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In situ, broadband measurement of the radio frequency attenuation length at Summit Station, Greenland

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Abstract

Over the last 25 years, radiowave detection of neutrino-generated signals, using cold polar ice as the neutrino target, has emerged as perhaps the most promising technique for detection of extragalactic ultra-high energy neutrinos (corresponding to neutrino energies in excess of 0.01 Joules, or 10¹⁷ electron volts). During the summer of 2021 and in tandem with the initial deployment of the Radio Neutrino Observatory in Greenland (RNO-G), we conducted radioglaciological measurements at Summit Station, Greenland to refine our understanding of the ice target. We report the result of one such measurement, the radio-frequency electric field attenuation length L_{α} . We find an approximately linear dependence of L_{α} on frequency with the best fit of the average field attenuation for the upper 1500 m of ice: $\langle L_{\alpha} \rangle = ((1154 \pm 121) - (0.81 \pm 0.14) (\nu/MHz))$ m for frequencies $\nu \in [145 - 350]$ MHz.

1. Introduction

We report a measurement of the radio frequency electric field attenuation length of deep glacial ice at the US National Science Foundation's Summit Station in Greenland. This measurement is of interest to the ultra-high energy neutrino (UHEN) community due to the development of the Radio Neutrino Observatory in Greenland (RNO-G), a particle astrophysics experiment that uses the ice as a target material in the search for astrophysical and cosmogenic neutrinos (Aguilar and others, 2021).

The IceCube experiment has placed a flux upper limit for astrophysical neutrinos of $E^2\phi \leq 2 \times 10^{-8} \text{ GeV}/(\text{cm}^2 \text{ s sr})$ at $E_{\nu} = 1 \text{ EeV}$ (Aartsen and others, 2018). At such fluxes, a particle detector requires an active volume of O (10 km³) or larger for a discovery-level detection within a detector's lifetime. A sparsely instrumented array of radio antennas, deployed in and on an extensive dielectric medium, can satisfy this volume requirement. An UHEN interaction creates an extensive electromagnetic shower that produces impulsive

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J. A. Aguilar and others

radio emission via the Askaryan effect (Askaryan, 1961). If the interaction occurs in an environment of low radio attenuation, a relatively small number of radio antennas can probe target volumes at the scale needed for UHEN observations.

Glacial ice has been measured to have long radio attenuation lengths due to low temperature and relatively high purity (Barwick and others, 2005; Besson and others, 2008; Barrella and other, 2011; Allison and others, 2012; Avva and others, 2015; Hanson and others, 2015). This, combined with the volume of glacial ice available in Greenland and Antarctica, makes polar ice sheets attractive sites for the construction of a radio neutrino detector.

RNO-G is one such experiment based on radio detection of UHEN in glacial ice (Aguilar and others, 2021), among others in Antarctica (Anker and others, 2019; Kravchenko and others, 2003; Gorham and others, 2009, 2019; Allison and others, 2012, 2020). RNO-G is being constructed near NSF's Summit Station at the highest point of the Greenland Ice Sheet. The planned detector will ultimately be composed of 35 autonomous stations separated by 1.25 km in a grid pattern. Each station is instrumented with radio antennas, with good response over the range 100–600 MHz, deployed both just below the surface and at depths down to 100 m in boreholes. Construction of the detector began during the summer of 2021 with the installation of the first three stations.

Previous measurements of radio attenuation lengths in Antarctica (Barwick and others, 2005; Besson and others, 2008; Barrella and other, 2011; Allison and others, 2012; Hanson and others, 2015) and Greenland (Paden and others, 2005; Avva and others, 2015; MacGregor and others, 2015) have demonstrated that radio attenuation lengths vary at different ice locations, due primarily to differences in ice temperature and impurity levels. Since electric field attenuation length is a primary determinant of the expected number of observed UHENs at energies greater than 1 EeV, a precise, *in situ* measurement is required at Summit Station to assess RNO-G's science potential.

Our work builds upon one previous *in situ* measurement of the bulk ice electric field attenuation length performed at Summit Station by Avva and others (2015); that effort reported a depth-averaged attenuation length $\langle L_{\alpha} \rangle = 947^{+92}_{-85}$ m at 75 MHz. We herein quantify the attenuation length at higher frequencies to better match RNO-G's frequency range of 100–600 MHz. In addition to that prior analysis, there have been several previous measurements of the radio ice properties at Summit Station, including radar attenuation length measurements from air-borne radio sounding in the Greenland Ice Sheet Project (MacGregor and others, 2015) and *in situ* radio sounding to investigate layering in the ice (Paden and others, 2005). We include a comparison of our reported attenuation with previous measurements at Summit Station and Antarctica in Section 4.8.

2. Experimental approach

Our approach is similar to previous work in the astro-particle physics field (Barwick and others, 2005; Besson and others, 2008; Barrella and other, 2011; Avva and others, 2015; Hanson and others, 2015).

We transmit an impulsive, broadband radio signal downwards into the ice via a wideband, directional antenna, and measure the return signal as a voltage versus time trace on a second, identical antenna. The transmitted signal propagates through the ice sheet, reflects off of the bedrock, and returns to the receiving antenna on the surface. After correcting for geometric path loss, bedrock coefficient of reflection and electric field amplification from the focusing effect of the firn, the remaining power loss is attributed to absorption and scattering in the ice. Note that, experimentally, we do not distinguish between the two – our quoted attenuation length implicitly includes both effects. (Possible dispersive effects at the bedrock are quantified in Section 4.2.) To reduce systematic uncertainties, we remove the system response of the electronics (initial impulse, antenna response, cables, amplifiers, filters) by normalizing against a second measurement run in air. We recreate the through-ice setup (same initial impulse, antenna polarization, cables, amplifiers and filters but additional attenuators) for two antennas transmitting over a short distance in air and thereby largely cancel dependence on the system response from the in-ice data run.

