

Surface Normal Lasing from CdSe Nanoplatelets Coupled to Aluminum Plasmonic Nanoparticle Lattices

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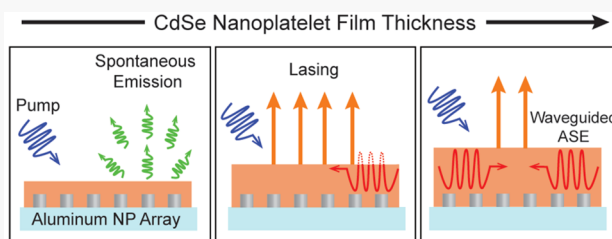
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ABSTRACT: This paper describes low-threshold lasing from colloidal CdSe nanoplatelets (NPLs) coated on two-dimensional plasmonic cavities composed of aluminum nanoparticles (NPs). We designed the NP lattice to support a spectrally narrow surface lattice resonance whose wavelength overlapped with the amplified spontaneous emission (ASE) from CdSe NPLs. Al NP lattices coated with CdSe NPL thin films were optically pumped and exhibited lasing in the surface normal direction with low angular divergence, narrow spectral line width (~ 1 nm), and a threshold of ~ 200 $\mu\text{J}/\text{cm}^2$. Nonlinear light emission characteristics were found to depend on the thickness of the CdSe NPL film. A minimum thickness of 150 nm was required to observe SLR-mediated lasing, but thinner films exhibited only photoluminescence. Films above 150 nm exhibited both in-plane waveguided ASE from the CdSe NPL film and lasing action from the Al NP lattice.



INTRODUCTION

Semiconductor nanoplatelets (NPLs) are promising for optoelectronic technologies such as light-emitting diodes and compact lasers due to their scalable synthesis, facile solution processing, narrow band-edge emission spectra, and large optical gain coefficients.^{1–8} Similar to 2D quantum wells, NPLs can be synthesized with an identical number of vertically defined monolayers and have comparatively large lateral dimensions for tunable, homogeneously broadened band-edge absorption and photoluminescence.² NPLs also offer advantages for gain and lasing relative to zero-dimensional quantum dots:^{9,10} the narrow band-edge line widths aid light amplification, the large lateral sizes (25 nm length \times 4 nm width \times 1.5 nm thickness) boost absorption cross sections by an order of magnitude,¹¹ and multiexciton lifetimes needed for population inversion can exceed those of the smaller-volume quantum dots from slower rates of Auger recombination.^{12–16} However, optical gain lifetimes for single-component (core-only) NPLs are subnanoseconds, and small cavity sizes are needed for light amplification.

Lasing action requires a cavity that provides low-loss constructive optical feedback at one or more wavelengths within the supported spectral profile of a population-inverted gain medium.¹⁷ Light amplification using semiconductor nanostructures has been demonstrated by using a wide variety of compact cavity architectures including whispering gallery mode resonators,^{18,19} distributed feedback gratings,^{20,21}

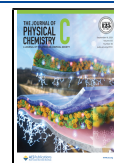
vertical cavities,^{15,22} and photonic crystals.^{6,23} We have reported how 2D plasmonic nanoparticle (NP) lattices can act as nanolaser cavities for colloidal quantum dots,^{24,25} upconverting nanoparticles²⁶ as well as organic dyes.^{27–34} Plasmonic NP lattices support two types of plasmons: (1) localized surface plasmons (LSPs), arising from collective electron oscillations in isolated metal NPs, and (2) surface lattice resonances (SLRs), which are LSPs coupled to Bragg modes defined by lattice periodicity.^{35–37} Several design parameters influence SLR characteristics such as lattice symmetry and spacing,^{38–40} refractive index of the substrate, medium surrounding NPs, NP size, and materials composition.^{41–47} When NP lattices are of high quality, the SLRs exhibit remarkably narrow spectral features (a few nanometers)^{43,48} that influence laser characteristics including spectral width,^{31,33} directionality of emission,^{25,32,49} temporal profile,^{50,51} and polarization.²⁴

