

Reachability Analysis for Attributes in ABAC with Group Hierarchy

Maanak Gupta, *Member, IEEE*, Ravi Sandhu, *Fellow, IEEE*, Tanjila Mawla, James Benson

Abstract—Attribute-based access control (ABAC) models are widely used to provide fine-grained and adaptable authorization based on the attributes of users, resources, and other relevant entities. Hierarchical group and attribute based access control (HGABAC) model was recently proposed which introduces the novel notion of attribute inheritance through group membership. GURA_G was subsequently proposed to provide an administrative model for user attributes in HGABAC, building upon the ARBAC97 and GURA administrative models. The GURA model uses administrative roles to manage user attributes. The reachability problem for the GURA model is to determine what attributes a particular user can acquire, given a predefined set of administrative rules. This problem has been previously analyzed in the literature. In this paper, we study the user attribute reachability problem based on directly assigned attributes of the user and attributes inherited via group memberships. We first define a restricted form of GURA_G, called rGURA_G scheme, as a state transition system with multiple instances having different preconditions and provide reachability analysis for each of these schemes. In general, we show PSPACE-complete complexity for all rGURA_G schemes. We further present polynomial time algorithms with empirical experimental evaluation to solve special instances of rGURA_G schemes under restricted conditions.

Index Terms—Access Control, ABAC model, Reachability Analysis, Group Hierarchy, Attributes Inheritance, Attributes Administration.

1 INTRODUCTION

ATTRIBUTE-based access control (ABAC) is considered as an important authorization system among practitioners and researchers. The system offers fine-grained and adaptable access control solutions based on the characteristics, referred to as attributes, of several entities. ABAC systems provide a flexible and scalable approach to secure resources in distributed environments and overcome some of the shortcomings of traditional discretionary access control (DAC) [1], mandatory access control (MAC) [2] and role based access control (RBAC) [3] models. Several attribute based access control models have been formulated [4], [5], [6], [7], [8], [9], [10], [11], [12], [13], [14], [15], [16], [17], [18], [19], [20], [21] but a strong consensus on its definitive characteristics is still to be achieved. More recently, hierarchical group and attribute based access control model (HGABAC) [22] was proposed, which introduced the notion of user and object groups to assign attributes to users and objects respectively. In this model, besides the direct assignment of attributes to users or objects, groups are also assigned attributes, which are then assigned to users and objects through corresponding group memberships. The most important advantage of this model is the ease of administration, since multiple attributes can be assigned or removed from users or objects through single administrative operation. The administrative model for HGABAC, referred as GURA_G, was defined in [23], to control user attribute assignment based on specified precondition rules and administrative roles. This model has three sub-models UAA (user attribute assignment), UGAA (user group attribute assignment) and UGA (user to user-group

assignment) which assigns attributes to users directly or indirectly through groups. The model extends well-known ARBAC97 [24] administrative model and recently published GURA administrative model [25] by introducing administration of attributes for user-groups and managing user to groups memberships.

In ABAC, the attributes of an entity are critical in determining its permissions. Therefore, it is an important question to compute the attribute values that an entity can acquire through the combination of administrative roles and rules. In the context of GURA_G, it is imperative to understand the set of attribute values a user can get based on direct assignment or via group memberships. Group hierarchy also exists in the HGABAC operational model which further complicates computation of the possible effective attribute values of a user. Although security administrators are trusted to assign attributes correctly, it is still desirable to understand the eventual set of attribute values that a user can acquire through multiple direct and indirect assignments. Such analysis can also help to identify a sequence of administrative actions required by administrators to assign certain attribute values to the users. It further allows administrators to know the future attribute values an entity can achieve based on predefined administrative rules, which can help them to understand if certain permissions can ever be granted to an entity.

As the number of attributes, attribute values and administrative rules become large, certain anomalies become hard to detect just by simple inspection. For example, suppose an administrative user having role RoomAdmin is allowed to add user attribute roomAcc with value 1.02 to a user only if the user's attribute status has value Grad and the user does not currently have roomAcc 2.01. Further, a user can be assigned status attribute with value Grad only through group G₁ membership since there is no direct assignment administrative rule for status attribute. Another administrative rule assigns roomAcc 2.01 to a group junior to G₁, thereby getting G₁ with roomAcc value 2.01. Now if a user is assigned to user-group G₁, she will get all G₁'s attributes, including roomAcc with value

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2.01. It might seem that user will not be able to get roomAcc value 1.02 and 2.01 together. However, it is possible if the junior group to G_1 is assigned value 2.01 after the user is assigned to user-group G_1 . Such security policy anomalies can be discovered with the help of reachability analysis, which checks if entities can get certain values together or whether the entity will get particular values based on the set of administrative rules defined through administrative models.

In this paper we analyze the attribute reachability analysis focusing on the effective attributes of the user achieved through direct assignment and through user-group memberships. This work extends the reachability analysis [26] done for GURA administrative model [25], where the attributes were only directly assigned to users without the concept of group memberships. In our analysis, we have defined a restricted $GURA_G$ model, called $rGURA_G$, which considers a subset of preconditions which can be created in $GURA_G$. We abstract $rGURA_G$ into a state transition system and specify three separate instances— $rGURA_{G_0}$, $rGURA_{G_1}$ and $rGURA_{G_{1+}}$ —to cover different set of prerequisite conditions for attributes assignments to a user or a group, and also for user to group membership assignment. Our reachability analysis primarily focuses on the effective set of attributes of users which is the union of direct attributes and attributes attained by group membership. We have defined reachability queries which is the required set of effective attributes a user can achieve in any target state. Two different types of reachability queries are discussed, one with the exact values and another with the superset of attribute values. We will show that the general reachability problem for $rGURA_G$ schemes is PSPACE-complete. We further identify certain more restricted cases of $rGURA_G$ schemes where the reachability problem can be solved in polynomial time. For such instances we will provide algorithms and a sequence of administrative requests (referred as reachability plan) to satisfy the reachability query.

The rest of this paper is organized as follows. Section 2 reviews the related work. In Section 3, we review the HGABAC model and $GURA_G$ administrative model. Section 4 discusses the generalized restricted $rGURA_G$ scheme and its instances. In Section 5, we formally define our user attribute reachability problem. Formal proofs for general $rGURA_G$ schemes are discussed in Section 6. Section 7 presents polynomial algorithms for some restricted versions of $rGURA_G$ schemes followed by example problems instances in Section 8 and experimental results in Section 9. Section 10 concludes this paper.

2 RELATED WORK

Reachability analysis for user attributes was first studied by Jin et al [26], based on the GURA administrative model [25]. In this analysis, attribute values are assigned to users directly based on certain attribute-based prerequisite conditions and by administrators assuming roles. This work proves PSPACE-complete complexity for generalized GURA scheme and also presents polynomial algorithms for some conditional cases. Our work extends the aforementioned reachability analysis where attributes are assigned to users as well as to groups to which users are members. This assignment of attributes to groups provides administrative benefits in addition and removal of multiple attributes to users with a single administrative operation.

Security policies have been widely analysed in several works including [27], [28], [29], [30], [31], [32], [33], [34], [35], [36], [37]. The safety analysis problem goes back to 1970's. In general,

the safety of access control matrix (ACM) model was shown to be undecidable in [27]. Tripunitara and Li presented an important theoretical comparison of expressive powers of different access control models in [28]. Many of our notations in this paper are adapted from this work. The same authors in [29] defined restricted forms of ARBAC97 (AATU and AAR) and provided algorithms for analysis problems including safety and availability in restricted forms. This work extends results from trust management policies in [30] where safety and availability security analysis on delegation of authority is discussed. The schematic protection model (SPM) [31] introduced typed security entities where each entity is associated with a security type, which remains unchanged. Sasturkar et al [32] analyse ARBAC97 administrative policies to determine reachability and availability problems, by establishing connections between artificial intelligence planning problem. Jha et al [36] classified analysis problems related to RBAC and claimed PSPACE-complete solutions for unrestricted classes whereas NP-complete and polynomial time algorithms for restricted subclasses. Lipton et al [34] presented a linear time algorithm for take and grant system. Alloy language is used for specification of role based system and analysis is done using Alloy constraint analyser in [35]. Recently, Rajkumar and Sandhu discussed safety problem for pre-authorization sub-model for $UCon_{ABC}$ in [37].

