

High Order Ab Initio Valence Force Field with Chemical Pattern Based Parameter Assignment

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Abstract

Bonded (or valence) interactions, which directly determine the local structures of the molecules, are fundamental parts of molecular mechanics force fields (FFs). Most popular classical FFs adopt the simple harmonic models for bond stretching and angle bending and ignore cross-coupling effects among the valence terms. This may lead to less accurate vibrational properties and configurations in molecular dynamics (MD) simulations. AMOEBA models utilize an MM3(MM4)-style bonded interaction model, in which the vibrational anharmonicity, the coupling effects among different energy terms, and the out-of-plane bending for sp^2 -hybridized atoms are considered. In this work, we report the development of bonded interaction parameters for a wide range of chemistry based on quantum mechanics (QM). About 270 atomic types defined by SMARTS strings were used to model the valence interactions. Our results indicate that the resulting valence parameters produce accurate vibrational frequencies (RMSD from QM is less than $\sim 36.6\text{ cm}^{-1}$) over a large set of molecules with diverse functional groups (445 molecules). By contrast, the harmonic models usually give an RMS error greater than 60 cm^{-1} . Meanwhile, this model accurately reflects the potential energy surface of the out-of-plane bending. Our model can generally be applied to the AMOEBA family and any MM3(MM4)-based molecular mechanics FFs.

KEYWORDS: AMOEBA potential, Force field, Bonded interactions, Normal mode frequencies

1. Introduction

Classical molecular dynamics (MD) simulations are widely applied by researchers to investigate various biomolecular systems. One of the essential elements determining the reliability of MD simulations is the underlying classical potentials, or force fields (FFs)¹⁻³, which describe the intra- and intermolecular interactions using empirical functional forms. Abundant studies focus on improving modeling the intermolecular (non-bonded) interactions as they are responsible for thermodynamic properties in protein-ligand binding⁴⁻⁷, protein folding⁸, enzymatic catalysis⁹, and other critical biomolecular processes. Nonetheless, bonded interactions are equally important as they determine the local structural ensemble sampled during the MD simulations.¹⁰

Most popular FFs, such as AMBER¹¹⁻¹⁴, OPLS¹⁵⁻¹⁷, and CHARMM¹⁸⁻²⁰, adopt simple harmonic functions to describe bond stretching and angle bending without considering the anharmonic nature of bonds and angles. AMBER omits cross-coupling effects between bond and angle terms, and it uses the Fourier style to describe out-of-plane effects. OPLS uses a similar functional form to AMBER. CHARMM employs a unique improper potential to represent the out-of-plane bending and a Urey-Bradley potential to account for the cross-coupling. Those methods are computationally efficient, but their accuracy is limited in complex molecular structures, especially in vibrational analysis. By contrast, AMOEBA-based models²¹⁻²³ use the sophisticated MM3(MM4)-style²⁴⁻²⁵ functional forms to describe these bonded interactions, in which the anharmonicity, cross-coupling effects, and out-of-plane bending (opbend) have been included. First, higher-order polynomial terms were added to the bond stretching and angle bending terms to capture the anharmonicity while avoiding abnormal effects on strained bonds or angles due to the negative contributions from odd polynomial terms. Second, the cross-coupling terms were proven to be essential for capturing the coupling effects and improving the vibrational frequencies. For example, it is evidenced that the combination of a high-order polynomial model and cross-terms can greatly enhance the description of equilibrium structure and vibrational frequencies of formate ion.²⁶⁻²⁷ Specifically, the average absolute deviation of vibrational frequencies ($|\Delta\nu|_{ave}$) plunges from 155.6 cm⁻¹ by the simple

harmonic model without any cross terms to 7.2 cm⁻¹ by a quartic model with third-order cross terms. Similar improvements have been found on systems including amides, peptides, and others.²⁸⁻²⁹ Finally, the out-of-plane bending (opbend)³⁰ is a necessary and important energy term to maintain planar structure around trigonal centers as a significant pyramidalization can form without seriously distorting any of the three angles of bonds involved.

MM3/MM4 parameters were derived almost three decades ago. Quantum mechanics (QM) calculations have significantly improved over the years, with energy, structures, vibrational frequencies closely matching experimental measurements. In addition, a more comprehensive range of coverage in chemical space is needed, and better ways for parameter assignment and typing (e.g., chemical pattern based) are readily available. This work aims to provide an up-to-date database of valence parameters for common organic molecules using atomic types determined by SMARTS strings. These parameters will be used for AMOEBA²¹ and AMOEBA+²² FFs but are also compatible with other classical FFs that use MM3/MM4 style valence terms. We have developed an automated Python program that implements the Modified Seminario method³¹ to generate bond and angle parameters from ab initio Hessian matrices. In addition, a reversed searching with the ranking tree was implemented inside this program to assign valence parameters for new molecules based on SMARTS patterns. Moreover, the anharmonicity, coupling effects, and out-of-plane bending have been analyzed on a large set of diverse molecules. The database of parameters will allow us to parameterize and simulate new biological and synthetic molecules, such as ligands and drug compounds by using AMOEBA and AMOEBA+ FFs.

2. Methodologies

2.1 Theoretical background

The bonded interactions of AMOEBA²¹ and AMOEBA+²²⁻²³ include five components: bond stretching, angle bending, out-of-plane bending (opbend), torsion, and cross-coupling terms for bond/angle/torsion, as shown in **Equation 1**.

$$E_{bonded} = E_{stretch} + E_{bend} + E_{torsion} + E_{opbend} + E_{cross} \quad (1)$$

This study focuses on bond stretching, angle bending, stretch-bend coupling, and opbend terms, which are the standard contributing elements to the total potential energy shared by almost all the molecules. The torsional energy involving four atoms in connection is usually coupled with other interactions such as electrostatics, van der Waals and polarization. The torsion term and related cross-coupling terms are treated as a residual correction to match the ab initio quantum mechanics reference energy after all the other terms of AMOEBA(+), including non-bonded terms are determined.

As mentioned above, the AMOEBA valence terms have been mostly inherited from MM3/MM4 model.²⁴⁻²⁵ The advantage of using the higher-order polynomials is that the energy variation within a wider range of geometry changes can be accurately captured. Bond stretching term adopts the quartic form (Equation 2), which can generate reliable energy for bond variation in the range of ± 0.3 Å from the equilibrium structure. Also, the sextet bending model is utilized, which can reliably reproduce ab initio energy for the angle variation in the range of $\pm 70^\circ$ and beyond.³² The out-of-plane bending (opbend) term is used to keep the planar structures for *sp*² atoms at and around the trigonal centers such as the amide group. Without the out-of-plane or improper torsion term used by some force fields, large pyramidalization may occur during the MD simulations without seriously distorting the bond lengths and angles. In AMOEBA, the opbend term (Equation (4)) shares a similar functional form to the angle bending term. The χ is defined as the bending angle between the plane and the central atom (**Figure 1**), which means each out-of-plane structure has three components contributed by each peripheral atom.

$$E_{stretch} = k_b \Delta r^2 \left[1 - 2.55 \Delta r + \frac{7}{12} \times 2.55^2 \Delta r^2 \right] \quad (2)$$

$$E_{bend} = k_a \Delta \theta^2 [1 - 0.014 \Delta \theta + 5.6(10)^{-5} \Delta \theta^2 - 7.0(10)^{-7} \Delta \theta^3 + 2.2(10)^{-8} \Delta \theta^4] \quad (3)$$

$$E_{oop} = k_{opbend} \Delta \chi^2 [1 - 0.014 \Delta \chi + 5.6(10)^{-5} \Delta \chi^2 - 7.0(10)^{-7} \Delta \chi^3 + 2.2(10)^{-8} \Delta \chi^4] \quad (4)$$

Here $\Delta r = r - r_0$ is the difference between the real bond length and the reference r_0 , also, we have $\Delta \theta = \theta - \theta_0$ and $\Delta \chi = \chi - \chi_0$. The cross-terms (Equation 5) describe the coupling effects among bond stretching, angle bending, and rotational torsion. In this study, we focus

on the stretch-bend cross term only. Torsion and related cross-terms are included in AMOEBA functional forms and will be considered later. These torsion-related cross-terms are needed to describe the hyperconjugation effects for conjugated molecules.³³ The stretch-bend cross-term is expressed in Equation (6): for any angle A-B-C, two parameters $k_{b,AB}$ and $k_{b,BC}$ denotes the coupling of the bond AB, BC respectively with angle ABC.

$$E_{cross} = E_{str-bnd} + E_{str-str} + E_{bnd-bnd} + E_{str-tors} + E_{bnd-tors} + E_{tors-tors} \quad (5)$$

$$E_{str-bnd} = [k_{ba,AB}\Delta r_{AB} + k_{ba,BC}\Delta r_{BC}]\Delta\theta_{ABC} \quad (6)$$

In this work, the distinct bond types are defined by the atomic types of 2 atoms forming the bond (A-B). Also, the different angle types have been classified by the atomic types of 3 atoms forming the angle (A-B-C).²³ Slightly simple types are used for the stretch-bend energy term, where any angles with the same central atom use the same parameters. Besides, the opbend terms have been classified by the type of central sp^2 atom with the type of one peripheral atom.

2.2 Initial bond/angle parameters from QM Hessian matrix

In this work, we adopt the modified Seminario method^{31, 34} to generate our initial bond stretching and angle bending parameters directly from the QM Hessian matrix. The modified Seminario method is a convenient and efficient way to derive accurate stretching and bending parameters with all other contributions ruled out (as opposed to fitting).

The Seminario method was initially designed for the generation of OPLS-AA³⁵ style parameters and written in MATLAB. We have re-written the code in Python based on the atom types we defined here for organic molecules (see **Data availability**).²³ The OPLS-AA FF uses the classical harmonic model for stretching and bending, which means the modified Seminario cannot be directly applied to the parameterization based on our model. The resulting parameters from this method serve as excellent initial values for further optimization against experimental data, which is significantly improved over the previous simple estimates used by Tinker³⁶ or Poltype³⁷ tools.

The mathematical details and principles about the modified Seminario are described here. The Hessian matrix is written based on the Cartesian coordinates of each atom, which is further divided into many small 3×3 matrices belonging to different bonds, such as $\mathbf{H}_{AB}$ for the bond AB in Equation (7). Stretching parameters can be obtained straightforwardly by using Equation (7), where $\lambda_i^{AB} (i = 1,2,3)$ are the eigenvalues of the small Hessian for the bond AB and $\vec{v}_i^{AB} (i = 1,2,3)$ are the corresponding eigenvectors, $\vec{u}_{AB}$ is the bond vector (All the vectors mentioned here and in the next paragraph are normalized).

$$\mathbf{H}_{AB} = \begin{bmatrix} \frac{\partial^2 E}{\partial x_A \partial x_B} & \frac{\partial^2 E}{\partial x_A \partial y_B} & \frac{\partial^2 E}{\partial x_A \partial z_B} \\ \frac{\partial^2 E}{\partial y_A \partial x_B} & \frac{\partial^2 E}{\partial y_A \partial y_B} & \frac{\partial^2 E}{\partial y_A \partial z_B} \\ \frac{\partial^2 E}{\partial z_A \partial x_B} & \frac{\partial^2 E}{\partial z_A \partial y_B} & \frac{\partial^2 E}{\partial z_A \partial z_B} \end{bmatrix}, k_{AB} = \sum_{i=1}^3 \lambda_i^{AB} |\vec{u}_{AB} \cdot \vec{v}_i^{AB}| \quad (7)$$

As to deriving angle bending parameters, additional work is involved. Inside the equations (8) below, we need to first derive the intermediate force constants in the direction perpendicular to the bonds forming the angle (vectors $\vec{u}_{PA}$ and $\vec{u}_{PC}$ with the orientation pointing to the interior in **Figure 2(a)**). Then, by considering the relation of those normal vectors and their contributions to the angle bending, the equations (9) and (10) are used to calculate the final bending force constants. More mathematical and analytical details about this method can be found elsewhere.³¹ The N is the number of angles in the FF with a central atom B and involves the bond AB. Take oxalic acid as an example in **Figure 2(b)**; atom A is the peripheral atom for two coupled angles: ABC and ABE. To obtain the force constant for angle ABC $k_{\theta(ABC)}$, we can see the vector $\vec{u}_{PA,1}$ perpendicular to bond AB points to ABC and $\vec{u}_{PA,2}$ perpendicular to bond AB points to ABE. However, this method is not appropriate to deal with angles involving *sp*-hybridized atoms, because it cannot detect the orientation. *Sp* atoms are not common, so some more rough estimates are used here for initial values in the subsequent fitting to QM vibrational frequencies (VF).

$$k_{PA} = \sum_{i=1}^3 \lambda_i^{AB} |\vec{u}_{PA} \cdot \vec{v}_i^{AB}|, \quad k_{PC} = \sum_{i=1}^3 \lambda_i^{CB} |\vec{u}_{PC} \cdot \vec{v}_i^{CB}| \quad (8)$$

$$s_{PA} = \begin{cases} 1 + \frac{\sum_{j=1}^N |\vec{u}_{PA,1} \cdot \vec{u}_{PA,j}|^2 - 1}{N - 1} & (N > 1) \\ 1 & (N = 1) \end{cases} \quad (9)$$

$$\frac{1}{k_{\theta(ABC)}} = \frac{s_{PA}}{R_{AB}^2 k_{PA}} + \frac{s_{PC}}{R_{CB}^2 k_{PC}} \quad (10)$$

It is convenient to derive the initial bond/angle parameters using the Modified Seminario method from the QM Hessian Matrix of a given molecule. However, since this model is appropriate mainly for the harmonic model, the parameters need to be further fitted to the QM VF. The whole procedure has been illustrated in **Figure 5** and implemented in an automated program which will be described in Section 2.4.

2.3 Computational details

(1). Selection of training set molecules

The training set consists of 445 molecules, with the distribution of the number of heavy atoms in each molecule shown in **Figure 3**. The whole range is 1 to 18 heavy atoms with most molecules having 5 to 9 heavy atoms. All the molecules have been classified into categories that span from alkane to bio-fragments, as illustrated in **Figure 4** and **Table 1**. In total there are grouped into seven categories: (1). alkanes and aliphatic rings; (2). molecules comprised of only single bonds; (3). molecules with double bonds or triple bonds; (4). benzene derivatives; (5). heterocyclics; (6). bio-fragments; (7). combinations of multiple aromatic cycles. The detailed list of molecules with their SMARTS and specific categories is in **Table S1**. The whole procedure of parametrization has been illustrated by the workflow in **Figure 5**.

(2). Initial bond/angle parameters from Hessian matrix

The frequencies of the normal modes have been calculated by using Gaussian09³⁸ with MP2/6-31g** (6-311g** for iodine atom) after the tight optimization with the same method and basis set. The bond/angle equilibrium values at MP2/6-31g** are close to the experiment for the organic molecules.³⁹ In this work, the reference bond lengths and angles were extracted from the final optimized structures and averaged based on the pre-defined bond and angle

types. Then, the initial force constant parameters for bonds and angles were derived from the Hessian matrix by using the modified Seminario method.³¹ These parameters were further refined in step (3), targeting the QM frequencies.

(3). Bond/angle parameters refinement using QM frequency

As suggested previously⁴⁰⁻⁴¹, the frequencies calculated by MP2/6-31g** (6-311g** for iodine) are scaled by a factor of 0.943 for better consistency with the experimental values. The vibrational analysis program (*vibrate.x*) in Tinker was used to generate normal mode frequencies for our models. Since we only focus on the interactions related to bonds and angles here and the frequencies of high range (usually large than 1000 cm⁻¹) are mainly contributed by those terms while the low range depends mainly on torsional terms, the reference data lower than 1000 cm⁻¹ are not used in the refinement. The least-square method from scipy⁴² is used to optimize the parameters for bond, angle, and stretch-bend cross-terms, with the cost, root-mean-square-error (RMSE in VF), as given by Equation 11.

$$RMSE(frequency) = \sqrt{\frac{1}{n} \sum_i (v^{MM} - v^{QM,scaled})^2} \quad (11)$$

(4). Opbend parameters derivation from potential energy surface fitting

The potential energy surfaces of the training set molecules were utilized to derive the out-of-plane bending (opbend) parameters (further details in **Table S2**). We focus on those molecules containing the *sp*² atoms that form trigonal planar structures. The central *sp*² atom was pulled out of the plane by 0.05, 0.1, 0.15 Å (Opbend-small subset hereafter), and 0.2, 0.25, 0.3 Å (Opbend-large subset hereafter), respectively, to create deformed configurations and corresponding energies. We obtained 4318 configurations for the training set, and the single point energy was calculated using Psi4⁴³ at MP2/aug-cc-pvtz (aug-cc-pvtz-pp for iodine) level of theory.

The least-square method was used to fit the opbend parameters by optimizing the weighted RMSE of the energy difference (shown by Equation 12). To ensure that our parameters are

not biased towards the high-energy (rare) structures far from equilibrium, we used a smaller weight (0.2) for configurations with energy 20 kcal/mol higher than that of equilibrium.

$$wRMSE(energy) = \sqrt{\frac{1}{n} \sum_i [(E^{MM,small} - E^{QM,small})^2 + 0.2 \times (E^{MM,large} - E^{QM,large})^2]} \quad (12)$$

(5). Validation

After obtaining the parameters by fitting frequencies and potential energy surface, we chose 120 new molecules as the validation set (see **Table S3 & S4** for details). The distribution of the number of heavy atoms in molecules of the validation set has been illustrated in **Figure 3**. Overall, the molecules in the validation set contain 4~14 heavy atoms. Those molecules are made of functional groups included in the training set molecules (**Table 1**). We mainly evaluated the bond/angle and coupling parameters by comparing the high-range frequencies of normal mode for these molecules. The opbend parameters were validated by comparing the energy differences between QM and our model for 829 configurations stemming from the 120 molecules in the validation set. This validation is intended to show the transferability of the current valence parameters.

2.4 Automated generation and assignment of valence parameters for new molecules

Although we have covered a range of chemistry (see **Table 1**) widely encountered in the practical simulations, there remains the possibility of failure to find the parameters for a certain molecule. For the molecules that the exact SMARTS patterns are missing in our database, we attempt to assign parameters based on the highest similarity to the existing chemical fragments.

Here we provide an automated program to determine the best matching atomic type for any new molecule and assign both valence parameters and our previously published charge-flux parameters²³ to each atom (see **Data availability**). It will attempt to find an *exact matching* from our database at first. When the *exact matching* fails, this program has implemented 2 methods to estimate those missing parameters: (1). Modified Seminario (in the red dash-line

rectangle of **Figure 5**); (2). Reversed searching by ranking tree (in cyan dash-line rectangle of **Figure 5**). In this work, we used the second method to generate the new parameters for the validation set.

The second method depends on the current parameter set to generate new parameters suitable for our model. We established a ranking tree where different types were placed in some positions in different levels determined by the complexity of the structure (**Figure 6**). For example, given a bond A-B which has no direct equivalent in the database, the program will check the position of types A and B in the ranking tree. It undergoes a reversed searching starting from the bottom (most complex), during which the types A and B are sequentially replaced by other types in the same level under the same root. If there is still no matching item, the searching will move to the upper level and continue this operation. The final parameter will be given by averaging the first 5 parameters found during the reversed searching.

For the common *sp*³ carbon, we have introduced canonical types (*nsp*³ C) based on the number of H atoms attached. They are designated as C30, C31, C32, C33, or C34 (See **Table S5**). Given a molecule, the detailed atom types of any *sp*³ C atoms will be identified by comparing their local environment (SMARTS) with the database. If there is no complete match, these canonical types will be used to generate parameters. For instance, if we have a molecule CH₃-CH(CH₃)-CH₂-CHO and find no angle parameter of CH-CH₂-CHO, then we will collect all the known angle parameters for the structure as *nsp*³ C – *nsp*³ C – CHO in the database to compute the average value and assign its value to the above angle. If still no appropriate parameter is found, we will continue reversed searching on the carbon atoms which are not *sp*³. If high accuracy is required under this method, we can use the frequency fitting to improve all the valence terms except the opbend terms.

3. Results and discussion

3.1 Overview of the atomic types and valence parameters

Currently, we have determined the valence parameters based on about 270 atomic types.

All the parameters were derived by both fitting to QM data or the ranking tree. To be specific, we generated 768 bond terms (of which 42 terms from the ranking tree, with each term including k_b and b_0), 1946 angle terms (of which 186 terms from the ranking tree, with each term involving k_a and θ_0), 109 stretch-bend terms (one term involves $k_{ba,AB}$ and $k_{ba,BC}$), and 565 opbend terms (of which 34 from the ranking tree, one term involves k_{opbend}).

The force constants have been determined for different structures by using our version of the modified Seminario program for bond and angle parameters. All the reference bond (b_0) and angle (θ_0) are averaged over the same atomic types. The current atomic types can keep the overall RMSD of the reference bond length less than 0.05Å and angle degree less than 5° for our training set comparing to the QM optimized structures (see **Data availability**), which is acceptable in MD simulations²³. As to cross terms, our current setting only turns on the stretching-bending coupling effects. The stretch-bend parameters are only distinguished by the atomic type of the central atom, i.e., all the angle structures with the same central atom share the same stretch-bend parameters. Next, the classification of out-of-plane bending terms (opbend) only considers the atomic type of the central atom and the side atom, which possibly pop out of the triangle plane. We will analyze this in detail in the following sections.

3.2 Analysis on parameters of the valence terms

We examined the force constants (k_b) and equilibrium bond lengths (b_0) between different *sp*³ C and H. It is observed from **Table 2** that the *sp*³ C with different numbers of the bonded hydrogens does not show a remarkable change in the bond length of C-H and corresponding force constant, especially the negligible difference among C(H3)-H, C(H2)-H, C(H1)-H. So, the bond type for terminal C and H can be equated with that for middle C and H. For most cases, the local functional groups have minimal effects on C-H because the RMSD of the lengths of all the matching bonds in the database is below 0.03 Å.

