

# Statistical Analysis of Simulated Spaceborne Thermodynamics Lidar Measurements in the Planetary Boundary Layer

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10

11 **Abstract**

12 The performance of a spaceborne Raman lidar offering measurements of water vapor, temperature,  
13 aerosol backscatter and extinction is assessed statistically by use of a lidar simulator and a global  
14 model to provide inputs for simulation. The candidate thermodynamics lidar system is envisioned to  
15 make use of a sun-synchronous, dawn/dusk orbit. Cloud-free atmospheric profiles simulated by the  
16 NASA/GSFC GEOS model for the orbit of the CALIPSO satellite on July 15, 2009 were used as  
17 input to a previously validated lidar simulator where GEOS profiles that satisfy the solar zenith angle  
18 restrictions of the dawn/dusk orbit, and are located within the Planetary Boundary Layer as defined  
19 by the GEOS model, were selected for the statistical analysis. To assess the performance of the  
20 simulated thermodynamics lidar system, measurement goals were established by considering the  
21 WMO Observing Systems Capability Analysis and Review (OSCAR) requirements for Numerical  
22 Weather Prediction. The efforts of Di Girolano et al., 2018 established the theoretical basis for the  
23 current work and discussed many of the technological considerations for a spaceborne  
24 thermodynamics lidar. The work presented here was performed during 2017-2018 under the auspices  
25 of the NASA/GSFC Planetary Boundary Layer Science Task Group and expanded on previous  
26 efforts by considerably increasing the statistical robustness of the performance simulations and  
27 extending the statistics to include those of aerosol backscatter and extinction measurements. Further  
28 work that is currently being conducted includes Observing Systems Simulation Experiments to assess  
29 the impact of a thermodynamics lidar on global forecast improvement.

30

31 **1 Introduction**

32 The National Academy of Science (NAS) in the 2018 Decadal Survey (NAS, 2018) identified the  
33 Planetary Boundary Layer (PBL) as a key targeted observable and specified lidar as one of the prime  
34 technologies for measuring it. There are many reasons for the identified high importance of the PBL  
35 within the Decadal Survey. Accurate, high spatial and temporal resolution observations in the PBL of  
36 temperature and water vapor, referred to as thermodynamic profiles, are essential for improving  
37 weather forecasting (Crook et al., 1996, Dierer et al., 2009) and model re-analysis (Bengtsson et al,  
38 2004). Furthermore, these measurements are also important for understanding land-surface  
39 interactions and thus parameterizations of those processes and others in regional climate models  
40 (Warrach-Sagi et al., 2013, Kotlarski et al., 2014). Wulfmeyer et al., 2015 demonstrated that global  
41 scale measurements of thermodynamics profiles within the PBL would have a significant impact on  
42 our understanding of the Earth's systems. In response to the NAS findings in the Decadal Survey and  
43 in support of European Space Agency initiatives, Di Girolamo et al., 2018 (DiG2018) simulated the  
44 measurement capability of a spaceborne thermodynamics lidar utilizing a sun-synchronous  
45 dawn/dusk orbit. They studied the performance of lidar system using US Standard, Tropical, mid-  
46 latitude Winter and Summer atmospheres and considered attenuation by clouds. Here we use the  
47 NASA/GSFC GEOS model to provide a large number of cloud-free input profiles permitting a  
48 statistical analysis of the measurement capability of the thermodynamics lidar system, first studied in  
49 DiG2018, within the PBL.

50 The work reported here occurred during the period 2017-2018 under the auspices of the  
51 NASA/GSFC PBL Science Task Group. It is part of an on-going effort, led by the Universities of  
52 Basilicata and Hohenheim, focused on determining the utility of spaceborne thermodynamics lidar in  
53 improving short term weather forecasting and other predictive parameters. The goal of the overall  
54 activity is to use simulated thermodynamics lidar profiling as demonstrated here in Observation  
55 Systems Simulation Experiments (OSSE) to assess the impact of the spaceborne lidar system.

56 The paper is structured as follows. In part 2 we review the methods, pertinent equations and datasets  
57 used in the study. In part 3 we provide visual displays of the performance of the spaceborne lidar for  
58 measuring temperature, water vapor and aerosols under both day and night, cloud-free, conditions.  
59 Then a selection of profiles is made consistent with a dawn/dusk orbit. Using that orbit, the  
60 performance of the lidar system within the PBL is analyzed statistically. Part 4 concludes the paper  
61 with a discussion of the results here and looks toward the additional work involving OSSEs that fully  
62 considers the influence of clouds and is currently in progress.

63 **2 Methods and Techniques**

64 Raman lidar has been used for several decades for a wide variety of studies including that of water  
65 vapor profiling in the lower atmosphere (Melfi and Whiteman, 1985, Goldsmith et al., 1998,  
66 Whiteman, 2003 a,b), temperature profiling in the convective boundary layer (Behrendt et al., 2015),  
67 aerosol backscatter and extinction for studying aerosol hygroscopic growth (Ferrare et al., 1998a,  
68 1998b, Veselovskii et al., 2009). The lidar technique makes use of a laser transmitter, telescope  
69 receiver, wavelength selection optics and sophisticated data acquisition electronics to acquire profiles  
70 of atmospheric constituents with high temporal and spatial resolution and has been extensively  
71 discussed previously (e.g. Weitkamp, 2005). The Raman lidar makes use of an inelastic scattering  
72 process, first discovered by C. V. Raman and K. S. Krishnan in 1928 (Raman, 1928, Raman and

73 Krishnan, 1928), that exploits molecular vibrational or rotational transitions and spectroscopic  
 74 techniques in order to identify different atmospheric molecules such as water vapor, nitrogen,  
 75 oxygen, carbon dioxide, etc.

76 Much has been written previously about the use of Raman lidar for a wide variety of atmospheric  
 77 studies so we will refer readers to the references cited above for further background and the equations  
 78 that give the lidar signal as a function of range. For the purposes of the lidar simulations performed  
 79 here we will briefly detail the important equations to illustrate which quantities must be simulated in  
 80 order to assess the measurement performance of the lidar system. The Raman lidar as studied here  
 81 collects four lidar signals: the water vapor vibrational Raman signal,  $P_{H2O}(z)$ , two rotational Raman  
 82 signals from high- and low-quantum number transitions,  $P_{LoJ}(z)$  and  $P_{HiJ}(z)$ , and the direct backscatter  
 83 signal at  $\lambda_0$ ,  $P_{\lambda_0}(z)$ . The fundamental equations for the various  $P_X$  terms can be found in the  
 84 references listed below. One point to note is that the temperature dependence of Raman water vapor  
 85 scattering (Sherlock et al., 1999, Whiteman, 2003a,b) has not been accounted for in the  $P_X$  equations  
 86 used here since the focus was on determining random uncertainty budgets which are dominated by  
 87 the Poisson statistics relating to the measurement process and not by the primarily systematic effects  
 88 introduced by the temperature dependence. Correction techniques for these temperature dependent  
 89 effects are relatively straightforward and would need to be included in any real space mission but  
 90 excluding them here does not influence the results of the statistical analysis.