Jajodia et al [38] presented a logical language to express positive, negative and derived authorization policies, and provided polynomial algorithms to check completeness and consistency. Cholvy and Cuppens [39] discussed the problem of policy consistency and offered a methodology to solve it. They further suggested the use of roles priorities to resolve normative conflicts in policies. [40] provides a method to transform policy specifications into event calculus based formal notation. It further describes the use of abductive logical reasoning to perform a priori analysis of various policy specifications. Jaeger et al [41] presented the concept of access control space and its use in managing access control policies. These spaces are used to represent permission assignment to subjects or roles. Authors in [42] presented decision diagram based algorithms to analyze XACML based policies and compute the semantic differencing information between versions of policies. Stoller et al [43] provided algorithms for ARBAC97 policies limited to rules with one positive precondition and unconditional role revocations. Same authors in [44] defined PARBAC (parameterized ARBAC) and determined user-reachability problem as undecidable over an infinite types of parameter. It further assumed all parameters as atomic-valued and are changed when the role is modified. Gupta et al [45] discussed rule-based administrative model to control addition and removal of facts (attributes) and rules. It further proposed an abductive algorithm which can analyse policies even when the facts (attributes) are unavailable based on computation of minimal sets of facts. The work in [46] provides analysis of expressive power of generalized temporal role-based access control (GTRBAC) which offers a set temporal constraints to specify fine grained time based policies.

Several works [23], [24], [25], [47] have been presented to discuss administrative models for well known access control models. ARBAC97 [24] discusses the user to role assignment based on the administrative rules comprising of administrative roles and prerequisite conditions based on roles. The $GURA_G$ administrative model [23] provides a generalized administrative model for attributes based access control models by asserting role as one of the several user attributes. These works define attribute

as \succeq_{ug} , where $ug_1 \succeq_{ug} ug_2$ represents ug_1 is senior to ug_2 or ug_2 is junior to ug_1 . As shown in gray the area of Figure 2, $UGH = \{(G_1, G_1), (G_2, G_2), (G_3, G_3), (G_1, G_2), (G_1, G_3)\}$. This UGH relation results in inheritance of attributes from junior to senior group (will discuss in a moment).

Attribute values can be directly assigned to user and user groups which is denoted by function att in UA. As defined in Figure 2 and Table 2, user Bob is directly assigned $\{c, java\}$ for attribute function skills. Similarly, other direct attributes are given for Bob and user groups G_1, G_2, G_3 . The function $directUg$ specifies the user groups to which the user is directly assigned. In our example, Bob is directly assigned to user group G_1 . We also define the effective user groups of the user (denoted by $effUg$), which states all the groups to which the user is either directly or indirectly assigned via UGH relation. Effective user group for Bob will be $\{G_1, G_2, G_3\}$, since Bob is directly assigned to G_1 and G_1 has junior groups as G_2 and G_3 .

The effective values of an attribute att ($effUG_{att}$) for a user group is the union of the user's direct attribute values and the effective values of all its junior groups in UGH relation. Note that this definition is well formed since \succeq_{ug} is a partial order. For the minimal groups ug_j in this ordering, we have $effUG_{att}(ug_j) = att(ug_j)$, giving us base cases for this recursive definition. For simplicity, we defined $e_{att}(ug) = effUG_{att}(ug)$ for $ug \in UG$. Therefore, for attribute $roomAcc$, effective values for user group G_2 is $e_{roomAcc}(G_2) = \{3.02\}$. This value is same as its direct value for $roomAcc$ attribute, since G_2 has no junior group in UGH. For user group G_1 , $e_{roomAcc}(G_1) = \{2.03, 2.04, 3.02\}$ as it inherits values from G_2 and G_3 . The function $effU_{att}$ maps the user to the effective values for attribute att , which is the union of its direct values and the effective values of att for all its direct groups. For convenience we defined $e_{att}(u) = effU_{att}(u)$ for user $u \in U$ and as shown in Table 2, the effective values for attribute $roomAcc$ for user Bob, written as $e_{roomAcc}(Bob) = \{1.2, 2.03, 2.04, 3.02\}$ which is the union of its directly assigned value for $roomAcc$ and values inherited from group G_1 . Similarly other effective attributes for user Bob can be calculated. The prime benefit of HGABAC model, which is easy assignment of multiple attributes to a user with user group memberships, is reflected in this function where user u is assigned multiple attributes with direct group membership of G_1 .

Subject $s \in S$ created by the user $u \in U$ will then assume a subset of all effective attributes of user u . Similar effective attributes can be assigned to objects, which is out of scope of our reachability analysis and is not discussed. Authorization policies are pre-defined in the system, using propositional logic formula, for each operation in OP (set of operations) by security administrators, which determine if a subject is allowed to perform operations on objects, based on their effective attributes.

Note: HGABAC only allows set-valued attributes. ABAC models generally allow set-valued as well as atomic-valued attributes (for example [4]). Inheritance of values via group membership for an atomic-valued attribute is problematic since such attributes can have only one value. Hence, while the GURA administrative model allows both atomic and set valued attributes the HGABAC only allows set values.

3.2 GURA_G Administrative Model

The GURA_G administrative model [23] was proposed to regulate the assignment of user attribute values in HGABAC model via

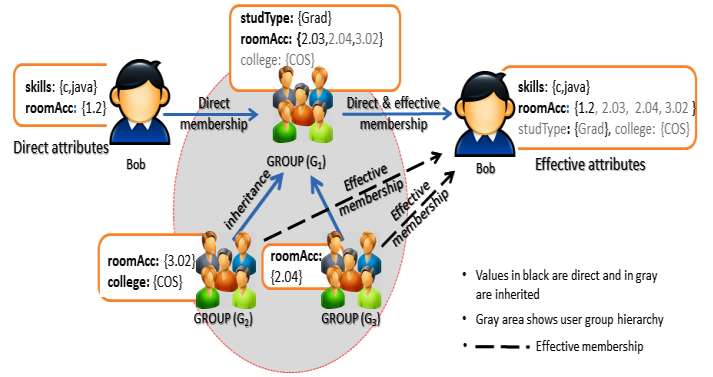


Fig. 2: Example User and User Group Attributes

TABLE 2: Example Configuration as Defined in Fig 2

Basic Sets and Relations

- $U = \{Bob\}$, $UG = \{G_1, G_2, G_3\}$.
- $UA = \{skills, roomAcc, studType, college\}$.
- SCOPE of each att in UA, denoted by $SCOPE_{att}$:
 $studType = \{Grad, UnderGrad\}$, $college = \{COS, COE, BUS\}$
 $skills = \{c, c++, java\}$, $roomAcc = \{1.2, 2.03, 2.04, 3.02\}$.
- UGH is given in Figure 2, highlighted in gray area.

Direct Attributes

- $skills(Bob) = \{c, java\}$, $roomAcc(Bob) = \{1.2\}$,
- $roomAcc(G_2) = \{3.02\}$, $college(G_2) = \{COS\}$,
- $roomAcc(G_3) = \{2.04\}$, $studType(G_1) = \{Grad\}$,
- $roomAcc(G_1) = \{2.03\}$.

Direct User Groups

- $directUg(Bob) = \{G_1\}$.

Effective User Groups

- $effUg(Bob) = \{G_1, G_2, G_3\}$

Effective User Group Attributes

- $e_{roomAcc}(G_2) = \{3.02\}$, $e_{college}(G_2) = \{COS\}$,
- $e_{roomAcc}(G_3) = \{2.04\}$, $e_{studType}(G_1) = \{Grad\}$,
- $e_{roomAcc}(G_1) = \{2.03, 2.04, 3.02\}$, $e_{college}(G_1) = \{COS\}$.

Effective User Attributes

- $e_{skills}(Bob) = \{c, java\}$,
- $e_{roomAcc}(Bob) = \{1.2, 2.03, 2.04, 3.02\}$,
- $e_{studType}(Bob) = \{Grad\}$, $e_{college}(Bob) = \{COS\}$.

direct user attributes, user-group attributes and user to group memberships. For convenience we understand the term “assignment of attributes” to mean “assignment of attribute values.” The model is inspired by ARBAC97 [24] and GURA [25] administrative models, where administrative roles and current attributes of user and groups or user to group memberships are considered to make future attributes or groups assignments. Administrative role hierarchy also exists in the system where senior administrator roles inherit permissions from junior roles. The GURA_G model has three sub models (shown in Figure 1): user attribute assignment (UAA), user group attribute assignment (UGAA) and user to group assignment (UGA), which regulates the direct and effective attributes of users. It should be noted that user group hierarchy (UGH) is considered fixed in the system and is not modified. Each of these sub models have different sets of administrative relations and preconditions definition using policy language as discussed in following subsections.

The main difference between GURA and GURA_G is that GURA_G includes the assignment of attributes to groups and user to group memberships. Further, the prerequisite conditions specified in GURA_G are more expressive, as it also checks

TABLE 3: Administrative Requests

In the following requests: $ar \in AR, att \in UA, val \in SCOPE_{att}, u \in U, ug \in UG$	
– For User Attributes	$add(ar, u, att, val)$ $delete(ar, u, att, val)$
– For User Group Attributes	$add(ar, ug, att, val)$ $delete(ar, ug, att, val)$
– For User to User-Group Membership	$assign(ar, u, ug)$ $remove(ar, u, ug)$

TABLE 4: GURA_G Administrative Model

– User Attribute Assignment (UAA):	
For each att in UA,	
	$canAddU_{att} \subseteq AR \times C \times SCOPE_{att}$
	$canDeleteU_{att} \subseteq AR \times C \times SCOPE_{att}$
– User Group Attribute Assignment (UGAA):	
For each att in UA,	
	$canAddUG_{att} \subseteq AR \times C \times SCOPE_{att}$
	$canDeleteUG_{att} \subseteq AR \times C \times SCOPE_{att}$
– User to User Group Assignment (UGA):	
	$canAssign \subseteq AR \times C \times UG$
	$canRemove \subseteq AR \times C \times UG$

the current effective attributes or effective group memberships of entities to make future assignments.

