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4                   **Enhanced Feedback between Shallow Convection and Low-level**  
5                   **Moisture Convergence Leads to Improved Simulation of MJO**  
6                   **Eastward Propagation**

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## Abstract

Recent study indicates that the noninstantaneous interaction of convection and circulation is essential for large-scale convective systems. It is incorporated into cumulus parameterization (CP) by relating cloud-base mass flux of shallow convection to a composite of subcloud moisture convergence in the past. Three pairs of 19-yr simulations with original and modified CP schemes are conducted in a tropical channel model to verify their ability to reproduce the MJO. Improved eastward propagation signal and stronger intraseasonal variability are observed in the simulations with the modified CP schemes based on the noninstantaneous interaction. It is found that enhanced feedback between shallow convection and low-level moisture convergence results in amplified shallow convective heating and/or extended heating duration, shaping tilted heating as in observations. It also generates enhanced moisture convergence which transports more moisture upward. The improved simulations of eastward propagation of the MJO are largely attributed to higher specific humidity in the lower troposphere to the east of maximum rainfall center, which is related to stronger boundary layer moisture convergence forced by shallow convection. Large-scale horizontal advection causes asymmetric moisture tendencies relative to rainfall center (positive to the east and negative to the west) and also gives rise to eastward propagation. The zonal advection, especially the advection of anomalous specific humidity by mean zonal wind, is found to dominate the difference of horizontal advection between each pair of simulations.

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46 **1. Introduction**

47 The Madden-Julian oscillation (MJO) is a planetary-scale convectively coupled  
48 equatorial wave that usually propagates eastward at a speed of 5-8 m s<sup>-1</sup> (see Zhang  
49 (2005) for a complete review). The MJO has long been the focus of research community  
50 for its far-reaching influences on global climate and weather systems (Lau and Waliser  
51 2012; Zhang 2013). Though much improvement in the simulations of MJO has been  
52 made in terms of model resolution, physical parameterization, air-sea coupling, etc.,  
53 general circulation models still struggle to realistically simulate the MJO (Lin et al.  
54 2006; Hung et al. 2013; Jiang et al. 2015). Among the most salient features that should  
55 be reproduced, eastward propagation is hardly captured by models participating in the  
56 MJO task force global model comparison project (Jiang et al. 2015). More than two  
57 thirds of participating models show a stationary or even westward propagating  
58 intraseasonal signals.

59 Associated with the eastward-moving convective envelope of the MJO, a  
60 prominent transition from convectively suppressed to active phase can be observed in  
61 the regions of equatorial Indian and western Pacific oceans (Hendon and Salby 1994;  
62 Johnson and Ciesielski 2013). During the transition period, clouds over the region also  
63 develop gradually from shallow cumulus/congestus mode to deep convective and  
64 stratiform mode (Kikuchi and Takayabu 2004; Riley et al. 2011; Xu and Rutledge 2016).  
65 Considering the significant importance of tropospheric moisture content for tropical  
66 convection (Bretherton et al. 2004; Holloway and Neelin 2009, Ahmed and  
67 Schumacher 2018), it is proposed that shallow convection serves to moisten the lower

68 troposphere for subsequent transition to deep convection and thus is vital for the  
69 eastward propagation of the MJO.

70 A direct moistening mechanism related to shallow convection is vertical transport  
71 of the tropospheric moisture. Benedict and Randall (2007) conducted moisture-budget  
72 analysis using reanalysis data and found that vertical advection by shallow cumulus  
73 dominated moisture tendency prior to the onset of deep convection. This gradual  
74 increase of positive moisture and temperature anomaly corresponds to the “recharge”  
75 process of organized convection in the tropics (Bladé and Hartmann 1993; Kemball-  
76 Cook and Weare 2001). By comparing performance of parameterized shallow and deep  
77 cumulus in the global compressible nonhydrostatic Model for Prediction Across Scales  
78 (MPAS), Pilon et al. (2016) showed that shallow convection plays a key role in  
79 transporting moisture upward to the lower and middle troposphere and then enhances  
80 diabatic heating and precipitation. Many other studies also come to a similar conclusion  
81 though different observation data or numerical simulations are analyzed (e.g., Hagos  
82 and Leung 2011; Del Genio et al. 2012; Bellenger et al. 2015; Janiga and Zhang 2016;  
83 Hirota et al. 2018).

84 However, local (convective scale) moistening of shallow cumulus and congestus  
85 clouds seems inadequate to explain the observed increase in lower-troposphere  
86 moisture. According to the estimation made by Hohenegger and Stevens (2013) with  
87 bulk analysis and large-eddy simulations, actual time taken by the transition from  
88 congestus to deep convection is much shorter than that needed for congestus clouds to  
89 sufficiently moisten the atmosphere. They suggested that upward motion forced by

90 large-scale disturbances may contribute to the extra moistening. Hagos et al. (2014)  
91 conducted a regional cloud-resolving simulation that captures the shallow-to-deep  
92 convection transition of the MJO. Their results indicate that the probability of transition  
93 is highly sensitive to midlevel large-scale humidity and uplift. The increased moisture  
94 at midlevel can also be attribute to large-scale updraft. Observation analysis with  
95 satellite (Masunaga 2013) and radar (Kumar et al. 2013) data both confirm the  
96 significant moistening by large-scale process. Particularly, Masunaga (2013)  
97 highlighted the importance of large-scale upward transport of moisture and heat through  
98 cloud base (i.e., large-scale convergence in subcloud layer) to this moistening,  
99 especially in organized convective systems.

100 Evidence also exists that interaction between large-scale disturbances and shallow  
101 convective heating/moistening favors initiation and propagation of MJO convection  
102 (e.g., Hsu and Li 2012; Ruppert and Johnson 2015; Rowe and Houze 2015). Wave-  
103 CISK is one of the mechanisms that explain the interaction, but horizontal scale  
104 predicted by wave-CISK is unrealistically small (Crum and Dunkerton 1992; Matthews  
105 and Lander 1999). Recently, Liu et al. (2019, hereafter LTW19) revealed that bottom-  
106 heavy heating profile of shallow convection drives intense wind response and  
107 converges low-level moisture, which effectively feeds back to diabatic heating via  
108 upward transport and condensation. This cooperative interaction between shallow  
109 convection and low-level moisture convergence may lead to unstable growth and  
110 upscale organization of convection systems. Unlike conventional wave-CISK, feedback  
111 in LTW19 is noninstantaneous as the time is needed for convective heating to force

112 low-level moisture convergence, and moisture convergence to moisten and heat the  
113 lower troposphere as well. Although the noninstantaneous wave-CISK mechanism has  
114 been proved to be able to capture the eastward propagation of large-scale Kelvin wave  
115 signals quite well in an idealized model as in LTW19, its performance in reproducing  
116 the propagation of the MJO in a more realistic model configuration still needs to be  
117 verified.

118 A tropical channel configuration of the Weather Research and Forecasting (WRF;  
119 Skamarock et al. 2008) model is widely used to test mechanisms of the MJO (Ray et al.  
120 2011; Ulate et al. 2015; Hall et al. 2017), for its convenience in choosing different  
121 boundary conditions and physical parameterizations. In the present study the tropical  
122 channel model is used with cumulus parameterizations (CPs) modified to incorporate  
123 the basic idea of noninstantaneous convection-circulation interaction based on the  
124 theoretical diagram in LTW19. Comparison is made between simulations with original  
125 and modified CP schemes to see how feedback between shallow convection and low-  
126 level moisture convergence (hereafter FSM) influence convective organization and  
127 promote eastward propagation of the MJO. Relative contributions of convergence  
128 (vertical transport) and horizontal advection are identified.

129 The remainder of the paper is arranged as follows. We first briefly introduce the  
130 basic concept of noninstantaneous wave-CISK in section 2. In section 3, introduction  
131 of data sources, model settings and modification of CP scheme is given. Section 4  
132 presents mean-state features of simulations with different CP schemes. Section 5 and 6  
133 compare related processes that lead to enhanced FSM and improved eastward

134 propagation. Discussion and summary are offered in section 7 and 8.

135

136 **2. Noninstantaneous wave-CISK**

137 It is compelling that the time scale of large-scale system is larger than that of  
138 individual cumulus convection embedded in it. As small-scale convective process can  
139 be regarded as instantaneous (ignoring the convective time scale of hours), large-scale  
140 system is rather noninstantaneous. The time scale generally comes from two main  
141 aspects of large-scale convective process (or two legs of convection-circulation  
142 feedback). Firstly, even suitable dynamical condition for convection is provided by  
143 large-scale circulation, it still takes time for numerous clouds to moisten the troposphere  
144 through detrainment and re-evaporation of precipitation and thus morphological  
145 structures could be built up (Johnson and Ciesielski 2013; Powell and Houze 2015).  
146 Secondly, time is also needed for the forced response to convective heating to propagate  
147 out and serve the development and propagation of convective system (e.g., Wu 2000).

148 In order to represent this noninstantaneous character of the FSM, LTW19  
149 constructed a simple cumulus parameterization scheme in which shallow convective  
150 heating is determined by the weighted mean of subcloud moisture convergence in the  
151 past period, i.e.,

$$152 M^* = \frac{\int_{t-\tau}^t rM dt_i}{\int_{t-\tau}^t r dt_i}, \quad (1)$$

153 where  $M$  is the subcloud moisture convergence at the time of  $t_i$ ,  $t$  is the current time,  $\tau$   
154 is the specific time scale of composite, which is called the accumulation-consumption  
155 time scale of moisture in LTW19. The quantity  $r$  is a time dependent weighting function

156 of which the definition is:

$$157 \quad r = 1 - \left[ \frac{t_i - (t - \tau/2)}{\tau/2} \right]^2, \quad t - \tau \leq t_i \leq t. \quad (2)$$

158 In this circumstance, moisture convergence keeps nourishing convective development  
159 (by releasing latent heat) for a period of  $\tau$  once it is forced by convective heating. On  
160 the other hand, convective heating is also slowly varying and exerting long-term  
161 influence on the atmosphere.

162

### 163 **3. Data and model runs**

#### 164 **3.1. Data**

165 The European Center for Medium-Range Weather Forecasting (ECMWF) ERA-  
166 Interim reanalysis data (Dee et al. 2011) are used for model initiation and lateral  
167 boundary conditions. Atmospheric state computed with ERA-interim data is also  
168 referred to as observation. Sea surface temperature (SST) data is obtained from NOAA  
169 1/4° daily Optimum Interpolation Sea Surface Temperature Analysis Version 2  
170 (OISSTv2; Reynolds et al. 2007). In order to validate simulated rainfall and propagation  
171 signal of MJO, we utilize data of the Global Precipitation Climatology Project (GPCP)  
172 daily precipitation estimates (Huffman et al. 2001) and the National Oceanic and  
173 Atmospheric Administration (NOAA) Climate Data Record (CDR) of Daily Outgoing  
174 Longwave Radiation (OLR; Lee and NOAA CDR Program 2011). Both of them are  
175 daily analysis data defined on a global  $1.0^\circ \times 1.0^\circ$  longitude-latitude grid.

176

#### 177 **3.2. Model configuration**

178 The model used is the WRF Model version 3.7.1 with a tropical channel  
179 configuration, which is similar to that of Ray et al. (2009) and Hall et al. (2017).  
180 Horizontal resolution is set to  $1.0^\circ \times 1.0^\circ$ . 32 model levels are placed vertically with the  
181 top level at 50 hPa. The model domain is periodic in the zonal direction and bounded  
182 at  $30^\circ\text{S}$  and  $30^\circ\text{N}$  in the meridional direction. Geopotential, temperature, relative  
183 humidity, and zonal and meridional winds from ERA-Interim reanalysis are  
184 interpolated to model grids at these boundaries. Prescribed SST from OISSTv2  
185 interpolated to  $1^\circ$  resolution and 4 times daily is also used as lower boundary to force  
186 the model. The followings are the physical parameterization schemes used in this study:  
187 the WRF single-moment 3-class simple ice scheme (Hong et al. 2004), the Yonsei  
188 University planetary boundary layer scheme (Hong et al. 2006) with a surface layer  
189 scheme based on the Monin-Obukhov similarity theory (Monin and Obukhov 1954),  
190 the unified NOAA land-surface model (Chen and Dudhia 2001), the Rapid Radiative  
191 Transfer Model for longwave scheme (Mlawer et al. 1997), and the Dudhia (1989)  
192 shortwave scheme.

193 FSM emphasizes the importance of low-level moisture convergence forced by  
194 shallow convection to upward transport of moisture and heat, which is usually  
195 determined by mass flux at cloud base in some CPs. To facilitate modification and  
196 analysis, three mass-flux type CP schemes with particular treatments of shallow  
197 convection are chosen for the control runs in the present study. These schemes are the  
198 new Simplified Arakawa-Schubert (SAS) scheme (Han and Pan, 2011), the new Tiedtke  
199 (TDK) scheme (Zhang and Wang, 2017), and the Kain-Fritsch scheme (Kain, 2004)

200 with the Ma-Tan trigger (Ma and Tan, 2009; hereafter KFMT). The new trigger is used  
201 in Kain-Fritsch scheme for its better performance under weak synoptic forcing.  
202 Although these schemes differ greatly in their treatment of convective process (see the  
203 listed papers above and the references therein), they can all be divided into relatively  
204 separated parts, i.e., convective trigger, cloud model and closure assumption. Here we  
205 modify closure assumptions of these three schemes to that constructed based on the  
206 noninstantaneous wave-CISK.