Next, we listed the possible pairs of the bonds between the canonical *sp*³ C in **Table 2**. The bond lengths between *sp*³ C and *sp*³ C with the different number of connected hydrogens are mostly within the range of 1.52 Å~1.53 Å, but it is observed that less number of bonded

hydrogens lead to longer bond lengths and smaller force constants. The C(H3)-C(H1) has the largest force constant, but it involves a terminal carbon with 3 H atoms. For those carbons of the interior, this trend is mostly correct, suggesting a strong coupling between bonds and the chemical environment (other bonds and angles) inside the molecule.

As for other kinds of bonds and angles, the analysis is becoming complicated, and no clear trend is observed.

3.3 Normal mode frequency

The frequencies of the normal modes for all 445 molecules in the training set have been utilized for determining force constants after a tight structure optimization. The correlation between QM reference and our model is illustrated in **Figure 7(a)**. The RMSD of the frequency of the normal modes reaches 36.6 cm^{-1} for the whole training set; at the same time, the relative error percentage is around 1.7% (

Table 3). By comparison, it was observed that OPLS combined with the modified Seminario method could generate frequencies with the relative errors of 7.4% (RMSD: 59.4 cm⁻¹) in general.³¹ AMBER-type valence terms combined with a strategy of partial hessian fitting gives out RMSD ~81.4 cm⁻¹ from a much smaller database,⁴⁴ and GAFF would show frequency error mostly larger than 100 cm⁻¹.¹ Meanwhile, these previous works on vibration analysis used small databases limited in the number and the variety of molecules, which in turn demonstrates the reliability of the valence model and parameters derived in this work using a large and diverse set of molecules.

As seen in **Figure 7(a)**, most valence related vibration frequencies concentrate on two areas (1000~1800 cm⁻¹ and 2800~3600 cm⁻¹). The valence terms can capture those modes in the range 2800~3600 cm⁻¹, which are contributed mainly by the fast stretching between heavy atoms and hydrogen such as C-H, N-H, or O-H. These motions occur at the terminal of the molecule, indicating limited coupling effects with the local angle bending. It is a common practice to restrain the H related high frequency stretching during molecular simulation to allow larger time steps⁴⁵⁻⁴⁶, while we have found reversible reference system propagator algorithms (RESPA) is a more effective approach – a small time step (e.g., 0.5 fs) can be used for valence forces and a large time step (e.g., 2 fs) is applied to the other contributions. The situation becomes more complicated when it comes to the range of 1000~1800 cm⁻¹. These involve double bond stretching, angle bending, and the mixture of several other motions. Because these motions directly affect the properties of interest in MD, the use of cross-terms and high-order polynomial models (for anharmonicity) becomes important. The detailed frequency comparisons for several typical molecules have been displayed in **Figure S1**, proving the reliability of our current model and parameters.

Some data points in **Figure 7(a)** with relatively large deviations arise from carbamate and guanine derivatives (several molecules having such functional groups). In carbamic acid and carbamate ion, we found that the normal mode contributed by the stretching of C=O is mixed with certain local angles bending (O-C-O, N-C-O, and more) lower frequency. The QM gives 1752 cm⁻¹ in carbamate ion and 1893 cm⁻¹ in carbamic acid for this coupled motion, while our

model gives the frequencies inside 2000~2100 cm^{-1} . For guanine, the deviation also happens on the C6=O stretching. It involves the angle bending N1-C6-C5 and both two ring structures show large deformation. Because we only utilized stretch-bend cross-terms in this work, there might be part of coupling effects that cannot be fully described. More coupling terms between different structures (such as those involving torsion) can be included to improve the performance for these complex situations further.

Here we assessed how much the cross-terms and the opbend terms contribute to the overall performance in **Table 4**. We re-classify Group (1)~(3) into 2 groups: Group A and Group B by the number of heavy atoms in each molecule (Group A: <10 ; Group B: ≥ 10). The cross-terms impact the overall performance of vibration analysis, but opbend terms show minimal influence since the previous works about the simple quadratic model for stretching and bending reported the best RMSD up to nearly 60 cm^{-1} . It reveals that anharmonicity plays the most significant role in generating accurate frequencies. Besides, the results are improved consistently for all the groups except Group B when stretch-bend cross terms have been used in this work, indicating that cross terms can capture more details in structural vibrations. The molecules in Group B mostly include long carbon chain or large carbon ring, which demand more coupling effects considered. Notably, the improvement for those molecules with largely conjugated structures is remarkable: the RMSD for benzene derivatives is decreased by 27.3%, 16.1% for heterocyclics, 16.5% for bio-fragments, and 31.6% for the combinations of multiple aromatic cycles. These molecules possess complex structures, so the motion of interior atoms can easily impact the surrounding bonds and angles. In general, the RMSD of frequencies for the training set goes down by 13.6% by adding cross-terms. Opbend terms have very little effect on the frequencies and made them slightly worse for certain groups. These are likely vibration modes involving the motion in which some sp^2 atoms popping out of the plane and adding opbend helps keep the correct structure and energy while introducing noise to vibrational frequencies.

3.4 Potential energy surface for opbend parameters

Out-of-plane parameters are used to avoid the abnormal pyramidalization of the planar structures with sp^2 atoms in the center. The results of the current polynomial model with the

corresponding parameters of the training set for opbend fitting have been illustrated in **Figure 8**. In **Figure 8**. Most of the data points are well matched between the model and QM energy within a wide range up to ~90 kcal/mol, while the model collectively underestimates the QM reference values. This suggests that our model can reflect the shape of potential energy surface during pyramidalization with high accuracy, even when the deformation of the structure is very large. The energy RMSD for the training set is 0.8375 kcal/mol for the Opbend-small set (maximum QM energy 22.9956 kcal/mol with average 2.3185 kcal/mol), 3.5226 kcal/mol for the Opbend-large set (maximum QM energy 91.0101 kcal/mol with average 12.9017 kcal/mol) and 2.5582 kcal/mol for the whole set (

Table 5). Although Allinger's model can improve the description of potential energy surface in the out-of-plane bending, the simple model cannot capture the effect fully. As a result, the model energy tends to be smaller than expected from overall observation. Nonetheless, this model separates the out-of-plane motion into three components from each side atoms, which makes the parameters more transferable and flexible in applying in many distinct planar structures.

3.5 Validation

To test the accuracy and transferability of the valence parameters derived in this work, we applied these parameters to all the 120 molecules in the validation set. All the parameters for the validation set molecules are automatically assigned or generated via the ranking tree method described in Methodologies. Frequency validation results are shown in **Figure 7(b)** and

Table 3. The RMSD in frequencies for each group of validation set is mostly consistent with the results from the training set, ca. $\sim 34\text{ cm}^{-1}$. In addition, we compared the equilibrium b_0 and θ_0 parameters assigned based on atom type with QM-optimized geometry for the 120 molecules. The overall RMSD is less than $0.05\text{\AA}$ for b_0 and less than 5° for θ_0 (see **Data Availability**). For the out-of-plane effects, the performance of the opbend parameters is satisfying as shown in **Figure 8(b)** and

Table 5. The RMSD between QM and MM energy for all the 829 configurations from 120 molecules is ~2.8 kcal/mol. Overall the validation results demonstrated high accuracy and transferability of our parameters for a wide range of small organic molecules.

4. Conclusion

The classical harmonic equations have been used for decades to calculate the potential energy of bonded interactions by many FFs. While computationally attractive, it shows deficiencies in describing the potential energy surface and vibrational frequencies of molecules compared to quantum calculations. AMOEBA-family FFs apply the MM3(MM4)-style, anharmonic valence interaction model to improve the accuracy of structure and spectroscopic properties. The model employs high-order polynomial functionals in bond stretching and angle bending, the cross-terms that couple different valence motions, and out-of-plane bending terms. The benefits of these high-order and coupling terms are evidenced in this work. They noticeably improve the accuracy of normal mode frequencies, indicating a strong anharmonicity in bonds and angles. The cross-terms capture more details of the intramolecular motions and significantly improve normal mode frequencies with consistently high accuracy, especially for large structures and conjugation molecules. In addition, our results indicate that opbend terms generate correct potential energy surface around the planar structure for those *sp*² atoms.

The current parameter set can be applied to a wide range of distinct functional groups, and it is expandable to tackle additional chemistry in the future. The modified Seminario method has been combined with the current atom types of the AMOEBA(+) model, providing reliable initial force constant parameters of bond stretching and angle bending as reference values from QM Hessian. Refinement of bond, angle, and bond-angle coupling explicitly targeting the QM frequency data further increases the quality of these force constant parameters. The opbend parameters are derived by fitting to the potential energy surface of distorted structures composing *sp*² atoms. It is interesting to examine how good our model can describe the overall geometry of simple compounds comparing to high-level QM or experimental structures.

However, this will not be practical until all the other energy components are parameterized, as both the valence and non-bonded interactions are responsible for the accurate prediction of the molecular geometry. An automated program to assign the parameters has also been presented in this work, which is accessible to the public (see Data availability). This program as well as the parameters, will be further implemented in the canonical Tinker³⁶ and Poltype software packages³⁷.

Acknowledgments

This work was supported by the National Institutes of Health (R01GM106137 and R01GM114237), and National Science Foundation (CHE-1856173).

Data availability

1. The molecules in tinker format and final bonded parameters can be accessed at:

https://github.com/prenlab/amoebaplus_data/tree/master/valence2021

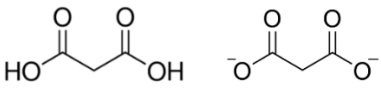
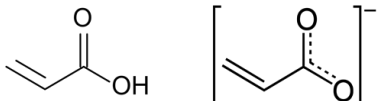
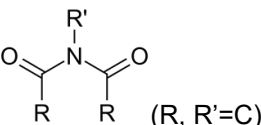
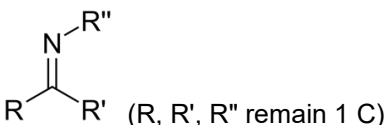
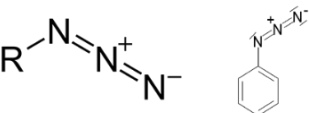
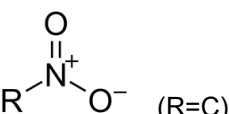
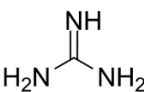
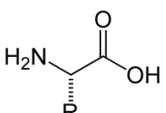
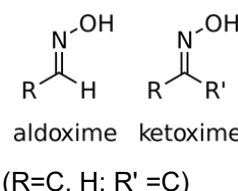
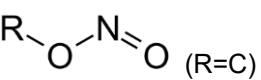
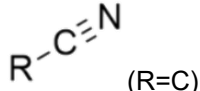
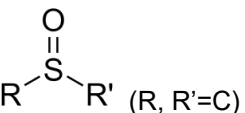
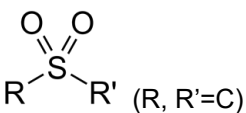
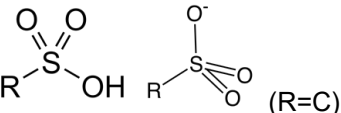
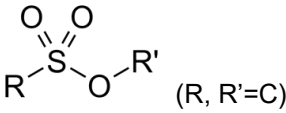
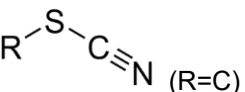
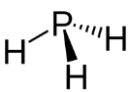
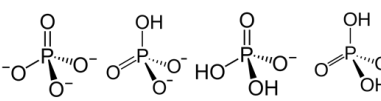
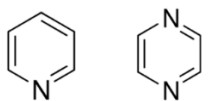
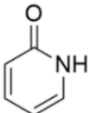
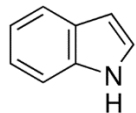
2. The programs developed in this work are accessible through the GitHub repository at:

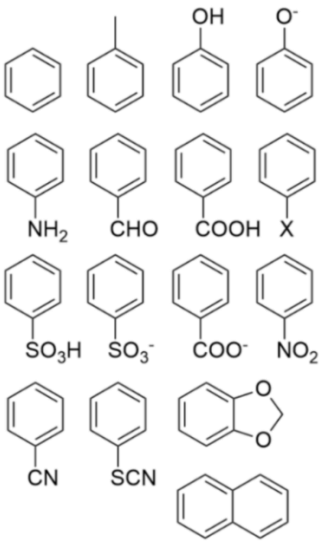
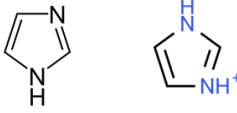
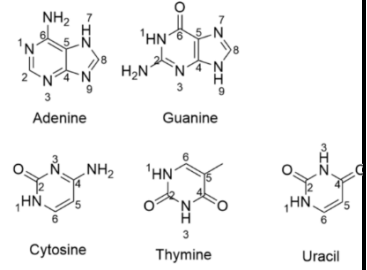
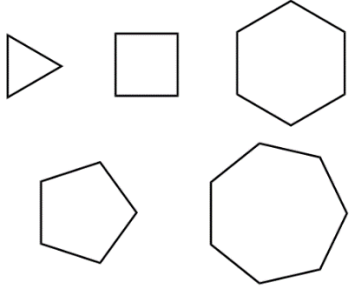
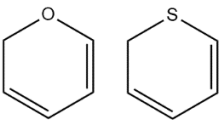
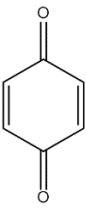
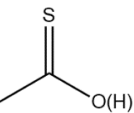
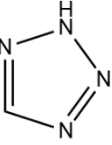
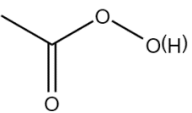
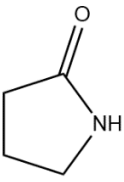
https://github.com/prenlab/amoebaplus_parameter

Tables

Table 1. A general illustration of the functional groups and distinct chemical structures covered in the current study.

Group	Chemical structure	Group	Chemical structure
Alkane	$\left[\begin{array}{c} \text{C} \\ \\ \text{C} \end{array} \right]$ (chain & cyclic)	Alkene	$\text{C}=\text{C}$
Alkyne	$\text{HC}\equiv\text{CH}$	Conjugated molecules	$\text{CH}_2=\text{CH}-\text{CH}=\text{CH}_2$ $\text{CH}_2=\text{CH}-\text{CH}=\text{O}$
Amine	$\text{R}-\text{N} \begin{array}{l} \text{R}'' \\ \text{R}' \end{array}$ (all R = H, C)	Ammonium	$\text{R}_1-\text{N}^+ \begin{array}{l} \text{R}_4 \\ \text{R}_2 \text{ R}_3 \end{array}$ (all R = H, C)
Alcohol	$\text{R}-\text{O}-\text{H}$ (R = C)	Ether	$\text{R}-\text{O}-\text{R}'$ (all R = C)
Di-oxyl	$\begin{array}{c} \text{O}-\text{R} \\ \diagdown \quad \diagup \\ \text{O}-\text{R}' \end{array}$ (all R = C)	Thiol	$\text{R}-\text{S}-\text{H}$ (R = C)
Sulfide	$\text{R}-\text{S}-\text{R}'$ (all R = C)	Disulfide	$\text{R}-\text{S}-\text{S}-\text{R}'$ (all R = C)
Halide	$\text{R}-\text{X}$ (R = C; X=F, Cl, Br, I)	Aldehyde	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{H} \end{array}$ (R=C, H)
Ketone	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{R}' \end{array}$ (R=C)	Carboxylic acid / Carboxylate	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{O}^- \end{array}$ $\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{OH} \end{array}$ (R=C, H)
Carboxylate ester	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{O}-\text{R}' \end{array}$ (R=C, H; R'=C)	Carbamic acid / Carbamate	$\text{H}_2\text{N}-\begin{array}{c} \text{O} \\ \\ \text{C}-\text{OH} \end{array}$ $\text{H}_2\text{N}-\begin{array}{c} \text{O} \\ \\ \text{C}-\text{O}^- \end{array}$
Amide	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{N} \begin{array}{l} \text{R}'' \\ \text{R}' \end{array} \end{array}$ (R, R', R''=C, H)	Carbonate / Bicarbonate	$\text{R}-\text{O}-\begin{array}{c} \text{O} \\ \\ \text{C} \end{array}-\text{O}-\text{R}'$ (R=C, H; R'=C)
Anhydride	$\begin{array}{c} \text{R}^1 \quad \text{O} \quad \text{R}^2 \\ \quad \diagdown \quad \diagup \quad \\ \text{C} \quad \text{O} \quad \text{C} \end{array}$ (R ¹ , R ² =C)	Acyl halide	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{X} \end{array}$ (R=C; X=F, Cl, Br)
Oxalic acid Oxalate	$\text{HO}-\text{C}(=\text{O})-\text{C}(=\text{O})-\text{OH}$ $\left[\begin{array}{c} \text{O} \quad \text{O} \\ \quad \\ \text{C} \quad \text{C} \\ \quad \\ \text{O} \quad \text{O} \end{array} \right]^{2-}$	α-keto acetate / β-keto acetate	$\begin{array}{c} \text{O} \\ \\ \text{R}-\text{C}-\text{OH} \end{array}$ $\begin{array}{c} \text{O} \quad \text{O} \\ \quad \\ \text{R}-\text{C}-\text{CH}_2-\text{C}-\text{OH} \end{array}$ (R=C)

Malonic acid / Malonate		Acrylic acid/ Acrylate	
Imide		Imine (Aldimine/ Ketimine)	
Azide		Azo-compound	
Nitro-compound		Guanidine	
Amino acid		Oxime	
Nitrite		Nitrile	
Sulfoxide		Sulfone	
Sulfonic acid / Sulfonate		Sulfonate ester	
Thiocyanate		Phosphine	
Phosphoric acid / Phosphate		Pyridine / Pyrazine	
Benzene Derivatives		Conjugated lactam	
		Indole	

		Imidazole / Imidazolium	
NA Base		Aliphatic cycles and derivatives	
Pyran		Benzoquinone	
Thioacetate		Tetrazole	
Peracetic acid/ Peroxoate		Pyrrolidinone	

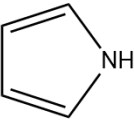
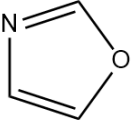
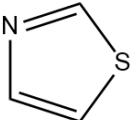
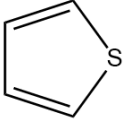
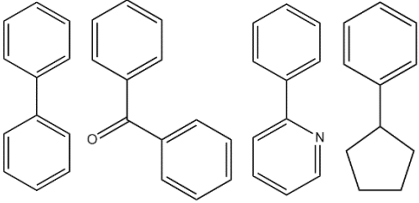
Pyrrole		Oxazole	
Thiazole		Thiophene	
Connected structure of double heterocyclics, benzenes or aliphatic cycles			

Table 2. The comparison of equilibrium bond lengths and corresponding force constants among *sp*³ C and H. ^{a)}

bond ^{b)}	Equilibrium length (Database) ^{c)}		Force constant (Database) ^{c)}
C[H4]-H	1.0897	(4) <u>0.0000</u>	383.57
C[H3]-H	1.0940	(1297) <u>0.0297</u>	345.98
C[H2]-H	1.0957	(448) <u>0.0028</u>	340.53
C[H1]-H	1.0980	(52) <u>0.0034</u>	338.72
C[H3]-C[H3]	1.5255	(1) <u>0.0000</u>	266.49
C[H3]-C[H2]	1.5225	(153) <u>0.0065</u>	203.31
C[H3]-C[H1]	1.5240	(82) <u>0.0052</u>	280.35
C[H3]-C[H0]	1.5306	(16) <u>0.0044</u>	210.15
C[H2]-C[H2]	1.5236	(30) <u>0.0046</u>	205.76
C[H2]-C[H1]	1.5231	(9) <u>0.0112</u>	214.73
C[H2]-C[H0]	1.5352	(3) <u>0.0094</u>	190.84
C[H1]-C[H1]	1.5420	(1) <u>0.0000</u>	172.75
C[H0]-C[H0]	1.5697	(1) <u>0.0000</u>	133.12

a) Statistics are reported from all the configurations in our database.

b) Here, C[H n] means the *sp*³ C with n hydrogens bonded.

c) The numbers in the parenthesis represent the number of matching structures in the database, and the underlined number means the RMSD: root mean square derivation. (Unit: length – Å, force constant – kcal·mol⁻¹·Å⁻¹)

Table 3. Statistical comparison of QM scaled frequencies of normal modes and the values calculated by MM model.

Statistics ^{a)}	Training set ^{b)}			Validation set ^{b)}		
	RMSE	MRE	Num.	RMSE	MRE	Num.
Group A	38.4279	1.81%	4846	37.9629	1.82%	1181
Group B	34.2120	1.72%	354	35.2745	1.59%	146
Benzene derivatives	28.5765	1.45%	1433	32.1555	1.48%	982
Heterocyclics	41.0277	1.91%	1122	33.3864	1.71%	541
Bio-fragments	39.0039	1.84%	831	38.6137	1.94%	81
Combination of multiple aromatic cycles	28.8252	1.41%	752	26.0445	1.30%	449
Total	36.6139	1.73%	9338	34.0284	1.62%	3410
R ² =0.9981			R ² =0.9983			

a) Group A includes those molecules with less than 10 heavy atoms (non-hydrogen) and Group B means those molecules with ≥ 10 heavy atoms. Both Group A and Group B contain those molecules which are not involved in other categories listed in the table.

b) RMSE: root mean square error (unit: cm^{-1}); MRE: mean relative error ($\frac{1}{N} \sum_{i=1}^N \frac{|v(QM) - v(MM)|}{v(QM)} \times 100\%$). The number of respective unique data points is marked with Num. R²: correlation coefficient.