We take the reflection off the bedrock to be specular. Motivation for this decision is described in Section 4.2 below. Given a specular reflection, the radar range equation reduces to the Friis equation (Friis, 1946), and the direct through-air transmission formalism is applicable to our observed bedrock echoes. In that case, following the notation used by Avva and others (2015), the ratio of recorded voltages for each configuration (through-air vs. through-ice) as a function of frequency v is,

$$\frac{V_{\nu,\text{ice}}}{V_{\nu,\text{air}}} = \sqrt{F_f R} T_{\text{ratio}} \frac{d_{\text{air}}}{d_{\text{ice}}} \exp\left(-\frac{d_{\text{ice}}}{\langle L_\alpha \rangle}\right),\tag{1}$$

where d_{air} and d_{ice} are the distances the ice and air signals travel between antennas, *R* is the power reflection coefficient of the bedrock, *F*_f is a focusing factor from the changing index of refraction in the firm (Stockham and others, 2016; Stockham, 2018), *T*_{ratio} corrects for the change of transmission coefficient at the antenna feed between the antenna operating in air and in ice, and $\langle L_{\alpha} \rangle$ is the depth-averaged electric field attenuation length over the entire depth of the ice. Solving for the attenuation gives,

$$\langle L_{\alpha} \rangle = d_{\rm ice} / \ln \left(\sqrt{F_f R} T_{\rm ratio} \frac{V_{\nu, \rm air}}{V_{\nu, \rm ice}} \frac{d_{\rm air}}{d_{\rm ice}} \right). \tag{2}$$

This equation differs from that in Avva and others (2015) by the inclusion of the focusing factor, which arises from the amplification of field strength from propagation in the firn (Sodha and others, 1969). The addition of the focusing factor modifies the Avva and others (2015) bulk attenuation result from 947^{+92}_{-85} to 913_{-79}^{+85} m. We assume that the firn has an index of refraction varying linearly with the ice density profile $\rho(z)$ at Summit Station (Kovacs and others, 1995). The density profile has been experimentally measured (Alley and Koci, 1988; Alley and others, 1997; Hawley and others, 2008; Arthern and others, 2013) and fit to a double exponential (Deaconu and others, 2018), leading to a refractive index varying between $n \sim 1.4$ at the surface and $n \sim$ 1.78 in deep (<100 m) ice. The changing index of refraction focuses power from the transmitter on the downwards path, such that the Fresnel zone radius at the bedrock is reduced relative to the constant refractive index case. After reflection at the bedrock, the signal is partially de-focused on the return path, however the electric field areal flux density at the surface receiver is still amplified compared to the n = constant case. The focusing factor is equivalent to a correction to the expected $1/R^2$ geometric spread factor, mathematically formalized by Červený and others (1974). The focusing factor is present in MacGregor and others (2015), Matsuoka and others (2004), and Stockham and others (2016), among others. We have used the finite-different time domain electrodynamics simulation software MEEP (Oskooi and others, 2010) to confirm this effect.



Fig. 1. Diagram of experimental setup for bedrock reflection. On the transmitting side, we use a self-triggering FID Technologies +5 kV high voltage pulse generator connected to a buried log-periodic dipole antenna (LPDA); an AVTECH fast pulse generator triggered by the FID pulser is connected to an in-air LPDA. On the receiving side, both the buried downward-pointing, and the in-air LPDAs are connected to a +59 dB low noise amplifier; those outputs are then recorded on a Tektronix digital oscilloscope, triggered by the in-air signal.

3. Experimental setup

A system diagram of the experiment is presented in Figure 1. This measurement was performed in August 2021 at Summit Station, Greenland, using a separation distance of 244 m between the transmitter (coordinates 72.5801° N, 38.4569° W) and receiver (coordinates 72.5786° N, 38.4527° W) sites. The large separation distance assured that direct propagation from the transmitting antenna to the receiving antenna did not saturate the receiving amplifier. All antennas used were commercially available Create CLP-5130-2N (Creative Design Corp, 1994) log-periodic dipole antennas (LPDA) with ~8 dBi in-air forward gain over the band 105–1300 MHz.

Due to the large distance between stations, two parallel electronics signal chains are used, for triggering and the bedrock echo measurement, respectively. The bedrock echo electronics signal chain starts with the self-triggered high voltage FID Technology¹ model FPG6-1PNK pulse generator, which delivers a + 5 kV signal to a 50 Ω coaxial feed. After the FID output, we apply a 100 MHz high pass filter using a Minicircuits² NHP-100 filter. Following the filter, the signal is conveyed over $12\mbox{ m of LMR-400}$ 50Ω coaxial cable to an LPDA buried in the ice and pointed vertically downwards toward the bedrock; the bedrock-reflected return signal is then measured by a similarly-buried, downwards-pointing, receiver LPDA. The receiving antenna, located 244 m away along the surface of the ice, is aligned with the antenna tines parallel and collinear to the ones of the transmitting antenna, so that each antenna is in the gain null of the other to minimize contamination from horizontal ray paths. After measurement in the receiving antenna, the signal travels over a 10 m LMR-400 cable, bandpass filtered from 145-575 MHz using Minicircuits VHF-145+ and VLF-575+ filters, and then amplified by a custom RNO-G design low-noise amplifier with +59 dB of gain over the band 80-750 MHz. After

²https://www.minicircuits.com/products/RF-Filters.html

the amplifier, the signal is bandpass filtered again using Minicircuits NHP-200 and VLF-575 + filters, and then recorded on a 2 GHz-bandwidth Tektronix MSO5204B oscilloscope.

The oscilloscope is triggered by the second electronic signal chain, ensuring a stable trigger over the distance between transmitter and receiver. The second chain begins with an AVTECH AVIR-1-C pulse generator triggered by the FID pulse generator TRG OUT, producing an impulsive, O(1 ns) pulse. The pulse generator is connected over a 12 m LMR-400 cable to an elevated, in-air LPDA pointed at a similarly elevated receiver LPDA located 244 m away and viewing the transmitter on boresight. The received in-air signal is then attenuated by 20 dB to prevent saturation, bandpass filtered using Minicircuits VHF-145 + and VLF-575 + filters, amplified by + 59 dB using the RNO-G lownoise amplifier, bandpass filtered again using Minicircuits VHF-145 + and VLF-575 + filters and finally captured by the oscilloscope. This in-air signal was used to trigger the oscilloscope, and therefore provides the reference t_0 for our measurements.