207

### 208 **3.3. Modification of cumulus parameterization**

209 According to LTW19, two main facts that should be considered in CP are: 1)  
210 shallow convection drives low-level moisture convergence which is strong enough to  
211 sustain itself, while deep convection does not; 2) feedback between shallow convection  
212 and low-level moisture convergence is noninstantaneous and usually takes a couple of  
213 days for large-scale convection systems. Noninstantaneous wave-CISK assumes that  
214 convective heating rate is proportional to low-level moisture convergence, but in mass-  
215 flux type CP schemes, it is difficult to assign heating rate directly. Closure assumptions  
216 of SAS, TDK and KFMT all relate cloud-base mass flux to boundary layer process  
217 (Table 1), which controls the intensity of shallow convective activity. As noted by  
218 Arakawa (2004), boundary layer moisture convergence is the dominant contributor to  
219 moisture flux tendency. Suhas and Zhang (2015) also confirmed the significant positive  
220 correlation between moisture convergence and mass flux. Here cloud-base mass flux is  
221 set to be proportional to a composite of subcloud moisture convergence in the past. In

222 this way, shallow convective heating is related to low-level moisture convergence  
 223 indirectly. We still use Eq. (1) and (2) to calculate the composite of moisture  
 224 convergence. The time scale  $\tau$ , which can be regarded as the time needed for moisture  
 225 convergence to force upward mass flux, is set to 6 h after several sensitive tests. Low-  
 226 level moisture convergence is calculated as:

$$227 \quad \begin{aligned} M &= -\int_0^{z_b} \rho \nabla_h \cdot (\mathbf{v} q) dz \\ &= -\int_0^{z_b} \rho q \nabla_h \cdot \mathbf{v} dz - \int_0^{z_b} \rho \mathbf{v} \cdot \nabla_h q dz, \end{aligned} \quad (3)$$

228 where  $\rho$  and  $q$  are the density of air and the specific humidity respectively,  $z_b$  is the  
 229 height of cloud base (calculated in each CP schemes), and  $\mathbf{v}$  is horizontal velocity. The  
 230 last two terms in Eq. (3) represent mass convergence and horizontal moisture advection  
 231 respectively. The modified closure assumption can thus be written as:

$$232 \quad F = \begin{cases} \alpha M^*, & M^* > 0 \\ 0, & M^* \leq 0, \end{cases} \quad (4)$$

233 where  $F$  is cloud-base mass flux,  $\alpha$  is a factor tuned in each CP schemes. Except for  
 234 closure assumption of shallow convection parameterization, other aspects of CP are  
 235 kept unchanged.

236 The procedure to distinguish deep and shallow convection follows that of original  
 237 CP schemes. Table 1 summaries the criteria for shallow convection in each scheme. At  
 238 each time step, subcloud moisture convergence ( $M$ ) is saved once the criteria for  
 239 shallow convection are satisfied, but shallow convection will not be activated until the  
 240 time composite of moisture convergence ( $M^*$ ) turns positive. After the transition from  
 241 shallow to deep convection, stored memory of moisture convergence is eliminated for  
 242 the consumption of them by deep convection is very fast (LTW19). It should also be

243 noted that definitions of shallow convection are different in these schemes, but the main  
244 conclusion drawn in this study is not altered by the difference.

245

246 **4. Mean-state feature**

247 In this study, six 19-yr simulations from 1996 to 2014 are carried out with original  
248 (denoted as SAS, TDK and KFMT, respectively) and modified (denoted as SAS-n,  
249 TDK-n and KFMT-n, respectively) CP schemes. Diagnostics are focused on boreal  
250 winters (November-April) during this period. Averaged winter precipitation for  
251 observation and simulations is shown in Fig. 1. All the experiments with original CP  
252 schemes reproduce rain belts along climatological convergence zones in the western  
253 Pacific and over the Maritime Continent, though the amount of rainfall is generally  
254 overestimated (left panels of Fig. 1). However, these simulations miss the rainfall center  
255 in the eastern Indian Ocean and produce too much rainfall in the middle to western  
256 Indian Ocean. In the right panels, boreal winter-mean precipitation differences between  
257 modified and original schemes are displayed. Although the modification is only made  
258 to shallow convection which basically is nonprecipitating, rainfall is still modulated  
259 through interaction between shallow and deep convection. The modulation is quite  
260 moderate over the simulation region, except that precipitation is largely suppressed over  
261 the Maritime Continent in TDK-n. It means deep convection is largely mitigated in this  
262 case.

263 As rainfall is overestimated in the Indian Ocean, so is the MJO-filtered  
264 precipitation variance (Fig. 2). Here only eastward-propagating signals with zonal

265 wavenumbers 1–5 and periods 20–100 days are saved in order to filter MJO-related  
266 precipitation. Modification of shallow convection schemes is able to raise the  
267 precipitation variance to a level close to observation, but the location is still uncorrected.  
268 The precipitation variance over the Maritime Continent in TDK-n also decreases as  
269 precipitation itself.

270 In the following analyses, a lag-regression/correlation method is used. Before  
271 calculating regression/correlation coefficient, the climatological annual cycle (annual  
272 mean and three leading harmonics) is removed first, and then a 20–100 day band-pass  
273 filtering is operated with Butterworth filter. Regression/correlation coefficients are thus  
274 calculated against anomalies averaged over a box (80–90°E; 5°S–5°N) in the Indian  
275 Ocean. Lag correlations of filtered OLR with itself averaged over the box is shown in  
276 Fig. 3. Compared to observations, the propagation signals in control runs are rather  
277 weak and confined in the Indian Ocean area. Modification of shallow convection  
278 schemes helps to strengthen the eastward propagation of convection systems and extend  
279 them further into the western Pacific Ocean. Notice that the most significant  
280 improvement is observed in TDK-n (Fig. 3e), but the rainfall and its variance are  
281 decreased markedly (Figs. 1e and 2e). It suggests that vigorousness of shallow  
282 convection may lead to a suppression of deep convection.

283 Following Wheeler and Kiladis (1999), the wave number-frequency power spectra  
284 of equatorially symmetric component of tropical OLR between 15°S and 15°N is  
285 depicted in Fig. 4. Although control runs are able to reproduce the spectral power peak  
286 in the right range corresponding to MJO, its amplitude is reduced to a much lower level.

287 The modification of CPs generally augments the spectral power, especially in TDK-n  
288 and KFMT-n.

289

290 **5. Enhanced feedback between shallow convection and low-level  
291 moisture convergence**

292 As seen from above assessments, modification of shallow convection produces  
293 stronger intraseasonal variability and more importantly the improved eastward  
294 propagation. To figure out how the noninstantaneous moisture convergence closure  
295 improve MJO simulations, we will investigate the process of FSM first. Moisture  
296 content has been recognized to dominate the buildup and propagation of MJO  
297 convection (Sobel and Maloney 2012; Raymond and Fuchs 2009; Majda and  
298 Stechmann 2009). Fig. 5 displays lagged regression of specific humidity anomaly at  
299 850 hPa against rainfall over the Indian Ocean, together with regressed zonal wind at  
300 the same level. With the implication of new shallow convection closure, moisture and  
301 zonal wind anomalies increase, propagation signals extend to the further east, and the  
302 propagation speed slows down to that of the MJO ( $8 \text{ m s}^{-1}$ ). According to Wu (2003),  
303 decreased propagation speed is due to the smaller equivalent depth corresponding to  
304 enhanced shallow convection. Another noteworthy feature is that moisture anomalies  
305 lag easterly winds and collocate with the convergence zone of easterly winds. Above  
306 analysis indicates a concurrent enhancement of large-scale convergence, shallow  
307 convection, and low-level moisture content.

308 To display the changes of FSM brought about by noninstantaneous moisture

309 convergence closure, we calculate lag-regression of 10°S-10°N averaged diabatic  
310 heating at the longitude of 90°E against intraseasonal precipitation over the Indian  
311 Ocean. The total diabatic heating is derived with a residual budget analysis based on  
312 the temperature equation (Yanai et al., 1973; Ling and Zhang, 2011). Vertical-time  
313 regression pattern is shown in Fig. 6. The vertical backward tilting of diabatic heating  
314 is clearly seen in observation, but few of the control runs reproduce this tilted structure.  
315 As modified closure strengthens shallow convective heating which usually leads the  
316 main convective heating of MJO, simulations with modified CP schemes show more  
317 tilted heating structures. In simulations with TDK scheme, the time lag between shallow  
318 and deep convection on intraseasonal timescales is so short that they burst almost at the  
319 same time (Fig. 6d). Modification of shallow convection closure marginally alters the  
320 time lag, but it effectively enhances shallow convective heating and inhibits deep  
321 convective heating (Fig. 6e).

322 As in Fig. 6, the regression patterns of mass convergence and horizontal moisture  
323 advection terms composing moisture convergence (rhs terms of Eq. 3) are plotted in  
324 Figs. 7 and 8, respectively. The magnitude of horizontal advection is about one order  
325 smaller than that of mass convergence, so it is the mass convergence term that  
326 dominates moisture convergence. Similar to that of diabatic heating, regression patterns  
327 of mass convergence also show tilted structures which are better captured with modified  
328 CP schemes. Since shallow convection transports moisture upward (Benedict and  
329 Randall 2007; Pilon et al. 2016), enhanced shallow convection helps to extend mass  
330 convergence zone to higher levels. In contrast, horizontal advection of moisture usually

331 leads diabatic heating by about 10 days. Larger positive moisture advection seen near  
332 day -10 in modified simulations may be related to more suppressed convection ahead  
333 of major convection (Kim et al., 2014). This positive moisture advection contributes to  
334 moisture convergence and thus helps to trigger noninstantaneous convection-  
335 circulation feedback. Afterwards, enhanced shallow convection induces stronger  
336 moisture advection in the boundary layer (near day 0 in Fig. 8). It also helps to  
337 transports more moisture to higher levels and increase moisture content in the lower  
338 troposphere.

339 To better illustrate the influence of shallow convection closure on FSM, evolutions  
340 of regressed diabatic heating in the lower troposphere (850 hPa) and moisture  
341 convergence in the boundary layer (925 hPa) are plotted in Fig. 9. These two particular  
342 layers are chosen because shallow convective heating usually peaks at 850 hPa and  
343 moisture convergence maximizes and is vertically uniform in the boundary layer (Fig.  
344 7). In observation, diabatic heating leads boundary layer moisture convergence, which  
345 may be related to the fact that anomalous short wave heating starts near the surface  
346 before day -10 when convection is suppressed (Ciesielski et al. 2017). Numerical  
347 simulations seem not able to reproduce this time lag. Low-level diabatic heating and  
348 moisture convergence are almost in phase therein. Introducing a shallow convection  
349 closure based on the noninstantaneous wave-CISK helps to extend heating duration  
350 (Fig. 9b), increase heating amplitude (Fig. 9c), or both (Fig. 9d), and strengthen  
351 boundary layer moisture convergence as well. Although LTW19 suggests  
352 noninstantaneous convection-circulation feedback should be able to alter the phase

353 relationship between heating and moisture convergence, a finer time resolution is  
354 needed to display this change.

355

356 **6. Eastward propagation of MJO convection**

357 The remained question is, how this enhanced FSM promotes eastward propagation  
358 of MJO convection. Fig. 10 displays horizontal patterns of regressed moisture  
359 convergence at 925 hPa and horizontal winds at 850 hPa. Note that convection  
360 (precipitation) center is located in the Indian Ocean box ( $80^{\circ}$ - $90^{\circ}$ E;  $5^{\circ}$ S- $5^{\circ}$ N). The  
361 prominent feature of observation is that boundary layer moisture convergence extends  
362 to the east of MJO convection center and all the way to the western Pacific Ocean.  
363 Easterly winds are prevalent over the Indo-Pacific warm pool region and located to the  
364 further east of moisture convergence. These features can also be found in numerical  
365 simulations, with increased convergence and easterly winds over the warm pool region  
366 in SAS-n and KFMT-n. In the simulations with TDK type schemes, eastward extension  
367 of low-level moisture convergence is narrowly confined near the convection center over  
368 the Indian Ocean, which is consistent with the little vertical tilt in regressed heating  
369 structure (Fig. 6). Besides the enhanced shallow convective heating, boundary layer  
370 friction may also contribute to the increased moisture convergence (Wang and Rui 1990;  
371 Hsu and Li 2012).

