



A density functional theory investigation of the reaction of water with Ce_2O^-

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ABSTRACT

Cerium suboxide clusters are a recent catalyst class that has received interest for the generation of H_2 from water. Using density functional theory calculations, this work examines the reaction of Ce_2O^- clusters with H_2O . It is shown that the reaction can proceed along both doublet and quartet pathways. In both cases, hydrogen formation is facilitated by intermediate structures featuring bridging hydride and hydroxide ligands. Interestingly, it is shown that metal d electrons facilitate the reduction of water. This work provides new understanding of this reaction and provides new insight into the reactivity of small lanthanide-based clusters with water.

1. Introduction

Water, being one of the most abundant substances in nature, has been the subject of intense interest for scientists to study its physical and chemical properties.[1–11] In addition to the roles water plays in myriad chemical reactions and biological systems, H_2O has been a key focus in energy related research. Of particular interest are catalysts facilitating the four-electron $2\text{H}_2\text{O} \rightarrow 2\text{H}_2 + \text{O}_2$ reaction.[12–17] Cerium oxides attracted special interest recently due to their ability to efficiently catalyze a wide range of oxidation and reduction reactions, including water–gas shift reactions.[18–22] Several studies have also shown that cerium oxide-supported metal surfaces exhibit increased catalytic activity relative to their non-cerium oxide supported analogues.[23–35].

Surface defects due to metal or oxide deficiencies possess unique electronic properties and facilitate increased reactivity. Such defect sites exhibit incomplete valencies and localized electronic structures.[36] As with other metal oxides, the catalytic activity of lanthanide oxide surfaces is most active at surface defect sites. However, studying extended surfaces is complicated by the low concentration of surface defects and the continuous structural changes along the surfaces. Alternatively, small gas-phase lanthanide oxide clusters can serve as representative model systems for studying reactivity of defect sites on extended surfaces.

Several experimental and computational studies have been performed on cerium oxide clusters in order to better understand the electronic structure features that pave the way to a thorough

understanding of their reactivity and catalytic activity. In addition, various experimental and theoretical studies have explored the reactivity of classes of cerium-based clusters with various gas-phase small molecules.[37,38,19,39–49,17,50,51] Of particular interest here are computational studies conducted by Zhou and co-workers on the reactivity of Ce_n ($n = 1–3$) with up to six water molecules.[37,38] Their results indicate high reactivity of these cerium clusters and their efficiency in decomposing multiple water molecules. Recently, Jarrold and co-workers reported mass spectra of Ce_xO_y^- systems ($x = 2,3, y = 1–4$) and their products from reactions of the clusters with water.[17] Their results indicate that cerium oxide clusters undergo three types of reactions: hydrogen gas production, water abstraction, and hydroxide abstraction. The relative selectivity of one reaction type over the others is highly dependent on the stoichiometry of the cluster. For example, Ce_2O^- , Ce_3^- , Ce_3O_2^- , and Ce_3O_2^- preferentially produce H_2 gas, while clusters with equal stoichiometric ratios of Ce and O undergo OH abstraction, and clusters bearing more oxide than cerium ions undergo water abstraction.

In this work, we consider the simplest stoichiometric cluster of cerium oxide capable of efficient H_2 gas production, Ce_2O^- . Previously reported experimental results include data from mass-spectrometry and photoelectron spectroscopy, which provide valuable information on the geometric and electronic structures of the studied molecules.[17,48] We note that this particular cluster is explored here to specifically examine these gas phase experimental results and is not a direct model for the extended surface system. Below, we first examine the geometric and

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electronic structure of different clusters potentially involved in the reaction. We then explore the potential energy surfaces corresponding to various states and identify a likely pathway for H_2 formation from water at Ce_2O^- clusters.

2. Computational Methods

Calculations were performed using a development version of the GAUSSIAN suite of electronic structure programs.[52] The B3PW91 density functional was employed.[53–57] The unrestricted formalism was used for all calculations.[58,59] The stability of all calculated Kohn–Sham determinants was verified.[60–62] The Stuttgart relativistic small core atomic natural orbital basis set and corresponding effective core potential (ANO/ECP) basis set with 28 core electrons and a contracted valence basis set (14s13p10d8f6g)[6s6p5d4f3g] was used for cerium center.[63] The Dunning style correlation-consistent basis set aug-cc-pVTZ was used for oxygen and hydrogen centers.[64,65].

Geometry optimizations were carried out using standard methods and the nature of each located potential energy surface stationary point was confirmed by vibrational frequency analysis.[66] Intrinsic reaction coordinate (IRC) calculations were performed to ensure that optimized transition structures connect appropriate potential energy surface minima.[67,68] Reported enthalpies of reactions were calculated at 298 K. Relative energies including zero-point corrections at 0 K are reported in the supporting information.

We note that systems featuring multiple metal centers and open-shell electronic structure, such as those studied here, can potentially exhibit multi-reference character. In particular, these systems might exhibit close-lying electronic states with relatively small energy gaps. For this reason, the results from DFT calculations must be interpreted with some caution and detailed analysis. As such, all calculations reported involved evaluation of Kohn–Sham determinant stability, analysis of spin contamination, and manual inspection of the occupied one-electron molecular orbitals. This approach follows from our previous experience working with such systems as well as studies reported by other groups in which DFT calculations for similar systems have yielded energies and observables that are in good agreement with experimental results.[69,70,47,71,72,46,73,74,51,75].

