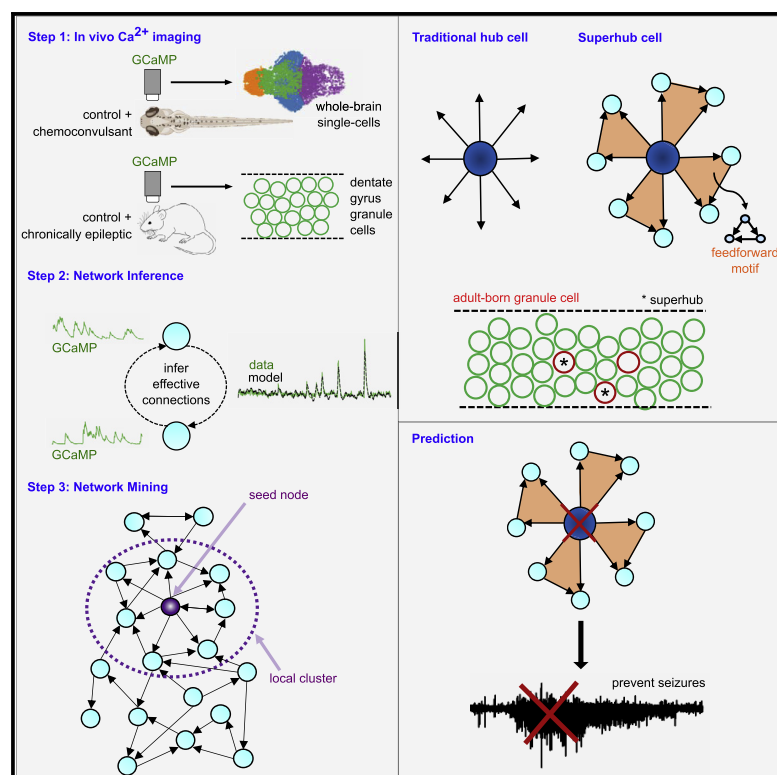


Maximally selective single-cell target for circuit control in epilepsy models

Graphical abstract



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In brief

Hadjiabadi et al. reveal a novel functional cell type, the superhub, that preferentially emerges in the pre-seizure brain to powerfully propagate excitation. Disconnecting superhubs in simulations stabilizes epileptic circuits more effectively than disconnecting traditional hubs, predicting a new single-cell target for seizure control.

Highlights

- Motif patterns of epileptic networks were inferred from single-cell calcium data
- Superhubs rich in excitatory feedforward motifs emerged in the pre-seizure state
- Disconnecting superhubs effectively stabilized epileptic circuits in simulations
- Superhubs are predicted to be adult-born granule cells in the mouse dentate gyrus



Article

Maximally selective single-cell target for circuit control in epilepsy models

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SUMMARY

Neurological and psychiatric disorders are associated with pathological neural dynamics. The fundamental connectivity patterns of cell-cell communication networks that enable pathological dynamics to emerge remain unknown. Here, we studied epileptic circuits using a newly developed computational pipeline that leveraged single-cell calcium imaging of larval zebrafish and chronically epileptic mice, biologically constrained effective connectivity modeling, and higher-order motif-focused network analysis. We uncovered a novel functional cell type that preferentially emerged in the pre-seizure state, the superhub, that was unusually richly connected to the rest of the network through feedforward motifs, critically enhancing downstream excitation. Perturbation simulations indicated that disconnecting superhubs was significantly more effective in stabilizing epileptic circuits than disconnecting hub cells that were defined traditionally by connection count. In the dentate gyrus of chronically epileptic mice, superhubs were predominately modeled adult-born granule cells. Collectively, these results predict a new maximally selective and minimally invasive cellular target for seizure control.

INTRODUCTION

Methods in network science have been instrumental in deciphering neural communication associated with neurological disorders (Bullmore and Sporns, 2009; Fornito et al., 2015). One such disorder, epilepsy, is characterized by spontaneous and recurrent seizures that arise from abnormal neural activity and synchronization across brain regions (Jiruska et al., 2013; Kramer and Cash, 2012). Epilepsy affects more than 60 million individuals worldwide, and many of these children and adults have medically uncontrolled seizures and suffer from debilitating cognitive and emotional comorbidities. One primary reason for this is that current anti-epileptic treatments lack spatial, temporal, and cell type specificity and instead attempt to broadly restrict excitability that can at best mask symptoms while producing various side effects (Löscher and Schmidt, 2011). Recently, a number of experimental studies demonstrated that it is possible to control spontaneous chronic seizures and co-

morbidities through closed-loop interventions. Importantly, these studies targeted specific cell ensembles in given brain regions and delivered intervention stimuli selectively only at particular times, all with minimal side effects (Bui et al., 2018; Krook-Magnuson and Soltesz, 2015; Krook-Magnuson et al., 2013, 2015). Although these experiments targeted groups of cells, the most desirable target for intervention would be single cells that exert maximal control over epileptic networks. In this study, we searched for a novel class of potential neuronal targets that could serve as maximally selective controllers for interventions to stabilize epileptic dynamics. To achieve this ambitious goal, we sought to uncover new features of cell-cell communication networks extracted from experimental data that are essential for pathological seizure dynamics to emerge.

One common feature of complex networks is the presence of richly connected yet sparse hub neurons (Barabási and Albert, 1999). It has been shown that these neurons are critical for influencing network dynamics in biological neural circuits (Bocchio

et al., 2020; Bonifazi et al., 2009; Morgan and Soltesz, 2008). Specifically, experimental studies have shown that hub neurons orchestrate network synchrony in the developing brain (Bonifazi et al., 2009) and maintain their effectiveness in adulthood (Bocchio et al., 2020). Simulations in a large-scale data-driven hippocampal dentate gyrus (DG) computational model of temporal lobe epilepsy (TLE) predicted that perturbation of a population of neurons that included hubs was sufficient to initiate a seizure (Morgan and Soltesz, 2008). These efforts have sparked significant interest in targeting hub neurons for effective seizure control (Bui et al., 2018; Krook-Magnuson et al., 2015). Although hub neurons are traditionally identified by considering lower order connectivity patterns at the level of nodes and edges, there is current interest in elucidating the higher order organization of complex networks. Specifically, the higher order organization of a complex network can be understood by identifying how small patterns of interconnections called motifs, which are widely believed to inform network function (Benson et al., 2016; Sporns and Kötter, 2004), are distributed throughout the network and causally drive functional dynamics. Therefore, it remains an open question whether a specialized subset of hub neurons can be leveraged for improved selective seizure control on the basis of their surrounding higher order network structure.

To address the latter question, we deployed whole-brain cellular resolution calcium imaging to capture neural dynamics in larval zebrafish, whose neuronal circuitry shares many conserved features with mammals (Lovett-Barron et al., 2017) and thus have been instrumental in basic (Burrows et al., 2020; Liu and Baraban, 2019) and translational (Baraban et al., 2013; Burrows et al., 2020) epilepsy research. Imaging was performed in a well-characterized zebrafish model of acute seizures (Baraban et al., 2005). The underlying cell-cell effective connectivity (i.e., communication) networks for baseline and pre-seizure neural dynamics were extracted (Sompolinsky et al., 1988; Sussillo and Abbott, 2009) and biologically constrained to the zebrafish neuroanatomical connectome for the first time (Kunst et al., 2019). Simulated perturbation of a single traditional hub neuron significantly destabilized pre-seizure networks compared with baseline networks. Higher order motif-focused analysis (Yin et al., 2017) of traditional hubs revealed that network instability in epileptic circuits is causally linked to a specific subset of hubs, which we call superhubs, whose surrounding neighborhood is rich in feedforward motifs, enhancing downstream excitation. Disconnecting these specialized superhub neurons robustly stabilized networks to perturbation, even though superhubs did not have the highest connection count among the broader hub cell class.

Importantly, similar results were also found in the hippocampal DG of chronically epileptic mice compared with control, indicating that our key findings hold in the mammalian brain and in a model of chronic TLE. Furthermore, superhubs in mice with chronic TLE were identified as being predominantly adult-born granule cells (abGCs), which are thought to play key roles in driving epileptiform activity in the DG network (Sparks et al., 2020) following seizure-induced reorganization (Danzer, 2018, 2019) and integration into the circuit (Toni et al., 2007, 2008). Collectively, these results identify superhubs as representing a new class of maximally selective potential targets for the control of epileptic networks.

RESULTS

Whole-brain calcium imaging of larval zebrafish acute seizure model at single-cell resolution

Whole-brain larval zebrafish (*Tg[elavl3:H2B-GCaMP6s]*; $N = 3$) imaging was performed with volumetric two-photon microscopy for 25 min at a 2 Hz capture rate (Figure 1A; see STAR Methods). This imaging approach enabled us to study intracellular calcium activity, where increases in the measured calcium signal correspond to an increase in neuronal firing rate. Five minutes of baseline calcium data were recorded for each fish, followed by a 15 mM pentylenetetrazol (PTZ) (Baraban et al., 2005; Liu and Baraban, 2019) bath application, which blocks inhibitory GABA_A conductance (Huang et al., 2001). Each fish exhibited at least one seizure prior to cessation of imaging. Local field potential (LFP) recording was not included, as previous studies have shown a robust correlation between calcium signal and field potentials in a PTZ model (Liu and Baraban, 2019). Anatomical volume stacks were registered, and neural somata (Figure 1B) were extracted with methods used by Lovett-Barron et al. (2017). We extracted fluorescence time series from 5,000–7,000 active neurons per fish across all major brain regions (Figure 1C).

The start of the pre-seizure state was defined as 1 min after PTZ was introduced, to account for transient activity. Seizure initiation was defined as 3 standard deviations above the population mean calcium signal during baseline (pre-PTZ), and termination was defined as when the population mean signal dropped below this threshold. In agreement with prior literature (Liu and Baraban, 2019), calcium dynamics within the detected seizure periods lasted 35–40 s and displayed significantly higher synchronicity (i.e., hypersynchronous state) compared with baseline (one-sided paired *t* test, adjusted $p = 0.034$) and pre-seizure (one-sided paired *t* test, adjusted $p = 0.006$) epochs (Figures 1D and 1E; synchronization: in baseline network, 0.28 ± 0.024 ; in pre-seizure network, 0.375 ± 0.04 ; in seizure network, 0.55 ± 0.038). For this work, we will be modeling baseline and pre-seizure calcium dynamics (Figure 1F), and we will not be focusing on seizure or post-seizure periods.

Cellular resolution effective connectivity modeling to extract cell-cell communication networks

Effective connectivity modeling was performed with chaotic recurrent neural networks (RNNs) (Sompolinsky et al., 1988; Figure 2A; see STAR Methods) to extract cell-cell communication networks. These methods have been previously successful in fitting cellular resolution calcium dynamics in the zebrafish (Andalman et al., 2019). Each neuron imaged experimentally is represented by a node in the model. The parameters of the model are the effective connections between nodes, interpreted as how much causal influence a source has on its target over a sub-second temporal window, and can vary in sign and magnitude. The self-perpetuating chaotic dynamics were controlled through FORCE learning (Sussillo and Abbott, 2009; STAR Methods), which uses a recursive least square optimization on the connectivity parameters to reproduce a specified target output.

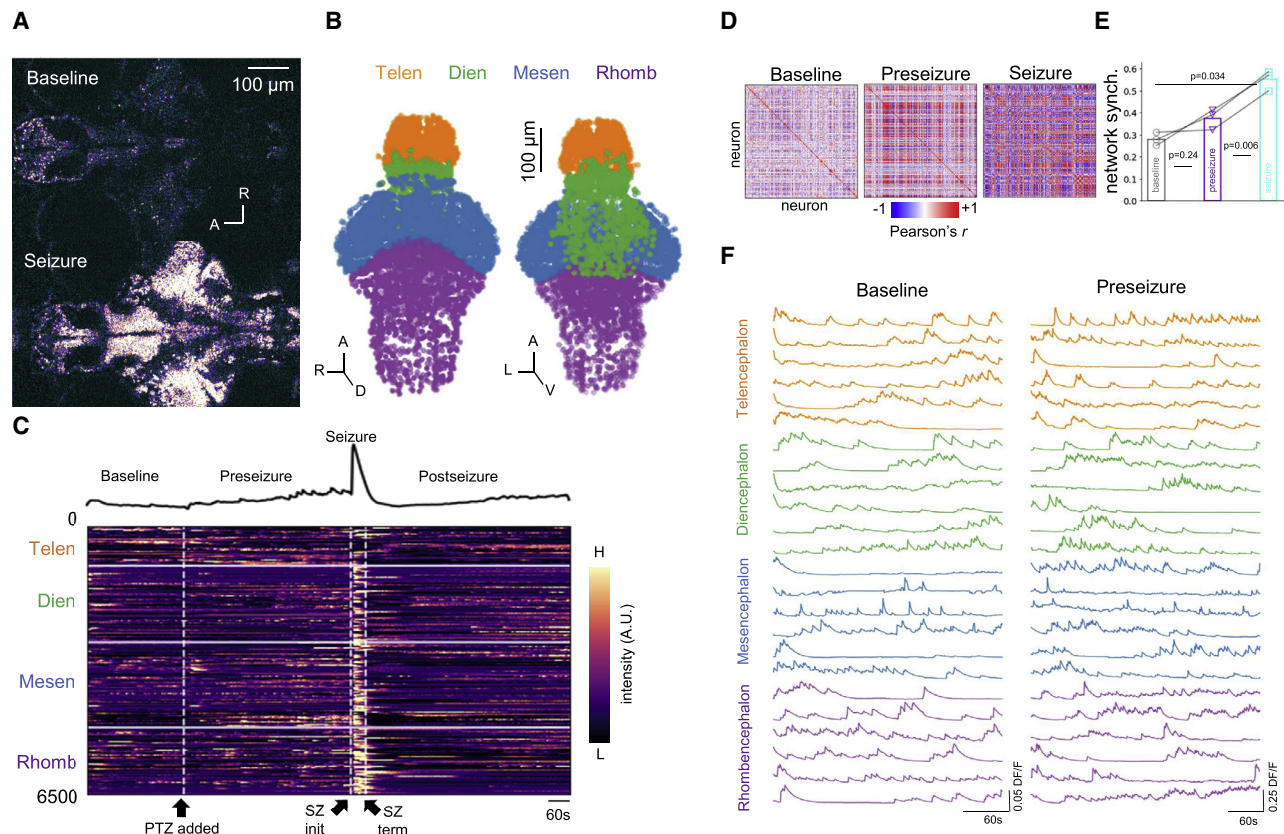


Figure 1. Whole-brain imaging of larval zebrafish acute seizure model at single-cell resolution

(A) Representative z-plane images acquired from whole-brain cellular resolution two-photon microscopy of larval zebrafish before PTZ application (Baseline; top) and during PTZ-induced seizure (Seizure; bottom).

