER also achieved better coverage in about 83 of 180 challenges and the same coverage on 60 challenges. More importantly, AFL-HIER can find the same amount of bugs and achieve the same coverage faster than AFLFAST. On FuzzBench, AFL++-HIER achieved higher coverage on 10 out of 20 projects than AFL++ (Qemu).

Contributions. This paper makes the following contributions:

- We propose multi-level coverage metrics that bring a novel approach to incorporate sensitive coverage metrics in greybox fuzzing.
- We design a hierarchical seed scheduling algorithm to support the multi-level coverage metric based on the multi-armed bandits model.
- We implement our approach as an extension to AFL and AFL++ and release the source code at <https://github.com/bitsecurerlab/aflplusplus-hier>.
- We evaluate our prototypes on DARPA CGC and Google FuzzBench. The results show that our approach not only can trigger more bugs and achieve higher code coverage, but also can achieve the same coverage faster than existing approaches.

II. BACKGROUND

A. Greybox Fuzzing

Algorithm 1 illustrates the greybox fuzzing process in more detail. Given a program to fuzz and a set of initial seeds, the fuzzing process consists of a sequence of loops named rounds. Each round starts with selecting the next seed for fuzzing from the pool according to the scheduling criteria. The scheduled seed is assigned to a certain amount of power that determines how many new test cases will be generated in this round. Next, test cases are generated through (random) mutation and crossover based on the scheduled seed. Compared to blackbox and whitebox fuzzing, the most distinctive step of greybox fuzzing is that, when executing a newly generated input, the fuzzer uses lightweight instrumentations to capture runtime features and expose them to the fitness function to measure the

“quality” of a generated test case. Test cases with good quality will then be saved as a new seed into the seed pool. This step allows a greybox to gradually evolve towards a target (e.g., more coverage). The effectiveness and efficiency of greybox fuzzing depend on the following factors.

Algorithm 1: Greybox Fuzzing Algorithm

```

Input: target program  $P$ , set of initial seeds  $S^0$ 
Output: unique seed set  $S^*$ ,
          bug-triggering seed set  $S^v$ 
Data: seed  $s$  and test case  $I$ 
Function Main( $P, S^0$ ):
  1    $S^* \leftarrow S^0$ 
  2    $S^v \leftarrow \emptyset$ 
  3   while true do
  4      $s \leftarrow \text{SelectNextSeedToFuzz}(S^*)$ 
  5      $s.\text{power} \leftarrow \text{AssignPower}()$ 
  6     while  $s.\text{power} > 0$  do
  7        $s.\text{power} \leftarrow s.\text{power} - 1$ 
  8        $I \leftarrow \text{MutateSeed}(s)$ 
  9        $\text{status} \leftarrow \text{RunAndEval}(I)$ 
 10      if  $\text{status}$  is Bug then
 11         $S^v \leftarrow S^v \cup \{I\}$ 
 12      else if  $\text{status}$  is NewCovExplored then
 13         $S^* \leftarrow S^* \cup \{I\}$ 
 14      else
 15         $\text{continue} // \text{ drop } I$ 
 16      end
 17    end
 18     $\text{PayReward}(s)$ 
 19  end
 20 end
 21 End

```

Test case measurement. As a genetic process, the fitness function of the fuzzer decides what kind of program properties the fuzzer can discover [32]. While fuzzing has been successfully applied to many different domains in recent years with different fitness functions, the most popular one is still code coverage (i.e., a test case that triggers new coverage will be saved as a new seed). However, coverage measurements can be diverse. Notably, AFL [55] measures the edge coverage of test cases. More precisely, it maintains a global map where the hashed value of an edge (i.e., the pair of the current basic block address and the next basic block address) is used as an indexing key to access the `hit_count` of the edge, which records how many times it has been taken so far. The hit counts are bucketized into small powers of two. After a test case completes its execution, the global `hit_count` map will be updated according to its edges, and it will be selected as a new seed if a new edge is found or the hit count of one edge increases into a new bucket. As we can see, this measurement does not consider the order of edges and can miss interesting seeds if the hash of a new edge collides with the hash of an already covered edge [19].

Seed scheduling criteria. The limited processing capability makes it essential to prioritize some seeds over others in order to maximize the coverage. For example, AFL [55] prefers seeds with small sizes and short execution time to achieve a higher fuzzing throughput. Furthermore, it maintains

a minimum set of seeds that stress all the code coverage so far, and focus on fuzzing them (i.e., prefers exploitation). AFLFAST [9] models greybox fuzzing as a Markov chain and prefers seeds exercising paths that are rarely exercised, as high-frequency paths tend to be covered by invalid test cases. LIBFUZZER [39] prefers seeds generated later in a fuzzing campaign. Entropic [7] prefers seeds with higher information gains.

Seed mutation strategy. The mutation strategy decides how likely a new test case could trigger new coverage(s) and be selected as a new seed. Off-the-shelf fuzzers like AFL and LIBFUZZER use random mutation and crossover. Recent work aims to improve the likelihood by using data-flow analysis to identify which input bytes should be mutated [18], [37], [52], by using directed searching [12], [13], [40], [42], and by learning the best mutation strategies [11], [29].

Fuzzing throughput. Fuzzing throughput is another critical factor that decides how fast a fuzzer can discover new coverage. AFL [55] uses the fork server and persistent mode to reduce initialization overhead, thus improving the throughput. Xu et al. [51] proposed new OS primitives to improve fuzzing throughput further. FirmAFL [57] uses augmented emulation to speed-up fuzzing firmware. Because high throughput is the key factor that allows greybox fuzzers to beat whitebox fuzzers in practice, one must pay special attention to the trade-off between throughput and the above three factors (coverage measurement, scheduling algorithm, and mutation strategy). That is, improvements of the above three factors at the cost of throughput may unexpectedly result in worse fuzzing performance.

B. Multi-Armed Bandit Model

The multi-armed bandit model offers a fundamental framework for algorithms that learn optimal resource allocation policies over time under uncertainty. The term “bandit” comes from a gambling scenario where the player faces a row of slot machines (also known as one-armed bandits) yielding random payoffs and seeks the best strategy of playing these machines to gain the highest long-term payoffs.

In the basic formulation, a multi-armed bandit problem is defined as a tuple $(\mathcal{A}, \mathcal{R})$, where \mathcal{A} is a known set of K arms (or actions) and $\mathcal{R}^a(r) = \mathbb{P}[r|a]$ is an unknown but fixed probability distribution over rewards. At each time step t the agent selects an arm a_t , and observes a reward $r_t \sim \mathcal{R}^{a_t}$. The objective is to maximize the cumulative rewards $\sum_{t=1}^T r_t$.

Initially, the agent has no information about which arm is expected to have the highest reward, so it tries some randomly and observes the rewards. Then the agent has more information than before. However, it has to face the trade-off between “exploitation” of the arm that is with the highest expected reward so far, and “exploration” to obtain more information about the expected rewards of the other arms so that it does not miss out on a valuable one by simply not trying it enough times.

Various algorithms are proposed to make the optimal trade-off between exploitation and exploration of arms. Upper Confidence Bound (UCB) algorithms [5] are a family of

bandit algorithms that perform impressively. Specifically, they construct a confidence interval to estimate each arm’s true reward, and select the arm with the highest UCB each time. Notably, the confidence interval is designed to shrink when the arm with its reward is sampled more. As a result, while the algorithm tends to select arms with high average rewards, it will periodically try less explored arms since their estimated rewards have wider confidence intervals.

Take UCB1 [2], which is almost the most fundamental one, as an example. It starts with selecting each arm once to obtain an initial reward. Then at each time step, it selects arm a that maximizes $Q(a) + C \times \sqrt{\frac{\log(N)}{n_a}}$ where $Q(a)$ is the average reward obtained from arm a , C is a predefined constant that is usually set to $\sqrt{2}$, N is the overall number of selections done so far, and n_a is the number of times arm a has been selected.

Seed scheduling can be modeled as a multi-armed bandit problem where seeds are regarded as arms [49], [54]. However, to make the fuzzer benefit from this model, such as maximizing the code coverage, we need to design the reward of scheduling a seed carefully.

III. MULTI-LEVEL COVERAGE METRICS

In this section, we discuss what are multi-level coverage metrics and why they are useful for greybox fuzzing.

A. Sensitivity of Coverage Metrics

Given a mutation-based greybox fuzzer, a fuzzing campaign starts with a set of initial seeds. As the fuzzing goes on, more seeds are added into the seed pool through mutating the existing seeds. By tracking the evolution of the seed pool, we can see how each seed can be traced back to an initial seed via a mutation chain, in which each seed is generated from mutating its immediate predecessor. If we consider a bug triggering test case as the *end* of a chain and the corresponding initial seed as the *start*, those internal seeds between them serve as waypoints that allow the fuzzer to gradually reduce the search space to find the bug [32].

The coverage metric used by a fuzzer plays a vital role in creating such chains, from two main aspects. First, if the chain terminates earlier before reaching the bug triggering test case, then the bug may never be discovered by the fuzzer. Wang et al. [45] formally model this ability to preserve critical waypoints in seed chains as the *sensitivity* of a coverage metric. For example, consider the maze game in Listing 1, which is widely used to demonstrate the capability of symbolic execution of exploring program states. In this game, a player needs to navigate the maze via the pair of (x, y) that determines a location for each step. In order to win the game, a fuzzer has to try as many sequences of (x, y) pairs as possible to find the right route from the starting location to the crashing location. This simple program is very challenging for fuzzers using edge coverage as the fitness function, because there are only four branches related to every pair of (x, y) , each checking against a relatively simple condition that can be satisfied quite easily. For instance, five different inputs: “a,” “u,” “d,” “l,” and “r” are enough to cover all branches/cases of the `switch` statement. After this, even if the fuzzer can generate new interesting

```

1  char maze[7][11] = {
2      "++-----+",
3      "| | | # | |",
4      "| | -+ | | |",
5      "| | | | | | |",
6      "| +-- | | | |",
7      "| | | | | |",
8      "+-----+";
9  int x = 1, y = 1;
10 for (int i = 0; i < MAX_STEPS; i++) {
11     switch (steps[i]) {
12         case 'u': y--; break;
13         case 'd': y++; break;
14         case 'l': x--; break;
15         case 'r': x++; break;
16         default:
17             printf("Bad step!"); return 1;
18     }
19     if (maze[y][x] == '#') {
20         printf("You win!");
21         return 0;
22     }
23     if (maze[y][x] != ' ') {
24         printf("You lose.");
25         return 1;
26     }
27 }
28 return 1;

```

Listing 1: A Simple Maze Game

inputs that indeed advance the program’s state towards the goal (e.g., “dd”), these inputs will *not be selected as new seeds* because they do not provide new edge coverage. As a result, it is extremely hard, if not impossible, for fuzzers that use the edge coverage to win the game [3].

On the contrary, as we will show in §V-G, if a fuzzer can measure the different combinations of x and y (e.g., by tracking different memory accesses via $*(maze + y + x)$ at line 10), then reaching the winning point will be much easier [3], [45]. Similarly, researchers have also observed that the orderless of branch coverage and hash collisions can cause a fuzzer to drop critical waypoints hence prevent certain code/bugs from being discovered [19], [27], [30].