Table 4. Statistical comparison of QM scaled frequency of normal modes and the values calculated by MM model with or without coupling terms and opbend terms in the training set.

Group name ^{a)}	w. coupling w. opbend ^{b)}		w. coupling w.o. opbend ^{b)}		w.o. coupling w. opbend ^{b)}	
	RMSE	MRE	RMSE	MRE	RMSE	MRE
Group A	38.4279	1.81%	39.0842	1.83%	41.9415	1.95%
Group B	34.2120	1.72%	33.4050	1.69%	33.2874	1.73%
Benzene derivatives	28.5765	1.45%	28.5561	1.45%	39.3057	1.93%
Heterocyclics	41.0277	1.91%	39.8838	1.89%	48.8816	2.38%
Bio-fragments	39.0039	1.84%	38.7749	1.88%	46.6939	2.33%
Combination of multiple cycles	28.8252	1.41%	28.8945	1.42%	42.4678	2.11%
Total	36.6139	1.73%	36.7788	1.75%	42.6315	2.04%

a) Group A means those molecules with less than 10 heavy atoms (non-hydrogen) and Group B means those molecules with ≥ 10 heavy atoms. Both Group A and Group B contain those molecules which are not involved in other categories listed in the table.

b) RMSE: root mean square error (unit: cm^{-1}); MRE: mean relative error ($\frac{1}{N} \sum_{i=1}^N \frac{|v(QM) - v(MM)|}{v(QM)} \times 100\%$) has been included in the parenthesis. R^2 : correlation coefficient.

Table 5. Statistical comparison of QM energy differences and the values calculated by the MM model.

Group name ^{b)}		Training set ^{c)}	Validation set ^{d)}
Opbend-small ^{a)}	RMSE	0.8375	1.3453
	QM_Max	22.9956	17.6173
	QM_Ave	2.3185	3.4736
Opbend-large ^{a)}	RMSE	3.5226	4.1265
	QM_Max	91.0101	53.3861
	QM_Ave	12.9017	15.4029
Total	RMSE	2.5582	2.8082
	R ²	0.9743	0.9471
	QM_Ave	7.6003	8.2367

a) Opbend-small and Opbend-large groups rely on the scale of deformation of the specified structures (see section 2.2).

b) RMSE: root mean square error; QM_Max: maximum of the absolute QM ΔE ; QM_Ave: average of the absolute QM ΔE . (Unit: kcal·mol⁻¹).

c) R²: correlation coefficient. The total number of configurations for the training set is 4318.

d) R²: correlation coefficient. The total number of configurations for the validation set is 829.

Figures

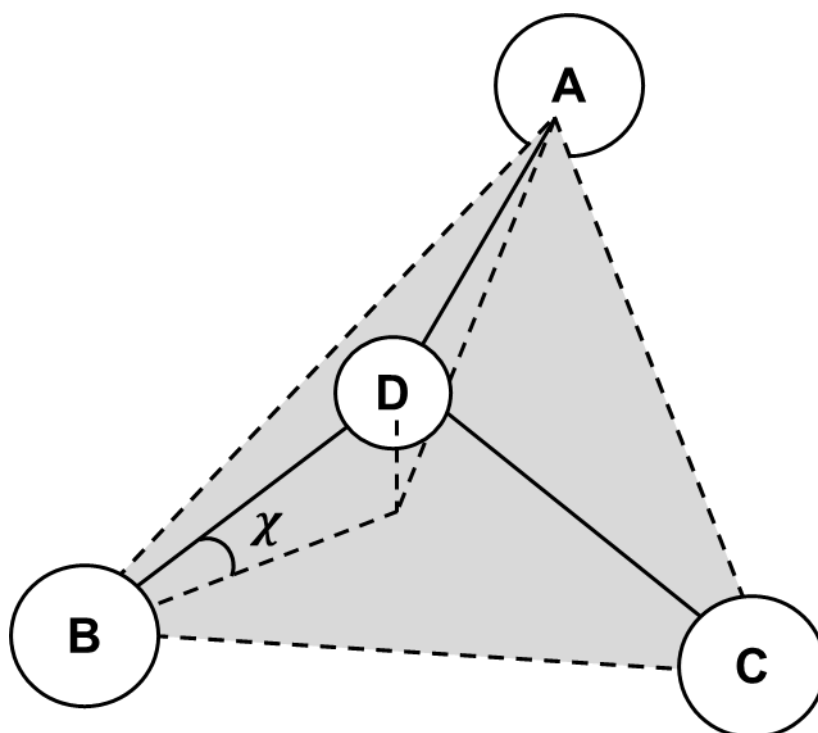


Figure 1. An illustration of a trigonal center D pyramidalizing from plane ABC. The out-of-plane angle χ has been defined as illustrated.

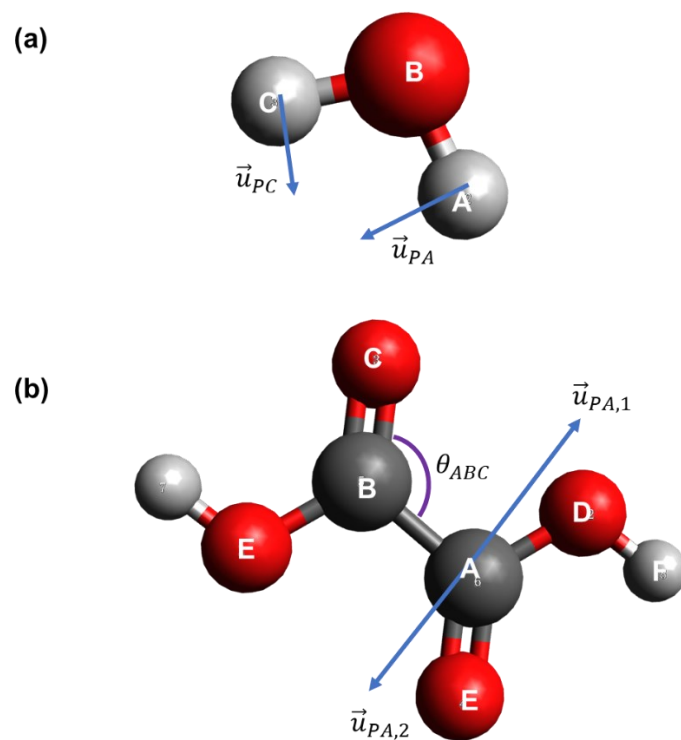


Figure 2. An illustration of the vectors used in the Seminario method. (a) The 2 vectors $\vec{u}_{PA}$ and $\vec{u}_{PC}$ contributing to the force constant of angle ABC in water molecule; (b). The 2 vectors pointing to 2 coupling angles with A as a side atom in oxalic acid.

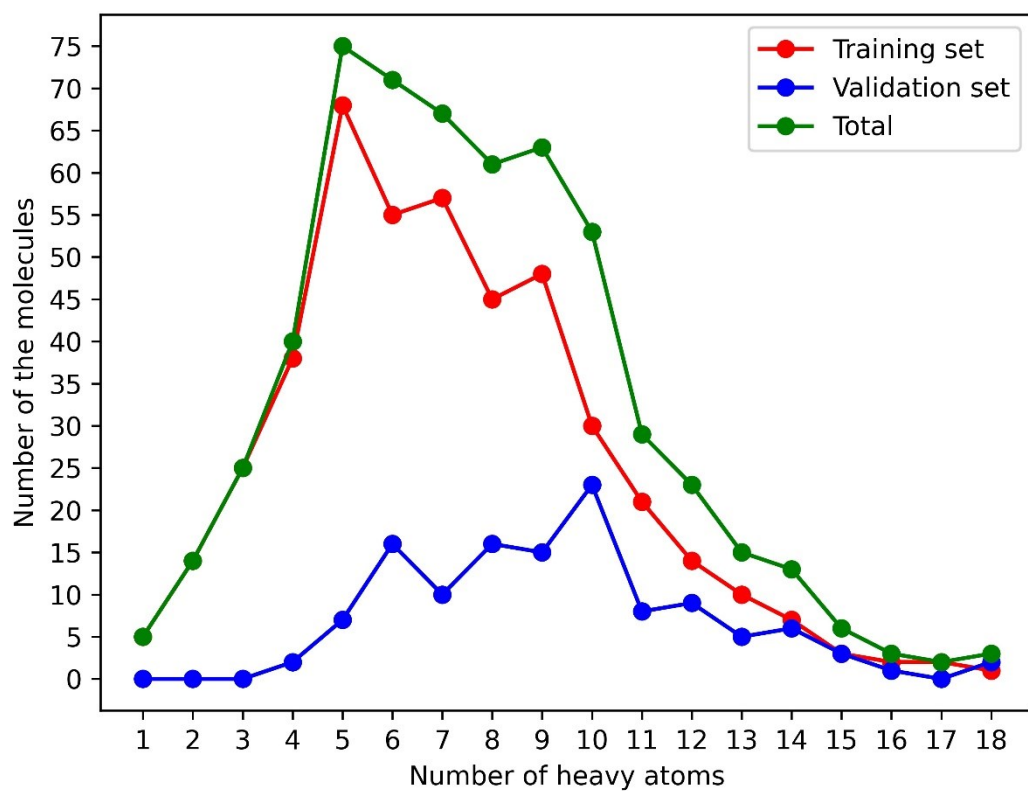


Figure 3. Distribution of the number of heavy atoms in different molecules. (Red: training set; Blue: validation set; Green: total.)

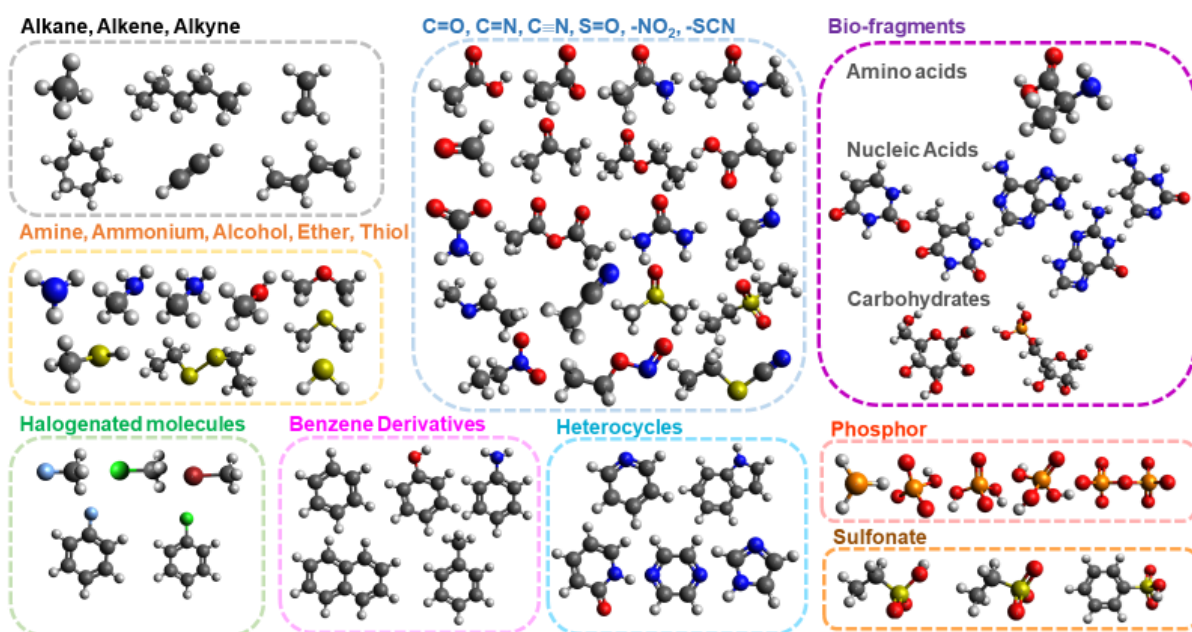


Figure 4. Representatives of the organic molecules covered in this study.

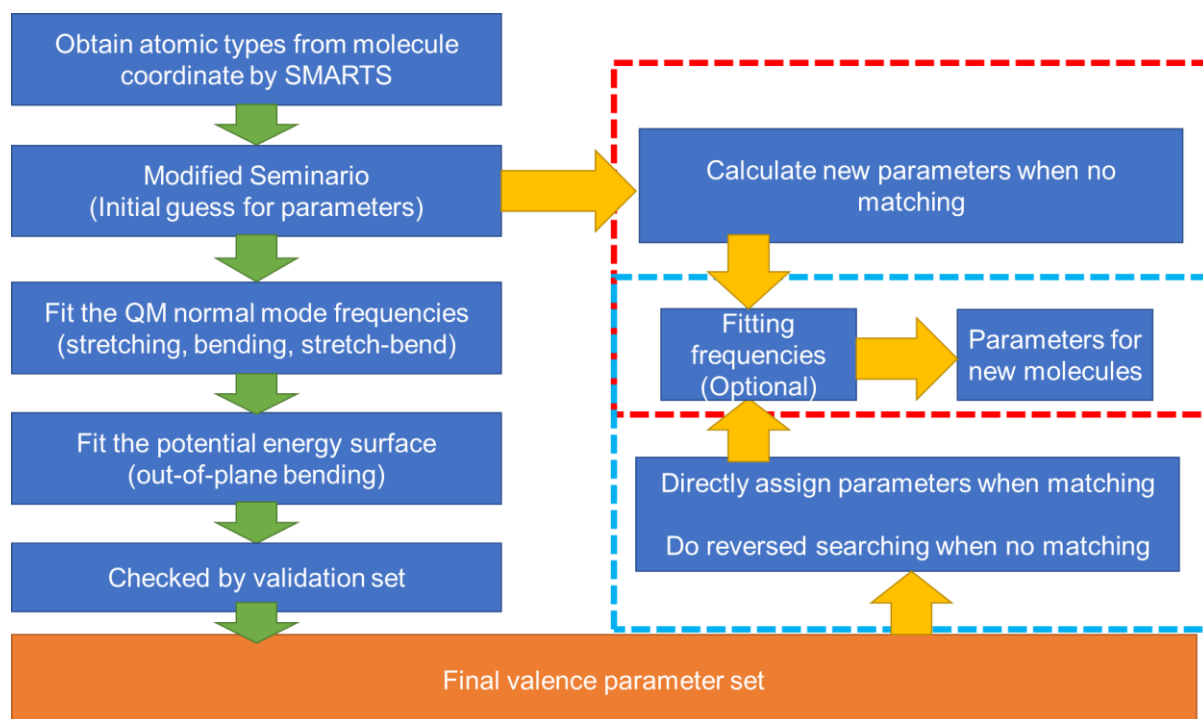


Figure 5. The procedure to generate the final valence parameter set (green arrows) and the methods to obtain and assign parameters for any new molecule (yellow arrows): assignment by Modified Seminario is shown inside the red dash box, and assignment by reversed searching is shown inside the blue dash box.

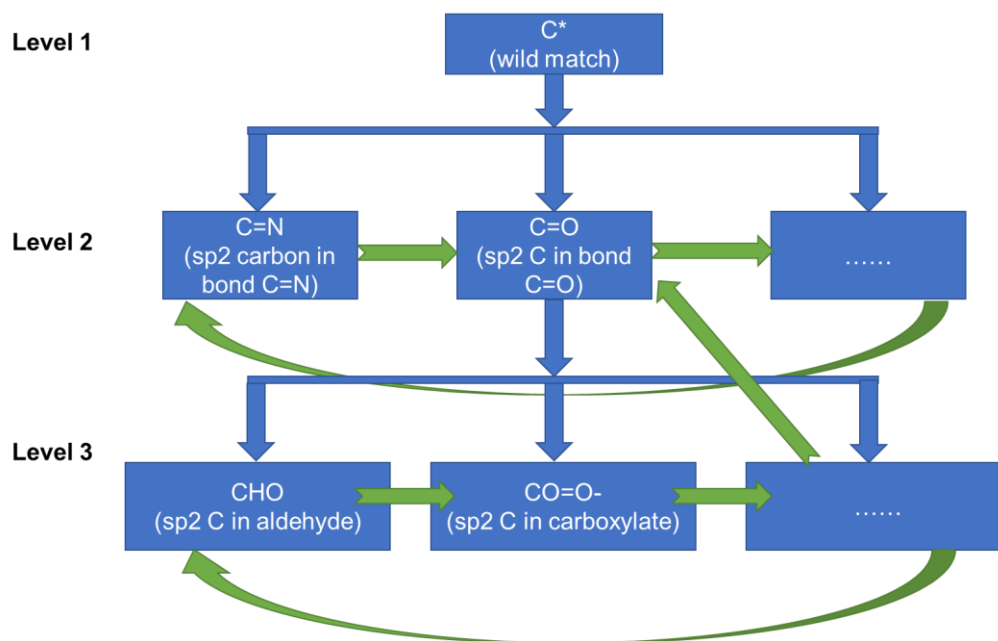


Figure 6. The basic structure of the ranking tree (simplified). The green arrows show the sequence of searching in the same level and reversely to the upper levels.

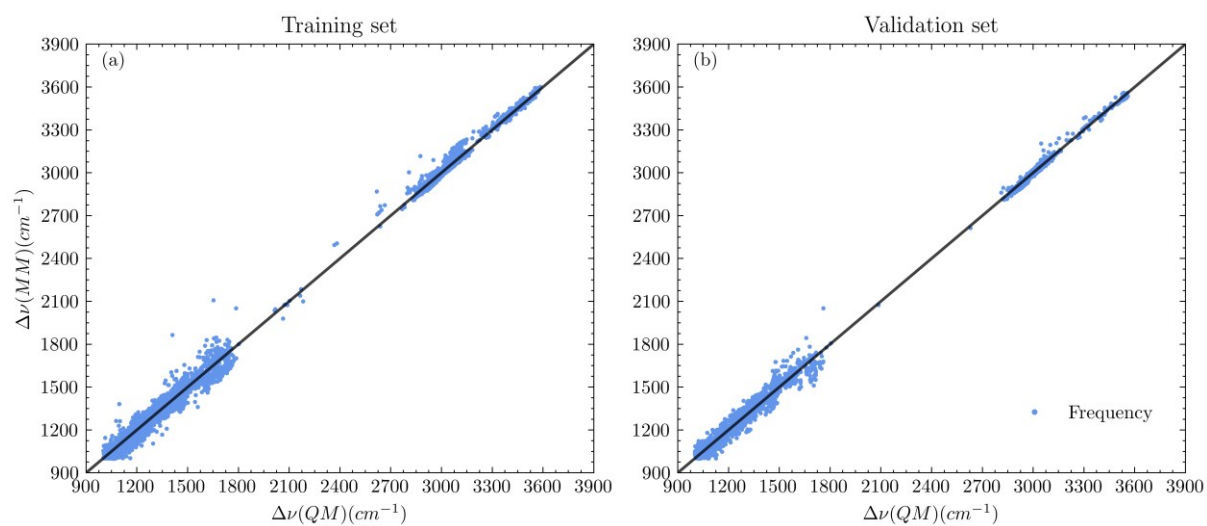


Figure 7. The correlation between the QM and MM normal mode frequencies(cm^{-1}) for the molecules in **(a)** the training set and **(b)** the validation set.

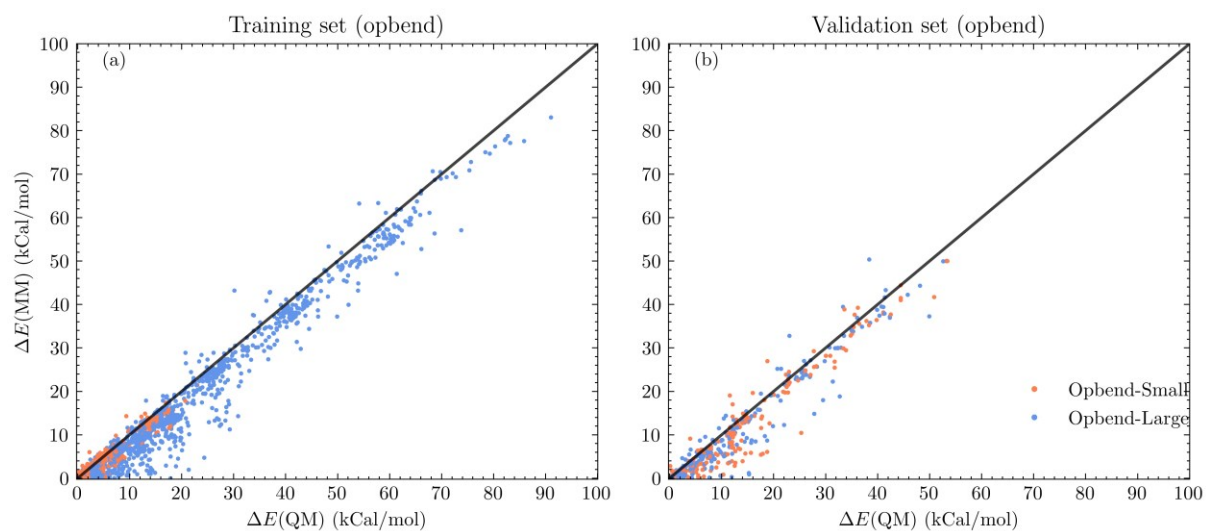


Figure 8. The correlation between the energy difference calculated by QM and MM for all the configurations in **(a)** the training set and **(b)** the validation set. Opbend-small refers to small deformation and opbend-large set refers to large deformation of the specified structures, as described in Section 2.3(4).

References

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Supplementary Information

High Order Ab Initio Valence Force Field with Chemical Pattern Based Parameter Assignment

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Table S1. The molecules in the training set

The training set has been shown with their name, their classified group, and the SMILE strings (445 molecules). We have 7 groups: (1).alkanes and aliphatic rings; (2).molecules comprised of only single bonds; (3).molecules with double bonds or triple bonds; (4).benzene derivatives; (5).heterocyclics; (6).bio-fragments; (7).combinations of multiple aromatic cycles.

