

Anisotropy and Modal Hybridization in Infrared Nanophotonics Using Low-Symmetry Materials

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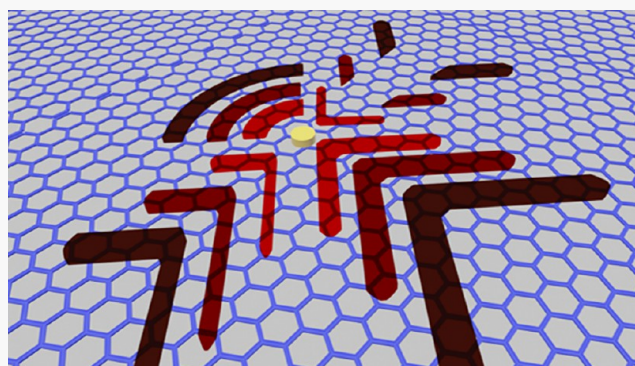
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ABSTRACT: Anisotropy has been a key property employed in the design of optical components for hundreds of years. However, in recent years there has been growing interest in polaritons supported within anisotropic (low crystal symmetry) materials for their ability to compress light to smaller, deeply subwavelength dimensions. While historically the first anisotropic polaritons probed were hyperbolic modes, research into anisotropic materials has recently turned toward hybrid materials and optical modes, employing phenomena such as phonon confinement, polaritonic strong coupling, and Moiré structures to design the optical properties. In this Perspective, we will briefly introduce the physics and theories of polariton anisotropy, review recently investigated anisotropic and two-dimensional materials, and then move on to a discussion of approaches toward realizing hybrid modes and identifying new materials. Based on the results from the past few years, we extend these discussions to highlight outstanding challenges and outline what we perceive as promising paths to further explore the potential for polariton anisotropy and hybrid systems in future nanophotonic optical devices.

KEYWORDS: polaritons, anisotropy, hyperbolic



INTRODUCTION

Anisotropy is at the heart of a broad range of optical phenomena, most notably using polarization manipulation in waveplates and in magneto-optic effects such as Kerr and Faraday rotation. Optical anisotropy means that light polarized along different crystal axes propagates within the medium at different velocities and, thus, wavelengths due to the variation in the dielectric permittivity tensors. As such, this gives rise to a so-called “fast” and “slow” axis for light propagation in the medium, with the differences between the tensor magnitudes (real part of the permittivity at a given frequency) driving the degree of polarization rotation as a function of path length (e.g., waveplate thickness). Historically, anisotropic dielectric species, such as calcite, have been employed for broadband applications as the dielectric function is also nominally constant over a broad spectral range. In such materials the degree of anisotropy (defined as the difference in refractive index along the directions, Δn) is typically small, only on the order of 0.1. Yet, near a strong material resonance (e.g., a crystal vibration), giant birefringence can be observed,¹ illustrating dramatic differences in the refractive index along orthogonal directions $\Delta n > 1$, enhancing material anisotropy. In extreme cases, such resonances can induce the permittivity tensor to become negative over specific spectral ranges,

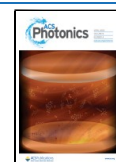
resulting in metallic behavior and the strong reflection of light. Further, such a negative permittivity is necessary for the opportunity to stimulate and exploit surface polaritons, that is, quasi-particles comprised of strongly coupled coherently oscillating charges in matter with a photon. In the infrared (IR), coupling light with coherent free-carrier oscillations (e.g., conduction electrons or holes) gives rise to surface plasmon polaritons (SPPs), while polar optic phonons offer the opportunity to stimulate surface phonon polaritons (SPhPs).^{2–5} These surface waves are exemplified by a polariton wavelength (λ_p), which is shorter than light of the same frequency in free space (λ_{FS}), thereby serving as the basis for IR nanophotonics and for deeply subdiffractional and compact optical components. Beyond the intriguing physics within such simple polaritonic materials, these surface waves are significantly modified within strongly anisotropic materials that support them, giving rise to exciting phenomena such as

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hyperbolicity⁶ (discussed below), which enables new paradigms in optical engineering that are unattainable with traditional refractive optics.

In certain extremely anisotropic materials (lower symmetry), resonances can cause the dielectric permittivity to be negative along certain crystal axes while remaining positive along others. Under such conditions the material simultaneously behaves as an optical metal (negative real part of the permittivity tensor, $\text{Re}(\epsilon) < 0$) and a dielectric ($\text{Re}(\epsilon) > 0$), a phenomenon known as hyperbolicity.^{6,7} This form of anisotropy has seen intense interest in recent years following the first observation of naturally hyperbolic materials,^{8–12} as it offers significantly improved compression of light and does so within the volume, rather than the surface of the medium, as well as enabling the manipulation of properties not inherent to isotropic materials. Notably, the role that strong material anisotropy plays in controlling polariton propagation has led to exciting new developments, such as in-plane hyperbolicity^{13–16} and so-called “ghost”¹⁷ and “shear”¹⁸ polaritons in low symmetry off-cut crystals and monoclinic and triclinic crystals, respectively. However, in addition to hyperbolic behavior, advances in artificial stacking and structuring of materials (both isotropic and anisotropic in nature) through heterostructure and superlattice fabrication have given rise to hybrid materials, such as the electromagnetic^{19–21} or crystalline hybrid materials,^{20–23} as well as the field of twist-optics.^{24,25} Such discoveries have enabled advances in our understanding of light–matter interactions at nanoscale dimensions, including realizing the ability to restrict light propagation to specific directions, providing the subdiffractional equivalent of Fabry–Perot cavities and offering frequency-dependent polariton propagation rotation. In this Perspective, we first discuss the physics behind polaritons supported by anisotropic materials, moving to highlight recent advances in naturally anisotropic polaritonic materials, hybrid materials, and their influence on the field of infrared nanophotonics. We conclude with an overview of existing challenges that remain for the field before such opportunities can be truly exploited for advanced nanophotonic concepts and devices.

THEORIES OF POLARITON ANISOTROPY

While highly anisotropic crystals have been employed in optics for a broad array of functions, it has only been in the last two decades that extreme forms of anisotropy have been explored for light confinement and subdiffractional manipulation and collection. One phenomenon in this vein is hyperbolicity, as described above. Highly reflective materials, such as metals in the visible spectral range, are mathematically defined by $\text{Re}(\epsilon) < 0$, while more traditional refractive dielectrics have a positive permittivity. Therefore, hyperbolic media can be considered as a material exhibiting metallic and dielectric optical properties simultaneously at the frequencies of interest.

Probing Polaritons. Prior to describing polaritonic modes in isotropic and anisotropic media, we briefly introduce the approaches to probe polaritons, as these optical modes exhibit high-momenta that cannot be directly excited and probed in the free space. The probing of surface-bound and hyperbolic polaritons stressed in this Perspective can be realized in both the near- and far-field. In the near-field, they can be measured directly via scattering-type scanning near-field optical microscopy (s-SNOM) and a similar technique referred to as nano-FTIR, allowing the user to acquire information on the local photonic density of states.^{26–28} Technical details of these

metrologies can be found in several reviews.^{29,30} Both techniques employ a metal-coated atomic-force microscope (AFM) tip close to the material surface (~ 10 – 70 nm) to scatter the incident light, enabling the excitation and detection of the supported high momentum signal (here polaritonic response) to be collected. As such, the tip itself behaves as an excitation (scatters light into high momentum polaritons) and detection point (collects high momentum light, e.g., polaritons) simultaneously. However, for polaritons probed within slabs of two-dimensional materials, interference effects must be exploited for them to be observed, thus, they cannot be observed in pristine and infinitely large hyperbolic media via these techniques. To observe propagating polaritons, a second scattering object must be included to induce the interference effect. The most common ways are³¹ (1) relying on a physical edge of the polariton supporting material to realize tip- and/or edge-launched polaritons; (2) creating a dielectric environment difference under and/or above the 2D polaritonic medium; and (3) providing a highly scattering object such as a metal nanostructure. These methodologies have been thoroughly studied with the launching efficiencies found to vary between the different methods.^{31,32} Note that s-SNOM can also be used to directly probe the propagation of polaritons (i.e., with no tip-induced excitation) by employing a dielectric (typically silicon) AFM tip.^{33,34} In this case, polaritonic nanostructures with enhanced LDOS, such as resonant nanoantennas,³³ are used as polaritonic sources. In the far-field, hyperbolic polaritons can be launched via Mie scattering of patterned antennae,^{8,35–39} scattering off of periodically patterned gratings,^{40–43} or evanescent coupling through a high index prism^{44–47} in either the Otto or Kretschmann configuration. These approaches have the primary advantage that they allow coupling to highly specific wavevectors of light while losing the ability to spatially resolve the local density of photonic states. Thus, one can interpret near-field techniques as operating in the spatial, with far-field measurements operating in the momentum domain. However, it is important to note that modes in nanostructured films are no longer the exact same electromagnetic modes excited in planar films. Importantly, the photonic bands can be formed and altered when the hBN and/or the underlying structure are patterned and the (subdiffractional) photonic crystals have been studied in both infrared (polaritonic)^{48–51} and visible (dielectric).⁵² The choice of technique to probe a hyperbolic polariton therefore depends on whether it is more critical to accurately determine the spatial or the momentum information from the system.