The second impact of a coverage metric has on creating seed chains is the *stride* between a pair of seeds in a chain. Specifically, the sensitivity of a coverage metric also determines how likely (i.e., the probability) a newly generated test case will be saved as a new seed. For instance, it is easier for a fuzzer that uses edge coverage to discover a new seed than a fuzzer that uses block coverage. Similarly, as we have discussed in §I, it is much easier to find a match for an 8-bit integer than a 32-bit integer. Böhme et al. [9] model the minimum effort to discover a neighbouring seed as the required *power* (i.e., mutations). Based on this modeling, a more sensitive coverage metric requires less power to make progress, i.e., a shorter stride between two seeds. Although each seed only carries a small step of progress, the accumulation of them can narrow the search space faster.

While the above discussion seems to suggest that a more sensitive coverage metric would allow fuzzers to detect more

bugs, the empirical results from [45] showed this is not always the case. For instance, while memory access coverage would allow a fuzzer to win the maze game (Listing 1), it did not perform very well on many of the DARPA CGC challenges. The reason is that, a more sensitive coverage metric will also create a larger seed pool. As a result, the seed scheduler needs to examine more candidates each time when choosing the next seed to fuzz. In addition to the increased workload of the scheduler, a larger seed pool also increases the difficulty of seed exploration, i.e., trying as many fresh seeds as possible. Since the time of a fuzzing campaign is fixed, more abundant seeds also imply that the average fuzzing time of each seed could be decreased, which could negatively affect seed exploitation, i.e., not fuzzing interesting seeds enough time to find critical waypoints.

Overall, a more sensitive coverage metric boosts the capability (i.e., upper bound) of a fuzzer to explore deeper program states. Nevertheless, in order to effectively utilize its power and mitigate the side effects of the resulting excessive seeds, the coverage metric and the corresponding seed scheduler should be carefully crafted to strike a balance between exploration and exploitation.

B. Seed Clustering via Multi-Level Coverage Metrics

The similarity and diversity of seeds, which can be measured in terms of the exercised coverage, drive the seed exploration and exploitation in a fuzzing campaign. In general, a set of similar seeds gains less information about the program under test than a set of diverse seeds. When a coverage metric measures more fine-grained coverage information (e.g., edge), it can dim the coarse-grained diversity (e.g., block) among different seeds. First, it encourages smaller variances between seeds. Second, it loses the awareness of the potential larger variance between seeds that can be detected by a more coarse-grained metric. For instance, a metric measuring edge coverage is unaware of whether two seeds exercise two different sets of basic blocks or the same set of basic blocks but through different edges. Therefore, it is necessary to illuminate seed similarity and diversity when using a more sensitive coverage metric.

Clustering is a technique commonly used in data analysis to group a set of similar objects. Objects in the same cluster are more similar to each other than to those in a different cluster. Inspired by this technique, we propose to perform seed clustering so that seeds in the same cluster are similar while seeds in different clusters are more diverse. In other words, these clusters offer another perspective that allows a scheduler to zoom in the similarity and diversity among seeds.

Based on the observation that the sensitivity of most coverage metrics for greybox fuzzing can be directly compared (i.e., the more sensitive coverage metric can subsume the less sensitive one), we propose an intuitive way to cluster seeds—using a coarse-grained coverage measurement to cluster seeds selected by a fine-grained metric. That is, seeds in the same cluster will have the same coarse-grained coverage measurement. Moreover, we can use more than one level of clustering to provide more abstraction at the top level and more fidelity at the bottom level. To this end, the coverage metric should allow the co-existence of multiple coverage measurements. We name such a coverage metric a *multi-level coverage metric*.

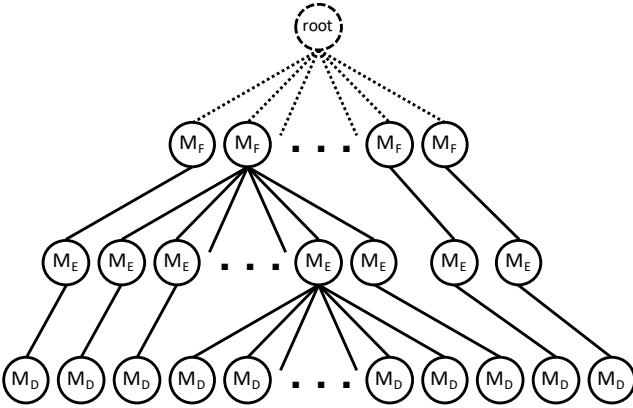


Fig. 2: A multi-level coverage metric that measures function coverage at top-level, edge coverage at mid-level, and hamming distance of comparison operands at leaf-level. The root node is a virtual node only used by the scheduler.

C. Incremental Seed Clustering

With the multi-level coverage metric in place, if a test case is assessed as exercising a new coverage (feature) by any of the measurements, it will be retained as a new seed and put in a proper cluster as described in [Algorithm 2](#). Generally, except for the top-level measurement M_1 that directly classifies all seeds into different clusters, the following lower-level measurement M_i ($i = 2, \dots, n$) works on each of the clusters generated by M_{i-1} separately, classifying seeds in it into smaller sub-clusters, which is named incremental seed clustering.

In more detail, given a multi-level coverage metric as shown in [Figure 2](#), a test case exercising any new function, edge, or distance coverage will be assessed as a new seed. Then the root node starts the seed clustering. It will find from its child nodes an existing M_F node that covers the same functions as the new seed, or create a new M_F node if the desired node does not exist. Next, the seed clustering continues in a similar way that puts the new seed into a M_E node with the same edge coverage. Finally, a child M_D node of the M_E node is selected to save the new seed according to its distance coverage.

Terms used in the algorithm are defined as follows.

Definition III.1. A coverage space Γ defines the set of enumerable features we pay attention to that can be covered by executing a program.

Some typical coverage spaces are:

- Γ_F is the set of all program functions.
- Γ_B is the set of all program blocks.
- Γ_E is the set of all program edges. Note that an edge is a transition from one block to the next.

It is worth mentioning that in real-world fuzzers such as AFL, the coverage information is recorded via well-crafted hit_count maps. Consequently, the features are signified by entries of the maps.

Definition III.2. A coverage metric $C : (\mathcal{P} \times \mathcal{I}) \rightarrow \Gamma^*$ measures the execution of a program $P \in \mathcal{P}$ with an input

$I \in \mathcal{I}$, and produces a set of features that are exercised by it at least once, denoted as $M \in \Gamma^*$.

Since coverage metric is mainly characterized by the coverage space Γ , it can be simplified with the coverage space. Some typical coverage metrics are:

- C_F measures the functions that are exercised by an execution.
- C_B measures the blocks that are exercised by an execution.
- C_E measures the edges that are exercised by an execution.

Finally, we give the definition of a multi-level coverage metric.

Definition III.3. A coverage metric $C^n : (\mathcal{P} \times \mathcal{I}) \rightarrow \langle \Gamma_1^*, \dots, \Gamma_n^* \rangle$ consists of a sequence of coverage metrics $\langle C_1, \dots, C_n \rangle$. It measures the execution of a program $P \in \mathcal{P}$ with an input $I \in \mathcal{I}$, and produces a sequence of measurements $\langle M_1, \dots, M_n \rangle$.

A multi-level coverage metric combines multiple metrics at different levels to assess a seed. As a result, it relies on lower-level coverage measurements to preserve minor variances among seeds so that there will be more abundant seeds in a chain. This helps to reduce the search space of finding bug triggering test cases. Meanwhile, it allows a scheduler to use upper-level measurements to detect major differences among seeds. Note that when $n = 1$, it is reduced to a traditional single level coverage metric.

D. Principles and Examples of Multi-level Coverage Metrics

To further illustrate how a multi-level coverage metric works, we propose some representative examples. We first discuss some principles for developing an effective multi-level coverage metric $C^n \sim \langle C_1, \dots, C_n \rangle$ for fuzzing a program P .

1) Principles: Through the incremental seed clustering, all seeds are put into a hierarchical tree that lays the foundation of our hierarchical seed scheduling algorithm, which will be described in [§IV](#). However, the scheduling makes sense only when a node at an upper level can have multiple child nodes at lower levels. This indicates that the cases where if a set of seeds are assessed to be with the same coverage measurement M_i , all following measures M_{i+1}, \dots, M_n will also be the same should be excluded. Motivated by this fundamental requirement, the main principle is that measurements generated by a less sensitive metric should always cluster seeds prior to more sensitive ones. Here, we use the same definition of sensitivity between two coverage metrics as in [\[45\]](#).

Definition III.4. Given two coverage metrics C_i and C_j , we say C_i is “more sensitive” than C_j , denoted as $C_i \succ_s C_j$, if

- (i) $\forall P \in \mathcal{P}, \forall I_1, I_2 \in \mathcal{I}, C_i(P, I_1) = C_i(P, I_2) \rightarrow C_j(P, I_1) = C_j(P, I_2)$, and
- (ii) $\exists P \in \mathcal{P}, \exists I_1, I_2 \in \mathcal{I}, C_j(P, I_1) = C_j(P, I_2) \wedge C_i(P, I_1) \neq C_i(P, I_2)$

Specifically, take the multi-level metric in [Figure 2](#) as an example. Seeds in the same M_F clusters must have the same function coverage. However, since M_E is more sensitive than

Algorithm 2: Seed Selection Algorithm

Input: test case I
Output: return a status code indicating whether I triggers a bug or covers new features
Data: program being fuzzed P ,
existing seed set S^* ,
existing feature set M^* ,
current working cluster cc ,
map from feature sets to sub clusters $cc.map$,
coverage metric $C^n \sim \langle C_1, \dots, C_n \rangle$
coverage measurements $\langle M_1, \dots, M_n \rangle$

Result: put I in a proper cluster if it is a new seed

1 Function RunAndEval (I):

2 $\langle M_1, \dots, M_n \rangle \leftarrow$
 RunWithInstrument (P, I, C^n)

3 **if** bug triggered **then**
4 | **return** Bug
5 **end**
6 $M^t \leftarrow M_1 \cup \dots \cup M_n$
7 **if** $M^t \subseteq M^*$ **then**
8 | **return** Known
9 **else**
10 | $M^* \leftarrow M^* \cup M^t$
11 | **foreach** $i \in \{1, \dots, n\}$ **do**
12 | $next_cc \leftarrow cc.map[M_i]$
13 | **if** $next_cc = NULL$ **then**
14 | | $next_cc \leftarrow new_cluster()$
15 | **end**
16 | move I into $next_cc$
17 | $cc.map[M_i] \leftarrow next_cc$
18 | $cc \leftarrow next_cc$
19 | **end**
20 | **return** NewCovExplored
21 **end**
22 **End**

M_F , these seeds are likely to have different edge coverage, resulting in multiple different sub-clusters. However, if we use M_E to cluster seeds prior to M_F , since seeds with the same edge coverage must also have the same function coverage, it is impossible further to put them into different sub- M_F clusters. As a result, each M_E node will have only a single M_F node, making the clustering useless.

As discussed in [45], \succ_s is a partial order, so it is possible that two metrics are not comparable. To solve this problem, we propose a weaker principle: given two non-comparable coverage metrics, we should cluster a seed with the metric that will select fewer seeds before the one that will select more seeds.

2) *Examples:* Following the above principles, we propose two multi-level coverage metrics as examples. Both examples use three-level clustering that works well in our evaluation.