The oscilloscope was set to collect data over a $50\,\mu s$ window; 10 000 individual triggers are averaged to suppress incoherent noise contributions and that average is written to scope memory. Twenty 10 000-event runs were collected, and then again averaged in post-processing, bringing the total number of triggers to 200 000.

To perform the air \rightarrow air normalization run, we swapped the cables for the in-ice antennas with those from the in-air antennas. On the receiving side, two modifications were made: we added a 46 dB attenuator to prevent amplifier saturation and, for this configuration, we self-triggered on the arriving signal.

4. Experimental results

4.1. Bedrock power reflection coefficient

The power reflection coefficient at the ice-rock interface is not well-known and constitutes the largest uncertainty in our measurement of attenuation length. Taking an approach similar to Avva and others (2015), we take the power reflection coefficient to have a mean value of 0.215, a typical value for ice-bedrock interfaces as derived from radio sounding experiments (Barwick and others, 2005; Christianson and others, 2016). For uncertainty analysis, we assume the reflection coefficient can be drawn from a probability density function, uniformly distributed in the log of the reflection coefficient over the range from 0.01 to 1.0, which represent plausible extrema for the interface, from a frozen bedrock with high water content to an underlying layer of water (Christianson and others, 2016).

The observed return echo, in principle, could include both coherent and also incoherent contributions. Whereas the former sum linearly with the number of average triggers, the latter will scale as the square root of the number of events averaged $N_{\rm avg}$ (Paden, 2006). We have explicitly verified that our final results are insensitive to $N_{\rm avg}$, consistent with the assumption that the observed specular return echo, after subtracting the contribution from noise, is dominated by coherent scattering.

4.2. Bedrock echo

The reflection from the bedrock is visible above thermal noise in the time domain voltage trace of the receiving antenna, at a signal onset time of $35.55 \,\mu s$ after the oscilloscope trigger (Fig. 2). The bedrock echo is observed to include two components: a predominantly-specular, sharp, faster impulse (of duration ~ 500 ns), and a long (> 2 μs) extended signal which we associate with more diffuse, multi-path reflections off irregular features, both on the surface of, and within, the underlying bed reflector. For the purposes of the

¹http://www.fidtechnology.com



Fig. 2. Top: Recorded voltage as a function of time for the receiving in-ice antenna. Bottom: Recorded power, integrated in a sliding window of 100 ns to account for the group delay of the LPDA antennas. The specular component of the bedrock echo 'signal' is highlighted in magenta. Sub-surface internal layer reflections are visible at times earlier than 22 µs, after which noise dominates up to the point at which the bedrock echo is evident.

bulk radio attenuation measurement, and since an extended tail is not present for the in-air normalization run, we restrict consideration to the fast, specular component.

The uncertainty in the time window of the specular reflection is of O(10 ns), dominated by noise fluctuations at the edges of the window. This uncertainty is neglected since it is sub-dominant relative to the other systematic uncertainties in our final measurement. The final window start and end times are therefore defined to be 35.55 and 36.05 μ s, respectively.

To determine the impact of neglecting the diffuse component of the bedrock echo on our final measured value of bulk attenuation, we investigate the dependence of our numerical result on the window length used in our analysis. We expect the measured attenuation to increase with increased window length due to the extended integration of power returning from the bedrock; at frequencies below 250 MHz, we obtain a \sim 10% larger attenuation length, but with increased uncertainty, as seen in Figure 3. At frequencies above 250 MHz, there is a negligible increase in



Fig. 3. Measurement of the depth-averaged electric field attenuation at 200 MHz as a function of the window length used to select the bedrock echo. We note that including the entire diffuse component of the reflection into the final attenuation calculation increases the final result by no more than 10%.

attenuation length with increased window length. We note that the additional attenuation length is within the systematic uncertainties of our stated result due to the large bedrock reflection coefficient uncertainty.

The relationship between bulk ice attenuation and received power is different for the specular vs. diffuse components. We define attenuation from the Friis transmission equation (implicit in Eqn (1)) (Friis, 1946). The Friis transmission equation is applicable for a specular reflection as it assumes direct line-of-sight propagation without interference within the first Fresnel zone, leading to a geometric path loss $\propto d_{ice}^2$. The radar range equation is more applicable to the diffuse component since it includes power contributions from a rough surface via the definition of a radar cross-section and a geometric path loss $\propto (d_{\rm ice}/2)^4$ (Balanis, 2016). We find that use of the radar range equation instead of the Friis equation over the combined specular and diffuse components also increases the measured attenuation length at lower frequencies by a maximum of 10%, albeit introducing more model dependence from the unknown value of bedrock radar cross-section.

Based on the relatively small increase in obtained attenuation length from including the diffuse component, we quote our final result based on the Friis equation; this choice is consistent with previous similar measurements (Paden and others, 2005; Barwick and others, 2005; Besson and others, 2008; Barrella and other, 2011; Hanson and others, 2015; Avva and others, 2015).

4.3. Bedrock depth

The bedrock depth can be derived from the absolute time of flight of the transmitted pulse and a model for the index of refraction of the ice as a function of depth. To reduce systematic biases (from location extrapolation and bedrock radio properties) and also as a cross check of our absolute timing calibration, we measure the bedrock depth from these data, rather than relying on previous measurements. The relationship between time of flight (Δt) and bedrock depth (half of the total distance propagated by the transmitted signal, d_{ice}) can be found by solving for d_{ice} in the integral:

$$\Delta t = \frac{2}{c} \int_0^{a_{\rm ice}/2} n(z) dz, \qquad (3)$$

where n(z) is the model for the index of refraction as a function of depth [m]. Index of refraction is related to dielectric constant (ϵ') via $n(z) = \sqrt{\epsilon'(z)}$. The value of $\epsilon'(z)$ is derived from its relationship with measured ice density (ρ ,[kg/m³]) (Kovacs and others, 1995; Barwick and others, 2018):

$$\epsilon'(z) = (1 + 0.854\rho(z))^2.$$
(4)

The parameterization of the dependence of ice density on depth follows Deaconu and others (2018), who performed a double exponential fit with a critical density at a depth of 14.9 m (Herron and Langway, 1980):

$$\rho(z) = \begin{cases} 0.917 - 0.594e^{-z/30.8} & z \le 14.9 \,\mathrm{m} \\ 0.917 - 0.367e^{-(z-14.9)/40.5} & z > 14.9 \,\mathrm{m} \end{cases}$$
(5)

The uncertainty on the depth determination arises primarily from the uncertainty in the asymptotic index of refraction of deep glacial ice, which we take to be $n = 1.78 \pm 0.03$ (Bogorodsky and others, 1985) for ice below the firn (deeper than 100 m at Summit Station). Using this refractive index profile, we calculate the bedrock to be at a depth of 3004^{+50}_{-52} m, corresponding to $d_{ice} = 6008^{+100}_{-104}$ m for the through-ice bedrock echo total travel distance.