Isotropic Media and Surface Polaritons. To appreciate the implications of hyperbolic materials, the benefits afforded by surface polaritons must first be presented. For light in an isotropic dielectric (e.g., air), the wavelength follows the well-known $\hbar\omega = \hbar c\sqrt{\epsilon/\lambda_{\text{FS}}} = \hbar c\sqrt{\epsilon}k_{\text{FS}}$, where ω and k_{FS} represent the incident frequency and the wavevector (momentum) of light in free-space (see green line, Figure 1a–c). We note that this propagation can occur in any direction at a given frequency, which can be represented through plotting the possible wavevectors allowed for propagation in the form of an iso-frequency surface in the wavevector space, as shown in Figure 1d. For isotropic materials exhibiting a negative real part of the permittivity, strong coupling between light and matter causes a splitting of the dispersion relation, leading to a bulk polariton gap, which we represent in Figure 1a for a phonon polariton material,

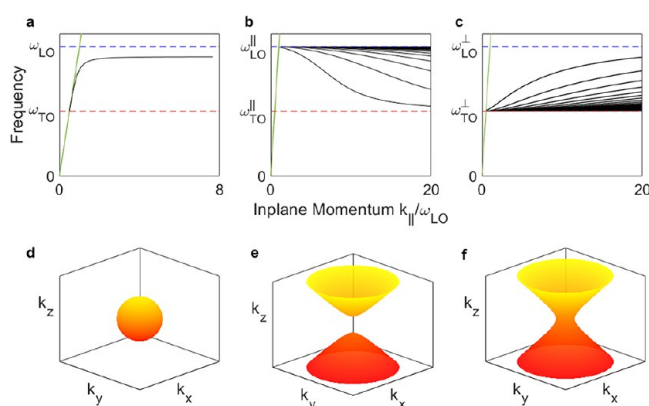


Figure 1. Isotropic and Hyperbolic Phonon Polaritons. Generic dispersion of (a) isotropic SPhPs, (b) type-I volume-confined HPhPs, and (c) type-II volume-confined HPhPs. Corresponding (d) isotropic and (e) type I and (f) type II hyperbolic isofrequency contours.

where SPhPs can be supported between transversal (TO) and longitudinal optic (LO) phonon frequencies in a region called the Reststrahlen band.^{2,5,53} Optical modes can be supported in this forbidden band, provided part of the energy does not reside inside the polaritonic material; that is, the mode exists as an evanescent field confined to the surface or interface with an adjacent dielectric.⁵⁴ As this results from strong coupling between light and coherent charges, surface polaritons behave light-like at lower frequencies, as indicated by the coincidence of the light-line with the polaritonic dispersion (see Figure 1a,

where the green and black curves converge near the red dashed line) transitioning to higher momenta (shorter wavelengths) associated with a more charge-like response as the frequency increases (black curve toward blue dashed line Figure 1a). Polaritons exist in many forms,⁵⁵ including (but not limited to) SPhPs (Figure 1a),^{2,5} SPPs,⁵⁴ exciton,^{3,4,56,57} Cooper-pair,³ magnon,^{3,58–60} Landau,^{61–63} vibrational,^{64–67} and molecular polaritons,^{68–70} yet for this Perspective we will confine our focus to PhPs and PPs.

Uniaxial Hyperbolicity. In a uniaxial hyperbolic medium, two of the crystal axes have an identical dielectric function, with the third exhibiting a dielectric permittivity tensor that is opposite in sign. Thus, light propagation in the hyperbolic media is different from that within either isotropic dielectrics or isotropic polaritonic materials. As the permittivity along at least one material axis is negative, polaritons can be supported and light can be confined to subdiffractional dimensions. However, unlike surface polaritons, the positive permittivity along the other axis (axes) ensures polaritons can still propagate within the volume of the hyperbolic media, leading to subdiffractional volumetric confinement of light.^{6,8,71} In further contrast to isotropic polaritonic media, hyperbolic materials can support almost arbitrary, thickness-dependent wavevectors of polaritonic modes with increasing momenta (decreasing wavelength) simultaneously, giving rise to ray-like propagation. Yet, this extended range of accessible momenta comes at the “cost” of a restriction in the propagation to a frequency-dependent fixed angle, as can be parametrized by calculating the possible wave vectors supported at a fixed

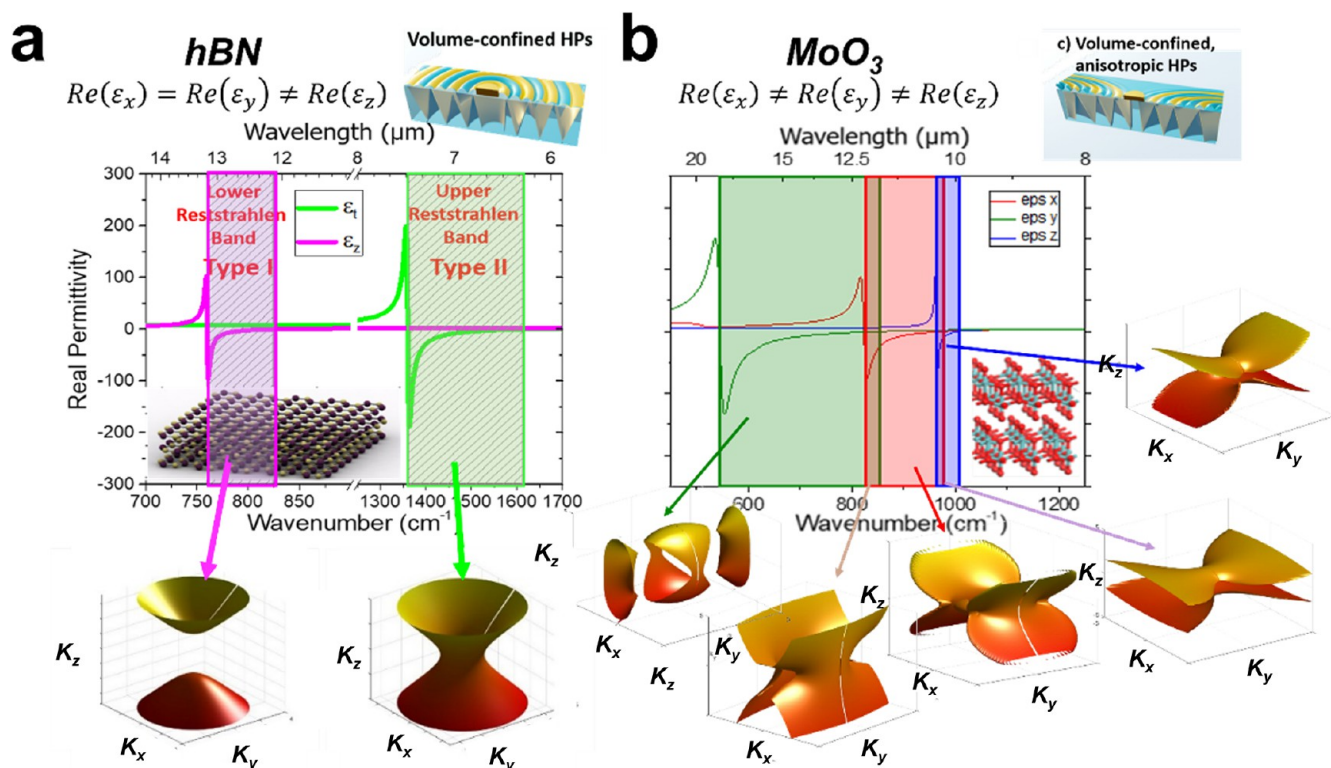


Figure 2. Isofrequency contour of exemplary hyperbolic materials. (a) hBN supports uniaxial hyperbolicity, and HPhPs are isotropic in the x – y plane. (b) The dielectric function of α -MoO₃ exhibits different values along different crystal directions, supporting biaxial hyperbolicity. In-plane and elliptical HPhPs are supported in different frequency ranges. Isofrequency contours representative of the specific spectral ranges where hyperbolicity is observed are provided for both materials. Panel (a) is adapted with permission from ref 8. Copyright 2014 Nature Publishing Group. Panel (b) is adapted with permission from ref 81. Copyright 2020 John Wiley & Sons, Inc.