The top-level metric in both examples is C_F , which measures the function coverage. The middle-level metric is edge coverage C_E . Functions invoked are essential runtime features that are commonly used to characterize an execution, and edge coverage is widely used in fuzzers such as AFL and LIBFUZZER. Notably $C_E \succ_s C_F$.

The most important one is the bottom-level metric, which is the most sensitive one. In this work, we mainly evaluated a bottom-level metric called *distance* metric C_D . It traces conditional jumps (i.e., edges) of a program execution, calculates the hamming distances of the two arguments of the conditions as covered features, and treats each observed new distance of a conditional jump as new coverage. Unlike C_E or C_F that traces control flow features, C_D focuses on data-flow features and actively accumulates progress made in passing condition checks for fuzzing.

To understand whether our approach can support different coverage metrics (fitness functions), we also evaluated another coverage metric called *memory access* metric C_A . As the name implies, this metric traces all memory reads and writes, captures continuous access addresses as array indices, and treats each new index of a memory access as new coverage. C_A pays attention to data flow features and accumulates progress made in accessing arrays that might be long. To distinguish memory accesses that happen at different program locations, the measurement also includes the address of the last branch. However, since not all basic blocks contain memory accesses, C_A is not directly comparable to C_E using sensitivity. However, we observe that C_A can generate much more seeds than C_E , so C_A comes after C_E and its measurement M_A stays at the bottom level.

IV. HIERARCHICAL SEED SCHEDULING

This section discusses how to schedule seeds against hierarchical clusters generated by a multi-level coverage metric.

A. Scheduling against A Tree of Seeds

Conceptually, a multi-level coverage metric $C^n \sim \langle C_1 \dots C_n \rangle$ organizes coverage measurements (M_i) and seeds as a tree, where each node at layer (or depth) $i \in \{1, \dots, n\}$ represents a cluster represented by M_i and its child nodes at layer $i+1$ represent sub-clusters represented by M_{i+1} . At leaf-level, each node is associated with real seeds. Additionally, at layer 0 is a virtual root node representing the whole tree. To schedule a seed, the scheduler needs to seek a path from the root to a leaf node.

Exploration vs Exploitation. The main challenge a seed scheduler faces is the trade-off between seed exploration (trying out other fresh seeds) and exploitation (keep fuzzing a few interesting seeds to trigger a breakthrough). On the one hand, fresh seeds that have rarely been fuzzed may lead to surprisingly new coverage. On the other hand, a few valuable seeds that have led to significantly more new coverage than others in recent rounds encourage to focus on fuzzing them.

Organizing seeds in a tree with hierarchical clusters facilitates a more flexible control over the seed exploration and exploitation. Specifically, fuzzers can focus on a single cluster in which seeds cover the same functions at the first layer and then try out many (sub-)clusters with seeds exercising different edges at the second layer. Alternatively, fuzzers can also try out seeds exercising different groups of functions, then only pick seeds covering some specific edges.

In this work, we explore the feasibility of modeling the fuzzing process as a multi-armed bandit (MAB) problem [49], [54] and using the existing MAB algorithms to balance between exploitation and exploration. After trying several different MAB algorithms, we decide to adopt the UCB1 algorithm [2], [5] to schedule seeds, since it works the best empirically, despite being one of the simplest MAB algorithms. As illustrated by function `SelectNextSeedToFuzz()` in [Algorithm 3](#), starting from the root node, our scheduling algorithm selects the child node with the highest score, which is calculated based on the coverage measurements, until reaching the last layer to select among leaf nodes that are associated with real seeds. Because all seeds have the same coverage at the leaf level, we scheduling them with round robin for simplicity.

At the end of each round of fuzzing, nodes along the scheduled path will be rewarded based on how much progress the current seed has made in this round, e.g., whether there are new coverage features exercised by all the generated test cases. In this way, seeds that perform well are expected to have increased scores for competing in the following rounds, while seeds making little progress will be de-prioritized.

Note that a traditional MAB problem assumes a fixed number of arms (nodes in our case) so that all arms can get an estimation of their rewards at the beginning. However, our setup breaks this assumption since the number of nodes grows as more and more seeds are generated. To address this issue, we introduce a rareness score of a node, so that each new node will have an initial score to differentiate itself from other new nodes. We will discuss seed scoring in more detail later in [SIV-B](#).

It is also worth mentioning that a recent work Ecofuzz [54] proposed using a variant of the adversarial multi-armed bandit (AMAB) model to perform seed scheduling. However, it can not solve the seed exploration problem caused by more sensitive coverage metrics, as it attempts to explore all existing seeds at least once. Moreover, we have also experimented with the EXP3 algorithm that aims to solve the AMAB problem; but it performed worse than UCB1 in our setup.

Algorithm 3: Seed Scheduling Algorithm

Input: seed set S
Output: return the seed to fuzz
Data: the tree T with n layers
 current working tree node cx

1 Function `SelectNextSeedToFuzz (S):`

2 $T \leftarrow S.\text{tree}$
3 $cx \leftarrow T.\text{root}$
4 **foreach** $i \in \{1, \dots, n\}$ **do**
5 $children \leftarrow cx.\text{child_nodes}$
6 $cx \leftarrow \text{argmax}_{x \in children} \text{Score}(x)$
7 **end**
8 $s \leftarrow cx.\text{next_seed}()$
9 **return** s

10 End

11

B. Seed Scoring

How to score seeds directly affect the trade-off between exploration and exploitation. First, for exploitation, seeds that have performed well *recently* should have high scores as they are expected to make more progress. Second, for exploration, the scoring system should also consider the uncertainty of rarely explored seeds. We extended the UCB1 algorithm [2], [5] to achieve a balance between exploitation and exploration. From a high level, our scoring method considers three aspects of a seed: (1) its own rareness, (2) easiness to discover new seeds from this seed, and (3) uncertainty.

In order to discuss this in more detail, let us first define some terms more formally. First, we define the hit count of a feature $F \in \Gamma_l$ at level l as the number of test cases ever generated that cover the feature.

Definition IV.1. Let P be the program under fuzzing, \mathcal{I} be the set of all test cases that have been generated so far. The hit count of a feature F is $\text{num_hits}[F] = |\{I \in \mathcal{I} : F \in C_l(P, I)\}|$.

As observed in [Q](#), features that are rarely exercised by test cases deserve more attention because they are not likely to be exercised by valid inputs. The rareness of a feature describes how rarely it is hit, which is the inverse of the hit count.

Definition IV.2. The rareness of a feature F is $\text{rareness}[F] = \frac{1}{\text{num_hits}[F]}$

Before describing how we calculate the reward of a round of fuzzing, we first define the feature coverage of fuzzing seed s at round t .

Definition IV.3. Let P be the program under fuzzing, $\mathcal{I}_{s,t}$ be the set of test cases generated at round t via fuzzing seed s . We denote the feature coverage at level C_l , $l \in \{1, \dots, n\}$ as $\text{fcov}[s, l, t] = \{F : F \in C(P, I) \ \forall I \in \mathcal{I}_{s,t}\}$

Next, we describe how we calculate the reward to the seed just fuzzed after a round of fuzzing. An intuitive way is to count the number of new features covered as the reward. However, we quickly noticed that this does not work well. As the fuzzing campaign goes on, the probability of exercising new coverage is dramatically decreased, indicating that a seed can hardly obtain new rewards. Consequently, the mean reward of seeds may quickly decrease to zero. When we have many seeds with minor variances near zero, the UCB algorithm cannot properly prioritize seeds. Moreover, under the common observation that infrequent coverage features deserve more exploration than others, seeds that can lead to inputs that exercise rare features are definitely more valuable, even if they do not cover new features. Motivated by these observations, we take the rareness of the rarest feature that is exercised by all generated inputs as the reward to the schedule seed. Formally, for a seed s that is fuzzed at round t , its fuzzing reward w.r.t. coverage metric C_l is

$$\text{SeedReward}(s, l, t) = \max_{F \in \text{fcov}[s, l, t]} (\text{rareness}[F]) \quad (1)$$

Based on the seed reward, we compute the reward to a

cluster by propagating seed rewards to clusters scheduled at upper levels. More formally, let $\langle a^1, \dots, a^n, a^{n+1} \rangle$ be the sequence of nodes (in the seed tree) selected at round t , where a^{n+1} is the seed node for s and a_i is coverage measurements for the corresponding clusters. Since scheduling node a^l affects the following scheduling of nodes a^{l+1}, \dots, a^n at lower layers, the reward of node a^l as feedback consists of the seed reward regarding coverage levels $l, l+1, \dots, n$ as illustrated in [Equation 2](#). Note that we use the geometric mean here since it can handle different scalars of the involved values with ease.

$$Reward(a^l, t) = \sqrt[n-l+1]{\prod_{l \leq k \leq n} SeedReward(s, k, t)} \quad (2)$$

Right now, we are able to estimate the expected performance of fuzzing a node using the formula of UCB1 [\[2\]](#), [\[5\]](#). Formally, the fuzzing performance of a node a is estimated as

$$FuzzPerf(a) = Q(a) + U(a) \quad (3)$$

$Q(a)$ is the empirical average of fuzzing rewards that a obtains so far, and $U(a)$ is radius of the upper confidence interval.

Unlike UCB1 which calculates $Q(a)$ using the arithmetic mean of the rewards that node a obtains so far, we use the weighted arithmetic mean instead. More specifically, during the fuzzing, the rareness of a feature is decreasing as it is exercised by more and more test cases. As a result, even the same fuzzing coverage can lead to different fuzzing rewards for mutating a seed: the reward of an earlier round might be significantly higher than that of a later round. To address this issue, we introduce a discount factor as weight in order to favor newer rewards rather than older ones. More formally, given a node a that is selected for round t , we update its weighted mean at the end of round t in such a way that we progressively decrease the weight to the previous mean reward in order to give higher weights to newer rewards as illustrated in [Equation 4](#)

$$Q(a, t) = \frac{Reward(a, t) + w \times Q(a, t') \times \sum_{p=0}^{N[a, t]-1} w^p}{1 + w \times \sum_{p=0}^{N[a, t]-1} w^p} \quad (4)$$

$N[a, t]$ denotes the number of times that node a has been selected so far at the end of round t , t' is the last round at which node a was selected, and w is the discount factor. Note that the smaller w is, the more we ignore the past rewards. When w is set to 0, all the past rewards are ignored. To study how w affects the fuzzing performance, we conduct an empirical experiments [\(§V-F\)](#). Based on the results, we empirically set w to 0.5 in our evaluation.

$U(a)$ is the estimated radius factoring in the number of times a has been selected. In addition, we also consider the number of seeds that a contains based on the insight that nodes with more seeds should be scheduled more for seed

exploration. More formally, given a seed a and its parent a' , we calculate $U(a)$ as

$$U(a) = C \times \sqrt{\frac{Y[a]}{Y[a']}} \times \sqrt{\frac{\log N[a']}{N[a]}} \quad (5)$$

$Y[a]$ denotes the number of seeds in the cluster of node a , and $N[a]$ denotes the times a has been selected so far. C is a pre-defined parameter that configures the relative strength of exploration and exploitation. In particular, a larger C results in a relatively wider radius in [Equation 3](#), which encourages exploring fresh nodes that have been fuzzed fewer times. This can help a fuzzer get out of code regions that are too hard to solve. On the contrary, a smaller C indicates that the empirical average of fuzzing rewards gets weighted more, thus promoting nodes that have recently led to good progress. As a result, the fuzzer will focus on these nodes and is expected to reach more new code coverage. To further demonstrate how it affects the fuzzing performance, we fuzz the CGC benchmark with different values of C and show the results in [\(§V-F\)](#). Based on the results, we set C to 1.4 in our evaluation.