372 Vertical-longitude regressions of specific humidity anomaly averaged between  
373  $10^{\circ}$ S and  $10^{\circ}$ N associated with rainfall over the Indian Ocean box are shown in Fig. 11.  
374 Westward tilt of specific humidity can be observed in observation, with positive

375 moisture anomaly in the lower troposphere to the east of convection center (80°-90°E).  
376 Comparing simulation results with different CP schemes, the biggest change is the  
377 enhanced positive moisture anomaly in lower levels to the east of 90°E, corresponding  
378 to the enhanced moisture convergence zone (Fig. 10).

379 Following Eq. 3, moisture convergence is decomposed into two terms associated  
380 with mass convergence and moisture advection. Difference between regressed moisture  
381 convergence terms at 925 hPa are plotted in Fig. 12. Obviously, mass convergence term  
382 dominates moisture convergence. In SAS simulations, modified CP scheme increases  
383 moisture convergence along the equator from the middle Indian Ocean to the western  
384 Pacific Ocean. While in the other two cases moisture convergence increments are found  
385 in smaller regions, they help to foster new convection to the east of convection center  
386 all the same. In contrast, positive horizontal advection in the boundary layer is usually  
387 located in regions where vigorous deep convection present, which can also be deduced  
388 from Fig. 8.

389 Although advection term makes little contribution to the total amount of moisture  
390 convergence, it may noticeably modulate the propagation of MJO due to its asymmetric  
391 pattern relative to convection center. Here the longitude-height plot of horizontal  
392 moisture advection averaged in tropical belt (10°S–10°N) and the difference between  
393 simulations with modified schemes and original ones are shown in Fig. 13. In  
394 agreement with previous studies (Kim et al. 2014; Adames and Wallace 2015; Zhu and  
395 Hendon 2015), the asymmetric structure of horizontal advection relative to rainfall  
396 center also contributes to eastward propagation (Figs. 13a, 13b, 13d and 13f). It

397 moistens the lower troposphere before the maximum rainfall (east of 90°E) while dries  
398 the lower troposphere after that (west of 90°E). Compared to control runs, modified  
399 schemes almost double the asymmetric advective tendencies and thus give rise to the  
400 eastward propagation (Figs. 13c, 13e and 13g).

401 Differences of horizontal moisture advection can be partitioned into contributions  
402 from zonal and meridional components. Fig. 14 displays differences of regressed zonal  
403 (Figs. 14a, 14c and 14e) and meridional (Figs. 14b, 14d and 14f) advection between  
404 simulations with modified CP schemes and control runs. Obviously, the difference of  
405 horizontal moisture advection mainly comes from the difference of zonal advection  
406 over the Indian and western Pacific Ocean. This result contradicts previous studies that  
407 the meridional component plays a key role in producing the asymmetric structure of  
408 horizontal moisture advection (Maloney 2009; Kim et al. 2014; Zhu and Hendon 2015).  
409 It may be related to enhanced shallow convection that usually locates to the east of  
410 maximum rainfall center and causes kelvin-wave response.

411 Following Maloney (2009) and Zhu and Hendon (2015), further analysis by  
412 separating horizontal advection into time mean and deviation from the time mean shows  
413 that the main contribution of the difference of regressed zonal advection is from that of  
414 advection of anomalous specific humidity by mean zonal wind (not shown). It means  
415 that, although enhanced shallow convection with modified CP schemes does not induce  
416 substantially stronger easterly winds to the east of 90°E (Fig. 10), it effectively moistens  
417 the lower troposphere there (Fig. 11), and then easterly winds advect anomalous  
418 moisture in the region of 90°E–120°E (see Fig. 14a, 14c and 14e).

419

420 **7. Discussion**

421 Previous studies demonstrate that shallow convection preconditions the  
422 atmosphere for the subsequent onset of active deep convection, which is fundamental  
423 to the eastward propagation of the MJO (Benedict and Randall 2007; Adames and  
424 Wallace 2015). However, if upward transport by large-scale forcing is not incorporated,  
425 shallow convection alone is not able to sufficiently moisten the lower troposphere  
426 (Hohenegger and Stevens 2013; Masunaga 2013; Kumar et al. 2013). In fact, shallow  
427 convective activity cannot be separated readily from its large-scale background, since  
428 a strong interaction exists between them. Notice that modified closure assumption of  
429 shallow convection only relates cloud-base mass flux to low-level moisture  
430 convergence. The feedback between shallow convection and low-level moisture  
431 convergence is not guaranteed therein. Improved simulation with modified CP scheme  
432 demonstrates that this feedback is an intrinsic character of large-scale convective  
433 system, and that the modified closure assumption helps to patch this feedback to make  
434 it work.

435 It is widely recognized that improved simulation of the MJO can be realized by  
436 increasing the sensitivity of deep convection to tropospheric humidity, such as  
437 increasing convective entrainment rate (Tokioka et al. 1988; Bechtold 2008; Benedict  
438 et al. 2014) or rain evaporation fraction (Maloney 2009; Hannah and Maloney 2011;  
439 Kim et al. 2012). These two modifications both help to suppress deep convection until  
440 other processes like shallow convection sufficiently moisten the atmosphere.

441 Noninstantaneous wave-CISK mechanism behaves quite similarly. Change of the ratio  
442 of shallow and deep convection in three pairs of simulations are plotted in Fig. 15. In  
443 agreement with above discussion, enhanced shallow convection is related to suppressed  
444 deep convection. KFMT scheme produces the largest increment of shallow convection,  
445 consistent with the strongest heating and moistening tendency seen in Figs. 6 and 11 in  
446 the lower troposphere. In this sense, merely modifying closure assumption seems  
447 inadequate to get a satisfying MJO simulation. Further work is required to study the  
448 interaction of shallow and deep convection and improve its description in CP scheme  
449 in the future.

450 Jiang et al. (2016) analyzed simulations with 25 climate models and observed an  
451 anti-correlation between convective time scale and MJO amplitude. The variable of  
452 convective time scale in their study is a measure of how rapidly precipitation must  
453 increase to remove excess column water vapor (see also Bretherton et al., 2004; Sobel  
454 and Maloney 2012). Similarly, the time scale ( $\tau$ ) here is a description of how rapidly  
455 converged moisture is transported upward through cloud base.  $\tau = 6$  h used in modified  
456 CP schemes is a rather rough estimation. We cannot determine its exact value at this  
457 moment. Sensitivity tests show that increased time scale leads to decreased amplitude  
458 of intraseasonal variability and westward propagation tendency. Suhas and Zhang (2015)  
459 estimated a time lag between moisture convergence and mass flux of about 1 h using  
460 cloud-resolving model simulation. But their model domain is  $256 \times 256$  km<sup>2</sup>, which  
461 means only meso-scale or small-scale process is included. Considering the large-scale  
462 system we intend to deal with, the time scale of 6 h is a reasonable estimation. More

463 study on the time scale  $\tau$  with observations and high-resolution numerical simulations  
464 will be conducted in the future.

465

466 **8. Summary**

467 Based on the noninstantaneous wave-CISK proposed in LTW19, three CP schemes  
468 are modified to couple shallow convection with large-scale circulation through low-  
469 level moisture convergence in this study. Simulations with modified CP schemes show  
470 improved eastward propagation signals and stronger intraseasonal variabilities of  
471 convection (OLR) without degrading the mean states. Through positive feedback  
472 between shallow convection and large-scale circulation, the intrinsic instability of  
473 noninstantaneous wave-CISK incorporated in CP schemes results in amplified shallow  
474 convective heating and/or extended heating duration, shaping tilted heating structure as  
475 in observations (Fig. 6). On the other hand, enhanced moisture convergence transports  
476 more moisture upward with horizontal advection augmenting the moistening prior to  
477 deep convection onset (Fig. 7 and 8).

478 The eastward propagation of the MJO is highly sensitive to the lower troposphere  
479 moisture content. To the east of major convection center, strong boundary layer  
480 moisture convergence is forced by shallow convection, which effectively moistens the  
481 lower atmosphere. Large-scale horizontal advection gives rise to eastward propagation  
482 by causing positive moisture tendency in the front of convection center and negative  
483 tendency in the tail. Zonal component is found to dominate the changes of moisture  
484 advection brought about by modification of CP schemes. In addition, the difference of

485 zonal advection mainly comes from the advection of anomalous specific humidity by  
486 mean zonal wind, which means FSM generates larger moisture anomaly than zonal  
487 wind anomaly.

488

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494

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688

689 **Table captions**

690 **Table 1.** Summary of criteria and closure assumptions for shallow convection in 3

691 cumulus parameterization schemes used in this study.  $P_s$  is the surface pressure.

692  $D_{\min}$  is the minimum cloud depth, which is a function of the temperature of lifting

693 condensation level.

694

695 **Tables**

CP schemes	Criteria for shallow convection	Closure assumptions for shallow convection (cloud-base mass flux)
Simplified Arakawa-Schubert ( <b>SAS</b> )	Cloud depth $\leq 150$ hPa, cloud top pressure $\geq 0.7P_s$	Related to surface buoyancy flux
Tiedtke ( <b>TDK</b> )	Cloud depth $\leq 200$ hPa	Related to tendency of boundary layer moist static energy
Kain-Fritsch with trigger ( <b>KFMT</b> )	Cloud depth $\leq D_{\min}$ , $D_{\min}$ varies from 2 km to 4 km	Related to subcloud layer turbulent kinetic energy

696 **Table 1.** Summary of criteria and closure assumptions for shallow convection in 3  
 697 cumulus parameterization schemes used in this study.  $P_s$  is the surface pressure.  $D_{\min}$  is  
 698 the minimum cloud depth, which is a function of the temperature of lifting condensation  
 699 level.  
 700

701 **Figure captions**

702 **Figure 1.** Boreal winter-mean precipitation ( $\text{mm d}^{-1}$ ) in observation (a) and simulations  
703 with CP schemes of SAS (b), TDK (d) and KF (f). The difference of boreal winter-  
704 mean precipitation ( $\text{mm d}^{-1}$ ) between simulations of SAS-n and SAS (c), TDK-n  
705 and TDK (e), KF-n and KF (g).

706 **Figure 2.** Boreal winter variance of MJO-filtered (periods 20-100 days, eastward  
707 propagating wavenumbers 1-5) precipitation ( $\text{mm}^2 \text{ d}^{-2}$ ) in observation (a) and  
708 simulations with CP schemes of SAS (b), SAS-n (c), TDK (d), TDK-n (e), and KF  
709 (f) and KF-n (g).

710 **Figure 3.** Longitude-time evolution of OLR anomalies by lag correlations of 20-100  
711 day band-pass-filtered anomalous OLR with itself averaged over the equatorial  
712 Indian Ocean box ( $80\text{-}90^\circ\text{E}$ ;  $5^\circ\text{S}\text{-}5^\circ\text{N}$ ). (a) is for observation and (b)-(g) are for  
713 simulations with different CP schemes. Fields are averaged between  $10^\circ\text{S}$  and  
714  $10^\circ\text{N}$ . Solid lines in each panel denote the eastward propagation speed of  $8 \text{ m s}^{-1}$ .

715 **Figure 4.** Frequency-zonal wavenumber power spectra of the symmetric component  
716 (about the equator) of OLR for (a) observation and (b)-(g) simulations with  
717 different CP schemes. Shaded is the base-10 logarithm of the averaged power  
718 between  $15^\circ\text{S}$  and  $15^\circ\text{N}$ .

719 **Figure 5.** Longitude-time evolution of specific humidity anomalies ( $\text{g kg}^{-1}$ , shading)  
720 and 850 hPa zonal wind anomalies (contours, interval of  $0.3 \text{ m s}^{-1}$ , positive, zero  
721 and negative values represented by thin dashed, thick solid and thin solid lines) by  
722 lag regression of 20-100 day band-pass-filtered anomalous specific humidity and

723 zonal wind against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for  
724 observation and (b)-(g) are for simulations with different CP schemes. Regression  
725 is scaled to 3 mm d<sup>-1</sup> precipitation rate. Fields are averaged between 10°S and  
726 10°N. Solid straight lines in each panel denote the eastward propagation speed of  
727 8 m s<sup>-1</sup>.

728 **Figure 6.** Time-height structures of diabatic heating anomalies (K) by lag regression of  
729 20-100 day band-pass-filtered anomalous total diabatic heating at the longitude of  
730 90°E against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation  
731 and (b)-(g) are for simulations with different CP schemes. Thick solid lines  
732 represent zero heating anomaly. Regression is scaled to 3 mm d<sup>-1</sup> precipitation rate.  
733 Fields are averaged between 10°S and 10°N.

734 **Figure 7.** As in Fig. 6, but for the mass convergence term (10<sup>-6</sup> g kg<sup>-1</sup> s<sup>-1</sup>) in Eq. (3).

735 **Figure 8.** As in Fig. 6, but for the horizontal moisture advection term (10<sup>-6</sup> g kg<sup>-1</sup> s<sup>-1</sup>) in  
736 Eq. (3).