## 91 2.1 Calculation of temperature, water vapor mixing ratio, aerosol backscatter and extinction

92 The direct calculation of atmospheric temperature is obtained from the rotational Raman  
 93 backscattered signals through the expression (Behrendt and Reichardt, 2000):  
 94

$$95 \quad T(z) = \frac{\alpha}{\ln[Q(z) - \beta]} \quad (1)$$

96 where  $Q(z) = P_{HiJ}(z) / P_{LoJ}(z)$  and  $P_{LoJ}(z)$  and  $P_{HiJ}(z)$  are the low ( $LoJ$ ) and high ( $HiJ$ ) quantum  
 97 number rotational Raman backscatter signals at wavelengths  $\lambda_{LoJ}$  and  $\lambda_{HiJ}$ , respectively, received from  
 98 altitude  $z$  in the anti-Stokes branch of the rotational Raman spectrum, and  $\alpha$  and  $\beta$  are two calibration  
 99 constants. The spectral locations of  $\lambda_{LoJ}$  and  $\lambda_{HiJ}$  were identified through a sensitivity analysis that  
 100 accounted for various atmospheric and instrumental parameters such as the signal-to-background  
 101 ratio, the filter bandwidths and filter shapes, and the temperature range of interest. (Hammann and  
 102 Behrendt, 2015). For the present system  $\lambda_{LoJ}$  and  $\lambda_{HiJ}$  were identified with the purpose of optimizing  
 103 daytime measurement performances in the convective PBL and were found to be  $\lambda_{LoJ} = 354.36$  nm  
 104 and  $\lambda_{HiJ} = 353.29$  nm.  
 105

106 The direct calculation of the water vapor mixing ratio,  $w$ , is obtained from Raman backscattered  
 107 signals through the following equation (Whiteman et al., 1992)  
 108

$$109 \quad w_{H2O}(z) = K \Delta T(z) \frac{P_{H2O}(z)}{P_{ref}(z)} \quad (2)$$

110 where  $P_{H2O}(z)$  is the water vapor vibrational Raman lidar signal at wavelength  $\lambda_{H2O}$ , while  $P_{ref}(z)$  is a  
 111 nearly temperature-independent reference signal obtained through a linear combination of the two  
 112 temperature sensitive rotational Raman lidar signals  $P_{LoJ}(z)$  and  $P_{HiJ}(z)$  at the two nearby  
 113 wavelengths  $\lambda_{LoJ}$  and  $\lambda_{HiJ}$ ,  $K$  is a calibration constant (Whiteman et al., 1992, Whiteman, 2003b, Di  
 114 Girolamo et al, 2018),  $\Delta T(z)$  is the differential transmission term accounting for the different  
 115 atmospheric transmission by molecules and aerosols at  $\lambda_{H2O}$  and  $\lambda_{HiJ/LoJ}$ .

116 The vertical profile of the particle backscattering coefficient  $\beta_{\lambda_0}^{par}(z)$  at  $\lambda_0=354.7$  nm is  
 117 calculated from the ratio of the elastic backscatter signal  $P_{\lambda_0}(z)$  and the essentially temperature-  
 118 independent reference signal  $P_{ref}(z)$  through equation 3 (Ansmann et al., 1992):  
 119

$$120 \quad \beta_{\lambda_0}^{par}(z) = \beta_{\lambda_0}^{mol} \left[ \frac{P_{\lambda_0}(z)}{k P_{ref}(z)} - 1 \right] \quad (3)$$

121 where  $\beta_{\lambda_0}^{mol}$  is the backscattering coefficient at  $\lambda_0$  due to Rayleigh scattering from primarily oxygen  
 122 and nitrogen molecules, and  $k$  is a normalization term. The vertical profile of the particle extinction  
 123  $\alpha_{\lambda_0}^{par}(z)$  can be obtained from  $P_{ref}(z)$  through a modified form (Di Girolamo et al., 2006) of the  
 124 equation defined by Ansmann et al.(1990)  
 125

$$126 \quad \alpha_{\lambda_0}^{par}(z) = \frac{1}{2} \frac{d}{dz} \ln \left[ \frac{n(z)}{P_{ref}(z) z^2} \right] - \alpha_{\lambda_0}^{mol}(z) \quad (4)$$

127 where  $\alpha_{\lambda_0}^{mol}(z)$  is the molecular extinction coefficient at  $\lambda_0$  and  $n(z)$  represents the ambient gas  
 128 number density.

129 Thus, the simulation of the performance of the candidate Raman lidar is accomplished by  
 130 numerically evaluating the equations above, along with their corresponding uncertainty equations, to  
 131 generate synthetic signals due to backscattered radiation at the laser wavelength (354.7 nm),  
 132 vibrational Raman scattering from water vapor (407.5 nm), rotational Raman scattering from HiJ  
 133 (353.29 nm) and LoJ (354.36 nm) channels. The methods used to simulate these signals will now be  
 134 discussed.

## 135 2.2 Raman Water vapor Lidar model and previous use, comparison with Di Girolamo et al.

136 The Raman lidar simulator that was used here has been used extensively for simulations of lidar  
 137 measurements of water vapor from both airborne (Whiteman et al., 2001) and ground-based  
 138 (Whiteman et al., 2010) platforms and is an implementation of the lidar equation, (Measures, 1984)  
 139 that carries physical units through the entire simulation chain including for background skylight. The  
 140 model was also recently upgraded to perform simulations of spaceborne measurements of aerosol  
 141 backscatter and extinction (Whiteman et al., 2018). To support the studies here, that model was  
 142 extended further to include simulations of lidar signals from rotational Raman scattering. Prior to the  
 143 work described here, comparisons were made between the water vapor and temperature profile  
 144 simulations of this revised model and those in DiG2018 and excellent agreement between the models  
 145 was found.

146 DiG2018 used four standard atmospheres (US Standard-1976, Tropical, Mid-Latitude Summer and  
 147 Mid-Latitude Winter) to perform their study of spaceborne thermodynamics lidar performance. Here  
 148 we make use of a 24-hour orbit simulation performed by the NASA/GSFC GEOS model (Rienecker  
 149 et al., 2008) to provide a large number of simulated lidar profiles under a range of geographic and  
 150 climate conditions.