(B) Extracted neural somata point cloud. Colors indicate major brain regions. Orange, telencephalon; green, diencephalon; blue, mesencephalon; purple: rhombencephalon.

(C) (Top) Population mean calcium signal and (bottom) heatmap of single-cell functional calcium dynamics from neurons extracted in (B). PTZ application, seizure initiation, and seizure termination are demarcated by black arrows at bottom. Imaging was performed for 25 min and PTZ was added 5 min into the imaging session.

(D) Correlation coefficient matrices of single-cell calcium dynamics during baseline, pre-seizure, and seizure epochs.

(E) Quantification of network synchrony from correlation coefficient matrices in (D) show that single-cell calcium dynamics during seizure epoch are significantly more synchronized compared with single-cell calcium dynamics in baseline (one-sided paired t test, adjusted $p = 0.034$) and in pre-seizure (one-sided paired t test, adjusted $p = 0.006$ epochs). Bar graphs represent the mean of the population ($N = 3$ zebrafish).

(F) Single-cell calcium traces over major anatomical regions plotted during baseline and pre-seizure epochs. Note the differences in vertical scale bars.

Target outputs were the experimentally acquired calcium dynamics. We furthermore used a 10% sparsity constraint ($\binom{N_s(N-1)}{10}$ total parameters) to match reported connectivity patterns (Song et al., 2005) and to prevent overfitting. One major issue is whether local minima visited during optimization lead to parameter sets that are realistic given the underlying neuroanatomy. To mitigate this, we constrained the optimization procedure using the known zebrafish structural connectome (Kunst et al., 2019; Figure 2B; STAR Methods). Specifically, weights are adjusted proportional to how strongly connected the regions in which the source soma and target soma inhabit (Figure 2C, “Learning rule”). Pre-seizure networks were optimized from best-fit baseline networks in order to untangle cell-cell effective rewiring caused by PTZ (Figure 2C, “Training pipeline”). For consistency, this was repeated three times with different initial conditions for each fish. Models converged for both baseline and pre-seizure

state (Figure 2C, “Training pipeline”), and FORCE learning captured individual and global calcium dynamics (Figure 2D, note scale bars).

Community detection using the Leiden algorithm (Traag et al., 2019) on the constrained optimized parameter matrix identified relevant macroscale anatomical structures that were not observed in the unconstrained models (Figure S1; see STAR Methods). Furthermore, model dynamics were driven primarily by synaptic transmission and not noise (Figures S2A and S2B). For each modeled zebrafish, the outgoing inhibition per neuron, calculated as the absolute value of the sum of outgoing negative effective weights, decreased on average across the population after PTZ application (Figure S2C). This suggests that the modeled communication networks capture the primary effect of PTZ, which is known to be a reduction of inhibitory conductances (Huang et al., 2001).

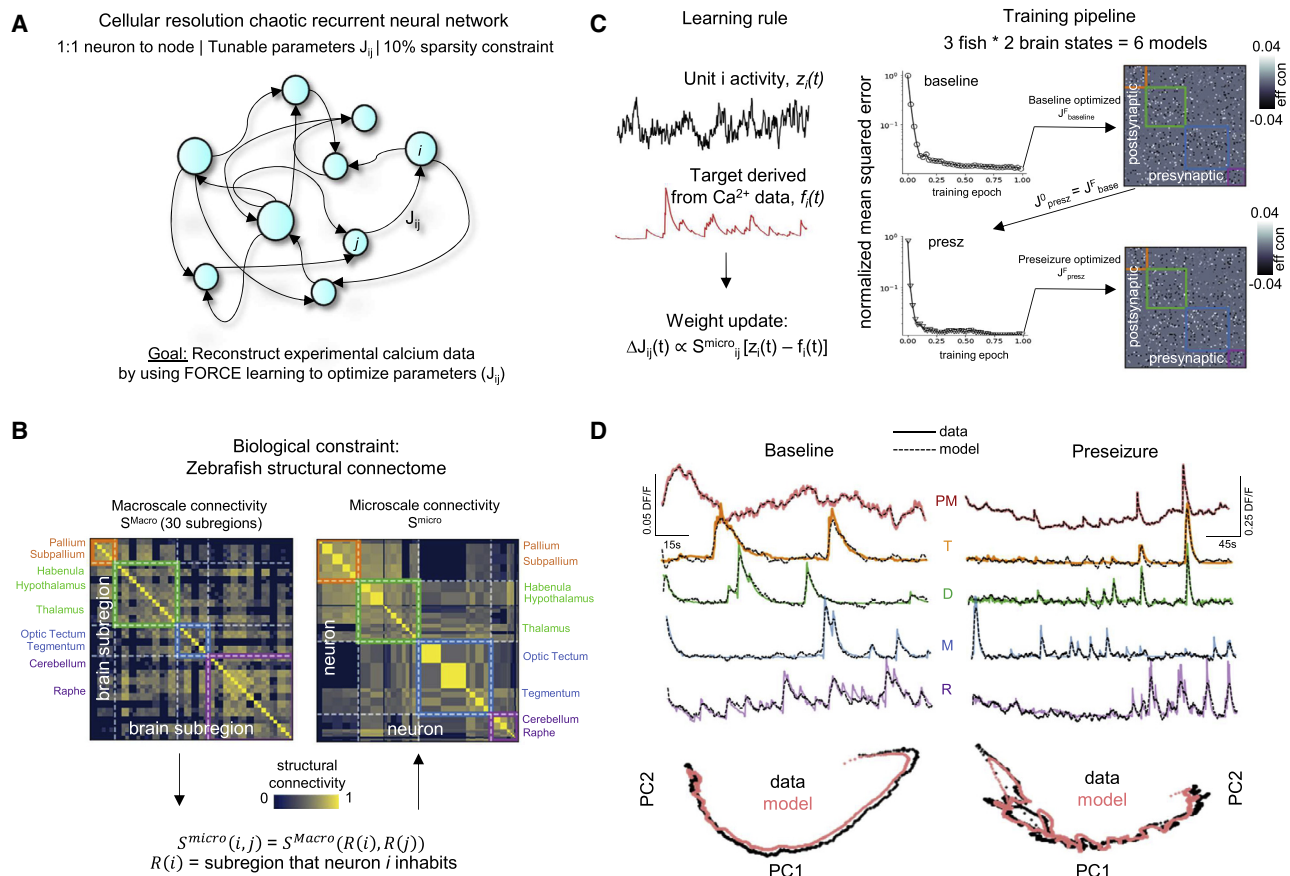


Figure 2. Cellular resolution effective connectivity modeling to extract cell-cell communication networks

(A) Cellular resolution chaotic recurrent neural network (RNN) with 10% sparsity constraint to prevent overfitting. Each neuron imaged in the larval zebrafish is represented as a node in the RNN. Edges represent parameters of the model and were optimized with FORCE learning to match experimental calcium data.

(B) The zebrafish structural connectome was incorporated as a biological constraint. Left: zebrafish macroscale connectivity matrix (S^{Macro}). Right: zebrafish microscale connectivity (S^{Micro}), which represents the strength of connectivity between the regions in which neurons i and j occupy.

(C) Learning rule: FORCE learning tunes the weight J_{ij} between neuron i (target) and j (source). The update is proportional to the structural connectivity score S^{Micro}_{ij} , multiplied by the difference between unit activity of node i (black trace) and target Ca^{2+} waveform acquired experimentally (red trace). Training pipeline: models converged using the weight update that incorporated the structural connectome. The baseline model was trained on baseline calcium dynamics with an initial random matrix. To map the changes to the underlying microcircuit connectivity resulting from bath wash in of PTZ, the optimized parameters of the baseline model were then used as the seed for training the preseizure model on preseizure calcium dynamics. See also Figure S1.

(D) Representative examples of mean population Ca^{2+} trace and individual Ca^{2+} traces with modeled fits overlaid for baseline (left) and preseizure (right) dynamics. Note the scale bars. Bottom: principal-component analysis (PCA) of experimental (black) and modeled (red) calcium activity. PM, population mean; T, telencephalon; D, diencephalon; M, mesencephalon; R, rhombencephalon. See also Figure S2.

Identification of outgoing and incoming traditional hubs

Traditional hub neurons were segregated into two classes on the basis of connection count: incoming and outgoing (Figure 3A). Outgoing hubs project while incoming hubs receive numerous strong connections. The optimized parameter matrix was binarized by keeping only the strongest excitatory connections (top 10%; Figure 3B). The outgoing and incoming degree distributions across brain states were quantified and displayed heavy-tailed properties, as reported experimentally (Bonifazi et al., 2009; Figure 3C). Outgoing hubs were defined as the top 10% (i.e., 90th percentile and above) of cells with the most outgoing connections, and incoming hubs were defined as the top 10% of cells with the most incoming connections (note that changing the cutoff to a different percentile did not alter the key findings;

see below). The cutoff values were independently calculated for incoming and outgoing hubs and between baseline and preseizure distributions (Figure 3C).

Importantly, the normalized outgoing (baseline, 0.0129 ± 0.0006 ; preseizure, 0.0135 ± 0.0005) and incoming (baseline, 0.0131 ± 0.00022 ; preseizure, 0.0124 ± 0.0007) hub cutoff thresholds, reported as the outgoing and incoming cutoff threshold divided by the number of possible connections a single node can make in a graph with N nodes (i.e., $N - 1$) was not significant between modeled baseline and modeled preseizure networks (two-sided unpaired t test, $p > 0.05$) (Figure 3D). Additionally, the percentage change of the average outgoing (incoming) degree of outgoing (incoming) hubs in modeled preseizure networks relative to modeled baseline networks was not statistically

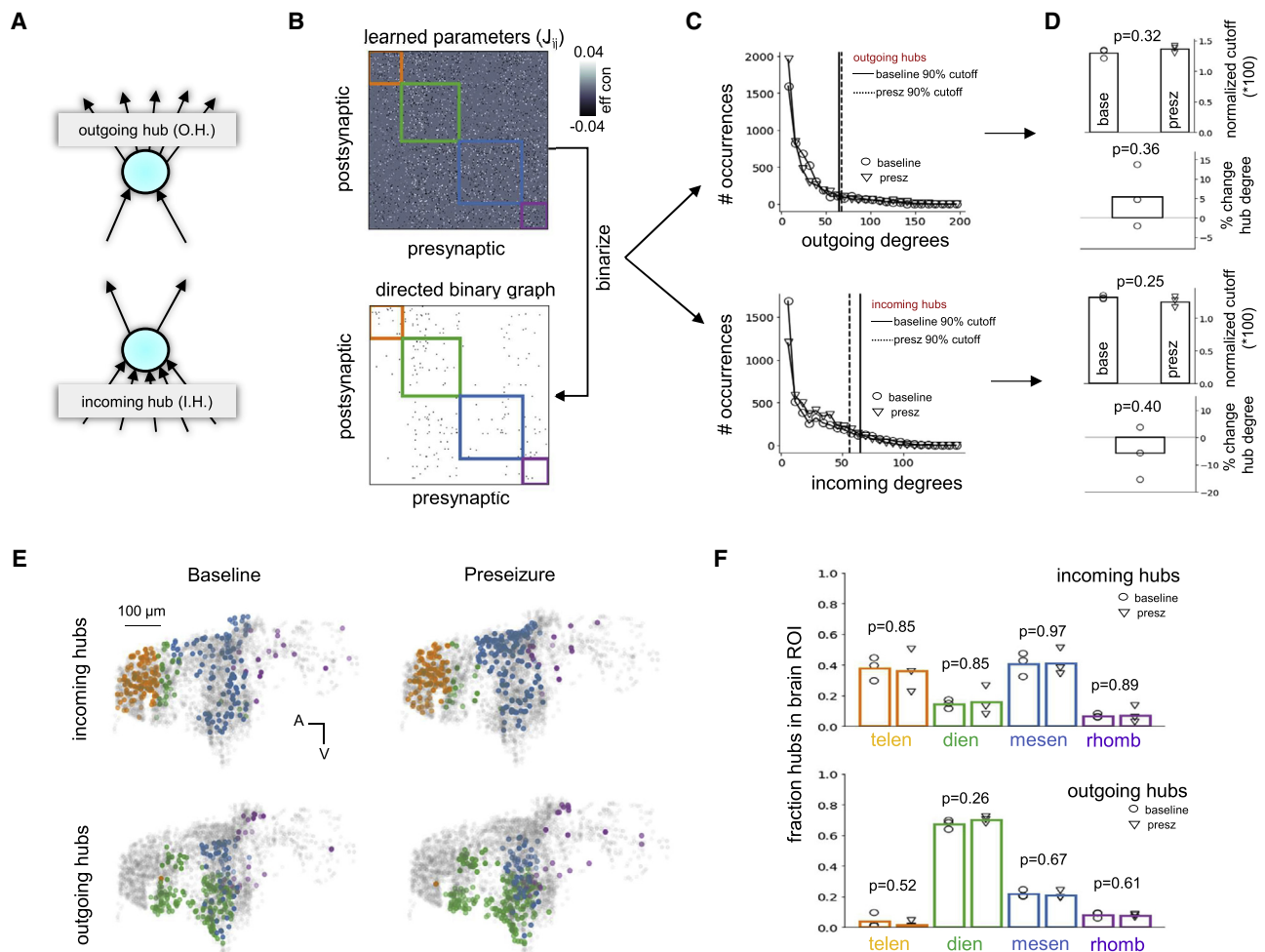


Figure 3. Identification of outgoing and incoming hubs

(A) Hub neurons from modeled networks were separated into incoming (numerous and strong postsynaptic inputs) and outgoing (numerous and strong presynaptic outputs).