3.2.1 Administrative Requests

Definition 1 (Administrative Requests). The attributes and group memberships of entities are changed by administrative request made by administrators with certain administrative roles as defined in Table 3, where AR is the finite set of administrative roles. The administrative request $add(ar, u, att, val)$ is made by administrator with role ar to add value val to attribute att of user u . Similar administrative requests are used for groups also. Administrative requests assign and remove are required for managing group memberships. Each administrative request can add or delete a single attribute value from a user or group.

3.2.2 Administrative Rules

Definition 2 (Administrative Rules). Administrative rules are tuples in administrative relations which specify conditions under which administrative requests are authorized. Each of the three sub-models (UAA, UGAA, UGA) in GURA_G model have administrative relations to define these rules.

The UAA sub-model deals with addition or deletion of attributes from the user. It has two administrative relations shown in Table 4, where a rule $\langle ar, c, val \rangle \in canAddU_{att}$ authorizes request $add(ar, u, att, val)$ if user u satisfies precondition c . Similarly, rule $\langle ar, c, val \rangle \in canDeleteU_{att}$ authorizes $delete(ar, u, att, val)$ requests if user u satisfies precondition c . In UAA, the precondition $c \in C$ includes only current direct and effective attributes of user u . Similar relations also exist for administering attributes of user groups as discussed in sub-model

UGAA. In UGAA, $c \in C$ involves current direct or effective attributes of the group whose attributes are modified.

The UGA sub-model has two relations shown in lower part of Table 4. The rule $\langle ar, c, ug \rangle \in canAssign$ authorizes user to group assignment request $assign(ar, u, ug)$ if user u satisfies the precondition c . Similarly rule $\langle ar, c, ug \rangle \in canRemove$ authorizes remove request $remove(ar, u, ug)$ if user u satisfies precondition c . The precondition $c \in C$ involves both current direct or effective attributes and groups of user u .

The expressive power of the GURA_G model is primarily determined by the richness of the policy language used to define the preconditions C in Table 4. The most general language for this purpose is defined in [23], similar to the most general language of [25] (but without atomic attributes).

Note: In the original GURA_G definition [23], the administrative relations of Table 4 are defined with $2^{SCOPE_{att}}$ substituted for $SCOPE_{att}$ and 2^{UG} substituted for UG. With the modification of Table 4 the administrative relations can grow linearly in the size of $SCOPE_{att}$ and UG. This does not materially impact the complexity analysis of the reachability problem.

3.2.3 GURA_G scheme

For purpose of our reachability analysis, we express the GURA_G model according to the notations developed in [28], following the treatment in [26]. The GURA_G scheme is presented as a state transition system where each state consists of direct attribute assignments for each attribute of every user and group, and also each user to groups membership. A transition between states occurs when an authorized administrative request changes either direct user or group attribute, or changes user to group membership. The general definition for GURA_G scheme is as follows.

Definition 3 (GURA_G Scheme). A GURA_G scheme is a state transition system $\langle U, UA, AR, SCOPE, UG, \succeq_{ug}, \Psi, \Gamma, \delta \rangle$ where,

- (i) $U, UA, AR, UG, \succeq_{ug}$ are as defined in Tables 1 and 3.
- (ii) $SCOPE = \langle SCOPE_{att_1} \dots SCOPE_{att_n} \rangle$ where $att_i \in UA$, is the collection of scopes of all attributes.
- (iii) Ψ is the collection of all administrative rules in UAA, UGAA and UGA sub-models.
- (iv) Γ and δ are set of states and transition function respectively, defined in following parts of this subsection.

3.2.4 Direct State

Γ is the finite set of states where each state $\gamma \in \Gamma$ records directly assigned attributes of each user and user group, along with user to groups membership. The direct user attribute assignment in state γ , denoted by UAA_γ , contains tuples of the form $\langle u, att, val \rangle$ for every $u \in U$ and every $att \in UA$ such that $att(u) = val$ and $val \in Range(att)$ in state γ . To ensure uniqueness of user attribute values we require the following.

$$\langle u, att, val_1 \rangle \in UAA_\gamma \wedge \langle u, att, val_2 \rangle \in UAA_\gamma \Rightarrow val_1 = val_2$$

Similarly, direct user group attribute assignment in state γ , denoted by $UGAA_\gamma$, contains tuples of the form $\langle ug, att, val \rangle$ for every $ug \in UG$ and every $att \in UA$ such that $att(ug) = val$ and $val \in Range(att)$ in state γ , with the following uniqueness requirement.

$$\langle ug, att, val_1 \rangle \in UGAA_\gamma \wedge \langle ug, att, val_2 \rangle \in UGAA_\gamma \Rightarrow val_1 = val_2$$

TABLE 5: Transition Function

(1) γ_1 and γ_2 are the source and target states respectively. (2) Let $: ar \in AR, u \in U, ug \in UG, att \in UA, val' \in SCOPE_{att}, ug' \in UG$. (3) $Satisfy_u: U \times C \times \Gamma \rightarrow \{\mathbf{true}, \mathbf{false}\}$, returns true if user $u \in U$ satisfies precondition $c \in C$ in state $\gamma \in \Gamma$, else false . (4) $Satisfy_{ug}: UG \times C \times \Gamma \rightarrow \{\mathbf{true}, \mathbf{false}\}$, returns true if user group $ug \in UG$ satisfies precondition $c \in C$ in state $\gamma \in \Gamma$, else false . (5) $Satisfy_{u-ug}: U \times C \times \Gamma \rightarrow \{\mathbf{true}, \mathbf{false}\}$, returns true if user $u \in U$ satisfies precondition $c \in C$ in state $\gamma \in \Gamma$, else false .		
Request	Pre-Conditions	Target State
$add(ar, u, att, val')$	$\exists \langle ar, c, val' \rangle \in \text{canAddU}_{att}.$ $(Satisfy_u(u, c, \gamma_1) \wedge val' \notin att_{\gamma_1}(u))$	$att_{\gamma_2}(u) = att_{\gamma_1}(u) \cup \{val'\},$ $att_{\gamma_2}(ug) = att_{\gamma_1}(ug), \text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u),$ $UAA_{\gamma_2} = UAA_{\gamma_1} \setminus \langle u, att, att_{\gamma_1}(u) \rangle \cup \langle u, att, att_{\gamma_2}(u) \rangle.$
$delete(ar, u, att, val')$	$\exists \langle ar, c, val' \rangle \in \text{canDeleteU}_{att}.$ $(Satisfy_u(u, c, \gamma_1) \wedge val' \in att_{\gamma_1}(u))$	$att_{\gamma_2}(u) = att_{\gamma_1}(u) \setminus \{val'\},$ $att_{\gamma_2}(ug) = att_{\gamma_1}(ug), \text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u),$ $UAA_{\gamma_2} = UAA_{\gamma_1} \setminus \langle u, att, att_{\gamma_1}(u) \rangle \cup \langle u, att, att_{\gamma_2}(u) \rangle.$
$add(ar, ug, att, val')$	$\exists \langle ar, c, val' \rangle \in \text{canAddUG}_{att}.$ $(Satisfy_{ug}(ug, c, \gamma_1) \wedge val' \notin att_{\gamma_1}(ug))$	$att_{\gamma_2}(ug) = att_{\gamma_1}(ug) \cup \{val'\},$ $att_{\gamma_2}(u) = att_{\gamma_1}(u), \text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u),$ $UGAA_{\gamma_2} = UGAA_{\gamma_1} \setminus \langle ug, att, att_{\gamma_1}(ug) \rangle \cup \langle ug, att, att_{\gamma_2}(ug) \rangle.$
$delete(ar, ug, att, val')$	$\exists \langle ar, c, val' \rangle \in \text{canDeleteUG}_{att}.$ $(Satisfy_{ug}(ug, c, \gamma_1) \wedge val' \in att_{\gamma_1}(ug))$	$att_{\gamma_2}(ug) = att_{\gamma_1}(ug) \setminus \{val'\},$ $att_{\gamma_2}(u) = att_{\gamma_1}(u), \text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u),$ $UGAA_{\gamma_2} = UGAA_{\gamma_1} \setminus \langle ug, att, att_{\gamma_1}(ug) \rangle \cup \langle ug, att, att_{\gamma_2}(ug) \rangle.$
$assign(ar, u, ug')$	$\exists \langle ar, c, ug' \rangle \in \text{canAssign}.$ $(Satisfy_{u-ug}(u, c, \gamma_1) \wedge ug' \notin \text{directUg}_{\gamma_1}(u))$	$\text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u) \cup \{ug'\}$ $att_{\gamma_2}(u) = att_{\gamma_1}(u), att_{\gamma_2}(ug) = att_{\gamma_1}(ug),$ $UGA_{\gamma_2} = UGA_{\gamma_1} \setminus \langle u, \text{directUg}_{\gamma_1}(u) \rangle \cup \langle u, \text{directUg}_{\gamma_2}(u) \rangle.$
$remove(ar, u, ug')$	$\exists \langle ar, c, ug' \rangle \in \text{canRemove}.$ $(Satisfy_{u-ug}(u, c, \gamma_1) \wedge ug' \in \text{directUg}_{\gamma_1}(u))$	$\text{directUg}_{\gamma_2}(u) = \text{directUg}_{\gamma_1}(u) \setminus \{ug'\}$ $att_{\gamma_2}(u) = att_{\gamma_1}(u), att_{\gamma_2}(ug) = att_{\gamma_1}(ug),$ $UGA_{\gamma_2} = UGA_{\gamma_1} \setminus \langle u, \text{directUg}_{\gamma_1}(u) \rangle \cup \langle u, \text{directUg}_{\gamma_2}(u) \rangle.$