We note that, while our transmitting and receiving antennas were separated by 244 m, the through-ice signal approximately propagates vertically and Eqn (3) holds true. Over the measured 6 km propagation distance, horizontal propagation results in 4 m extra path length.

This bedrock depth is consistent with previous measurements of the bedrock depth from Greenland Ice Core Project (1994), at 3053.5 in 1993, and from Avva and others (2015), at 3014^{+48}_{-50} m in 2015.

4.4. Antenna coupling

The antenna transmission coefficient is defined as the quantity of power transmitted by the antenna from an incident radio frequency signal on a 50 Ω transmission line at the antenna feed point (S₂₁ in the scattering matrix). The transmission coefficient depends upon the dielectric properties of the antenna's embedded environment (Barwick and others, 2015; Glaser and others, 2019). To increase the power transmitted into the ice, we buried our antennas so that all active conductors were at least $\sim 20 \text{ cm}$ below the surface, thereby embedding them in an environment of $n \approx 1.4$. The antennas used for the normalization are in air, for which $n \sim 1.0$. To correct for the change in match, we calculate a T_{ratio} from the measured reflection coefficient (S₁₁ as shown in Figure 4) of the four antennas, two in air and two in ice, taken in the field. Assuming that all power not reflected at the feed is transmitted, the ratio becomes, in terms of the reflection coefficient S_{11} in dB,

$$T_{\text{ratio}} = \frac{1 - 10^{S_{11,\text{ice}}/10}}{1 - 10^{S_{11,\text{air}}/10}}.$$
 (6)

The antennas were found to transmit nearly all incident power in the frequency range of interest (150–550 MHz) in both the in-air and in-ice cases, resulting in a small $T_{\rm ratio}$ correction. Averaged over frequency in the range of interest, $T_{\rm ratio} = 1.00 \pm 0.05$, with the uncertainty assessed empirically from the variance of the measured match over the band. Our result is consistent with $T_{\rm ratio}$ measured by other groups using the same or similar antennas (Barrella and other, 2011; Avva and others, 2015).



Fig. 4. Measured S_{11} of each antenna used in the experiment. The difference in the low-frequency cutoff of the antenna when it is embedded in the ice compared to in air is due to the different indices of refraction of the two environments.

In situ measurements, as well as simulations (Barwick and others, 2015; Glaser and others, 2019), have shown that the frequency-dependent antenna gain G_0 , measured in air, also changes when the antenna is embedded in a dielectric medium. This change can be modeled as a down-shift in frequency, by the index of refraction of the medium ($G'(v) = G_0(v/n)$). For the LPDA used in this work, the gain over the frequency band of interest is uniform to < 0.5 dBi (Creative Design Corp, 1994), rendering the shift between in-air and in-ice measurements a subdominant systematic bias. The down-shift in frequency will cause a corresponding shift in low-frequency cutoff both in the gain and in the S_{11} (as shown in Fig. 4), but the cutoff in both environments is below the high-pass filter of our analysis.

We note that there will be different contributions from the ice surface in both the in-air and in-ice antenna responses. We neglect these effects because they are likely to be small so long as the directional antennas (front-to-back [F/B] ratio of the LPDA \sim -15 dB) are pointed away from the surface (Barwick and others, 2015).

4.5. Firn focusing

There is a geometric amplification of the bedrock echo electric field at the surface of the ice due to the changing index of refraction of the firn. To calculate the power focusing factor, for a negligibly thin firn layer, straightforward application of Snell's law prescribes that the electric field flux density measured at the surface, after bedrock reflection, follows (Stockham and others, 2016):

$$F_{\rm f} = \left(\frac{n(z=0)}{n(z=d_{\rm ice}/2)}\right)^2.$$
 (7)

We have verified that this equation agrees with a ray tracing simulation and 3D FDTD simulation. The uncertainty on the focusing factor arises from the uncertainty in the index of refraction model. Using $n = 1.78 \pm 0.03$ (Bogorodsky and others, 1985) (as described previously in Section 4.3), and $n = 1.4 \pm 0.1$ for the surface ice (Bogorodsky and others, 1985), we obtain a final focusing factor of $F_{\rm f} = 1.61 \pm 0.24$.

4.6. In-air normalization amplitude

The amplitude of the signal from the in-air normalization run can be systematically biased from reflections off of the ice surface, -45

-50

-55



Data

xFDTD Simulation

WIPL-D Simulation

absolute amplitude expectation as derived from two separate LPDA simulations. No systematic bias is evident within the ±10% voltage uncertainty in the antenna model (Barwick and others, 2015, 2017), over the frequency band of this analysis. The sharp dip between 180 and 220 MHz seen in data and simulations is most likely due to fine details in tine length and separation, which may be difficult to accurately simulate (Barwick and others, 2017).

increasing or decreasing the recorded power observed from the direct line-of-sight signal. Given the antenna heights above the ice (1.5 m) and distance between antennas (244 m), the first Fresnel zone is comprised by a nearly uniform, planar surface ice reflector, at all frequencies of interest. This leads to potential interference from reflections, depending on geometry: direct rays will interfere destructively/constructively with rays at the center/periphery of the Fresnel zone. To quantify any possible systematic bias, we compare the data against the absolute amplitude expectation of the signal from simulation. The absolute amplitude is derived from a measurement of the FID pulse shape, amplifier response, filter response, free space path loss and two independent simulations of the LPDA antenna response. Our simulations use either the Method of Moments software WIPL- D^3 or Finite Difference Time Domain software xFDTD⁴, and have been found to agree with anechoic chamber measurements to 10% uncertainty (Barwick and others, 2017, 2015). The comparison of the simulated result with our data, seen in Figure 5, demonstrates that any possible systematic bias is not greater than 10% in voltage, consistent with previous results (Barwick and others, 2017, 2015).