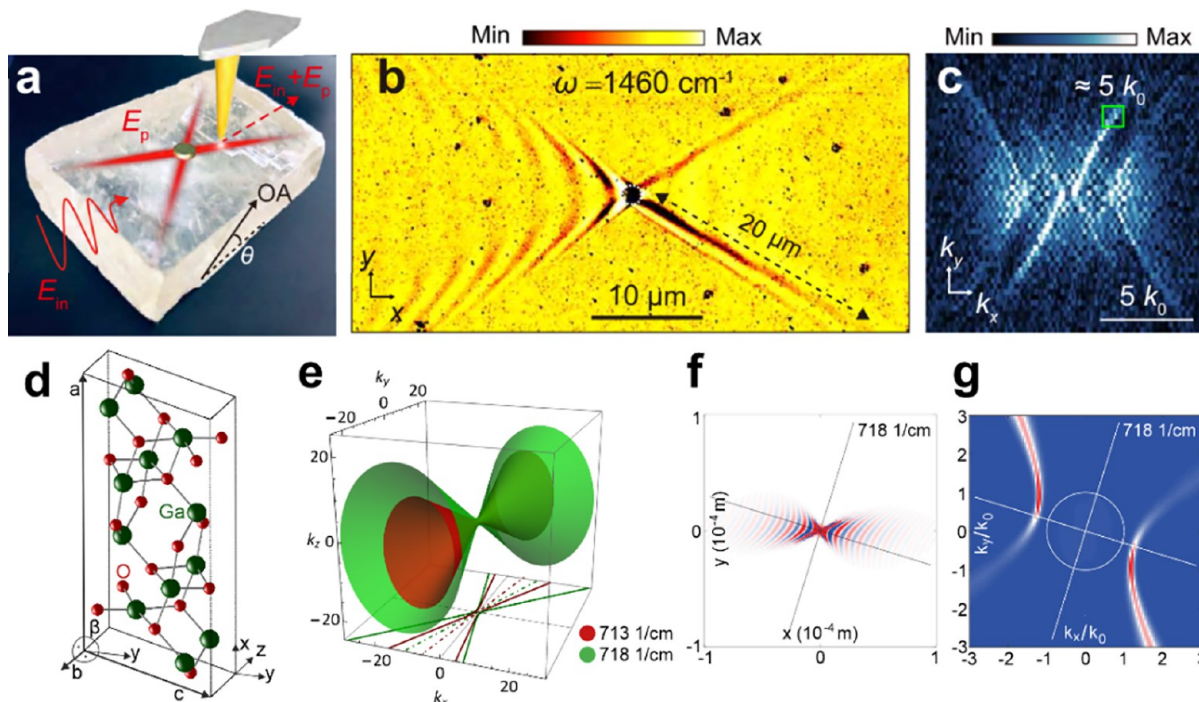


Figure 3. Off-cut and lower symmetry hyperbolicity. (a–c) Ghost hyperbolic polaritons supported by off-cut calcite crystal. (a) Measurement schematic; (b) Experimental s-SNOM measurement of ghost polaritons; (c) Absolute value of the Fourier transform of the image shown in panel (b); (d–g) Shear polaritons supported by β -Ga₂O₃. (d) Crystal structure of monoclinic β -Ga₂O₃; (e) Isofrequency surface of β -Ga₂O₃; Calculated fields of (f) real-space electric fields at the β -Ga₂O₃ surface; (g) Two-dimensional Fourier transformation of panel (f). Panels (a)–(c) are reprinted with permission from ref 17. Copyright 2021 Springer Nature. Panels (d)–(g) are reprinted with permission from ref 18. Copyright 2022. Springer Nature, licensed under a Creative Commons Attribution (CC BY) license: <https://creativecommons.org/licenses/by/4.0/>.

frequency (so-called iso-frequency contours). These are found most easily in a material with an arbitrary dielectric tensor ϵ by considering light with a fixed frequency of wavevector $\mathbf{k} = n\mathbf{k}_0$ with a direction defined by a real vector $\mathbf{k}_0 = \frac{2\pi}{\lambda}(\eta_x\hat{x} + \eta_y\hat{y} + \eta_z\hat{z})$, where $\eta_x^2 + \eta_y^2 + \eta_z^2 = 1$, with a complex refractive index n . By finding the determinant of the following matrix:

$$\begin{vmatrix} \epsilon_{xx} + n^2(\eta_x^2 - 1) & \epsilon_{xy}\eta_x\eta_y & \epsilon_{xz}\eta_x\eta_z \\ \epsilon_{xy}\eta_x\eta_y & \epsilon_{yy} + n^2(\eta_y^2 - 1) & \epsilon_{yz}\eta_y\eta_z \\ \epsilon_{xz}\eta_x\eta_z & \epsilon_{yz}\eta_y\eta_z & \epsilon_{zz} + n^2(\eta_z^2 - 1) \end{vmatrix} = 0$$

it is possible to find the complex wave vectors of light in different propagation directions.^{72,73} In the limit of high photon wavevectors in a uniaxial material, where the in-plane transverse permittivities are equivalent ($\epsilon_t = \epsilon_{xx} = \epsilon_{yy}$) and the out-of-plane (ϵ_{zz}) is different and opposite in sign, and all off-diagonal elements are zero, then this can be generalized to $\tan(\theta) \propto \sqrt{\epsilon_t/\epsilon_{zz}}i$, with i representing the imaginary unit.^{71,74} In finite thickness slabs, the restricted angle of propagation dictates a defined path length inside the material, resulting in specific conditions where the path length is a multiple of one of the series of compressed λ_{ps} , leading to a series of standing polaritonic waves with the supported wavevectors written as⁹

$$k(w) = k' + ik'' = -\frac{\psi}{d} \left[\text{atan}\left(\frac{\epsilon_o}{\epsilon_i\psi}\right) + \text{atan}\left(\frac{\epsilon_s}{\epsilon_i\psi}\right) + \pi l \right], \quad \psi = -i\sqrt{\frac{\epsilon_{zz}}{\epsilon_t}} \quad (1)$$

where d is the thickness, ϵ_o and ϵ_s are the complex dielectric functions of air and the substrate, respectively, and l is the

modal order. This implies that hyperbolic media behave like a subdiffractional Fabry–Perot cavity, with multiple branches in the polaritonic dispersion that each exhibit a progressively reduced λ_p (Figure 1b,c). The behavior depends on which axis (axes) is negative, with the most common forms being the Type I (one axis exhibits negative permittivity, typically z ; Figure 1b,e) and Type II (two axes negative, typically $x = y$; Figure 1c,f). However, it has been challenging to observe such ray-like propagation directly, as hyperbolic materials typically exhibit this behavior in out-of-plane directions that are difficult to experimentally probe. Yet, using hexagonal boron nitride (hBN) frustums (truncated cones), the ray-like propagation was directly confirmed by employing scattering-type scanning near-field scanning optical microscopy (s-SNOM) along the sloped sidewalls.⁷⁴ This material is a two-dimensional van der Waals crystal similar to graphene/graphite in structure⁷¹ that serves as an exemplary natural hyperbolic material supporting hyperbolic phonon polaritons (HPhPs) in two spectrally distinct Reststrahlen bands⁵³ (RBs). The lower frequency RB is type I (Figure 1b,e) and is observed within $\lambda_{FS} \sim 12.1$ – 13.2 μm (Figure 2a, pink region), while the upper is type II (Figure 1c,f) and occurs within $\lambda_{FS} \sim 6.2$ – 7.3 μm (Figure 2a, green region).^{8,9} Similarly, the demonstration of natural hyperbolicity was also reported in quartz¹⁰ and calcite,⁷⁵ among an ever-growing list.^{4,11,76} Notably, HPhP modes would strongly increase the local density of photonic states due to the coupling to high- k modes.⁷⁷

Biaxial Hyperbolicity. Analogous to uniaxial hyperbolicity, biaxial hyperbolicity occurs within materials where $\text{Re}(\epsilon)$ values are different, but this holds for all three crystal axes, with one being opposite in sign to the others. As such, these materials can show type I and type II hyperbolic bands that

Near-field observation

Far-field observation

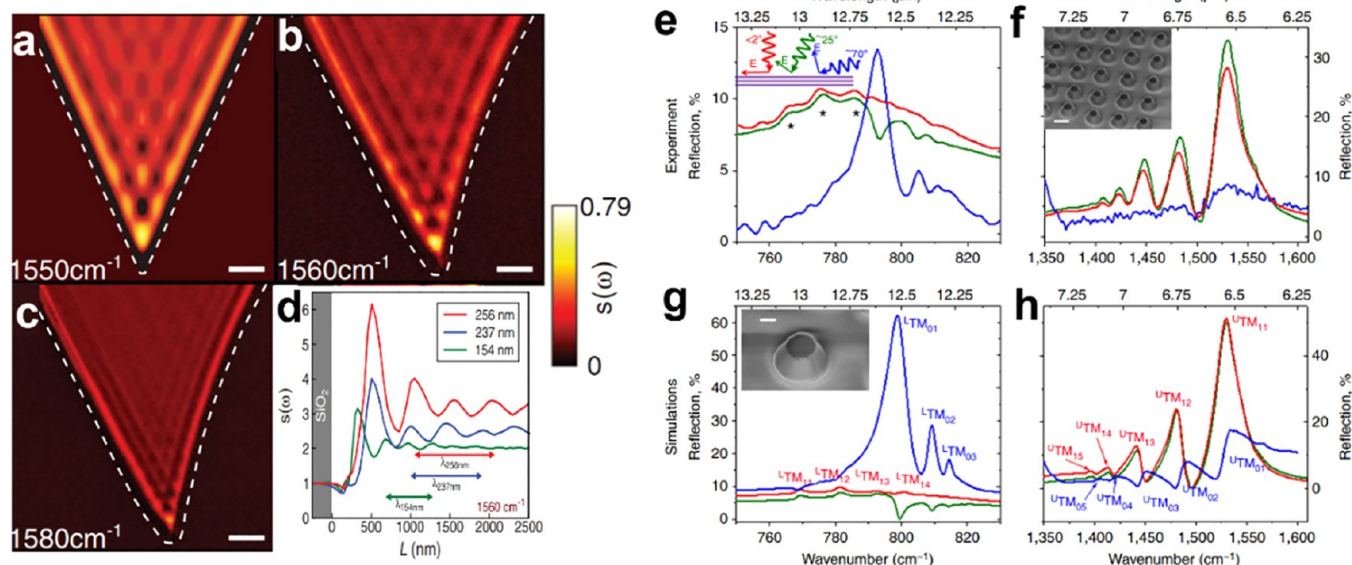


Figure 4. Experimentally observed hyperbolic phonon polaritons supported by hBN. (a–c) Experimentally observed propagating HPhPs supported in a hBN slab in the near-field via s-SNOM. At different frequencies, the polariton wavelength varies, dictated by eq 1. (d) Line scans extracted from s-SNOM measurements on variable thickness hBN are provided, from which the HPhP wavelength at 1560 cm^{-1} was extracted. (e–h) High-order HPhP modes supported by nanostructured hBN are observed in the far-field from frustums fabricated into hBN flakes (inset SEM). Experimental and simulated spectra within the lower and upper Reststrahlen bands of hBN are provided and demonstrate that the higher order modes can be directly excited from the far-field. Panels (a)–(d) are adapted with permission from ref 9. Copyright 2014 AAAS. Panels (e)–(h) are reprinted with permission from ref 8. Copyright 2014 Nature Publishing Group.