Name	Group	SMILE
Water	0	O
Methane	1	C
Ammonia	2	N
Methylamine	2	CN
Methanol	2	CO
N-Methylacetamide	3	CC(=O)NC
Acetic acid	3	CC(=O)O
Acetamide	3	CC(=O)N
Uracil	6	C1=CNC(=O)NC1=O
Pyridine	5	C1=CC=NC=C1
Benzene	4	C1=CC=CC=C1
Ethene	1	C=C
Pentane	1	CCCCC
Neopentane	1	CC(C)(C)C
Cyclopentane	1	C1CCCC1
Methane thiol	2	CS
DMSO	3	CS(=O)C
Fluorobenzene	4	C1=CC=C(C=C1)F
Chlorobenzene	4	C1=CC=C(C=C1)Cl
Bromobenzene	4	C1=CC=C(C=C1)Br
DimethylSulfide	2	CSC
Imidazole	5	C1=CN=CN1
Pyrrolidine	5	C1CCNC1
Phenol	4	C1=CC=C(C=C1)O
Indole	5	C1=CC=C2C(=C1)C=CN2
Difluoromethane	2	C(F)F
Dichloromethane	2	C(Cl)Cl
Dibromomethane	2	C(Br)Br
Fluoromethane	2	CF
Chloromethane	2	CCl
Bromomethane	2	CBr
Hydrogenphosphate	6	OP(=O)([O-])[O-]
Dihydrogen phosphate	6	OP(=O)(O)[O-]
Phosphorous acid	6	OP(O)O
Methylammonium	2	C[NH3+]
1H-imidazol-3-ium	5	C1=C[NH+]=CN1

Guanidine	2	<chem>C(=N)(N)N</chem>
Acetate	3	<chem>CC(=O)[O-]</chem>
Formimidamide	3	<chem>C(=N)N</chem>
Formamide	3	<chem>C(=O)N</chem>
Formicacid	3	<chem>C(=O)O</chem>
Ethane	1	<chem>CC</chem>
Ethanol	2	<chem>CCO</chem>
7-Methylindole	5	<chem>CC1=C2C(=CC=C1)C=CN2</chem>
Methylguanidine	2	<chem>CN=C(N)N</chem>
4-Methylimidazole	5	<chem>CC1=CN=CN1</chem>
2-Propanol	2	<chem>CC(C)O</chem>
Ethyne	1	<chem>C#C</chem>
2-Aminopyridine	5	<chem>C1=CC=NC(=C1)N</chem>
2-Pyridone	5	<chem>C1=CC(=O)NC=C1</chem>
Hydrogen sulfide	2	<chem>S</chem>
Pyrazine	5	<chem>C1=CN=CC=N1</chem>
Thymine	6	<chem>CC1=CNC(=O)NC1=O</chem>
Adenine	6	<chem>C1=NC2=NC=NC(=C2N1)N</chem>
Formaldehyde	3	<chem>C=O</chem>
Acetonitrile	3	<chem>CC#N</chem>
Dimethylamine	2	<chem>CNC</chem>
Isobutane	1	<chem>CC(C)C</chem>
Trimethylamine	2	<chem>CN(C)C</chem>
Trimethylammonium	2	<chem>C[NH+](C)C</chem>
Ethane thiol	2	<chem>CCS</chem>
Methyl benzene	4	<chem>CC1=CC=CC=C1</chem>
Dimethylammonium	2	<chem>C[NH2+]C</chem>
Acetone	3	<chem>CC(=O)C</chem>
Cyclohexane	1	<chem>C1CCCCC1</chem>
Dimethylether	2	<chem>COC</chem>
Naphthalene	4	<chem>C1=CC=C2C=CC=CC2=C1</chem>
Guanine	6	<chem>C1=NC2=C(N1)C(=O)NC(=N2)N</chem>
Diethylether	2	<chem>CCOCC</chem>
Acetaldehyde	3	<chem>CC=O</chem>
Cytosine	6	<chem>C1=C(NC(=O)N=C1)N</chem>
Phenolate	4	<chem>C1=CC=C(C=C1)[O-]</chem>
Aniline	4	<chem>C1=CC=C(C=C1)N</chem>
Tetrafluoromethane	2	<chem>C(F)(F)(F)F</chem>
Tetrachloromethane	2	<chem>C(Cl)(Cl)(Cl)Cl</chem>
Trifluoromethane	2	<chem>C(F)(F)F</chem>
Trichloromethane	2	<chem>C(Cl)(Cl)Cl</chem>
Tribromomethane	2	<chem>C(Br)(Br)Br</chem>
Acetic Anhydride	3	<chem>CC(=O)OC(=O)C</chem>

Carbamic acid	3	<chem>C(=O)(N)O</chem>
1-Butylamine	2	<chem>CCCCN</chem>
3-Methylindole	5	<chem>CC1=CNC2=CC=CC=C12</chem>
4-Methylimidazole	5	<chem>CC1=CN=CN1</chem>
Ethyl methyl sulfide	2	<chem>CCSC</chem>
1-Propylguanidinium	2	<chem>CCC[NH+]=C(N)N</chem>
Propionamide	3	<chem>CCC(=O)N</chem>
Propionic acid	3	<chem>CCC(=O)O</chem>
Diethyl sulfone	3	<chem>CCS(=O)(=O)CC</chem>
Diethyl disulfide	2	<chem>CCSSCC</chem>
Formate	3	<chem>C(=O)[O-]</chem>
Propionyl chloride	3	<chem>CCC(=O)Cl</chem>
Propionyl fluoride	3	<chem>CCC(=O)F</chem>
Propionyl bromide	3	<chem>CCC(=O)Br</chem>
Diethyl carbonate	3	<chem>CCOC(=O)OCC</chem>
Ethyl hydrogen carbonate	3	<chem>CCOC(=O)O</chem>
Diethoxymethane	2	<chem>CCOCOCC</chem>
Benzonitrile	4	<chem>C1=CC=C(C=C1)C#N</chem>
Phosphane	6	<chem>P</chem>
Propionate	3	<chem>CCC(=O)[O-]</chem>
Propionaldehyde	3	<chem>CCC=O</chem>
2-Butanone	3	<chem>CCC(=O)C</chem>
N-Ethylformamide	3	<chem>CCNC=O</chem>
Dimethyl formamide	3	<chem>CN(C)C=O</chem>
1,3-Benzodioxole	4	<chem>O1c2c(OC1)cccc2</chem>
Dioxolane	2	<chem>C1COCO1</chem>
Ethanamine	3	<chem>CCN</chem>
Ethanimine	3	<chem>CC=N</chem>
Methanamine	3	<chem>CN</chem>
2-Propanimine	3	<chem>CC(=N)C</chem>
Ethyl Acetoacetate	3	<chem>CCOC(=O)CC(=O)C</chem>
Oxalic acid	3	<chem>C(=O)(C(=O)O)O</chem>
Hydrogen oxalate	3	<chem>C(=O)(C(=O)[O-])O</chem>
Oxalate	3	<chem>C(=O)(C(=O)[O-])[O-]</chem>
Malonic acid	3	<chem>C(C(=O)O)C(=O)O</chem>
Hydrogen malonate	3	<chem>C(C(=O)O)C(=O)[O-]</chem>
Malonate	3	<chem>C(C(=O)[O-])C(=O)[O-]</chem>
2-Oxobutanoic Acid	3	<chem>CCC(=O)C(=O)O</chem>
2-Oxobutanoate	3	<chem>CCC(=O)C(=O)[O-]</chem>
Dipropionamide	3	<chem>CCC(=O)NC(=O)CC</chem>
Nitroethane	3	<chem>CC[N+](=O)[O-]</chem>
Nitrobenzene	4	<chem>C1=CC=C(C=C1)[N+](=O)[O-]</chem>
Ethyl N-ethyl-N-	3	<chem>CCN(C)C(=O)OCC</chem>

methylcarbamate		
Methylcarbamic acid	3	CNC(=O)O
Carbamate	3	C(=O)(N)[O-]
Ethyl nitrite	3	CCON=O
Benzenediazonium	4	C1=CC=C(C=C1)[N+]#N
Azobenzene	4	C1=CC=C(C=C1)N=NC2=CC=CC=C2
1-[(S)-Methylsulfinyl]ethane	3	[S@@](=O)(CC)C
Ethane sulfonic acid	7	CCS(=O)(=O)O
Ethane sulfonate	7	CCS(=O)(=O)O
Benzene sulfonic acid	7	C1=CC=C(C=C1)S(=O)(=O)O
Benzene sulfonate	7	C1=CC=C(C=C1)S(=O)(=O)[O-]
Ethyl acetate	3	CCOC(=O)C
Ethyl methanesulfonate	7	CCOS(=O)(=O)C
Ethyl thiocyanate	3	CCSC#N
Phenyl thiocyanate	4	C1=CC=C(C=C1)SC#N
Butadiene	1	C=CC=C
Acrolein	3	C=CC=O
Propionaldehyde oxime	3	CCC=NO
Acetone oxime	3	CC(=NO)C
Benzyl alcohol	4	C1=CC=C(C=C1)CO
Ethylbenzene	4	CCC1=CC=CC=C1
Benzylamine	4	C1=CC=C(C=C1)CN
Benzaldehyde	4	C1=CC=C(C=C1)C=O
Benzoic acid	4	C1=CC=C(C=C1)C(=O)O
Benzoate	4	C1=CC=C(C=C1)C(=O)[O-]
Acrylic Acid	3	C=CC(=O)O
Acrylate	3	C=CC(=O)[O-]
L-Alanine	6	CC(C(=O)O)N
Pyrophosphate ion	6	[O-]P(=O)([O-])OP(=O)([O-])[O-]
Phenylazanium	4	C1=CC=C(C=C1)[NH3+]
Glucose	6	C(C1C(C(C(C(O1)O)O)O)O)O
Ribose phosphate	6	C(C(C(C(C(=O)O)O)O)O)OP(=O)(O)O
Glyoxal	3	C(=O)C=O
2-Methyl-1-butene	1	CCC(=C)C
(E)-but-2-ene	1	CC=CC
Glycolic acid	3	C(C(=O)O)O
Glycolate	3	C(C(=O)[O-])O
Malonaldehyde	3	C(C=O)C=O
Urea	3	C(=O)(N)N
Fluoroethane	2	CCF
Chloroethane	2	CCCl
Bromoethane	2	CCBr
2,3-Dimethylbutane	1	CC(C)C(C)C

2,2-Dimethylbutane	1	<chem>CCC(C)(C)C</chem>
3-Ethylpentane	1	<chem>CCC(CC)CC</chem>
2,2,3,3-Tetramethylbutane	1	<chem>CC(C)(C)C(C)(C)C</chem>
Propane	1	<chem>CCC</chem>
Glycerol	2	<chem>C(C(CO)O)O</chem>
1,3-Diaminopropane	2	<chem>C(CN)CN</chem>
1,3-Propanedithiol	2	<chem>C(CS)CS</chem>
1,2,3-Trifluoropropane	2	<chem>C(C(CF)F)F</chem>
1,2,3-Trichloropropane	2	<chem>C(C(CCl)Cl)Cl</chem>
1,2,3-Tribromopropane	2	<chem>C(C(CBr)Br)Br</chem>
3-Aminopropanol	2	<chem>C(CN)CO</chem>
3-Mercaptopropanol	2	<chem>C(CO)CS</chem>
3-Fluoropropanol	2	<chem>C(CO)CF</chem>
3-Chloropropanol	2	<chem>C(CO)CCl</chem>
Diethylammonium	2	<chem>CC[NH2+]CC</chem>
Diethylamine	2	<chem>CCNCC</chem>
Diisopropylether	2	<chem>CC(C)OC(C)C</chem>
Diisopropyl sulfide	3	<chem>CC(C)SC(C)C</chem>
Dipropyl disulfide	3	<chem>CCCSSCCC</chem>
Citric acid	3	<chem>C(C(=O)O)C(CC(=O)O)(C(=O)O)O</chem>
Alpha-Ketoglutarate	3	<chem>C(CC(=O)[O-])C(=O)C(=O)[O-]</chem>
Succinate	3	<chem>C(CC(=O)[O-])C(=O)[O-]</chem>
Malic acid	3	<chem>C(C(C(=O)O)O)C(=O)O</chem>
Cysteine	6	<chem>C(C(C(=O)O)N)S</chem>
Ethyl propionate	3	<chem>CCC(=O)OCC</chem>
Arginine	6	<chem>C(CC(C(=O)O)N)CN=C(N)N</chem>
Glutamine	6	<chem>C(CC(=O)N)C(C(=O)O)N</chem>
Diisopropyl sulfoxide	3	<chem>CC(C)S(=O)C(C)C</chem>
Isopropyl sulfone	3	<chem>CC(C)S(=O)(=O)C(C)C</chem>
Isobutyric anhydride	3	<chem>CC(C)C(=O)OC(=O)C(C)C</chem>
Diisopropyl carbonate	3	<chem>CC(C)OC(=O)OC(C)C</chem>
N-Methyl-1-butanamine	3	<chem>CCCC=NC</chem>
2-Methyl-1-nitropropane	3	<chem>CC(C)C[N+](=O)[O-]</chem>
Fumaric acid	3	<chem>C(=CC(=O)O)C(=O)O</chem>
Hexa-1,3,5-triene	1	<chem>C=CC=CC=C</chem>
3-Pentanone	3	<chem>CCC(=O)CC</chem>
Butyraldehyde	3	<chem>CCCC=O</chem>
2-Butyne	1	<chem>CC#CC</chem>
Butyronitrile	3	<chem>CCCC#N</chem>
Hexamethylbenzene	4	<chem>CC1=C(C(=C(C(=C1)C)C)C)C</chem>
Salicylic acid	3	<chem>C1=CC=C(C(=C1)C(=O)O)O</chem>
Cumene	4	<chem>CC(C)C1=CC=CC=C1</chem>
p-Cresol	4	<chem>CC1=CC=C(C=C1)O</chem>

3-Methylanilinium	4	<chem>CC1=CC(=CC=C1)[NH3+]</chem>
3-Methylbenzaldehyde	4	<chem>CC1=CC(=CC=C1)C=O</chem>
p-Toluidine	4	<chem>CC1=CC=C(C=C1)N</chem>
3-Nitrotoluene	4	<chem>CC1=CC(=CC=C1)[N+](=O)[O-]</chem>
4-Fluorophenol	4	<chem>C1=CC(=CC=C1O)F</chem>
1,3,5-Trichlorobenzene	4	<chem>C1=C(C=C(C=C1Cl)Cl)Cl</chem>
1,3-Dibromobenzene	4	<chem>C1=CC(=CC(=C1)Br)Br</chem>
P-dioxane	5	<chem>C1COCCO1</chem>
D-Galactose	6	<chem>C(C1C(C(C(C(O1)O)O)O)O)O</chem>
THF	5	<chem>C1CCOC1</chem>
4-Aminopyridine	5	<chem>C1=CN=CC=C1N</chem>
1-Propanol	2	<chem>CCCO</chem>
1,3-Propanediol	2	<chem>C(O)CC(O)</chem>
Ethylamine	2	<chem>CCN</chem>
Propylamine	2	<chem>CCCN</chem>
1-Methylcytosine	6	<chem>CN1C=CC(=NC1=O)N</chem>
1-Methylthymine	6	<chem>CC1=CN(C(=O)NC1=O)C</chem>
1-Methyluracil	6	<chem>CN1C=CC(=O)NC1=O</chem>
9-Methyladenine	6	<chem>CN1C=NC2=C(N=CN=C21)N</chem>
9-Methylguanine	6	<chem>CN1C=NC2=C1N=C(NC2=O)N</chem>
Cytidine	6	<chem>C1=CN(C(=O)N=C1N)C2C(C(C(O2)CO)O)O</chem>
Deoxycytidine	6	<chem>C1C(C(OC1N2C=CC(=NC2=O)N)CO)O</chem>
Dimethylphosphate	6	<chem>COP(=O)(O)OC</chem>
Methylphosphate	6	<chem>COP(=O)([O-])[O-]</chem>
Ribose	6	<chem>C1C(C(C(C(O1)O)O)O)O</chem>
Trimethylphosphate	6	<chem>COP(=O)(OC)OC</chem>
Propan-2-amine	2	<chem>CC(C)N</chem>
2-chloropropane	2	<chem>CC(C)Cl</chem>
2-methylpropan-2-ol	2	<chem>CC(C)(C)O</chem>
2-methoxypropane	2	<chem>CC(C)OC</chem>
1,1,1-trifluoroethane	2	<chem>CC(F)(F)F</chem>
2-methylpropanal	3	<chem>CC(C)C=O</chem>
ethyl(trimethyl)azanium	2	<chem>CC[N+](C)(C)C</chem>
(2R)-2-aminopropanoic acid	3	<chem>CC(C(=O)O)N</chem>
2-methylpropanoic acid	3	<chem>CC(C)C(=O)O</chem>
methyl propanoate	3	<chem>CCC(=O)OC</chem>
hex-3-yne	1	<chem>CCC#CCC</chem>
2-ethoxypropane	2	<chem>CCOC(C)C</chem>
(2R)-2-hydroxypropanoic acid	3	<chem>CC(C(=O)O)O</chem>
(2S)-2-hydroxypropanoic	3	<chem>CC(C(=O)O)O</chem>

acid		
3-methylbutan-2-one	3	<chem>CC(C)C(=O)C</chem>
(E)-pent-2-enal	3	<chem>CCC=CC=O</chem>
(2S)-3-methylbut-3-en-2-ol	3	<chem>CC(C(=C)C)O</chem>
(E,2R)-hex-3-en-2-ol	3	<chem>CCC=CC(C)O</chem>
(E,2S)-hex-3-en-2-ol	3	<chem>CCC=CC(C)O</chem>
Ethyl dihydrogen phosphate	6	<chem>CCOP(=O)(O)O</chem>
(Z)-1-ethoxybut-1-ene	3	<chem>CCC=COCC</chem>
N-ethylpropanamide	3	<chem>CCC(=O)NCC</chem>
S-ethyl propanethioate	3	<chem>CCC(=O)SCC</chem>
propan-2-yl acetate	3	<chem>CC(C)OC(=O)C</chem>
(E)-pent-2-enoic acid	3	<chem>CCC=CC(=O)O</chem>
2-methylpentan-3-one	3	<chem>CCC(=O)C(C)C</chem>
(Z)-pent-2-enoic acid	3	<chem>CCC=CC(=O)O</chem>
propan-2-yl propanoate	3	<chem>CCC(=O)OC(C)C</chem>
N-propan-2-ylpropanamide	3	<chem>CCC(=O)NC(C)C</chem>
(2S)-N-ethyl-2-hydroxypropanamide	3	<chem>CCNC(=O)C(C)O</chem>
(2R)-N-ethyl-2-hydroxypropanamide	3	<chem>CCNC(=O)C(C)O</chem>
ethyl 2-methylpropanoate	3	<chem>CCOC(=O)C(C)C</chem>
(E)-4-oxohex-2-enal	3	<chem>CCC(=O)C=CC=O</chem>
3-oxopentanoic acid	3	<chem>CCC(=O)CC(=O)O</chem>
octa-3,5-diyne	1	<chem>CCC#CC#CCC</chem>
(E)-hex-3-enoic acid	3	<chem>CCC=CCC(=O)O</chem>
diethyl hydrogen phosphate	6	<chem>CCOP(=O)(O)OCC</chem>
(2S)-2-hydroxy-N-propan-2-ylpropanamide	3	<chem>CC(C)NC(=O)C(C)O</chem>
(2R)-2-hydroxy-N-propan-2-ylpropanamide	3	<chem>CC(C)NC(=O)C(C)O</chem>
4-ethylphenol	3	<chem>CCC1=CC=C(C=C1)O</chem>
(2S,3E,5E)-octa-3,5-dien-2-ol	3	<chem>CCC=CC=CC(C)O</chem>
(2R,3E,5E)-octa-3,5-dien-2-ol	3	<chem>CCC=CC=CC(C)O</chem>
(E)-4-oxohex-2-enoic acid	3	<chem>CCC(=O)C=CC(=O)O</chem>
2-(propanoylamino)acetic acid	3	<chem>CCC(=O)NCC(=O)O</chem>
5-ethylbenzene-1,3-diol	4	<chem>CCC1=CC(=CC(=C1)O)O</chem>
(2R)-2-(propanoylamino)propanoic acid	3	<chem>CCC(=O)NC(C)C(=O)O</chem>
(2S)-2-	3	<chem>CCC(=O)NC(C)C(=O)O</chem>