4.7. Result and error analysis

The measured depth-averaged field attenuation length is presented in Figure 6. The previous in situ measurement reported by Avva and others (2015) is included for comparison, adjusted to remove the systematic bias from firn focusing not previously included in that analysis, resulting in a correction of their published result (from 947^{+92}_{-85} to 913^{+85}_{-79} m). We report the measurement only within the bandpass limits of our system, over which we have the highest sensitivity and lowest systematic biases from antenna modeling and filter response. Beyond the system bandpass limits, we have checked that our procedure yields an attenuation length numerically consistent with zero as expected for a noise-dominated regime.

Contributions of different sources of uncertainty are calculated using a Monte Carlo method. We numerically calculate the

³https://wipl-d.com ⁴https://www.remcom.com/xfdtd-3d-em-simulation-software



Fig. 6. Measurement of the depth-averaged electric field attenuation as a function of frequency at Summit Station, within the system bandpass (shown as red dashed lines). Definitions of the error bars (and displayed upper limits) are provided in the text. The corrected result from Avva and others (2015) is shown for comparison. The frequency v in the fit has units of MHz.

estimated probability density distribution (PDF) of the bulk electric field attenuation within each frequency bin by repeatedly drawing random values of each component of the final measurement from their respective PDFs. For systematic uncertainties, we assume that each measured quantity used in the calculation of bulk field attenuation is uncorrelated and has a PDF either of a normal distribution (as is the case for $F_{f_{f}}$ T_{ratio} and d_{ice}) or the distribution already described in the text (as is the case for R). The main component of statistical uncertainty is due to fluctuations in the power contributions from thermal noise in the recorded oscilloscope trace. In the 150-300 MHz band, the uncertainty from noise statistical fluctuation is sub-dominant to systematic uncertainties, contributing less than 10% to the quoted uncertainty of each frequency bin. The final measurement is reported as a central value with one standard deviation (statistical plus systematic) error bars for those frequency bins that yield statistically significant results. For all other frequency bins, we report a 95% confidence level upper limit.

It is important to note that the majority of uncertainties are correlated in each frequency bin of the final measurement, with the primary contributions to the uncertainty arising from finite noise statistics and small systematic biases from the difference in LPDA response in ice vs. air. For the linear fit presented below, the visibly high goodness of fit is due to this correlation of uncertainties between frequency bins.

The reported bulk attenuation length includes losses from layer scattering. While expected to be a subdominant effect for vertical propagation due to the low reflection coefficient of the observed layers (Paden and others, 2005), quantifying effects due to layer scattering for the more horizontal neutrino geometries must account for the larger Fresnel reflection coefficients at more glancing layer incidence angles (Aguilar and others, 2022).

Birefringence of the ice can result in rotation of the signal that is dependent on polarization, leading to apparent loss of power at the co-polarized receiver. Measurements of the crystal orientation at Summit Station indicate uniaxial fabric at all depths (Thorsteinsson, 1996), unlike South Pole (Matsuoka and others, 2003; Barwick and others, 2005), indicating that birefringence will matter less for the Greenland site, though this remains to be quantified.

4.8. Discussion and summary

We derive the electric field attenuation length as a function of depth using a model of the field attenuation's dependence on

temperature and chemical impurities, as described in detail in MacGregor and others (2007), MacGregor and others (2015) and Wolff and others (1997). For a medium with non-zero intrinsic conductivity, the attenuation length can be expressed as:

$$L_{\alpha}(f,z) = A(f) \frac{\epsilon_0 \sqrt{\epsilon'_r(z)}c}{\sigma_{\infty}(z)},$$
(8)

where c is the speed of light, ϵ_0 is the permittivity of free space, $\epsilon'_r(z)$ is the real component of the relative permittivity at a given depth z (defined in Eqn (4)), $\sigma_{\infty}(z)$ is the infinite frequency limit of the electrical conductivity at a given depth, and the parameter A(f) is extracted experimentally, by requiring that the integrated, depth-dependent attenuation match our measured value of full-path attenuation, at each frequency *f*. Fujita and others (2000) suggest that the infinite frequency limit conductivity is valid at radio frequencies, since the molar conductivity does not change from low frequency (the frequency at which reference conductivity was measured, 0.3–3 MHz (Wolff and others, 1997)) to our frequency band (VHF/UHF, 150-550 MHz). The infinity frequency conductivity is related to chemical impurities and temperature via,

$$\sigma_{\infty}(z) = \sigma_{\text{pure}} \exp\left[\frac{E_{\text{pure}}}{k} \left(\frac{1}{T_{\text{r}}} - \frac{1}{T(z)}\right)\right] + \mu_{\text{H}^{+}}[\text{H}^{+}](z) \exp\left[\frac{E_{\text{H}^{+}}}{k} \left(\frac{1}{T_{\text{r}}} - \frac{1}{T(z)}\right)\right] + \mu_{\text{CI}^{-}}[\text{CI}^{-}](z) \exp\left[\frac{E_{\text{CI}^{-}}}{k} \left(\frac{1}{T_{\text{r}}} - \frac{1}{T(z)}\right)\right] + \mu_{\text{NH}_{4}^{+}}[\text{NH}_{4}^{+}](z) \exp\left[\frac{E_{\text{NH}_{4}^{+}}}{k} \left(\frac{1}{T_{\text{r}}} - \frac{1}{T(z)}\right)\right],$$
(9)

where k is Boltzmann's constant, T(z) is in-ice temperature at a given depth as measured at the GRIP borehole Greenland Ice Core Project (1994)⁵, T_r is a reference temperature, σ_{pure} is the conductivity of pure ice, μ_{H^+} , μ_{Cl^-} and $\mu_{\mathrm{NH}^+_4}$ are molar conductivities, E_{pure} , E_{H^+} , E_{Cl^-} and $E_{\text{NH}_4^+}$ are activation energies, and [H⁺] $(z)^6$, $[Cl^-](z)^7$ and $[NH_4^+](z)^7$ are depth-dependent molar concentrations as measured at the GRIP borehole (Legrand and others, 1993; Greenland Ice Core Project, 1994; Wolff and others, 1995). The values of molar conductivities, conductivity of free ice and activation energies as measured by MacGregor and others (2007) and MacGregor and others (2015) and used in this analysis are given in Table 1. Note that, in this formulation, the temperature dependence of the attenuation length is explicitly absorbed into the conductivity dependence on temperature - the zero conductivity limit would correspond to no absorption and, correspondingly, no attenuation, for any temperature.