The fuzzing performance estimated by [Equation 3](#) based on fuzzing coverage is limited by what can be observed. This limitation can impact seeds that have never been scheduled and seeds that exercise rare features themselves but usually lead to inputs that exercise high-frequency features (e.g., for a program with rigorous input syntax checks, random mutations usually lead to invalid paths, hence lowering the reward). To mitigate this limitation, when evaluating a seed, we also consider features that it exercises. Particularly, we calculate the rareness of a seed via aggregating the rareness of features that it covers. More formally, let P be the program under fuzzing, given a seed s , its rareness regarding M_l , $l \in \{1, \dots, n\}$ is

$$SeedRareness(s, l) = \sqrt{\frac{\sum_{F \in C_l(P, s)} rareness^2[F]}{|\{F : F \in C_l(P, s)\}|}} \quad (6)$$

Note that here we take quadratic mean rather than, e.g., arithmetic mean because it preserves more data diversity. The rareness of a node a^l measured by M_l is completely decided by its child seeds as they share the same coverage regarding M_l . Let $\langle a^1, \dots, a^n, a^{n+1} \rangle$ be the sequence of nodes selected at round t , where a^{n+1} is the leaf node representing a real seed s , then at the end of round t the rareness of node a^l is updated as

$$Rareness(a^l) = SeedRareness(s, l) \quad (7)$$

Notably, we update the rareness score of seeds and nodes lazily for two reasons. First, it reduces the performance overhead. Second, it can lead to overestimating the rareness of a node that has not been fuzzed for a long time, so that seed is more likely to be scheduled.

In addition to updating the rareness of a node picked in the past round, we also calculate the rareness of each new node similarly. As discussed previously, this makes each new

node have an initial score to differentiate itself from other new nodes before its reward is estimated.

Finally, we have the score of a node a via multiplying its rareness and estimated fuzzing performance together as shown in [Equation 8](#). This score is the one used in [Algorithm 3](#) to determine which nodes will be picked and which seed will be fuzzed next.

$$Score(a) = \text{Rareness}(a) \times \text{FuzzPerf}(a) \quad (8)$$

V. EVALUATION

Our main hypothesis is that our multi-level coverage metric and hierarchical seed scheduling algorithm driven by the MAB model can achieve a good balance between exploitation and exploration, thus boosting the fuzzing performance. To validate our hypothesis, we implemented two prototypes AFL-HIER and AFL++-HIER, one based on AFL [\[55\]](#) and the other based on AFL++ [\[17\]](#), and evaluated them on various benchmarks aiming to answer the following research questions.

- **RQ1** Can AFL-HIER/AFL++-HIER detect more bugs than the baseline?
- **RQ2** Can AFL-HIER/AFL++-HIER achieve higher coverage than the baseline?
- **RQ3** How much overhead does our technique impose on the fuzzing throughput?
- **RQ4** How well does our hierarchical seed scheduling mitigate the seed explosion problem caused by high sensitive of coverage metrics?
- **RQ5** How do the hyper-parameters affect the performance of our hierarchical seed scheduling algorithm?
- **RQ6** How flexible is our framework to integrate other coverage metrics?

A. Experiment Setup

1) **Benchmarks:** The first set of programs are from DARPA Cyber Grand Challenge (CGC) [\[10\]](#). These programs are carefully crafted by security experts that embed different kinds of technical challenges (e.g., complex I/O protocols and input checksums) and vulnerabilities (e.g., buffer overflow, integer overflow, and use-after-free) to comprehensively evaluate automated vulnerability discovery techniques. There are 131 programs from CGC Qualifying Event (CQE) and 74 programs from CGC Final Event (CFE), a total of 205. CGC programs are designed to run on a special kernel with seven essential system calls so that competitors can focus on vulnerability discovery techniques. In order to run those programs within a normal Linux environment, we use QEMU to emulate the special system calls. Unfortunately, due to imperfect simulation, some CGC programs fail to be run correctly. We also cannot handle programs that consist of multiple binaries, which communicate with each other through pre-defined inter-process communication (IPC) channels. As a result, we can only successfully fuzz 180 CGC programs (or binaries, in other words). We fuzz each binary for two hours and repeat each experiment 10 times to mitigate the

effects of randomness. Each fuzzing starts with a single seed “123\n456\n789\n”. We chose this initial because the initial seed affects the fuzzing progress a lot: seeds that are too good may make most code covered at the beginning if the program is not complex, while poor ones may make the fuzzing get stuck before reaching the core code of the program. These two cases both will make the fuzzing reach the plateau early, and fail to show the performance differences between our approach and other fuzzers. The seed we chose showed a good capability to reveal performance differences between fuzzers.

The second benchmark set is the Google FuzzBench [\[21\]](#) that offers a standard set of tests for evaluating fuzzer performance. These tests are derived from real-world open-sourced projects (e.g., libxml, openssl, and freetype) that are widely used in file parsers, protocols, and font operations. For this dataset, we used the standard automation script to run the benchmarks, so each benchmark uses the seeds provided by Google.

2) *Implementations:* For evaluation over the CGC dataset, we used a prototype built on top of the code open-sourced by Wang et al. [\[45\]](#), which is based on AFL QEMU-mode, for its support for binary-only targets and its emulation of CGC system calls. For evaluation over the FuzzBench dataset, we used a prototype built upon the AFL++ project [\[17\]](#) (QEMU-mode only), for its support of persistent mode and higher fuzzing throughput.

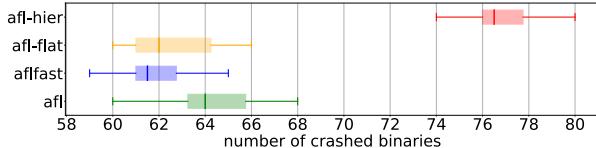
3) *Baseline Fuzzers:* For AFL-based prototype, we choose three fuzzers as the baseline for comparison: the original AFL [\[55\]](#), AFLFAST [\[9\]](#), and AFL-FLAT [\[45\]](#). AFL-FLAT is configured with edge sensitivity C_E and distance sensitivity C_D (see [§III-D2](#) for more details), but uses the power scheduler from AFLFAST instead of our hierarchical scheduler. As discussed in [§II-A](#), the performance of greybox fuzzing is mainly affected by four factors: seed selection, seed scheduling, mutation strategies, and fuzzing throughput. We made all fuzzers use the same mutation strategy to reflect the benefit of our approach, and ran the experiments ten times to minimize the impact of randomness [\[24\]](#). We also ran all fuzzers in the QEMU mode so they can have similar fuzzing throughput, which also makes it easier to assess AFL-HIER’s performance overhead. Comparisons with AFL and AFLFAST aim to show the overall performance improvement of AFL-HIER; and comparison with AFL-FLAT aims to show the necessity/benefit of our scheduler (i.e., increasing the sensitivity of the coverage metric alone is not enough).

For AFL++-based prototype, we choose two fuzzers as the baseline: the original AFL++² [\[17\]](#) and AFL++-FLAT. We ran all fuzzers in the QEMU-mode and enabled persistent mode for better throughput

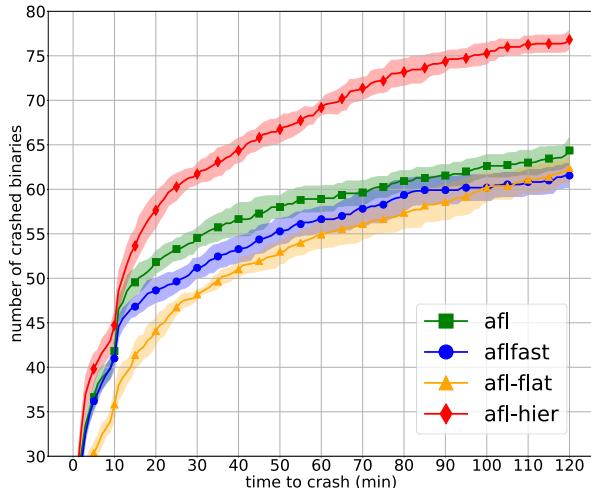
4) *Computing Resources:* All the experiments are conducted on a 64-bit machine with 48 cores (2 Intel(R) Xeon(R) Platinum 8260 @2.40GHz), 375GB of RAM, and Ubuntu 18.04. Each fuzzing instance is bound to a core to avoid interference.

¹We are working with Google to provide a more thorough comparison with other fuzzers.

²The version is 2.68c which our prototype is built on.



(a) Number of crashed CGC binaries.



(b) Number of CGC binaries crashed over time.

Fig. 3: Crash detection on CGC benchmarks.

B. RQ 1. Bug Detection

* In experiments with CGC benchmarks, AFL-HIER crashes more binaries and faster. Especially, it crashes the same number of binaries in 30 minutes, that AFLFAST crashes in 2 hours.

In this experiment, we evaluate fuzzers' capability of detecting known bugs embedded in the CGC binaries. Figure 3a shows the number of crashed CGC binaries across ten rounds of trials. Note that since each binary supposedly only has one vulnerability, this number equals the total number of unique crashes. On average, AFL crashed 64 binaries, AFLFAST crashed 61 binaries, and AFL-FLAT crashed 62 binaries. In contrast, AFL-HIER crashes about 77 binaries on average, which is about 20% more binaries in the 2-hour fuzzing campaign. AFL-HIER also performed much better when we look at the lower and upper bound: its lower bound of crashes (74) is always higher than the upper bound of all other fuzzers. Notably, these vulnerabilities are carefully designed by security experts to highly mimic real-world security-critical vulnerabilities.

Table 1 shows the pairwise comparisons of CGC binaries

TABLE I: Pairwise comparisons (row vs. column) of uniquely crashed on CGC benchmark.

	AFL	AFLFAST	AFL-FLAT	AFL-HIER
AFL	-	8	16	5
AFLFAST	3	-	13	5
AFL-FLAT	11	13	-	1
AFL-HIER	17	22	18	-

uniquely crashed by a fuzzer across ten rounds of trials. As we can see, the added (distance) sensitivity C_D allows AFL-FLAT and AFL-HIER to crash a considerable amount of binaries that edge sensitivity (i.e., AFL and AFLFAST) cannot crash. However, due to the seed explosion problem, AFL-FLAT could not efficiently explore the seed pool; so it also missed many bugs AFL and AFLFAST can trigger. In contrast, AFL-HIER can achieve a good balance between exploration and exploitation: it crashed more unique binaries and missed much less.