(propanoylamino)propanoic acid		
S-ethyl 3-oxopentathioate	3	<chem>CCC(=O)CC(=O)SCC</chem>
2,5-diethyl-3,4-dimethylfuran	5	<chem>CCC1=C(C(=C(O1)CC)C)C</chem>
[(E)-3-methylpent-2-enyl] propanoate	3	<chem>CCC(=CCOC(=O)CC)C</chem>
ethyl [(2R,3R,5S,6R)-2,3,4,5,6-pentahydroxycyclohexyl] hydrogen phosphate	6	<chem>CCOP(=O)(O)OC1C(C(C(C(C1O)O)O)O)O</chem>
Cyclopropane	1	<chem>C1CC1</chem>
Cyclobutane	1	<chem>C1CCC1</chem>
Methyldiphosphate	6	<chem>CO[P](O[P](=O)([O-])[O-])(=O)[O-]</chem>
Methyltriphosphate	6	<chem>CO[P](O[P](O[P]([O-])(=O)[O-])(=O)[O-])(=O)[O-]</chem>
D-Alaninate	6	<chem>CC(C(=O)[O-])N</chem>
D-Alaninium	6	<chem>CC(C(=O)O)[N+]</chem>
D-Alanine zwitterion	6	<chem>CC(C(=O)[O-])[N+]</chem>
2-methylpropanoate	3	<chem>CC(C)C(=O)[O-]</chem>
(2R)-2-hydroxypropanoate	3	<chem>CC(C(=O)[O-])O</chem>
(2S)-2-hydroxypropanoate	3	<chem>CC(C(=O)[O-])O</chem>
Ethyl hydrogen phosphate	6	<chem>CCOP(=O)([O-])O</chem>
Ethyl phosphate	6	<chem>CCOP(=O)([O-])[O-]</chem>
(E)-pent-2-enoate	3	<chem>CCC=CC(=O)[O-]</chem>
(Z)-pent-2-enoate	3	<chem>CCC=CC(=O)[O-]</chem>
3-oxopentanoate	3	<chem>CCC(=O)CC(=O)[O-]</chem>
(E)-hex-3-enoate	3	<chem>CCC=CCC(=O)[O-]</chem>
Diethyl phosphate	6	<chem>CCOP(=O)([O-])OCC</chem>
2-(propanoylamino)acetate	3	<chem>CCC(=O)NCC(=O)[O-]</chem>
(2R)-2-(propanoylamino)propanoate	3	<chem>CCC(=O)NC(C)C(=O)[O-]</chem>
Methanethiolate	2	<chem>C[S-]</chem>
Thioethoxide	2	<chem>CC[S-]</chem>
Propane-2-thiolate	2	<chem>CC([S-])C</chem>
N,N-Diethylethanesulfonamide	3	<chem>CCN(CC)S(=O)(=O)CC</chem>
Methanesulfonamide	3	<chem>CS(=O)(=O)N</chem>
Propan-2-aminium	2	<chem>CC(C)[N+]</chem>
D-deoxyribose	6	<chem>O1[C@@H]([C@@H](O[H])C[C@@H]1O[H])CO[H]</chem>

CH3I	2	IC
CH2I2	2	ICI
CHI3	2	IC(I)I
CI4	2	IC(I)(I)I
CBr4	2	BrC(Br)(Br)Br
Benzotrifluoride	4	C(C1=CC=CC=C1)(F)(F)F
Benzotrichloride	4	C(C1=CC=CC=C1)(Cl)(Cl)Cl
111-trichloropropane	2	ClC(Cl)(Cl)CC
111-trifluoropropane	2	FC(F)(F)CC
222-trifluoroethylbenzene	4	FC(F)(F)CC1=CC=CC=C1
222-trichloroethylbenzene	4	ClC(Cl)(Cl)CC1=CC=CC=C1
Tribromoethylbenzene	4	C1(=CC=CC=C1)CC(Br)(Br)Br
Benzyl iodide	4	C1(=CC=CC=C1)CI
Iodobenzene	4	C1(=CC=CC=C1)I
1,1,1-Tribromopropane	2	C(CC)(Br)(Br)Br
1,1,1,3,3,3-Hexafluoropropane	2	C(CC(F)(F)F)(F)(F)F
1,1,1,3,3,3-Hexachloropropane	2	C(CC(Cl)(Cl)Cl)(Cl)(Cl)Cl
1-Phenylpiperazinium	4	C1=CC=C(C=C1)N2CC[N+]CC2
1-Ethyl-1-methylpiperidin-1-ium	2	C1CCCC[N+]1(C)CC
Tribromomethylbenzene	4	C(C1=CC=CC=C1)(Br)(Br)Br
Biphenyl	7	C1=CC=CC=C1C2=CC=CC=C2
Diphenylmethane	7	C1=CC=CC=C1CC2=CC=CC=C2
1,1-Diphenylethane	7	C1=CC=CC=C1C(C2=CC=CC=C2)C
2-Phenoxypyridine	7	C1=CC=CC=C1OC2=CC=CC=N2
2-Anilinopyridine	7	C1=CC=CC=C1NC2=NC=CC=C2
Phenyl-2-pyridyl-methylamine	7	C1=CC=CC=C1N(C)C2=NC=CC=C2
Diphenylamine	7	C1=CC=CC=C1NC2=CC=CC=C2
Caprolactam	3	C1(CCCCCN1)=O
N-Methylcaprolactam	3	C1(CCCCCN1C)=O
1,3,4,5-Tetrahydro-2H-1-benzazepin-2-one	4	C2(CCCC1=CC=CC=C1N2[H])=O
2,3,4,5-Tetrahydro-benzo[c]azepin-1-one	4	C2CCC1=CC=CC=C1C(N2[H])=O
1-Methyl-1,3,4,5-tetrahydro-2H-1-benzazepin-2-one	4	C1=CC2=C(C=C1)CCCC(N2C)=O
5-Methyl-1H-benzo[e][1,4]diazepin-2(3H)-one	4	C2(CN=C(C1=CC=CC=C1N2[H])C)=O

Benzamide	4	<chem>C1=CC(=CC=C1)C(N)=O</chem>
1-Benzoylpiperidine	4	<chem>C1=CC(=CC=C1)C(N2CCCCC2)=O</chem>
(2R)-1-Benzoyl-2alpha-methylpiperidine	4	<chem>C1=CC(=CC=C1)C(=O)N2[C@@H](CCCC2)C</chem>
2-(1Methyl-Imidazol-2-yl)pyrimidine	7	<chem>C1=NC(=NC=C1)C2=[N](C=C[N]2)C</chem>
2-(5-Methylpyrazol-1-yl)pyrimidine	7	<chem>C1=NC(=NC=C1)[N]2N=CC=C2C</chem>
3-(2-Pyridyl)furan	7	<chem>C1=CC(=NC=C1)C2=COC=C2</chem>
2-(2-Pyridyl)thiazole	7	<chem>C1=CC(=NC=C1)C2=NC=CS2</chem>
Phenetole	4	<chem>C1(=CC=CC=C1)OCC</chem>
1-Methyl-2-phenyl-1H-pyrrole	7	<chem>[N]1(C(=CC=C1)C2=CC=CC=C2)C</chem>
2-Phenyl-1H-pyrrole	7	<chem>[N]1(C(=CC=C1)C2=CC=CC=C2)[H]</chem>
1-Phenylpyrazole	7	<chem>[N]1(N=CC=C1)C2=CC=CC=C2</chem>
Methyl2-(methylamino)benzoate	4	<chem>O(C(=O)C1=CC=CC=C1N(C)[H])C</chem>
2-Aminobenzophenone	7	<chem>O=C(C1=CC=CC=C1N([H])[H])C2=CC=CC=C2</chem>
(2-(methylamino)phenyl)phenyl-Methanone	7	<chem>O=C(C1=CC=CC=C1N(C)[H])C2=CC=CC=C2</chem>
Dimethylaminobenzophenone	7	<chem>O=C(C1=CC=CC=C1N(C)C)C2=CC=CC=C2</chem>
2-Aminobiphenyl	7	<chem>N(C1=CC=CC=C1C2=CC=CC=C2)([H])[H]</chem>
2-(Pyridin-2-yl)aniline	7	<chem>N1=CC=CC=C1C2=CC=CC=C2N([H])[H]</chem>
N-Methyl-2-(2-pyridyl)aniline	7	<chem>N(C1=CC=CC=C1C2=CC=CC=N2)(C)[H]</chem>
N,N-Dimethyl-2-pyridin-2-ylaniline	7	<chem>N(C1=CC=CC=C1C2=CC=CC=N2)(C)C</chem>
Ethylcyclopropane	1	<chem>C1C(C1)CC</chem>
1-(Hydroxymethyl)cyclopropanol	2	<chem>C1C(C1)(CO)O</chem>
N-Cyclopropylacetamide	3	<chem>C1C(C1)NC(=O)C</chem>
N-Methylcyclopropanecarboxamide	3	<chem>C1C(C1)C(=O)NC</chem>
Ethylcyclopropanecarboxylate	3	<chem>C1C(C1)C(=O)OCC</chem>
Cyclopropylpropanoate	3	<chem>C1C(C1)OC(CC)=O</chem>
Methyl1-fluorocyclopropanecarboxyl	3	<chem>C1C(C1)(C(=O)OC)F</chem>

ate		
1-Fluoro-N-methylcyclopropane-1-carboxamide	3	<chem>FC1(CC1)C(=O)N(C)[H]</chem>
1-Cyclopropyl-3-methylurea	3	<chem>C1C(C1)NC(=O)N(C)[H]</chem>
Ethylcyclobutane	1	<chem>C1C(CC1)CC</chem>
3-ethyl-3-methyl-oxetane	2	<chem>C1C(CO1)(CC)C</chem>
3-(Hydroxymethyl)oxetan-3-ol	2	<chem>C1C(CO1)(CO)O</chem>
Thietane	2	<chem>C1CCS1</chem>
2,3-Diethylthietane	2	<chem>C1(C(CS1)CC)CC</chem>
Ethylcyclopentane	1	<chem>C1(CCCC1)CC</chem>
Tetrahydrothiophene	2	<chem>C1CCCCS1</chem>
Pyrrole	5	<chem>C1=CC=C[N]1</chem>
N-Methyl-1H-imidazole-2-carboxamide	5	<chem>C1=C[N]C(=N1)C(=O)N(C)[H]</chem>
N,1-Dimethylimidazole-2-carboxamide	5	<chem>C1=C[N](C(=N1)C(=O)N(C)[H])C</chem>
Oxazole	5	<chem>C1=CN=CO1</chem>
N-Methyl-1,3-oxazole-2-carboxamide	5	<chem>C1(=NC=CO1)C(=O)NC</chem>
Thiazole	5	<chem>C1=NC=CS1</chem>
N-Methyl-1,3-thiazole-2-carboxamide	5	<chem>C1(=NC=CS1)C(=O)NC</chem>
Thiophene	5	<chem>C1=CC=CS1</chem>
N-Methylthiophene-2-carboxamide	5	<chem>C1(=CC=CS1)C(=O)NC</chem>
2-Acetylthiophene	5	<chem>C1(=CC=CS1)C(=O)C</chem>
N-methylfuran-2-carboxamide	5	<chem>C1(=CC=CO1)C(=O)N(C)[H]</chem>
N-Methyl-N-thiophen-2-ylacetamide	5	<chem>C1(=CC=CS1)N(C(C)=O)C</chem>
N-(Furan-2-yl)-N-methylacetamide	5	<chem>C1(=CC=CO1)N(C(C)=O)C</chem>
N-(Furan-2-yl)acetamide	5	<chem>C1(=CC=CO1)NC(C)=O</chem>
Pyrazole	5	<chem>C1=CC=N[N]1</chem>
3-Methoxy-1h-pyrazole	5	<chem>C1=CC(=N[N]1)OC</chem>
5-Methoxy-1-methyl-1H-pyrazole	5	<chem>C1(=CC=N[N]1C)OC</chem>
N,N,1-Trimethyl-1H-imidazole-2-carboxamide	5	<chem>C1=CN=C([N]1C)C(=O)N(C)C</chem>
N,1-dimethylpyrrole-2-carboxamide	5	<chem>C1=CC=C([N]1C)C(=O)NC</chem>

1H-Pyrrol-3-ol	5	<chem>C1=CC(=C[N]1)O</chem>
3-Methoxy-1h-pyrrole	5	<chem>C1=CC(=C[N]1)OC</chem>
1H-Pyrrol-3-amine	5	<chem>C1=CC(=C[N]1)N</chem>
3-Fluoro-1H-pyrrole	5	<chem>C1=CC(=C[N]1)F</chem>
3-Chloro-1H-pyrrole	5	<chem>C1=CC(=C[N]1)Cl</chem>
Anisole	5	<chem>C1(=CC=CC=C1)OC</chem>
2-Methoxypyridine	5	<chem>C1(=NC=CC=C1)OC</chem>
(Trifluoromethoxy)benzene	4	<chem>C1(=CC=CC=C1)OC(F)(F)F</chem>
(Trichloromethoxy)benzene	4	<chem>C1(=CC=CC=C1)OC(Cl)(Cl)Cl</chem>
1-ethyl-2(1H)-Pyridinone	5	<chem>C1(C=CC=CN1CC)=O</chem>
1-Cyclopropyl-1,2-dihydropyridine-2-one	5	<chem>C1(C=CC=CN1C2CC2)=O</chem>
6-Ethyl-1H-pyridin-2-one	5	<chem>C1(C=CC=C(N1)CC)=O</chem>
3-Ethylpyridin-2-ol	5	<chem>C1(C(=CC=CN1[H])CC)=O</chem>
2-ethyl-1,3-oxazole	5	<chem>C1(=NC=CO1)CC</chem>
2-Ethylthiazole	5	<chem>C1(=NC=CS1)CC</chem>
N,N-Dimethylaniline	4	<chem>C1(=CC=CC=C1)N(C)C</chem>
Cyclopropylbenzene	4	<chem>C1(=CC=CC=C1)C2CC2</chem>
2-Cyclopropylpyridine	5	<chem>C1(=NC=CC=C1)C2CC2</chem>
2-Cyclopropylpyrimidine	5	<chem>C1(=NC=CC=N1)C2CC2</chem>
Cyclopentylbenzene	4	<chem>C1=CC(=CC=C1)C2CCCC2</chem>
Benzylmethylether	4	<chem>C1=CC(=CC=C1)COC</chem>
N-Methylacetanilide	4	<chem>C1=CC(=CC=C1)N(C(C)=O)C</chem>
Acetanilide	4	<chem>C1=CC(=CC=C1)N(C(C)=O)[H]</chem>
N-Methylbenzenesulfonamide	4	<chem>C1=CC(=CC=C1)[S](=O)(=O)NC</chem>
Ethylphenylsulfone	4	<chem>C1=CC(=CC=C1)[S](=O)(=O)CC</chem>
N,N-dimethyl-1H-imidazole-2-sulfonamide	5	<chem>C1=CN=C([N]1)[S](=O)(=O)N(C)C</chem>
N,N-dimethyl-2-thiophenesulfonamide	5	<chem>C1=CC=C([S](=O)(=O)N(C)C)S1</chem>
Phenyltrifluoromethylsulfone	4	<chem>C1(=CC=CC=C1)[S](C(F)(F)F)(=O)=O</chem>
trichloromethylphenylsulfone	4	<chem>C1(=CC=CC=C1)[S](C(Cl)(Cl)Cl)(=O)=O</chem>
Thiopyran	5	<chem>C1=CC=CCS1</chem>
2H-Pyran	5	<chem>C1=CC=CCO1</chem>
1,4-Benzoquinone	5	<chem>O=C1C=CC(=O)C=C1</chem>
S-Ethylethanethioate	3	<chem>CC(=O)SCC</chem>
Thioaceticacid	3	<chem>CC(=O)S</chem>
Thioacetate	3	<chem>CC(=O)[S-]</chem>
1H-Tetrazole	5	<chem>C1=N[N]N=N1</chem>
1,2,3-Triaza-4-	5	<chem>C1=N[N-]N=N1</chem>

azanidacyclopenta-2,5-diene		
Ethoxyacetate	3	<chem>CC(=O)OOCC</chem>
Peraceticacid	3	<chem>CC(=O)OOH</chem>
Ethaneperoxoate	3	<chem>CC(=O)O[O-]</chem>
1-Ethyl-2-pyrrolidinone	3	<chem>C1CCC(=O)N1CC</chem>
Pyrrolidinium	2	<chem>C1CCC[N+]1</chem>
1-Ethylpyrrolidinium	2	<chem>C1CCC[N+]1CC</chem>
Carbonate	3	<chem>C(=O)([O-])[O-]</chem>
Bicarbonate	3	<chem>C(=O)([OH])[O-]</chem>
3-Hydroxytetrahydro-2h-pyran-2-one	3	<chem>C1(C(CCCO1)O)=O</chem>
2-Piperidone	3	<chem>C1(CCCCN1)=O</chem>
alpha-Hydroxy-gamma-butyrolactone	3	<chem>C1(C(CCO1)O)=O</chem>

Table S2. Training set for out-of-plane bending

The training set for out-of-plane bending has been shown with their name, the number of conformations chosen for each molecule, and the related group number as mentioned. (The equilibrium structure has been counted)

Index	Name of molecule	Number of configurations
1	N-Methylacetamide	13
2	Acetic acid	7
3	Acetamide	7
4	Uracil	25
5	Pyridine	19
6	Benzene	7
7	Fluorobenzene	25
8	Chlorobenzene	25
9	Bromobenzene	25
10	Imidazole	25
11	Phenol	25
12	Indole	55
13	1H-imidazol-3-ium	19
14	Guanidine	19
15	Acetate	7
16	Formimidamide	13
17	Formamide	13
18	Formicacid	7
19	7-Methylindole	55
20	Methylguanidine	25
21	4-Methylimidazole	25
22	2-Aminopyridine	31
23	2-Pyridone	37
24	Pyrazine	7
25	Thymine	37
26	Adenine	43
27	Formaldehyde	7
28	Methyl benzene	25
29	Acetone	7
30	Naphthalene	19
31	Guanine	49
32	Acetaldehyde	7
33	Cytosine	37
34	Phenolate	25
35	Aniline	7
36	Acetic Anhydride	7
37	Carbamic acid	7
38	3-Methylindole	55

39	4-Methylimidazole	25
40	1-Propylguanidinium	19
41	Propionamide	13
42	Propionic acid	7
43	Formate	7
44	Propionyl chloride	7
45	Propionyl fluoride	7
46	Propionyl bromide	7
47	Diethyl carbonate	7
48	Ethyl hydrogen carbonate	7
49	Diethoxymethane	7
50	Benzonitrile	19
51	Propionate	7
52	Propionaldehyde	7
53	N-Ethylformamide	13
54	Dimethyl formamide	13
55	1,3-Benzodioxole	19
56	Ethanamine	7
57	Ethanimine	7
58	2-Propanimine	7
59	Ethyl Acetoacetate	13
60	Hydrogen oxalate	13
61	Oxalate	7
62	Malonic acid	7
63	Hydrogen malonate	13
64	Malonate	7
65	2-Oxobutanoic Acid	13
66	2-Oxobutanoate	13
67	Dipropionamide	13
68	Nitroethane	7
69	Nitrobenzene	31
70	Ethyl N-ethyl-N-methylcarbamate	7
71	Methylcarbamic acid	13
72	Carbamate	13
73	Benzenediazonium	7
74	Azobenzene	7
75	Benzene sulfonic acid	19
76	Benzene sulfonate	25
77	Ethyl acetate	7
78	Phenyl thiocyanate	25
79	Butadiene	7
80	Acrolein	13
81	Acetone oxime	7

82	Benzyl alcohol	7
83	Ethylbenzene	7
84	Benzylamine	7
85	Benzaldehyde	31
86	Benzoic acid	25
87	Benzoate	31
88	AcrylicAcid	13
89	Acrylate	13
90	L-Alanine	7
91	Phenylazanium	25
92	Glyoxal	7
93	2-Methyl-1-butene	7
94	(E)-but-2-ene	7
95	Glycolic acid	7
96	Glycolate	7
97	Malonaldehyde	7
98	Urea	13
99	Citric acid	19
100	Alpha-Ketoglutarate	19
101	Succinate	7
102	Malic acid	13
103	Cysteine	7
104	Ethyl propionate	7
105	Arginine	25
106	Glutamine	19
107	Isobutyric anhydride	7
108	Diisopropyl carbonate	7
109	N-Methyl-1-butanamine	7
110	2-Methyl-1-nitropropane	7
111	Fumaric acid	12
112	Hexa-1,3,5-triene	13
113	3-Pentanone	7
114	Butyraldehyde	7
115	Hexamethylbenzene	7
116	Salicylic acid	43
117	Cumene	7
118	p-Cresol	25
119	3-Methylanilinium	37
120	3-Methylbenzaldehyde	43
121	p-Toluidine	30
122	3-Nitrotoluene	13
123	4-Fluorophenol	13
124	1,3,5-Trichlorobenzene	13

125	1,3-Dibromobenzene	25
126	4-Aminopyridine	19
127	1-Methylcytosine	37
128	1-Methylthymine	37
129	1-Methyluracil	37
130	9-Methyladenine	31
131	9-Methylguanine	43
132	Cytidine	37
133	Deoxycytidine	37
134	(2R)-2-aminopropanoic acid	7
135	2-methylpropanoic acid	7
136	methyl propanoate	7
137	(2R)-2-hydroxypropanoic acid	7
138	(2S)-2-hydroxypropanoic acid	7
139	3-methylbutan-2-one	7
140	(E)-pent-2-enal	19
141	(2S)-3-methylbut-3-en-2-ol	7
142	(E,2R)-hex-3-en-2-ol	13
143	(E,2S)-hex-3-en-2-ol	13
144	(Z)-1-ethoxybut-1-ene	13
145	N-ethylpropanamide	13
146	S-ethyl propanethioate	7
147	propan-2-yl acetate	7
148	(E)-pent-2-enoic acid	19
149	2-methylpentan-3-one	7
150	(Z)-pent-2-enoic acid	19
151	propan-2-yl propanoate	7
152	N-propan-2-ylpropanamide	13
153	(2S)-N-ethyl-2-hydroxypropanamide	13
154	(2R)-N-ethyl-2-hydroxypropanamide	13
155	ethyl 2-methylpropanoate	7
156	(E)-4-oxohex-2-enal	25
157	3-oxopentanoic acid	13
158	(E)-hex-3-enoic acid	19
159	(2S)-2-hydroxy-N-propan-2-ylpropanamide	13
160	(2R)-2-hydroxy-N-propan-2-ylpropanamide	13
161	4-ethylphenol	13
162	(2S,3E,5E)-octa-3,5-dien-2-ol	25
163	(2R,3E,5E)-octa-3,5-dien-2-ol	25
164	(E)-4-oxohex-2-enoic acid	25
165	2-(propanoylamino)acetic acid	19