Here we report the lasing characteristics of CdSe NPL films on Al NP lattices. CdSe NPLs were deposited on NP lattices with narrow SLRs (<4 nm), resulting in the formation of

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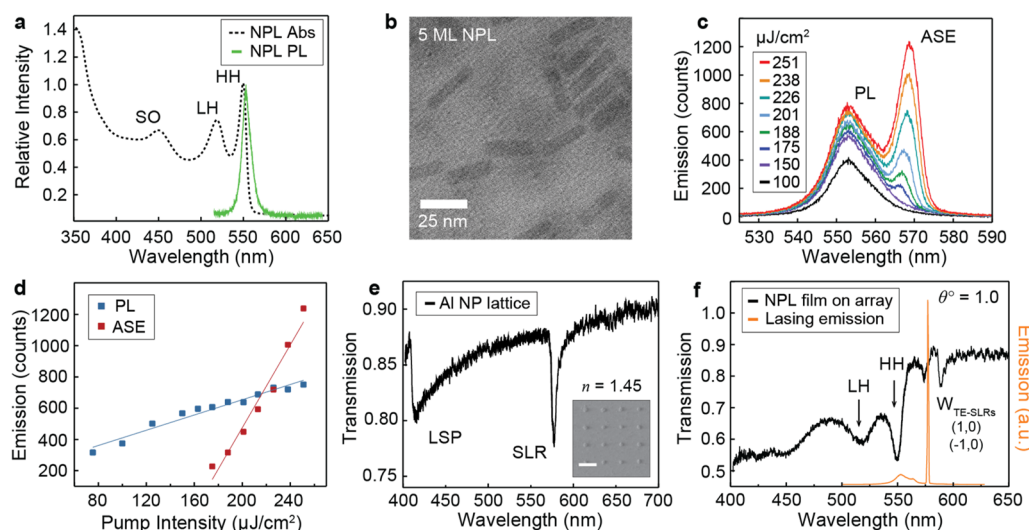


Figure 1. Characterization of 5-monolayer CdSe NPLs on quartz and on a patterned Al NP lattice. (a) UV–vis absorption (dashed line) and photoluminescence (solid line) spectra of 5-monolayer-thick CdSe NPLs. Absorption was measured in hexane solution, and the emission was measured from a drop-cast film. (b) Bright-field transmission electron microscopy image of synthesized NPLs; short edge length = 7.6 ± 0.9 nm and long edge = 24.7 ± 3.0 nm. (c) Emission from CdSe NPLs drop-cast on a quartz substrate as a function of pump fluence with an ASE threshold of $175 \mu\text{J}/\text{cm}^2$. (d) Emission intensity at 552 nm shows a sublinear dependence on pump intensity (log–log slope of 0.72 ± 0.003) while the ASE maxima rises superlinearly (4.78 ± 0.11). (e) Transmission spectrum of an Al NP lattice on quartz substrate ($n = 1.46$ at 570 nm) surrounded by an index-matched oil. Inset: SEM image of a square Al NP lattice. Scale bar is 400 nm. (f) Transmission spectrum of an Al NP lattice with a 150 nm thick CdSe NPL film shows light hole (LH) and heavy hole (HH) absorption features as dips at 512 and 550 nm, respectively; $W_{\text{TE-SLR}}$ modes appear near 574 and 589 nm. Optical excitation above threshold yields narrow spectrum laser emission that overlaps with a $W_{\text{TE-SLR}}$ mode.

waveguide SLRs. When optically pumped, nonlinear lasing emission from the hybrid mode was dependent on the NPL film thickness. For NPL films at least 150 nm thick, lasing emission in the far field exhibited small divergence ($<1^\circ$), low threshold ($\sim 200 \mu\text{J}/\text{cm}^2$), and ultrafast decay dynamics near the position of the waveguide SLR. Thinner films exhibited only photoluminescence, while thicker films produced waveguided ASE in addition to the surface normal lasing.