Next, we measured the time to first crash (TFC) and show the accumulated number within a 95% confidence of binaries crashed over time in Figure 3b. As shown in recent studies [6, 22], TFC is a good metric to measure the performance of fuzzers. The x-axis presents the time in minutes, and the y-axis shows the number of crashed binaries. As shown in the graph, AFL-HIER stably crashed about 20% more binaries than other fuzzers from the beginning to the end. Notably, AFL-HIER crashed the same number of binaries in 30 minutes as AFLFAST did in 120 minutes; and crashed the same number of binaries in 40 minutes as AFL did in 120 minutes. In contrast, AFLFAST was lagging behind AFL and AFLFAST in most of the time and only surpassed AFLFAST after 100 minutes. This result showed that our hierarchical scheduler not only can find many unique bugs but also can efficiently explore the search space.

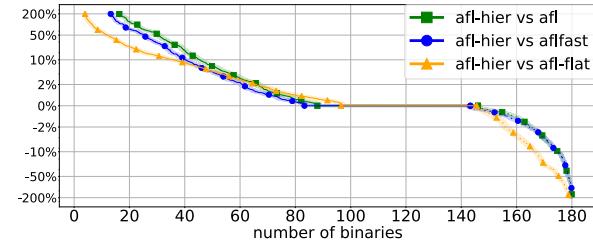
C. RQ 2. Code Coverage

* Results on CGC binaries demonstrate that AFL-HIER generally achieved more code coverage and achieved the same coverage faster. Specifically, AFL-HIER increases the coverage by more than 100% for 20 binaries, and achieves the same coverage in 15 minutes that AFLFAST achieves in 120 minutes for about half of the binaries. On FuzzBench, AFL++-HIER achieved higher coverage on 10 out of 20 projects.

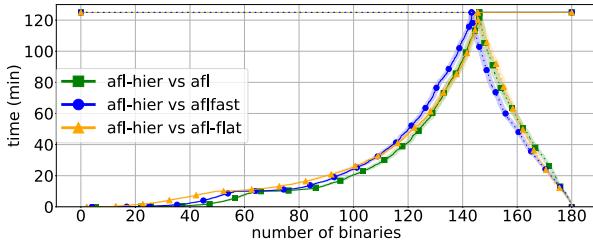
CGC Benchmark. In this experiment, we first measured the edge coverage achieved by fuzzers using QEMU (i.e., captured during binary translation) on CGC binaries.

Figure 4a illustrates the mean code coverage increase of AFL-HIER over other fuzzers for the 180 CGC binaries, after 2 hours of fuzzing. The curve above 0% means AFL-HIER covered more and the curve below 0% means AFL-HIER covered less. The x-axis presents the accumulated number of binaries within a 95% confidence, and the y-axis shows the increased coverage in logarithmic scale. For example, there are about 20 binaries for which the code coverage is increased by at least 100%, and about 45 binaries for which the code coverage is increased by at least 10%. After 2 hours of fuzzing, AFL-HIER achieved more coverage for about 90 binaries than other fuzzers and achieved the same coverage for 50 binaries. Among about 30 binaries on which AFL-HIER achieves less coverage, on half of them the difference is lower than 2%; and only on five of them the difference is greater than 10%. This result shows that our approach can cover more or similar code on most binaries besides detecting more bugs.

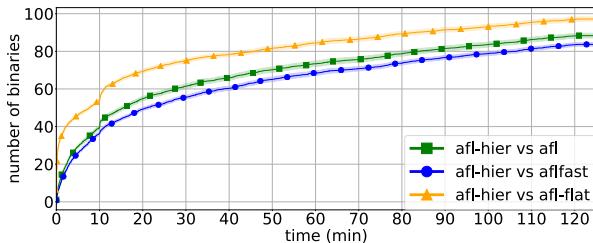
Figure 4b illustrates how fast AFL-HIER can achieve the same coverage as other fuzzers in two hours. The dashed lines



(a) **Mean coverage increase.** For X binaries, AFL-HIER achieves at least Y% more coverage than other fuzzers. A curve towards upper-right indicates that AFL-HIER outperforms the other more significantly.



(b) **Time to coverage.** For X binaries, AFL-HIER achieved the same coverage in Y minutes, as the other fuzzer achieved in 2 hours (solid line). A curve in solid line towards the lower right with its counterpart in dashed line towards lower left indicates a more statistical significance of that AFL-HIER achieve coverage faster than the opponent.



(c) **Better coverage.** After X minutes of fuzzing, AFL-HIER achieves more coverage than other fuzzers for Y binaries. An curve towards upper left indicates that AFL-HIER achieves better coverage than the opponent more significantly.

Fig. 4: Coverage improvement on the CGC benchmarks.

(on the right-hand-side after hitting 120 min) show for the cases where baseline fuzzers achieved more final coverage in two hours. The x-axis shows the accumulated number of binaries within a 95% confidence, while the y-axis shows the time in minutes. We can see that for about half of the total 180 binaries, AFL-HIER achieved the same coverage in 15 minutes as baseline fuzzers did in 2 hours. Moreover, for about 110 binaries, AFL-HIER achieves the same coverage in half an hour; and for about 130 binaries, AFL-HIER achieves the same coverage in one hour. Similar to TFC (time to first crash), this result also shows that our approach can achieve the same coverage faster, indicating it can balance exploration and exploitation well.

Figure 4c shows the number of binaries for which AFL-HIER achieved *more* coverage than other fuzzers over time.

The x-axis represents the time in minutes and the y-axis shows the accumulated number of binaries within a 95% confidence that AFL-HIER won on coverage. We can observe that after 10 minutes, AFL-HIER already won for about 40 binaries over AFL and AFLFAST. After 1 hour, it further increased the gap by winning for more than 70 binaries. Overall, AFL-HIER steadily won for more and more binaries throughout the process of the 2-hour fuzzing campaign. This indicates that AFL-HIER can continuously make breakthroughs in new coverage for binaries when other fuzzers plateaued.

FuzzBench. Next, we compare AFL++-HIER with two baseline fuzzers (AFL++ and AFL++-FLAT) on Google FuzzBench benchmarks. Figure 5 shows the mean coverage (with confidence intervals) over time during 6-hour fuzzing campaigns³. The y-axis presents the number of covered edges and the x-axis represents time. Please note that the x-axis is in *logarithmic* scale, as recent work suggests the required efforts to achieve more coverage grow exponentially [6]. Meanwhile, the Vargha-Delaney [43] effect size \hat{A}_{12} is shown at the bottom of each sub-figure, where the left one is of between AFL++-HIER over AFL++ (Qemu) and the right one is of between AFL++-HIER and AFL++-FLAT, respectively. A value above 0.5735, 0.665, 0.737 (or below 0.4265, 0.335, 0.263) indicates a small, medium, large effect size. More intuitively, a larger value above 0.5 indicates a higher probability of that AFL++-HIER will cover more edges than AFL++ (Qemu) or AFL++-FLAT in a fuzzing campaign. Moreover, a value starting with a star indicates a statistical significance tested by Wilcoxon signed-rank test ($p < 0.05$). Overall, AFL++-HIER could beat AFL++ (Qemu) and AFL++-FLAT on about ten projects, and achieved significantly more coverage on projects openthread, sqlite3, and proj4.

Table II shows the unique edge coverage of AFL++ (Qemu) and AFL++-HIER. The results indicate even on programs where AFL++-HIER has lower mean coverage than AFL++, it still can cover some unique edges AFL++ does not cover. Note that here we union edge coverage across different runs, so for some benchmarks like lcms and libpcap, though the mean coverage differences are large, the unique coverage differences are much smaller.

Compared to the results on the CGC benchmarks, we observe that our performance is not significantly better than AFL++ on most of the FuzzBench benchmarks. We suspect the reason is that our UCB1-based scheduler and the hyper-parameters we used in the evaluation prefer exploitation over exploration. As a result, when the program under test is relatively smaller (e.g., CGC benchmarks), our scheduler can discover more bugs without sacrificing the overall coverage by too much. But on FuzzBench programs, breaking through some unique edges (Table II) can be overshadowed by not exploring other easier to cover edges.

D. RQ 3. Fuzzing Throughput

* Results on CGC benchmarks show that AFL-HIER has a competitive throughput as AFL and AFLFAST. Moreover, even built on the faster fuzzer AFL++, AFL++-HIER still

³We are working with Google to provide a 23-hour run that compares with more fuzzers.

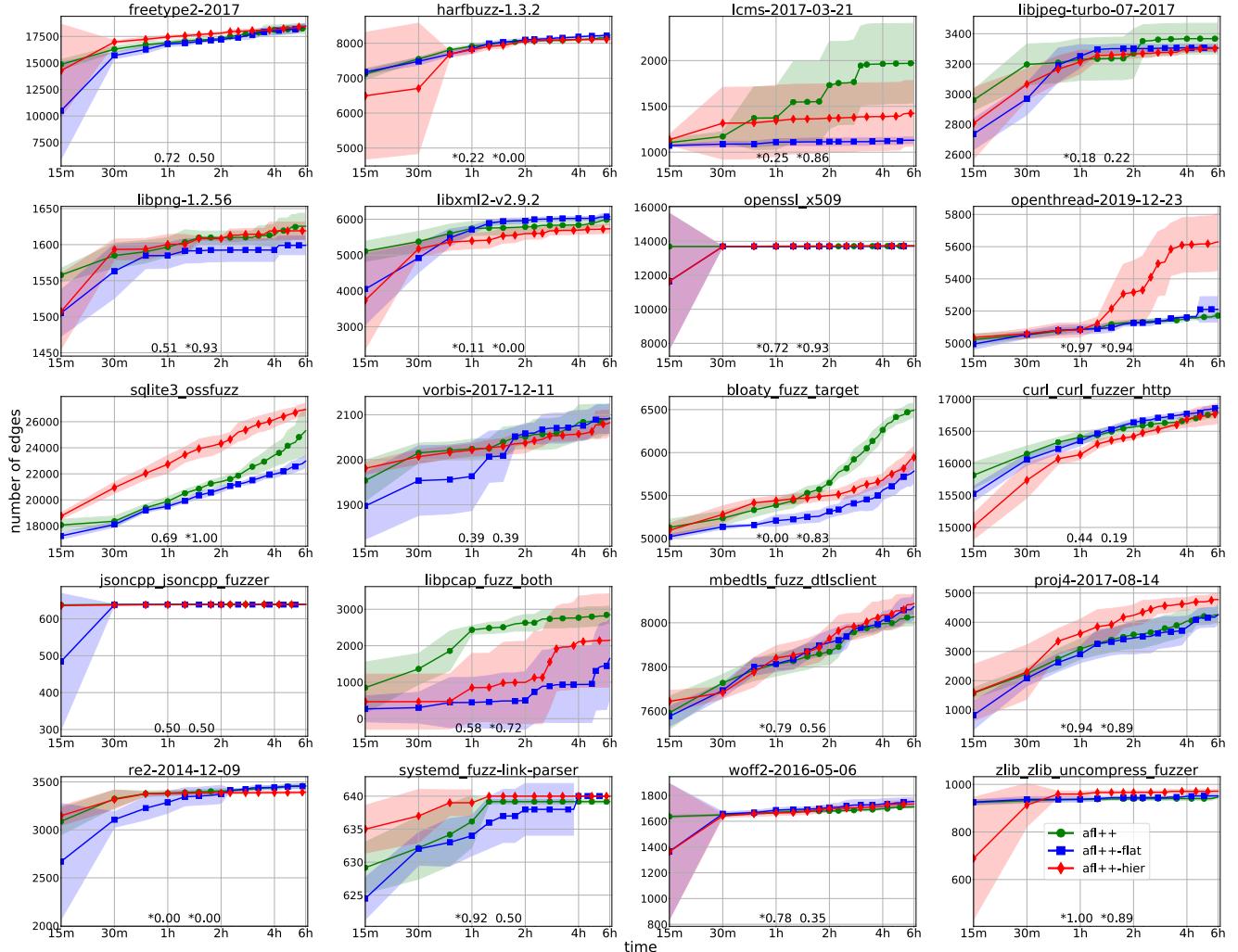


Fig. 5: Mean coverage in a 6 hour fuzzing campaign on FuzzBench benchmarks.

has a comparable throughput as shown by the results on FuzzBench benchmarks.