## 151 2.3 GEOS dataset and 3+2 simulations

152 The atmospheric profiles of water vapor, temperature, aerosols and atmospheric density that were  
 153 used as input to the lidar simulator were provided by the NASA/GSFC GEOS model (Rienecker et  
 154 al. 2008) for a 24-hr orbit of the CALIPSO platform on July 15, 2009. A 10-sec temporal resolution  
 155 was used in the simulations resulting in 8640 profiles with horizontal resolution of approximately 80  
 156 km. This is the same simulation dataset that was used in Whiteman et al., 2018 for simulating

157 spaceborne measurements of aerosol backscatter and extinction. Skylight irradiance values are  
 158 provided along with the GEOS simulations by the VLIDORT (Vector LInearized Discrete Ordinate  
 159 Radiative Transfer) radiative transfer model (Spurr, 2006).

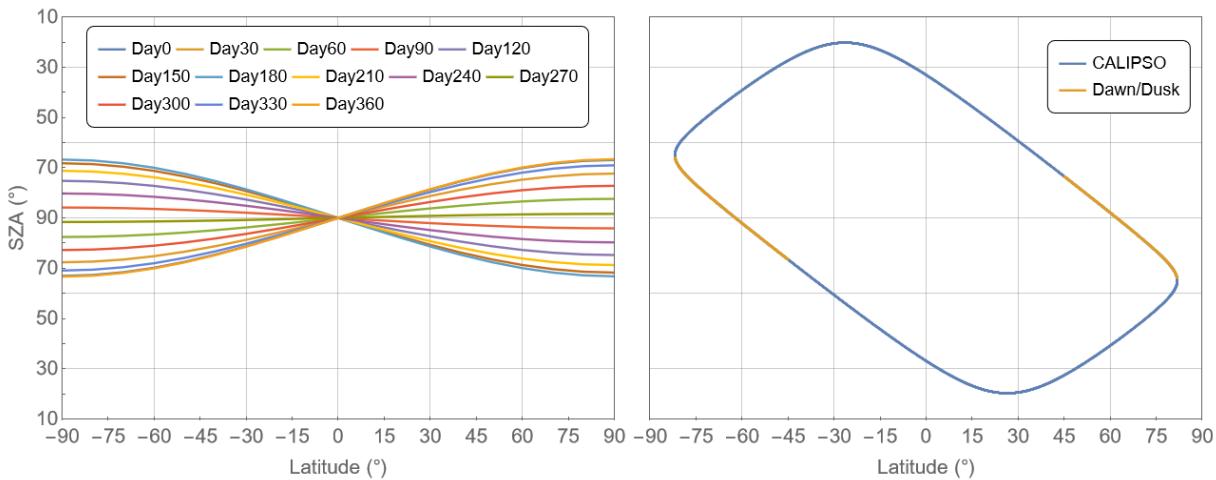
160 **2.4 Thermodynamics spaceborne lidar specifications**

161 The spaceborne platform that is simulated here is the same as studied in DiG2018. It consists of a 4m  
 162 diameter telescope, 100 Hz laser with 2.5 J per pulse @ 354.7 nm. The optical receiver uses a field of  
 163 view of 25  $\mu$ rad and collects and processes signals from water vapor Raman backscatter (407.5 nm),  
 164 Rayleigh-Mie backscatter (354.7 nm), H<sub>2</sub>J and L<sub>2</sub>J rotational Raman backscatter (353.29, 354.36 nm,  
 165 respectively). The orbit considered has an altitude of 450 km and is sun-synchronous such that the  
 166 solar zenith angle (SZA) always exceeds 65°. This orbit was selected to avoid the high solar  
 167 background associated with brighter parts of the day. DiG2018 studied 4 standard atmosphere  
 168 scenarios and concluded that the candidate thermodynamics lidar system is able to perform day- and  
 169 night-time atmospheric water vapor mixing ratio and temperature measurements in cloud-free  
 170 conditions with an accuracy fulfilling observational requirements for NWP. Many more details of the  
 171 spaceborne lidar are contained in DiG2018, to which the authors refer the reader, and thus will not be  
 172 repeated here.

173 Here we extend the work of DiG2018 by considering a 24-hr simulation of atmospheric profiles  
 174 along the CALIPSO orbit of July 15, 2009 provided by the NASA/GSFC GEOS model. Only clear  
 175 sky scenarios are considered here. DiG2018 considered the influence of clouds and found that NWP  
 176 and climate research observational requirements can be met above and below thin cirrus clouds with  
 177 optical depths of 0.3. The more detailed OSSE work currently being performed will consider the full  
 178 influence of clouds on forecast improvement.

179 **2.4.1 Orbit and skylight considerations, selection from the GEOS dataset**

180 As mentioned above, a dawn/dusk orbit for which the solar zenith angle is always greater than 65°  
 181 was simulated in DiG2018. The range of SZA experienced during the dawn/dusk orbit varies by time  
 182 of the year and by latitude as can be seen on the left side of Figure 1 which is reproduced from  
 183 DiG2018. The CALIPSO platform follows the A-train orbit and thus covers SZAs that are as small as  
 184 ~20°. To assess the performance of the thermodynamics lidar for a dawn/dusk orbit, therefore, a  
 185 selection from the full 24-hr CALIPSO simulation that is consistent with the dawn/dusk orbits was  
 186 performed. That selection is shown on the right side of Figure 1 with the selected {latitude, SZA}  
 187 pairs being shown in yellow. This selection yielded 2117 profiles out of the total 8640 profiles  
 188 contained in the 24-hr CALIPSO orbit simulation and resulted in latitudes between  $\pm 45.0$ -81.8  
 189 degrees being included in the study here. Note that this sampling of the CALIPSO orbit excludes the  
 190 elevated water vapor mixing ratio conditions that characterize the PBL in the lower latitudes. The  
 191 effect of this selection will be discussed later. These 2117 profiles were used as input to the lidar  
 192 simulator in order to perform a statistical study of the uncertainties in the measurements of water  
 193 vapor, temperature, aerosol backscatter and extinction within the PBL.



194

195 **Figure 1 (Left)** Solar zenith angle as a function of latitude and Julian day of the year for the dawn/dusk  
 196 orbit envisioned for the thermodynamics lidar. **(Right)** SZA vs latitude for the CALIPSO orbit of July  
 197 15, 2009 (blue and orange) with the selection of the portion of the orbit characterized by SZA values  
 198 corresponding to the dawn/dusk orbit shown (orange).