(B and C) Algorithm for identifying incoming and outgoing hub neurons in an effective connectivity matrix optimized through constrained FORCE learning. (B) The learned parameters (top) are binarized into a 0-1 graph (bottom) by keeping the top 10% of excitatory weights. Then, the incoming and outgoing degree for each neuron is calculated from the binarized graph. (C) Baseline and pre-seizure network degree distributions for outgoing (top) and incoming (bottom) degree are heavy tailed, resembling a power law. A 90% cutoff (vertical lines) was used to identify outgoing and incoming hubs in each network.

(D) Ninety percent threshold cutoff normalized by the number of possible connections a single node can make in a graph with N total nodes (i.e., $N - 1$) and percentage change of average hub degree as measured from outgoing (top) and incoming (bottom) degree distributions. Neither parameter was statistically significant between baseline and pre-seizure networks (two-sided unpaired t test, $p > 0.05$). Bar graphs represent the mean of the population ($N = 3$ zebrafish).

(E) Spatial distribution of incoming (top) and outgoing (bottom) hubs for modeled baseline and pre-seizure networks. Orange, telencephalon; green, diencephalon; blue, mesencephalon; purple, rhombencephalon.

(F) Fraction of incoming (top) and outgoing (bottom) hubs residing in each macroscale brain region for baseline (open circle) and pre-seizure (open triangle) networks. Incoming hubs were consistently localized to telencephalon and mesencephalon. Outgoing hubs were consistently localized to diencephalon. Baseline and pre-seizure networks had similar macroscale spatial organization of incoming and outgoing hubs (two-sided unpaired t test, $p > 0.05$). Bar graphs represent the mean of the population ($N = 3$ zebrafish).

different from zero (two-sided unpaired t test, $p > 0.05$; outgoing hubs percentage change in outgoing degree, $5.4\% \pm 6\%$; incoming hubs percentage change in incoming degree, $-5.8\% \pm 7.8\%$) (Figure 3D). The spatial locations of outgoing and incoming hub neurons were visualized in the zebrafish anatomy for both baseline and pre-seizure networks (Figure 3E). Outgoing hubs were located primarily in the diencephalon, and incoming hubs were located primarily in the mesencephalon

and the telencephalon (Figure 3F). PTZ did not cause significant changes in the macroscale anatomical locations of outgoing and incoming hubs (Figure 3F) (two-sided unpaired t test, $p > 0.05$).

Perturbation of individual outgoing hubs destabilizes pre-seizure networks

Chaotic RNNs are a generative model and can therefore create synthetic calcium traces for each cell. Single-cell perturbation

simulation studies are of growing importance for studying functional properties of large neural populations and have to date elucidated how activity is coordinated in recurrent cortical networks (Sadeh and Clopath, 2020). With this in mind, we tested the hypothesis that the modeled pre-seizure networks are more sensitive to perturbation of a single hub neuron compared with baseline networks. Simulated perturbations involved 500 ms depolarizing current injection into a single hub neuron after 20% of epoch duration had elapsed. We quantified the effect of perturbation on global network dynamics by measuring the “trajectory deviation,” which is the time-normalized Euclidean distance between the mean population calcium signal of the unperturbed network and the mean population calcium signal of the perturbed network. Intuitively, the trajectory deviation metric captures how far network dynamics deviate after a user-defined perturbation, relative to the unperturbed network. The larger the trajectory deviation, the more effect a perturbation has on the system. Note that only one neuron was depolarized at a time during a given perturbation simulation.

Depolarizing a single outgoing hub in the pre-seizure network caused significantly higher deviation (one-sided Mann-Whitney U test, $p < 0.001$) in global dynamics (Figures 4B and 4C) compared with equivalent simulations in baseline networks (Figures 4A and 4C). Depolarizing a single incoming hub and a single non-hub had significantly less influence in both networks compared with depolarizing individual outgoing hubs (Figure 4C; Figures S3A and S3B). Additionally, the effect of perturbation of single neurons was larger in modeled pre-seizure networks than in modeled baseline networks. Importantly, perturbation of a single incoming hub affected dynamics to a greater degree (one-sided Mann-Whitney U test, $p < 0.001$) in pre-seizure networks compared with baseline networks (Figure 4C). We normalized the trajectory deviation distribution acquired from perturbing individual outgoing hubs by the median trajectory deviation from the incoming hub population. The data show that perturbation of a single outgoing hub in the pre-seizure state altered global dynamics more significantly compared with baseline networks both within individual fish (one-sided Mann-Whitney U test, $p < 0.001$) (Figure 4D) and across the population (one-sided paired t test, $p = 0.041$) (Figure 4E; percentage deviation: baseline, $170\% \pm 24\%$; pre-seizure, $327\% \pm 66\%$). Taken together, these results suggest that pre-seizure networks are more sensitive to perturbations and that perturbing even a single outgoing hub neuron can significantly influence global dynamics.

Visualizing connections between outgoing and incoming hubs

PTZ application did not significantly change several parameters associated with the outgoing and incoming degree distributions (Figures 3C and 3D) and did not significantly reorganize which macroscale anatomical regions the hub cells occupied (Figures 3E and 3F). Therefore, we hypothesized that nuanced rewiring of microcircuit effective connectivity patterns may be critical for understanding the increased sensitivity of the network to perturbation in the pre-seizure state (Figure 4). We visualized the connectivity patterns between outgoing and incoming hubs for baseline (Figure 4F) and pre-seizure (Figure 4G) networks using force-directed graphs (Barnes and Hut, 1986; STAR

Methods). Importantly, nodes clustered in the force-directed graphs are highly connected. We observed an increased number of outgoing-outgoing hub connections (Figure 4G, note golden edges forming a “core”; see also Figure S3C) in the pre-seizure networks compared with the baseline networks. We next performed rich-club analysis (Smilov and Kocarev, 2010; Towilson et al., 2013) to determine if the increase in connections between outgoing hubs in the pre-seizure networks led to the emergence of a “rich-club” phenomenon. Intuitively, a rich-club describes a highly privileged group of strongly connected nodes that are very tightly connected with one another. This idea is captured by measuring the rich-club coefficient, which varies as a function of degree k and is normalized to random graphs. If the coefficient is greater than 1 as k approaches k_{max} , the highest observed degree in the graph, then this implies the existence of a rich-club. We observed that both the baseline and pre-seizure networks exhibited a rich-club phenomenon only when considering the fully directed graph and that the outgoing rich-club coefficient was higher for the pre-seizure network (Figure S3D). Therefore, this further validates the observed increase in effective connections between outgoing hubs (Figure S3C) in the pre-seizure brain and the existence of the golden “core” in Figure 4G.

To better interrogate how effective connections in the pre-seizure networks are distributed across the outgoing hub population, we turned to understanding the distribution of higher order motifs, which are, as previously mentioned, small patterns of interconnections that are thought to provide insight on the functional properties of complex systems (Benson et al., 2016; Sporns and Kötter, 2004). In a baseline toy model (Figure 4H, top), there is a single connection between outgoing hubs and two feedforward motifs present. On the basis of observations in Figure 4G, there are more connections between outgoing hubs. Thus, the pre-seizure toy model (Figure 4H, bottom) includes an additional connection between outgoing hubs 2 and 3. As a result of adding a single connection, there are now four feedforward motifs present in the network. Therefore, we hypothesized that the multiplicative emergence of feedforward motifs may be a core feature of cell-cell communication networks that destabilize the pre-seizure brain.

Preferential emergence of superhubs in the pre-seizure brain

Graph clustering is an intuitive method to isolate groups of nodes in a network that form numerous intra-group connections. Specifically, we predict the emergence of superhubs—hubs surrounded by higher order motifs—using a higher order motif-focused local clustering concept. To this effect, we deployed the Motif-based Approximate Personalized PageRank (MAPPR) algorithm (Yin et al., 2017), which finds higher order motif-focused clusters. The inputs to the algorithm were the directed binarized graph (Figure 3B), a motif M , and an individual outgoing hub identified in Figure 3C (i.e., the seed). The algorithm finds an optimal local cluster surrounding the seed that is rich in M with run time that is invariant of the graph size (Figure 5A, left). Traditional edge clustering was also performed as a control using the APPR algorithm (Andersen et al., 2006; Figure 5A, right). Note that the MAPPR algorithm is a more generalized form of the APPR algorithm, as the latter considers only simple edges. To

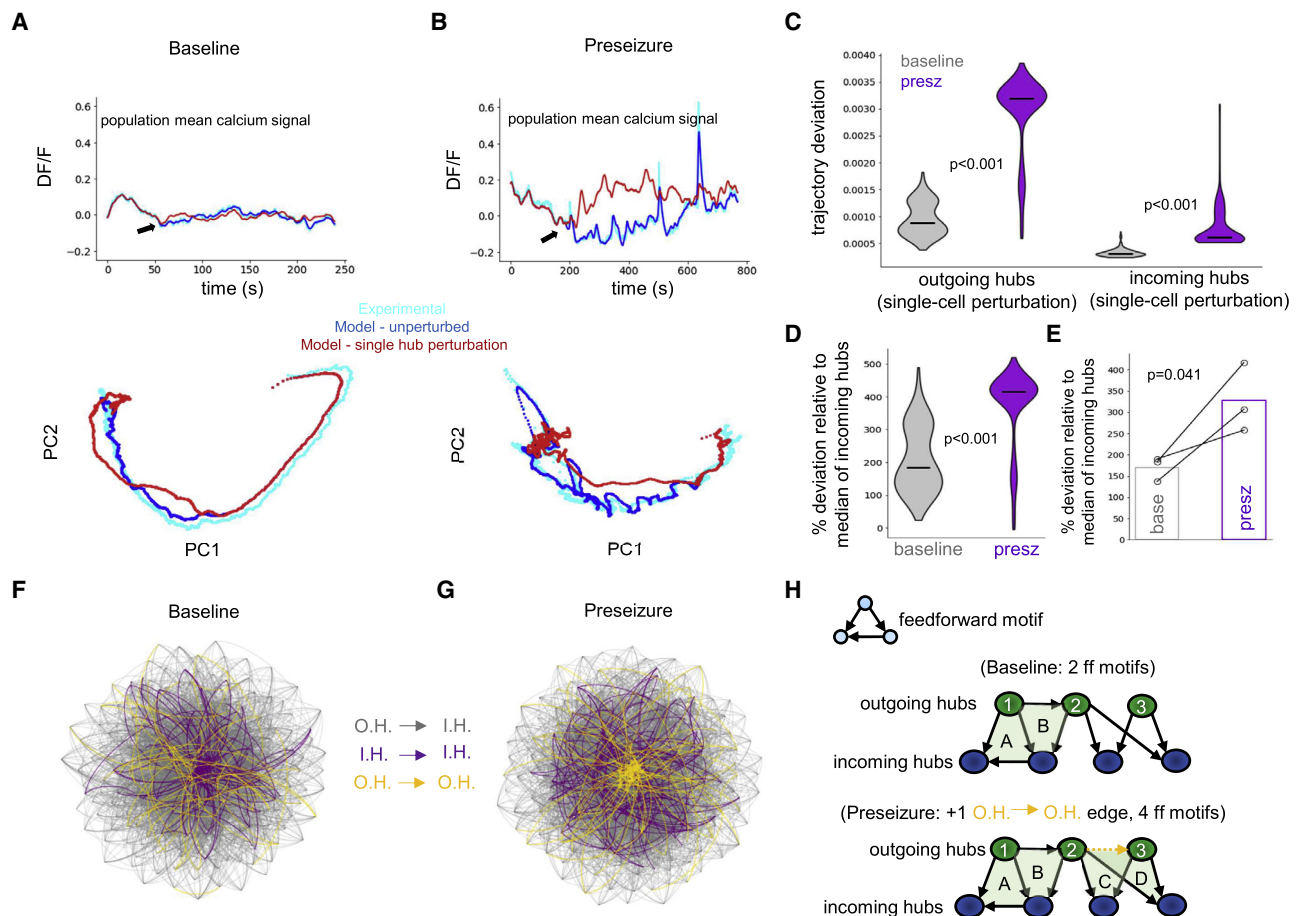


Figure 4. Perturbation of individual outgoing hubs destabilizes pre seizure networks

(A) Modeled control network response to perturbation (black arrow) of a single outgoing hub. Top: population mean calcium signal of experimental data (cyan), unperturbed model (blue), and perturbed model simulation (red). Bottom: principal-component analysis (PCA) reveals little change in network dynamics in response to perturbation.

(B) Perturbation of a single outgoing hub in modeled pre seizure network showing significant changes to network dynamics compared with (A).

(C) Violin plots show that perturbing individual outgoing hubs (one-sided Mann-Whitney U test, $p < 0.001$; $N = 310$ modeled cells) and incoming hubs (one-sided Mann-Whitney U test, $p < 0.001$; $N = 300$ modeled cells) in modeled pre seizure networks (purple) had significantly higher influence on network dynamics compared with similar simulations in baseline networks (gray). See also Figure S3. Center marker of the violin plot represents the median.

(D) Outgoing hub trajectory deviation distributions in modeled baseline (gray) and pre seizure networks (purple) normalized by incoming hub median trajectory deviation score for the respective populations. Perturbation of outgoing hubs in pre seizure state has significantly more influence over network dynamics (one-sided Mann-Whitney U test, $p < 0.001$; $N = 310$ modeled cells). Center marker of the violin plot represents the median.

(E) Median values from (D) were extracted for each fish and plotted, revealing that pre seizure networks have significantly reduced resiliency to perturbation of a single outgoing hub (one-sided paired t test, $p = 0.041$). Bar graphs represent the mean of the population ($N = 3$ zebrafish).