exhibit momenta dependent on the direction of propagation. Therefore, these materials will be inherently more dispersive in terms of their waveguiding properties. Due to the varying properties of each of the crystal axes, in-plane hyperbolic behavior and ray-like propagation are more easily observed in biaxial hyperbolic materials.¹⁵ Furthermore, this allows for controlling polarization more easily, even at near-normal incidence,⁷⁸ versus only being readily accessible at high angles for uniaxial materials with the optical axis normal to the surface, as in hBN.⁷⁹ An exemplary material in this regard is MoO_3 ,^{14,80,81} whereby the anisotropic optic phonons along the three principal axes give rise to multiple RBs (Figure 2b), where polariton propagation can be supported as designated by the overlaid shaded regions in the dielectric function of MoO_3 .^{79,81} For instance, within the blue region, only the out-of-plane permittivity tensor is negative, giving rise to a similar hyperbolic response to that of the upper RB of hBN, albeit with the polaritonic waves propagating along the x and y directions exhibiting different λ_{ps} . However, in the red- and green-shaded regions the x - and y -axes permittivities become negative, respectively, giving rise to in-plane hyperbolicity; that is, the polariton propagation is restricted to the condition:

$$|\tan(k_{xx}/k_{yy})| < \sqrt{(\epsilon_{yy}/\epsilon_{xx})}/i \text{ (see cross-sectional schematic in upper right, Figure 2b), which stands in stark contrast to the isotropic in-plane propagation of hyperbolic polaritons in hBN (top right, Figure 2a). Additional regimes where these bands overlap (purple arrow, yellow arrow in Figure 2b) result in even more complicated hyperbolic propagation as evidence by the representative isofrequency contours for each of these regimes (Figure 2b).}$$

Off-Cut and Lower Symmetry Hyperbolicity. When studying hyperbolic materials, it is often convenient to operate

with the optical axes of the crystal aligned with the coordinate system in the laboratory. This allows for an easier definition of the dielectric properties of materials, as well as easing the understanding of any surface- or volume-confined waves. However, in both uniaxial (e.g., calcite) and biaxial materials it is possible to produce crystal off-cuts where the crystal axes are misaligned with the surface (Figure 3a). This is also common in various silicon carbide polytypes as the off-cuts are used to induce stepwise epitaxial growth,⁸² as well as for sapphire, where multiple off-cuts are commercially available for improved lattice match for heteroepitaxy. In such off-cut, anisotropic crystals one can support so-called “Ghost polaritons”, which are defined as those that are partially evanescent and propagating waves in character.¹⁷ The formation of polariton rays can be explained by the larger local photonic density of states. Experimentally, the polaritons can be observed via s-SNOM measurements on off-cut calcite surfaces (Figure 3b), with the resultant momentum-space plots extracted via Fourier transforms (Figure 3c). Hyperbolicity can also arise from crystals with further reduced symmetry, such as those featuring monoclinic (Figure 3d for β -phase Ga_2O_3) and triclinic Bravais lattices, where the nonorthogonal nature of at least one of the principal crystal axes leads to a permittivity tensor matrix that cannot be diagonalized. Such low crystal symmetry gives rise to a shear force applied to the hyperbolic polaritons supported, resulting in so-called “shear polaritons”, where the propagation direction is found to rotate in the plane as the incident frequency is modified within a given RB (Figure 3e,f).¹⁸ The Fourier transform of Figure 3f illustrates such a frequency-dependent rotation as well as the strong anisotropy in the momentum space plot (Figure 3g).

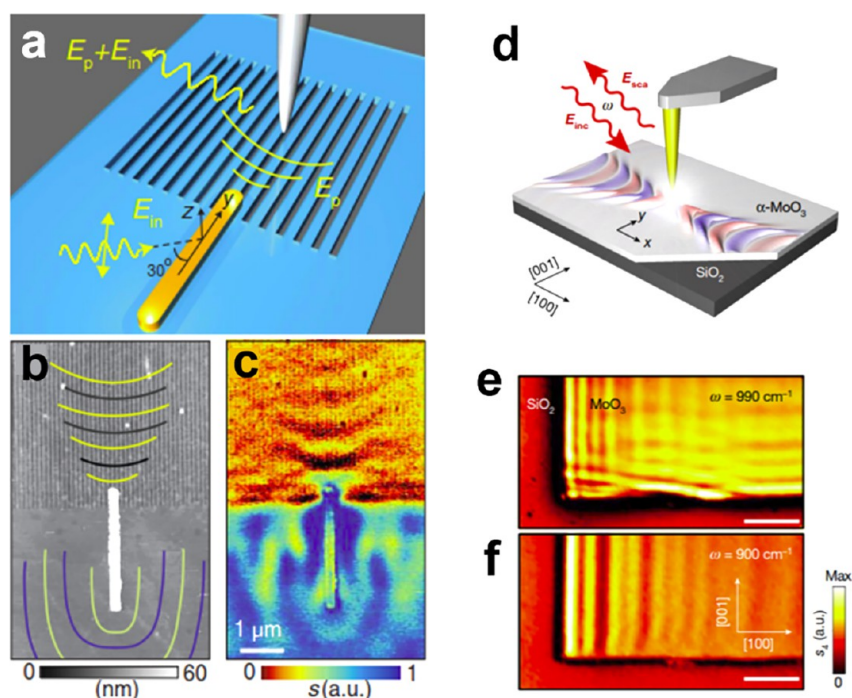


Figure 5. Artificial and natural biaxial hyperbolic materials. (a) Patterned hBN nanostructure shows in-plane hyperbolicity, resulting from effective media effect (hBN/air alternating layers). (b, c) The in-plane hyperbolicity is confirmed by s-SNOM measurement. (d) Natural in-plane hyperbolic material (MoO_3). (e) HPhPs are both supported in $[001]$ and $[100]$ crystal directions at 990 cm^{-1} , albeit with different polariton wavelength (elliptical band). (f) At the in-plane hyperbolic range, e.g., 900 cm^{-1} , only HPhPs along $[100]$ crystal direction are allowed. Panels (a)–(c) are adapted with permission from ref 13. Copyright 2018 AAAS. Panels (d)–(f) are adapted with permission from ref 14. Copyright 2018 Springer Nature.

■ MATERIALS FOR POLARITON ANISOTROPY

From Artificial to Natural Uniaxial Hyperbolic Materials. Originally, hyperbolic behavior was investigated using artificial hyperbolic metamaterials (HMMs)^{6,77,83,84} featuring alternating subwavelength scale metal and dielectric domains, with the hyperbolic behavior well-described by the effective medium approximation.⁸⁵ While many novel physical phenomena have been reported using such systems, including negative refraction,^{86–91} hyperlensing,^{92–96} and subdiffractional-lithography,^{97,98} the high optical losses resulting from the metal elements^{99–101} severely restricts their use beyond the laboratory. However, in 2012 and 2014 hyperbolic behavior was reported for the first time in the naturally anisotropic crystals quartz¹⁰ and hexagonal boron nitride (hBN),^{8,9} respectively. In the case of the latter, the seminal works of Dai et al.⁹ demonstrated the thickness-dependent dispersion of hyperbolic modes (Figure 4a–d), indicating that $\lambda_p(\omega)$ changes as a function of slab thickness, while Caldwell et al.⁸ experimentally confirmed that multiple higher-order HPhP modes could be supported simultaneously within nanostructures (Figure 4e–h), giving rise to multiple resonant conditions with progressively decreasing λ_p . Later work by Giles et al.¹⁰² employed isotopically enriched hBN to enable the direct observation of these higher-order HPhPs propagating simultaneously at a fixed incident frequency using s-SNOM, with such modes previously only observed via Fourier transforms of s-SNOM linescans near hBN flake edges.⁹⁶ Note that monolayer hBN can also support ultrahigh momentum HPhPs.^{103–105} The optic phonon origin of the HPhPs significantly reduced the optical losses in contrast to previously reported HMMs, resulting in significant improvements in

hyperlens imaging resolution,^{95,96,106} Q-factors,^{8,107} and propagation lengths.^{9,37,102,108–110}

From Artificial to Natural Biaxial Hyperbolic Materials. Beyond hBN, a whole host of natural hyperbolic materials have been identified.^{4,11,71,76} However, extending beyond the simplified types I and II HPhPs supported in hBN, the realization of in-plane hyperbolicity ($\text{Re}(\epsilon) < 0$ along one in-plane direction, while it is $\text{Re}(\epsilon) > 0$ along the other) promises significant opportunities⁷⁸ by enabling the restriction of propagation to a single in-plane direction,^{13,14,80} as highlighted above for MoO_3 . Again, such so-called “in-plane hyperbolicity” was initially demonstrated in HMMs,¹¹¹ and was later identified in hBN patterned into strips via focused ion beam (FIB),¹³ as shown in Figure 5a. Thus, in this structured system the polaritonic wavefront is launched via scattering off a metal antenna (Figure 5a–c) and was directionally propagated parallel to the hBN stripes (here, perpendicular to the gold antenna tip). However, in 2018 such in-plane hyperbolic response was observed within the natural crystal MoO_3 .^{14,80} Here using s-SNOM again, but on unpatterned crystals of MoO_3 , the same highly directional propagation of HPhPs was observed within in-plane hyperbolic bands (Figure 5d,f), while in others where the two in-plane bands are of the same sign, but different magnitudes, where polaritonic waves are observed to propagate in both directions, albeit with distinctly different λ_p (Figure 5e, “elliptical band”).