166	5-ethylbenzene-1,3-diol	25
167	(2R)-2-(propanoylamino)propanoic acid	19
168	(2S)-2-(propanoylamino)propanoic acid	19
169	S-ethyl 3-oxopentanethioate	13
170	2,5-diethyl-3,4-dimethylfuran	13
171	[(E)-3-methylpent-2-enyl] propanoate	19
172	D-Alaninate	7
173	D-Alaninium	7
174	D-Alanine zwitterion	7
175	2-methylpropanoate	7
176	(2R)-2-hydroxypropanoate	7
177	(2S)-2-hydroxypropanoate	7
178	(E)-pent-2-enoate	7
179	(Z)-pent-2-enoate	19
180	3-oxopentanoate	13
181	(E)-hex-3-enoate	19
182	2-(propanoylamino)acetate	19
183	(2R)-2-(propanoylamino)propanoate	19
184	Benzotrifluoride	7
185	Benzotrichloride	7
186	2,2,2-trifluoroethylbenzene	7
187	2,2,2-trichloroethylbenzene	7
188	Tribromoethylbenzene	7
189	Iodobenzene	7
190	1-Phenylpiperazinium	6
191	Tribromomethylbenzene	7
192	Biphenyl	13
193	Diphenylmethane	7
194	2-Phenoxy pyridine	13
195	2-Anilinopyridine	13
196	Phenyl-2-pyridyl-methylamine	13
197	Diphenylamine	7
198	Caprolactam	7
199	N-Methylcaprolactam	7
200	1,3,4,5-Tetrahydro-2H-1-benzazepin-2-one	19
201	2,3,4,5-Tetrahydro-benzo[c]azepin-1-one	19
202	1-Methyl-1,3,4,5-tetrahydro-2H-1-benzazepin-2-one	19
203	5-Methyl-1H-benzo[e][1,4]diazepin-2(3H)-one	25
204	Benzamide	13
205	1-Benzoylpiperidine	13

206	(2R)-1-Benzoyl-2alpha-methylpiperidine	13
207	2-(1Methyl-Imidazol-2-yl)pyrimidine	37
208	2-(5-Methylpyrazol-1-yl)pyrimidine	43
209	3-(2-Pyridyl)furan	55
210	2-(2-Pyridyl)thiazole	25
211	Phenetole	7
212	1-Methyl-2-phenyl-1H-pyrrole	31
213	2-Phenyl-1H-pyrrole	37
214	1-Phenylpyrazole	31
215	Methyl2-(methylamino)benzoate	13
216	2-Aminobenzophenone	37
217	(2-(methylamino)phenyl)phenyl-Methanone	31
218	2-Aminobiphenyl	7
219	2-(Pyridin-2-yl)aniline	43
220	N-Methyl-2-(2-pyridyl)aniline	37
221	N,N-Dimethyl-2-pyridin-2-ylaniline	7
222	1-Cyclopropyl-3-methylurea	7
223	Pyrrole	13
224	N-Methyl-1H-imidazole-2-carboxamide	25
225	N,1-Dimethylimidazole-2-carboxamide	25
226	Oxazole	19
227	N-Methyl-1,3-oxazole-2-carboxamide	25
228	Thiazole	19
229	N-Methyl-1,3-thiazole-2-carboxamide	25
230	Thiophene	13
231	N-Methylthiophene-2-carboxamide	31
232	2-Acetylthiophene	31
233	N-methylfuran-2-carboxamide	31
234	N-Methyl-N-thiophen-2-ylacetamide	25
235	N-(Furan-2-yl)-N-methylacetamide	31
236	N-(Furan-2-yl)acetamide	31
237	Pyrazole	19
238	3-Methoxy-1h-pyrazole	19
239	5-Methoxy-1-methyl-1H-pyrazole	19
240	N,N,1-Trimethyl-1H-imidazole-2-carboxamide	25
241	N,1-dimethylpyrrole-2-carboxamide	19
242	1H-Pyrrol-3-ol	19
243	3-Methoxy-1h-pyrrole	19
244	1H-Pyrrol-3-amine	19
245	3-Fluoro-1H-pyrrole	7
246	3-Chloro-1H-pyrrole	7

247	Anisole	7
248	2-Methoxypyridine	7
249	(Trifluoromethoxy)benzene	7
250	(Trichloromethoxy)benzene	7
251	1-ethyl-2(1H)-Pyridinone	31
252	1-Cyclopropyl-1,2-dihydropyridine-2-one	31
253	6-Ethyl-1H-pyridin-2-one	7
254	3-Ethylpyridin-2-ol	13
255	2-ethyl-1,3-oxazole	19
256	2-Ethylthiazole	19
257	N,N-Dimethylaniline	7
258	Cyclopropylbenzene	7
259	2-Cyclopropylpyridine	7
260	2-Cyclopropylpyrimidine	19
261	Cyclopentylbenzene	7
262	N-Methylacetanilide	7
263	Acetanilide	7
264	N-Methylbenzenesulfonamide	7
265	Ethylphenylsulfone	7
266	N,N-dimethyl-1H-imidazole-2-sulfonamide	13
267	N,N-dimethyl-2-thiophenesulfonamide	25
268	Phenyltrifluoromethylsulfone	7
269	trichloromethylphenylsulfone	7
270	Thiopyran	25
271	2H-Pyran	25
272	1,4-Benzoquinone	13
273	S-Ethylethanethioate	7
274	Thioaceticacid	7
275	Thioacetate	7
276	1H-Tetrazole	7
277	1,2,3-Triaza-4-azanidacyclopenta-2,5-diene	7
278	Ethoxyacetate	7
279	Peraceticacid	7
280	Ethaneperoxoate	7
281	1-Ethyl-2-pyrrolidinone	7
282	Carbonate	6
283	Bicarbonate	6
284	3-Hydroxytetrahydro-2h-pyran-2-one	6
285	2-Piperidone	6
286	alpha-Hydroxy-gamma-butyrolactone	6

Table S3. The molecules in the validation set

The validation set has been shown with their name, their classified group, and the SMILE strings (120 molecules). We have 7 groups: (1).alkanes and aliphatic rings; (2).molecules comprised of only single bonds; (3).molecules with double bonds or triple bonds; (4).benzene derivatives; (5).heterocyclics; (6).bio-fragments; (7).combinations of multiple aromatic cycles.

Name	Group	SMILE
1,2-Ethanediol	2	<chem>(CO)O</chem>
1-Amino-2-butanol	2	<chem>C(C(CN)O)C</chem>
1,2-Butanediamine	2	<chem>C(C(CN)N)C</chem>
1-Chloro-3-fluoropropane	2	<chem>C(CCCl)F</chem>
1-Bromo-3-chloropropane	2	<chem>C(CCCl)Br</chem>
1-Bromo-3-fluoropropane	2	<chem>C(CCF)Br</chem>
1,3-Diodopropane	2	<chem>C(CCI)I</chem>
Tetramethylammonium	2	<chem>C[N+](C)(C)C</chem>
2-Hydroxyethyltrimethylammonium	2	<chem>C[N+](CCO)C</chem>
3,5-Dihydroxycyclohexanamine	2	<chem>C1C(CC(CC1O)O)N</chem>
1,3,5-Trifluorocyclohexane	2	<chem>C1C(CC(CC1F)F)F</chem>
Cyclopentanemethanol	2	<chem>C1(CCCC1)CO</chem>
Cyclopentanemethylamine	2	<chem>C1(CCCC1)CN</chem>
1,3-Diethylcyclobutane	2	<chem>C1C(CC1CC)CC</chem>
2,4-Diethyloxetane	2	<chem>C1(CC(O1)CC)CC</chem>
1,2,3-Trimethylcyclopropane	2	<chem>C1(C(C1C)C)C</chem>
Ethylisobutyl disulfide	2	<chem>C(SSCC)C(C)C</chem>
1,2-Dimethoxyethane	2	<chem>COCCOC</chem>
2-Methylpropane-1-thiolate	2	<chem>CC(C)CS-</chem>
Hexa-2,4-diene	3	<chem>C(C=CC)=CC</chem>
3-Methyl-2-butenal	3	<chem>C(=CC=O)(C)C</chem>
3-Ethylhexane-2,4-dione	3	<chem>C(C(C(=O)C)CC)(=O)CC</chem>
5-Oxohexanal	3	<chem>C(CCCC(=O)[H])(=O)C</chem>
Succinamide	3	<chem>C(CC(=O)N)C(=O)N</chem>
Diethyloxalate	3	<chem>C(C(=O)OCC)(=O)OCC</chem>
Succinyl fluoride	3	<chem>C(CCC(=O)F)(F)=O</chem>
Succinyl chloride	3	<chem>C(CCC(=O)Cl)(Cl)=O</chem>
Butanedioyldibromide	3	<chem>C(CCC(=O)Br)(Br)=O</chem>
Isovaleronitrile	3	<chem>CC(CC#N)C</chem>
4-Methyl-1-pentyne	3	<chem>CC(CC#C)C</chem>
N-Ethylbutane-2-imine	3	<chem>C(=NCC)(CC)C</chem>
Butan-2-imine	3	<chem>C(=N)(CC)C</chem>

Monomethylsuccinate	3	<chem>C(CCC(=O)OC)(=O)O</chem>
Monomethylsuccinate-ion	3	<chem>C(CCC(=O)OC)(=O)[O-]</chem>
2,3-Dimethyl-2-butenic acid	3	<chem>C(=C(C)C)(C(=O)O)C</chem>
Thioisobutyric acid	3	<chem>C(C([S][H])=O)(C)C</chem>
2-Methylpropanethioate	3	<chem>C(C([S-])=O)(C)C</chem>
3-Methylbutanoylacetate	3	<chem>C(C(=O)OC(C)=O)C(C)C</chem>
1-Ethyl-1-methylurea	3	<chem>C(=O)(N(C)CC)N</chem>
Cyclohexylammonium	2	<chem>C1(CCCCC1)[N+]</chem>
1,4-Dimethylpiperazine	3	<chem>C1CN(CCN1C)C</chem>
Isobutylpropylsulfoxide	3	<chem>C([S])(CC(C)C)=O)CC</chem>
2-Methyl-1-propylsulfonylpropane	3	<chem>C([S])(CC(C)C)(=O)=O)CC</chem>
Ethyl-2-methylpropane-1-sulfonate	3	<chem>[S](CC(C)C)(=O)(=O)OCC</chem>
Isopropylmethanesulfonate	3	<chem>[S](CC(C)C)(=O)(=O)[O-]</chem>
2-Methyl-1-nitropropane	3	<chem>CC(C[N])(=O)=O)C</chem>
Isopropylphosphate	6	<chem>CC(C)O[P](=O)([O-])[O-]</chem>
Urethane	3	<chem>C(OC(=O)N)C</chem>
Propan-2-yl-hydrogencarbonate	3	<chem>CC(C)OC(=O)O</chem>
D-gluconic acid	6	<chem>O([C@@H]([C@H](O[H])[C@@H](O[H])C(O[H])=O)[C@H](O[H])CO[H])[H]</chem>
Gluconolactone	6	<chem>O1[C@@H]([C@@H](O[H])[C@H](O[H])[C@@H](O[H])C1=O)CO[H]</chem>
N-Methylsalicylamide	4	<chem>C1(=CC=CC=C1C(=O)NC)O</chem>
2-Chloroacetanilide	4	<chem>C1(=CC=CC=C1NC(C)=O)Cl</chem>
2-Fluoroanisole	4	<chem>C1(=CC=CC=C1OC)F</chem>
2-Methylanisole	4	<chem>C1(=CC=CC=C1OC)C</chem>
3-Fluoro-2-methoxyphenol	4	<chem>C1(=C(C=CC=C1O)F)OC</chem>
N,2,6-Trimethylaniline	4	<chem>C1(=C(C=CC=C1C)C)NC</chem>
3-methyl-2-(methylamino)phenol	4	<chem>C1(=C(C=CC=C1C)O)NC</chem>
2-Hydroxyacetophenone	4	<chem>C1(=CC=CC=C1C(C)=O)O</chem>
2-Methoxybenzamide	4	<chem>C1=CC=CC(=C1OC)C(=O)N</chem>
Phthalamide	4	<chem>C1=CC=CC(=C1C(=O)N)C(=O)N</chem>
2-Aminobenzamide	4	<chem>C1(=CC=CC=C1C(=O)N)N</chem>
2,4,6-Trinitrobenzoic acid	4	<chem>C1(=CC(=C(C(=C1)[N+](=O)[O-])C(=O)O)[N+](=O)[O-])[N+](=O)[O-]</chem>
2,4,6-Trinitrobenzoate	4	<chem>C1(=CC(=C(C(=C1)[N+](=O)[O-])C(=O)[O-])[N+](=O)[O-])[N+](=O)[O-]</chem>
3,5-Dimethylbenzenaminium	4	<chem>C1(=CC(=CC(=C1)C)C)[N+]</chem>

3,5-Dimethylbenzenesulfonicacid	4	<chem>C1(=CC(=CC(=C1)C)C)[S](O)(=O)=O</chem>
3,5-Dimethylbenzenesulfonate	4	<chem>C1(=CC(=CC(=C1)C)C)[S]([O-])(=O)=O</chem>
2-Methylbenzotrifluoride	4	<chem>C1=CC=CC(=C1C(F)(F)F)C</chem>
2-Methylbenzotrichloride	4	<chem>C1=CC=CC(=C1C(Cl)(Cl)Cl)C</chem>
3,5-Dichlorotoluene	4	<chem>C1=C(C=C(C=C1Cl)C)Cl</chem>
3,5-Difluorotoluene	4	<chem>C1=C(C=C(C=C1F)C)F</chem>
3,5-Dibromotoluene	4	<chem>C1=C(C=C(C=C1Br)C)Br</chem>
5,6-Dimethyl-1,3-benzodioxole	4	<chem>C12=CC(=C(C=C1OCO2)C)C</chem>
o-Tolylaceticacid	4	<chem>C1(=CC=CC=C1CC(=O)O)C</chem>
2-methylphenylacetate	4	<chem>C1(=CC=CC=C1CC(=O)[O-])C</chem>
2-Methylbenzylalcohol	4	<chem>C1(=C(C=CC=C1)C)CO</chem>
2-Methylbenzaldehyde	4	<chem>C1(=C(C=CC=C1)C)C=O</chem>
2-Chloroacetophenone	4	<chem>C1(=C(C=CC=C1)Cl)C(=O)C</chem>
2-Methoxy-3-methylpyridine	5	<chem>C1(=CC=CN=C1OC)C</chem>
1-propan-2-ylpyridin-2-one	5	<chem>C1=CC=CN(C1=O)C(C)C</chem>
3,4,5-trimethyl-1H-pyridin-2-one	5	<chem>C1(=C(C(=CNC1=O)C)C)C</chem>
9-Methyl-2,3,4,5-tetrahydro-2-benzazepin-1-one	4	<chem>C1(C2=C(CCCN1[H])C=CC=C2C)=O</chem>
(2-methylphenyl)-piperidin-1-ylmethanone	4	<chem>C1CCCCN1C(C2=CC=CC=C2C)=O</chem>
3-Methyl-2-(5-methyl-1H-imidazol-2-yl)pyridine	7	<chem>C1=NC(=C(C=C1)C)C2=NC=C([N]2)C</chem>
3-methyl-1-(2-pyridyl)pyrazole	7	<chem>C1=NC(=CC=C1)[N]2C=CC(=N2)C</chem>
2-Isopropylloxazole	5	<chem>C1=COC(=N1)C(C)C</chem>
2-Isopropylthiazole	5	<chem>C1=CSC(=N1)C(C)C</chem>
2-(4-Methylpyridin-2-yl)-1,3-thiazole	7	<chem>C1=NC(=CC(=C1)C)C2=NC=CS2</chem>
2-(2-Furyl)-4-methylpyridine	7	<chem>C1=NC(=CC(=C1)C)C2=CC=CO2</chem>
4-Methyl-2-pyridin-2-ylaniline	7	<chem>C1=NC(=CC=C1)C2=C(C=CC(=C2)C)N</chem>
1-Methyl-4-(phenoxyethyl)benzene	7	<chem>C1=CC(=CC=C1COC2=CC=CC=C2)C</chem>
(3-Methylcyclopentyl)benzene	4	<chem>C1=CC=CC=C1C2CCC(C2)C</chem>

2-(3-Methylcyclopentyl)pyridine	5	<chem>C1=NC(=CC=C1)C2CCC(C2)C</chem>
1-cyclopropyl-4-methylbenzene	4	<chem>C1=CC(=CC=C1C2CC2)C</chem>
2-Cyclopropyl-5-methylpyridine	5	<chem>C1=NC(=CC=C1C)C2CC2</chem>
2-Cyclopropyl-5-methylpyrimidine	5	<chem>C1=NC(=NC=C1C)C2CC2</chem>
4-Benzyltoluene	4	<chem>C1=CC=C(C=C1)CC2=CC=C(C=C2)C</chem>
5-Methyl-2-phenoxy pyridine	7	<chem>C1=CC=C(C=C1)OC2=NC=C(C=C2)C</chem>
5-Methyl-N-phenylpyridin-2-amine	7	<chem>C1=CC=C(C=C1)NC2=NC=C(C=C2)C</chem>
4-methyl-N-phenylaniline	7	<chem>C1=CC=C(C=C1)N(C2=CC=C(C=C2)C)</chem>
N,5-Dimethyl-N-phenylpyridin-2-amine	7	<chem>C1=CC=C(C=C1)N(C2=NC=C(C=C2)C)C</chem>
4-Benzyltoluene	7	<chem>C1=CC(=CC=C1C2=CC=CC=C2)C</chem>
N,4-Dimethylfuran-2-carboxamide	5	<chem>C1=C(OC=C1C)C(=O)NC</chem>
N,4-Dimethylthiophene-2-carboxamide	5	<chem>C1=C(C(=O)N(C)[H])SC=C1C</chem>
4-Methylthiophene-2-carbaldehyde	5	<chem>C1=C(C=O)SC=C1C</chem>
3-Methyl-5-acetamidofuran	5	<chem>C1=C(OC=C1C)NC(C)=O</chem>
N-(4-Methylthiophen-2-yl)acetamide	5	<chem>C1=C(N(C(C)=O)[H])SC=C1C</chem>
N,N-Dimethyl-1,3-oxazole-2-carboxamide	5	<chem>C1(=NC=CO1)C(=O)N(C)C</chem>
1-(2-Methylphenyl)piperazin-4-ium	5	<chem>C1=CC(=C(C=C1)N2CC[N+]CC2)C</chem>
2-Amino-4-methylbenzophenone	7	<chem>C1(=CC=C(C=C1)C)C(C2=CC=CC=C2N)=O</chem>
1-Methylpyrazole	5	<chem>C1=C[N](N=C1)C</chem>
4-Methyl-2H-pyran	5	<chem>C1=CC(=CCO1)C</chem>
2-Methylperoxypropionicacid	3	<chem>C(C(=O)OO)(C)C</chem>
Peroxypropionate	3	<chem>C(C(=O)O[O-])C</chem>
3-Methylpyrrolidin-1-ium	2	<chem>C1C(CC[N+]1)C</chem>
1,3,4-Trimethylpyrrolidin-1-ium	2	<chem>C1C(C)C(C[N+]1)C</chem>
4-Triflyltoluene	4	<chem>C1(=CC=C(C=C1)C)[S](C(F)(F)F)(=O)=O</chem>
4-Methyl-2H-thiopyran	5	<chem>C1C=C(C=CS1)C</chem>

2,6-Dimethylbenzoquinone	5	<chem>C1(C=C(C(C(=C1)C)=O)C)=O</chem>
1-Iodopropane	2	<chem>CCCI</chem>
1,1,1-Triiodopropane	2	<chem>CCC(I)(I)I</chem>
1-Iodo-3,5-dimethylbenzene	4	<chem>C1(=CC(=CC(=C1)C)C)I</chem>
1-(iodomethyl)-3,5-dimethylbenzene	4	<chem>C1(=CC(=CC(=C1)C)C)CI</chem>

Table S4. Validation set for out-of-plane bending

The validation set for out-of-plane bending has been shown with their name, the number of conformations chosen for each molecule, and the related group number as mentioned. (The equilibrium structure has been counted)

Index	Name of molecule	Number of configurations
1	Hexa-2,4-diene	11
2	3-Methyl-2-butenal	16
3	3-Ethylhexane-2,4-dione	6
4	5-Oxohexanal	11
5	Succinamide	6
6	Diethyloxalate	6
7	Succinylfluoride	6
8	Succinylchloride	6
9	Butanedioyldibromide	6
10	N-Ethylbutane-2-imine	6
11	Butan-2-imine	6
12	Monomethylsuccinate	6
13	Monomethylsuccinate-ion	6
14	2,3-Dimethyl-2-butenic acid	11
15	Thioisobutyric acid	6
16	2-Methylpropanethioate	6
17	3-Methylbutanoylacetate	11
18	1-Ethyl-1-methylurea	6
19	2-Methyl-1-nitropropane	6
20	Urethane	6
21	Propan-2-yl-hydrogencarbonate	6
22	Gluconolactone	6
23	N-Methylsalicylamide	6
24	2-Chloroacetanilide	6
25	2-Fluoroanisole	11
26	2-Methylanisole	11
27	3-Fluoro-2-methoxyphenol	16
28	N,2,6-Trimethylaniline	21
29	3-methyl-2-(methylamino)phenol	16
30	2-Hydroxyacetophenone	16
31	2-Methoxybenzamide	21
32	Phthalamide	11
33	2-Aminobenzamide	21
34	2,4,6-Trinitrobenzoic acid	11
35	2,4,6-Trinitrobenzoate	6
36	3,5-Dimethylbenzenaminium	6
37	3,5-Dimethylbenzenesulfonic acid	11
38	3,5-Dimethylbenzenesulfonate	11