(F and G) Visual representation of connections between outgoing and incoming hubs for baseline (F) and pre seizure (G) network after constrained FORCE learning. Graphs were generated using the Barnes-Hut algorithm (Barnes and Hut, 1986). Gray edges, outgoing hubs (O.H.) to incoming hubs (I.H.); purple edges, incoming hubs to incoming hubs; golden edges, outgoing hubs to outgoing hubs. See also Figure S3.

(H) Toy model of connections between outgoing (green) and incoming (blue) hubs for baseline (top) and pre seizure (bottom) networks.

find optimal clusters, both algorithms minimize a conductance metric (edge conductance for APPR, motif conductance for MAPPR; see STAR Methods), the edge (motif) conductance metric was furthermore used to capture how much information or activity propagates from the traditional (motif-focused) cluster to the rest of the network (Figure 5B) and can be thought of as an analog to conductance in an electrical circuit.

Edge conductance and feedforward motif conductance were elevated in the modeled pre seizure networks both across indi-

vidual fish (Figure 5C; edge conductance: one-sided Mann-Whitney U test, $p < 0.001$; feedforward motif conductance: one-sided Mann-Whitney U test, $p < 0.001$) and across the population (Figure 5D; edge conductance: baseline, 0.39 ± 0.0068 ; pre seizure, 0.41 ± 0.005 ; one-sided paired t test, $p = 0.011$; feedforward conductance: baseline, 0.145 ± 0.01 ; pre seizure, 0.218 ± 0.017 ; one-sided paired t test, $p = 0.033$). However, the increase in feedforward motif conductance relative to baseline was significantly higher (one-sided paired t test, $p = 0.047$)

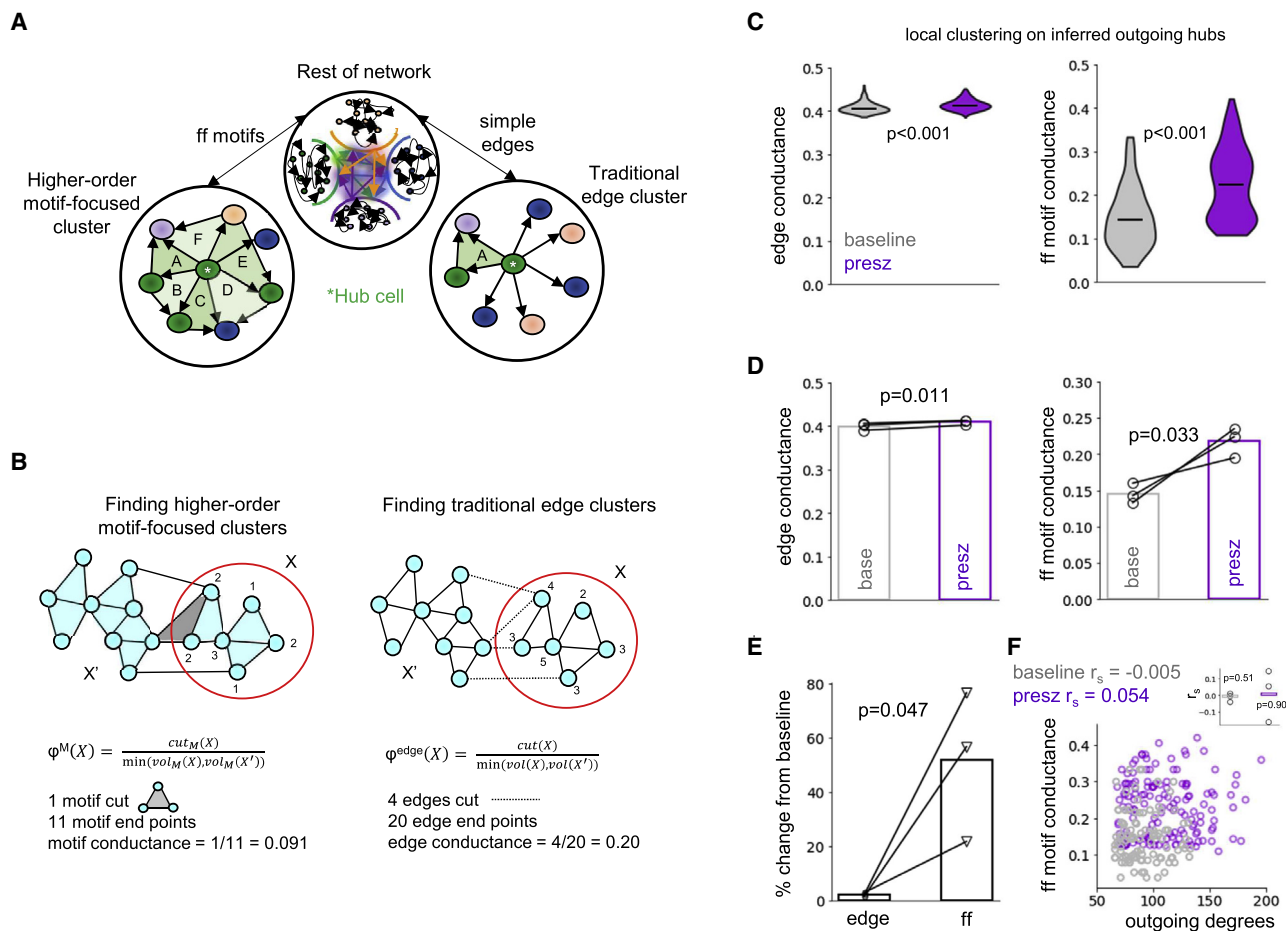


Figure 5. Preferential emergence of superhubs in the preseizure brain

(A) Higher order motif-focused clustering enables identification of a collection of nodes that form rich feedforward connections with a single hub neuron (left). This approach contrasts to traditional edge clustering, which considers only simple edges (right). Note that different clusters emerge depending on which method is used.

(B) Toy model of higher order motif-focused clustering (left) and edge clustering (right) (from Yin et al., 2017). Edge conductance quantifies the cluster quality by considering the ratio of edges that span between partitions and that reside completely inside the partition. The motif conductance metric measures the same ratio but with respect to motifs. Intuitively, the higher the conductance, the more easily it is for excitatory activity to propagate downstream.

(C) Violin plots of edge conductance (left) and feedforward motif conductance (right) of outgoing hub neurons, with the center marker representing the median. Both edge (one-sided Mann-Whitney U test, $p < 0.001$; $N = 310$ modeled cells) and feedforward motif conductance (one-sided Mann-Whitney U test, $p < 0.001$; baseline $N = 103$ modeled cells, presz $N = 151$ modeled cells) are higher in modeled preseizure than modeled baseline networks. However, note the differences in range. This predicts the emergence of “superhubs” in preseizure networks. See also Figures S4 and S5 and see STAR Methods for exclusionary criteria when quantifying feedforward motif conductance.

(D) Edge conductance (one-sided paired t test, $p = 0.011$) and feedforward motif conductance (one-sided paired t test, $p = 0.033$) are significantly increased in modeled preseizure networks across the sample population. Medians from (C) are plotted, and bar graphs represent the mean of the population ($N = 3$ zebrafish).

(E) Percentage change of feedforward motif conductance relative to baseline was significantly greater than edge conductance (one-sided paired t test, $p = 0.047$). Bar graphs represent the mean of the population ($N = 3$ zebrafish).

(F) Scatterplot of feedforward motif conductance versus outgoing degree of hubs in baseline ($N = 103$ modeled cells) and preseizure ($N = 151$ modeled cells) networks reported no significant correlation (baseline Spearman’s $\rho = -0.005$, $p > 0.05$; preseizure Spearman’s $\rho = 0.054$, $p > 0.05$) between the two variables individually or as a group (see inset; bar graph represents the mean of the population, $N = 3$ zebrafish). See also Figure S6.

than edge conductance ($51.8 \pm 22.7\%$ versus $2.4 \pm 0.55\%$; Figure 5E). We also performed local higher order motif-focused clustering on additional motifs, such as cycles, but found no examples of cycle motifs surrounding outgoing hubs. More specifically, motif enumeration using an efficient detection algorithm (Wernicke, 2006) showed that <10 cycles existed in the full zebrafish network for both baseline and preseizure states, whereas

feedforward motifs were extremely dominant ($>25,000$) (Figure S4). Therefore, these data suggest that a subset of outgoing hubs in preseizure networks allows excitation to propagate more readily to the rest of the network via feedforward motifs, predicting the preferential emergence of “superhubs.” Importantly, both individually (baseline Spearman’s $\rho = -0.005$, $p > 0.05$; preseizure Spearman’s $\rho = 0.054$, $p > 0.05$) and as a group

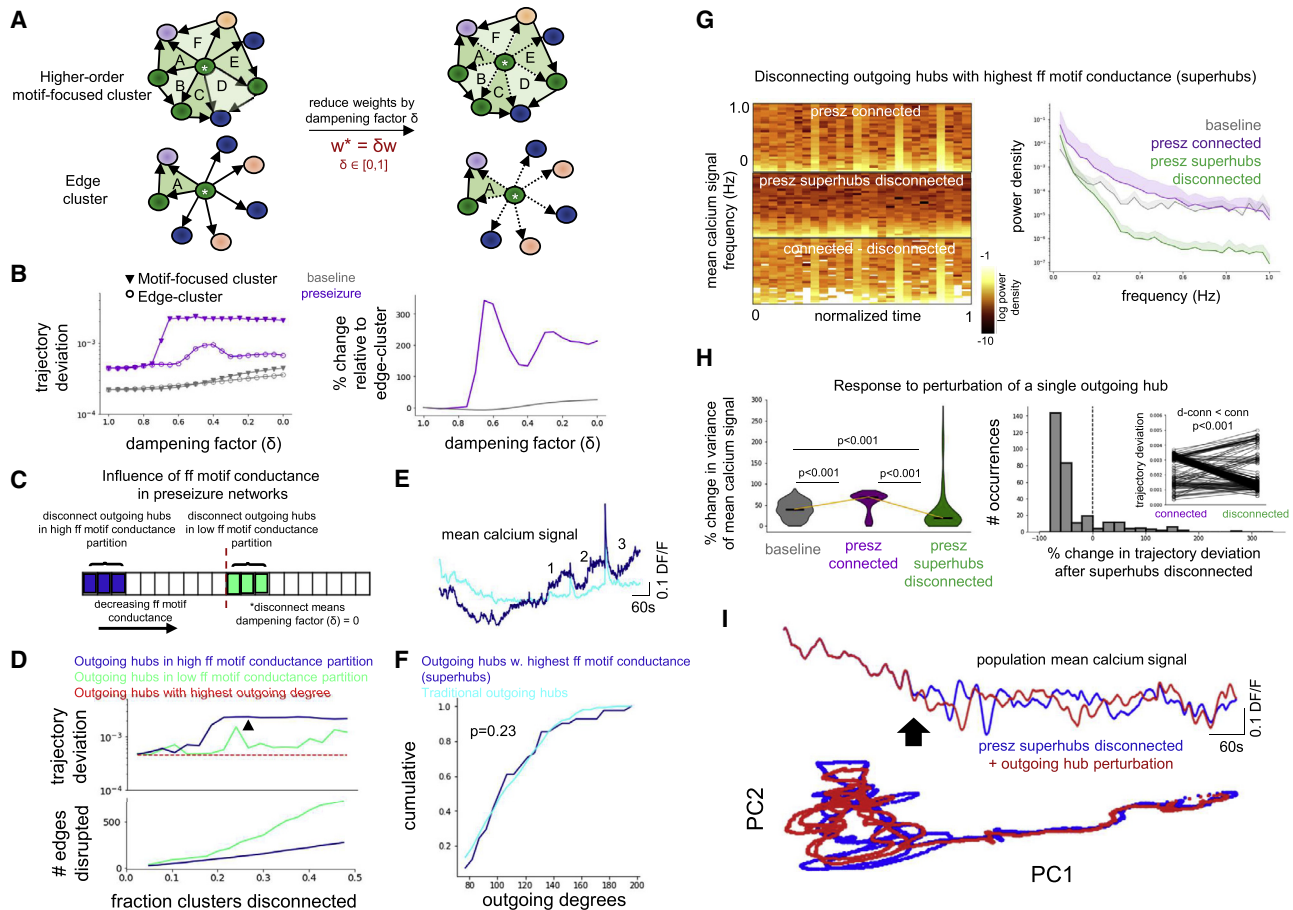


Figure 6. Disconnecting superhubs stabilizes pre-seizure networks

(A) Edge weights of all outgoing hubs targeting its edge cluster constituents and higher order motif-focused cluster constituents were dampened to explore relative importance of simple edges versus edges belonging to feedforward motifs on network dynamics.

(B) Left: connections from outgoing hubs projecting to their traditional edge-cluster (open circle) and to their higher order motif-focused clusters (closed triangle) were progressively dampened for modeled baseline (gray) and pre-seizure (purple) networks. Dampening higher order motif-focused clusters had greater effect on network dynamics than dampening traditional edge clusters, as measured by trajectory deviation. Right: trajectory deviation from dampening higher order motif-focused clusters relative to dampening traditional edge clusters shows a greater effect in the pre-seizure network than the baseline network.

(C) Schematic for testing the effect of disconnecting outgoing hubs with the highest feedforward motif conductance versus lowest feedforward motif conductance on modeled pre-seizure network dynamics.

(D) Top: trajectory deviation versus fraction of higher order motif-focused clusters disconnected in the high feedforward motif conductance (blue) and low feedforward motif conductance (green) partitions show that disconnecting higher conductance clusters has greater effect on network dynamics. The black arrowhead is located at the 27.5% cutoff for superhubs ($N = 41$ modeled cells), which is where blue trace exhibits a stable plateau in the trajectory deviation. Bottom: number of edges disconnected for each group shows that the high conductance partition (blue) contains fewer edges than the low conductance partition (green).