3. Results

In the discussion that follows, structures are labeled as **X-n**, where **X** = **A, B, C...** represents a particular molecular structure and the value of *n* indicates the multiplicity of the cluster. For example, **A-4** refers to the quartet spin state of structure **A**. Transition structures are labeled as **TS1-n** and **TS2-n**. Again, *n* denotes the spin multiplicity of the transition structure. A thorough search for numerous isomers and electronic states was performed to identify candidate reactants, intermediates, products, and transition structures.

As discussed in greater detail below, this investigation ultimately identified two viable pathways for the reaction $\text{Ce}_2\text{O}^- + \text{H}_2\text{O} \rightarrow \text{Ce}_2\text{O}_2^- + \text{H}_2$. Specifically, it was found that reactions along doublet and quartet pathways are both likely. In both cases, the reaction begins water addition to a Ce_2O anion cluster, followed by formation of hydride and then hydroxide bridges, and finally yields evolution of molecular hydrogen (Scheme 1).

3.1. Reactant and Product Cerium Oxide Clusters

Prior to exploring the mechanism of $\text{Ce}_2\text{O}^- + \text{H}_2\text{O} \rightarrow \text{Ce}_2\text{O}_2^- + \text{H}_2$, we considered possible structures of the initial Ce_2O^- cluster species and the final oxidized cluster Ce_2O_2^- . Various molecular structures and electronic configurations were considered. For the Ce_2O^- molecular cluster, two general structural motifs are possible: (1) the oxygen atom can bridge the two cerium atoms (Compound **A**, Fig. 1); or (2) the oxygen can be in a terminal position and bound to only one cerium site as only (Compound **B**, Fig. 1). In addition to the molecular structure, we examined multiple spin-states. Specifically, calculations were carried out on the doublet, (ground-state) quartet, and sextet multiplicities.

Our calculations showed that several different structures of Ce_2O^- species exist. Fig. 1 shows the energetically competitive Ce_2O^- species. The ground state of Ce_2O^- , **A-4**, is a quartet state featuring a bridging oxide. In this structure, the two Ce–O bonds are equivalent with a bond length of 2.06 Å and a Ce–O–Ce angle of 120.8°. The sextet **A-6** lies 3.92 kcal/mol higher than **A-4** and the doublet state **A-2** is only 2.1 kcal/mol higher in energy than the ground state. These results are in agreement with the anion photoelectron spectroscopy results published by Kafader et al.[47].

Another located structure, **B-6**, features a terminal oxide and has a sextet spin ground state. This structure is much higher in energy than the others, at 48.40 kcal/mol higher than **A-4**. Quartet and doublet states were not found for structure **B**. Despite its absence in the previously reported photoelectron spectrum of Ce_2O^- [47] and its higher energy relative to the ground-state **A-2**, we still considered the possibility of the role of **B-6** in the reaction with water and consequent H_2 production. Nevertheless, we were unable to locate a reaction pathway starting with **B-6** and leading to the evolution of H_2 .

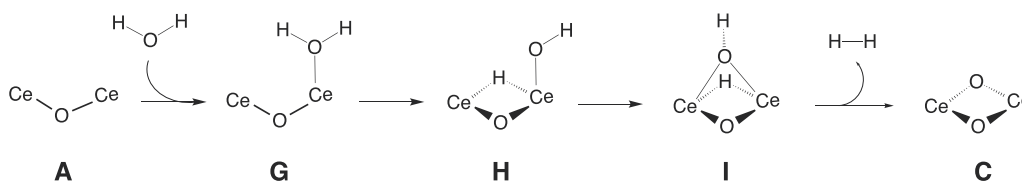
We next considered candidates for the product Ce_2O_2^- clusters. As for the initial cluster species **A** and **B**, each oxide in the product cluster can either be at terminal or bridging positions. We found four different general geometric structures; considering doublet, quartet, and sextet spin states resulting in 11 distinct candidate final product clusters, which are shown with their relative energies in Fig. 2.

The ground state product cluster, **C-4**, is a quartet planar compound with both oxygens bridging the two cerium ions. Another closely lying state is doublet **C-2**, which has a geometry similar to the ground-state. **C-2** lies only 0.63 kcal/mol higher than **C-4**, and the geometries of the two structures are quite similar.

Compounds **C-6** and **F-2** lie approximately 25 kcal/mol higher in energy than **C-2** and **C-4**. Sextet **C-6** is 24.94 kcal/mol higher in energy than **C-4**. Although the structure of **C-6** is similar to **C-4** and **C-2**, **C-6** is not a planar structure. Specifically, the Ce–O–Ce–O torsion angle is 20.3°, unlike **C-4** and **C-2** that are planar.

An additional set of higher energy Ce_2O_2^- isomers (**D**, **E**, and **F**) were also located. The geometry of **F-2**, which is close in energy to **C-6** at 27.14 kcal/mol relative to the lowest-energy **C-4** cluster, is quite different. Specifically, one oxide is terminal while the other one is bridging. Given that **D-2**, **D-4**, **D-6**, **E-2**, **E-4**, **E-6**, and **F-6** are all much higher in energy (58.73–162.47 kcal/mol) we presume that they do not contribute to the mechanistic study presented in this paper and do not consider them further.

In previous work, Kafader et al. reported the anion photoelectron spectra of Ce_2O^- and Ce_2O_2^- together with a computational analysis to



Scheme 1. Overview of the proposed mechanism for the reaction $\text{Ce}_2\text{O}^- + \text{H}_2\text{O} \rightarrow \text{Ce}_2\text{O}_2^- + \text{H}_2$.