737 **Figure 9.** Time evolution of diabatic heating (K, red line) and moisture divergence (10<sup>-6</sup> g kg<sup>-1</sup> s<sup>-1</sup>, sign reversed moisture convergence, blue line) anomalies by lag  
738 regression of 20-100 day band-pass-filtered anomalous of 850-hPa total diabatic  
739 heating and 925-hPa moisture convergence at the longitude of 90°E against Indian  
740 Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation and (b)-(d) are for  
741 simulations with different CP schemes. In (b)-(d), solid and dashed lines represent  
742 original and modified schemes respectively. Regression is scaled to 3 mm d<sup>-1</sup>  
743 precipitation rate. Fields are averaged between 10°S and 10°N.

745 **Figure 10.** Horizontal patterns of moisture convergence ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ) and horizontal  
746 wind anomalies calculated by zero lag-regression of 20-100 day band-pass-filtered  
747 anomalous 925-hPa moisture convergence and 850-hPa horizontal wind against  
748 Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation and (b)-(d)  
749 are for simulations with different CP schemes. Regression is scaled to  $3 \text{ mm d}^{-1}$   
750 precipitation rate.

751 **Figure 11.** Longitude-height structures of specific humidity ( $\text{g kg}^{-1}$ ) calculated by zero  
752 lag-regression of 20-100 day band-pass-filtered anomalous specific humidity  
753 against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation and  
754 (b)-(g) are for simulations with different CP schemes. Regression is scaled to 3  
755  $\text{mm d}^{-1}$  precipitation rate. Fields are averaged between 10°S and 10°N.

756 **Figure 12.** Horizontal patterns of the differences of moisture convergence terms ( $10^{-6}$   
757  $\text{g kg}^{-1} \text{ s}^{-1}$ ) between 3 pairs of simulations with different CP schemes, calculated by  
758 zero lag-regression of 20-100 day band-pass-filtered anomalous 925-hPa mass  
759 convergence (a, c, e) and moisture advection (b, d, f) against Indian Ocean  
760 precipitation (80-90°E; 5°S-5°N). Regression is scaled to  $3 \text{ mm d}^{-1}$  precipitation  
761 rate.

762 **Figure 13.** Longitude-height structures of moisture advection ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ) calculated  
763 by zero lag-regression of 20-100 day band-pass-filtered anomalous horizontal  
764 moisture advection against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is  
765 for observation and (b), (d), (f) are for simulations with SAS, TDK, and KF  
766 schemes respectively. (c), (e), (g) are the differences between 3 pairs of

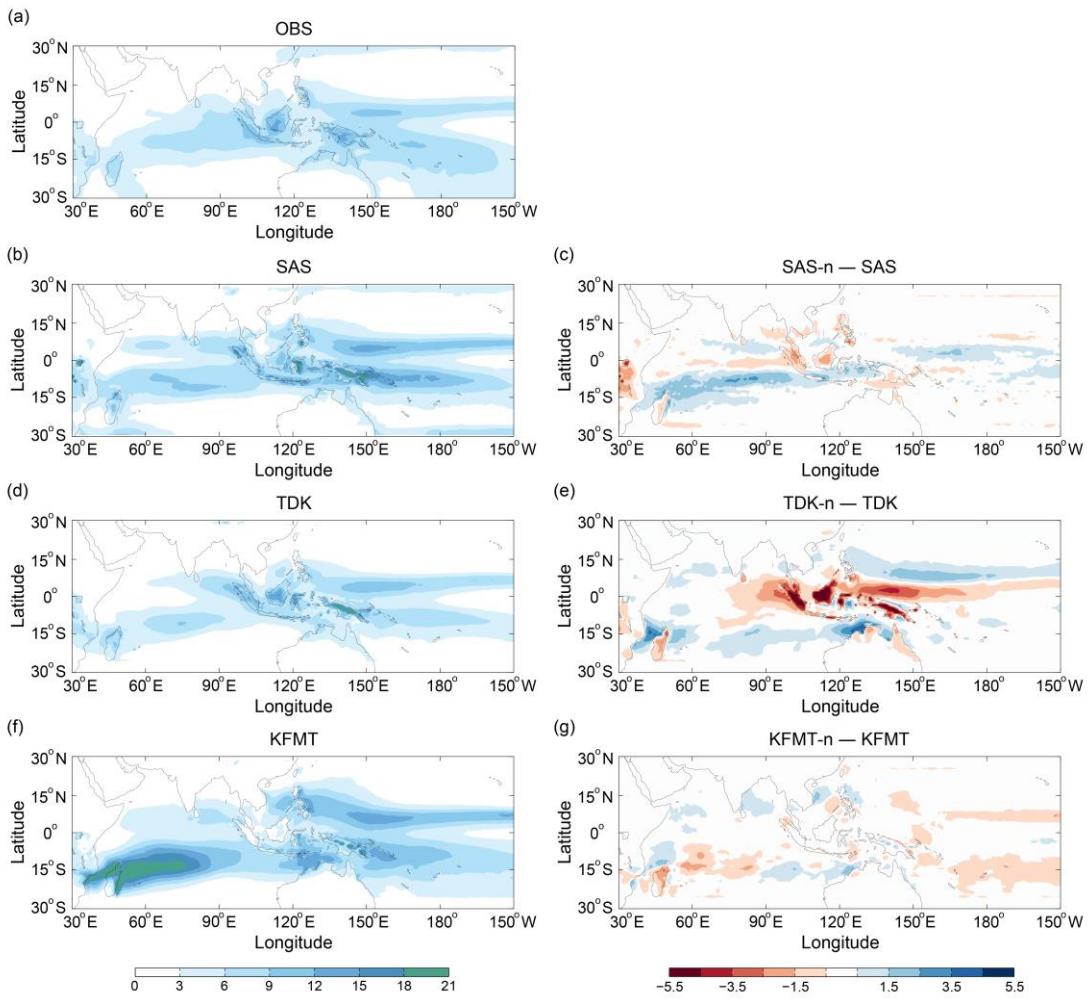
767 simulations. Regression is scaled to 3 mm d<sup>-1</sup> precipitation rate. Fields are  
768 averaged between 10°S and 10°N.

769 **Figure 14.** As in Fig. 13 (c), (e) and (g), but for the zonal (a, c, e) and meridional (b, d,  
770 f) moisture advection ( $10^{-6}$  g kg<sup>-1</sup> s<sup>-1</sup>).

771 **Figure 15.** Ratio number (occurrence times averaged by total time steps and the number  
772 of horizontal grids in the region of 60-180°E, 15°S-15°N) change for shallow  
773 (circle) and deep (triangle) convection in 3 pairs of simulations with different CP  
774 schemes.

775

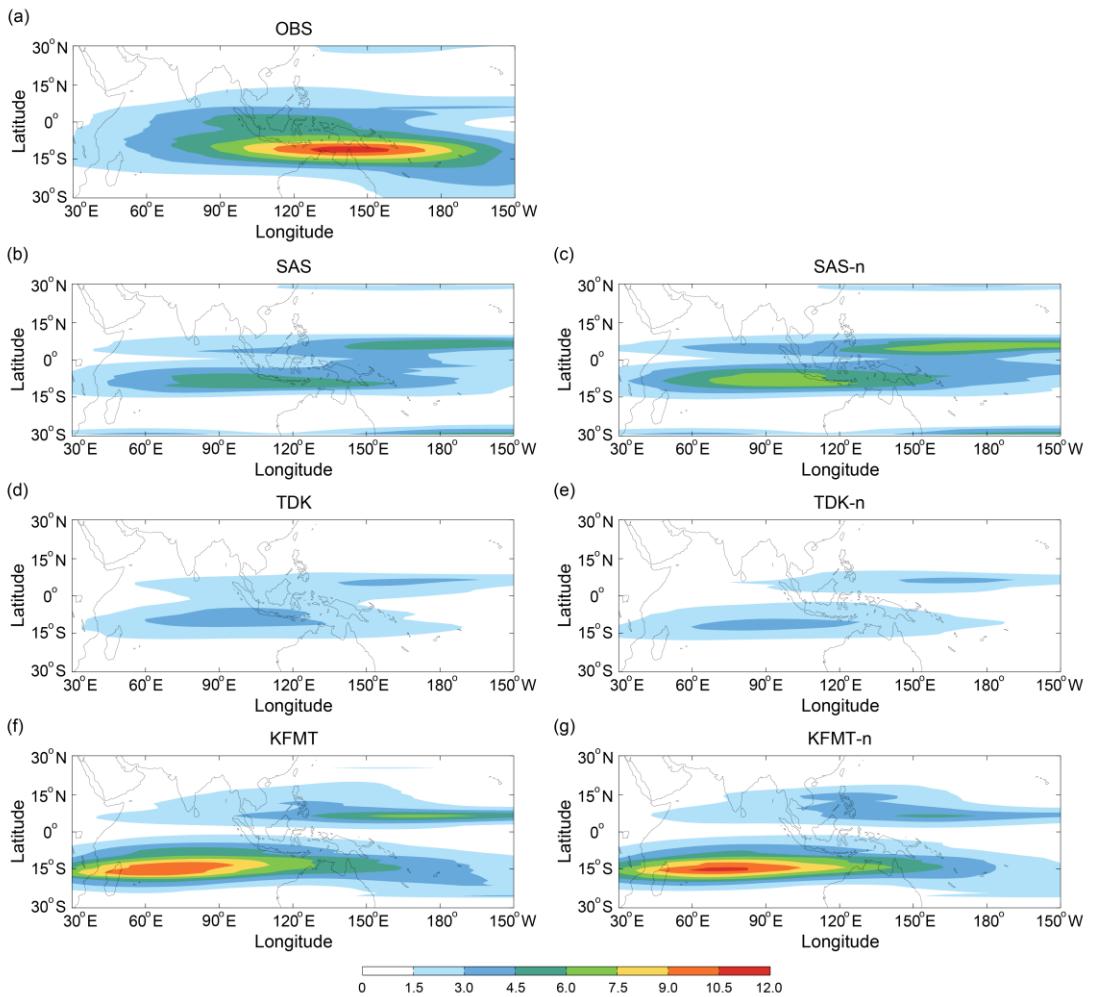
776 **Figures**



777

778 **Figure 1.** Boreal winter-mean precipitation (mm d⁻¹) in observation (a) and simulations  
 779 with CP schemes of SAS (b), TDK (d) and KFMT (f). The difference of boreal winter-  
 780 mean precipitation (mm d⁻¹) between simulations of SAS-n and SAS (c), TDK-n and  
 781 TDK (e), KFMT-n and KFMT (g).