While prior calculations and measurements of MoO_3 had been employed to extract an approximate uniaxial dielectric function, it was through correlated far-field Fourier-transform infrared spectroscopy (FTIR) and near-field s-SNOM measurements that the quantification of the IR dielectric function of this material was extracted (Figure 2b),⁸¹ with

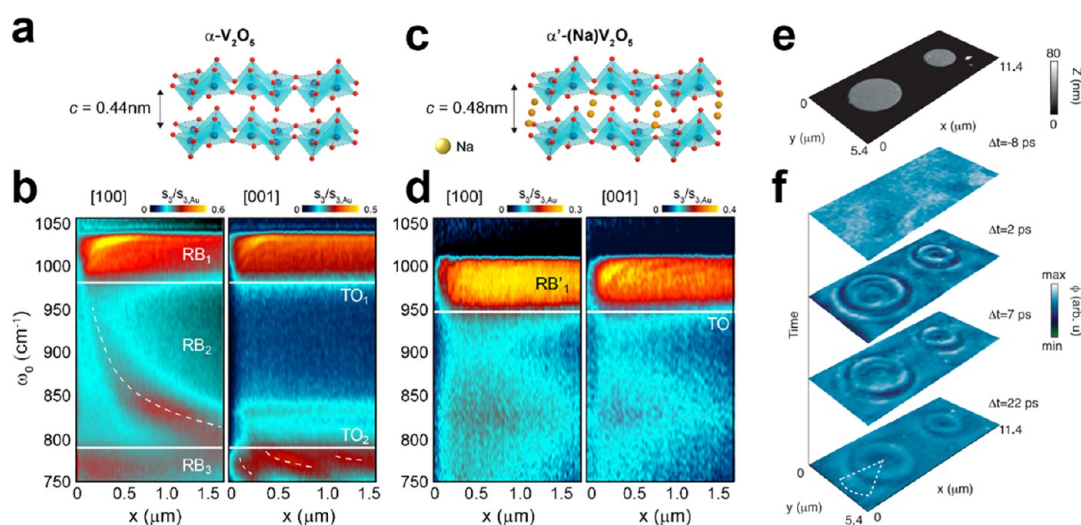


Figure 6. Dynamic hyperbolic materials. (a, b) The HPhP response supported by α - V_2O_5 can be (c, d) spectrally tuned by Na^+ intercalation.¹⁶ The (a) crystal structure of the pristine α - V_2O_5 and corresponding (b) nano-FTIR measurements along two crystal directions are presented without any intercalation, showing the natural in-plane hyperbolicity within RB2. After Na^+ intercalation, (c) the lattice expands causing (d) the RB1 is shifted to lower frequency, while RB2 is no longer observed. (e, f) The transient hyperbolic Rydberg polaritons are supported by WSe_2 when photoinjected carriers are at a sufficient level.¹¹⁹ Panels (a)–(d) are reprinted with permission from ref 16. Copyright 2020 Springer Nature. Panels (e)–(f) are reprinted with permission from ref 119. Copyright 2021 AAAS.

these results validating the previously measured s-SNOM and nano-FTIR experiments within the three RBs of the material (Figure 5d–f). Such directional propagation is further extended to nonsymmetric cases within calcite¹⁷ and β - Ga_2O_3 ¹⁸ that have been recently shown to exhibit the more exotic forms of polaritons discussed above.

From Static to Dynamic Hyperbolic Materials. Despite an increasing array of anisotropic and hyperbolic materials, single materials often limit the engineering control and frequency tuning of the supported polaritonic modes. Dynamic tuning of HPhPs is especially problematic, as these modes arise from the lattice vibrations of a polar material and are inherently fixed in frequency for a given material composition. For instance, while hBN offers high Q -factor resonances and long propagating HPhPs, the large bandgap (~ 5.95 eV)^{112,113} precludes free-carrier injection for active modulation as has been demonstrated for SiC, InP, and GaN,^{114–116} therefore, requiring external stimuli to the surrounding medium to induce any changes in polaritonic response.^{117,118} Recently, Taboada-Gutiérrez et al.¹⁶ demonstrated frequency tuning of the hyperbolicity in V_2O_5 by sodium intercalation, thereby providing significantly greater flexibility via a hybrid material approach (Figure 6a–d). In addition, hyperbolic Rydberg polaritons, i.e., quantum transitions between different states within the excitonic Rydberg series leading to long-lived spectral weight at the mid-infrared, can be turned on and off at picosecond time scales in WSe_2 slabs (Figure 6e,f), as demonstrated by Sternbac et al.¹¹⁹ Yet, such approaches still represent material-specific opportunities rather than general approaches to dynamic tuning appropriate for any HPhP-supporting material, and thus, additional solutions to this challenge must also be identified.

ENGINEERING POLARITON ANISOTROPY THROUGH HYBRID MATERIALS

The significant opportunities in nanophotonics afforded by material anisotropy can be further expanded by artificially engineering the supported polaritons. In the context of

dynamic tuning, such engineering can provide alternative platforms for active control of polaritonic properties through stimuli to the local environment or an adjacent polaritonic material. Two principal methods have been discussed: (1) controlling/modifying the local environment^{117,118,120} and (2) coupling between different polaritonic modes in adjacent materials.^{45,121–125} However, such hybridization concepts have also been exploited to completely modify the dielectric function of materials through the (3) crystalline hybrid concept that can be realized through atomic-layer superlattice design.^{20,22}

Controlling the Local Environment. The first method toward engineering polaritonic properties is based on controlling the local environment. While broadly implemented for various SPP-based concepts, including the ubiquitous surface plasmon resonance (SPR) biosensing scheme,^{126–128} the volume-confined nature of HPhPs implies a more limited influence on the local environment.⁸ However, recent experiments have demonstrated that such hyperbolic modes indeed remain sensitive to the local refractive index, as shown in eq 1. It has been experimentally demonstrated that HPhPs supported by hBN over materials of various refractive indices exhibit different wavevectors¹¹⁸ and, thus, different λ_{ps} , and the propagation within a given slab of a hyperbolic material over a domain between two different dielectric environments results in in-plane refraction.¹¹⁷ In the case of HPhPs in hBN, due to their in-plane isotropic propagation, refraction occurs under the most common expression of Snell's law (Figure 7a), that is, the waves bend toward the normal to the boundary when passing from a low- (inside white dashed triangular area in Figure 7a: hBN/air) to a high-refractive index (outside white dashed triangular area in Figure 7a: hBN/ SiO_2) medium. However, in the case of in-plane HPhPs such as those supported in MoO_3 , refraction is a more exotic phenomenon,¹²⁹ yielding the polaritonic wavevector ($\mathbf{k}_{\text{out-exp}}$) to refract toward the normal while the energy flux bends away from it (Figure 7b).^{130,131} This unusual phenomenon has been recently exploited to demonstrate a refractive planar hyperlens

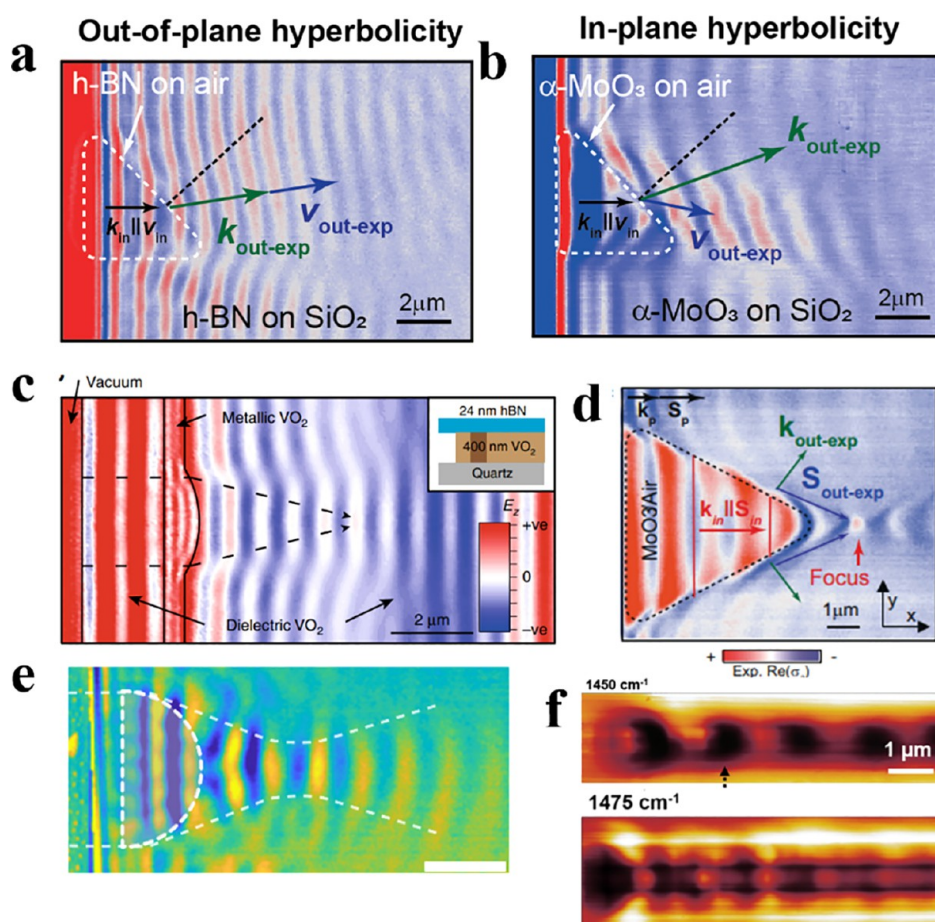


Figure 7. Engineering polariton propagations via polaritonic refractions. (a) Manipulation of in-plane isotropic HPhPs in hBN via local environment. Refraction takes place under the most conventional form of Snell's law. (b) Manipulation of in-plane hyperbolic HPhPs in MoO₃ via the same approach. Refraction gives rise to nonintuitive directions of propagation of both wavevector k and Poynting vector S . (c, d) In-plane lens formed by underlying patterns. (e, f) In-plane lens and waveguides of HPhPs formed by the underlying patterns. Panels (a), (b), and (d) are adapted with permission from ref 132 (with changes). Copyright 2021 Springer Nature, licensed under a Creative Commons Attribution (CC BY) license: <https://creativecommons.org/licenses/by/4.0/>. Panel (c) is reprinted with permission from ref 117 (no changes). Copyright 2018 Springer Nature, licensed under a Creative Commons Attribution (CC BY) license: <https://creativecommons.org/licenses/by/4.0/>. Panel (e) is reprinted with permission from ref 120 (no changes). Copyright 2019 Springer Nature, licensed under a Creative Commons Attribution (CC BY) license: <https://creativecommons.org/licenses/by/4.0/>. Panel (f) is reprinted with permission from ref 133. Copyright 2021 John Wiley & Sons, Inc.