Using the model of electric field attenuation length as a function of depth, we then unfold and solve for the parameter A(f), requiring that the depth-integrated attenuation matches our measured depth-averaged attenuation. The result reported at 300 MHz is plotted in Figure 7. We note a conspicuous enhancement in the $L_{\alpha}(z)$ profile at depth \geq 1600 m; this feature tracks a similarly precipitous drop in the tabulated GRIP H^+ and NH_4^+ molar concentrations at $z \sim 1600$ m, resulting in a corresponding enhanced radio-frequency transparency at those depths.

Table 1. Values of parameters used in the conductivity model of ice at summit station.

Symbol	Description	Unit	Value
T _r	Reference temperature	°C	-21
$\sigma_{\rm pure}$	Conductivity of pure ice	μS/m	9.2 ± 0.2
μ_{H^+}	Molar conductivity of H ⁺	S/m/M	3.2 ± 0.2
μ_{Cl^-}	Molar conductivity of Cl ⁻	S/m/M	0.43 ± 0.07
$\mu_{\rm NH^+}$	Molar conductivity of NH ⁺	S/m/M	0.8
Epure	Activation energy of pure ice	eV	0.51 ± 0.01
E _H +	Activation energy of H ⁺	eV	0.20 ± 0.04
E _{Cl} -	Activation energy of Cl ⁻	eV	0.19 ± 0.02
E _{NH⁺}	Activation energy of NH ⁺	eV	0.23
T(z) ^₄	Ice temperature at depth z	°C	See 5
$[H^{+}](z)$	Molar concentration of H ⁺	μM	See 6
$[Cl^{-}](z)$	Molar concentration of Cl ⁻	μM	See 7
[NH ₄ ⁺](z)	Molar concentration of NH_4^+	μM	See 7

Compiled from MacGregor and others (2007) and MacGregor and others (2015) and from the GRIP borehole (Greenland Ice Core Project, 1994). Molar concentrations and ice temperature are tables of data measured at the GRIP borehole, and are available at the corresponding links in the footnotes.



Fig. 7. Electric field attenuation length as a function of depth at 300 MHz as derived from the two models of ice attenuation, one derived from temperature and chemical impurities (MacGregor and others, 2007, 2015) (black) and another from temperature alone (Bogorodsky and others, 1985)(red). Hatched and filled regions denote $\pm 1\sigma$.

Avva and others (2015) derived the electric field attenuation length as a function of depth using a simplified model of the field attenuation dependence on temperature alone. They assume a linear relationship between the log of the attenuation versus the temperature of the ice:

$$L_{\alpha}(f, T(z)) = A(f) \cdot 10^{mT(z)}.$$
 (10)

The parameter *m* is taken to be the average of the two sites measured by Bogorodsky and others (1985) and set equal to -0.017 (° *C*)⁻¹. The parameter A(f) is derived from measured value of bulk field attenuation at each frequency *f* and set equal to 200–280 m. For comparison, our result using the simplified model as reported at 300 MHz is plotted in Figure 7.

The average electric field attenuation length of the top 1500 m of ice is of particular interest to RNO-G as the majority of neutrino interactions detectable by the experiment occur in this region (Aguilar and others, 2022). It can be extracted from the bulk result using the field attenuation versus depth relation defined by MacGregor and others (2007) and MacGregor and others (2015). The average field attenuation length for the top 1500 m of ice result is shown in Figure 8. For reference, the bulk attenuation measurement at 300 MHz is 756^{+71}_{-87} m

⁵ftp://ftp.ncdc.noaa.gov/pub/data/paleo/icecore/greenland/summit/grip/physical/ griptemp.txt

⁶ftp://ftp.ncdc.noaa.gov/pub/data/paleo/icecore/greenland/summit/grip/ecm/gripdep.txt

⁷ftp://ftp.ncdc.noaa.gov/pub/data/paleo/icecore/greenland/summit/grip/chem/gripion.txt



Fig. 8. Measurement of the average electric field attenuation for the top 1500 m of the ice sheet, as a function of frequency at Summit Station, derived from the measured bulk field attenuation in Figure 6 and the relationship between attenuation and temperature. Overlaid is the $\pm 1\sigma$ confidence interval of a linear fit of the data. Parameters of the fit are described in the text. Frequency v in the fit is in units of MHz.

 $(-11.49^{+1.49}_{-0.99} \text{ dB/km})$ while the average attenuation measurement of the top 1500 m of ice is 926^{+107}_{-124} m $(-9.38^{+1.45}_{-0.97} \text{ dB/km})$.

Our measurement can be used in simulations that calculate RNO-G's sensitivity to astrophysical neutrinos. For those simulations, we include, for convenience, a linear fit to the average electric field attenuation length for the top 1500 m of ice, shown in Figure 8. We find a significant correlation between the two parameters of the linear fit, which yields a slope of -0.81 ± 0.14 m/MHz (-0.12 ± 0.02 dB/km/MHz), intercept of 1154 ± 121 m (-7.53 ± 0.72 dB/km), and a correlation coefficient $\rho = -0.95$.

We compare our obtained result of the average electric field attenuation length for the top 1500 m at 300 MHz of 926^{+107}_{-124} m to other similar measurements. Avva and others (2015) extrapolated their results at 75–300 MHz and estimated $\langle L_{\alpha} \rangle = 1022^{+230}_{-253}$ m, consistent (within uncertainty) with the result presented herein. The electric field attenuation length at the South Pole has been measured, with the focusing factor included, to be $\langle L_{\alpha} \rangle = 1660^{+255}_{-120} \text{ m}$ at 300 MHz for the top 1500 m of ice (Allison and others, 2012), a factor 1.8 times longer than our measurement. A linear fit to the log of attenuation length versus temperature (only) from Bogorodsky and others (1985), 20°C colder ice yields an expected attenuation length ~ 2.2 times longer at South Pole than at Summit, however, the higher concentration of Cl⁻ at South Pole (~4 μ M (MacGregor and others, 2007) compared to ~0.5 μ M at Summit Station in the top 1500 m of ice) moderates this expectation.