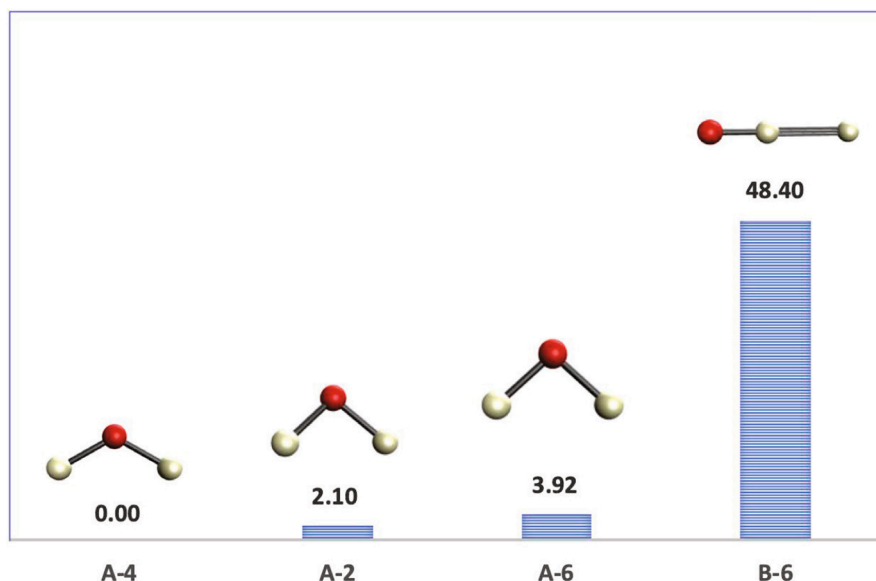


Fig. 1. Optimized structures and energies of located Ce_2O^- clusters. Energies are given in kcal/mol and are relative to that of A-4. Cerium atoms are shown in gold and oxygen atoms are shown in red. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

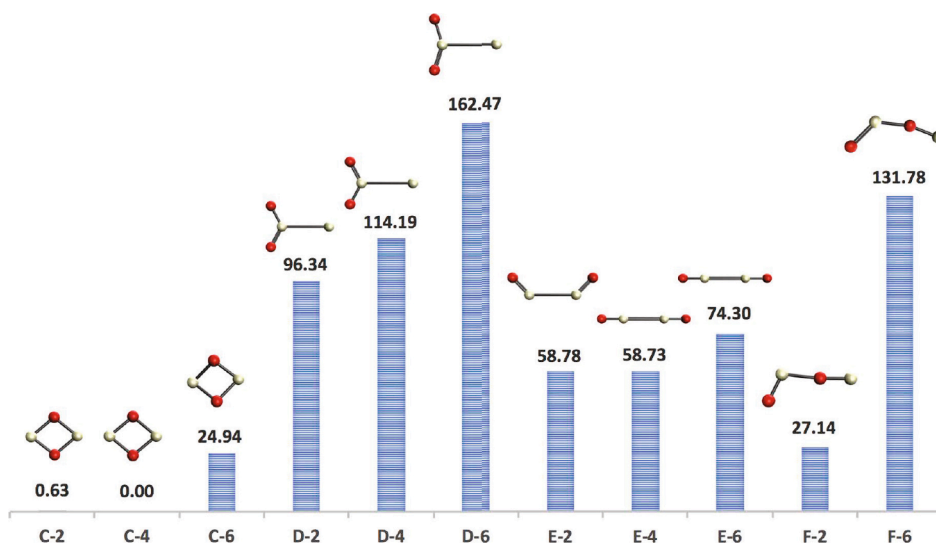


Fig. 2. Optimized structures and energies of located Ce_2O_2^- clusters. Energies are given in kcal/mol and are relative to that of C-4. Cerium atoms are shown in gold and oxygen atoms are shown in red. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

fully characterize the observed structures.[47] DFT calculations and Franck–Condon simulations were used to determine that the ground-state configuration of Ce_2O^- is a $^4\text{A}_2$ state with the Ce–O–Ce bridge bonding being the favored structural motif, resulting in C_{2v} symmetry. They found another close-lying $^2\text{A}_2$ state with a bonding motif resembling the ground-state quartet species. These two structures correspond to A-2 and A-4 structures reported in this work (Fig. 1). Using the same approach, Kafader et al. determined the ground-state configuration for Ce_2O_2^- to be a $^4\text{A}_g$ state with the $^2\text{A}_g$ state being slightly higher in energy. Both structures exhibit D_{2h} symmetry and Franck–Condon simulations confirmed their contributions to the photoelectron spectrum. These two structures resemble C-4 and C-2 shown in Fig. 2, respectively. As far as the starting materials and the final products are concerned, our computational results are in good agreement with the results reported by Kafader and coworkers. Thus, the two (non-relativistic) potential energy surfaces to be explored are the $^4\text{A}_2$ and $^2\text{A}_2$ routes that start with compounds A-4 and A-2 and lead to $^4\text{A}_g$ and $^2\text{A}_g$ clusters C-4 and C-2.

Fig. 3 shows the frontier molecular orbitals (MOs) of A-2 and A-4. The MO diagram of A-4 is comprised of three general manifolds: 4f, σ/σ^* , and 5d orbitals. The first frontier orbital group includes two singly occupied 4f orbitals localized on the cerium centers. The σ and σ^* orbitals are doubly occupied and are predominantly Ce 6s-based. Finally, the highest occupied MO (HOMO) of quartet Ce_2O^- A-4, is a 5d-based singly occupied orbital with the electron delocalized across the two cerium centers. Similar to A-4, the frontier MOs for A-2 feature doubly-occupied 6s $_{\sigma}$ and 6s $_{\sigma}^*$, and singly-occupied 5d $_{\sigma}$ β orbital and 4f orbitals. The difference between the MO diagrams of A-4 and A-1 is the spin of the occupied 5d $_{\sigma}$ orbital.