199 **2.5 Performance Metrics**

200 To assess the performance of the simulated thermodynamics lidar system, measurement metrics were  
 201 established by considering the WMO Observing Systems Capability Analysis and Review (WMO  
 202 OSCAR, 2021) requirements for Global NWP and are listed in Table 1. OSCAR is the official  
 203 repository of requirements for observation of physical variables in support of World Meteorological  
 204 Programs. In the OSCAR database of atmospheric parameters, different measurement requirements  
 205 are identified as "threshold", "goal", or "breakthrough" where "threshold" specifies the minimum  
 206 requirement to be met to ensure that data are useful. As described in the OSCAR documentation,  
 207 the "goal" is an ideal requirement above which further improvements are not necessary.  
 208 The "breakthrough" is an intermediate level between "threshold" and "goal" which, if achieved,  
 209 would result in a significant improvement for the targeted application. The breakthrough level may  
 210 be considered as optimum, from a cost-benefit point of view, when planning or designing observing  
 211 systems (WMO OSCAR, 2021). For characterizing the performance of the spaceborne  
 212 thermodynamics lidar measurements of temperature and water vapor (specific humidity), we will  
 213 consider the OSCAR "breakthrough" requirements for global Numerical Weather Prediction (NWP)  
 214 which are listed in Table 1. The OSCAR requirements for measurements of aerosol backscatter and  
 215 extinction are not well defined so we will consider metrics for those quantities that are similar to  
 216 spatial and temporal resolution of airborne measurements of aerosol backscatter and extinction  
 217 (Whiteman et al., 2010). The 2117 profiles that are consistent with a dawn/dusk orbit will be assessed  
 218 for their measurement performance based on the metrics specified in Table 1. Prior to presenting that  
 219 statistical analysis, however, a visual illustration of simulated lidar performance within the PBL will  
 220 be presented next.

221

Table 1. OSCAR Measurement Metrics

Parameter	Horizontal Resolution	Vertical Resolution	Random Uncertainty
Temperature (K)	100 km	1000 m	1K

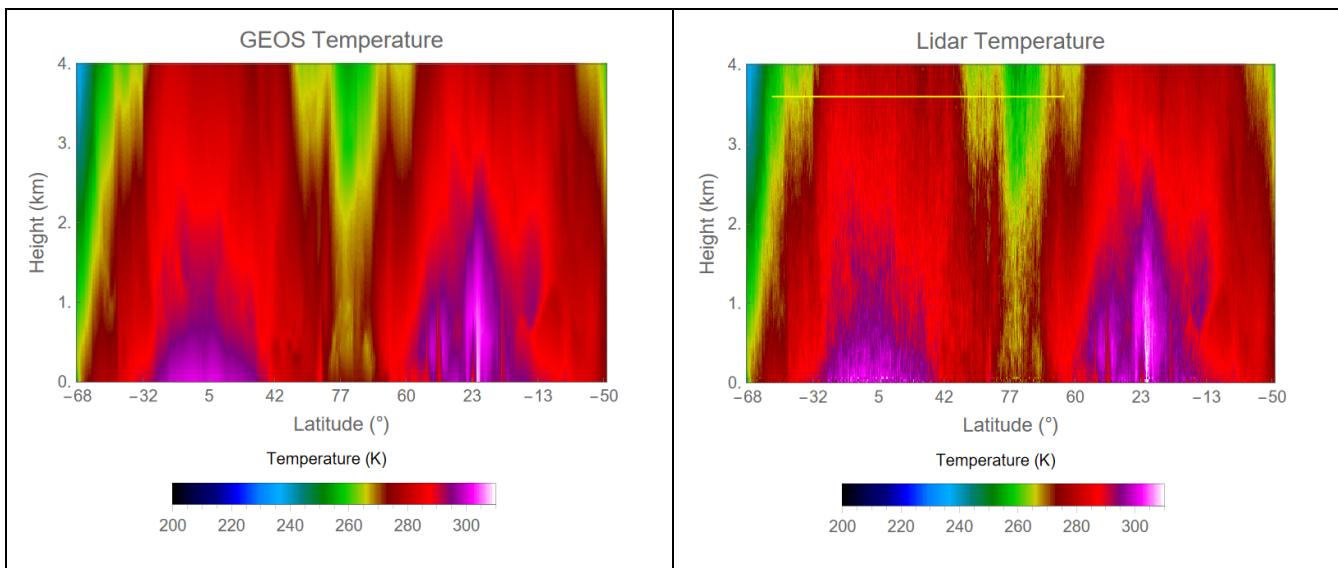
Specific Humidity (g/kg)	50 km	1000 m	5 %
Aerosol Backscatter Coefficient ( $\text{km}^{-1} \text{ sr}^{-1}$ )	50 km	30 m	5%
Aerosol Extinction ( $\text{km}^{-1}$ )	80 km	250m	20%