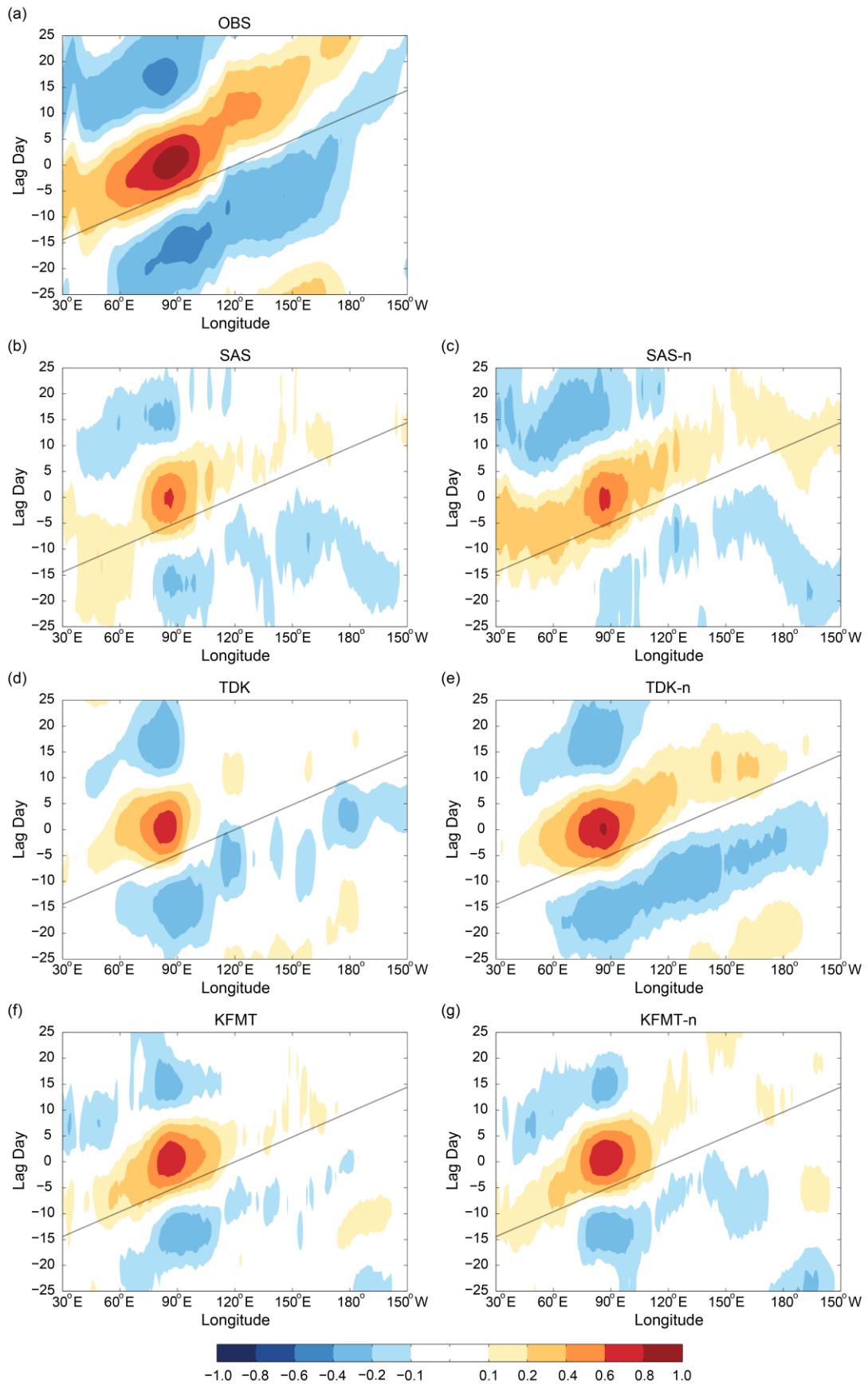
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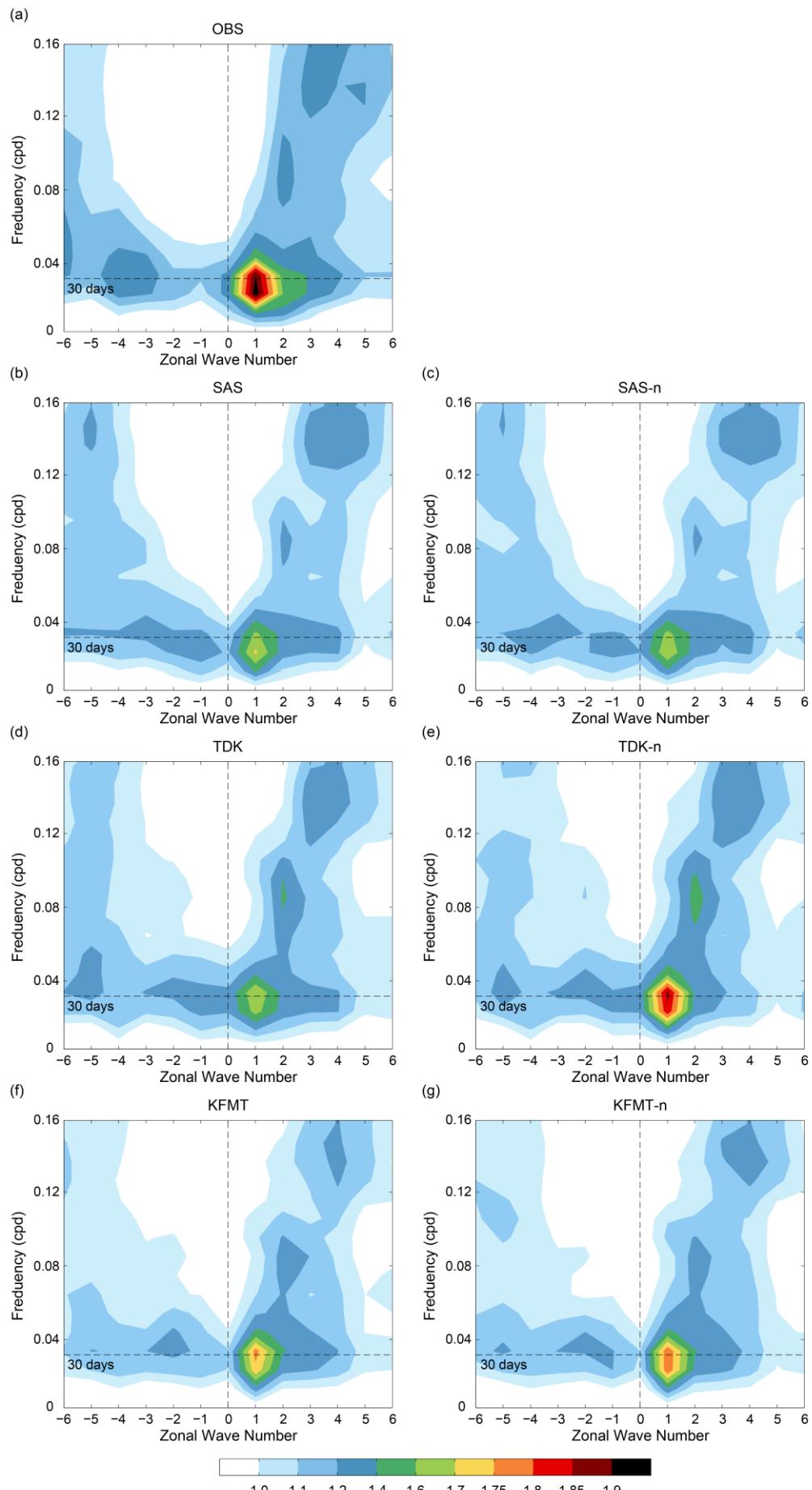
783

784 **Figure 2.** Boreal winter variance of MJO-filtered (periods 20-100 days, eastward  
 785 propagating wavenumbers 1-5) precipitation ( $\text{mm}^2 \text{ d}^{-2}$ ) in observation (a) and  
 786 simulations with CP schemes of SAS (b), SAS-n (c), TDK (d), TDK-n (e), KFMT (f)  
 787 and KFMT-n (g).

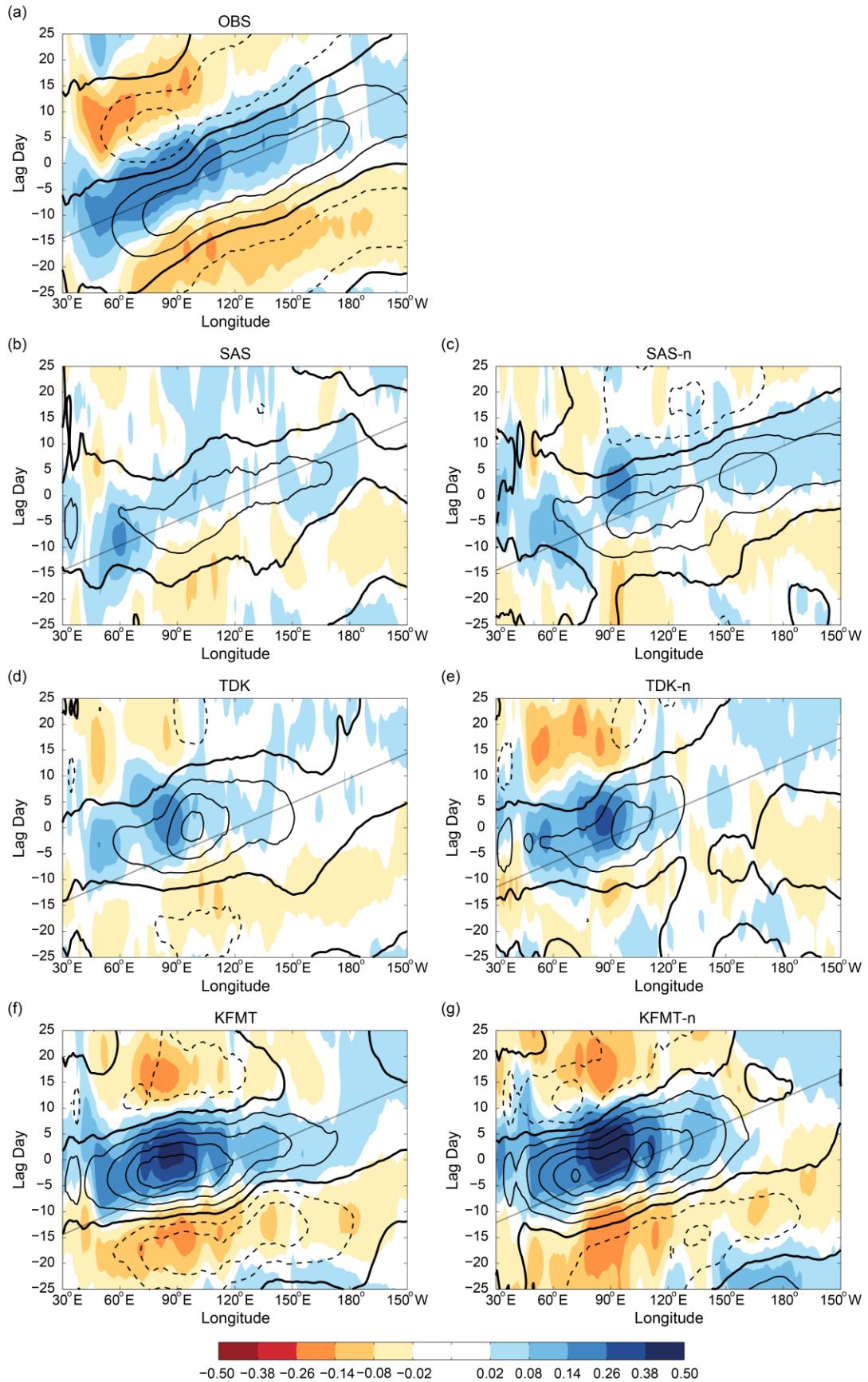
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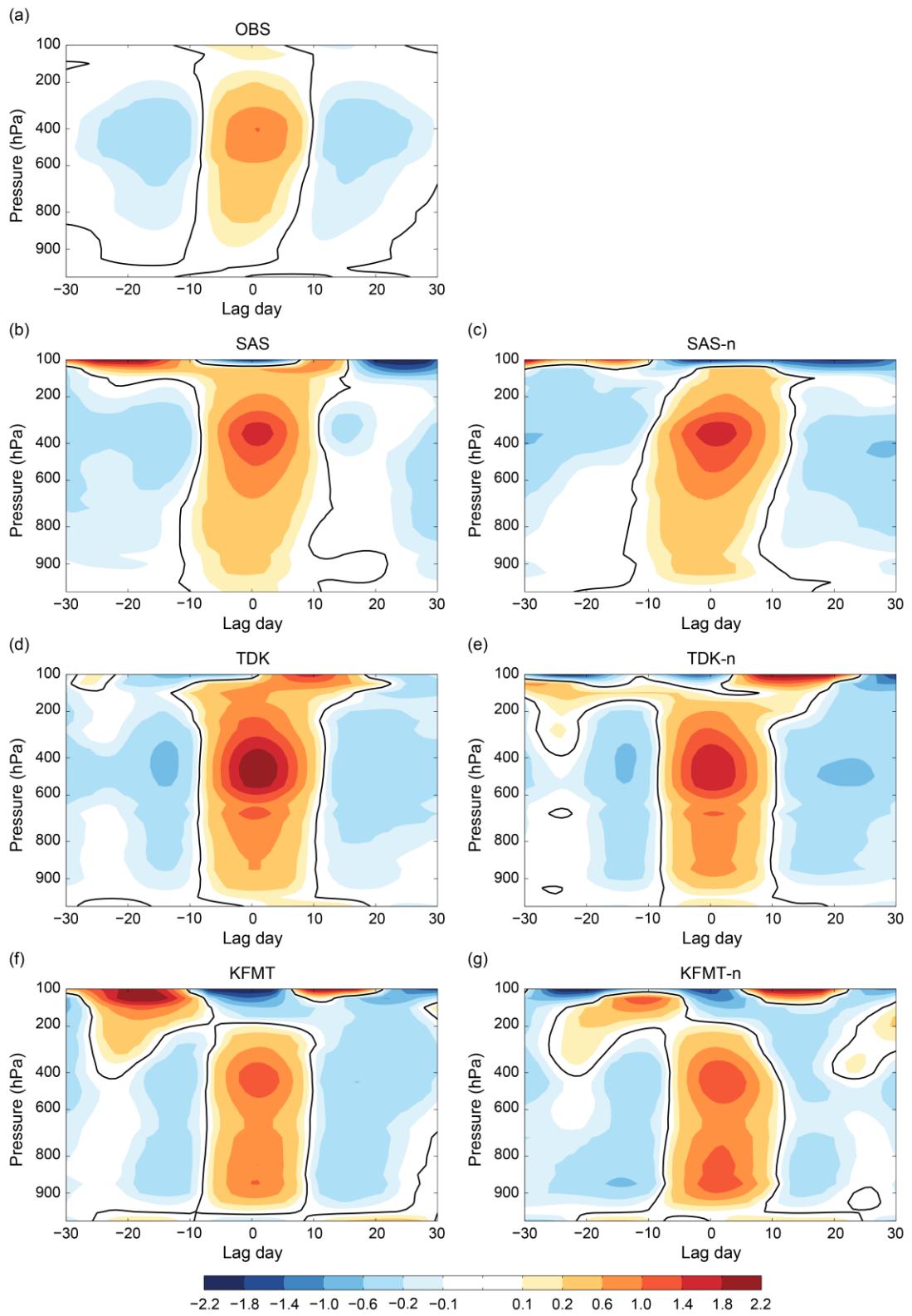
790 **Figure 3.** Longitude-time evolution of OLR anomalies by lag correlations of 20-100  
791 day band-pass-filtered anomalous OLR with itself averaged over the equatorial Indian  
792 Ocean box ( $80\text{-}90^\circ\text{E}$ ;  $5^\circ\text{S}\text{-}5^\circ\text{N}$ ). (a) is for observation and (b)-(g) are for simulations  
793 with different CP schemes. Fields are averaged between  $10^\circ\text{S}$  and  $10^\circ\text{N}$ . Solid lines in  
794 each panel denote the eastward propagation speed of  $8 \text{ m s}^{-1}$ .  
795