Measurements of the bulk radio field attenuation length at Summit Station have also been performed using air-borne radio sounding data. MacGregor and others (2015) inferred the bulk radio field attenuation by comparing the relative strengths of internal reflectors, obtaining attenuation lengths of 750–850 m at 150–200 MHz around Summit Station, consistent (within uncertainty) with the result presented herein. Stockham and others (2016) measured the bulk radio field attenuation using the relative strength of the radio echo from the snow surface and the bedrock, obtaining at an attenuation length of 546 ± 23 m at 150-200 MHz around Summit Station. This measurement is notably lower than our result and the measurement done by MacGregor and others (2015) potentially due to radiometric calibration issues (MacGregor and others, 2015; Stockham and others, 2016).

The RNO-G experiment, currently under construction at Summit Station in Greenland, is set to be one of the world's largest particle detectors. Our measurement of the bulk electric field attenuation length at Summit Station is consistent with previous measurements, with reduced systematic uncertainties. Our measurement will ultimately increase the precision of RNO-G's UHEN sensitivity estimates, which will either better motivate upper limits in the case of a null result or decrease uncertainties on the measured flux of ultra-high energy neutrinos in the universe in the case of observation.

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References

- Aartsen MG and 52 others (2018) Differential limit on the extremely-high-energy cosmic neutrino flux in the presence of astrophysical background from nine years of IceCube data. *Physical Review D* 98(6), 062003. doi: 10.1103/PhysRevD.98.062003
- Aguilar JA and 54 others (2021) Design and sensitivity of the Radio Neutrino Observatory in Greenland (RNO-G). JINST 16(03), P03025. doi: 10.1088/ 1748-0221/16/03/P03025
- Aguilar JA and 57 others (2022) Reconstructing the neutrino energy for in-ice radio detectors: a study for the Radio Neutrino Observatory Greenland (RNO-G). *The European Physical Journal C* 82(2), 147. doi: 10.1140/epjc/s10052-022-10034-4
- Alley R and 11 others (1997) Visual-stratigraphic dating of the GISP2 ice core: basis, reproducibility, and application. *Journal of Geophysical Research: Oceans* **102**(C12), 26367–26381. doi: 10.1029/96JC03837
- Alley R and Koci B (1988) Ice-core analysis at Site A, Greenland: preliminary results. Annals of Glaciology 10, 1–4. doi: 10.3189/S0260305500004067
- Allison P and 46 others (2012) Design and initial performance of the Askaryan radio array prototype EeV neutrino detector at the South Pole. Astroparticle Physics 35, 457–477. doi: 10.1016/j.astropartphys.2011.11.010
- Allison P and 72 others (2020) Constraints on the diffuse flux of ultrahigh energy neutrinos from four years of Askaryan Radio Array data in two stations. *Physical Review D* 102(4), 043021. doi: 10.1103/PhysRevD.102.043021
- Anker A and 23 others (2019) Targeting ultra-high energy neutrinos with the ARIANNA experiment. Advances in Space Research 64, 2595–2609. doi: 10. 1016/j.asr.2019.06.016
- Arthern RJ, Corr HFJ, Gillet-Chaulet F, Hawley RL and Morris EM (2013) Inversion for the density-depth profile of polar firn using a steppedfrequency radar. *Journal of Geophysical Research (Earth Surface)* 118(3), 1257–1263. doi: 10.1002/jgrf.20089
- Askaryan GA (1961) Excess negative charge of an electron-photon shower and the coherent radio emission from it. *Soviet Physics JETP* **41**, 616–618.
- Avva J, Kovac JM, Miki C, Saltzberg D and Vieregg AG (2015) An in situ measurement of the radio-frequency attenuation in ice at Summit Station, Greenland. *Journal of Glaciology* 61, 1005–1011. doi: 10.3189/ 2015JoG15J057
- **Balanis CA** (2016) *Antenna Theory: Analysis and Design*, 4th ed. Hoboken, New Jersey: Wiley Interscience.
- Barrella T, Barwick S and Saltzberg D (2011) Ross Ice Shelf (Antarctica) in situ radio-frequency attenuation. *Journal of Glaciology* 57(201), 61–66. doi: 10.3189/002214311795306691
- Barwick SW, Besson DZ, Gorham PW and Saltzberg DP (2005) South Polar in situ radio-frequency ice attenuation. *Journal of Glaciology* **51**(173), 231– 238. doi: 10.3189/172756505781829467
- Barwick SW and 15 others (2015) Time domain response of the ARIANNA detector. Astroparticle Physics 62, 139–151. doi: 10.1016/j.astropartphys. 2014.09.002