(black dashed triangle in Figure 7d), yielding subdiffractional foci as small as $\sim \lambda_p/6$.¹³² These refractive phenomena allow for the deterministic control of the wavelength of the anisotropic modes, thereby providing a path to chemical sensors based on the surface-enhanced IR absorption (SEIRA) concept,¹²⁴ as well as on-chip photonic components, such as waveguides (Figure 7f), lenses (Figure 7c,e), and resonators.^{117,120} Furthermore, such an approach was recently demonstrated to provide frequency multiplexing within unpatterned hBN, with the wave propagation dictated by the underlying silicon photonic architecture.¹³³ However, while such an approach enables direct control of HPhP propagation, and potentially in an active and reconfigurable manner,^{117,120} this does not inherently provide a methodology to modify or remove the inherent anisotropy of the polaritonic material or modes.

Coupling among Different Photonic Modes. The second approach, which is similar but fundamentally different from the first, is to introduce polaritonic coupling, thereby giving rise to SPP/HPhP, HPhP/HPhP, or SPhP/HPhP hybrid modes. Just as strong coupling between a photon and

a coherent charge oscillation gives rise to a polariton mode that exhibits hybrid properties of both constituents, polariton–polariton strong coupling offers similar benefits.¹³⁴ As originally demonstrated by Woessner et al.,¹³⁵ a heterostructure comprised of hBN and graphene enabled the opportunity to significantly extend the lifetimes and propagation lengths of SPPs in graphene in the spectral ranges outside of the RBs of hBN. Subsequent efforts within similar heterostructures by Dai et al.¹⁹ demonstrated that, within these bands, SPP–HPhP strong coupling could be induced, which in turn enabled the ability to control the hybrid λ_p and propagation characteristics through electrostatic gating of the graphene,^{136–138} while maintaining the volume-confinement and multiple polariton branches associated with the hBN HPhPs (Figure 8a,b). This approach, later referred to as the electromagnetic hybrid concept,²¹ offers significant opportunities for controlling polaritonic properties in lower symmetry materials, as discussed below. More recent efforts have extended into the realm of polaritonic strong coupling, which has enabled the hybridization of so-called epsilon-near-zero-polaritons (ENZ) and propagating SPPs¹²³ or SPhPs,⁴⁵

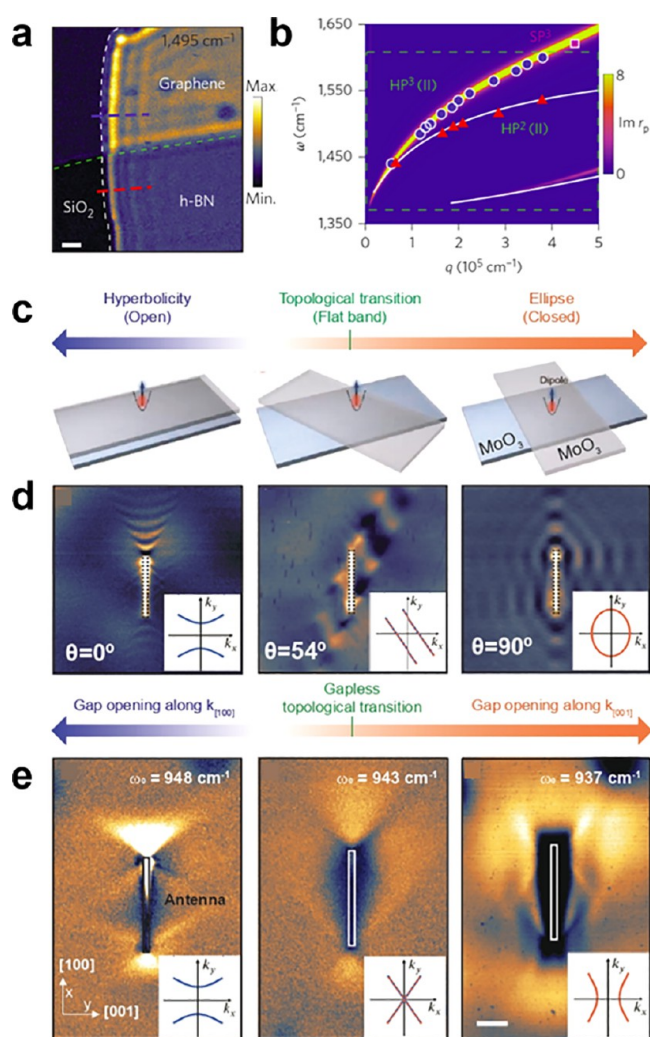


Figure 8. Engineered in-plane anisotropy of HPhPs by electromagnetic mode coupling. (a, b) The HPhPs supported by hBN (in-plane isotropic) can be coupled to isotropic SPPs supported by graphene, leading to hybridized modes.¹⁹ (c, d) Photonic topological transition in twisted bilayered α -MoO₃: the polaritonic isofrequency curve (IFC) transits from an open hyperbola (left panel) to a closed ellipse (right panel) passing through a “flat band” regime (two parallel lines, middle panel) at which polaritons propagate along one specific direction (canalization regime).²⁴ (e) Photonic topological transition in α -MoO₃/4H-SiC heterostructures: the polaritonic IFC transits from an open hyperbola centered along the [100] crystal direction (left panel) to an open hyperbola centered along the [001] crystal direction (right panel). The transition occurs through a gapless IFC formed by two crossing lines (middle panel). The propagation direction of HPhPs in α -MoO₃ can thus be reverted via mode coupling.¹⁴⁷ Panels (a) and (b) are adapted with permission from ref 19. Copyright 2015 Springer Nature. Panels (c) and (d) are adapted with permission from ref 24. Copyright 2020 American Chemical Society. Panel (e) is reprinted with permission from ref 147. Copyright 2021 AAAS. Distributed under a CC BY-NC 4.0 license <http://creativecommons.org/licenses/by-nc/4.0/>. The isofrequency curves are added onto the original figure.

enabling the potential to dictate the polaritonic dispersion, including modifying the group velocity, field concentration, and polaritonic wavevector. However, in all such approaches, only the wavelength of the anisotropic polaritons is directly controlled, yet we envision that similar electromagnetic hybrids can be realized by graphene and biaxial hyperbolic materials in

which the polariton propagation direction also changes. For instance, one can potentially change the propagation direction of in-plane hyperbolic polaritons in MoO₃ when a graphene layer is included,¹³⁹ while such observations could also be observed by locally changing the carrier density in the vicinity of shear polaritons.

In addition to coupling between isotropic SPPs and anisotropic SPhPs, the coupling between two anisotropic PhP media may also provide significant benefits. Notably, inspired by the discovery of flat-band superconductivity¹⁴⁰ and ferromagnetism¹⁴¹ in twisted bilayer graphene, it has been reported that stacks of two twisted layers of α -MoO₃ allow further design freedom in engineering the direction of propagation of hybrid HPhP modes, thus, introducing an unprecedented degree of control over the manipulation of in-plane anisotropic polaritons through the implementation of the field of “twist-optics”.^{24,142,143} In these works, hybrid HPhPs/HPhPs were demonstrated, showing altered directionality of propagating HPhPs (Figure 8c,d). The images revealed polaritonic isofrequency contours in the hybrid system with different geometries that can be tuned by simply changing the twist angle between the principal crystalline axis of the stacked individual α -MoO₃ slabs. Remarkably, these isofrequency contours exhibit extreme topological transitions from open hyperbolic-like to closed spherical/elliptical curves, thus, having a profound effect on the anisotropic propagation properties of such hybrid modes.¹⁴⁴ Indeed, it was identified that at a critical twist angle, extreme directional propagation of all polaritonic wavevectors along specific in-plane directions emerges, the so-called canalization regime.¹⁴⁵ While this case demonstrated enormous potential for controlling polariton propagation, it does not alter the forbidden propagation direction. By coupling the HPhP with a dielectric-SPhP mode, the allowed (and forbidden) propagation direction can be inverted, which is experimentally demonstrated in the heterostructure of α -MoO₃/SiC (Figure 8e).^{146,147} Specifically, it was visualized that the propagation of in-plane HPhPs in α -MoO₃ rotates 90° when the crystal is placed on SiC. Importantly, due to the unique low-loss nature of the topological transition, it was possible to visualize intermediate propagating states, which permits the unveiling of the topological origin of the transition. The general and fundamental characters of these findings extend the unique possibilities of twisted polaritons discussed above to develop optical applications requiring propagation of the electromagnetic energy flow along specific directions, for example, directional coupling between molecules¹⁴⁸ or quantum emitters¹⁴⁹ or directional thermal management.^{150–154}