797 **Figure 4.** Frequency-zonal wavenumber power spectra of the symmetric component  
798 (about the equator) of OLR for (a) observation and (b)-(g) simulations with different  
799 CP schemes. Shaded is the base-10 logarithm of the averaged power between 15°S and  
800 15°N.  
801

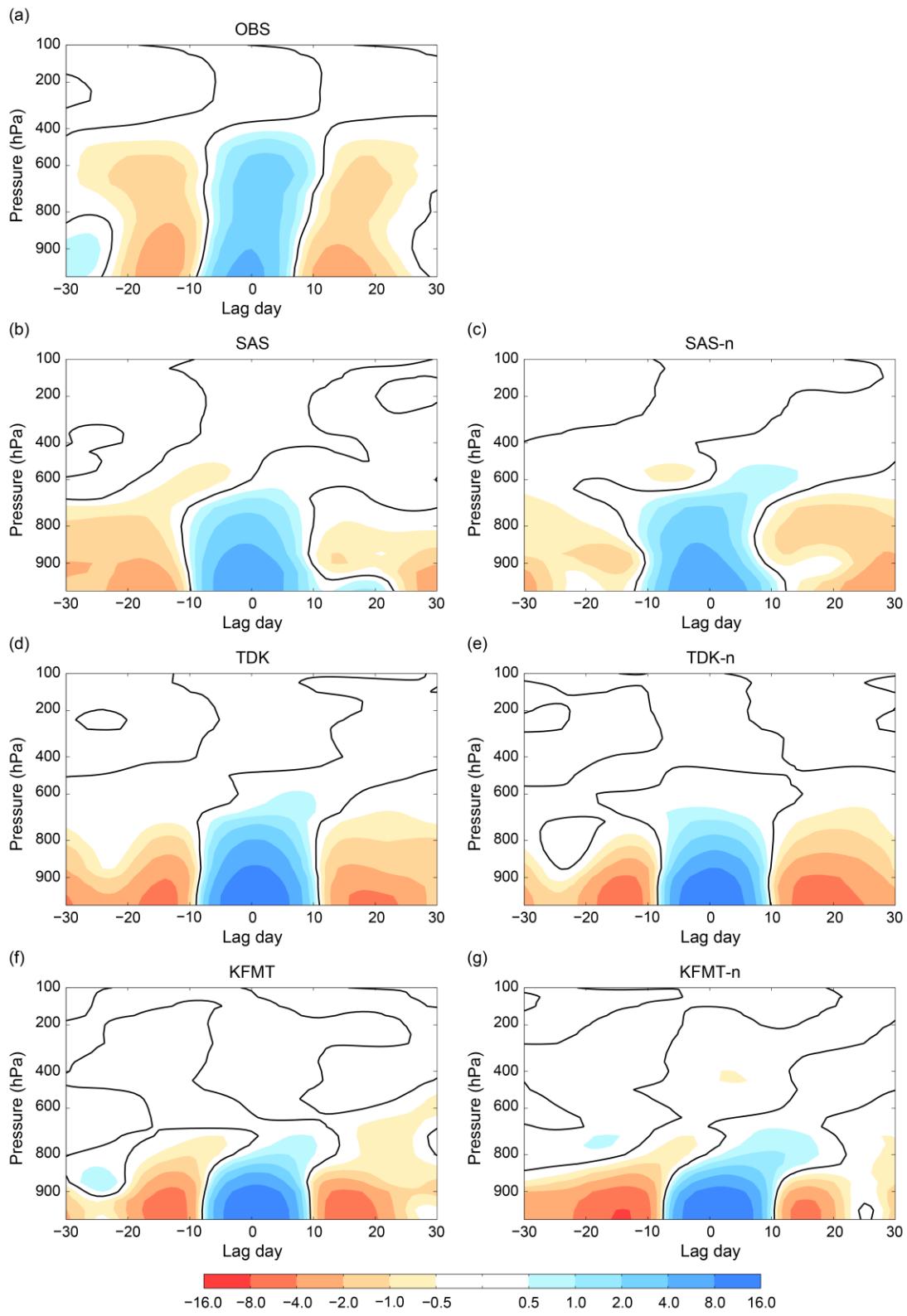


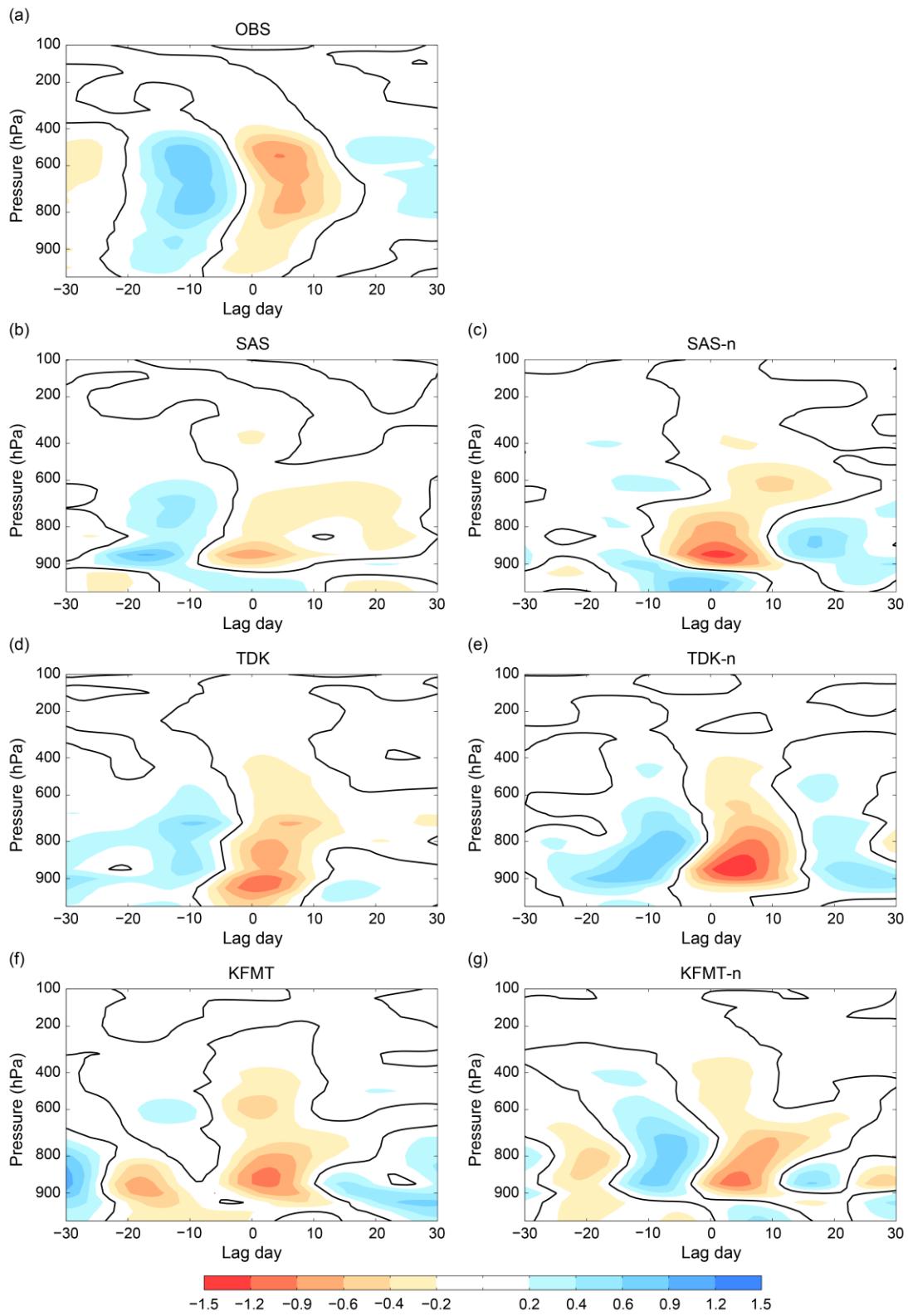
803 **Figure 5.** Longitude-time evolution of specific humidity anomalies ( $\text{g kg}^{-1}$ , shading)  
804 and 850 hPa zonal wind anomalies (contours, interval of  $0.3 \text{ m s}^{-1}$ , positive, zero and  
805 negative values represented by thin dashed, thick solid and thin solid lines) by lag  
806 regression of 20-100 day band-pass-filtered anomalous specific humidity and zonal  
807 wind against Indian Ocean precipitation ( $80\text{-}90^\circ\text{E}$ ;  $5^\circ\text{S}\text{-}5^\circ\text{N}$ ). (a) is for observation and  
808 (b)-(g) are for simulations with different CP schemes. Regression is scaled to  $3 \text{ mm d}^{-1}$   
809 precipitation rate. Fields are averaged between  $10^\circ\text{S}$  and  $10^\circ\text{N}$ . Solid straight lines in  
810 each panel denote the eastward propagation speed of  $8 \text{ m s}^{-1}$ .  
811



813 **Figure 6.** Time-height structures of diabatic heating anomalies (K) by lag regression of  
814 20-100 day band-pass-filtered anomalous total diabatic heating at the longitude of 90°E  
815 against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation and (b)-  
816 (g) are for simulations with different CP schemes. Thick solid lines represent zero  
817 heating anomaly. Regression is scaled to 3 mm d<sup>-1</sup> precipitation rate. Fields are  
818 averaged between 10°S and 10°N.

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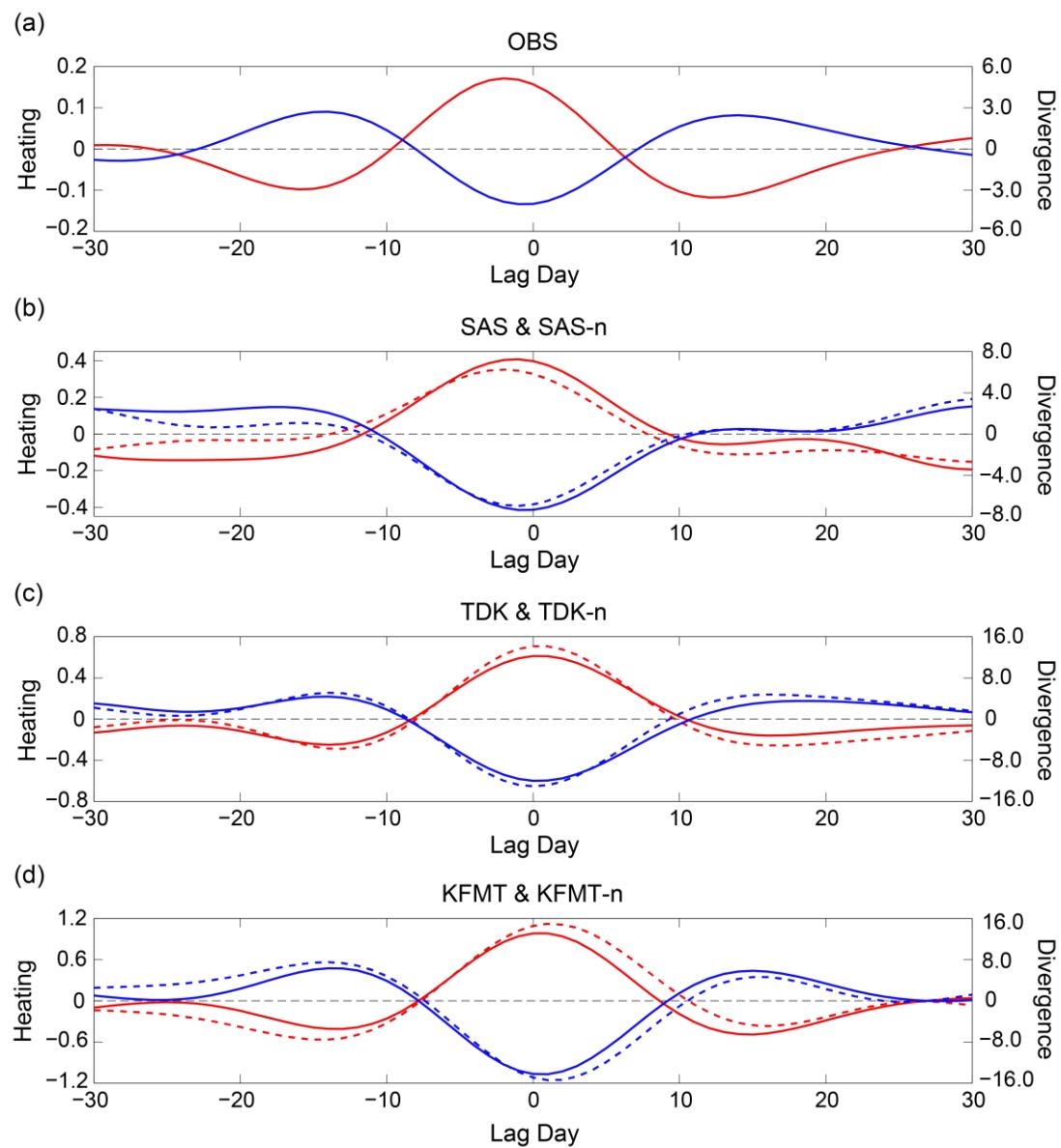




823

824 **Figure 8.** As in Fig. 6, but for the horizontal moisture advection term ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ) in  
825 Eq. (3).