(E) Mean calcium signal of outgoing hubs with the highest feedforward motif conductance values (i.e., superhubs) and the traditional outgoing hub population. Note the numbers identifying an increase in the mean calcium signal of superhubs preceding and between high-calcium events.

(F) Outgoing degree cumulative distribution for superhubs ($N = 41$ modeled cells) versus traditional outgoing hubs ($N = 269$ modeled cells). Importantly, superhubs are not biased toward the highest outgoing degrees (one-sided KS-test, $p = 0.23$).

(G) Left: mean population calcium signal spectrograms generated from unchanged/connected pre-seizure network (top), pre-seizure network with superhubs disconnected (middle), and difference. Right: power spectral density (PSD) of mean population calcium signal for baseline (gray), connected pre-seizure (violet), and pre-seizure network with superhubs disconnected (green). Disconnecting superhubs reduces power over the measured frequency ranges.

(H) Left: the variance (i.e., total power) of the mean population calcium signal is measured before and after perturbation of a single outgoing hub, and the percentage change is quantified. The percentage change in total power is elevated when perturbing individual outgoing hubs in the fully connected pre-seizure network (purple) compared with baseline network (gray) (one-sided Mann-Whitney U test, adjusted $p < 0.001$), indicating that the pre-seizure network is more unstable. The percentage change in total power is significantly lower in the pre-seizure network with superhubs disconnected (green) compared with the fully connected pre-seizure network (purple) (one-sided Wilcoxon signed-rank test, adjusted $p < 0.001$). Furthermore, the percentage change in total power after perturbing individual hubs is significantly lower between the pre-seizure network with superhubs disconnected (green) and the baseline network (gray) (one-sided Mann-Whitney U test, adjusted $p < 0.001$), altogether providing evidence that disconnecting superhubs very robustly stabilizes pre-seizure networks. $N = 310$ modeled cells for all groups. Center marker of violin plots represents the median. Right: percentage change of the network trajectory deviation is significantly

(legend continued on next page)

(unpaired two-sided *t* test, $p > 0.05$), feedforward motif conductance was not correlated to outgoing degree of the outgoing hub (Figure 5F). These findings were not dependent on the sparsity constraint used (Figure S5). Additionally, feedforward motif conductance was not correlated to other widely used network measures that leverage traditional edge information, such as local clustering coefficient (Watts and Strogatz, 1998; Figure S6A) and betweenness centrality (Freeman, 1977; Figure S6B).

Disconnecting superhubs stabilizes pre seizure networks

Our evidence so far suggests a correlation between two findings: (1) perturbation of a single outgoing hub in pre seizure networks has significant influence on global network dynamics, and (2) emergence of superhubs in the pre seizure state, defined as outgoing hub neurons with elevated feedforward motif conductance, may play a critical role in propagating excitatory activity to the rest of the network. To establish a causal link, we performed several computational experiments. These simulations involved targeted attacks on hub neurons. The motivation for this is that complex networks in nature are vulnerable to attacks on hub neurons (Albert et al., 2000), which has been validated in neural circuits through closed-loop optogenetic studies (Bui et al., 2018; Krook-Magnuson et al., 2013).

We first compared the role of feedforward motifs versus simple edges on network function. Edges that projected from outgoing hubs and targeted neurons in its local motif-focused cluster or its local edge cluster were damped by a factor ranging from 0 (disconnect) to 1 (no change) (Figure 6A). Dampening the outputs of outgoing hubs to their respective motif-focused cluster had a greater effect on network activity in both baseline and pre seizure networks than dampening the output of outgoing hubs to their respective traditional edge cluster (Figure 6B, left). However, this effect was more pronounced for the pre seizure state (Figure 6B, right).

Second, we validated that outgoing hubs with the highest feedforward motif conductance (i.e., could propagate activity downrange more easily) have greater influence over network dynamics than outgoing hubs with low feedforward motif conductance. Outgoing hubs in pre seizure networks were ranked on the basis of their feedforward motif conductance score and split into either top half or bottom half. Within each half, an equivalent fraction of motif-focused clusters was disconnected from the network (Figure 6C; dampening factor = 0.0) in decreasing order. Simulations confirmed that disconnecting outgoing hubs in the high feedforward motif conductance partition was more effective in changing global network activity (Figure 6D, top). Interestingly, this effect was observed despite more edges being removed in the bottom half group (Figure 6D, bottom) and in total represented less than 0.1% of all edges in the network. We additionally verified that disconnecting hubs with the highest outgoing degree did not significantly alter network dynamics (Figure 6D,

top, red trace), further suggesting that the higher order organization of pre seizure networks gives critical insight into network function. On the basis of Figure 6D (top, blue trace), the trajectory deviation reached a plateau when approximately one-quarter of the outgoing hubs, ordered by decreasing feedforward motif conductance values, was disconnected from the network. Therefore, we considered the outgoing hubs with the top 27.5% feedforward motif conductance value (i.e., just after a stable plateau was reached with the trajectory deviation following the progressive disconnection of the outgoing hubs with the highest feedforward conductance values, indicated by the black arrowhead in Figure 6D) as superhubs, and outgoing hubs that scored below this were deemed traditional outgoing hubs (note that increasing this percentile cutoff further to 30% or 35% did not change the key results). Superhubs displayed increased activity preceding and in between high calcium events compared with the traditional outgoing hub population (Figure 6E, note periods indicated by numbers 1–3) and were not biased toward having the highest outgoing degree values (one-sided Kolmogorov-Smirnov [KS] test, $p > 0.05$) (Figure 6F). Therefore, feedforward motif conductance gives important insight into network function and that this insight could not have been revealed through mining the network for simple edges. As an additional validation, disconnecting individual superhubs had greater effect on network dynamics than disconnecting individual traditional outgoing hubs (Figure S6C).

Third, we tested the hypothesis that disconnecting superhubs rendered the network more stable to perturbation. Disconnecting all superhubs in the pre seizure network at the same time dampened oscillatory power over all frequency bands for most measured time periods (Figure 6G). Next, we perturbed a single outgoing hub and recorded the percentage change in signal variance (i.e., total power) of the mean population calcium signal before and after perturbation. This perturbation experiment was repeated for all outgoing hubs. As expected, the percentage change in signal variance in response to single outgoing hub perturbation in the fully connected pre seizure network was significantly higher than in the baseline network (39.8% to 69.1%; one-sided Mann-Whitney U test, adjusted $p < 0.001$) (Figure 6H, left, baseline versus pre seizure connected), indicating that the pre seizure network is more unstable. Importantly, disconnecting all superhubs from the pre seizure network simultaneously significantly reduced the percentage change in signal variance in response to single outgoing hub perturbation from 69.1% to 19.2% (one-sided Wilcoxon signed-rank test, adjusted $p < 0.001$) (Figure 6H, left, pre seizure connected versus pre seizure superhubs disconnected) and this percentage change was furthermore lower than baseline networks (one-sided Mann-Whitney U test, adjusted $p < 0.001$). Collectively, these data provide evidence that disconnecting superhubs robustly stabilized pre seizure networks. Disconnecting superhubs significantly decreased the trajectory deviation of global network activity in

reduced after disconnecting superhubs (one-sided Wilcoxon signed-rank test, $p < 0.001$; $N = 310$ modeled cells). This was quantified by measuring trajectory deviation before and after perturbation of a single outgoing hub in the fully connected pre seizure network and the pre seizure network with superhubs disconnected. See also Figure S6.

(I) Top: mean population calcium signal of a disconnected pre seizure network before (blue) and after (red) perturbation of a single outgoing hub. Bottom: principal component analysis (PCA) before (blue) and after (red) perturbation.

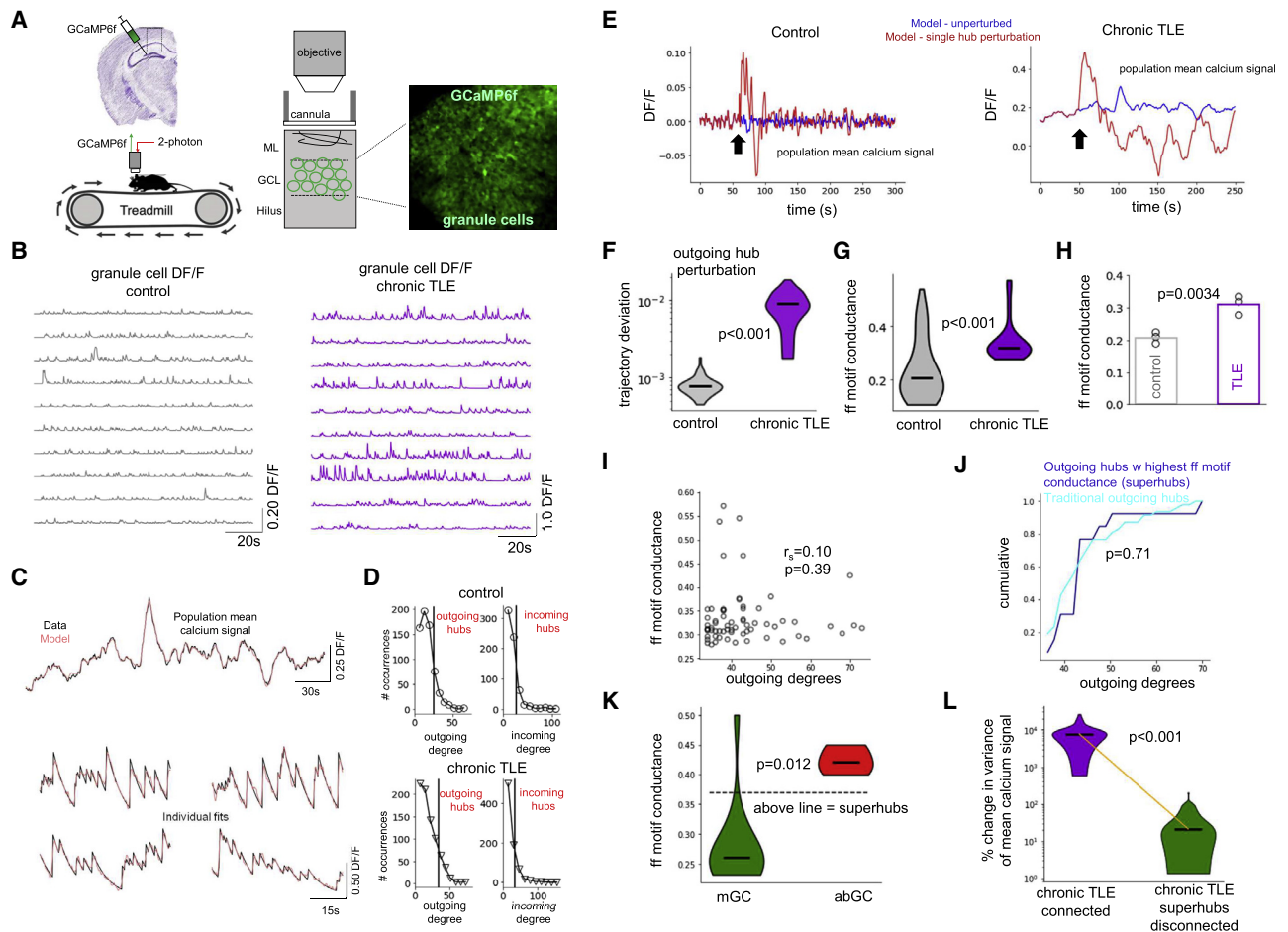


Figure 7. Superhubs in the intrahippocampal kainic acid mouse model of chronic temporal lobe epilepsy

(A) Experimental setup. Control and chronically epileptic mice were virally injected with GCaMP in dentate gyrus (DG) and imaged with two-photon (2p) microscope.

(B) DG granule cell DF/F for control and chronically epileptic mouse.

(C) Model fits of experimentally recorded granule cells from chronically epileptic granule mouse using FORCE learning.

(D) Outgoing and incoming degree distributions for modeled control dentate and chronically epileptic dentate networks showing heavy-tailed distributions.

(E) Network response to perturbation (black arrows) of a single outgoing hub neuron in a modeled control (left) and modeled chronically epileptic (right) network.

(F) Trajectory deviation in response to perturbation of individual outgoing hubs is significantly higher (one-sided Mann-Whitney U test, $p < 0.001$) in modeled chronically epileptic dentate network (purple, $N = 28$ modeled cells) than in modeled control network (gray; $N = 59$ modeled cells). Center marker of the violin plot represents the median.

(G) Feedforward motif conductance of individual outgoing hubs is significantly higher (one-sided Mann-Whitney U test, $p < 0.001$) in modeled chronically epileptic dentate network (purple, $N = 27$ modeled cells) than in modeled control network (gray; $N = 49$ modeled cells). Center marker of the violin plot represents the median.

(H) Feedforward motif conductance is significantly increased in modeled chronically epileptic networks across the sample population (one-sided unpaired t test, $p = 0.0034$). Bar graphs represents the mean of the population ($N = 3$ mice).

(I) Outgoing degrees and feedforward motif conductance are not significantly correlated (Spearman's $\rho = 0.10$, $p = 0.39$; $N = 49$ modeled neurons).

(J) Outgoing degree cumulative distribution for superhubs ($N = 8$ modeled cells) versus traditional outgoing hubs ($N = 19$ modeled cells). Superhubs did not have the highest outgoing degrees (one-sided KS-test, $p = 0.71$).

(K) Feedforward motif conductance of adult-born granule cells (red; $N = 6$ modeled cells) is significantly greater than mature granule cells (green; $N = 21$ modeled cells) (one-sided Mann-Whitney U test, $p = 0.012$). Dashed line represents cutoff for superhub status. Center marker of the violin plot represents the median.