Finally, direct user to group assignment in state γ , denoted UGA_γ , contains tuples of the form $\langle u, val \rangle$ for every $u \in U$ such that $\text{directUg}(u) = val$ and $val \in 2^{UG}$ in state γ , with the following uniqueness requirement.

$$\langle u, val_1 \rangle \in UGA_\gamma \wedge \langle ug, val_2 \rangle \in UGA_\gamma \Rightarrow val_1 = val_2$$

Note that information in a state can be used to calculate the effective attributes for user or group and effective user to groups membership in that state. For convenience we understand the notation $att_\gamma(u)$, $att_\gamma(ug)$ and $\text{directUg}_\gamma(u)$ to denote the values of these functions in state γ for $u \in U$ and $ug \in UG$.

3.2.5 Transition Function

Any change in the direct state records (UAA_γ , $UGAA_\gamma$, UGA_γ) will transform the current state to a new state. The transition function specifies the change from one state to another in a $GURA_G$ system based on current direct or effective values and administrative requests, as shown in Table 5. Formally, $\delta: \Gamma \times \text{REQ} \rightarrow \Gamma$, where REQ is the set of possible administrative requests.

4 RESTRICTED GURA_G (rGURA_G)

In this section, we introduce a restricted form of $GURA_G$ administrative model, called $rGURA_G$, used in our attribute reachability analysis. This restricted form allows a subset of the precondition language defined for $GURA_G$ [23], whereby our analysis also establishes lower bound results on the complexity analysis for richer $GURA_G$ model. We first present a generalized policy language for $rGURA_G$, followed by three specific instances— $rGURA_{G_0}$, $rGURA_{G_1}$, and $rGURA_{G_{1+}}$.

The left side of Figure 3 shows the relation between these schemes, while the right side shows the $rGURA$ schemes discussed in [26]. At a high level, $rGURA_{G_0}$ and $rGURA_{G_1}$ add group attributes respectively to $rGURA_0$ and $rGURA_1$, while $rGURA_{G_{1+}}$ further adds administration of user membership in groups. Thereby, in $rGURA_{G_0}$ and $rGURA_{G_1}$ the administrative relations canAssign and canRemove are empty whereas they are populated in $rGURA_{G_{1+}}$. Table 6 provides example administrative rules for each $rGURA_G$ instance, as will be explained below.

Definition 4 (rGURA_G Scheme). The $rGURA_G$ scheme uses the policy grammar below, to specify preconditions C in Table 4,

$$\varphi ::= \neg \varphi \mid \varphi \wedge \varphi \mid svalue \in \text{direct} \mid svalue \in \text{effective} \\ svalue ::= sval_1 \mid sval_2 \mid \dots \mid sval_m$$

where $SCOPE_{att} = \{sval_1, sval_2, \dots, sval_m\}$. The two non-terminals direct and effective , are individually defined in its three instances— $rGURA_{G_0}$, $rGURA_{G_1}$ and $rGURA_{G_{1+}}$ —in following subsections.

4.1 The rGURA_{G₀} Scheme

In $rGURA_{G_0}$ scheme, preconditions for rules in canAddU_{att} and canDeleteU_{att} relations only allow the same attribute att whose value is added or deleted from user. Therefore, conditions for user u have non-terminals direct and effective defined as follows.

$$\text{direct} ::= att(u) \quad \& \quad \text{effective} ::= e_att(u)$$

Similarly, the administrative relations in canAddUG_{att} and canDeleteUG_{att} for user group ug have direct and effective defined as follows.

$$\text{direct} ::= att(ug) \quad \& \quad \text{effective} ::= e_att(ug)$$

TABLE 6: Example Rules in rGURA_{G_0} , rGURA_{G_1} and $\text{rGURA}_{G_{1+}}$ Schemes

Relation	Admin Role	Pre-requisite Condition	Value
Rules in rGURA_{G_0} scheme			
canAddU_{skills}	DeptAdmin	$c \in e_{skills}(u) \wedge \neg (\text{java} \in skills(u))$	c++
$\text{canDeleteU}_{roomAcc}$	BuildAdmin	$3.02 \in e_{roomAcc}(u)$	1.2
$\text{canAddUG}_{college}$	UnivAdmin	$\neg (\text{COE} \in college(ug))$	COS
$\text{canDeleteUG}_{roomAcc}$	BuildAdmin	$2.04 \in e_{roomAcc}(ug)$	2.03
Rules in rGURA_{G_1} scheme further add			
$\text{canAddU}_{studType}$	DeptAdmin	$\text{java} \in e_{skills}(u) \wedge 2.03 \in roomAcc(u)$	Grad
$\text{canDeleteU}_{roomAcc}$	BuildAdmin	$3.02 \in roomAcc(u) \wedge \text{COS} \in college(u)$	3.02
canAddUG_{skills}	DeptAdmin	$\text{COS} \in college(ug) \wedge \text{UnderGrad} \in e_{studType}(ug)$	java
$\text{canDeleteUG}_{college}$	UnivAdmin	$2.04 \in e_{roomAcc}(ug) \wedge 2.03 \in e_{roomAcc}(ug)$	BUS
Rules in $\text{rGURA}_{G_{1+}}$ scheme further add			
canAssign	DeptAdmin	$1.02 \in e_{roomAcc}(u) \wedge \neg (\text{BUS} \in college(u)) \wedge G_2 \in \text{directUg}(u)$	G_1
canRemove	GroupAdmin	$G_1 \in \text{effUg}(u) \wedge G_2 \in \text{directUg}(u)$	G_2

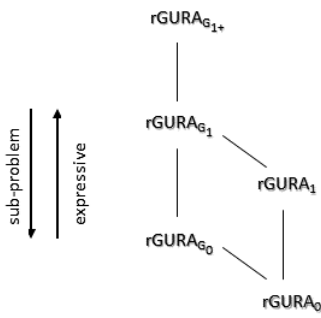


Fig. 3: rGURA_G (Left Side) and rGURA (Right Side) Schemes

The examples for rGURA_{G_0} shown in Table 6 conform to these restrictions. Note that the attribute being updated is given as the subscript in the Relation column and the conditions in the Pre-requisite Condition column only involve this attribute.

4.2 The rGURA_{G_1} Scheme

In rGURA_{G_1} scheme, the precondition can include any attribute from the set of attributes. Therefore, conditions in rules for canAddU_{att} and canDeleteU_{att} relations for user u have direct and effective defined as follows where $att_i \in \text{UA}$.

$$\text{direct} ::= att_i(u) \quad \& \quad \text{effective} ::= e_{att_i}(u)$$

Similarly, the conditions for user group ug in relations canAddUG_{att} and canDeleteUG_{att} have non-terminals direct and effective defined as follows.

$$\text{direct} ::= att_i(ug) \quad \& \quad \text{effective} ::= e_{att_i}(ug)$$

The added rules for rGURA_{G_1} in Table 6 illustrate this, where the preconditions involve attributes other than the one being updated. The earlier rules for rGURA_{G_0} continue to be valid for rGURA_{G_1} .

4.3 The $\text{rGURA}_{G_{1+}}$ Scheme

The $\text{rGURA}_{G_{1+}}$ scheme allows changes in user group memberships besides modifying the attributes of user and user groups. Therefore, in addition to the grammar supported by rGURA_{G_1} scheme, $\text{rGURA}_{G_{1+}}$ also includes user's direct or effective group memberships as preconditions in rules for canAssign and canRemove administrative relations. The additional grammar to specify such preconditions is specified below:

$$\varphi ::= ug \in \text{directUg}(u) \mid ug \in \text{effUg}(u)$$

In Table 6, rule in canAssign includes effective values for $roomAcc$, direct values for $college$ attribute and direct groups of user u .