A multi-level coverage metric requires collecting more coverage measurements during runtime and performing more operations to insert a seed into the seed tree. Similarly, our hierarchical scheduler also requires more steps than the power scheduler of AFL and AFLFAST. Therefore, we expect our approach to have a negative impact on fuzzing throughput. Moreover, the multi-level coverage metric is sensitive to minor variances of test cases and execution paths; consequently, it is more likely to schedule larger and more complex seeds leading to longer execution time.

To quantify the impact on fuzzing throughput, we first investigated the proportion of the time that AFL-HIER spends in scheduling, which involves maintaining the incidence frequencies and the tree of seeds and choosing the next seed to fuzz. The results on CGC benchmarks are shown in Figure 7, where the x-axis represents individual runs (in total $10 \times 180 = 1800$) and the y-axis shows the portion of time spent on scheduling. We can see that the median overhead is as low as 3%, and most overhead is lower than 10%. On AFL++-based prototype, we observed lower performance overhead, as shown in Figure 9.

Next, we measured the throughput of AFL-HIER versus AFL and AFLFAST on CGC benchmarks. Figure 6 shows the ratio of AFL-HIER's throughput over AFL and AFLFAST in an ascending order. The x-axis represents different CGC binaries while the y-axis shows the ratio within a 95% confidence in *logarithmic* scale. Surprisingly, AFL-HIER only leads to a lower throughput for about a quarter of the binaries; and for another quarter of the binaries, AFL-HIER's throughput is at least twice as AFLFAST's. This indicates that the specific optimizations for AFL-HIER act very well. A similar trend is also observed on the AFL++-based prototype, as shown in Figure 8.

E. RQ 4. Performance Boost via Hierarchical Seed Scheduling

* Experiment results on CGC and FuzzBench benchmarks demonstrate that our hierarchical seed scheduler dramatically reduces the number of candidates to be examined.

Previous experiments already show that our hierarchical seed scheduler is more suitable for highly sensitive coverage metrics, as AFL-HIER can achieve higher coverage faster than AFL-FLAT and find more bugs. In this evaluation, we

TABLE II: Unique edge coverage between afl++ (Qemu) and afl++-hier (Hier) on FuzzBench benchmarks. The coverage is union over different runs.

Benchmark	Total	Hier - Qemu	Qemu - Hier
bloaty_fuzz_target	102417	24	674
curl_curl_fuzzer_http	143182	203	114
freetype2-2017	56114	774	1227
harfbuzz-1.3.2	13073	58	124
jsoncpp_jsoncpp_fuzzer	2583	0	0
lcms-2017-03-21	12817	36	33
libjpeg-turbo-07-2017	18486	0	237
libpcap_fuzz_both	11800	141	195
libpng-1.2.56	5944	6	54
libxml2-v2.9.2	89852	52	210
mbedtls_fuzz_dtlsclient	32046	142	102
openssl_x509	115381	26	14
openthread-2019-12-23	42901	344	0
proj4-2017-08-14	10434	109	67
re2-2014-12-09	5904	2	100
sqlite3_ossfuzz	48181	1880	965
systemd_fuzz-link-parser	4167	0	0
vorbis-2017-12-11	6372	8	4
woff2-2016-05-06	6401	54	8
zlib_zlib_uncompress	1664	24	0

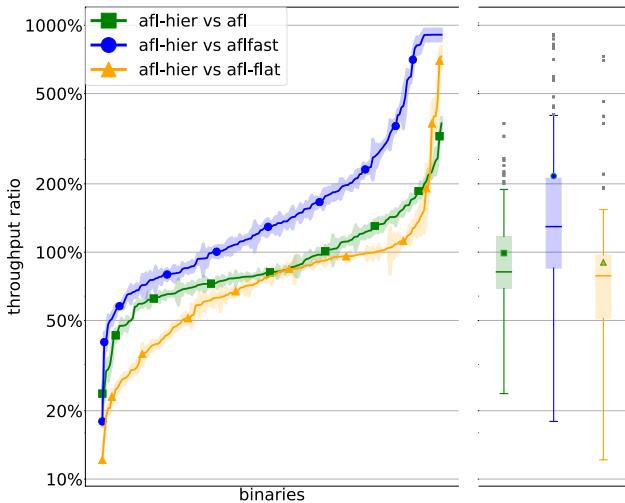


Fig. 6: Comparison between Throughput of AFL-HIER, AFL, AFLFAST and AFL-FLAT on CGC benchmarks.

investigate the number of seeds generated by each fuzzer to validate that such improvement is indeed caused by the scheduler. Figure 10 shows the number of seeds generated by each fuzzer on the left side, as well as the number of nodes at different levels of the tree in AFL-HIER on the right side. The y-axis is in *logarithmic* scale. We can observe that due to the increased sensitivity of distance metric C_D , both AFL-HIER and AFL-FLAT selected one magnitude more seeds than AFL and AFLFAST, which uses edge coverage with hit count. However, by clustering the seeds in a hierarchical structure, AFL-HIER dramatically reduced the number of candidates to examine when scheduling. Specifically, on average there are about $21 + 1102/21 + 2350/1102 + 2608/2350 \approx 77$ examinations to perform for each scheduling, which is significantly less than examining 2608 seeds. As a result, even with the most number of seeds (more than AFL-FLAT), AFL-HIER can still balance exploration and exploitation and achieve better

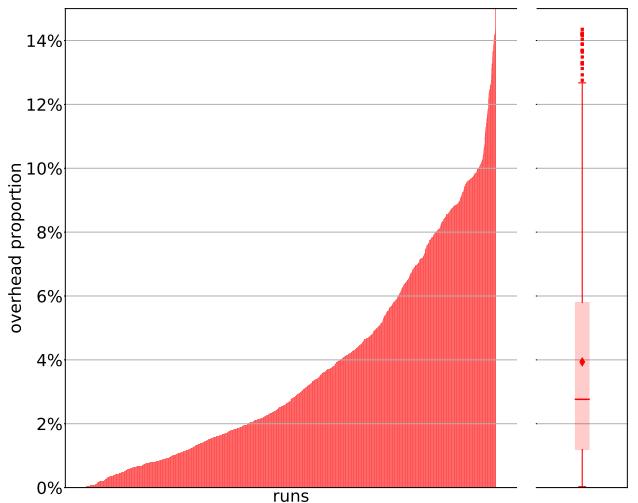


Fig. 7: Overhead of AFL-HIER Scheduler on CGC benchmarks.

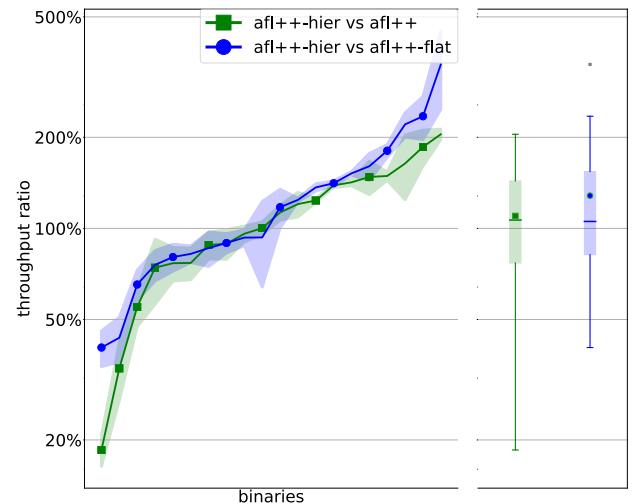


Fig. 8: Comparison between Throughput of AFL++-HIER, AFL++, and AFL++-FLAT on FuzzBench benchmarks.

fuzzing performance (in terms of coverage and detected bugs) than baseline fuzzers.

On FuzzBench benchmarks, we also observed a similar level of reduction, as shown in Figure 11. More importantly, we can see that our scheduling algorithm can scale to larger programs with significantly more edges and more saved seeds. As shown in Table II, all the benchmarks have at least thousands of edges in total, and some even contain more than one hundred thousand edges.

F. RQ 5. Hyper-parameters

* Experiment results on CGC benchmarks demonstrate that the hyper-parameters will affect the performance in terms of crashes and edge coverage.

As discussed in §IV-B, the seed scoring involves two hyper-parameters. One is w in Equation 4 that determines how much

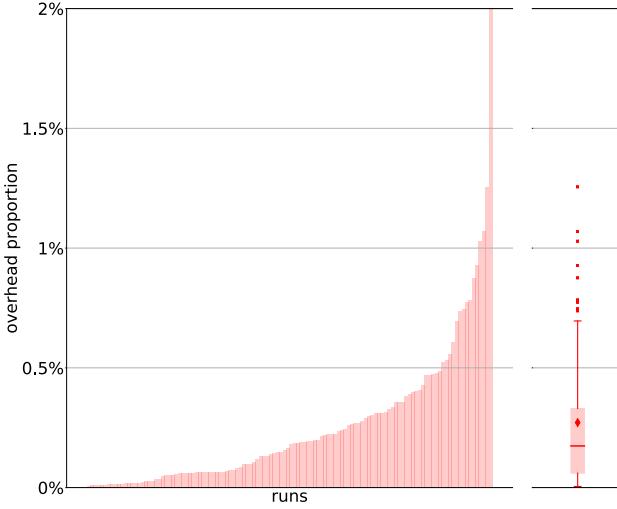


Fig. 9: Overhead of AFL++-HIER Scheduler on FuzzBench benchmarks.

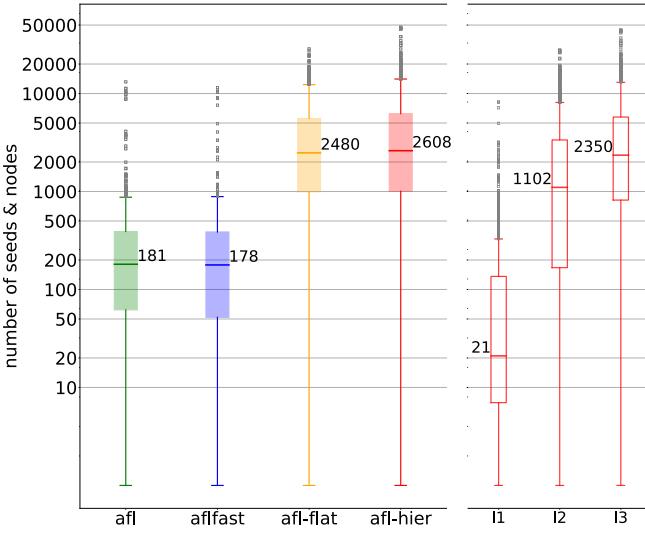


Fig. 10: Number of Seeds and Nodes on CGC benchmarks.

we will decrease weights to old rewards when calculating the mean reward. The other one is C in [Equation 5](#) that controls the trade-off between seed exploration and exploitation. In this evaluation, we investigate when they are set to different values, how the fuzzing performance will vary. [Table III](#) and [Table V](#) show the average number of crashed binaries and covered edges with different values of C and w , respectively. In addition, we also investigate the number of binaries uniquely crashed as shown in [Table IV](#) and [Table VI](#), where each cell represents the number of binaries that have been crashed by the setting of the row once but never by the setting of the column. We can observe that different settings will lead to different results.