(L) Disconnecting all superhubs simultaneously significantly reduced the response of a modeled chronically epileptic dentate network to single outgoing hub perturbation, as measured by the percentage change in global signal variance (one-sided Wilcoxon signed-rank test, $p < 0.001$; $N = 27$ modeled cells). Center marker of the violin plot represents the median. See also Figure S7.

response to single outgoing hub perturbation compared with the fully connected pre-seizure network (one-sided Wilcoxon signed-rank test, $p < 0.001$) (Figures 6H and 6I). In addition, control simulations showed that disconnecting superhubs resulted in a

significantly lower percentage change in signal variance (i.e., more effectively stabilized the network) in response to perturbation than either disconnecting the same number of traditional outgoing hubs randomly (19.2% versus 57.1%; one-sided

Wilcoxon signed-rank test, $p < 0.001$) or the same number of traditional outgoing hubs with the lowest feedforward motif conductance values (19.2% versus 77.4%; one-sided Wilcoxon signed-rank test, $p < 0.001$) (Figures S6D and S6E).

Therefore, the network is more resilient to perturbation when superhubs are disconnected. Taken together, these three computational experiments reveal that the higher order microcircuit connectivity architecture surrounding hub neurons is a critical novel feature of stability in epileptic networks.

Superhubs in a mouse model of chronic TLE

Next, we tested the hypothesis that superhubs may also play a role in the pathological activity dynamics of a chronically epileptic mammalian brain circuit. Specifically, we sought to determine whether our key findings from the zebrafish acute seizure model also held in chronically epileptic mice. Therefore, we applied the same computational pipeline as above on two-photon single-cell resolution calcium imaging data obtained from the DG of healthy control ($N = 3$) and epileptic mice ($N = 3$) using the intrahippocampal kainic acid (KA) model of chronic TLE, the most prevalent form of epilepsy in adults. Mice expressed GCaMP6f in dorsal DG and the epileptic group had KA injected unilaterally into the ipsilateral ventral hippocampus. Two-photon calcium imaging of DG granule cells (GCs) was performed in healthy and in chronically epileptic mice (Figures 7A and 7B, note differences in vertical axis of the scale bars). GC calcium dynamics were modeled for both groups of mice using FORCE optimization (600–800 neurons/mouse, 3–5 min window; Figure 7C), and incoming and outgoing hubs were identified (Figure 7D) with similar methods as used in zebrafish.

Importantly, our results showed that the modeled control networks were more resilient to single outgoing hub perturbation than modeled chronically epileptic dentate networks (Figures 7E and 7F). In addition, global network dynamics were significantly less affected (one-sided Mann-Whitney U test, $p < 0.001$) when perturbing incoming hubs compared with outgoing hubs for both networks (Figures S7A and S7B). Similar to zebrafish, feedforward motif conductance of local higher order motif-focused clusters seeded on outgoing hubs was significantly higher (one-sided unpaired t test, $p = 0.0034$) in chronically epileptic dentate networks compared with control dentate networks (Figures 7G and 7H; feedforward conductance: control, 0.21 ± 0.014 ; TLE, 0.31 ± 0.024). Feedforward motif conductance was not correlated to outgoing degree (Spearman's $\rho = 0.10$, $p > 0.05$) (Figure 7I), and hubs with the top motif conductance scores were not biased toward the highest outgoing degree values (one-sided KS test, $p > 0.05$) (Figure 7J). For the studies below, outgoing hubs with the top 20% feedforward motif conductance value were considered superhubs, on the basis of an analysis protocol similar to the one applied to the zebrafish data above in relation to Figure 6D (Figure S7C). More specifically, as for the zebrafish, the particular 20% cutoff value was chosen for the mouse superhubs because it was just above the feedforward motif conductance value where a plateau was reached with the trajectory deviation (indicated by a black arrowhead in Figure S7C) after progressively disconnecting the outgoing hubs with the highest feedforward conductance values (note that increasing the cutoff percentile further to 25% did not change the key results).

Is there a potential biological correlate of the superhubs identified by our computational pipeline from the mouse DG cellular resolution functional imaging data? A particularly intriguing possibility in this regard are the epilepsy-related abGCs (Althaus et al., 2016; Danzer, 2018; Varma et al., 2019), which have been suggested to be crucial in driving epileptiform activity in the mouse DG (Sparks et al., 2020). In order to test this possibility, we identified the abGCs among the broader imaged GC population using previously published methods (Sparks et al., 2020; Figure S7D; STAR Methods). Critically, effective connectivity optimization and higher order network analysis revealed that 75% of superhubs were indeed the modeled abGCs, despite abGCs representing <18% of the total imaged GC population. In addition, abGCs in the computational model had significantly higher feedforward motif conductance scores compared with their more mature GC counterparts (one-sided Mann-Whitney U test, $p = 0.012$) (Figure 7K; feedforward conductance: mature GCs, 0.26 ± 0.048 ; abGCs, 0.431 ± 0.017). These data demonstrate that superhubs identified through our computational pipeline applied to two-photon imaging data obtained from the DG of epileptic mice represent a specific biological cell population thought to be involved in seizures (Sparks et al., 2020), independently validating our approach.

Next, in order to investigate the role of the mouse superhubs further, we disconnected superhubs in the modeled chronically epileptic dentate networks. Single outgoing hub perturbation simulations showed significant reduction in both the change in global network trajectory deviation (one-sided Wilcoxon signed-rank test, $p < 0.001$; Figure S7E) and in the change in global network signal variance after superhubs were disconnected (one-sided Wilcoxon signed-rank test, $p < 0.001$; Figure 7L). These data indicate that disconnecting superhubs effectively stabilized modeled chronically epileptic dentate networks. Furthermore, the percentage change in signal variance in response to single outgoing hub perturbation was significantly lower when disconnecting superhubs compared with disconnecting the same number of traditional outgoing hubs randomly (one-sided Wilcoxon signed-rank test, $p = 0.0077$) or traditional outgoing hubs with the lowest feedforward motif conductance values (one-sided Wilcoxon signed-rank test, $p = 0.0024$) (Figures S7F and S7G). Last, we modeled GC dynamics over multiple non-overlapping frames within a 1 h imaging window to test if superhub identities were stable. Although superhubs represented 2% of the total cell population, we observed that 54% of identified superhubs in one frame were superhubs in a subsequent frame whose start time was 15 min later.

These similar findings across both an acute seizure model in zebrafish and in chronically epileptic mice suggest that the emergence of superhubs is a core principle of network reorganization that may be a key feature contributing to the destabilization of the epileptic brain. Targeting these superhubs may be more effective in the cellular scale control of epileptic circuits than hubs defined traditionally on the basis of connection count.

DISCUSSION

Here, we sought to characterize the connectivity patterns of cell-cell communication networks in epileptic circuits. Our findings

reveal that superhubs, defined through analysis of the higher order organization of modeled networks extracted from functional calcium imaging data, emerge as key cellular controllers that can powerfully destabilize epileptic circuits. Disconnecting these superhubs was effective in stabilizing modeled networks in larval zebrafish, and importantly, these results also held true in the modeled DG of chronically epileptic mice. Critically, in the modeled DG of mice with chronic TLE, superhubs were predominantly abGCs. Therefore, these results predict the existence of fundamentally novel single-cell targets for maximally selective, minimally invasive seizure control in epilepsy.

Search for new interventional targets guided by large-scale cellular resolution functional imaging

Current clinical assessment and treatment of epilepsy is to a large extent based on analysis of networks constructed from population recordings such as LFPs (Jiruska et al., 2013) or functional magnetic resonance imaging (fMRI) (Gotman and Pittau, 2011). However, recent studies have shown that single-cell activity can diverge significantly from what population recordings would predict. For example, apparently self-repeating, macroscopically recurrent epileptiform LFP activity (inter-ictal spikes) indicating network synchrony have been shown to emerge from non-recurrent microscopic single-cell activity. In other words, each inter-ictal event is generated by a different combination of participating cells (Liu and Baraban, 2019; Feldt Muldoon et al., 2013; Sparks et al., 2020). This “macro-micro” disconnect (Farrell et al., 2019) is a significant challenge for the field and indicates that a more nuanced understanding of pathways at the level of microcircuits is needed to treat the underlying disease (Soltesz and Losonczy, 2018). Therefore, in an effort to search for novel forms of maximally selective, ideally single cell-level targets for interventions for seizure control, we performed large-scale calcium imaging at cellular scale and used this as our primary data source for the subsequent modeling and analysis.

Computational pipeline to study superhubs in cell-cell communication networks

Our computational methodology for uncovering the role of superhubs in destabilizing epileptic circuits was performed using three distinct yet integrated modules: effective connectivity modeling, higher order motif-focused network analysis, and single-cell perturbation simulations.

Effective connectivity modeling is a widely used technique for gaining insights on interactions between pairs of connected nodes under a network model of causal dynamics (Friston, 2011). Methods to perform effective connectivity modeling have been deployed to study the brain under various pathological conditions (Huang et al., 2011; Nejad et al., 2012; Rosch et al., 2018) and have also been used to elucidate macroscopic brain interactions responsible for seizure propagation in the larval zebrafish (Rosch et al., 2018). Here, we interrogated changes to cell-cell effective connectivity networks as a result of PTZ induced reduction of inhibition (Huang et al., 2001) in the larval zebrafish acute seizure model, and as a result of various epilepsy-related persistent alterations such as mossy fiber sprouting (Sutula et al., 1989) and hilar cell loss (Kobayashi and Buckmaster, 2003) in the DG of

chronically epileptic mice. We used chaotic RNNs (Sompolinsky et al., 1988) and FORCE optimization (Sussillo and Abbott, 2009) techniques, which have been shown to be effective for modeling neural dynamics related to hippocampal sequence generation (Rajan et al., 2016), motor planning (Li et al., 2016), and coping (Andalman et al., 2019). Using this approach on calcium imaging data acquired from the larval zebrafish at whole-brain single-cell resolution, we present for the first time biologically constrained effective connectivity models of control and pre-seizure networks, where the biological constraint was incorporated by the inclusion of the zebrafish structural connectome (Kunst et al., 2019) in the weight-update step. As a result, macroscale subnetworks that resembled major anatomical subregions emerged (Figure S1). These specific partitions agree with converging evidence that suggest a functional (Ahrens et al., 2013; Betzel, 2020; Liu and Baraban, 2019) separation between the various front and mid-/hindbrain structures.

The parameters of the model form a directed weighted graph, which allowed us to quantify chemoconvulsant- or chronic epilepsy-induced changes to the underlying graph structure using novel methods in network science (Yin et al., 2017). We first found heavy-tailed degree distributions of strong excitatory connections for both zebrafish and mouse models (Figures 3C and 7D; Bonifazi et al., 2009), a feature that is common in large complex networks. This enabled us to identify both incoming and outgoing traditional hub neurons on the basis of incoming and outgoing connection counts. To further analyze the connectivity structure surrounding traditional hubs, we deployed novel local motif-focused clustering techniques and quantified motif conductance (Figures 5A and 5B). Importantly, the MAPPR algorithm (Yin et al., 2017) identified optimal clusters, which allowed us to directly compare motif conductance between baseline and pre-seizure networks. Although we reported a non-significant increase (~5%) in average outgoing degrees in pre-seizure networks (Figures 3C and 3D), feedforward motif conductance of higher order clusters surrounding outgoing hubs increased significantly by 50% on average (Figure 5E).

Single-cell perturbation simulations are important tools for generating predictions of how individual cells influence network dynamics (Sadeh and Clopath, 2020). Measures were taken in the modeling step to prevent overfitting, such as including a sparsity constraint on the number of model parameters, which allowed us to perform controlled perturbation simulations. We first interrogated network stability in modeled control and pathological circuits. Results revealed that perturbation of just a single outgoing hub neuron can significantly influence epileptic global network dynamics compared with similar computational experiment in baseline networks (Figures 4 and 7). One reason for this may be due to compromised inhibition in epileptic circuits (Huang et al., 2001; Kobayashi and Buckmaster, 2003; Korn et al., 1987), which normally functions to stabilize network activity (Isaacson and Scanziani, 2011; Murphy and Miller, 2009; Sadeh and Clopath, 2020). Taken together, these results highlight that pre-seizure networks are unstable (Chang et al., 2018; Sadeh and Clopath, 2020). Additionally, we showed that targeted-attack simulations of identified superhubs (i.e., outgoing hubs with high feedforward motif conductance) can stabilize networks to perturbation. These causality-establishing simulations

(Figures 6 and 7) predict that superhubs can more readily propagate sustained excitatory activity downstream in epilepsy compared with control, baseline networks.

Superhubs in the epileptic brain

The primary conceptual advance in this work was brought to light from mining large-scale cellular resolution networks extracted from experimental neural data for higher order connectivity patterns called motifs. Highly connected but rare hub neurons have been of great interest for studies working toward the goal of advancing seizure control with minimal side effects (Bui et al., 2018; Krook-Magnuson and Soltesz, 2015; Krook-Magnuson et al., 2015). This has been motivated by experimental work showing that hub neurons orchestrate network synchrony (Bocchio et al., 2020; Bonifazi et al., 2009) and by computational work predicting their role in the transition from inter-ictal to ictal discharge (Morgan and Soltesz, 2008).

However, hub neurons are traditionally defined by simple connection counts, a definition that does not consider the rich higher order motif patterns that are often found in complex networks (Benson et al., 2016; Sporns and Kötter, 2004). As these motifs are thought to influence network function in biological neural circuits (Sporns and Kötter, 2004), we deployed our computational pipeline toward the goal of identifying potential new targets for control of pathological circuits. The key results presented in this paper could not have been uncovered with traditional lower order graph mining techniques, as the primary metric to extract superhubs, motif conductance, was not correlated to connection count (Figures 5F, 6F, and 7J), local clustering coefficient score, or betweenness centrality (Figures S6A and S6B). Furthermore, because disconnecting superhubs stabilized networks, these findings suggest that complex networks can be susceptible to targeted attacks of nodes when considering rich higher order motif features rather than simple connection count. This shift in perspective—specifically looking at the patterns of connectivity surrounding hubs as opposed to connections from hubs—may also be important for how we interpret the underlying microscale dynamics from macroscale recordings (Farrell et al., 2019), evaluate the efficacy of anti-epileptic drugs (AEDs) (Baraban et al., 2013), and develop more strategic closed-loop interventions (Bui et al., 2018; Krook-Magnuson and Soltesz, 2015; Krook-Magnuson et al., 2013, 2015).