826

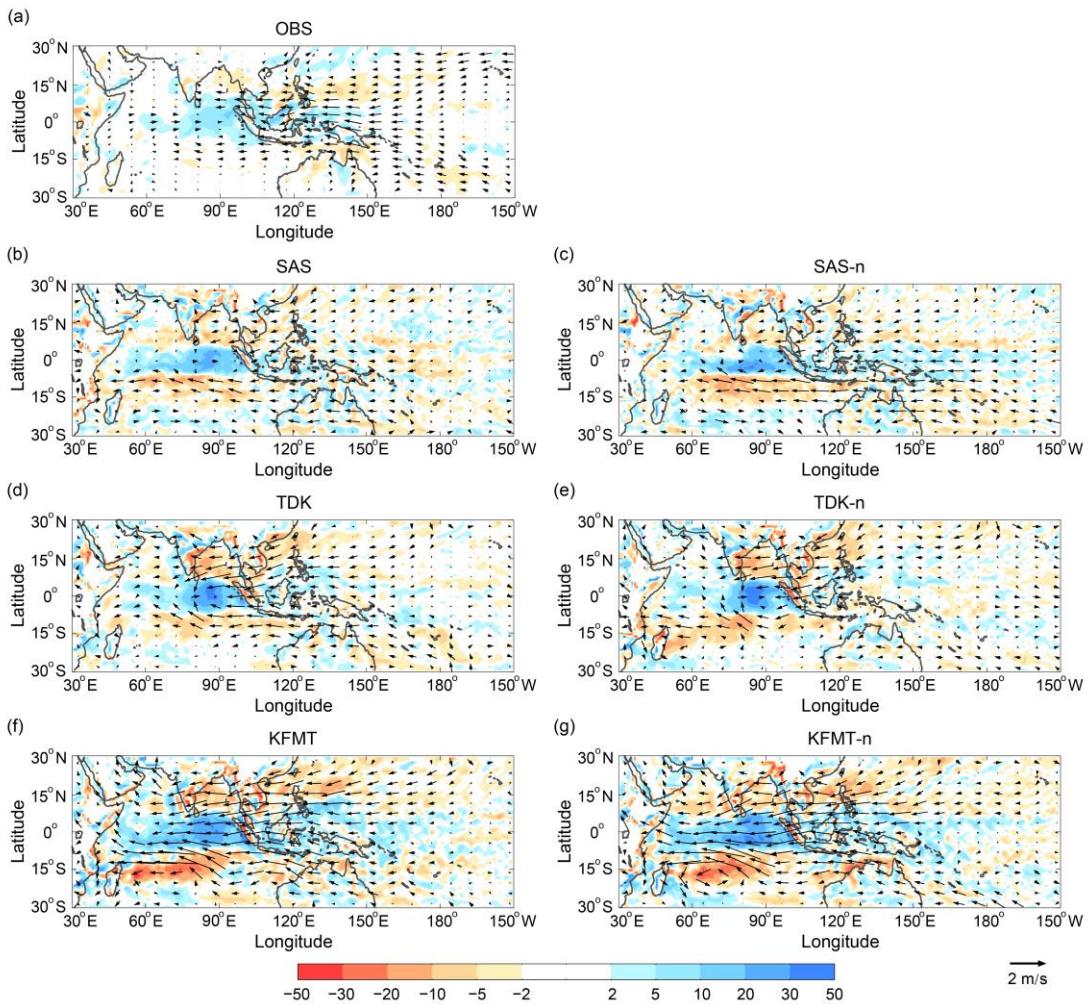


827

828 **Figure 9.** Time evolution of diabatic heating (K, red line) and moisture divergence ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ , sign reversed moisture convergence, blue line) anomalies by lag regression  
829 of 20-100 day band-pass-filtered anomalous of 850-hPa total diabatic heating and 925-hPa moisture convergence at the longitude of 90°E against Indian Ocean precipitation  
830 (80-90°E; 5°S-5°N). (a) is for observation and (b)-(d) are for simulations with different  
831 CP schemes. In (b)-(d), solid and dashed lines represent original and modified schemes  
832 respectively. Regression is scaled to  $3 \text{ mm d}^{-1}$  precipitation rate. Fields are averaged  
833 between 10°S and 10°N.

834

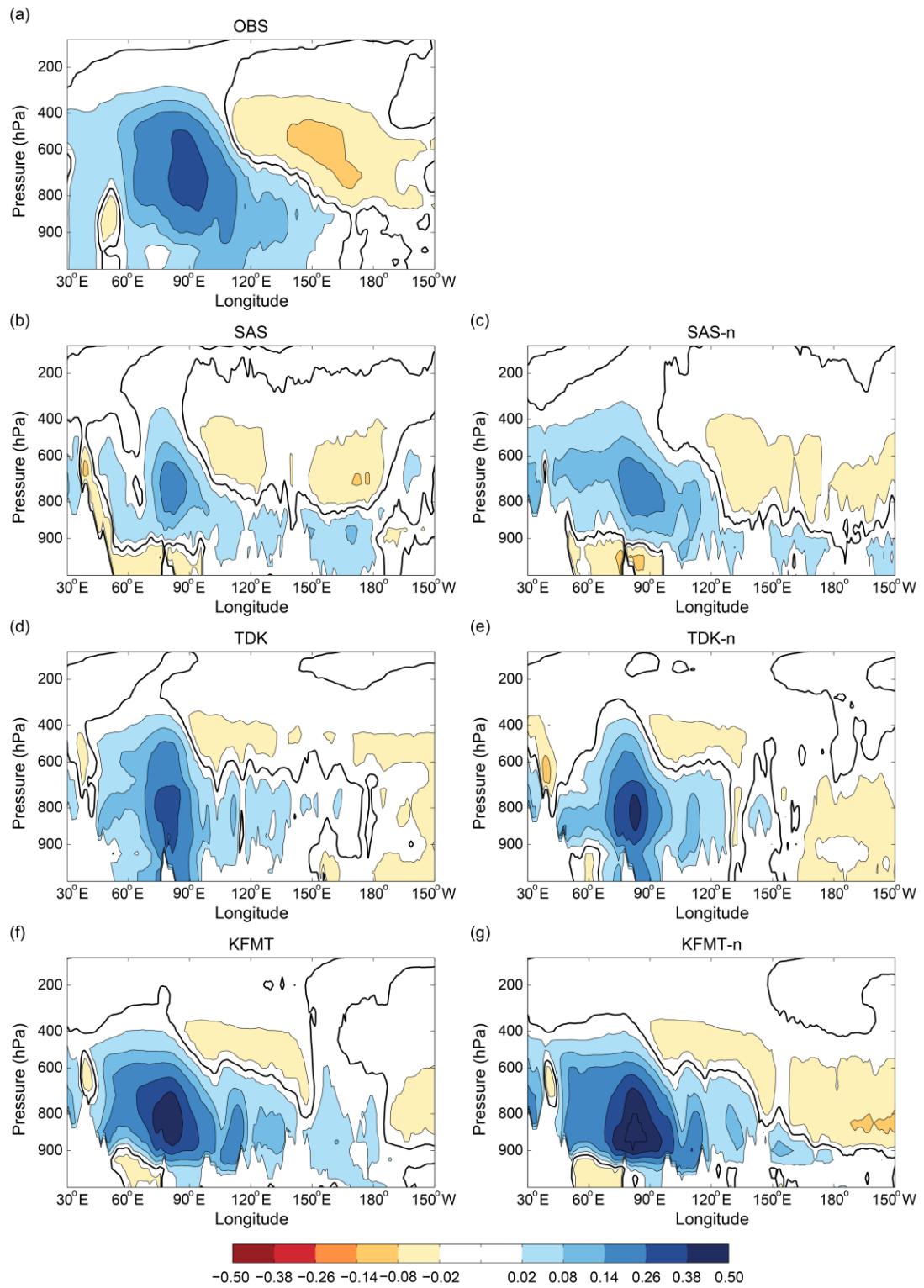
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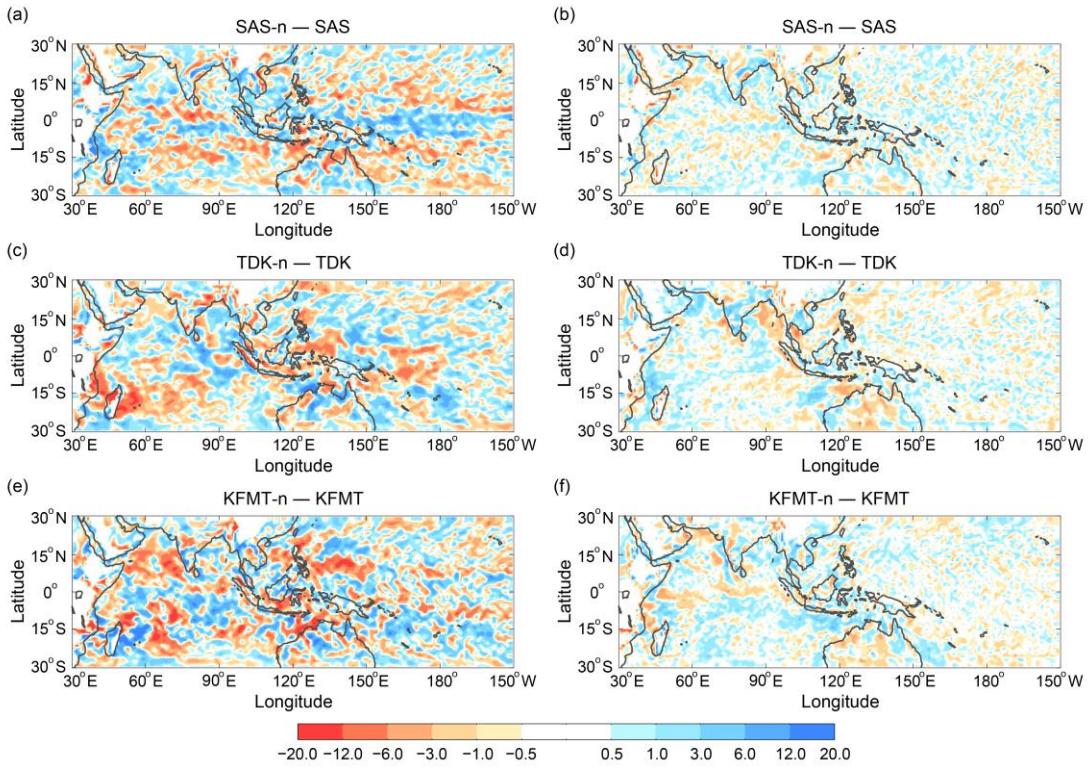
838 **Figure 10.** Horizontal patterns of moisture convergence ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ) and horizontal  
 839 wind anomalies calculated by zero lag-regression of 20-100 day band-pass-filtered  
 840 anomalous 925-hPa moisture convergence and 850-hPa horizontal wind against Indian  
 841 Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation and (b)-(g) are for  
 842 simulations with different CP schemes. Regression is scaled to  $3 \text{ mm d}^{-1}$  precipitation  
 843 rate.