5 REACHABILITY PROBLEM DEFINITION

In this section, we provide a formal definition of our attribute reachability problem along with the reachability query and different query types supported in our analysis. The general approach is similar to that of [26], except that atomic-valued attributes are excluded (as noted in Section 3.1.2) and reachability is defined with respect to effective rather than direct attributes (Research in [26] does not have the notion of effective attributes).

The user attribute reachability analysis problem (or reachability problem) is based on the effective attributes of the user. Informally, the problem can be stated as: Given an initial transition system state with a set of attribute assignments of the user, the user's group memberships and the attributes of all the user's member groups, can administrators with a given set of administrative roles issue one or more administrative requests, which transition to a target state having the set of specified effective attributes for that user? We highlight some simplifications in our reachability analysis process. First, as the changes made to the attributes or group memberships of one user do not affect the attributes or group memberships of another user, our analysis will only determine the effective attributes of a single user of interest and hence will only consider attribute assignment of that user, its group memberships and attributes of these groups. Formally, we assume $U = \{u\}$ in our analysis [26]. Second, as the reachability analysis focuses on powers of a certain set of administrative roles $\text{SUBAR} \subseteq \text{AR}$, we do not consider the administrative rules specified for roles outside of SUBAR. In other words, we can assume $\text{AR} = \text{SUBAR}$. These simplifications gives our analysis more convenient statements without losing generality.

Definition 5 (Reachability Query). A reachability query $q \in Q$ specifies a subset of effective values of a user for some attributes in any target state. Formally,

$$q \subseteq \{\langle u, e_{att}, vset \rangle \mid u \in U, att \in \text{UA}, vset \in \text{Range}(att)\}$$

In the example problems discussed in Section 8, we will use the following notation to specify our query, which is equivalent to the notation defined above:

$$q \subseteq \{e_att(u) = vset \mid u \in U, att \in UA, vset \in Range(att)\}$$

For example,

$$q = \{\langle u, e_roomAcc, \{2.04\} \rangle, \langle u, e_skills, \{c\} \rangle, \langle u, e_college, \{COS, COE\} \rangle\}$$

is equivalent to

$$q = \{e_roomAcc(u) = \{2.04\}, e_skills(u) = \{c\}, e_college(u) = \{COS, COE\}\}.$$

Two types of reachability query are defined in the system. A query is called “strict” satisfied if every effective attribute value specified in the query is exactly the same as that in the target state. A query is called “relaxed” satisfied by the user if in the target state every effective attribute value of the user is a superset of the corresponding attribute values specified in the reachability query. For example, let $UA = \{skills\}$, $U = \{Bob\}$ and reachability query $q = \langle Bob, e_skills, \{c, java\} \rangle$. For strict query type, q can be satisfied in states $\gamma' \in \Gamma$ where $e_skills_{\gamma'}(u) = \{c, java\}$. In relaxed query type, q can be satisfied by any state $\gamma'' \in \Gamma$ where $e_skills_{\gamma''}(u) = setval$ and $\{c, java\} \subseteq setval$. For ease of understanding, we represent the effective value of attribute att for user u in state $\gamma \in \Gamma$ as $e_att_{\gamma}(u)$. The formal definition for reachability query types is given below:

Definition 6 (Reachability Query Types). For any rGURA_G scheme $\langle U, UA, AR, SCOPE, UG, \succeq_{ug}, \Psi, \Gamma, \delta \rangle$, we formally define two Reachability Query Types as:

- $RP_{=}$ or strict satisfied queries have the entailment function $\vdash_{RP_{=}}: \Gamma \times Q \rightarrow \{\mathbf{true}, \mathbf{false}\}$ which returns **true** (i.e., $\gamma \vdash_{RP_{=}} q$) if $\forall \langle u, e_att, vset \rangle \in q. e_att_{\gamma}(u) = vset$.
- RP_{\supseteq} or relaxed satisfied queries have the entailment function $\vdash_{RP_{\supseteq}}: \Gamma \times Q \rightarrow \{\mathbf{true}, \mathbf{false}\}$ which returns **true** (i.e., $\gamma \vdash_{RP_{\supseteq}} q$) if $\forall \langle u, e_att, vset \rangle \in q. e_att_{\gamma}(u) \supseteq vset$.

It is clear that given a scheme and problem instance, if $RP_{=}$ query problem is satisfied then RP_{\supseteq} problem is also satisfied, but not vice versa. The following two definitions are same as defined in [26], but we will state them for the sake of completeness.

Definition 7 (Reachability Plan). A Reachability Plan or plan is a sequence of authorized administrative requests to transition from initial state to the target state. For any rGURA_G scheme $\langle U, UA, AR, SCOPE, UG, \succeq_{ug}, \Psi, \Gamma, \delta \rangle$ and states $\gamma_0, \gamma' \in \Gamma$, reachability plan is a sequence of authorized requests $\langle req_1, req_2, \dots, req_n \rangle$ where $req_i \in REQ$ ($1 \leq i \leq n$), to transition from an initial state γ_0 to target state γ' if: $\gamma_0 \xrightarrow{req_1} \gamma_1 \xrightarrow{req_2} \gamma_2 \dots \xrightarrow{req_n} \gamma'$. The arrow denotes a successful transition from one state to another due to an administrative request req_i authorized by rules in Ψ . We write $\gamma_0 \xrightarrow{plan_{\Psi}} \gamma'$ to abbreviate the complete plan.

Informally, a reachability problem deals if there exists a reachability plan to transition from an initial state to some target state where the effective attribute values of the user satisfy a particular reachability query. Formally,

Definition 8 (Reachability Problems). Given any rGURA_G scheme $\langle U, UA, AR, SCOPE, UG, \succeq_{ug}, \Psi, \Gamma, \delta \rangle$, the attribute reachability problem is as follows:

- $RP_{=}$ or strict reachability problem instance I is of the form $\langle \gamma_0, q \rangle$ where $\gamma_0 \in \Gamma$, $q \in Q$ and checks if there exist a reachability plan P such that $\gamma_0 \xrightarrow{P_{\Psi}} \gamma'$ and $\gamma' \vdash_{RP_{=}} q$.
- RP_{\supseteq} or relaxed reachability problem instance I is of the form $\langle \gamma_0, q \rangle$ where $\gamma_0 \in \Gamma$, $q \in Q$ and checks if there exist a reachability plan P such that $\gamma_0 \xrightarrow{P_{\Psi}} \gamma'$ and $\gamma' \vdash_{RP_{\supseteq}} q$.

6 PSPACE-COMPLETE REACHABILITY

In this section, we present our reachability analysis results for different rGURA_G schemes shown in Figure 3. These results are extensions to the results from GURA reachability analysis [26] and also considers groups for assigning attributes to its member users. Our analysis will prove that rGURA_G schemes in Figure 3 in general are PSPACE-complete. For such schemes we will first show that all rGURA_G schemes are in PSPACE and then reduce a known PSPACE-complete problem to our problem schemes. In the next section, we will provide polynomial algorithms for some restricted rGURA_G problem classes.

Lemma 1. Reachability problem for every rGURA_G scheme in Figure 3 is in PSPACE.

Proof. Each state of a non-deterministic Turing machine stores some information to predict future states. This information takes polynomial amount of space and therefore all instance are in PSPACE. This proof is similarly stated for GURA schemes in [26] and more details are presented in appendix. \square

Since all rGURA_G schemes are in PSPACE, it will now be sufficient to prove that all rGURA_G schemes are PSPACE-hard, which will conclude that the schemes are PSPACE-complete.

Corollary 1. Reachability query types RP_{\supseteq} and $RP_{=}$ for rGURA_G schemes in general is PSPACE-complete.

Proof. Recall that Figure 3 defines the relation between different rGURA_G schemes and rGURA₀. The reachability analysis for rGURA₀ scheme discussed in [26] describes the scheme is PSPACE-complete. This scheme only allows change in attributes of the user. With respect to rGURA_{G₀}, it can be said that rGURA₀ scheme is a sub-problem without user groups. Therefore, the reduction from known PSPACE-complete problem (rGURA₀) to rGURA_{G₀} is straightforward, which makes rGURA_{G₀} as PSPACE-hard. Further, using Lemma 1, it is justified to claim that rGURA_{G₀} is in PSPACE-complete.

Similar claim can also be made for rGURA_{G₁} scheme where rGURA_{G₀} is its sub-problem involving only the same attribute in preconditions for rules (Ψ). Therefore, rGURA_{G₁} is PSPACE-hard and using Lemma 1, it is also PSPACE-complete. The analysis for rGURA_{G₁₊} is also alike the above two schemes where rGURA_{G₁} is a sub-problem of rGURA_{G₁₊}, therefore, rGURA_{G₁₊} is in PSPACE-hard and hence PSPACE-complete also. More details are present in appendix. \square

7 POLYNOMIAL REACHABILITY FOR RESTRICTED CASES

In previous section, we proved that attribute reachability for any rGURA_G scheme in general is PSPACE-complete. However, we have identified some instances of rGURA_G schemes which can be solved in polynomial time under precondition restrictions on administrative rules (Ψ). The practicality and use of these restricted instances are discussed in the example problem use-case discussed in Section 8. Similar to [26], the following restrictions are considered where \bar{D} and SR_d are always imposed together:

- **No negation (\bar{N}):** Ψ satisfies \bar{N} if no administrative rules in Ψ use negation in preconditions.
- **No deletion (\bar{D}):** Ψ satisfies \bar{D} if for each attribute $att \in UA$, $canDeleteU_{att}$ and $canDeleteUG_{att}$ are empty. Further,

canRemove rules are also empty, meaning, attribute values or groups once added cannot be deleted.