Notably, when C is set to 0, which extremely encourages exploitation, it uniquely crashes the most binaries, but on average, it crashes the least. This indicates that although keeping exploitation may help to trigger a crash at the end of a

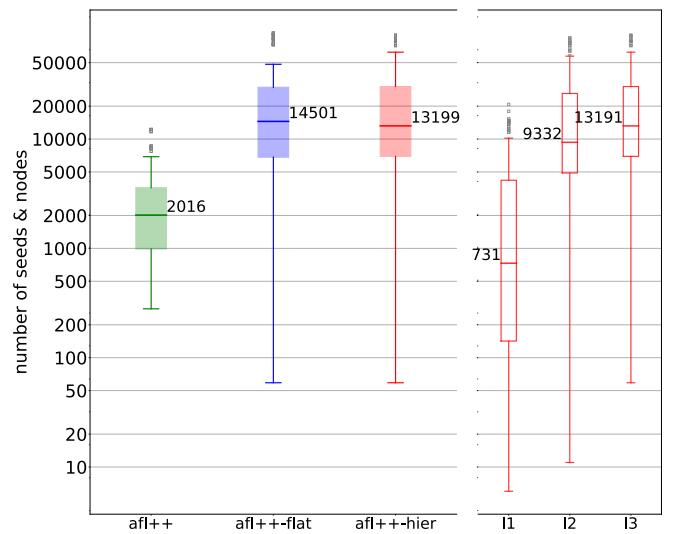


Fig. 11: Number of Seeds and Nodes on FuzzBench benchmarks.

TABLE III: Average number of crashed CGC binaries and mean edge coverage with different values of hyper-parameter C .

Value of C	0	0.014	0.14	1.4	14
Crash	74	75	75	76	75
Edge Cov	776	667	748	727	746

seed chain in one run, it also takes the risk of being trapped in fuzzing other seeds that previously have led to rarely explored coverage, thus missing the crash in other runs. In other words, high exploitation may do better in crash triggering than crash reproducing. Meanwhile, the result of edge coverage indicates that exploring more coverage may not be closely related to bug detection as expected when under different configurations of the relative strength of exploration and exploitation. For example, setting C to 0.014 will lead to significantly less coverage, but it crashes almost the same number of binaries as others.

In terms of the hyper-parameter w , note that a larger w makes old rewards more weighted, thus encourages seed exploitation rather than exploration. We can observe that setting w either too high (as 1.0) or too low (as 0.5) will lead to worse coverage, while setting w to 0.5 will lead to significantly more unique crashes.

Overall, we can observe that when setting C to 1.4, w to 0.5, they perform reasonably well in average crashes, unique crashes, and mean edge coverage. Thus we adapt these settings in our current implementation.

G. RQ 6. Ability to Support other Coverage Metrics

* Experiment results on the maze problem show that our hierarchical scheduler can also improve the fuzzing performance when using other sensitive coverage metrics.

As discussed in [§III-A](#) it is very hard, if not impossible, to use edge or even distance coverage to solve the maze problem

TABLE IV: Pairwise comparisons (row vs. column) of uniquely crashed on CGC benchmarks with different values of hyper-parameter C.

Value of C	0	0.014	0.14	1.4	14
0	-	8	7	4	9
0.014	3	-	2	3	4
0.14	4	4	-	5	5
1.4	3	7	7	-	9
14	3	3	2	4	-

TABLE V: Average number of crashed CGC binaries and mean edge coverage with different values of hyper-parameter W.

Value of W	0.10	0.25	0.50	0.75	0.90	1.00
Crash	74	73	76	72	75	75
Edge Cov	698	758	727	666	739	660

(Listing 1). However, it is possible to solve it using memory sensitivity C_A (see SIII-D2 for details). In this experiment, we investigate whether our hierarchical scheduler can also boost the performance of coverage metrics other than code-related coverage. Specifically, we configured AFL-FLAT and AFL-HIER to use memory access metric C_A instead of distance metric C_D and evaluate the two fuzzers on the maze problem. Table VII shows the results. As we can see, compared to the power scheduler used by AFL-FLAT, our hierarchical scheduler allows AFL-HIER to solve the maze problem much faster. This empirical result suggests that our scheduler is flexible to support different coverage metrics.

VI. RELATED WORK

A. Coverage Guided Greybox Fuzzing

Greybox fuzzing was introduced as early as in 2016 by Sidewinder [16]. Since then it has been extensively used in practice with the popularity of AFL [55] and LIBFUZZER [1]. Meanwhile, it has gained tremendous academic interest in various areas. On the one hand, various techniques including taint tracking [12], [37], [46], symbolic execution [4], [41], program transformation [23], [33], and deep learning [36], [40], are incorporated into greybox fuzzing to boost its performance.

TABLE VI: Pairwise comparisons (row vs. column) of uniquely crashed on CGC benchmarks with different values of hyper-parameter W.

Value of W	0.10	0.25	0.50	0.75	0.90	1.00
0.10	-	5	2	3	4	3
0.25	1	-	1	1	1	1
0.50	8	11	-	9	9	9
0.75	2	4	2	-	3	3
0.90	4	5	3	4	-	4
1.00	4	6	4	5	5	-

TABLE VII: Average solving time for the maze problem (Listing 1).

Fuzzer	AFL-FLAT	AFL-HIER
Time (sec)	383 ± 92	180 ± 36

Our approach relies little on these techniques and is orthogonal to these work. On the other hand, there is an increasing number of greybox fuzzers that are carefully crafted to test specific types of programs such as OS kernels [38], [53], firmware [57], protocol [35], smart contracts [31], deep neural networks [50]. It is promising for these fuzzers to adopt our techniques to improve their efficiency.

B. Improving Coverage Metric

Angora [12] involves calling context, and MemFuzz [15] involves memory accesses when calculating edge coverage to explore program states more pervasively. However, they pay little attention to the potential seed explosion problem. CollAFL [19] improves edge coverage accuracy via ensuring each edge has a unique hash, and utilizes various kinds of coverage information to prioritize seeds. However, it requires a precise analysis of the control flow graph of the target program. Wang et al. [47] differentiate edges based on their corresponding memory operations for seed prioritization to find memory corruption bugs. However, it is incapable of preventing a test case involving diverse memory operations from being dropped since it still relies on edge coverage to evaluate the quality of test cases. Greyone [18] augments edge coverage with data flow features where lightweight and accurate taint tracking is necessary. IJON [3] designs various primitives for annotating source code that will adapt the coverage metric to different kinds of challenges of exploring deep state space. However, it requires domain knowledge of the target program and much manual work. Ankou [30] proposes a new coverage metric that measures distances between execution paths of test cases, and employs adaptive seed pool update to mitigate seed explosion. By comparison, the distance we propose is between two arguments of conditions in conditional branches, and we address the seed explosion problem via organizing the seed pool as a multi-level tree.

Some research focuses on finding domain-specific bugs via specially designed coverage metrics. MemLock [48] takes memory consumption into account when evaluating a test case in order to trigger memory consumption bugs. SlowFuzz [34] counts the number of instructions executed by test case as coverage features to detect algorithm complexity bugs. Furthermore, PerfFuzz [26] records the number of times each block is executed by a test case and considers the test case as a new seed if it increases the execution count for any block in order to find hot spots. KRACE [56] develops a new coverage that captures the exploration progress in the concurrency dimension to find data races in kernel file systems. Our work offers a framework to combine these metrics with others so that they can benefit from more general metrics.

Wang et al. [45] systematically evaluate multiple coverage metrics, revealing that there is no grand slam coverage metric that can beat others, and it is promising to combine different coverage metrics together through cross seeding between multiple fuzzing instances. We combine coverage metrics within one fuzzing instance, avoiding the overhead of synchronizing seeds as well as redundant fuzzing. FuzzFactory [32] provides a platform that makes combining different coverage metrics easy and flexible. However, it does not address the seed explosion problem, as our experimental results demonstrate

that randomly combining different metrics without a proper organization may lead to negative impacts.

C. Smart Seed Scheduling

AFLFAST [9] focuses on fuzzing seeds exercising low-frequency paths and assigns more power to them through modeling greybox fuzzing as a Markov chain. FairFuzz [27] identifies low-frequency edges and prioritizes mutations satisfying these edges. Entropic [7] targets on the test cases that a seed has generated, evaluating the diversity of coverage features they exercise via the information-theoretic entropy. Consequently, seeds with higher information gains are more likely to be scheduled. Vuzzer [37] de-prioritizes seeds hitting error-handling or frequently visited code that is identified via heavyweight static and dynamic analysis. Cerebo [28] prioritizes seeds via various metrics including code complexity, coverage, and execution time. AFLGo [8] and UAFL [44] are directed fuzzers that favor seeds closer to targeted code. Compared to these work, our scheduling algorithm considers the rareness of both static features it covers and test cases it has generated when evaluating a seed.

Modeling scheduling as an MAB problem. Woo et al. [49] model blackbox mutational fuzzing as a classic Multi-Armed Bandit (MAB) problem. Nevertheless, its goal is to search for an optimal arrangement for a fixed set of program-seed pairs to maximize the unique bugs found. EcoFuzz [54] proposes a variant of the Adversarial Multi-Armed Bandit model for modeling seed scheduling. However, it explicitly puts seed exploration and exploitation in separate stages, launching exploitation only when all existing seeds have been explored once. Thus it is incapable of solving the seed explosion problem.

VII. CONCLUSION

Fine-grained coverage metrics, such as distances between operands of comparison operations and array indices involved in memory accesses, allow greybox fuzzers to detect bugs that cannot be triggered by traditional edge coverage. However, existing seed scheduling algorithms cannot efficiently handle the increased number of seeds. In this work, we present a new coverage metric design called multi-level coverage metric, where we cluster seeds selected by fine-grained metrics using coarse-grained metrics. Combined with a reinforcement-learning-based hierarchical scheduler, our approach significantly outperforms existing edge-coverage-based fuzzers on DARPA CGC challenges.