39	2-Methylbenzotrifluoride	16
40	2-Methylbenzotrichloride	16
41	3,5-Dichlorotoluene	11
42	3,5-Difluorotoluene	11
43	3,5-Dibromotoluene	11
44	5,6-Dimethyl-1,3-benzodioxole	16
45	o-Tolylaceticacid	16
46	2-methylphenylacetate	16
47	2-Methylbenzylalcohol	6
48	2-Methylbenzaldehyde	11
49	2-Chloroacetophenone	11
50	2-Methoxy-3-methylpyridine	11
51	1-propan-2-ylpyridin-2-one	16
52	3,4,5-trimethyl-1H-pyridin-2-one	16
53	9-Methyl-2,3,4,5-tetrahydro-2-benzazepin-1-one	11
54	(2-methylphenyl)-piperidin-1-ylmethanone	6
55	3-Methyl-2-(5-methyl-1H-imidazol-2-yl)pyridine	16
56	3-methyl-1-(2-pyridyl)pyrazole	16
57	2-Isopropylloxazole	11
58	2-Isopropylthiazole	11
59	2-(4-Methylpyridin-2-yl)-1,3-thiazole	21
60	2-(2-Furyl)-4-methylpyridine	11
61	4-Methyl-2-pyridin-2-ylaniline	6
62	(3-Methylcyclopentyl)benzene	6
63	2-(3-Methylcyclopentyl)pyridine	6
64	1-cyclopropyl-4-methylbenzene	6
65	2-Cyclopropyl-5-methylpyridine	6
66	2-Cyclopropyl-5-methylpyrimidine	16
67	5-Methyl-2-phenoxy pyridine	6
68	5-Methyl-N-phenylpyridin-2-amine	6
69	4-methyl-N-phenylaniline	6
70	N,5-Dimethyl-N-phenylpyridin-2-amine	6
71	4-Benzyltoluene	6
72	N,4-Dimethylfuran-2-carboxamide	16
73	N,4-Dimethylthiophene-2-carboxamide	16
74	4-Methylthiophene-2-carbaldehyde	26
75	3-Methyl-5-acetamidofuran	16
76	N-(4-Methylthiophen-2-yl)acetamide	16

77	N,N-Dimethyl-1,3-oxazole-2-carboxamide	16
78	1-(2-Methylphenyl)piperazin-4-ium	6
79	1-Methylpyrazole	16
80	4-Methyl-2H-pyran	11
81	2-Methylperoxypropionicacid	6
82	Peroxypropionate	6
83	4-Triflyltoluene	6
84	4-Methyl-2H-thiopyran	11
85	2,6-Dimethylbenzoquinone	11
86	1-Iodo-3,5-dimethylbenzene	6

Table S5. The overall atomic types based on SMARTS strings

SMARTS strings	General index	Type index	Short name	Column6
[H]*	1	1	H*	H*, wild matching Hydrogen
[C]*	2	2	C*	C*, wild matching Carbon
[c]*	3	3	c*	c*, wild matching Carbon (aromatic)
[N]*	4	4	N*	N*, wild matching Nitrogen
[n]*	5	5	n*	N*, wild matching Nitrogen (aromatic)
[O]*	6	6	O*	O*, wild matching Oxygen
[o]*	7	7	o*	o*, wild matching oxygen (aromatic)
[P]*	8	8	P*	P*, wild matching Phosphor
[S]*	9	9	S*	S*, wild matching Sulphur
[s]*	10	10	s*	s*, wild matching sulfur (aromatic)
[F]*	11	11	F	F*, wild matching Fluorine
[Cl]*	12	12	Cl	Cl*, wild matching Chlorine
[Br]*	13	13	Br	Br*, wild matching Bromine
[I]*	14	14	I	I*, wild matching Iodine
[OH2]	15	15	OW	OW: O on Water
[H][OH2]	16	16	HW	HW: H on Water
[H][OH1]	17	17	HO	HO, H on Oxygen
[H][C]	18	18	HC	HC, H on carbon
[H][CH]	19	19	HCH	HCH, H on sp3 carbon, -CH-
[H][CH2]	20	20	HCH2	HCH2, H on sp3 carbon, -CH2-
[H][CH3]	21	21	HCH3	HCH3, H on sp3 carbon, -CH3
[H][C]=[C,N,O]	22	22	HC2	HC2, H on sp2 carbon
[H][c]	23	23	Hc	HC, H on aromatic

				carbon
[H][N]	24	24	HN	HN, H on Nitrogen
[H][S]	25	25	HS	HS, H on Sulfur
[H][P]	26	26	HP	HP, H on Phosphor
[H][NX4]	27	27	H+	H+, H on NH4+, R-NH3+, R2-NH2+, R3-NH+
[H][N]=[C](N)[N]	28	27	H+	H+, H on Guandinium, Imidazolium
[H][N]-[C](=N)[N]	29	27	H+	H+, H on Guandinium, Imidazolium
[H][n]	30	28	Hn	Hn, H on aromatic N
[c]	31	29	car	car, aromatic carbon
[CH]1C=CC=CC1=O	32	29	car	car,
[C]1=CC=CC(=O)[CH]1	33	29	car	car,
[C]1=C[CH]C(=O)C=C1	34	29	car	car,
[C]1=CC(=O)[CH]C=C1	35	29	car	car,
[C]1=CC=C[CH]C1(=O)	36	29	car	car,
[C]1(=O)[CH]C=CC=C1	37	29	car	car,
[cr5H0]	38	30	c0r5	c0r5, aromatic carbon in 5-membered cycle without H
[c]([c])([c])[c]	39	31	car0	car, aromatic carbon without H
[CX4H0]	40	32	C30	C30, sp3 carbon with 0 Hydrogen
[CX4H1]	41	33	C31	C31, sp3 carbon with 1 Hydrogen
[CX4H2]	42	34	C32	C32, sp3 carbon with 2 Hydrogens
[CX4H3]	43	35	C33	C33, sp3 carbon with 3 Hydrogens
[CX4H4]	44	36	C34	C34, sp3 carbon with 4 Hydrogens, methane
[CX4]([O])[O]	45	37	C3O2	C3O2, sp3 carbon with 2 oxygens
[CX4r]	46	38	C3R	C3R, sp3 carbon on

				the cycle
[CX4r5]	47	39	C3R5	C3R5, sp3 carbon on 5-membered cycle
[CX3R5]	48	40	C2R5	C2R5, sp2 carbon on cycle
[CX4r5]([Or5])	49	41	C3O1R5	C3O1R5, sp3 carbon on 5-membered cycle bonded to 1 O on cycle
[CX4r5]([Or5])[Or5]	50	42	C3O2R5	C3O2R5, sp3 carbon on 5-membered cycle bonded to 2 O on cycle
[CX4r6]	51	43	C3R6	C3R6, sp3 carbon on 6-membered cycle
[CX4r3]	52	44	C3R3	C3R3, sp3 carbon on 3-membered cycle
[CX4r4]	53	45	C3R4	C3R4, sp3 carbon on 4-membered cycle
[C]1(CCO1)	54	46	C3R4O1	C3R4O1, sp3 C in oxetane ring closer to O
[CX4r7]	55	47	C3R7	C3R7, sp3 carbon in 7-membered ring
[CX3r7](=[O])	56	48	C=OR7	C=OR7, C=O in 7-membered ring (after CNN)
[CX4r6]([Or6])	57	49	C3O1R	C3O1R, sp3 carbon on 6-membered cycle bonded to 1 O on cycle
[CX4r5]([NH1])	58	50	C3N1R5	C3N1R5, sp3 carbon on 5-membered cycle bonded to 1 NH
[CX4r5]([NH1])([NH1])	59	51	C3N2R5	C3N2R5, sp3 carbon on 5-membered cycle bonded to 2 NH
[CX4]([C](=O))([C](=O))	60	52	C-Bket	C-Bket, sp3 carbon with 2 C=O
[\$([#6](-[#7])(-[#6]([#8])(-[#8]))))	61	53	CA	CA, sp3 carbon on alanine C chain
[C]([cr6])[cr6]	62	54	C3c6c6	C3c6c6, sp3 C connected with 2 benzene rings

[CX4]([F])[F]	63	55	CF2	CF2, sp3 carbon with 2 F
[CX4]([F])([F])[F]	64	56	CF3	CF3, sp3 carbon with 3 F
[CX4]([F])([F])([F])[F]	65	57	CF4	CF4, sp3 carbon with 4 F
[CX4][Cl]	66	58	CCl1	CCl1, sp3 carbon with 1 Cl
[CX4]([Cl])[Cl]	67	59	CCl2	CCl2, sp3 carbon with 2 Cl
[CX4]([Cl])([Cl])[Cl]	68	60	CCl3	CCl3, sp3 carbon with 3 Cl
[CX4]([Cl])([Cl])([Cl])[Cl]	69	61	CCl4	CCl4, sp3 carbon with 4 Cl
[CX4][Br]	70	62	CBr1	CBr1, sp3 carbon with 1 Br
[CX4]([Br])[Br]	71	63	CBr2	CBr2, sp3 carbon with 2 Br
[CX4]([Br])([Br])[Br]	72	64	CBr3	CBr3, sp3 carbon with 3 Br
[CX4]([Br])([Br])([Br])[Br]	73	65	CBr4	CBr4, sp3 carbon with 4 Br
[\$([CX3]=[CX3])]	74	66	C2C	C2C, sp2 carbon, CH2=CH2
[\$([#6]([#6])-[#6]([#6]))]	75	67	C2C2C	C2C2C, sp2 carbon, interior C of CH2=CH-CH=CH2
[\$([#6]([#6])-[#6]([#8]))]	76	68	C2C2O	C2C2O, sp2 carbon, interior C of CH2=CH-C=O
[CX3H1](=O)	77	69	CHO	C=O, sp2 carbon, aldehyde
[CX3H2](=O)	78	70	CH2O	C=O, sp2 carbon, formaldehyde
[CX3H1](=O)([CX3]([H])(=O))	79	71	CHO-2	C=O, sp2 carbon, glyoxal
[\$([#6]([#8])-[#6]([#6]))]	80	72	CHOC2C	CHOC2C, sp2 carbon, CHO of CHO-CH=CH2
[\$([#6]([#8])([H])([ccccc]))]	81	73	CHOben	CHOben, sp2 carbon, CHO of CHO-Ph
[CX3H0](=O)	82	74	C-Ket	C=O, sp2 carbon, ketone
[CX3H0](=O)([C](=O))	83	75	C-PRV	C=O, sp2 carbon,

[O])]				pyruvate
[CX3](=O)([OH0])	84	76	CO=O-	C=O, sp2 carbon, carboxylate
[CX3](=O)([OH0])(-[#6]=[#6])	85	77	COOC2C-	C=O, sp2 carbon, carboxylate bonded to C=C
[CX3](=O)([OH0])[ccc ccc]	86	78	COOben-	C=O, sp2 carbon, carboxylate on benzene
[\$([#6](-[#6](-[#8])=[#8])(=[#8])(-[OH0])))]	87	79	C-Oxa-	C=O, sp2 carbon, oxalate
[CX3](=O)([OH1])	88	80	CO=O	C=O, sp2 carbon, carboxylic acid
[\$([CX3](=O)([O]([C])))]	89	80	CO=O	C=O, sp2 carbon, carboxylic ester
[CX3]1(=[O])(OCCCC1)	90	81	COOR6	COOR6,
[CX3]1(=[O])(OCCC1)	91	82	COOR5	COOR5,
[CX3](=O)([SH1])	92	83	CS=O	C=O, sp2 carbon, thioate acid
[\$([CX3](=O)([S]([C])))]	93	83	CS=O	C=O, sp2 carbon, thioate ester
[CX3](=O)([OH1,OC1])(-[#6]=[#6])	94	84	COOC2C	C=O, sp2 carbon, carboxylic acid bonded to C=C
[\$([CX3](=O)([O]([C]))(-[#6]=[#6]))]	95	84	COOC2C	C=O, sp2 carbon, carboxylic ester bonded to C=C
[CX3](=O)([OH1])[ccc ccc]	96	85	COOben	C=O, sp2 carbon, carboxylic acid on benzene
[\$([CX3](=O)([O]([C]))[cccccc])]	97	85	COOben	C=O, sp2 carbon, carboxylic ester on benzene
[\$([#6](-[#6](-[#8])=[#8])(=[#8])(-[OH])))]	98	86	C-Oxa	C=O, sp2 carbon, oxalic acid
[CX3](=[OX1])[OX2][CX3](=[OX1])	99	87	CO=OC	C=O, sp2 carbon, anhydride
[CX3](=O)([OH0])[OH0]	100	88	CO3--	C=O, sp2 carbon, carbonate
[CX3](=O)([OH1])[OH	101	89	CO3-	C=O, sp2 carbon,

0]				bicarbonate
[CX3](=O)(O[C])(O[C])	102	90	CO3	C=O, sp2 carbon, carbonic ester
[CX3](=O)(O[C])(O[H])	103	91	CO3H	C=O, sp2 carbon, bicarbonate ester
[CX3](=O)([NX3])	104	92	CON	CON, sp2 carbon, peptide bond (amide)
[Cr5](=O)[Nr5]	105	93	CONR5	CONR5, CON in 5-membered ring
[CX3]1(=[O])(NCCCC1)	106	94	CONR6	CONR6, lactam
[C](=O)([NX3])([cccccc])	107	95	CONben	CONben, CON connected to benzene ring
[CX3](=O)([O])([NX3])	108	96	C-carb	C-carb, sp2 carbon, carbamic acid
[CX3](=O)([F])	109	97	COF	COF, sp2 carbon, acyl fluoride
[CX3](=O)([Cl])	110	98	COCl	COCl, sp2 carbon, acyl chloride
[CX3](=O)([Br])	111	99	COBr	COBr, sp2 carbon, acyl bromide
[C](=O)([O])([OH0]))	112	100	COOO-	COOO-, C=O in peracetate ion
[C](=O)([O])([OH1,OC1]))	113	101	COOOH	COOOH, C=O in peracetic acid or ester
[C]=[N]	114	102	C=N	C=N, sp2 carbon, formimidamide
[CX3R]=[N]	115	103	C=NR	C=N, sp2 carbon, connected to Nitrogen in a ring
[CH0]([c])([N])[NH2]	116	104	C-A6	C-A6, 6'-C in Adenine
[C](=O)([cr6])[cr6]	117	105	C=Oc6c6	C=Oc6c6, C=O connected with 2 benzene rings
[CH1R](=[N])([N]([c]))	118	106	C-A2	C-A2, 2'-C in Adenine
[C](=[NH2])(N)[N]	119	107	C+	C+, positively charged carbon, C+(NH2)3 and C+(NH2)2(NHCH3)
[\$([CX2]#[CX2])]	120	108	C1C	C1C, sp carbon, triple bond
[\$([CX2]([#CX2])-[CX2]#[CX2])]	121	109	C1C1C	C1C1C, sp carbon, triple bond bonded

				with another triple bond
[CX2]#[N]	122	110	C1N	C1N, sp carbon, nitrile
[\$([CX3N1]=[CX3N1])]	123	111	CCN	CCN, sp ² carbon, C=C in imidazole with positive charge
[CX3N2H1]	124	112	CNN	CNN, sp ² carbon, C between Ns in imidazole with positive charge
[CX3]=[S]	125	113	C=S	C=S, Carbon of C=S bond
[CX2](#[NX1])[SX2]	126	114	C-SCN	
[C]1([O,S]C=CC=C1)	127	115	C3-pyran	C3-pyran, sp ³ C in pyran ring
[\$([C]1(=CC=C[O,S]C1)), \$([C]1(=CC[O,S]C=C1)), \$([C]1(=CC=C[O,S]1)), \$([C]1(=C[O,S]CC=C1))]	128	116	C2-pyran	C2-pyran, sp ² C in pyran ring
[c]([c])[n]	129	117	ccn	ccn, aromatic carbon bonded to aromatic nitrogen
[cr5]([cr5])[nH0r5]	130	118	ccnr5	ccnr5, aromatic carbon bonded to aromatic nitrogen in 5-membered cycle
[c]([c]([c](=O)))([c])	131	119	c-PryO	c-PryO, side sp ² -C in 2-Prydone close to aromatic C=O
[cH1]([c]([nH1]))([c])	132	120	c-PryN	c-PryN, side sp ² -C in 2-Prydone close to aromatic NH
[c]([c])([c])[n]	133	121	cccn	cccn, aromatic carbon bonded to aromatic nitrogen without H
[cH0]([c])[nH1]	134	122	c0cn1	c0cn1, aromatic carbon bonded to aromatic NH and no H
[cH1]([c])[nH1]	135	123	c1cn1	c1cn1, aromatic carbon bonded to aromatic NH and 1 H
[cH1r5]([cr5])[nH1r5]	136	124	c1cn1r5	c1cn1r5, aromatic carbon bonded to

				aromatic NH and 1 H in 5-membered cycle
[c]([c])([C]([NH2]))[n]	137	125	c-A5	c-A5, 5'-C in Adenine
[c]([n])[NH2]	138	126	cnN2	cnN2, aromatic carbon bonded to 1 aromatic nitrogens and aliphatic NH2
[c]([c])([nH0])[NH2]	139	127	ccnN2	ccnN2, aromatic carbon bonded to aromatic nitrogen and aliphatic NH2 without H
[c]([c])([nH1])[NH2]	140	128	ccn1N2	ccn1N2, aromatic carbon bonded to aromatic NH and aliphatic NH2 without H
[c]([c]([n]))([n])[NH0]	141	129	c-A4	c-A4, 4'-C in Adenine
[c]([n])[n]	142	130	cnn	cnn, aromatic carbon bonded to 2 aromatic nitrogens
[c]([n])[nH1]	143	131	cnn1	cnn1, aromatic carbon bonded to 2 aromatic nitrogens and H
[cr5]([nr5])[nH1r5]	144	132	cnn1r5	cnn1r5, aromatic carbon bonded to 2 aromatic nitrogens and H in 5-membered cycle
[c]([n])([n])[c]([n])	145	133	c-G4	c-G4, 4'-C in Guanine and C in similar structure
[c]([n])([n])[N]	146	134	cnnN	cnnN, aromatic carbon bonded to 2 aromatic nitrogens and aliphatic N
[c]([c])[c](=O)	147	135	ccco	ccco, aromatic carbon bonded to aromatic C=O
[c]([c](=O))([c]([n])([n]))[n]	148	136	c-G5	c-G5, 5'-C in Guanine and C in similar structure
[c](=O)([c])[nH1]	149	137	c=On1	c=On1, aromatic C=O bonded to aromatic

				NH and carbon
[c](=O)([n])[nH1]	150	138	c=Onn1	c=Onn1, aromatic C=O bonded to aromatic N and NH
[c](=O)([nH1])[nH1]	151	139	c=On1n1	c=On1n1, aromatic C=O bonded to 2 aromatic NH
[c](=O)([c]([n]))[nH1]	152	140	c-G6	c-G6, 6'-C in Guanine and C in similar structure
[c]1(ccco1)	153	141	c-Fur-1	c-Fur-1, c in Furan ring closer to O
[c]1(cocc1)	154	142	c-Fur-2	c-Fur-2, c in Furan ring not near O
[c]1(cccs1)	155	143	c-Thp-1	c-Thp-1, c in Thiophene ring closer to S
[c]1(csc1)	156	144	c-Thp-2	c-Thp-2, c in Thiophene ring not near S
[c]1(ccnn1)	157	145	c-Prz-1	c-Prz-1, c in Pyrazole ring closer to n
[c]1(cnnc1)	158	146	c-Prz-2	c-Prz-2, c in Pyrazole ring which is not near n
[c]1(ncco1)	159	147	c-Oxz-1	c-Oxz-1, c in Oxazole ring between n and o
[c]1(ncoc1)	160	148	c-Oxz-n	c-Oxz-n, c in Oxazole ring closer to n
[c]1(ocnc1)	161	149	c-Oxz-o	c-Oxz-o, c in Oxazole ring closer to o
[c]1(ncs1)	162	150	c-Thz-1	c-Thz-1, c in Thiazole ring between n and s
[c]1(ncsc1)	163	151	c-Thz-n	c-Thz-n, c in Thiazole ring closer to n
[c]1(scnc1)	164	152	c-Thz-o	c-Thz-o, c in Thiazole ring closer to s
[c]1(ccccc1)([c]2(cccc c2))	165	153	c6-6	c6-6, The connecting C between 2 benzene rings
[c]1(ccccc1)([c]2(nccc 2))	166	154	c6-cn5	c6-cn5, connecting c between 6-ring and 5-ring with n
[c]1(nccc1)([c]2(ccccc	167	155	cn5-c6	cn5-c6, connecting c