Crystalline Hybrid. The third concept focuses on manipulating the fundamental atomic structure through an atomic-layer superlattice design.^{20,21} As the dielectric function within the IR for polar materials is dictated predominantly by the optic phonons, modifications to the fundamental frequencies, scattering lifetimes, and introduction of new phonon modes will in turn have direct implications on the IR properties. Such an approach gives rise to the so-called crystalline hybrid concept.²² Unlike in the above approaches where we take two relatively thick materials with fixed optical properties and directly couple them, here strongly bonded, atomically thin materials are found to give rise to emergent properties that are different from that of the bulk constituent materials. This is because as the thickness of individual layers within a superlattice are reduced, they approach the length-

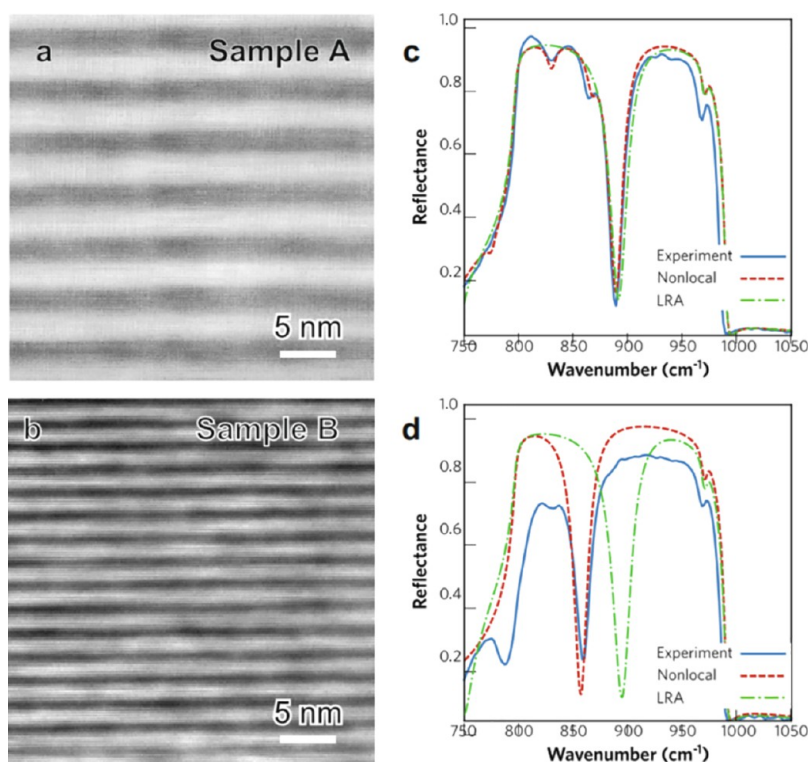


Figure 9. Nonlocal effect in crystalline hybrid. (a, b) Two AlN/GaN atomic-layer superlattices from ref 22, with average layer thicknesses of 2.2 nm (sample A) and 1.3 nm (sample B). (c, d) The reflectance of the two structures as obtained from experiments (blue solid lines), standard (local) and dielectric theory (green dash-dotted lines), and using the nonlocal theory from ref 23 (red dashed lines). The local theory, neglecting the dispersion of the phonons, fails to reproduce both the position of the main polaritonic resonance and the presence of further ones due to the hybridization with longitudinal modes. Panels a and b are adapted with permission from ref 22. Copyright 2019 American Chemical Society. Panels c and d are reprinted with permission from ref 23 (no changes). Copyright 2020 American Physical Society, licensed under a Creative Commons Attribution (CC BY) license: <https://creativecommons.org/licenses/by/4.0/>.

scale of the optic phonon wavelengths resulting in confinement with modified frequencies at the gamma point within the Brillouin zone.^{155–158} Moreover, at such length-scales, the approximation of optic phonons as nominally dispersionless (e.g., localized vibrations) fails, and their propagative and dispersive nature becomes important, leading to the appearance of so-called nonlocal phenomena.²³ In addition, the integration of multiple material interfaces with modified chemical bonding offers the potential to introduce new interface phonons, corresponding to vibrational states localized to the interfacial region.^{159–161} This has been observed to induce anomalous spectral shifts in localized SPhP resonances due to the introduction of new interface phonons between polar semiconductor and ultrathin dielectrics deposited via ALD.¹⁶² The incorporation of phonon confinement with new interface phonon modes, along with the resulting mixing of longitudinal and transverse charge oscillations, results in frequency shifts and the presence of novel discrete resonances in the far-field spectrum of thin layers, as well as the appearance of longitudinal resonances in the local photonic density of states.²³ Yet, it is important to note that such nonlocality also increases losses as high-momentum optic phonons can propagate away from the sample, effectively becoming a new loss channel.²³ In all, such modifications result in a fundamentally different dielectric function for this new crystalline hybrid material. These effects have been recently observed by Ratchford et al.²² within AlN/GaN short-period superlattices (TEM cross sections in Figure 9a,b), demonstrating a significantly modified IR reflectance (Figure 9c,d, blue

curves), and thus, dielectric function and polaritonic dispersion. While *ab initio* simulations were initially employed to study crystalline hybrids,²² nonlocal dielectric theories have more recently been shown to correctly reproduce experimental features with limited computational requirements (Figure 9c,d, red curves), making it possible to include nonlocal effects in the design of SPhP devices.^{163,164} Further, much like semiconductor quantum wells, this also provides the potential opportunity to inject free carriers in one of the constituents (e.g., GaN) to locally tune the SPhPs within the adjacent structure (e.g., AlN) through the electromagnetic hybrid effect.²¹ Thus, this could enable opportunities to actively tune polaritonic modes within materials where otherwise such effects are not possible.

Polariton Loss. While polaritons enable strong light–matter interactions through the subdiffractional confinement of light, it comes at the cost of increased losses. Although PhPs possess significantly reduced loss compared with plasmonic counterparts, the loss is still a limiting factor for many applications, for instance, chip-scale communications. To discuss the implications of these losses upon anisotropic polaritons, we first summarize the phonon lifetimes of several highlighted materials including hBN, MoO₃, V₂O₅, and calcite, as shown in Table 1. Besides the intrinsic properties, the polariton modes supported by those materials are more critical for applications. Thus, we employ an analytical solution (eq 1) to find the complex valued wavevectors of hyperbolic modes supported by 20 nm thick slabs of those materials. Additionally, the Q factor offers an indication of the loss-induced

Table 1. Phonon Lifetimes of Different Materials (Crystal Directions)^a

material	phonon frequencies ($\omega_{\text{TO}}/\omega_{\text{LO}}$ cm ⁻¹)	phonon damping (cm ⁻¹)	phonon lifetime (ps)
α -V ₂ O ₅ [001] ¹⁶	474.4/815.6	9.6	0.55
α -MoO ₃ [100] ⁸¹	821/963	6.0	0.88
α -MoO ₃ [001] ⁸¹	544/850	9.5	0.56
natural hBN in-plane ⁸	1360/1614	7	0.76
¹¹ B 99% hBN in- plane ¹⁰²	1359.8/1608.7	2.1	2.5
¹⁰ B 99% hBN in-plane ¹⁰²	1394.5/1650	1.8	2.9
natural hBN out-of-plane ⁸	760/825	3	1.8
¹¹ B 99% hBN out-of-plane ¹⁰²	755/814	1	5.3
¹⁰ B 99% hBN out-of-plane ¹⁰²	785/845	1.0	5.3
calcite [100] ^{17,166}	1410/1550	10	0.53

^aPhonon frequencies are TO and LO frequencies along the corresponding crystal axis. Phonon lifetimes are derived from the phonon damping, which is extracted from dielectric function fittings.

limitation on polariton propagation and is defined as $\frac{\text{real}(k)}{\text{imag}(k)} = 4\pi N$, where N defines the number of cycles that the HPhPs propagate until the electric field intensity decays to $1/e$, with the comparison of the Q factors for these materials provided in Figure 10a. Similarly, the propagation length, $L_p = \frac{1}{\text{imag}(k)}$ defines the distance the mode will propagate until

the amplitude of the electric field, which can be directly measured in s-SNOM, decays to $1/e$.¹⁶ In general, the polariton propagation lengths are limited to the micron scale, which is orders of magnitude below that of refractive optics, as shown in Figure 10b. However, polaritons provide the strong light–matter interactions and high confinement that dielectric materials cannot, thereby enabling significant benefits for sensing applications, compact nanophotonic- and metamaterial-based optics, as well as in nanoscale control of light propagation. We further calculated the polariton lifetime by $\tau = L_p/v_g$, where $v_g = \frac{\partial \omega}{\partial k}$ is the group velocity (Figure 10c). Note that the polariton lifetimes are not equivalent to phonon lifetimes due to differences in the group velocity (dispersion).