MO diagrams for C-2 and C-4 (shown in Fig. 4) exhibit more similarity to each other than A-2 and A-4. Both spin states of structure C include the two singly occupied 4f orbitals present in their respective starting A clusters. In addition, both doublet and quartet spin states have a doubly occupied 6s-based σ orbital and a singly occupied σ^* orbital. The only difference is the spin of the electron occupying the σ^* orbital.

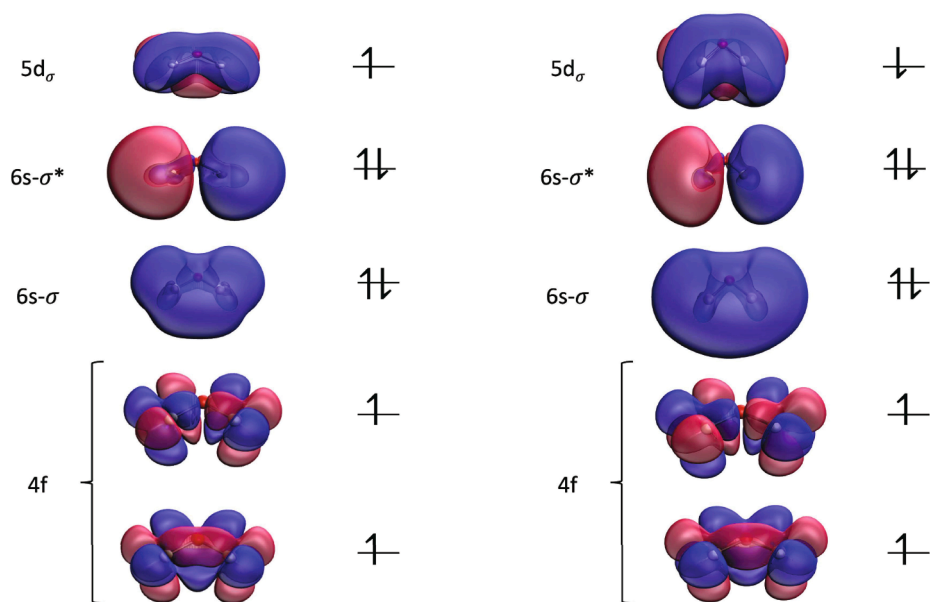


Fig. 3. Valence molecular orbitals of quartet (left) and doublet (right) Ce_2O^- .

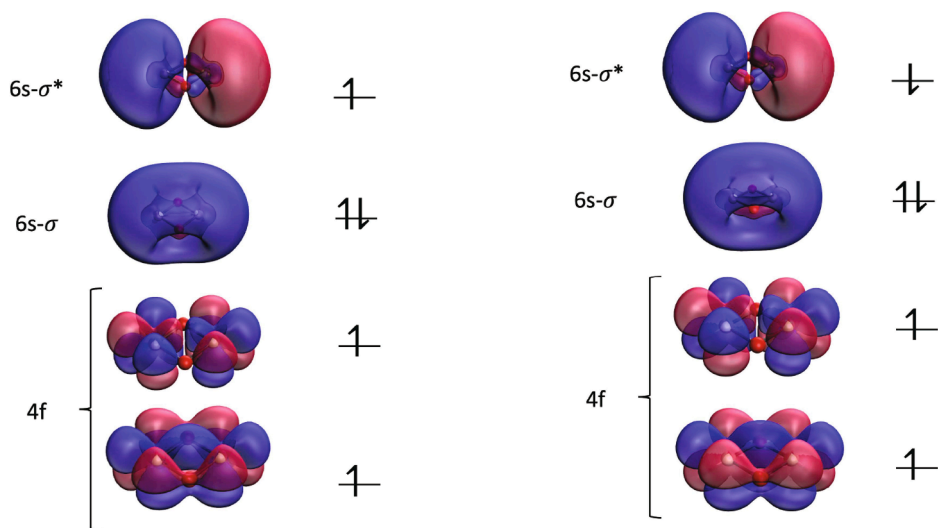


Fig. 4. Valence molecular orbitals of quartet (left) and doublet (right) Ce_2O_2^- .

The quartet has an α electron in the σ^* orbital, while that same orbital is occupied by a β electron in the doublet **C-2**. In a manner similar to the reactants, the doublet and quartet Ce_2O_2^- differ in the spin of the singly-occupied $6s_\sigma^*$ orbital.

The combined oxidation state of the two cerium centers is (+I) in Ce_2O^- and (+III) in Ce_2O_2^- . Figs. 3 and 4 show that the frontier molecular orbitals of both Ce_2O^- and Ce_2O_2^- exhibit delocalization of electrons over the two cerium metals. In addition, as discussed in the previous sections, all Ce–O bonds are equivalent within the same molecule in both the Ce_2O^- and Ce_2O_2^- . For these reasons, the oxidation states of the cerium centers should also be equal. Furthermore, given the delocalized nature of the frontier orbitals over the two cerium centers we take our computational results to suggest two resonance structures that have cerium centers with unequal oxidation states. For Ce_2O^- , the studied structure can be described by two resonance structures of Ce_2O^- , with each resonance form featuring one Ce(0) and one Ce(I) center. In a similar manner, the final Ce_2O_2^- structures **C-4** and **C-2** are described by two Ce(I)/Ce(II) resonance structures.