2))				between 5-ring with n and 6-ring
[c]1(ncccc1)([c]2(nccn2))	168	156	cn6-cnn5	cn6-cnn5, connecting c between 6-ring with n and 5-ring with 2 n
[c]1(nccn1)([c]2(ncccc2))	169	157	cnn5-cn6	cnn5-cn6, connecting c between 5-ring with 2 n and 6-ring with n
[c]1(ncccn1)([c]2(nccn2))	170	158	cnn6-cnn5	cnn6-cnn5, connecting c between 6-ring with 2 n and 5-ring with 2 n
[c]1(nccn1)([c]2(nccccn2))	171	159	cnn5-cnn6	cnn5-cnn6, connecting c between 5-ring with 2 n and 6-ring with 2 n
[c]1(ncccc1)([n]2(nccn2))	172	160	cn6-nnc5	cn6-nnc5, connecting c to n between 6-ring with n and 5-ring with 2 n
[c]1(ncccn1)([n]2(ncccc2))	173	161	cnn6-nnc5	cnn6-nnc5, connecting c to n between 6-ring with 2 n and 5-ring with 2 n
[c]1(ncccc1)([c]2(nccs2))	174	162	cn6-cns5	cn6-cns5, connecting c between 6-ring with n and 5-ring with n & s
[c]1(nccs1)([c]2(ncccc2))	175	163	cns5-cn6	cns5-cn6, connecting c between 5-ring with n & s and 6-ring with n
[c]1(ncccc1)([c]2(ccco2))	176	164	cn6-co5	cn6-co5, connecting c between 6-ring with n and 5-ring with o
[c]1(ccco1)([c]2(ncccc2))	177	165	co5-cn6	co5-cn6, connecting c between 5-ring with o and 6-ring with n
[c]1(ccccc1)([c]2(ccccn2))	178	166	c6-cn6	c6-cn5, connecting c between 6-ring and 6-ring with n
[c]1(ccccn1)([c]2(ccccc2))	179	167	cn6-c6	cn6-c6, connecting c between 6-ring with n and 6-ring
[c]1(ccco1)([c]2(ncccc2))	180	165	co5-cn6	co5-cn6, connecting c between 6-ring with n

				and 6-ring with o
[c]1(nnnn1)	181	168	cnnnnr	cnnnnr,
[n]	182	169	nar	nar, Aromatic Nitrogen in a ring
[NX4]	183	170	N4	N4, Nitrogen in Ammonium
[NX3]	184	171	N3	N3, sp3 Nitrogen
[NX3r5]	185	172	N3R5	N3R5, sp3 Nitrogen on 5-membered cycle
[NX4r5]	186	173	N4R5	N4R5, sp3 N with charge in 5-membered ring
[NX3r6]	187	174	N3R6	N3R6, sp3 N in 6-membered ring
[NX4r6]	188	175	N4R6	N4R6, sp3 N in 6-membered ring with charge
[Nr7]	189	176	N3R7	N3R7, sp3 N in 7-membered ring
[NX3H3]	190	177	N3H3	N3H3, ammonia N
[NX3H2]([C](=[N]))	191	178	N3C=N	N3C=N,
[NX3;!r]([CX3](=O))	192	179	NC=O	NC=O, sp3 Nitrogen in amide
[NX3H2]([C](=O)([O]))	193	180	N-carbH	N-carbH, sp3 Nitrogen in carbamic acid with H
[NX3H1]([C](=O)([O]))	194	180	N-carbH	N-carbH, sp3 Nitrogen in carbamic acid with H
[NX3H0]([C](=O)([O]))	195	181	N-carb	N-carb, sp3 Nitrogen in carbamic acid with no H
[NX3]([CX3](=O))([CX3](=O))	196	182	N-lmi	N-lmi, sp3 Nitrogen in imide
[NX3](=[O])[C]	197	183	NO2	NO2, nitryl
[NX3](=[O])[ccccc]	198	184	NO2ben	NO2ben, nitryl on benzene
[NX3](-[O])[O]	199	185	NOO	NOO, nitrite
[NX3H0]([NX3H0c0])[ccccc]	200	186	N2N	N2N, N in azobenzene
[NX1]	201	187	NT	, Triple bond Nitrogen
[NX1](#[CX2]([SX2]))	202	188	N-SCN	N-SCN
[NX3H0]([N])[ccccc]	203	189	N1Ni	N, Triple bond

				Nitrogen in diazonium (bond to other atoms)
[NX3H0]([N])[C]	204	189	N1Ni	N, Triple bond Nitrogen in diazonium (bond to other atoms)
[NX3]([NH0][ccccc])	205	190	N1No	N, Triple bond Nitrogen in diazonium (outer side)
[NH0]([NH0][ccccc])[ccccc]	206	191	N-Azo	N-Azo, N in Azobenzene
[NX2]=[C]	207	192	N=C	N=C, Double bond N=C
[NH2]=[C]	208	193	N=C+	N=C+, Double bond N+
[NH2]-[C](=[NH2])	209	193	N=C+	N=C+, Double bond N+
[NH1]-[C](=[NH2])	210	193	N=C+	N=C+, Double bond N+
[NH1]([C])([C](=[NH2]))	211	194	N=CC+	N=C+, Double bond N+ with 2 C
[NX2]([C]([NH2]))(=[C H1])	212	195	N-A1	N-A1, 1'-N in Adenine
[NH0]([c]([c])([CH]))	213	196	N-A3	N-A3, 3'-N in Adenine
[NH2]([ccccc])	214	197	NH2ben	NH2, Aniline N
[NH3]([ccccc])	215	198	NH3ben	NH3, Phenylazanium N
[NX3]([cr6])[cr6]	216	199	N3c6c6	N3c6c6, sp3 N connected with 2 benzene rings
[nX2H0]	217	200	n0	n0, sp2 aromatic nitrogen with no H
[nX2H0]([c]([NH2]))([c H0])	218	201	n-G3	n-G3, 3'-G in Guanine
[nX3H1]	219	202	n1	n1, sp3 aromatic nitrogen with H
[nX3]([c](=O))	220	203	nc=O	nc=O, sp3 aromatic nitrogen bonded to aromatic C=O
[nX3]([c](=O))([c](=O))	221	204	n2c=O	n2c=O, sp3 aromatic nitrogen bonded to 2 aromatic C=O
[n]1(nccc1)([c]2(nccc c2))	222	205	nnc5-cn6	nnc5-cn6, connecting n to c between 5-ring with 2 n and 6-ring

				with n
[n]1(nccc1)([c]2(nccc n2))	223	206	nnc5-cnn6	nnc5-cnn6, connecting n to c between 5-ring with 2 n and 6-ring with 2 n
[n]1(cccn1)	224	207	n-Prz	n-Prz, n in Pyrazole
[n]1(cocc1)	225	208	n-Oxz	n-Oxz, n in Oxazole
[n]1(csc1)	226	209	n-Thz	n-Thz, n in Thiazole
[n]1(ncnn1)	227	210	nncnncr	nncnncr,
[n]1(nnnnc1)	228	211	nnnnncr	nnnnncr,
[OX2H1]	229	212	OH	OH, Oxygen of Hydroxyl group
[OX2H1]([C](=O))	230	213	OCO	OCO, Oxygen of Carboxylic acid (protonated)
[OX2H1]([P])	231	214	O-P	O-P, Oxygen of phosphate, with H
[OX2H0]([P])	232	215	O-P-	O-P, Oxygen of phosphate, ionic state
[O]([N])(-[C])	233	216	O-N	O-N, Oxygen of nitrite
[OX2H1]([SX4])	234	217	O-S	O-S, Oxygen of Sulfoxide
[OX2]([N])(-[C])	235	218	O=N	O=N, Oxygen of nitrite
[OX1](=N)	236	218	O=N	O=N, Oxygen of nitryl
[OX1]=[CX3][OH1]	237	219	O=C	O=C, Oxygen of carbonyl group, Acetic Acid
[OX1]=[CX3]	238	219	O=C	O=C, Oxygen of carbonyl group
[\$([OX1]=[CX3][H])]	239	219	O=C	O=C, Oxygen of carbonyl group, O=C- H
[OX1]=[CX3][N]	240	219	O=C	O=C, Oxygen of carbonyl group, Amide, Formamide
[OX1](=[P])	241	220	O=P	O=P, Oxygen of phosphate
[OX2H0]([P])[C]	242	221	OP-est	OP-est, Oxygen in phosphate (bonded to C)
[OX2]([P])[P]	243	222	O2P	O2P, Oxygen to connect 2 P
[OX2H0]([C])[C]	244	223	OR2	OR2, Oxygen of ether

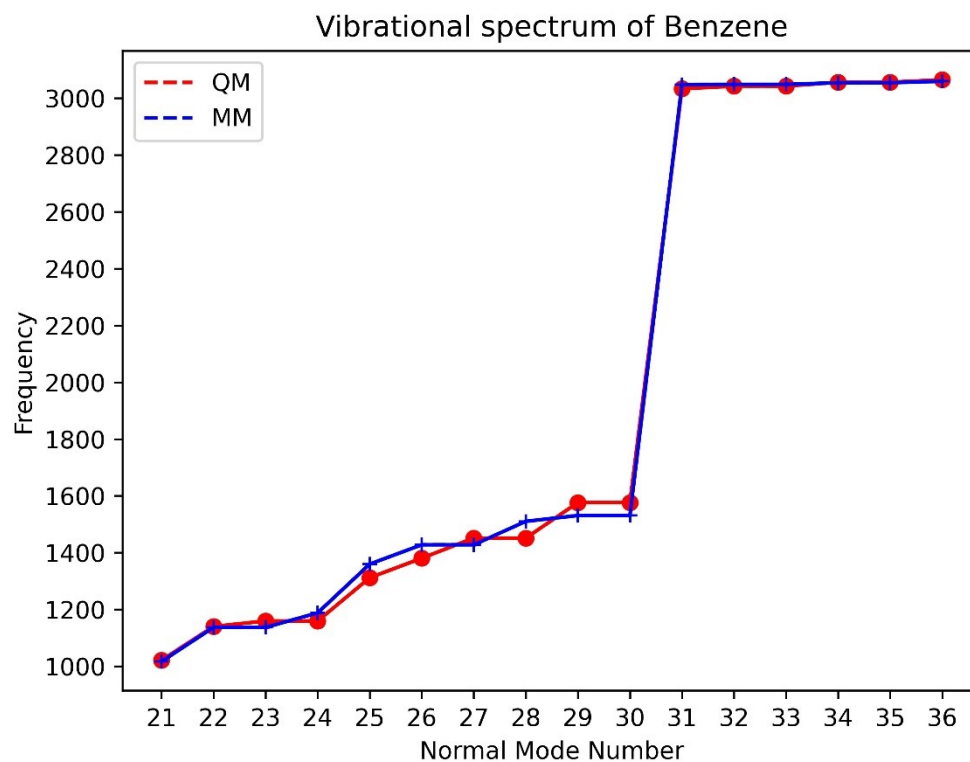
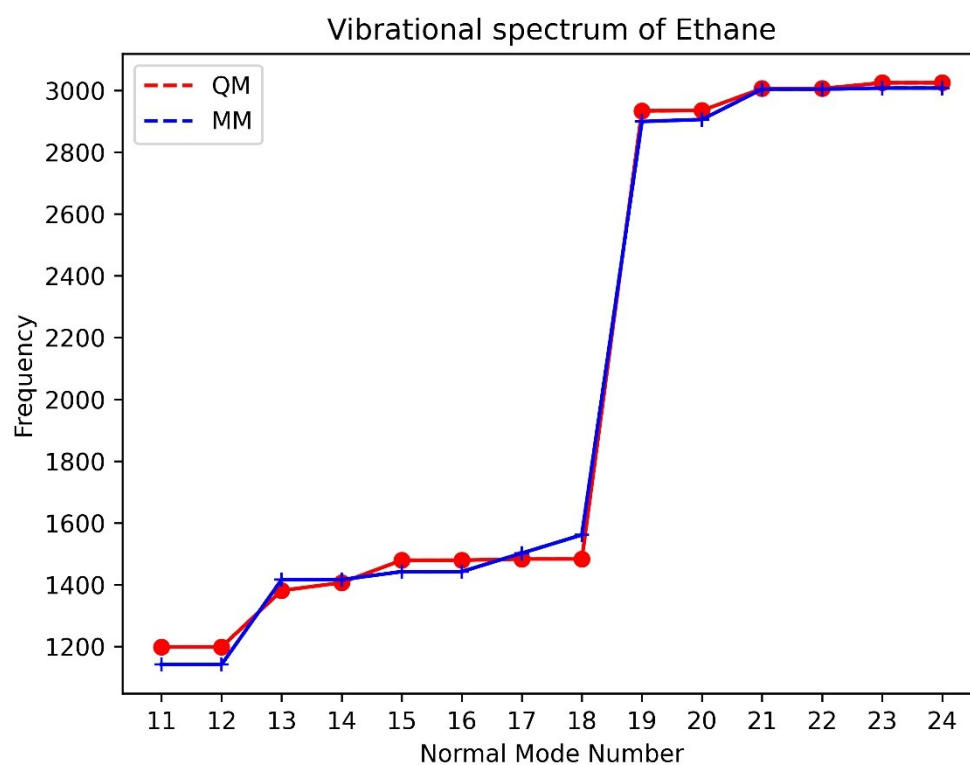
[OX2r6]([C])[C]	245	224	OR6	OR6, Oxygen in 6-membered cycle
[\$([OH0]=[C]([C,N])[OH0]),\$([OH0][C]([C,N])=[OH0])]	246	225	O-	O-, Oxygen of carboxinate
[\$([OH0]([CX3H1](=[O]))),\$([OH0](=[CX3H1]([OH0]))),\$([OH0]([CX3H0](=O)([OH0,O H1])))]	247	225	O-	O-, Oxygen of carboxinate
[\$([OH0]=[C]([ccccc])[OH0]),\$([OH0][C]([ccccc])=[OH0])]	248	225	O-	O-, Oxygen of carboxinate on benzene
[O]=[c]	249	226	Oar	Oar, sp2 Oxygen connected to aromatic ring
[OX2H0]([C](=O))[C]	250	227	O-est	O-est, Oxygen of ester
[\$([OH0]=[C]([O]([C])))]	251	219	O=C	O=C, Oxygen of carbonyl group (correct the O=C in ester)
[OH0]c1ccccc1	252	228	O-Phe-	O on Phenol minus
[OH1]([ccccc])	253	229	O-Phe	O on Phenol
[O;!r]([ccccc])([C])	254	230	O-Phe-est	O on Phenol
[OX2H0]([SX4])	255	231	O-S-	O-S-: Oxygen of sulfonate
[O]=[SX3]	256	232	O=S	O=S, Oxygen of DMSO
[O]=[SX4]	257	233	O=S=O	O=S=O, Oxygen of sulfone
[\$([O]([S]([O])([O][C])))]	258	234	OSO2	OSO2, oxygen of EMsulfonate
[OH0]([S]([ccccc]))	259	235	O-Sben-	O-Sben-, Oxygen of benzene sulfonate
[OH1]([S]([ccccc]))	260	236	O-Sben	O-Sben, Oxygen of benzene sulfonic acid
[OX2H0]([SX4]([OH1]))	261	237	O=SO2	O=SO2: Oxygen of Sulfonic acid
[OX2H0]([SX4]([O]([C])))([OH0])	262	237	O=SO2	O=SO2: Oxygen of Sulfonic acid
[O]([S]([O])([O])([C]))	263	238	OS-est	OS-est, oxygen of EMsulfonate
[OX2r5]([CX4r5]([OH	264	239	Oxo	Oxo, example:

[Or5]))				benzodioxole
[OX2r5]([CX4r5]([OH Or5]))[cccccc]	265	239	Oxo	Oxo, example: benzodioxole
[O][C](=[O])([NH2])	266	225	O-	O-, example: carbamate
[o]1cccc1	267	240	O-fur	O-fur, O on furan ring
[O](=[C]([O]([OH0])))	268	241	O=COO-	O=COO-, O=C in peracetate ion
[O](=[C]([O]([OH1])))	269	242	O=COOH	O=COOH, O=C in peracetic acid or ester
[O]([C](=[O]))([OH0])	270	243	OCO-1-	OCO-1-, O in the middle of (C=O)-O-O-
[OH0]([O]([C](=[O])))	271	244	OCO-2-	OCO-2-, O in the side of (C=O)-O-O-
[O]([C](=[O]))([OH1,O C1])	272	245	OCO-1	OCO-1, O in the middle of peracetic acid or ester
[OH1]([O]([C](=[O])))	273	246	OCO-2	OCO-2, O in the side of peracetic acid
[OC1]([O]([C](=[O]))([C]))	274	247	OCO-est	OCO-est, O in the side of peracetic ester
[O]1(CC=CC=C1)	275	248	O-pyran	O-pyran, O in pyran ring
[o]1(cncc1)	276	249	o-Oxz	o-Oxz, o in Oxazole
[SX2H2]	277	250	SH2	SH2, Sulphur in H2S
[SX2H0]	278	251	S3-	S3-, Sulphur in thiolate
[SX2H0]([C])[C]	279	252	SC2	SC2, Sulphur in SC2
[SX2H1]	280	253	S3	S3, Sulphur in thiol
[SX2H1]([C](=O))	281	254	SCO	SCO, Sulfur of thioate acid (protonated)
[SX2H0]([C](=O))[C]	282	255	S-est	S-est, Sulfur of thioate ester
[SX2]([S])[C]	283	256	SS	SS, Sulphur in disulfide
[SX3]=[O]	284	257	S=O	S=O, Sulphur in DMSO
[SX4](=[O])(=[O])	285	258	SO2	SO2, Sulphur in sulfone
[SX4]([OH0])([OH0])[OH0]	286	259	SO3-	SO3-, Sulphur in sulfonate
[SX4]([OH1])([OH0])([OH0])	287	260	SO3	SO3, Sulphur in sulfonic acid

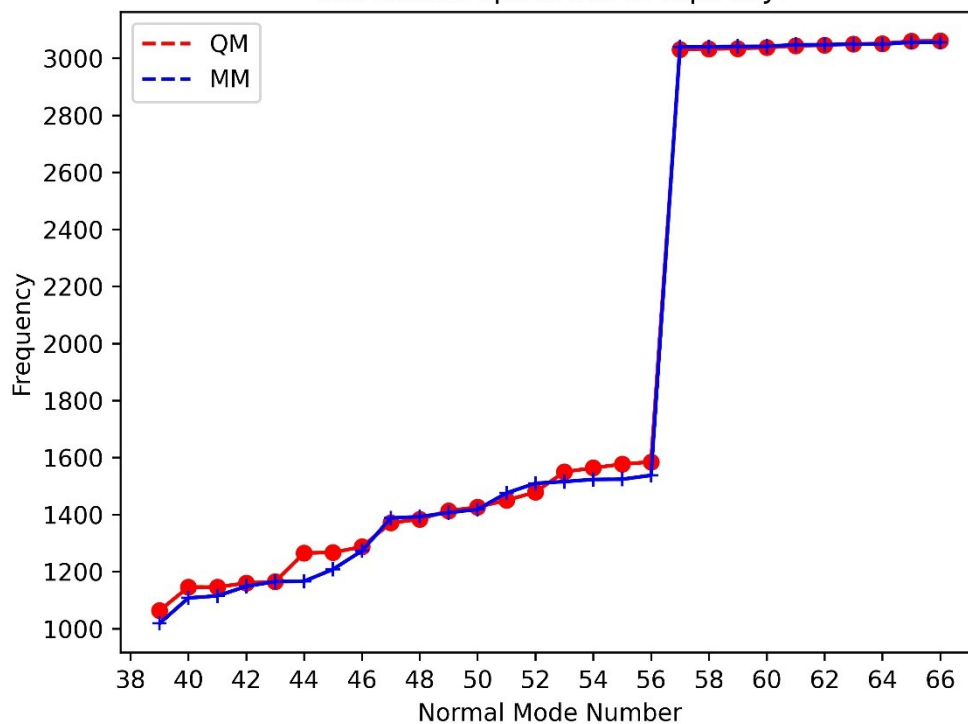
[SX4]([O]([C]))([OH0]) ([OH0])	288	260	SO3	SO3, Sulphur in sulfonic ester
[SX4]([OH0])([OH0])([OH0])[cccccc]	289	261	SO3ben-	SO3ben-, Sulphur in sulfonate on benzene
[SX4]([OH1])([OH0])([OH0])[cccccc]	290	262	SO3ben	SO3ben, Sulphur in sulfonic acid on benzene
[SX4]([O]([C]))([OH0]) ([OH0])[cccccc]	291	262	SO3ben	SO3ben, Sulphur in sulfonic acid on benzene
[SX2]([CX2](#[NX1]))	292	263	S-SCN	S-SCN,
[SX2]([CX2](#[NX1]))[cccccc]	293	264	S-SCNben	S-SCNben,
[S](=O)(=O)([c])	294	265	SO2ben	SO2ben, S in sulfone bonded to the benzene ring
[S](=O)(=O)([c])([NX3])	295	266	SO2Nben	SO2Nben, S in sulfone bonded to the benzene ring and sp3 N
[S]1(CC=CC=C1)	296	267	S-pyran	S-pyran, S in pyran ring
[s]1(cccc1)	297	268	s-Thp	s-Thp, s in Thiophene
[s]1(cncc1)	298	269	s-Oxz	s-Oxz, s in Thiazole
[PH3]	299	270	PH3	PH3, Phosphor in PH3
[PX4](=[O])([OH0])([OH0])[OH0]	300	271	PO4	PO4, Phosphor in Phosphate
[PX4](=[O])([OH1])([OH0])[OH0]	301	272	PO4H1	PO4H1, Phosphor in Phosphate
[PX4](=[O])([OH1])([OH1])[OH0]	302	273	PO4H2	PO4H2, Phosphor in Phosphate
[PX4](=[O])([OH1])([OH1])[OH1]	303	274	PO4H3	PO4H3, Phosphor in Phosphate
[PX4](=[O])([O][C])([O])[O]	304	275	PO4C1	PO4C1, Phosphor in Phosphate
[PX4](=[O])([O][C])([O][C])[O]	305	276	PO4C2	PO4C2, Phosphor in Phosphate
[PX4](=[O])([O][C])([O][C])([O][C])	306	277	PO4C3	PO4C3, Phosphor in Phosphate
[PX4](=[O])([O]([P]))([OH0])[OH0]	307	278	P-pyro	P-pyro, Phosphor in Pyrophosphate
[PX4](=[O])([O]([P]))([O]([P]))[OH0]	308	279	P-tri	P-tri, Phosphor in the middle of

				Triphosphate
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Figure S1. The normal mode frequencies of 10 common molecules by QM and MM. (Units: cm^{-1})



Vibrational spectrum of Biphenyl



Vibrational spectrum of Naphthalene