Motifs are a critical feature of the structural and functional connectomes (Sadeh and Clopath, 2020; Song et al., 2005; Sporns and Kötter, 2004), and it has been hypothesized that the brain maximizes the diversity of functional motifs (Sporns and Kötter, 2004). This diversity may be related to the phenomenon of criticality (sometimes called “edge of chaos”), a state marked by scale-invariant neural avalanches that has been reported in control zebrafish (Ponce-Alvarez et al., 2018). Prior research showed chemoconvulsant-induced disruption of excitation/inhibition (E/I) balance in cortical neural networks caused deviation away from criticality (one neuron activates one neuron) and into this supercritical regime (one neuron activates more than one neuron) (Shew et al., 2009). Indeed, hypersynchronous neuronal avalanches, evidence of a supercritical state, were recently reported in a zebrafish model of genetic epilepsy using *in vivo* calcium imaging (Liu et al., 2021). Here, we specifically observed that

preseizure networks contain elevated counts of two motif patterns that suggest the emergence of a supercritical regime: (1) the “push-out” motif (Figure S4C), in which the mother neuron activates two daughter neurons, and (2) the feedforward motif (Figure S4D), in which the mother neuron activates two daughter neurons and one of the daughter neurons activates its sibling. Therefore, our discovery of superhubs dense with feedforward connections simultaneously brings to the forefront a potential new network-level biomarker that may be able to capture a system’s divergence from criticality.

Our findings in the zebrafish brain in an acute seizure model were remarkably similar to the results from the hippocampal DG of chronically epileptic mice. Although zebrafish brains contain generally similar circuits compared with mice (Lovett-Barron et al., 2017), there are also important differences, for example, concerning cortical structures prevalent in mammals that are often sites of epileptic foci. Furthermore, acute seizure models lack persistent alterations to the underlying genes, ion channels, synapses, and morphological properties that are present in patients with epilepsy. We addressed both of these issues by modeling DG GC dynamics in mice with chronic TLE. Through our computational analysis pipeline, we were able to show that higher order motif interactions that predict the emergence of superhubs held in distinct experimental epilepsy models and in organisms far removed in evolutionary time. Furthermore, we identified a biological correlate to the superhub in the epileptic DG, specifically the abGCs (Figure 7K), effectively validating our computational methods. This finding also corroborates previous efforts using a separate modeling approach (Sparks et al., 2020) suggesting that abGCs are key drivers of epileptiform activity in a chronic model of TLE.

The investigations described in this paper, apart from the actual recording of the functional calcium dynamics, were performed *in silico*, so *in vivo* experimental studies will be needed to validate the major predictions of this work. Specifically, these results analyzing the higher order interactions of control and epileptic networks predict a new single-cell target, the superhub, for maximally selective, minimally invasive control of epileptic circuits. On the basis of our observations in epileptic mice that superhubs are temporally stable over the hour-long timescale and that modeling and mining effective connectivity networks can be done quickly (<20 min), closed-loop interventions that target individual superhubs (which, in the specific case of the DG in TLE, largely overlap with the genetically accessible abGCs) can be designed in the future to test the predictions of this study concerning the roles of superhubs in the epilepsies.

STAR★METHODS

Detailed methods are provided in the online version of this paper and include the following:

- KEY RESOURCE TABLE
- RESOURCE AVAILABILITY
 - Lead contact
 - Materials availability
 - Data and code availability

● EXPERIMENTAL MODEL AND SUBJECT DETAILS

- Zebrafish acute seizure model
- Intrahippocampal kainic acid mouse model of chronic temporal lobe epilepsy

● METHOD DETAILS

- *In vivo* two-photon imaging in zebrafish acute seizure model
- *In vivo* two-photon imaging of intrahippocampal kainic acid mouse model of chronic temporal lobe epilepsy
- Modeling neural dynamics in healthy and pathological brains
- Chaotic recurrent neural networks
- Reproducing experimental calcium data using FORCE learning
- Biologically constrained FORCE using zebrafish structural connectome
- Identifying modeled traditional hub neurons
- Identifying modeled superhubs
- Identifying modeled adult-born granule cells
- Perturbation simulations

● QUANTIFICATION AND STATISTICAL ANALYSIS

- Community detection
- Force-directed graphs
- Rich-club analysis
- Quantifying motif conductance using higher-order network analysis
- Constructing motif weighted graph W
- Compute the approximate personalized PageRank vector
- Identify higher-order motif-focused cluster as a set with minimal motif conductance
- Trajectory deviation
- Change in total power
- Statistical analysis

SUPPLEMENTAL INFORMATION

Supplemental information can be found online at <https://doi.org/10.1016/j.neuron.2021.06.007>.

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AUTHOR CONTRIBUTIONS

D.H., M.L.-B., S.C.B., J.L., A.L., K.D., and I.S. designed research. M.L.-B., F.S., and Z.L. collected data. D.H. performed modeling and simulations. D.H., I.R., and I.S. analyzed data. D.H. and I.S. wrote the manuscript. All authors edited the manuscript.

DECLARATION OF INTERESTS

K.D. is on the *Neuron* advisory board.

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STAR★METHODS

KEY RESOURCE TABLE

REAGENT or RESOURCE	SOURCE	IDENTIFIER
Bacterial and virus strains		
AAV1.Syn.GCaMP6f.WPRE.SV40	Penn Vector Core	N/A
ROSA26-CAG-stopfloxedTomato Ai9	JAX	007909
Chemicals, peptides, and recombinant proteins		
Pentylenetetrazol (PTZ)	Sigma-Aldrich	PubChem ID: 24278643
Kainic Acid (KA)	Sigma-Aldrich	PubChem ID: 24277985
Deposited data		
Functional calcium imaging data	This paper	Mendeley Data: https://dx.doi.org/10.17632/9936ryd5h7.2
Effective connectivity models	This paper	Mendeley Data: https://dx.doi.org/10.17632/dghdz45rfd.2
Experimental models: organisms/strains		
Zebrafish <i>Tg(elavl3:H2B-GCaMP6s)</i>	Vladimirov et al., 2014	jf5
Mouse <i>Nestin-CreERT2</i>	JAX	016261
Software and algorithms		
Python	Python.org	v3.6
SNAP	http://snap.stanford.edu/	v6
Networkx	https://networkx.org/	v2.5
Scipy	https://www.scipy.org/	v1.20
Leidenalg	Traag, 2021	v0.8.40
Igraph	Nepusz, 2021	v0.9.4
Fiji/ImageJ	NIH	v1.52p
CalmAn	Giovannucci et al., 2019	PMID: 30652683
Computational Morphometry Toolkit (CMTK)	NITRC	v3.3
FORCE	Sussillo and Abbott, 2009	PMID: 19709635
MAPPR	Yin et al., 2017	PMID: 28344853

RESOURCE AVAILABILITY

Lead contact

Further information and requests for resources should be directed to and will be fulfilled by the Lead Contact, Darian Hadjiabadi (dhah@stanford.edu).

Materials availability

This study did not generate new unique reagents.

Data and code availability

Zebrafish and mouse functional calcium imaging data (Mendeley Data: <https://dx.doi.org/10.17632/9936ryd5h7.2>) and effective connectivity networks (Mendeley Data: <https://dx.doi.org/10.17632/dghdz45rfd.2>) are publically available. All code to perform modeling and analyze effective connectivity models were written in python3 and is available at <https://github.com/dhadjia1/soltesz-lab-epilepsy-modeling>.

EXPERIMENTAL MODEL AND SUBJECT DETAILS

All procedures were approved by the Institutional Animal Care and Use Committee for both Stanford University and Columbia University.

Zebrafish acute seizure model

Tg(elavl3:H2B-GCaMP6s) (Freeman et al., 2014) fish (7 dpf) bred on a Nacre or Casper background were used for imaging and registration. Zebrafish were mounted dorsal side up in a thin layer of 2.5% low-melting point agarose (Invitrogen) in the lid of a 3 mm Petri dish (Fisher), using a sewing needle to position the fish under a stereomicroscope (Leica M80). Fish were group-housed under a 14:10 light:dark cycle until the day of experiments, and were fed with paramecia (*Parameciavap*) twice daily from 5–6 days post fertilization onward. All testing occurred during the late morning and afternoon. 15 mM bath application of the chemoconvulsant pentylenetetrazol (PTZ) was performed to induce spontaneous seizures (Baraban et al., 2005), serving as the acute seizure model. Zebrafish were randomly chosen and all fish that received PTZ developed seizures and were included for imaging. Note that each fish served as its own control before the chemoconvulsant treatment, making blinding not applicable. No power analysis was done to determine sample size.

Intrahippocampal kainic acid mouse model of chronic temporal lobe epilepsy

Male transgenic mice were obtained from The Jackson Laboratory (Nestin-CreER^{T2}:016261; ROSA26-CAG-stop^{flox}-tdTomato Ai9:007909) to establish a local breeding colony on a C57BL/6J background. The Nestin-Cre line was crossed with the Ai9 reporter line to express tdTomato in adult-born granule cell populations (Sparks et al., 2020). Mice were housed in the vivarium on a 12h light/dark cycle, were housed 3–5 mice per cage, and had access food and water *ad libitum*. Mice were randomly chosen for epilepsy induction (see *Inducing chronic epilepsy* in Method details). Mice were housed individually during video-EEG monitoring following kainic acid injection. Mature male and female mice (> 8 weeks of age) were used for all experiments and mice were included if spontaneous behavioral seizures were detected. Experimenters were not blinded to control versus epileptic group during recording and no power analysis was performed to determine sample size.

METHOD DETAILS

In vivo two-photon imaging in zebrafish acute seizure model

Two-photon volumetric imaging was performed using an Olympus FVMPE multiphoton microscope (Olympus Corporation), with a resonant scanner, in either unidirectional or bidirectional scanning mode. We used a 16x objective (0.8 NA; Nikon). Functional brain imaging was performed at 1.2x zoom (1.44 $\mu\text{m}/\text{pix}$) in 15 z-planes (15 μm spacing) at 0.59 s/vol (2500 volumes). Baseline control imaging was performed for 5 minutes followed by 15 mM bath application of PTZ to induce spontaneous seizures (Baraban et al., 2005). Functional imaging continued for an additional 20 minutes. All zebrafish exhibited at least one putative seizure prior to cessation of imaging.

After functional brain imaging, a structural stack was obtained at 1 μm spacing, starting 15 mm above the first z-plane, ending 15 mm below the last z-plane. Images were registered to Z-brain atlas *Tg(elavl3:H2B-RFP)* volume using the Computational Morphometry Toolkit (CMTK; <https://www.nitrc.org/projects/cmtk/>) and single-cell functional calcium dynamics were extracted and denoised with non-negative matrix factorization (NMF) based statistical approaches found in the CalMan library (Giovannucci et al., 2019). This preprocessing step is fully discussed in Lovett-Barron et al. (2017). All zebrafish calcium imaging data can be found in Hadjiabadi et al. (2021).

In vivo two-photon imaging of intrahippocampal kainic acid mouse model of chronic temporal lobe epilepsy

Virus injections

Two weeks prior to kainic acid (KA) injection, 3mg tamoxifen (TMX) (2mg/mL in corn oil/10% ethanol) was injected I.P/day for 5 consecutive days. abGCs were indelibly labeled with tdTomato following injections of TMX that drove expression of Cre in Nestin+ cells.

Inducing chronic epilepsy

Kainic Acid (KA) was injected into the ventral hippocampus to induce the epilepsy model and rAAV(Syn-GCaMP6f) was injected into the dorsal dentate gyrus ipsilateral to KA injection. Shortly after, a chronic imaging window was implanted over dorsal dentate and an LFP electrode was inserted adjacent to site of KA injection. Following recovery from injection of KA, mice were placed in video-EEG enabled housing where LFP and behavioral activity were continuously recorded to monitor ictogenesis. Three weeks post-KA injection, the video-EEG verified TLE mice were habituated to being head fixed under the two-photon microscope and concurrent Ca²⁺ imaging and LFP recording was performed. Detailed surgical procedures are reported in Sparks et al. (2020).

Two-photon imaging

Two-photon imaging of dentate gyrus granule cells was performed using the same set up as Danielson et al. (2016), at 4 images/second. Approximately 50–100 mW of laser power under the objective was used for excitation (Ti:Sapphire laser, (Chameleon Ultra II, Coherent) tuned to 920 nm), with adjustments in power levels to accommodate varying window clarity. To optimize light transmission, the angle of the mouse's head was adjusted using two goniometers (Edmund Optics, ± 10 -degree range) such that the imaging window was parallel to the objective. A piezoelectric crystal was coupled to the objective (Nikon 40X NIR water-immersion, 0.8 NA, 3.5mm WD), allowing for rapid displacement of the imaging plane in the z-dimension. Red (tdTomato) and green (GCaMP6f) channels were separated by an emission cube set (green, HQ525/70 m-2p; red, HQ607/45 m-2p) at 512 $\times$ 512 pixels covering 225 μm $\times$ 225 μm . OASIS (Friedrich et al., 2017) was used for denoising. While not being imaged, mice were routinely monitored for interictal and seizure events using a custom continuous video-EEG system previously described (Krook-Magnuson et al., 2013). Healthy control mouse data was obtained from Danielson et al. (2016), included two-photon recording of granule cells from approximately the same location in dentate gyrus as in epileptic mice. All mouse calcium imaging data can be found in Hadjiabadi et al. (2021).

Modeling neural dynamics in healthy and pathological brains

Zebrafish

The start of the pre-seizure state was defined as one minute after PTZ bath application. Seizure initiation was defined as three standard deviations above population mean calcium signal during baseline (pre-PTZ) and termination was defined as when the population mean signal dropped below this threshold. Correlation matrix analysis (Li et al., 2007) was deployed to quantify network synchronization. Modeling in zebrafish was performed on baseline control dynamics first, and the best fit model was used as the initial parameter matrix for learning pre-seizure dynamics. Community detection using the Leiden algorithm (Traag et al., 2019) on learned parameter matrix was used to identify communities with numerous intra-group connections. To account for potential abnormalities during the registration process, neurons were removed from modeling if their respective post-registration $|DF/F| > 10$ or if $|DF/F(t+1) - DF/F(t)| > 10$ at any point in the signal.