From these comparisons, one can derive some insights into how to decrease the loss of polaritons. The most obvious approach is to improve the material quality, for example, reducing the atomic impurities. For instance, isotopically enriched hBN has exhibited optic phonon lifetimes that are 3–4× longer than the naturally abundant form (20% ¹⁰B, 80% ¹¹B, Figure 10a–c).^{102,165} These improvements come from the suppressed isotopic mass-based scattering, while similar improvements are expected from reduced impurities. As such, it is expected that further materials engineering could improve the Q -factors of anisotropic polaritons, especially for materials with significant isotropic impurities, for example, MoO₃. Beyond such traditional approaches, mode engineering could also decrease the loss of polaritons. Confinement of a mode is typically negatively correlated with propagation length. For instance, for a given material (99% ¹⁰B hBN here), λ_p of the HPhP mode is reciprocal to the material thickness, and thicker hBN (lower confinement) leads to longer propagation

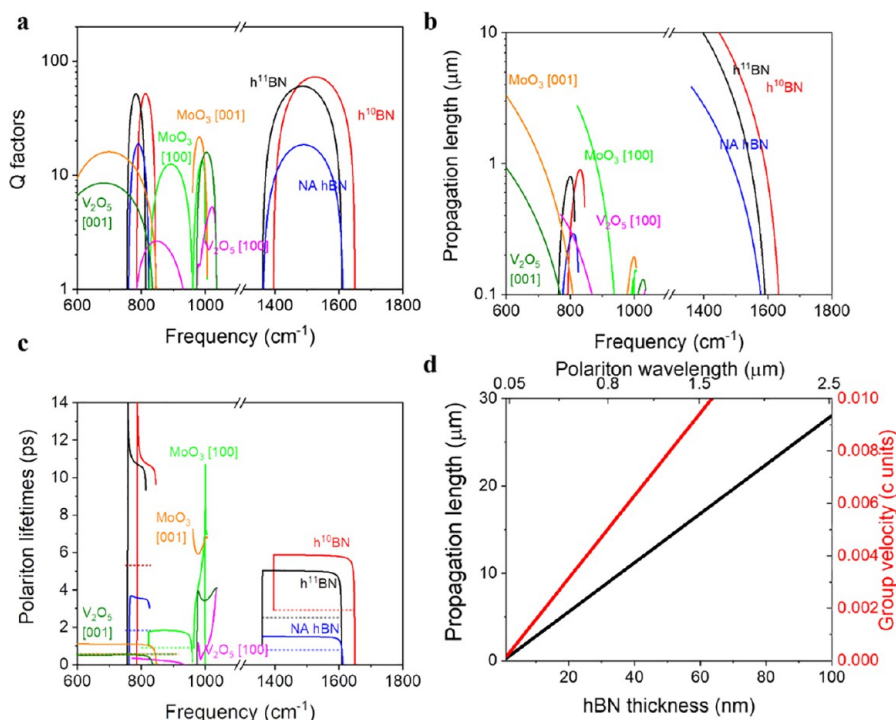


Figure 10. Polariton loss. (a) Q factors of HPhPs supported by different materials. (b) Propagation length of HPhPs supported by different materials. (c) Polariton lifetimes of HPhPs supported by different materials. Corresponding phonon lifetimes are plotted with dashed reference lines. Polariton lifetime is defined as $\tau = L_p/v_g$, where $v_g = \frac{\partial \omega}{\partial k}$ is the group velocity. (d) Propagation length and group velocities of HPhPs supported by h¹⁰BN at 1500 cm⁻¹. Note that the polariton lifetimes and Q -factors are irrelevant to hBN thicknesses.

lengths and higher group velocities (Figure 10d). It should be noted that the polariton lifetime does not change with thickness in this scenario. In addition to HPhP modes, unique anisotropic polaritons supported by off-cut crystals could also provide significant opportunities in loss engineering, such as observed for ghost polaritons supported by off-cut calcite, which reveals long propagation lengths upward of 20 μm . Similarly, the confinement of ghost polaritons is weaker than volume-confined modes in thin slabs, leading to a longer propagation length. Thus, engineering the dispersion and specifically the magnitude of the confinement allows for additionally tuning the propagation lengths to meet the requirements of a specific application. It was recently demonstrated that photonic modes supported by silicon photonic crystals could be hybridized with PhP modes, featuring unidirectional propagation with over 80 μm propagation distances.⁵¹

■ OPPORTUNITIES IN POLARITON ANISOTROPY FOR REALIZING EMERGENT PHENOMENA

Despite the above referenced advances, the community has still barely scratched the surface of the underlying physics and applications enabled by polariton anisotropy. Fruitful directions include identifying new materials, exploring nonlocal effects, and further advancements in twist-optics within heterogeneous structures. Below we highlight some specifics with reference to these directions.

Nondiagonalizable Materials Supporting Low-Loss Polaritons. While significant gains can be made in realizing novel optical phenomena through artificial structuring of materials, it has arguably been through the identification of natural, highly anisotropic materials, where the most recent advances have been identified. Thus, it is reasonable to anticipate that further efforts in this regard will continue to be impactful. For instance, expanding the range of materials probed to lower symmetry crystals, including additional monoclinic and triclinic phases, for both SPhPs and SPPs is of immediate interest, building off the recent work in the β -phase Ga_2O_3 .¹⁸ Understanding the role that the off-diagonal elements of the permittivity tensor play in driving polariton losses, and propagation can provide significant insights into what additional opportunities they can afford. Notably, several 2D materials offer such low symmetry crystal structures, while still maintaining the potential for exfoliating thin films, such as ReS_2 , which is a triclinic, van der Waals crystal with low-energy phonon modes¹⁶⁷ and the expectation of a series of broad bandwidth resonances in the far-infrared.

Nonlocal Effects. As most of the phenomena involved in hybrid materials generally pushes the sizes of structures and layer thicknesses to levels approaching or below that of the fundamental excitations on which they are based (e.g., electronic wave function, phonon wavelength), the role of nonlocal effects in driving emergent phenomena is of critical importance. Practically, this results in changing optical properties as a function of confinement. While such nonlocal effects have been studied in plasmonic systems using cathodoluminescence,^{168,169} s-SNOM,^{170–173} EELS,^{174,175} and polaritonic confinement¹⁷⁶ and theoretically explored using hydrodynamic models,^{177–179} the impact of nonlocality in phononic systems has only recently started to be investigated.^{23,163,164,180} Phononic nonlocality presents a unique phenomenology because, contrary to plasmonic systems that disperse toward the blue with reduced size,

optic phonons have an anomalous dispersion causing them to shift toward the red at large wavevectors, leading to the possibility of resonant energy exchange and even strong coupling between transverse SPhPs and longitudinal phonons.^{122,181,182} The resulting hybrid modes, called longitudinal-transverse phonon polaritons (LTPPs), were initially observed in 4H-SiC crystals¹²² where the long unit cell along the c -axis folds the longitudinal optic phonon dispersion back into the light-line, giving rise to zone-folded LO (ZFLO) phonons.¹⁸³ LTPP modes were then shown to be a general feature of nanostructures with nonlocal length scales, and they were spectroscopically observed in crystalline hybrids.¹⁸⁰ As electrical currents in polar crystals lose energy primarily through the emission of LO phonons via the Fröhlich interaction, it has been theoretically predicted that LTPP modes can be used to alter electron–phonon interactions, resonantly coupling electrical currents to far-field radiation.¹²² Although still in their infancy, the benefits of understanding nonlocality within phononic systems and hybrid structures promises to move beyond phenomena driven exclusively by the bulk permittivity tensors that are well described by effective medium approximations.

Twist-Optics. Related to the creation of hybrid materials is the concept of twistronics. Manipulating the twist angle between the two layers of typically 2D material flakes enables the fine control of the electronic band structure (twistronics), as well as new emergent optical properties.¹⁴⁴ For instance, materials such as bilayer graphene have been shown to display vastly different electronic behaviors from monolayer graphene,¹⁴⁰ ranging from nonconductive to superconductive conditions, with this conductivity sensitively dependent upon the angle between the principal crystal axes of the layers.¹⁸⁴ This concept has been applied to many other 2D materials, revealing exotic phenomena related to magnetism and transport. Note that the twist-optics we discuss here falls into two categories: structures where the properties are dictated by the electromagnetic hybrid (bulk property dictated) or atomic-stacking (atomic-level) methodologies. The former was discussed above, with the exemplary system of twisted layers of stacked MoO_3 and offers significant advantages. However, it is in the latter concept that the properties extend beyond those of the bulk permittivity tensors and emergent properties can be expected. For example, the twisted graphene¹⁸⁴ system can be used as a controllable circuit capable of routing plasmons with nanoscale precision by modifying the twist angle. Further, new collective excitations arising from interband electronic transitions in twisted bilayer graphene have been recently observed^{185,186} and others predicted, which includes chiral plasmons.¹⁸⁷ Other photonic phenomena, such as nonlinear responses, have been demonstrated to be induced in twisted $\text{MoSe}_2/\text{WS}_2$.¹⁸⁸ Thus, even after extensive research efforts, the field of twist-optics is still relatively young, and further theoretical and experimental studies are still required to provide insights into the emergence of optical topological transitions in 2D crystals, as well as the electromagnetic nature of the optical modes involved (note that the surface or volume character of canalized PhPs is still an open question). Further, extension of such twist-optics to incorporate materials of further reduced symmetries, such as exfoliated β - Ga_2O_3 flakes or ReS_2 , will require further developments in our theoretical understanding, while promising opportunities to control the polaritonic properties more precisely.

CONCLUSIONS

Efforts such as those outlined above offer the potential to not only expand the current toolbox of available polaritonic materials, but more broadly to offer insights and understanding to unexplored emergent physics resulting from atomic-scale interactions and the nonlocal effects they induce. During the past two decades the materials and physical understandings of anisotropic polaritons have been evolving quickly, from artificial to natural, from isotropic to uniaxial, biaxial, and more recently low symmetry and off-cut crystals, and the toolboxes to engineer such polaritons are expanding at a similarly fast rate. Despite those achievements, significant efforts are still necessary for this field, including physical understandings, material identifications, and fabrication techniques. The possibility of engineering materials with tailored optical response in the mid-infrared range opens up interesting perspectives for the use of these systems for optoelectronics.¹⁸⁹ The hybridization of longitudinal and transverse degrees of freedom due to nonlocal effects has already been theoretically predicted and experimentally observed in multiple systems.^{22,122,163} We expect it will provide a channel for electrically generated far-field emission of mid-infrared light without requiring complex injection minibands,¹⁹⁰ thus, providing a simpler alternative to quantum cascade lasers. Thus, in concert, the combination of reduced crystal symmetry, hybrid polaritonic and phonon modes, nonlocal effects within near atomic scale systems, and induced anisotropy through the field of twist-optics offer a collective path toward achieving novel optical and electro-optic devices, where light can be generated, manipulated, and directed with nanoscale precision.

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Notes

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