3.2. Water Addition

The reaction of Ce_2O^- with water begins with water addition. We have identified one unique mode for water addition to clusters **A-2** and **A-4**. This mode is best described as an interaction between the water oxygen and a terminal cerium atom, while the second cerium atom does not directly engage in this step. Water addition to the Ce_2O^- clusters **A-2** and **A-4** forms structures **G-2** and **G-4**. A notable feature about both adduct structures is that a water hydrogen is oriented towards the distant cerium, suggesting the feasibility of hydrogen interaction with the remote cerium center.

The relative heats of reactions of the water adducts are shown in Fig. 5. Formations of both adducts resulting from water addition to Ce_2O^- are exothermic, with ΔH values of -13.0 and -12.2 kcal/mol for the doublet and quartet states, respectively. For the formed intermediates, the distance between the water oxygen center and the cerium atom is 2.56 Å (**G-4**) and 2.49 Å (**G-2**). Additionally, the bound water is oriented such that a hydrogen atom is oriented toward the other cerium center.

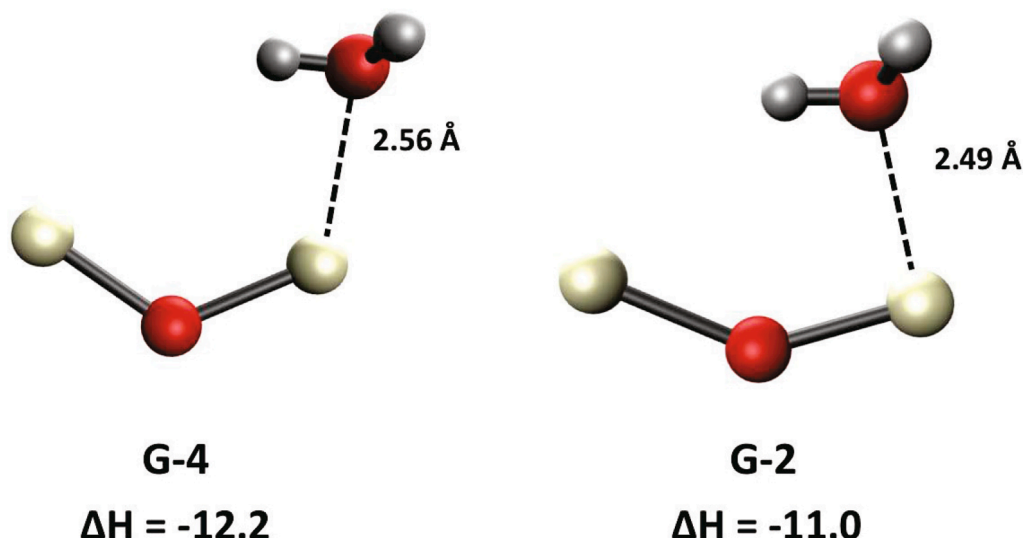


Fig. 5. Quartet G-4 (left) and doublet G-2 (right) with intermolecular distances given in Angstroms. Energies are given in units of kcal/mol and are relative to A-4 + H₂O. Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

3.3. Hydride Bridge Formation

Following water addition, the reaction undergoes Ce oxidation as a water O–H bond is cleaved and leads to formation of a bridging hydride. Structures H-2 and H-4 correspond to the resulting intermediates, Ce₂HO(OH)[−], that form from O–H bond cleavage in G-2 and G-4, respectively. Fig. 6 shows the structure and relative energies of two identified spin states that correspond to structure H.

The structure of H-2 and H-4 is best described as a four-member planar ring consisting of two cerium atoms, an oxygen, and a hydrogen, with a bound hydroxide ligand. The oxygen and hydrogen centers in the ring are both in bridging positions relative to the two cerium atoms. The bridging hydride binds to the Ce centers with bond lengths of 2.29 Å and 2.30 Å for both the doublet and quartet species. The O–H bond cleavage in both the quartet and doublet states is exothermic with heats of reaction of −73.0 kcal/mol (quartet state, G-4 → H-4) and −73.9 kcal/mol (doublet, G-2 → H-2) relative to their respective starting materials. Such exothermicity suggests the formation of H-2 and H-4 is highly thermodynamically favorable.

Transition structures TS1 connect G to H (Fig. 7). The two transition structures (TS1-4 and TS1-2) are geometrically similar to their respective reactants G-4 and G-2, with the water hydrogen oriented towards the two cerium centers. The Ce–H bond distances are 2.34 Å and 2.80 Å

(TS1-4) and 2.38 Å and 2.79 Å (TS1-2), respectively. Both G → H reaction steps are essentially barrierless. The TS1-4 and TS1-2 energy barriers are only 0.6 kcal/mol (−11.6 kcal/mol relative to A-4 + H₂O) and 0.2 kcal/mol relative to G-4 and G-2 (−11.2 kcal/mol relative to A-4 + H₂O).

3.4. Hydroxide Bridge Formation and H₂ Production

The relative positions of the two hydrogen centers is critical for the final H₂ formation step. With this in mind, we explored a series of possible rearrangement steps. Our calculations identified I-2 and I-4, both of which feature molecular orientations that are reasonable structural precursors to H₂ formation (Fig. 8). Structures I-2 and I-4 include a new hydroxide bridge between the cerium centers, resulting in the two hydrogens being in close proximity to one another (H–H distance is ~3 Å). These structures directly lead to subsequent release of H₂ and formation of product clusters C-2 and C-4. By comparing the Ce–H bond lengths of structures H-2 and H-4 with I-2 and I-4, we observe a decrease in bond distance as the hydroxide binds to the second cerium atom. Thus, the bond formation between the hydroxide and cerium plays a role in decreasing the distance between one of the cerium atoms and the hydride.