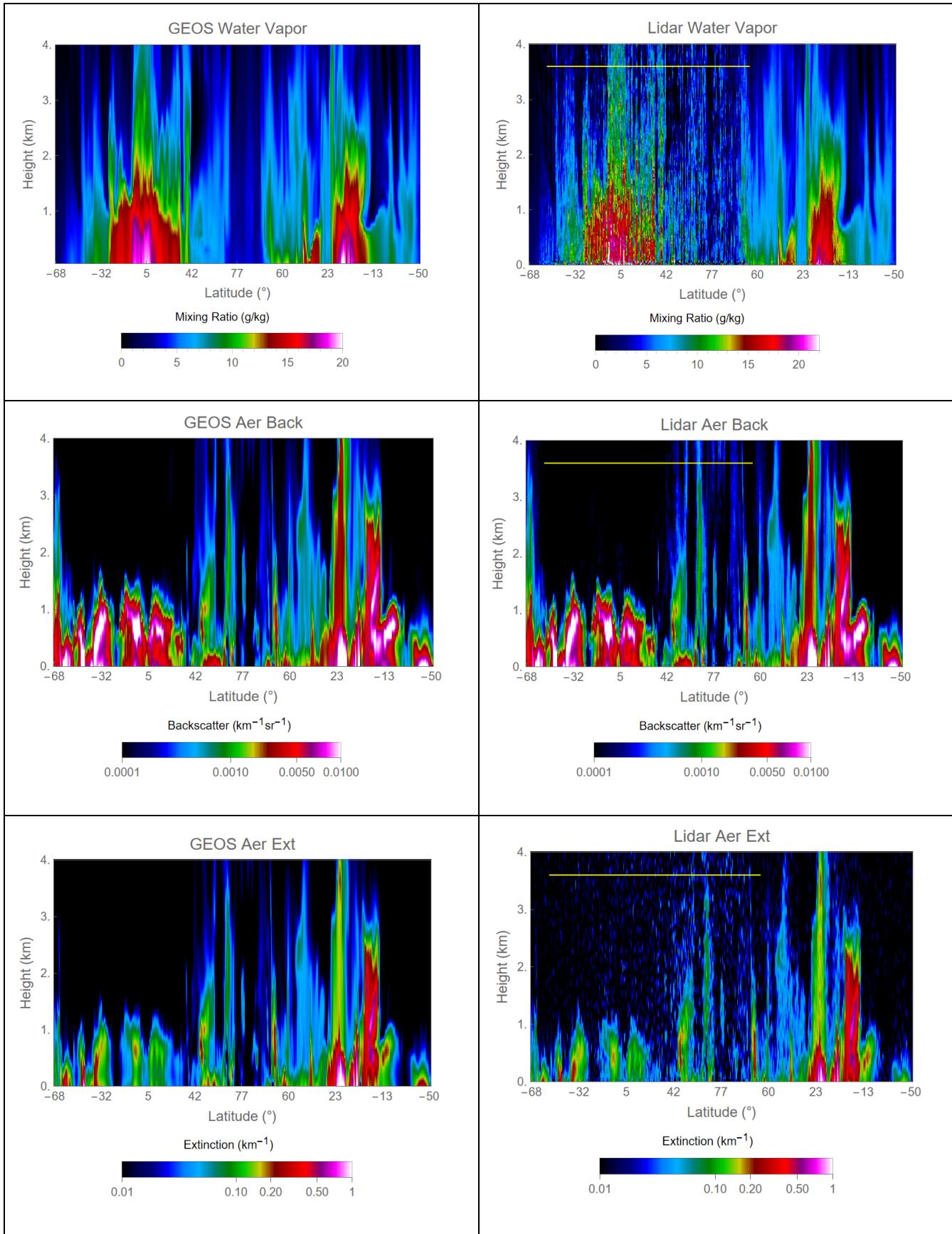
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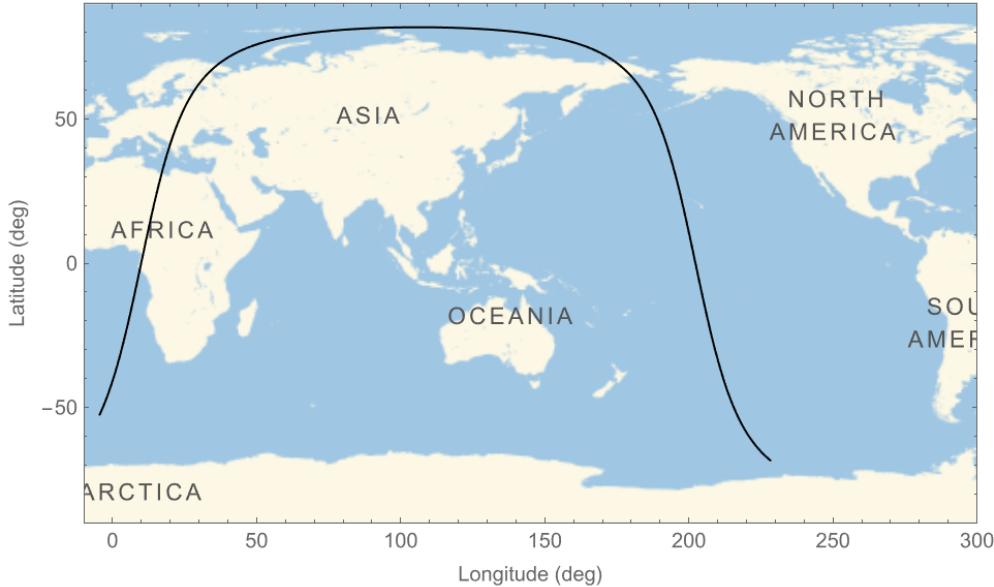
### 3 Results

224 To give a visual impression of what the measurements of the thermodynamics lidar system studied  
 225 here would be like for the full CALISO orbit, Figure 2 presents comparisons of approximately 1.25  
 226 hours (out of the full 24-hour orbit) of the GEOS input and lidar simulations of temperature, water  
 227 vapor, aerosol backscatter and aerosol extinction under cloud-free conditions. On the left side of  
 228 Figure 2 is shown the GEOS model inputs for temperature, water vapor mixing ratio, aerosol  
 229 backscatter and extinction. On the right side of the figure are shown the corresponding lidar  
 230 simulations. The orbit path that was simulated by the GEOS model is shown in Figure 3. The general  
 231 fidelity of all measurements is evident from these visual displays with the comparisons of  
 232 temperature and aerosol backscatter being the most impressive. There is, however, significant  
 233 degradation in the water vapor measurements during full. The portion of the dataset with the sun  
 234 above the local horizon is shown with a yellow line in the upper left of the lidar simulations.  
 235 Degradation in the water vapor measurement capability during the daytime is the main motivator for  
 236 the dawn/dusk orbit that was selected for the thermodynamics lidar analyzed here.





237 **Figure 2** Comparison of GEOS input and lidar simulations for approximately 1.25 hours of the 24  
 238 hour CALIPSO orbit. The plots extend to an altitude of 4 km consistent with the focus on lidar  
 239 performance within the PBL. The portion of the image where the sun is above the horizon is shown  
 240 with a yellow line in the upper left of the lidar images. See text for further details.



**Figure 3** Orbital path of the GEOS and lidar simulations shown in Figure 2.

### 241 3.1 Selection from the full CALIPSO orbit

242 Now we consider example profiles from the population selected according to the dawn/dusk criteria  
 243 illustrated in Figure 1 which will be used to quantify the performance of the thermodynamics lidar  
 244 according to the performance metrics shown in Table 1. Figure 4 presents the temperature, water  
 245 vapor mixing ratio, aerosol backscatter and extinction profiles for a location over south-central  
 246 Russia when the solar zenith angle was approximately 96 degrees. Both GEOS input and lidar  
 247 simulated profiles are shown. All lidar simulations use a 10-s average. The lidar simulated  
 248 temperature and water vapor profiles (top of Figure 4) are both presented with their base resolution of  
 249 30 m vertical resolution as well as averaged to 1000 m as needed for the statistical assessment based  
 250 on the OSCAR performance metrics shown in Table 1. The simulated lidar aerosol backscatter and  
 251 extinction profiles (bottom) are displayed with the 30 m and 250 m vertical resolutions, respectively,  
 252 that are indicated in Table 1. The lidar simulations represent well the GEOS inputs although the  
 253 random fluctuations due to both skylight background and counting statistics are evident. We will now  
 254 study the statistics of the 4 quantities shown in Figure 4 using the selected population that  
 255 approximates the dawn/dusk orbit shown in Figure 1.