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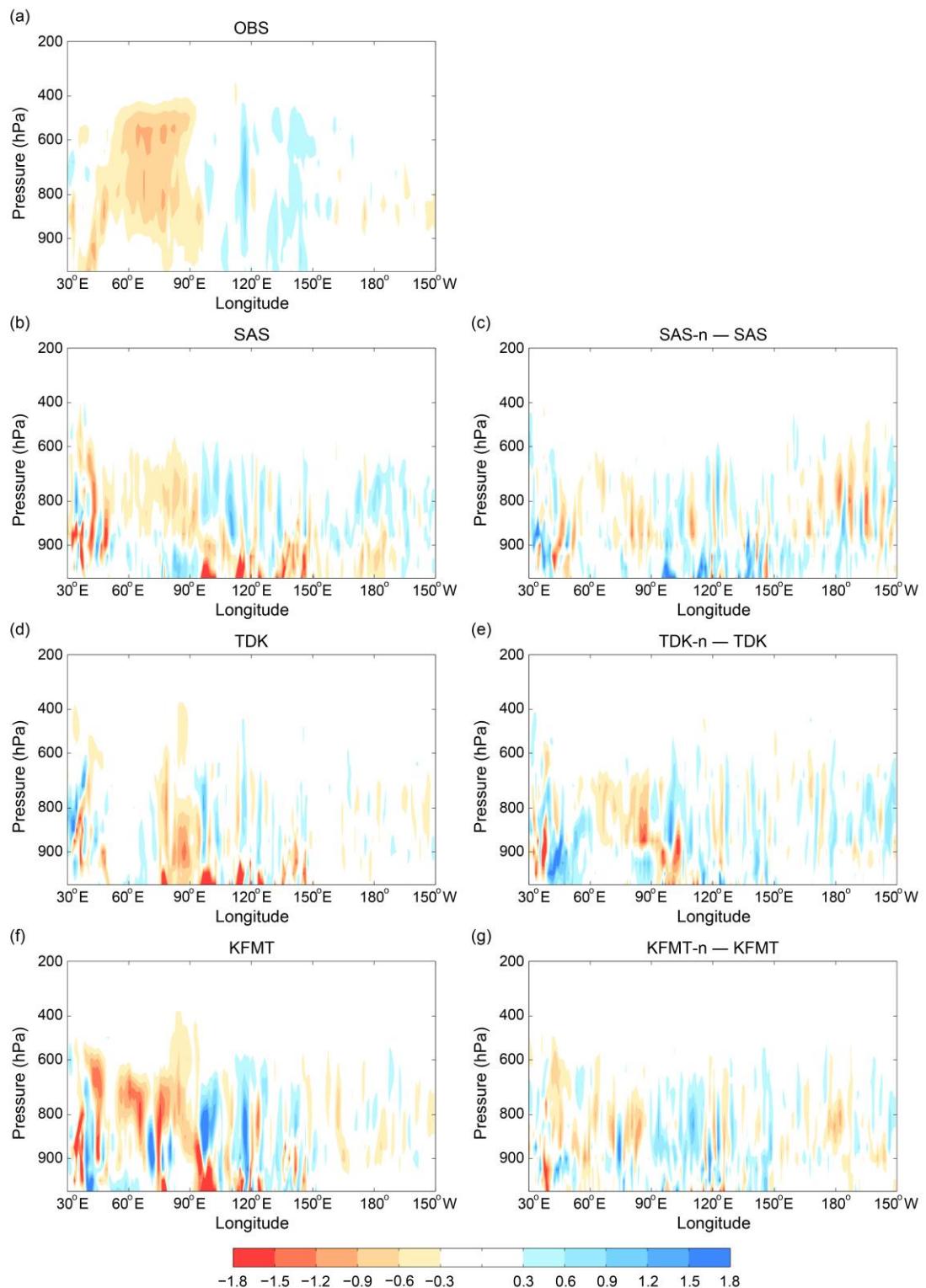
846 **Figure 11.** Longitude-height structures of specific humidity ( $\text{g kg}^{-1}$ ) calculated by zero  
847 lag-regression of 20-100 day band-pass-filtered anomalous specific humidity against  
848 Indian Ocean precipitation ( $80\text{-}90^\circ\text{E}$ ;  $5^\circ\text{S}\text{-}5^\circ\text{N}$ ). (a) is for observation and (b)-(g) are  
849 for simulations with different CP schemes. Regression is scaled to  $3 \text{ mm d}^{-1}$   
850 precipitation rate. Fields are averaged between  $10^\circ\text{S}$  and  $10^\circ\text{N}$ .

851

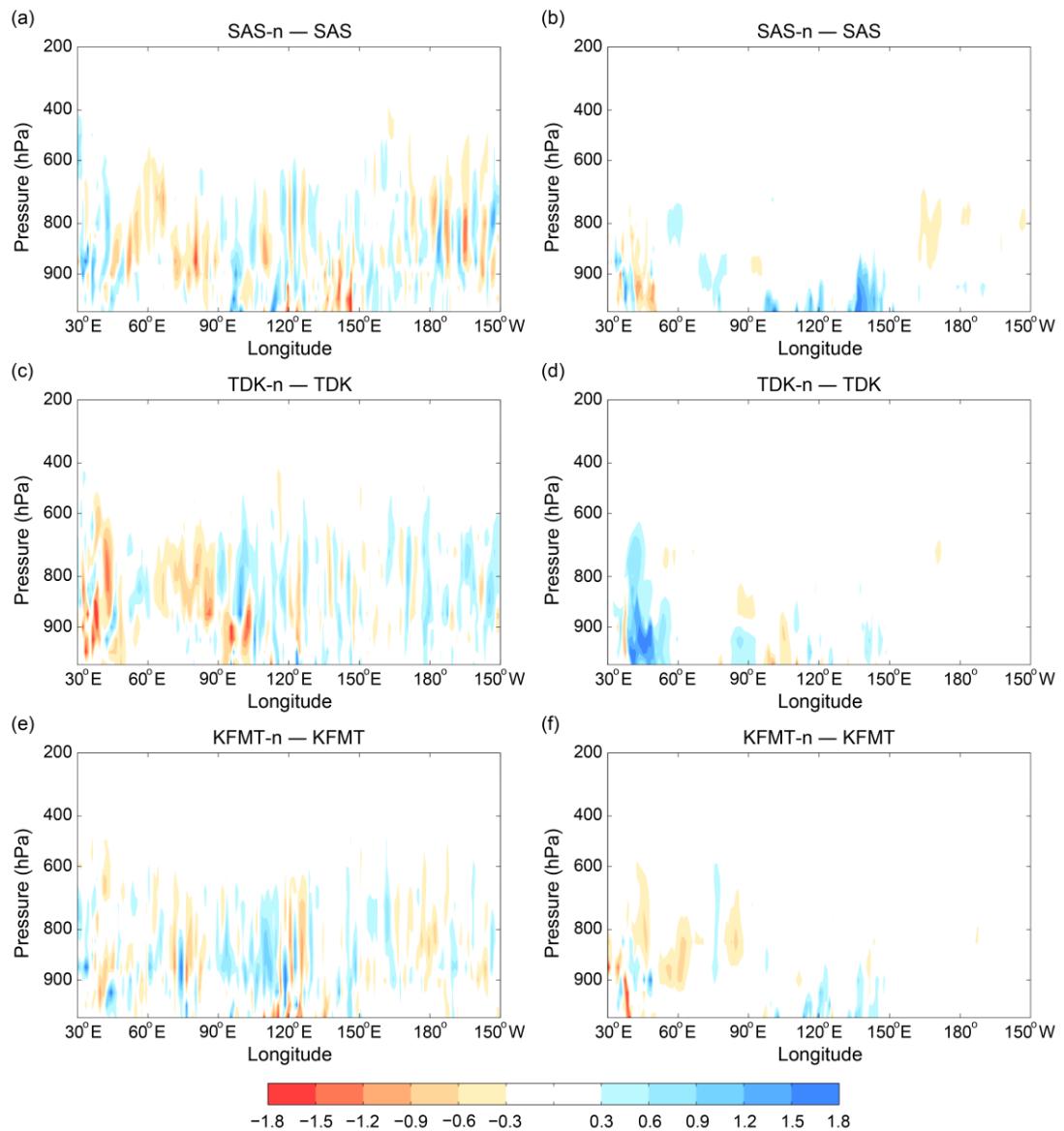


852

853 **Figure 12.** Horizontal patterns of the differences of moisture convergence terms ( $10^{-6}$   
 854  $\text{g kg}^{-1} \text{ s}^{-1}$ ) between 3 pairs of simulations with different CP schemes, calculated by zero  
 855 lag-regression of 20-100 day band-pass-filtered anomalous 925-hPa mass convergence  
 856 (a, c, e) and moisture advection (b, d, f) against Indian Ocean precipitation (80-90°E;  
 857 5°S-5°N). Regression is scaled to 3  $\text{mm d}^{-1}$  precipitation rate.  
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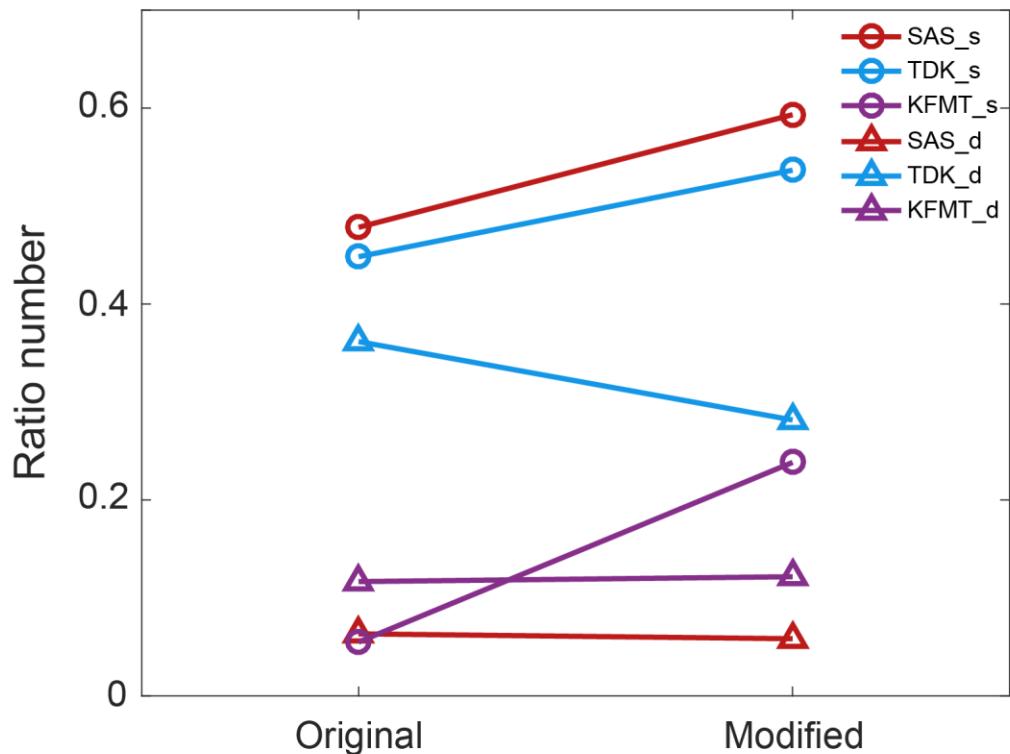
860 **Figure 13.** Longitude-height structures of moisture advection ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ) calculated  
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862 advection against Indian Ocean precipitation (80-90°E; 5°S-5°N). (a) is for observation  
863 and (b), (d), (f) are for simulations with SAS, TDK, and KFMT schemes respectively.  
864 (c), (e), (g) are the differences between 3 pairs of simulations. Regression is scaled to  
865 3 mm  $\text{d}^{-1}$  precipitation rate. Fields are averaged between 10°S and 10°N.  
866



867

868 **Figure 14.** As in Fig. 13 (c), (e) and (g), but for the zonal (a, c, e) and meridional (b, d, f) moisture advection ( $10^{-6} \text{ g kg}^{-1} \text{ s}^{-1}$ ).

870



871

872 **Figure 15.** Ratio number (occurrence times averaged by total time steps and the number  
 873 of horizontal grids in the region of 60-180°E, 15°S-15°N) change for shallow (circle)  
 874 and deep (triangle) convection in 3 pairs of simulations with different CP schemes.  
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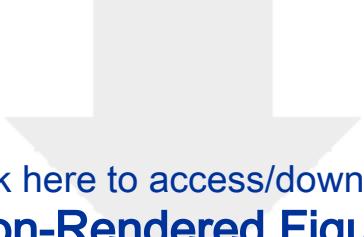
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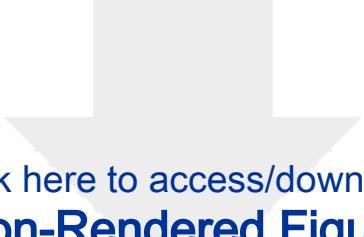


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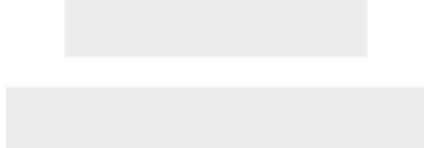


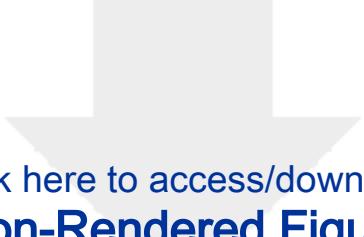


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