Our calculations identified transition structures connecting H-2 and

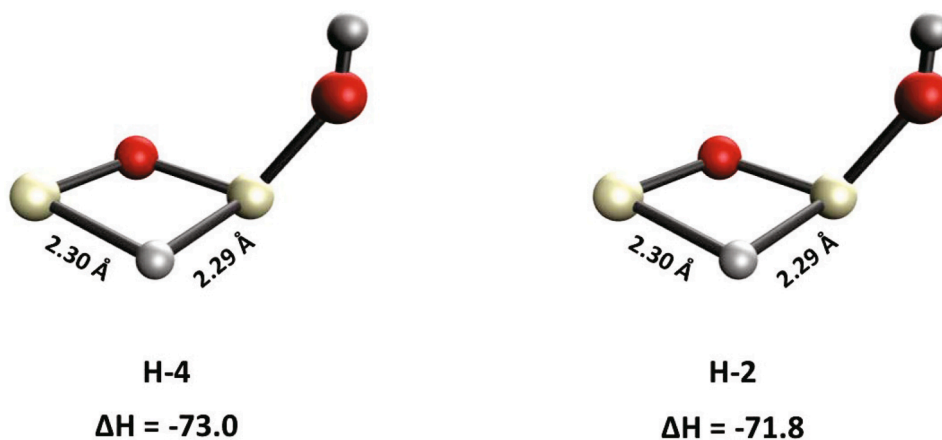


Fig. 6. Structures of quartet H-4 and doublet H-2, Ce–O distances are shown in units of Angstroms. Energies are given in units of kcal/mol and are relative to A-4 + H₂O. Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

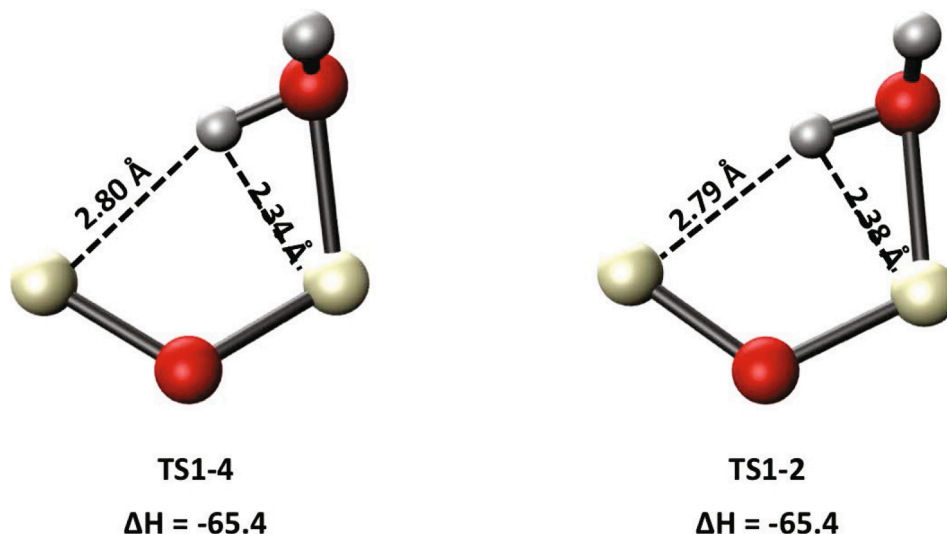


Fig. 7. Structure TS1-4 that connects G-4 and H-4 (left) and TS1-2 that connects G-2 and H-2 (right). Energies are given in units of kcal/mol and are relative to A-4 + H₂O. Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