RESULTS AND DISCUSSION

CdSe NPLs with a thickness of 5 monolayers were synthesized by using an established protocol¹⁵ and showed narrow band-edge transitions (~ 12 nm full width at half-maximum (FWHM), Figure 1a and Figure S1). The flat NPL morphology was confirmed by transmission electron microscopy (Figure 1b); the short and long edge dimensions were measured to be 7.6 ± 0.9 nm and 24.7 ± 3.0 nm, respectively. This thickness of the CdSe NPL was selected because of its high synthetic reproducibility and slow Auger recombination relative to thinner 3- and 4-monolayer thick NPLs.^{14,15} The refractive index of close-packed CdSe NPLs was determined to be $n = 1.8$ at 570 nm based on the volume fraction of CdSe ($n = 2.56$) and oleic acid ligands ($n = 1.46$).⁵² NPLs drop-cast on quartz substrates from a concentrated (~ 200 mg/mL) dispersion by using a 9:1 hexane:octane solution produced $t \sim 150$ nm thick films. When pumped at 400 nm with 35 fs pulses, the band-edge PL from single-exciton recombination was observed at low pump intensity ($<150 \mu\text{J}/\text{cm}^2$). Increasing the pump intensity to $170 \mu\text{J}/\text{cm}^2$ produced spectrally narrowed (~ 7 nm FWHM) amplified spontaneous emission (ASE) near 568 nm in the direction parallel to the plane of the film, with a superlinear intensity dependence on pump fluence that was distinct from the sublinear band-edge emission. The ASE from CdSe NPLs red-shifted to longer wavelengths (566–568 nm) relative to band-edge emission (552 nm) because of

attractive biexciton Coulombic interactions and reduced losses from reabsorption (Figures 1c,d).

The large refractive index mismatch of the CdSe NPL film layer ($n = 1.8$) and the quartz substrate ($n = 1.45$) results in an optical waveguide upon light excitation.⁵³ Hybridization between this waveguide mode and the SLR mode from the Al NP lattice produces waveguide surface lattice resonances (W-SLRs).^{24,25} Finite-difference time-domain simulations were used to model the properties of the NPL-NP lattice under s-polarized white light with adjustable particle sizes, periodicity, and refractive index environment (Supporting Information). A calculated W-SLR that spectrally overlaps with the NPL gain was supported by Al NPs with diameter $d = 75$ nm, height $h = 60$ nm, and lattice periodicity $a_0 = 400$ nm on a quartz ($n = 1.45$) substrate (Figure S2). Aluminum was selected as the plasmonic material of interest because of its low losses at both the emission wavelength and the 400 nm optical pump wavelength (Figure S3).⁴⁴

Because previous reports showed that the sidebands of W-SLR modes from colloidal quantum dots at nonzero k_{\parallel} provided optical feedback for lasing,^{24,25} we simulated off-normal transmission spectra to identify the W-SLR sidebands from the NPL-NP lattice (Figure S2a). Tuning the angle of incident light between 0° and 1° produced features that correspond to (1,0) and (−1,0) waveguided transverse electric SLR ($W_{\text{TE-SLR}}$) modes; the (1,0) mode is the sideband lasing mode. The experimentally measured lasing emission at 577 nm approximately matches the spectral position of the $W_{\text{TE-SLR}}$ sideband mode (587 nm) in the simulated results.

Large-area (cm^2) Al NP lattices were produced using a series of nanofabrication processes described previously (Figure S4).⁵⁴ Normal-incidence transmission spectra of the fabricated NP lattice in an index-matched environment of $n = 1.45$ revealed a spectrally narrow SLR with a 4 nm FWHM at 577 nm (Figure 1e). Transmission spectra of a 150 nm thick NPL

film on the same Al NP lattice showed reduced intensity from CdSe NPL absorption features and two W_{TE} -SLR modes with order (1, 0) and (−1,0) (Figure 1f). Figure 2 depicts the