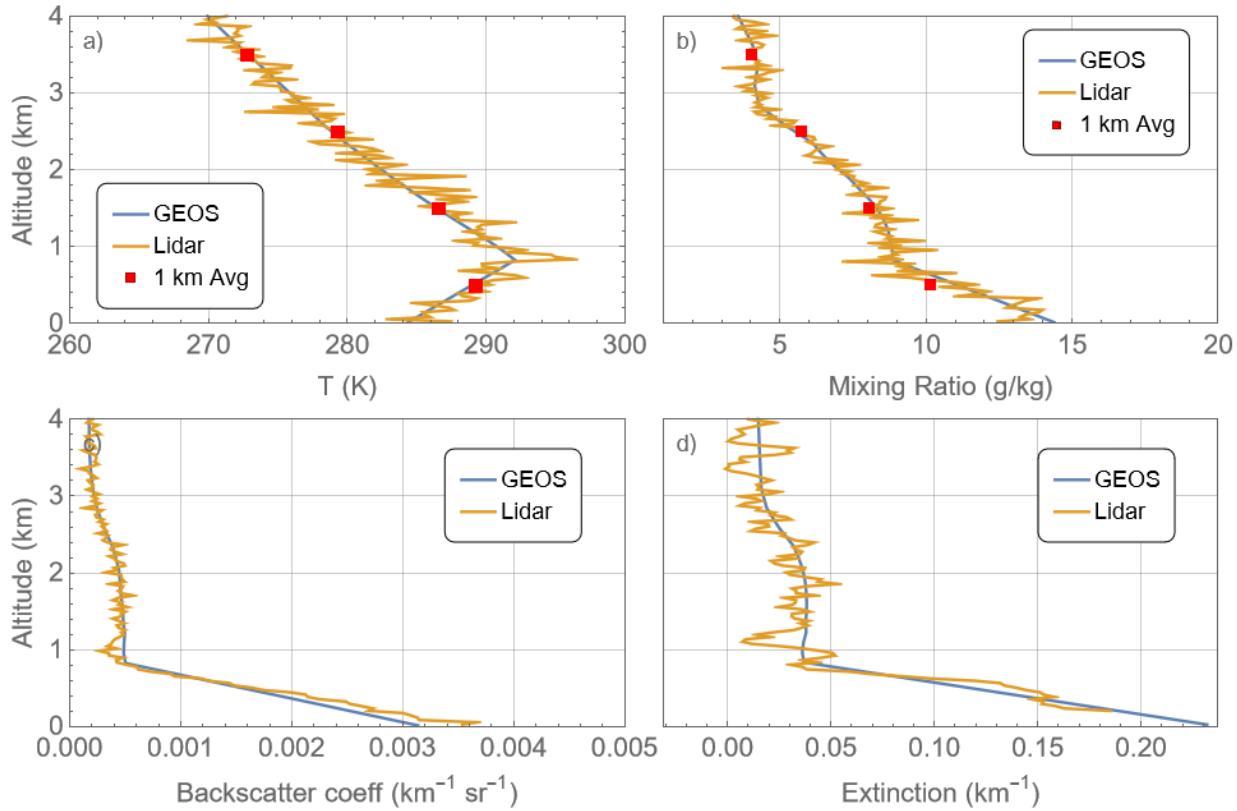


Figure 4 Temperature (a), water vapor (b), aerosol backscatter (c) and aerosol extinction (d) profile comparisons of GEOS inputs and lidar simulation. The temperature and water vapor profiles are displayed both at base resolution (30m, 80 km) and averaged to 1000 m per the OSCAR breakthrough metrics shown in Table 1. The aerosol backscatter and extinction profiles are displayed with the 30 m and 250 m vertical resolutions, respectively, that are indicated in Table 1.

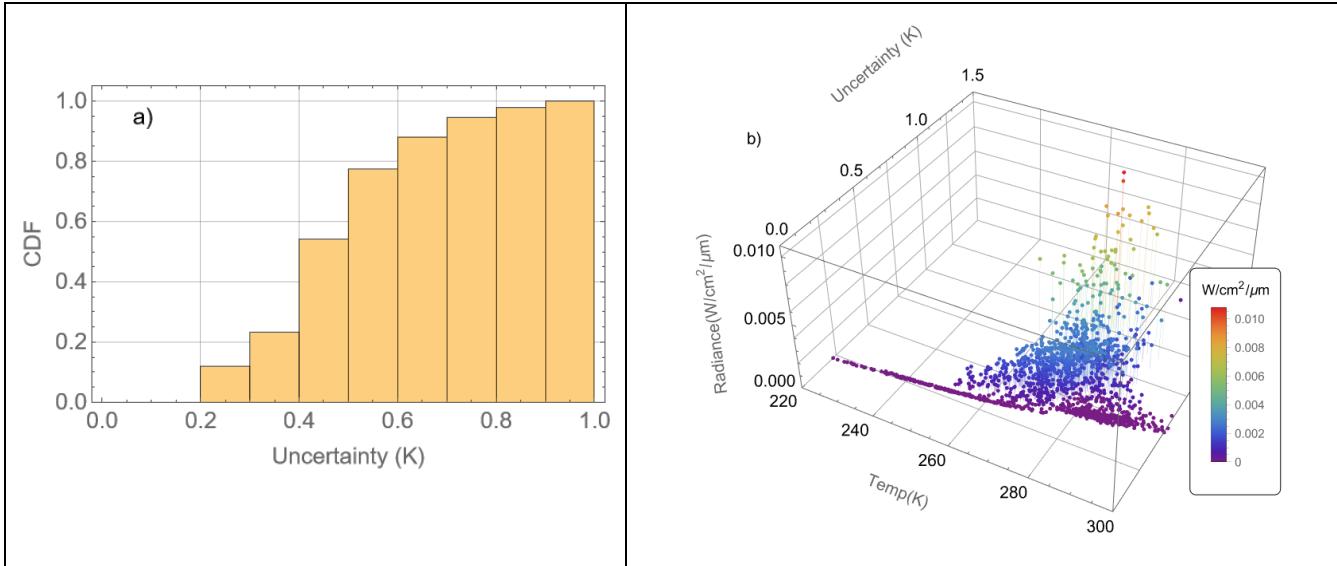
### 3.2 Temperature Statistics

Figure 5 presents the analysis of temperature uncertainty statistics using the uncertainty formulation shown in equation 5 (Behrendt and Reichardt, 2000, Di Girolamo et al., 2004).

$$\Delta T(z) = \frac{\partial T(z)}{\partial Q} Q(z) \sqrt{\frac{P_{LoJ}(z) + bk_{LoJ}}{P_{LoJ}^2(z)} + \frac{P_{HiJ}(z) + bk_{HiJ}}{P_{HiJ}^2(z)}} \quad (5)$$

where all terms have been previously defined except  $bk_{LoJ, HiJ}$  which represent the signal in the  $LoJ$  and  $HiJ$  rotational Raman channels due to sky brightness and are constant as a function of range. Recall that the OSCAR breakthrough requirement from Table 1 was 1K temperature uncertainty for measurements with 100 km horizontal and 1000 m vertical resolution. Using those averaging parameters, Figure 5a presents the cumulative distribution function of temperature uncertainty for all the measurements within the PBL as identified by the GEOS model for the selected dawn/dusk profiles. Essentially 100% of the selected measurements have uncertainties less than 1K. Figure 5b presents the dependence of those uncertainties on both temperature and sky radiance. Under low radiance conditions (purple-colored points), the relationship of temperature and uncertainty displays a square root relationship consistent with the Poisson statistics that govern the counting process for these measurements. The presence of higher background radiance, which is related to higher solar

277 elevation angles, increases the values of the  $bk_{LoJ, HiJ}$  terms in equation 5 and thus the total  
 278 uncertainty of the temperature measurements.