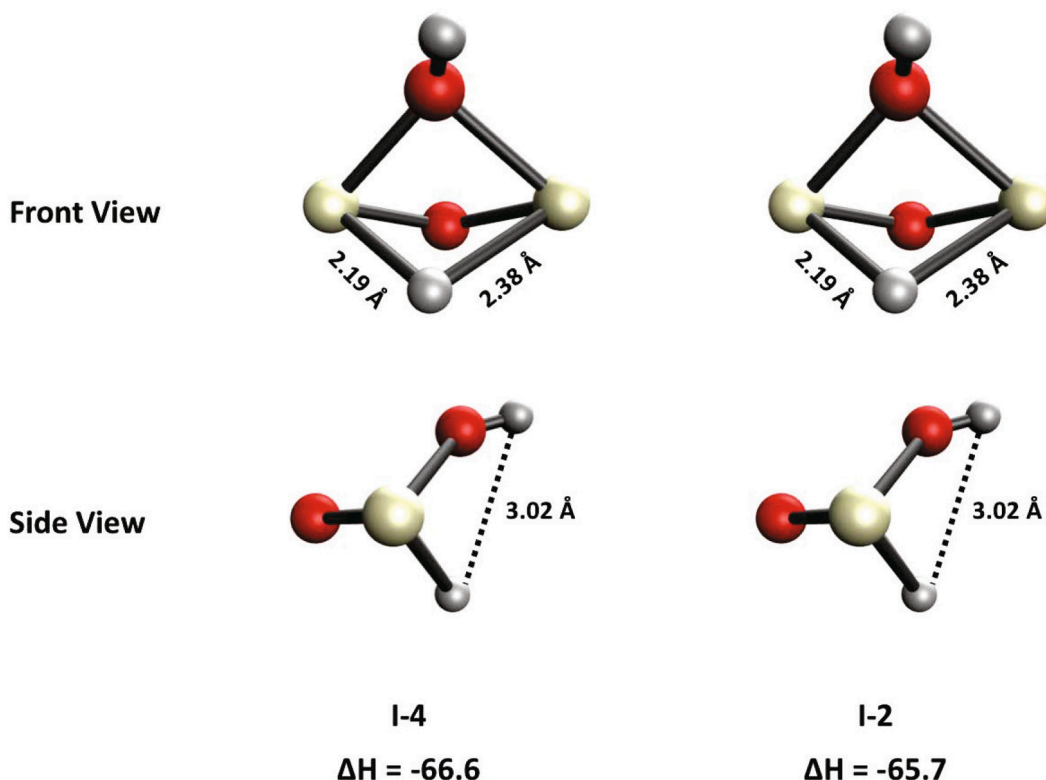


Fig. 8. Front and side view of the geometry of structures quartet I-4 (left) and doublet I-2 (right). Energies are given in units of kcal/mol and are relative to A-4 + H₂O. Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

H-4 to I-2 and I-4, shown in Fig. 9. In both cases, the transition structures present small reaction barriers (7.6 kcal/mol for the quartet and 6.5 kcal/mol for the doublet). In support of experimental interpretations,[47,48] these transition structures feature an electron rich hydroxide attracted by the electron-poor cerium centers resulting in diffuse multi-centered bonds involving the hydroxide and both cerium ions.

The final step of the mechanism involves H₂ production and formation of C-4 or C-2. In both quartet and doublet pathways, this final step is quite exothermic. The energies of the separated products are 24.7 kcal/

mol and 25.0 kcal/mol below the hydroxide/hydride bridge structures I-4 and I-2, respectively. Relative to the initial quartet Ce₂O⁺/water adduct, the reaction enthalpy for hydrogen gas evolution is −91.3 kcal/mol via the quartet pathway and −89.3 kcal/mol via the doublet pathway.

4. Discussion

Fig. 10 shows the full energy profile of the doublet (green) and quartet (orange) mechanistic routes. In both cases the overall reactions

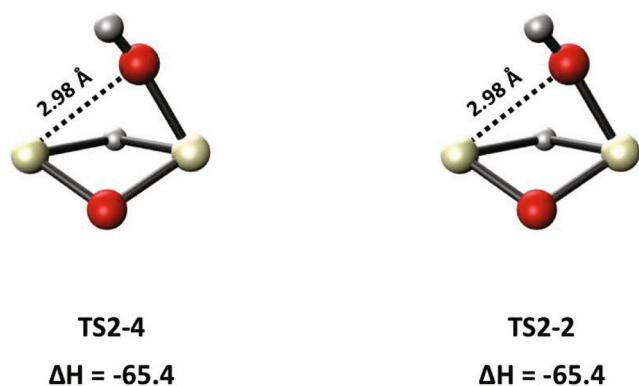


Fig. 9. Structures of **TS2-2** and **TS2-4** that connect **H-2** and **H-4** to **I-2** and **I-4**, respectively. Energies are given in units of kcal/mol and are relative to **A-4** + H_2O . Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

are barrierless, in agreement with the experimental data provided by Jarrold and coworkers.[48,47] The reaction can be summarized by four steps: (1) addition of water onto a cerium center of Ce_2O^- ; (2) hydride transfer from water into a bridging position between the two cerium atoms; (3) bond formation between hydroxide and the far cerium atom; and (4) evolution of H_2 . Importantly, the reaction profiles in Fig. 10 are based on calculations that implicitly treat scalar relativistic effects and ignore spin-orbit effects. These calculations predict energy gaps between 0.007 kcal/mol and 2.1 kcal/mol for the two lowest-energy pathways, which are related to one another by a single electron spin-flip. As such, both pathways are likely accessed due to the presence of the lanthanide centers that will provide spin-orbit coupling between

these two low-energy pathways.

The partially filled f-manifold in most lanthanide complexes lies close to the 5d and 6s orbitals of the lanthanide centers, yet it is non-bonding in nature and exhibits core-like behavior. Several studies have shown that the orbitals involved in chemical processes on lanthanides and lanthanide-based clusters involve 6s and 5p orbitals, while the occupation number of 4f orbitals remains intact.[69,70,47,71,72,46,76]. While the cerium-based 6s orbitals have been previously determined to be the sites of electron detachments in various cerium and cerium suboxide clusters (including Ce_2O^- and Ce_2O_2^-), we notice here that both σ and σ^* orbitals retain all or most of their electron occupations as the reaction proceeds. This shows that σ and σ^* electrons are not the source of metal facilitated reduction of water. Instead, the electron source in the studied reaction is the set of singly occupied 5d orbitals. This observation is consistent with the reported experimental result that reaction of Ce_2O_2^- with water yields H-radical rather than H_2 . The reaction of water with Ce_2O^- depletes the metal centers of their d electrons and prevents further H_2 production.[17].

There are features of the Ce_2O^- catalyzed reaction that are different from reports published for transition metal oxide cluster analogues. Three such examples include tungsten oxide, molybdenum oxide, and mixed manganese-molybdenum oxides.[77–80] The overall reaction barriers for those cases is similar to the case reported in this work, but a key difference lies in the mode of addition of water to the clusters. Indeed, previous reports found that the initial steps of water addition occur via a concerted step involving simultaneous addition of hydroxide (from water) to the metal center and O–H formation at an oxo site. As discussed above, our calculations identified a different pathway for the reaction with cerium oxide that occurs via a two-step process: water adds to the cerium center to form structures **G-2** and **G-4** (Fig. 5), then the hydrogen transfers to a bridging position between the two cerium centers.