Mice

For both control and chronically epileptic mice, calcium dynamics were acquired during a 60-minute epoch. Calcium recordings included artifacts from running and grooming that resulted in prolonged hyper-synchronous events. Therefore, a continuous 3-5 minute time window lacking such events was identified for each mouse and used to model calcium dynamics.

Chaotic recurrent neural networks

Models of cell-cell effective communication were built using chaotic recurrent neural networks (RNN) (Sompolinsky et al., 1988). Each neuron experimentally imaged was represented as a node in the network and edges represent the effective (causal) influence between pairs of nodes. The governing dynamics of the chaotic RNN are:

$$\tau \frac{dx_i(t)}{dt} = -x_i(t) + g \sum_{j=1}^N J_{ij} \varphi(x_j(t)) + h_i(t)$$

$$z_i(t) = \sum_{j=1}^N J_{ij} \varphi(x_j(t))$$

$$\varphi(\cdot) = \tanh(\cdot)$$

$x_i(t)$ is the inferred intracellular current of node i . $\varphi(x_i(t))$ represents firing rate. $z_i(t)$ is the estimated calcium signal. τ is the time constant of the system (zebrafish: 1.5 s; mouse: 0.625 s). $h_i(t)$ is uncorrelated white noise sampled from a normal distribution with mean 0 and standard deviation 0.05 (zebrafish) / 0.005 (mouse). g is the gain parameter that determines whether there will be chaos in the system ($g < 1$: stable equilibrium; $g > 1$: chaos). We used $g = 1.25$ for both zebrafish and mouse (Andalman et al., 2019; Rajan et al., 2016). Lastly, J is the effective connectivity matrix that represents the parameters of the model. At initiation of learning baseline control dynamics in zebrafish and learning both control and pre-seizure dynamics in mice, the values of J that were not removed after applying a sparsity mask (zebrafish: $p = 0.10$; mouse: $p = 0.40$) were sampled from a normal distribution with mean 0 and standard deviation $\frac{1}{\sqrt{Np}}$. N is the number of nodes and p is the sparsity. The models contain $p * N * (N - 1)$ parameters. Dynamics were solved using Euler's method ($dt = 0.25$ s).

Reproducing experimental calcium data using FORCE learning

The effective connectivity parameter matrix was optimized to reproduce the experimental calcium data through FORCE learning (Sussillo and Abbott, 2009). This was done through recursive least-squares optimization where at each time point an error signal $e_i(t) = z_i(t) - f_i(t)$ is calculated between node output $z_i(t)$ and experimental calcium trace $f_i(t)$. Given this error, the traditional learning rule is as follows:

$$\Delta J_{ij} = c * e_i(t) * \sum_{k=1}^N P_{jk} \varphi(x_k(t))$$

$$c = \frac{1}{1 + \varphi(t)^T P(t) \varphi(t)}$$

$$P(t) = P(t-1) - c P(t-1) \varphi(t) \varphi(t)^T P(t-1)$$

Where c is the effective learning rate used for stability and $P(t)$ is updated in a recursive fashion at every time point. At initiation, $P(0)$ was set to the identity matrix. Learning was performed for 500 epochs for all zebrafish and mouse models, where one epoch is defined as one run of the optimization routine for the duration of the experimental trial. Convergence was assessed by tracking the mean squared reconstruction error between unit activity and experimental data. All zebrafish and mouse models can be found in [Hadjabadi and Soltesz \(2021\)](#). To ensure replication, modeling was repeated three times with different initial conditions for each zebrafish and mouse.

Biologically constrained FORCE using zebrafish structural connectome

The zebrafish structural connectome ([Kunst et al., 2019](#)) was incorporated into zebrafish FORCE learning as a biological constraint. The structural connectome is a weighted undirected graph between 30 distinct subregions occupying the telencephalon, diencephalon, mesencephalon, and rhombencephalon. The modified weight-update step is:

$$\Delta J_{ij}^{\text{Constrained}} = S_{R(i),R(j)} * \Delta J_{ij}$$

where i, j are individual nodes (neurons) and $S_{R(i),R(j)}$ is the structural connectivity between subregions $R(i)$ and $R(j)$.

Identifying modeled traditional hub neurons

The optimized effective connectivity parameter matrix was binarized by converting the top 10% of edges to a 1 and converting the remaining edges to a 0. The outgoing and incoming degree was calculated for each neuron. Neurons above the 90th percentile outgoing (incoming) degree score were marked as outgoing (incoming) hubs.

Identifying modeled superhubs

Identified traditional outgoing hubs (see [Identifying modeled traditional hub neurons](#)) were used as the seed for local higher-order clustering on feedforward motifs and the feedforward motif conductance was quantified (see [Quantifying motif conductance using higher-order network analysis](#); note only seed neurons with at least 5 neighbors in the local higher-order cluster were considered for further analysis). Modeled neurons were ranked based on the feedforward motif conductance score in descending order. The top $x\%$ of hub neurons was “disconnected” by removing all edges from the hub neuron to its identified local higher-order cluster. The disconnected network was then simulated, and trajectory deviation quantified (see [Trajectory deviation](#)) for the fully connected network relative to the disconnected network. Superhubs were identified when a stable plateau in the trajectory deviation was reached as a function of the number of neurons disconnected (see [Figure 6D](#); [Figure S7C](#)).

Identifying modeled adult-born granule cells

Preprocessing steps were undertaken to match granule cell calcium dynamics with genetic identity as performed in [Sparks et al. \(2020\)](#). The individual performing analysis was blind to the identity of all abGCs until modeling was complete for all mice and higher-order analysis was performed for each modeled network.

Perturbation simulations

To simulate the effect of perturbation on network dynamics, a single hub neuron was ‘current clamped’ to achieve maximum firing rate (500ms step current). The current clamp perturbation was initiated at 0.2 normalized time, consistent for all zebrafish and mouse models. Synthetic calcium traces were then generated for each neuron before and after perturbation.

QUANTIFICATION AND STATISTICAL ANALYSIS

Community detection

Community detection is used to understand the structure of complex networks by identifying nodes clusters that form relatively dense groups. We used the *leidenalg* python package ([Traag, 2021](#)) which leverages the recently developed Leiden algorithm ([Traag et al., 2019](#)) to guarantee well-connected communities. Communities were identified by calling the function `leidenalg.find_partition(G, leidenalg.RBConfigurationVertexPartition, resolution_parameter = 1.0)`. Here, G is an *igraph* object ([Nepusz, 2021](#)). More specifically, G is a directed graph that has been binarized to exclude inhibitory edges and to include the remaining excitatory edges whose weights are in the top 50%.

Force-directed graphs

The effective connectivity matrix was visualized using the Barnes-Hut N-body simulation algorithm ([Barnes and Hut, 1986](#)). Here, each node can be thought of as a repelling particle and the edges between nodes are modeled as attractive springs. The objective of the algorithm is to find an optimal force-directed spatial configuration such that (i.e., net force = 0). The Barnes-Hut algorithm was applied to the binarized parameter matrix after thresholding for strongest connections (see [Identifying modeled traditional hub neurons](#)) and used to visualize incoming and outgoing hubs connections in zebrafish.

Rich-club analysis

The rich-club coefficient on the full baseline and pre-seizure binarized graphs were performed to identify if highly connected neurons are themselves connected to one another. We discuss the lesser known implementation of rich-club analysis on directed graphs using solutions provided in [Smilkov and Kocarev \(2010\)](#). Specifically, given a directed graph $G = (V, E)$, the outgoing rich club coefficient can be calculated as:

$$\phi^{\text{out}}(k) = \frac{\left(\frac{E_{>k}^{\text{out}}}{N_{>k}^{\text{out}}(N_{>k}^{\text{out}} - 1)} \right)}{\phi_{\text{rand}}^{\text{out}}(k)}$$

Here, $\phi^{\text{out}}(k)$ is the rich-club coefficient as a function of outgoing degree k and is normalized by the rich-club-coefficient over a random graph. $E_{>k}^{\text{out}}$ represents the number of outgoing edges between pairs of neurons whose outgoing degree is greater than k . $N_{>k}^{\text{out}}$ represents the number of nodes whose outgoing degree is greater than k . The analytic solution to $\phi_{\text{rand}}^{\text{out}}(k)$, the rich-club coefficient for a random graph, is the following:

$$\phi_{\text{rand}}^{\text{out}}(k) = \frac{N \sum_{k'=k+1}^{k_{\text{max}}} k' P_{\text{out}}(k') \sum_{k''=k+1}^{k_{\text{max}}} \langle k_{\text{in}}^{k_{\text{out}}=k''} \rangle P_{\text{out}}(k'')}{\langle k_{\text{out}} \rangle N_{>k}^{\text{out}} (N_{>k}^{\text{out}} - 1)}$$

Here, N is the total number of nodes in the network (i.e., $|V|$). $P_{\text{out}}(k')$ is the probability of a node having outgoing degree k' . $\langle k_{\text{in}}^{k_{\text{out}}=k''} \rangle$ is the mean incoming degree for nodes with outgoing degree k'' . $\langle k_{\text{out}} \rangle$ is the mean outgoing degree in the network. $N_{>k}^{\text{out}}$ represents the number of nodes whose outgoing degree is greater than k . If $\phi^{\text{out}}(k) > 1$ as k approaches the highest outgoing degree in the network (k_{max}), then it can be deduced that the graph exhibits a rich-club.

Quantifying motif conductance using higher-order network analysis

Motif-based approximate Personalized PageRank (MAPPR) algorithm ([Yin et al., 2017](#)) was used to identify an optimal higher-order motif-focused cluster (i.e., minimum motif conductance) surrounding a hub neuron. Given a motif M , MAPPR has three key steps.

Constructing motif weighted graph W

The input graph, taken to be the binarized parameter matrix after thresholding for strongest connections (see [Identifying modeled traditional hub neurons](#)), is transformed into a weighted graph W where the weight depends on M . Specifically, W_{ij} is the number of instances of M containing nodes i and j .

Compute the approximate personalized PageRank vector

The personalized PageRank (PPR) vector represents the stationary distribution of a modified random walk seeded on a hub node u . At each step of the random walk, the random walker is ‘teleported’ back to the specified seed node with probability $1 - \alpha$, where α was set to 0.98. The stationary distribution of this process for a seed node u (the PPR vector p_u), will have larger values for nodes ‘close’ to u . The stationary distribution is the solution to the following system of equations:

$$(I - \alpha AD^{-1})p_u = (1 - \alpha)e_u$$

Where I is the identity matrix, A is the adjacency matrix, D is the diagonal degree matrix, and e_u is the vector of all 0's except for a 1 in position u . The PPR vector p_u can be approximated via $\tilde{p}_u$ with accuracy $\epsilon = 0.0001$ such that

$$0 \leq D^{-1}p_u - D^{-1}\tilde{p}_u \leq \epsilon$$

Identify higher-order motif-focused cluster as a set with minimal motif conductance

A sweep procedure is used given approximated APPR vector $\tilde{p}_u$. Nodes are sorted by descending value of the vector $D^{-1}\tilde{p}_u$ and are incorporated one at a time into a growing set X . After a node added to the set, the motif conductance is calculated.

$$\phi^M(X) = \frac{\text{cut}_M(X)}{\min(\text{vol}_M(X), \text{vol}_M(X'))}$$

where $\text{vol}_M(X)$ is the number of motif endpoints in X , $\text{vol}_M(X')$ is the number of motif endpoints for nodes not in X , and $\text{cut}_M(X)$ is the number of instances of M that have at least one end point in X . The set with the smallest motif conductance is deemed optimal and returned. For traditional edge-based clustering, step one is skipped, and the edge conductance score is quantified as above but replacing motif instance M with simple edges. Only clusters with at least 5 nodes were considered for analysis. The MAPPR algorithm was run using Stanford Network Analysis Platform (SNAP) ([Leskovec and Sosić, 2016](#)).

Trajectory deviation

The Euclidean distance d between the mean calcium signals of two networks X and X' was calculated.

$$d(x(t), x'(t)) = \sqrt{\sum_{i=1}^T (x_i - x'_i)^2}$$

Here, $x(t)$ is the mean calcium signal for network X and $x'(t)$ is the mean calcium signal for network X'. In this work, X' is a network that underwent single-neuron perturbation (see [Perturbation simulations](#)) or had neurons “disconnected.” To compare simulations across control and epileptic networks, trajectory deviation TD was calculated as the Euclidean distance normalized by remaining time points left after start of perturbation t_o .

$$TD(x, x') = \frac{d(x, x')}{T - t_o}$$

Change in total power

To determine network response to perturbation (see [Perturbation simulations](#)), the variance of the mean calcium signal before and after perturbation was calculated. The percent change in the variance was measured:

$$\% \text{ change signal power}(x, x') = \frac{|var(x') - var(x)|}{var(x)}$$

Here, x represents the mean calcium signal of the unperturbed network and x' represents the mean calcium signal of the perturbed network. Note that signal variance is equal to the total power of the signal. Greater values indicate the network is less stable and is tightly correlated to trajectory deviation.

Statistical analysis

Values reported as $x \pm y$ represent mean $\pm$ standard deviation. Statistical analysis was performed using python *scipy.stats* ([Virtanen et al., 2020](#)) package. Parametric tests used: unpaired t test, paired t test. Non-parametric tests used: unpaired Mann-Whitney *U*-test, paired Wilcoxon signed-rank test, Kolmogorov-Smirnov test. Statistical details can be found in the results and figure legends. The Shapiro-Wilk test was used to determine if data met assumptions of normality. p values were corrected (“adjusted p”) using Bonferroni’s method for multiple comparisons. p values are reported in all figure subpanels except when $p < 0.001$. Statistical significance was set at 0.05.