- **Single rule with direct values** (SR_d): Ψ satisfies SR_d if for each attribute $att \in UA$, there is at most one precondition associated with a particular value assignment in rules of $canAddU_{att}$ or $canAddUG_{att}$. Therefore, an attribute value pair can either be added through user directly or through groups but not both. Similar, condition also exists for $canAssign$ rules. Further, only direct conjuncts i.e. $val \in att_i(u)$, $val \in att_i(ug)$ or $ug \in directUg(u)$ are allowed in prerequisite condition.

These restrictions are important in different kinds of attributes and scenarios. For instance, **No negation** (\bar{N}) restrictions have significance when attributes like *course* or *degree* are added to entities. It is likely that adding a new value for *course* attribute do not require negation of another course as the precondition. Similarly, **No deletion** (\bar{D}) restriction can apply for attributes like *skills* where a value once added to any entity will never be deleted. Ideally, an individual attaining some skill-set will never lose them. The SR_d restriction allows only unique preconditions in administrative relations for user and user groups. This restriction essentially separates set of attributes into two parts, one which can be assigned only to user directly and others assigned through groups. For example, attribute like *roomAccess* can be assigned through group as it is usually common to all users with certain characteristics, and if value changes for one user, it will change for all others too. Attribute like *advisor* is assigned individually to each user as change for one user may not change it in others. Therefore, these restrictions are relevant in applications.

We now discuss reachability analysis for restricted $rGURA_G$ schemes. The notation $[rGURA_{Gx}, Restriction]$ specifies special instances of $rGURA_G$ scheme where subscript x takes a value in 0, 1 or 1+ representing $-rGURA_{G_0}$, $rGURA_{G_1}$ or $rGURA_{G_{1+}}$ and $Restriction$ represents combinations of \bar{N} , \bar{D} and SR_d specifying that administrative rules Ψ in the scheme satisfy these restrictions. For example, $[rGURA_{G_0} - \bar{N}]$ denotes $rGURA_{G_0}$ scheme where rules in Ψ satisfy \bar{N} .

As shown in Figure 3, $rGURA_{G_{1+}}$ scheme is the most expressive scheme where new attribute values are achieved by direct assignment to the user or to its effective groups, and also by changing user to group memberships. It is clear from the previous discussions that the scheme covers $rGURA_{G_1}$ and $rGURA_{G_0}$, which only allow change in attributes of the user or its effective groups. Therefore, we will only discuss algorithm for restricted $rGURA_{G_{1+}}$ scheme which can be easily used for other two schemes by simply ignoring irrelevant administrative rules.

7.1 Reachability plan for $RP_{=}$ in $[rGURA_{G_{1+}} - \bar{N}]$

First we will discuss reachability query type $RP_{=}$ for $[rGURA_{G_{1+}} - \bar{N}]$ scheme which can be solved in polynomial time by Algorithm 1. This algorithm extends the algorithm discussed for $rGURA_1$ [26] by including user group attribute assignments and also modification in user to group memberships. The added restriction to this scheme (\bar{N}) requires preconditions in rules without negation conjuncts and therefore, administrative rules cannot specify addition of new attributes based on the absence of some other values. Hence, the current attribute values of user or groups are not required to be removed for adding new values or group, which precludes the need for investigating any $canDeleteU_{att}$, $canDeleteUG_{att}$ and $canRemove$ rules.

The algorithm starts with the current set of attribute values and group memberships for user, and the attribute values for its member groups. It traverse all relevant $canAddU_{att}$, $canAddUG_{att}$ or $canAssign$ rules to add new values to the attributes of user or to its effective user groups and also add new groups to the user. Since, the query type is restricted, the algorithm first checks if the current effective attributes of user are not more than what required in the query (line 4). If the current values are extra, the algorithm returns false, since there are no delete administrative relations to delete such values. The while loop (line 5–24) terminates when either the query is satisfied or when no other values can be added from the rules in $canAddU_{att}$ and $canAddUG_{att}$ or no new groups can be added to the user using $canAssign$ rules. When adding a new value to the user or its effective groups, the corresponding value must be checked against the query. If the value is present in the query, the addition is allowed. Similar check is also done to add new groups the user, where all the attributes present in the group should also be a part of the query. The order to add these values or new groups is independent to each other, since no negation conjuncts are required and presence of extra values in user or group will not stop from adding new values. Also, if later a new value is added to an entity, the while loop will again consider the relevant rules to add values based on the already added values. When a new attribute is added to user, its effective groups or a new group is assigned to the user, its corresponding administrative request is appended to the reachability plan *plan*. If the query is satisfied, the algorithm returns the corresponding reachability plan *plan* or returns false stating that the query is unsatisfiable and user will not achieve desired effective attributes as mentioned in query.

Theorem 1. Reachability query type $RP_{=}$ for scheme $[rGURA_{G_{1+}} - \bar{N}]$ is P.

Proof. Algorithm 1 describes the polynomial time algorithm.

Complexity: The complexity is determined by the number of times the administrative rules in $canAddU_{att}$, $canAddUG_{att}$ or $canAssign$ are traversed. If only one value is added by each of the rules, the complexity of Algorithm 1 is $\mathcal{O}(|canAssign| \times |UG| + ((\sum_{att \in UA} |SCOPE_{att}|) \times (|canAddU_{att}| + |canAddUG_{att}| \times |UG|)))$, where $|canAddU_{att}|$, $|canAddUG_{att}|$ and $|canAssign|$ represents number of the administrative rules in these relations and $|UG|$ represents the maximum number of groups assigned to the user. Clearly, the complexity of algorithm is polynomial. \square

The RP_{\supseteq} query type for $[rGURA_{G_{1+}} - \bar{N}]$ also has a polynomial algorithm, where the extra conditions to check the query before adding new values is removed since we can have values even if they are not required in the query. The complexity will remain the same as shown in Theorem 1. Similar algorithm can also be devised for $RP_{=}$ and RP_{\supseteq} query type in $[rGURA_{G_1} - \bar{N}]$ and $[rGURA_{G_0} - \bar{N}]$ schemes where $canAssign$ rules will not be considered into the while loop for adding new groups to the user. Hence these schemes can be also solved in polynomial time.

7.2 Reachability plan for $RP_{=}$ in $[rGURA_{G_{1+}} - \bar{D}, SR_d]$

We will now consider another restricted instance for $rGURA_{G_{1+}}$, $[rGURA_{G_{1+}} - \bar{D}, SR_d]$ which can be solved by Algorithm 2 and 3. The scheme has two restrictions, \bar{D} which removes the need to consider delete administrative relations – $canDeleteU_{att}$, $canDeleteUG_{att}$ and $canRemove$. The SR_d restriction allows single preconditions for each attribute value pair or user group,

Algorithm 1 Plan Generation for $RP_{=}$ in $[rGURA_{G_{1+}} - \bar{N}]$

```

1: Input: problem instance  $I = \langle \gamma_0, q \rangle$  Output: plan or false
2:  $plan := \langle \rangle$ ; ▷ Initialize plan
3:  $s := \gamma_0$ ; ▷ Initialize with state  $s$ 
4: if  $(\exists att \in UA \exists \langle u, e\_att, vset \rangle \in q. e\_att(u) - vset \neq \emptyset)$  then return false; ▷ Check if state  $s$  has more values than query
   ▷ Assign attribute values required in query to the user or its effective groups
5: while  $(s \not\models_{RP_{=}} q \wedge$ 
6:    $((\exists att' := att \in UA \exists rule := \langle ar, c, val \rangle \in canAddU_{att'}). (Satisfy_u(u, c, s) \wedge val \notin att'(u) \wedge \exists \langle u, e\_att', vset \rangle \in q. val \in vset))$ 
7:    $\vee$ 
8:    $((\exists att' := att \in UA \exists rule := \langle ar, c, val \rangle \in canAddUG_{att'}). (\exists ug' := ug \in effUg(u). Satisfy_{ug}(ug', c, s) \wedge val \notin att'(ug') \wedge$ 
9:      $\exists \langle u, e\_att', vset \rangle \in q. val \in vset))$ 
10:    $\vee$ 
11:    $((\exists ug'' := ug \in UG \exists rule := \langle ar, c, ug'' \rangle \in canAssign). (Satisfy_{u-ug}(u, c, s) \wedge ug'' \notin directUg(u) \wedge$ 
12:      $\forall att \in UA \exists \langle u, e\_att, vset \rangle \in q. e\_att(ug'') \subseteq vset)))$  do
13:      $s := s \ll rule$ ; ▷ apply rule on state  $s$ 
14:     switch ▷ append administrative request to plan
15:       case  $rule \in canAddU_{att'}$ :
16:          $plan := plan.append(add(ar, u, att', val));$ 
17:       break;
18:       case  $rule \in canAddUG_{att'}$ :
19:          $plan := plan.append(add(ar, ug', att', val));$ 
20:       break;
21:       case  $rule \in canAssign$ :
22:          $plan := plan.append(assign(ar, u, ug''));$ 
23:       break;
24: end while
25: if  $s \models_{RP_{=}} q$  then return plan else return false end if ▷ check if reachability query is satisfied