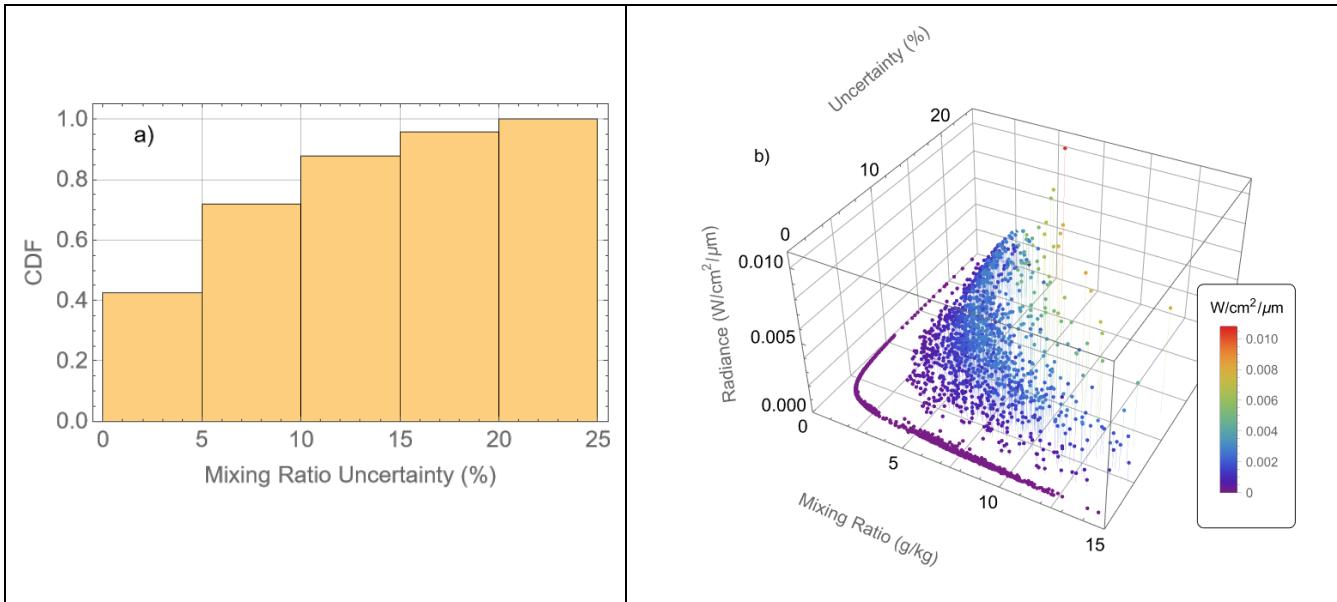
279 **Figure 5 (a) Cumulative Distribution Function for the PBL temperature uncertainty, (b) temperature**  
 280 **uncertainty as a function of background radiance.**

281 **3.3 Water Vapor Statistics**

282 Figure 6 presents an analysis of the mixing ratio uncertainty for the measurements selected that are  
 283 consistent with a dawn/dusk orbit and that occurred within the PBL as identified by the GEOS  
 284 model. The formulation for the water vapor mixing ratio uncertainty (Whiteman, 2003a,b, DiG2018)  
 285 that will be used is given in equation 6

$$286 \frac{\Delta w_{H_2O}(z)}{w_{H_2O}(z)} = 100 \times \sqrt{\frac{P_{H_2O}(z) + bk_{H_2O}}{P_{H_2O}^2(z)} + \frac{P_{ref}(z) + bk_{ref}}{P_{ref}^2(z)}} \quad (6)$$

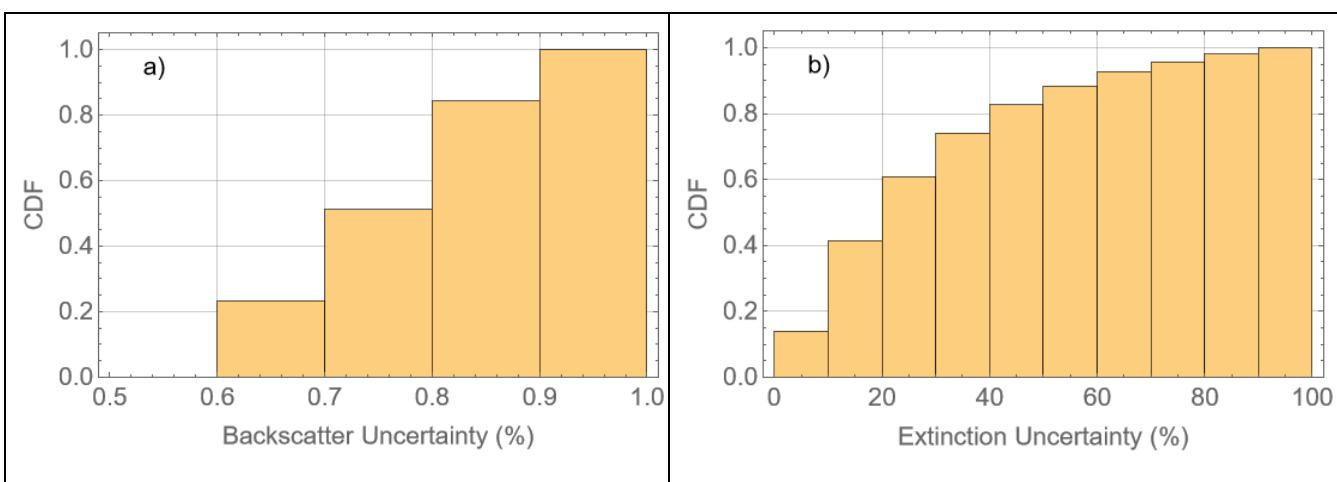
287 Considering the OSCAR threshold requirements of 1000 m vertical resolution and 50 km horizontal  
 288 resolution, Figure 6a indicates that 42% of the measurements meet the OSCAR requirement of 5%  
 289 uncertainty, while 72% of the measurements have random uncertainty less than 10% and essentially  
 290 all of the selected measurements have uncertainties less than 25%. These results are for a selection of  
 291 cases restricted to the latitude range of 45.0-81.8 degrees, as mentioned previously. Figure 6b  
 292 illustrates the effect of higher background radiance levels on the mixing ratio measurements. There is  
 293 a consistent increase in the uncertainty of the measurement when either the mixing ratio decreases or  
 294 the radiance value increases as expected from equation 6. As in the discussion relating to equation 5,  
 295 sun positions increasingly above the horizon are the main contributors to increasing background  
 296 radiance values.