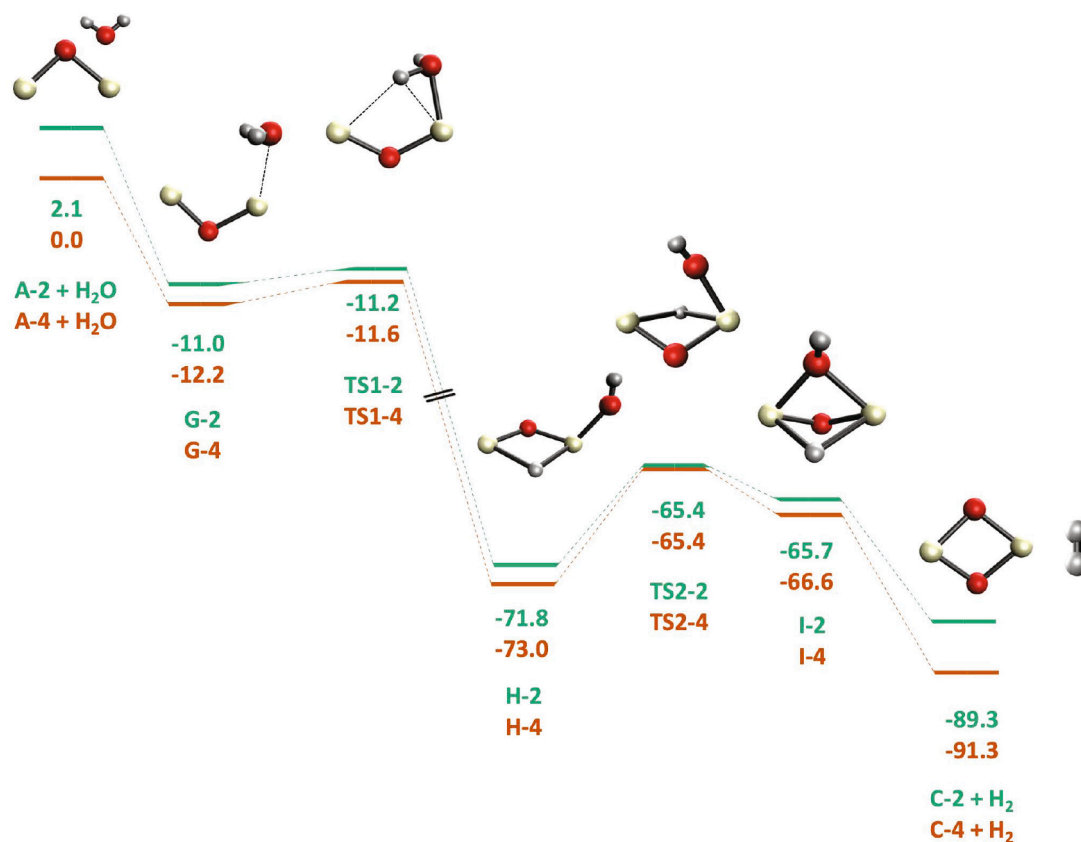


Fig. 10. Energy profile for the proposed $\text{Ce}_2\text{O}^- + \text{H}_2\text{O} \rightarrow \text{Ce}_2\text{O}_2^- + \text{H}_2$ quartet (orange) and doublet (green) mechanisms. Relative energies are presented in units of kcal/mol and are relative to **A-4** + H_2O . Cerium atoms are shown in gold, oxygen atoms are shown in red, and hydrogen atoms are shown in white.

In the reaction of Mn_xMo_y anions with water, both Mn and Mo are involved in the initial cluster-water formation.[80] However, only the Mo center undergoes oxidation. In fact, the reactivity of the Mn_xMo_y anion clusters with water depends on the oxidation state only of the molybdenum center. Once the Mo center reaches its highest oxidation state (VI), reaction with additional water molecules ends.

5. Conclusions

This work studied the reaction of water with Ce_2O^- clusters to produce Ce_2O_2^- and H_2 . Density functional theory calculations have been used to map out the full reaction pathway for hydrogen production. A thorough search for candidate intermediates and transition structures has shown that a key point in the progression of the reaction is the formation of successive bridging bonds that place the two hydrogen atoms in close proximity and eventually facilitates the production of H_2 . We have also shown that it is energetically possible for both experimentally identified electronic states of Ce_2O^- to react with water and eliminate molecular hydrogen with low energy barriers relative to the starting materials. Finally, while the valence molecular orbitals of the studied cerium oxide clusters consist of 4f, 5d, and 6s metal-centered orbitals, an examination of the molecular orbitals of initial and final cerium oxide clusters clearly indicates that the metal 5d electrons provide the means for water reduction. This work provides new insight to the reactivity of small lanthanide-based clusters with water.

The reaction studied in this work provides insight to key driving features of an important reaction catalyzed by lanthanide suboxide clusters. Interestingly, experimental results have shown that variations in the lanthanide to oxide ratios in Ce_xO_y anion clusters is a dictating factor in the mode of reactivity of these clusters with water.[17] While the effect of this ratio on the reactivity with water is still not fully understood, our analysis using a molecular orbital approach shows that the reaction of Ce_2O^- clusters is driven by delocalized 5d electrons. A similar feature has been observed in a recent study[69] in which we showed the significant role that lanthanide-based 5d orbitals play in the structure and bonding across the lanthanide hydroxide series. Studying cluster reactivity with varying ratios of lanthanides to oxides provides further understanding of the reactivity motifs of these clusters and insight for designing catalysts that can efficiently carry out efficient hydrogen gas production.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary material

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