```

Algorithm 2 Group Assignment Plan Generation for $RP_{=}$ in $[rGURA_{G_{1+}} - \bar{D}, SR_d]$

```

1: Input: problem instance  $I = \langle \gamma_0, q \rangle$  Output:  $plan_{ug}$ 
2: if  $\gamma_0 \models_{RP_{=}} q$  then return  $plan_{ug} := \langle \rangle$ ; ▷ Check initial state
3:  $G_{ug} := \langle V_{ug}, E_{ug} \rangle$ ;  $V_{ug} := \{ug \mid \exists ug \in UG. \exists ug \notin directUg(u). \exists \langle ar, c, ug \rangle \in canAssign(u). \forall att \in UA \exists \langle u, e\_att, vset \rangle \in q. e\_att(ug) \subseteq vset\}$ ;  $E_{ug} := \emptyset$ ; ▷ Construct a directed graph
4: for each pair of nodes  $(ug_1, ug_2) \in V_{ug}$  do
5:   if  $(\exists \langle ar, c, ug_2 \rangle \in canAssign. \text{"}(ug_1 \in directUg(u))\text{" is a conjunct in } c) \vee$ 
6:    $(\exists \langle ar, c, ug_1 \rangle \in canAssign. \text{"}\neg(ug_2 \in directUg(u))\text{" is a conjunct in } c))$ 
7:   then  $E_{ug} := E_{ug} \cup \{\langle ug_1, ug_2 \rangle\}$ ; end if ▷ Add edges
8: end for
9: if graph  $G_{ug}$  has cycles then remove the cyclic paths and  $plan_{ug} :=$  sequence of assign requests corresponding to the topological sort of  $G_{ug}$ ;

```

with only direct values as conjuncts in preconditions. This restriction results in rules which can be either satisfied by user or any of its effective groups but not both. We have divided the algorithm into two algorithm for ease of understanding and to show how these algorithms can be reused in other schemes also.

Algorithm 2 is used to add new groups to the user. Since the preconditions only involves user's direct groups as conjuncts (SR_d restriction), the addition of groups is independent of the attributes and can be calculated separately. The administrative rules in this scheme can have negation conjuncts in preconditions, therefore, the order of assigning new groups can be mutually dependent. The algorithm first creates a directed graph where vertices V_{ug} are user groups and edges E_{ug} are directed based on conjuncts in precondition of rules in $canAssign$. In line 3, before adding a group to V_{ug} , it is checked that all the attributes in group are required in query, as no extra attributes are allowed in $RP_{=}$ and deletion is not allowed. Line 4 – 8 creates edges in the graph, if a user group ug_1 is a negation conjunct to add another group ug_2 or ug_2 is a precondition for ug_1 , then edge is drawn from ug_2 to ug_1 , signifying that ug_2 should be added before ug_1 . If cycles exists in the created graph then remove the cyclic paths and create topological sort on the remaining graph. The set of administrative requests based on the sort will provide the $plan_{ug}$ for user to groups assignment. Once the requests are executed in order, new effective groups are calculated for the user and computation continues from Algorithm 3.

Algorithm 3 extends algorithm defined in [26], which checks the final set of values required to satisfy the reachability query and find $canAddU_{att}$ or $canAddUG_{att}$ rules to add those values. Further to add the values in precondition of rules, it may in-turn need some other rules and values and so on. Therefore, algorithm traverses backward to find the set of values required to satisfy the query. Since the values can be achieved by user directly or from any of its effective groups, this backward search is done for user and all its effective groups as calculated by Algorithm 2.

The algorithm starts by checking if the query is satisfied in the current state, in that case empty plan is returned signifying that with only new group assignments query is satisfied. Otherwise, it creates a set of attribute value pair for values required in query q and also for current attributes of user and its effective groups (line 4-5). Line 6 checks if the union of current values of the user or its effective groups is not more than values required in q . If extra values are there, the algorithm returns false, as no delete rules are allowed. The algorithm calculates all positive precondition attribute value pairs required by user or its effective groups to get values in $toadd$ (line 7-17). Therefore, the final set of values required includes the values in query ($toadd$) and positive preconditions in user or its effective groups excluding their current values. Line 18 checks if rules exists to add all required attribute value pair or else returns false, as the values can not be added. Line 19-21 calculate negative conjuncts in rules required to add required values and returns false if the such values are present in

Algorithm 3 Plan Generation for $RP_{=}$ in $[rGURA_{G_1} - \bar{D}, SR_d]$

```

1: Input: problem instance  $I = \langle \gamma_0, q \rangle$  Output: plan or false
2: if  $\gamma_0 \vdash_{RP_{=}} q$  then return plan :=  $\langle \rangle$ ; ▷ Check initial state
3:  $toadd := \{(att, val) \mid att \in UA, \langle u, e_{att}, vset \rangle \in q, val \in vset\}$  ▷ Values required in query
4:  $cur_u := \{(att, val) \mid att \in UA, val \in att(u)\}$  ▷ Current values of user
5: for each  $ug \in \text{effUg}(u)$  do  $cur_{ug} := \{(att, val) \mid att \in UA, val \in att(ug)\}$  end for ▷ Current values of user's effective groups
6: if  $(cur_u \cup (\bigcup_{ug \in \text{effUg}(u)} cur_{ug})) - toadd \neq \emptyset$  then return false; ▷ Check if state  $\gamma_0$  has more values than query
7:  $ppre_u := \emptyset$ ; for each  $ug \in \text{effUg}(u)$  do  $ppre_{ug} := \emptyset$ ; end for
8: for  $(att, val) \in toadd \cup ppre_u$  do ▷ Positive precondition values for user
9:    $ppre'_u := \{(att_1, val_1) \mid \exists (ar, c, val) \in \text{canAddU}_{att}. \text{"val}_1 \in att_1(u)\text{" is a conjunct in } c\}$ ;
10:    $ppre_u := (ppre_u \cup (ppre'_u \setminus ppre_u)) \setminus cur_u$ ;
11: end for
12: for  $ug \in \text{effUg}(u)$  do ▷ Positive precondition values for effective groups
13:   for  $(att, val) \in toadd \cup ppre_{ug}$  do
14:      $ppre'_{ug} := \{(att_1, val_1) \mid \exists (ar, c, val) \in \text{canAddUG}_{att}. \text{"val}_1 \in att_1(ug)\text{" is a conjunct in } c\}$ ;
15:      $ppre_{ug} := (ppre_{ug} \cup (ppre'_{ug} \setminus ppre_{ug})) \setminus cur_{ug}$ ;
16:   end for
17: end for
18: if  $(\exists (att, val) \in toadd \cup ppre_u \cup (\bigcup_{ug \in \text{effUg}(u)} ppre_{ug}) \setminus (cur_u \cup (\bigcup_{ug \in \text{effUg}(u)} cur_{ug}))) . \nexists (ar, c, val) \in \text{canAddU}_{att} \cup \text{canAddUG}_{att})$  then
   return false;
   ▷ Find negation values in rules required to add values for the user and its effective groups
19:  $npre_u := \{(att_1, val_1) \mid \exists (att, val) \in (toadd \cup ppre_u) \setminus cur_u . \exists (ar, c, val) \in \text{canAddU}_{att}. \text{"}\neg(val_1 \in att_1(u))\text{" is a conjunct in } c\}$ 
20: for each  $ug \in \text{effUg}(u)$  do  $npre_{ug} := \{(att_1, val_1) \mid \exists (att, val) \in (toadd \cup ppre_{ug}) \setminus cur_{ug} . \exists (ar, c, val) \in \text{canAddUG}_{att}. \text{"}\neg(val_1 \in att_1(ug))\text{" is a conjunct in } c\}$  end for
21: if  $((npre_u \cap cur_u \neq \emptyset) \vee (\forall ug \in \text{effUg}(u). npre_{ug} \cap cur_{ug} \neq \emptyset))$  then return false; ▷ Negation in current values
22:  $G := (V, E)$ ;  $V := toadd \cup ppre_u \cup (\bigcup_{ug \in \text{effUg}(u)} ppre_{ug}) \setminus (cur_u \cup (\bigcup_{ug \in \text{effUg}(u)} cur_{ug}))$ ;  $E := \emptyset$ ; ▷ Construct a directed graph
23: for each pair of nodes  $((att_1, val_1), (att_2, val_2)) \in V$  do
24:   if  $((\exists (ar, c, val_2) \in \text{canAddU}_{att_2}. \text{"val}_1 \in att_1(u)\text{" is a conjunct in } c) \vee$ 
25:    $(\exists (ar, c, val_1) \in \text{canAddU}_{att_1}. \text{"}\neg(val_2 \in att_2(u))\text{" is a conjunct in } c))$ 
26:   or
27:    $(\exists ug \in \text{effUg}(u). (\exists (ar, c, val_2) \in \text{canAddUG}_{att_2}. \text{"val}_1 \in att_1(ug)\text{" is a conjunct in } c) \vee$ 
28:    $(\exists (ar, c, val_1) \in \text{canAddUG}_{att_1}. \text{"}\neg(val_2 \in att_2(ug))\text{" is a conjunct in } c))$ 
29:   then  $E := E \cup \{(att_1, val_1), (att_2, val_2)\}$ ; end if ▷ Add edges to the graph
30: end for
31:  $valset := toadd - (cur_u \cup (\bigcup_{ug \in \text{effUg}(u)} cur_{ug}))$ ; ▷ Values in query not in state  $\gamma$ 
32: if  $\exists (att_1, val_1) \in valset \exists (att, val) \in E. (att, val) \notin valset$  then return false
33: else  $V := vset$   $E := E - \{(att, val), (att_1, val_1) \mid (att, val) \notin vset, (att_1, val_1) \notin valset\}$  end if
34: if graph  $G$  has a cycle then return false else return plan := sequence of administrative requests corresponding to the topological sort of  $G$ ;