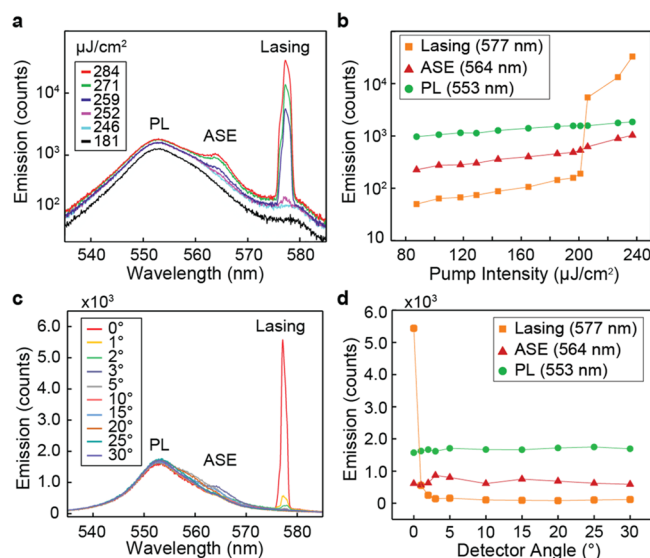


Figure 2. Light emission from a 150 nm thick CdSe NPL film on an Al NP lattice. (a) Normal incidence emission spectra measured for the indicated pump laser fluences show development of strong, spectrally narrow (1 nm FWHM) lasing emission at 577 nm and suppressed ASE at 563 nm. (b) Light emission from different optical processes shows that laser emission grows nonlinearly compared to PL above $\sim 200 \mu\text{J}/\text{cm}^2$. (c, d) Emission spectra at different detection angles using a pump fluence of $260 \mu\text{J}/\text{cm}^2$ shows highly directional emission for signals near 577 nm in contrast to PL and ASE.

fluence and angle dependence of light emission from the NPL-NP lattices. Emission was collected by using a fiber optic mounted on a concentric rotational stage that directed the light into a spectrograph and CCD. Detecting at normal incidence to the lattice, we measured NPL photoluminescence (PL) at low fluences centered around 553 nm, and then narrowband lasing emission at 577 nm was observed for a fluence of $200 \mu\text{J}/\text{cm}^2$ (Figure 2a); this threshold is relatively low compared to that from colloidal quantum dot systems.²⁴ Emission intensity vs pump fluence shows that the PL follows a linear trend while the 577 nm peak attributed to lasing rises superlinearly and narrows (Figure 2b). Time-correlated single photon counting (TCSPC) and streak camera measurements were used to compare the emission time scales of single-

exciton radiative recombination (nanoseconds) with the ultrafast dynamics (picoseconds) of lasing emission (Figure S5).⁵⁰ Emission directionality was evaluated by collecting spectra above the lasing threshold as a function of detection angle. The surface normal direction had a divergence of less than 1° , while both PL and ASE showed diffuse scattering (Figures 2c,d).