- Barwick SW and 18 others (2017) Radio detection of air showers with the ARIANNA experiment on the Ross Ice Shelf. *Astroparticle Physics* **90**, 50–68. doi: 10.1016/j.astropartphys.2017.02.003
- Barwick SW and 18 others (2018) Observation of classically 'forbidden' electromagnetic wave propagation and implications for neutrino detection. *JCAP* 07, 055. doi: 10.1088/1475-7516/2018/07/055
- Besson DZ and 42 others (2008) In situ radioglaciological measurements near Taylor Dome, Antarctica and implications for ultra-high energy (UHE) neutrino astronomy. *Astroparticle Physics* **29**(2), 130–157. doi: 10.1016/j. astropartphys.2007.12.004.
- Bogorodsky VV, Bentley CR and Gudmandsen PE (1985) Radioglaciology. Dordrecht, Holland: Reidel Publishing Co.
- Červený V, Langer J and Pšenčík I (1974) Computation of geometric spreading of seismic body waves in laterally inhomogeneous media with curved interfaces. *Geophysical Journal International* 38(1), 9–19. doi: 10.1111/j. 1365-246X.1974.tb04105.x
- Christianson K and 6 others (2016) Basal conditions at the grounding zone of Whillans Ice Stream, West Antarctica, from ice-penetrating radar. Journal of Geophysical Research: Earth Surface 121(11), 1954–1983. doi: 10.1002/ 2015JF003806
- Creative Design Corp (1994) Instruction Manual CLP5130-2 Create Radio Antenna.
- Deaconu C and 8 others (2018) Measurements and modeling of near-surface radio propagation in glacial ice and implications for neutrino experiments. *Physical Review D* 98(4), 043010. doi: 10.1103/PhysRevD.98.043010
- Friis H (1946) A note on a simple transmission formula. Proceedings of the IRE 34(5), 254–256. doi: 10.1109/JRPROC.1946.234568
- Fujita S, Matsuoka T, Ishida T, Matsuoka K and Mae S (2000) A summary of the complex dielectric permittivity of ice in the megahertz range and its applications for radar sounding of polar ice sheets. In *Physics of ice core records*, Hokkaido University Press, pp. 185–212.
- Glaser C and 8 others (2019) NuRadioReco: a reconstruction framework for radio neutrino detectors. *The European Physical Journal C* 79(6), 29. doi: 10.1140/epjc/s10052-019-6971-5.
- Gorham PW and 42 others (2009) The Antarctic impulsive transient antenna ultra-high energy neutrino detector design, performance, and sensitivity for 2006–2007 balloon flight. *Astroparticle Physics* **32**, 10–41. doi: 10.1016/j. astropartphys.2009.05.003
- Gorham PW and 59 others (2019) Constraints on the ultrahigh-energy cosmic neutrino flux from the fourth flight of ANITA. *Physical Review D* 99(12), 122001. doi: 10.1103/PhysRevD.99.122001
- Greenland Ice Core Project (1994) ftp://ftp.ncdc.noaa.gov/pub/data/paleo/icecore/greenland/summit/grip/.
- Hanson JC and 13 others (2015) Radar absorption, basal reflection, thickness and polarization measurements from the Ross Ice Shelf, Antarctica. *Journal* of Glaciology 61(227), 438–446. doi: 10.3189/2015JoG14J214
- Hawley RL, Morris EM and McConnell JR (2008) Rapid techniques for determining annual accumulation applied at Summit, Greenland. *Journal* of Glaciology 54(188), 839–845. doi: 10.3189/002214308787779951
- Herron MM and Langway CC (1980) Firn densification: an empirical model. Journal of Glaciology 25(93), 373–385. doi: 10.3189/S0022143000015239

- Kovacs A, Gow AJ and Morey RM (1995) The in-situ dielectric constant of polar firn revisited. *Cold Regions Science and Technology* 23(3), 245–256. doi: 10.1016/0165-232X(94)00016-Q
- Kravchenko I and 14 others (2003) Performance and simulation of the RICE detector. Astroparticle Physics 19, 15–36. doi: 10.1016/S0927-6505(02)00194-9
- Legrand M, De Angelis M and Maupetit F (1993) Field investigation of major and minor ions along summit (central greenland) ice cores by ion chromatography. *Journal of Chromatography A* 640(1), 251–258. doi: 10.1016/ 0021-9673(93)80188-E
- MacGregor JA and 5 others (2007) Modeling englacial radar attenuation at Siple Dome, West Antarctica, using ice chemistry and temperature data. *Journal of Geophysical Research: Earth Surface* 112(F3), 1–6. doi: 10.1029/ 2006JF000717.
- MacGregor JA and 11 others (2015) Radar attenuation and temperature within the Greenland Ice Sheet. *Journal of Geophysical Research: Earth Surface* **120**(6), 983–1008. doi: 10.1002/2014JF003418
- Matsuoka K and 6 others (2003) Crystal orientation fabrics within the Antarctic ice sheet revealed by a multipolarization plane and dual-frequency radar survey. *Journal of Geophysical Research* **108**, 2499. doi: 10.1029/2003JB002425
- Matsuoka K, Uratsuka S, Fujita S and Nishio F (2004) Ice-flow-induced scattering zone within the antarctic ice sheet revealed by high-frequency airborne radar. *Journal of Glaciology* 50(170), 382–388. doi: 10.3189/ 172756504781829891
- Oskooi AF and others (2010) Meep: a flexible free-software package for electromagnetic simulations by the FDTD method. *Computer Physics Communications* 181(3), 687–702. doi: 10.1016/j.cpc.2009.11.008
- Paden J (2006) Synthetic aperture radar for imaging the basal conditions of the polar ice sheets. Ph.D. thesis, Department of Electrical Engineering and Computer Science, University of Kansas, Lawrence, Kansas.
- Paden J and 5 others (2005) Wideband measurements of ice sheet attenuation and basal scattering. *IEEE Geoscience and Remote Sensing Letters* 2(2), 164– 168. doi: 10.1109/LGRS.2004.842474
- Sodha MS, Sirohi RS and Chakravarti AK (1969) Focusing factor in a stratified medium. British Journal of Applied Physics 2(2), 1457–1461. doi: 10. 1088/0022-3727/2/4/317.
- Stockham M (2018) Bulk and surface radio-frequency response of ice. Ph.D. thesis, University of Kansas, Lawrence, Kansas.
- Stockham M, Macy J and Besson DZ (2016) Radio frequency ice dielectric permittivity measurements using CReSIS data. *Radio Science* 51, 194–212. doi: 10.1002/2015RS005849
- Thorsteinsson T (1996) Textures and fabrics in the GRIP ice core, in relation to climate history and ice deformation. *Berichte zur Polarforschung (Reports* on Polar Research), 205, 52–71. doi: 10.1029/97JC00161.
- Wolff EW and 5 others (1995) Long-term changes in the acid and salt concentrations of the Greenland ice core project ice core from electrical stratigraphy. *Journal of Geophysical Research: Atmospheres* 100(D8), 16249– 16263. doi: 10.1029/95JD01174
- Wolff EW, Miners WD, Moore JC and Paren JG (1997) Factors controlling the electrical conductivity of ice from the polar regionsa summary. *The Journal of Physical Chemistry B* 101(32), 6090–6094. doi: 10.1021/jp9631543