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REFERENCES

- [1] “Libfuzzer: a library for coverage-guided fuzz testing,” <https://llvm.org/docs/LibFuzzer.html>
- [2] R. Agrawal, “Sample mean based index policies with $O(\log n)$ regret for the multi-armed bandit problem,” *Advances in Applied Probability*, pp. 1054–1078, 1995.
- [3] C. Aschermann, S. Schumilo, A. Abbasi, and T. Holz, “Ijon: Exploring deep state spaces via fuzzing,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2020.
- [4] C. Aschermann, S. Schumilo, T. Blazytko, R. Gawlik, and T. Holz, “Redqueen: Fuzzing with input-to-state correspondence,” in *Annual Network and Distributed System Security Symposium (NDSS)*, 2019.
- [5] P. Auer, N. Cesa-Bianchi, and P. Fischer, “Finite-time analysis of the multiarmed bandit problem,” *Machine learning*, vol. 47, no. 2-3, pp. 235–256, 2002.
- [6] M. Böhme and B. Falk, “Fuzzing: On the exponential cost of vulnerability discovery,” in *ACM SIGSOFT Symposium on the Foundations of Software Engineering (FSE)*, 2020.
- [7] M. Böhme, V. Manes, and S. K. Cha, “Boosting fuzzer efficiency: An information theoretic perspective,” in *ACM SIGSOFT Symposium on the Foundations of Software Engineering (FSE)*, 2020.
- [8] M. Böhme, V.-T. Pham, M.-D. Nguyen, and A. Roychoudhury, “Directed greybox fuzzing,” in *ACM Conference on Computer and Communications Security (CCS)*, 2017.
- [9] M. Böhme, V.-T. Pham, and A. Roychoudhury, “Coverage-based greybox fuzzing as markov chain,” in *ACM Conference on Computer and Communications Security (CCS)*, 2016.
- [10] D. CGC, “Darpa cyber grand challenge binaries,” <https://github.com/CyberGrandChallenge> 2014.
- [11] S. K. Cha, M. Woo, and D. Brumley, “Program-adaptive mutational fuzzing,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2015.
- [12] P. Chen and H. Chen, “Angora: Efficient fuzzing by principled search,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2018.
- [13] P. Chen, J. Liu, and H. Chen, “Matryoshka: Fuzzing deeply nested branches,” in *ACM Conference on Computer and Communications Security (CCS)*, 2019.
- [14] J. Choi, J. Jang, C. Han, and S. K. Cha, “Grey-box concolic testing on binary code,” in *International Conference on Software Engineering (ICSE)*, 2019.
- [15] N. Coppik, O. Schwahn, and N. Suri, “Memfuzz: Using memory accesses to guide fuzzing,” in *IEEE Conference on Software Testing, Validation and Verification (ICST)*, 2019.
- [16] S. Embleton, S. Sparks, and R. Cunningham, “Sidewinder: An evolutionary guidance system for malicious input crafting,” in *BlackHat*, 2006.
- [17] A. Fioraldi, D. Maier, H. Eißfeldt, and M. Heuse, “Afl++: Combining incremental steps of fuzzing research,” in *USENIX Workshop on Offensive Technologies (WOOT)*, 2020.
- [18] S. Gan, C. Zhang, P. Chen, B. Zhao, X. Qin, D. Wu, and Z. Chen, “Greyone: Data flow sensitive fuzzing,” in *USENIX Security Symposium (Security)*, 2019.
- [19] S. Gan, C. Zhang, X. Qin, X. Tu, K. Li, Z. Pei, and Z. Chen, “Collafl: Path sensitive fuzzing,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2018.
- [20] Google, “OSS-Fuzz - continuous fuzzing of open source software,” <https://github.com/google/oss-fuzz> 2016.
- [21] —, “Fuzzbench: Fuzzer benchmarking as a service,” <https://github.com/fuzzbench> 2020.
- [22] A. Hazimeh, A. HERRERA, and M. Payer, “Magma: A ground-truth fuzzing benchmark,” in *ACM on Measurement and Analysis of Computing Systems (SIGMETRICS)*, 2021.
- [23] U. Kargén and N. Shahmehri, “Turning programs against each other: high coverage fuzz-testing using binary-code mutation and dynamic slicing,” in *Proceedings of the 2015 10th Joint Meeting on Foundations of Software Engineering*, 2015.
- [24] G. T. Klees, A. Ruef, B. Cooper, S. Wei, and M. Hicks, “Evaluating fuzz testing,” in *ACM Conference on Computer and Communications Security (CCS)*, 2018.

[25] lafintel, “Circumventing fuzzing roadblocks with compiler transformations,” <https://lafintel.wordpress.com/>, 2016.

[26] C. Lemieux, R. Padhye, K. Sen, and D. Song, “Perffuzz: automatically generating pathological inputs,” in *International Symposium on Software Testing and Analysis (ISSTA)*, 2018.

[27] C. Lemieux and K. Sen, “Fairfuzz: A targeted mutation strategy for increasing greybox fuzz testing coverage,” in *IEEE/ACM International Conference on Automated Software Engineering (ASE)*, 2018.

[28] Y. Li, Y. Xue, H. Chen, X. Wu, C. Zhang, X. Xie, H. Wang, and Y. Liu, “Cerebro: context-aware adaptive fuzzing for effective vulnerability detection,” in *ACM SIGSOFT Symposium on the Foundations of Software Engineering (FSE)*, 2019.

[29] C. Lyu, S. Ji, C. Zhang, Y. Li, W.-H. Lee, Y. Song, and R. Beyah, “Mopt: Optimized mutation scheduling for fuzzers,” in *USENIX Security Symposium (Security)*, 2019.

[30] V. J. Manès, S. Kim, and S. K. Cha, “Ankou: Guiding grey-box fuzzing towards combinatorial difference,” in *International Conference on Software Engineering (ICSE)*, 2020.

[31] T. D. Nguyen, L. H. Pham, J. Sun, Y. Lin, and Q. T. Minh, “sfuzz: An efficient adaptive fuzzer for solidity smart contracts,” in *International Conference on Software Engineering (ICSE)*, 2020.

[32] R. Padhye, C. Lemieux, K. Sen, L. Simon, and H. Vijayakumar, “Fuzzfactory: domain-specific fuzzing with waypoints,” in *Annual ACM Conference on Object-Oriented Programming, Systems, Languages, and Applications (OOPSLA)*, 2019.

[33] H. Peng, Y. Shoshtaishvili, and M. Payer, “T-fuzz: fuzzing by program transformation,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2018.

[34] T. Petsios, J. Zhao, A. D. Keromytis, and S. Jana, “Slowfuzz: Automated domain-independent detection of algorithmic complexity vulnerabilities,” in *ACM Conference on Computer and Communications Security (CCS)*, 2017.

[35] V.-T. Pham, M. Böhme, and A. Roychoudhury, “Aflnet: A greybox fuzzer for network protocols,” in *IEEE International Conference on Software Testing, Verification and Validation (Testing Tools Track)*, 2020.

[36] M. Rajpal, W. Blum, and R. Singh, “Not all bytes are equal: Neural byte sieve for fuzzing,” *arXiv preprint arXiv:1711.04596*, 2017.

[37] S. Rawat, V. Jain, A. Kumar, L. Cojocar, C. Giuffrida, and H. Bos, “Vuzzer: Application-aware evolutionary fuzzing,” in *Annual Network and Distributed System Security Symposium (NDSS)*, 2017.

[38] S. Schumilo, C. Aschermann, R. Gawlik, S. Schinzel, and T. Holz, “kafl: Hardware-assisted feedback fuzzing for os kernels,” in *USENIX Security Symposium (Security)*, 2017.

[39] K. Serebryany, “Continuous fuzzing with libfuzzer and addresssanitizer,” in *IEEE Cybersecurity Development (SecDev)*. IEEE, 2016.

[40] D. She, K. Pei, D. Epstein, J. Yang, B. Ray, and S. Jana, “Neuzz: Efficient fuzzing with neural program learning,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2019.

[41] N. Stephens, J. Grosen, C. Salls, A. Dutcher, R. Wang, J. Corbetta, Y. Shoshtaishvili, C. Kruegel, and G. Vigna, “Driller: Augmenting fuzzing through selective symbolic execution,” in *Annual Network and Distributed System Security Symposium (NDSS)*, 2016.

[42] L. Szekeres, “Memory corruption mitigation via software hardening and bug-finding,” Ph.D. dissertation, Stony Brook University, 2017.

[43] A. Vargha and H. D. Delaney, “A critique and improvement of the cl common language effect size statistics of mcgraw and wong,” *Journal of Educational and Behavioral Statistics*, vol. 25, no. 2, pp. 101–132, 2000.

[44] H. Wang, X. Xie, Y. Li, C. Wen, Y. Li, Y. Liu, S. Qin, H. Chen, and Y. Sui, “Typestate-guided fuzzer for discovering use-after-free vulnerabilities,” in *International Conference on Software Engineering (ICSE)*, 2020.

[45] J. Wang, Y. Duan, W. Song, H. Yin, and C. Song, “Be sensitive and collaborative: Analyzing impact of coverage metrics in greybox fuzzing,” in *International Symposium on Research in Attacks, Intrusions and Defenses (RAID)*, 2019.

[46] T. Wang, T. Wei, G. Gu, and W. Zou, “Taintscope: A checksum-aware directed fuzzing tool for automatic software vulnerability detection,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2010.

[47] Y. Wang, X. Jia, Y. Liu, K. Zeng, T. Bao, D. Wu, and P. Su, “Not all coverage measurements are equal: Fuzzing by coverage accounting for input prioritization,” in *Annual Network and Distributed System Security Symposium (NDSS)*, 2020.

[48] C. Wen, H. Wang, Y. Li, S. Qin, Y. Liu, Z. Xu, H. Chen, X. Xie, G. Pu, and T. Liu, “Memlock: Memory usage guided fuzzing,” in *International Conference on Software Engineering (ICSE)*, 2020.

[49] M. Woo, S. K. Cha, S. Gottlieb, and D. Brumley, “Scheduling black-box mutational fuzzing,” in *ACM Conference on Computer and Communications Security (CCS)*, 2013.

[50] X. Xie, L. Ma, F. Juefei-Xu, M. Xue, H. Chen, Y. Liu, J. Zhao, B. Li, J. Yin, and S. See, “Deephunter: A coverage-guided fuzz testing framework for deep neural networks,” in *International Symposium on Software Testing and Analysis (ISSTA)*, 2019.

[51] W. Xu, S. Kashyap, C. Min, and T. Kim, “Designing new operating primitives to improve fuzzing performance,” in *ACM Conference on Computer and Communications Security (CCS)*, 2017.

[52] W. You, X. Wang, S. Ma, J. Huang, X. Zhang, X. Wang, and B. Liang, “Profuzzer: On-the-fly input type probing for better zero-day vulnerability discovery,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2019.

[53] W. You, P. Zong, K. Chen, X. Wang, X. Liao, P. Bian, and B. Liang, “Semfuzz: Semantics-based automatic generation of proof-of-concept exploits,” in *ACM Conference on Computer and Communications Security (CCS)*, 2017.

[54] T. Yue, P. Wang, Y. Tang, E. Wang, B. Yu, K. Lu, and X. Zhou, “Ecofuzz: Adaptive energy-saving greybox fuzzing as a variant of the adversarial multi-armed bandit,” in *USENIX Security Symposium (Security)*, 2020.

[55] M. Zalewski, “American fuzzy lop.(2014),” <http://lcamtuf.coredump.cx/afl/>, 2014.

[56] M. X. S. K. H. Zhao and T. Kim, “Krace: Data race fuzzing for kernel file systems,” in *IEEE Symposium on Security and Privacy (Oakland)*, 2020.

[57] Y. Zheng, A. Davanian, H. Yin, C. Song, H. Zhu, and L. Sun, “Firm-afl: high-throughput greybox fuzzing of iot firmware via augmented process emulation,” in *USENIX Security Symposium (Security)*, 2019.