An important parameter identified to control the emission characteristics of CdSe NPL-Al NP lattices was the thickness of the CdSe NPL film. Drop-cast films produce a “coffee ring effect” where the film is thickest near the droplet edge from particle transport during drying.^{55,56} Figure 3a shows an optical micrograph of different NPL film thicknesses on a Al NP lattice. Atomic force microscopy images confirmed that the thickest region of the NPL film was $t_2 = 200 \text{ nm}$; the center of the NP lattice and the thinnest film regions were measured to be 150 and 110 nm, respectively (Figures S6 and S7). The average roughness of the NPL film was determined to be 1.96 nm across a $7 \mu\text{m}$ region as calculated by the root-mean-square method (Figure S8). These different film thicknesses showed distinct behavior when optically pumped. Neither ASE nor lasing was observed for the thinnest ($t_1 = 110 \text{ nm}$) NPL region even for the highest pump fluence tested of $356 \mu\text{J}/\text{cm}^2$ (Figure 3b). In contrast, for $t_2 = 200 \text{ nm}$ areas, both ASE and lasing were present (Figure 3c). Note that the intermediate thickness of $t = 150 \text{ nm}$ in Figure 2a produced lasing with ASE suppressed. Angle-resolved emission showed that lasing signals were emitted normal to the surface (Figure S9), while ASE was observed over a wide range of angles ($0^\circ - 30^\circ$) consistent with incoherent scattering. For thin films, the CdSe NPL layer does not provide enough optical gain to overcome losses of the NP lattice cavity. To determine the minimum NPL film thickness required to observe lasing and ASE, we drop-cast a film using a dilute ($20 \text{ mg}/\text{mL}$) NPL dispersion (Figure S10). In this case, no ASE was generated, and only PL signals were detected despite exploring high excitation fluences ($>1 \text{ mJ}/\text{cm}^2$). These three classes of emission depend on the overall thickness of the CdSe NPL film because the refractive index of the film governs the W_{TE} -SLR wavelengths.²⁴ With an optimal film thickness of 150 nm, the W_{TE} -SLR cavity mode spectrally overlaps with the NPL emission and shows low-threshold lasing.

CONCLUSIONS

CdSe NPLs can function as high-performance solid-state laser gain media and exhibit room-temperature lasing when integrated with NP lattice nanocavities. Our findings provide

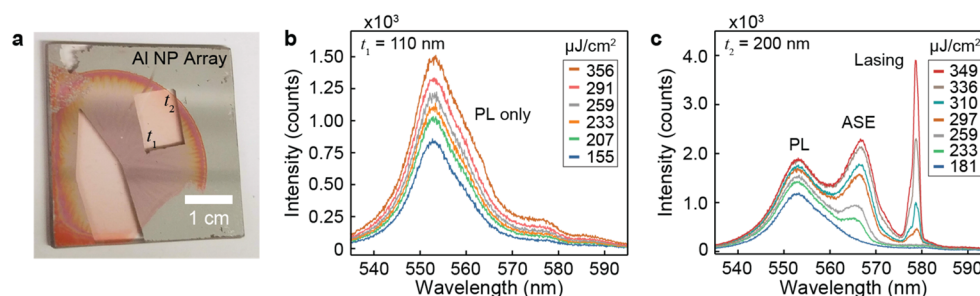


Figure 3. Light emission characteristics for different CdSe NPL film thickness on an Al NP lattice. (a) Optical micrograph of a drop-cast CdSe NPL film on an Al NP lattice. t_1 and t_2 denote regions with thicknesses of 110 and 200 nm, respectively. (b) Emission from the t_1 (thin) region of CdSe NPL film shows neither ASE nor lasing even at high pump fluences. (c) Emission from the t_2 (thick) CdSe NPL film shows both ASE and lasing.

insight into how high-index colloidal semiconductor gain can introduce waveguide effects that hybridize with plasmonic lattices. Because NPLs are anisotropic structures, the prospects of controlling particle orientation and thus dipole direction could potentially enable tailoring of the far-field laser beam profile, polarization state, and threshold. We demonstrated the capability of using core-only CdSe NPLs as a gain medium for lasing despite losses from nonradiative Auger recombination. For enhancing lasing performance further, core-shell and gradient shell approaches to growing NPL heterostructures will be investigated to prolong multiexciton lifetimes for increased optical gain.

■ ASSOCIATED CONTENT

SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcc.1c05662>.

Materials and methods used to synthesize CdSe NPLs and additional details on fabrication of Al nanoparticle lattices, measured transmission from neat CdSe NPL film, FDTD simulated transmission spectra, FDTD simulated electric near-field intensity of Al NP lattice, scanning electron microscopy images of lattice fabrication steps, atomic force microscopy characterization of Al NP height, NPL film thickness, and average film roughness, angle-resolved measurement of amplified spontaneous emission (ASE), emission dynamics captured with streak camera, and time-correlated single photon counting (PDF)

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Notes

The authors declare no competing financial interest.

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