297 **Figure 6 (a) Cumulative Distribution Function for the PBL water vapor mixing ratio simulations. (b)**  
 298 **water vapor mixing ratio uncertainty as a function of background radiance**

299 **3.4 Aerosol Backscatter and Extinction Statistics**

300 The equations used to assess the uncertainty of aerosol backscatter and extinction may be found in  
 301 DiG2018 and are not repeated here. Figure 7 presents the cumulative probability distributions for  
 302 uncertainties in aerosol backscatter (a) and aerosol extinction (b) using the set of 2117 selected  
 303 profiles. The results indicate that, using the performance metrics listed in Table 1 of 50 km  
 304 horizontal and 30m vertical resolution, the aerosol backscatter uncertainties always remain less than  
 305 1% easily exceeding the performance metric of 5%. This result is statistical confirmation of the high  
 306 fidelity simulations shown in Figure 2. Using the corresponding metrics for aerosol extinction of 80  
 307 km horizontal and 250m vertical resolution, 42% of the measurements are performed with  
 308 uncertainties of 20% or less.



309 **Figure 7 Cumulative Distribution Function for the uncertainty in PBL aerosol backscatter coefficient**  
 310 **(a) and aerosol extinction (b) simulations.**

311 **4 Discussion**

312 The performance of a spaceborne thermodynamics Raman lidar for measuring temperature, water  
 313 vapor and aerosols is studied here using a set of metrics derived from the OSCAR database, for  
 314 temperature and water vapor, as well as previous lidar performance metrics for aerosol backscatter  
 315 and extinction. We use a selected set of profiles within the PBL from a simulated CALIPSO orbit  
 316 performed by the NASA/GSFC GEOS model. The selection resulted in measurement simulations  
 317 with solar zenith angles of 65 degrees or greater being included thus making the sky background  
 318 conditions consistent with the assumed dawn/dusk orbit of the thermodynamics orbit. However, as  
 319 noted earlier, this selection of profiles included only latitudes between 45-81.8 degrees thus  
 320 systematically excluding the moist tropical and sub-tropical boundary layer environments. Note,  
 321 though, that the full range of longitudes is included in the selection. The proper simulation of the  
 322 thermodynamics lidar for a dawn/dusk orbit is in progress thus we only estimate here the influence of  
 323 this mid-high latitude selection bias on the statistical performance of the lidar system.

324 To first order, we assume that the mid-high latitude selection bias has no effect on the temperature  
 325 statistics since a wide range of temperatures is included in the selected profiles. We speculate that  
 326 there is likely a small effect on the aerosol backscatter and extinction statistics due to the mid-high  
 327 latitude selection. Some of the most polluted regimes are systematically excluded due to the current  
 328 selection and these areas might be measured with improved statistics. We do not consider this effect  
 329 to be large, however, thus we speculate that 50% or more of the extinction measurements could be  
 330 made with uncertainties of less than 20% if the full set of latitudes had been included. The aerosol  
 331 backscatter statistics will likely improve as well. However, they already well exceed the  
 332 measurement metrics shown in Table 1 indicating that the thermodynamics lidar studied here will be  
 333 sensitive to even very light aerosol scattering globally.

334 The measurement parameter that is most affected by the mid-high latitude bias is certainly water  
 335 vapor mixing ratio. The mean mixing ratio of the selected cases is less than 5 g/kg and only 5% of  
 336 the selected cases have mixing ratios that exceed 10 g/kg while in the tropics mixing ratios in the  
 337 boundary layer can exceed 20 g/kg. The water vapor signal received by the lidar is directly  
 338 proportional to the water vapor concentration thus one can expect that measurements in the tropics  
 339 could result in signals on average 3-4 times larger than the mean signals studied here. Equation 6  
 340 shows the square root relationship of the overall uncertainty and the  $P_{H_2O}$  term complicated by the  
 341 presence of the background in the water vapor channel,  $bk_{H_2O}$ . Thus, one cannot simply assume that  
 342 the statistical performance will be increased under tropical conditions by  $\sqrt{3}$  or  $\sqrt{4}$  over the statistics  
 343 shown here. Such an assessment is in progress with the proper dawn/dusk orbit. For now, we  
 344 conservatively estimate that more than 50% of the water vapor cases, perhaps much more, will meet  
 345 the OSCAR performance metrics shown in Table 1.

346 Summarizing the performance of the thermodynamics lidar with respect to the performance metrics  
 347 shown in Table 1 after considering the influence of the mid-high latitude bias in the case selection,  
 348 we find that for the cloud-free conditions within the planetary boundary layer considered here:

- 349 1. Temperature: 100% the measurements will be sampled with uncertainties of less than 1K
- 350 2. Water vapor mixing ratio: we estimate that more than 50% of the measurements, perhaps  
 351 much more, will possess uncertainties less than 5% and that more than 80% of the  
 352 measurements will possess uncertainties of less than 10%
- 353 3. Aerosol backscatter coefficient: 100% of the measurements will possess uncertainties less  
 354 than 1% easily exceeding the performance metric of 5% uncertainty for this parameter

355        4. Aerosol extinction coefficient: we estimate that more than 50% of the measurements will  
 356        possess random uncertainties of less than 20%

357        As already stated, the rigorous assessment of the uncertainties of the thermodynamics for a full  
 358        dawn/dusk orbit including the effects of clouds is in progress. However, the very positive  
 359        performance metrics demonstrated here by the thermodynamics lidar system indicates that having  
 360        such measurements on a global scale could strongly impact models used for weather forecasting,  
 361        calibration of space-borne passive remote sensing systems and for convective scale data assimilation  
 362        studies. Improvement in these areas implies that the thermodynamics lidar could thus greatly increase  
 363        our understanding of and ability to predict the Earth's water and energy cycles.

364        **5      Author Contributions**

365        DW was the first author and performed the numerical simulations of the thermodynamics lidar as  
 366        well as the analysis of its statistical performance. PDG and NF performed simulations of profiles to  
 367        compare with those generated by the model of DW in order to check and validate both models. AB  
 368        consulted in all areas of the effort but particularly in the area of temperature profile measurements by  
 369        lidar. VW consulted in all areas of the effort but particularly in the application of the measurements  
 370        to global studies.

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378        **8      References**

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465 **9 Data Availability Statement**

466 Upon final submission the data and code used to create all the figures will be provided as  
467 supplementary material.