```

TABLE 7: Example Problem Instance for $RP_{=}$ in $[rGURA_{G_1} - \bar{N}]$

Input: problem instance $I = \langle \gamma_0, q \rangle$ **Output:** *plan* or false
 $\psi \in \Psi$:
 $\text{canAddU}_{\text{roomAcc}} = \{ \langle \text{BuildAdmin}, c++ \in e_skills(u) \wedge 2.04 \in \text{roomAcc}(u), 1.2 \rangle \}$,
 $\text{canAddU}_{\text{college}} = \{ \langle \text{BuildAdmin}, python \in e_skills(u) \wedge 3.05 \in \text{roomAcc}(u), \text{COE} \rangle \}$,
 $\text{canAddU}_{\text{skills}} = \{ \langle \text{DeptAdmin}, c \in e_skills(u), python \rangle \}$,
 $\text{canAddUG}_{\text{roomAcc}} = \{ \langle \text{BuildAdmin}, 3.02 \in \text{roomAcc}(ug), 1.2 \rangle \}$,
 $\text{canAssign} = \{ \langle \text{DeptAdmin}, G_1 \in \text{directUg}(u), G_3 \rangle \}$
Queries:
 $q_1 \in Q = \{ e_roomAcc(u) = \{2.04, 2.03, 3.02, 1.2\}, e_skills(u) = \{c, c++, python\}, e_college(u) = \{\text{COS}\} \}$
 $q_2 \in Q = \{ e_roomAcc(u) = \{2.04, 2.03, 3.02, 1.2\}, e_skills(u) = \{c, c++\}, e_college(u) = \{\text{COS}, \text{COE}\} \}$

current state. After passing through all checks, the algorithm starts creating a directed graph. Vertices (V) in the graph are attribute value pair of the values required in the query q and the required positive preconditions excluding the values in the current state. Edges E will be drawn in the direction defined in the for loop (line 23-30). If the attribute value pair (att_1, val_1) is in the negative conjunct in administrative rule for (att_2, val_2) or (att_2, val_2) is a positive conjunct in a rule to add (att_1, val_1) , the edge is created from (att_2, val_2) to (att_1, val_1) . Since our query type is $RP_{=}$, it requires an additional check so that no extra values are added to the user. Therefore, once the graph is created, we create a set *valset*, which includes values required in query and not present in

the current state. If the created graph has vertex in *valset* having incoming edge not from vertex in *valset*, algorithm returns false (line 32). Otherwise it removes all the edges from vertices not in *valset*. If cycles exists in the remaining graph then algorithm returns false, else the set of administrative request corresponding to the topological sort will return the *plan*.

Therefore, the overall reachability plan returned will be *plan_{ug}* from Algorithm 2 and *plan* from Algorithm 3.

Theorem 2. Reachability query type $RP_{=}$ for scheme $[rGURA_{G_1} - \bar{D}, SR_d]$ is P.

Proof. Algorithm 2 and 3 describe the polynomial algorithms.

Complexity: The algorithm takes polynomial time to create directed graphs and then to compute topological sort. Its complexity is $\mathcal{O}(|UG| \times |\text{canAssign}| + ((\sum_{att \in U_A} |\text{SCOPE}_{att}|) \times (|\text{canAddU}_{att}| + |\text{canAddUG}_{att}| \times |UG|)))$. \square

In case of RP_{\supseteq} query type for $[\text{rGURA}_{G_1+} - \bar{D}, \text{SR}_d]$, we remove the extra checks to verify if no extra values are present in current state (line 6). Further line 31-33 is not required as extra values are allowed to be added to user. With these minor changes, the complexity of RP_{\supseteq} for scheme $[\text{rGURA}_{G_1+} - \bar{D}, \text{SR}_d]$ is P.

It should be noted that $\text{RP}_{=}$ for $[\text{rGURA}_{G_1-} - \bar{D}, \text{SR}_d]$ do not allow changes in group memberships of user. Therefore, computation for this scheme will start directly from Algorithm 3, obviating the execution of Algorithm 2. The RP_{\supseteq} query for $[\text{rGURA}_{G_1-} - \bar{D}, \text{SR}_d]$ will remove all extra conditions applied in Algorithm 3 for RP_{\supseteq} scheme for $[\text{rGURA}_{G_1+} - \bar{D}, \text{SR}_d]$ as discussed above. Also, since rGURA_{G_0} is a sub-problem of rGURA_{G_1} we can conjecture that $\text{RP}_{=}$ and RP_{\supseteq} for scheme $[\text{rGURA}_{G_0} - \bar{D}, \text{SR}_d]$ can be solved in polynomial time.

8 EXAMPLE PROBLEM INSTANCE

We will now illustrate the plan generation in two schemes discussed earlier with a sample input state and a set of reachability queries. Figure 4 defines the common input for both the schemes.

Plan Generation for $\text{RP}_{=}$ in $[\text{rGURA}_{G_1+} - \bar{N}]$: Figure 5 shows attributes of user and groups along with user to group direct membership. Table 7 defines set of administrative rules allowed in scheme along with two reachability queries. We will first try to find a reachability plan (if exists) for query q_1 using Algorithm 1.

Initially, *plan* is set to empty $\langle \rangle$. The initial state is checked to find if it has more attribute values than required in query q_1 . In state γ_0 , the effective values of user are $e_{\text{roomAcc}}(u) = \{2.04, 2.03\}$, $e_{\text{skills}}(u) = \{c, c++\}$, $e_{\text{college}}(u) = \{\text{COS}\}$, which are all required in query. The while loop checks if query q_1 is satisfied in state γ_0 , which is not true as some values are missing. Now algorithm starts adding new values to the user or its effective groups and also assign new groups to user based on administrative rules defined in Table 7. The first rule requires effective skills of user having value $c++$ and roomAcc attribute with value 2.04. to add 1.2 value to roomAcc by administrative role BuildAdmin . Since user satisfy these conditions and 1.2 value is not directly assigned in $\text{roomAcc}(u)$ and the value is required in q_1 , it adds 1.2 value to $\text{roomAcc}(u)$. The administrative request $\text{add}(\text{BuildAdmin}, u, \text{roomAcc}, 1.2)$ is also appended to the *plan*. The algorithm again goes through the while loop and checks if q_1 is satisfied. The user is still missing skills attribute value python. The algorithm now tries to add group G_3 to user u . The precondition of canAssign rule is satisfied by user, but the effective values for roomAcc attribute for group G_3 are $\{3.05, 2.04\}$, which is not the subset of values required in query. Hence, G_3 cannot be assigned to user u . Next, the algorithm checks rule for skills attribute to add value python and finds that preconditions to add value python are satisfied by user u . It appends the corresponding request $\text{add}(\text{DeptAdmin}, u, \text{skills}, \text{python})$ to *plan* which results in total of two requests in the plan. The algorithm again checks the new state against q_1 and finds the query is “strict” satisfied. It breaks the while loop and returns *plan* = $\text{add}(\text{BuildAdmin}, u, \text{roomAcc}, 1.2), \text{add}(\text{DeptAdmin}, u, \text{skills}, \text{python})$.

We now check the satisfiability of query q_2 with the same initial state. Similar to q_1 , query is checked against initial state to

$U = \{u\}$,
 $UA = \{\text{college}, \text{roomAcc}, \text{skills}\}$,
 $AR = \{\text{DeptAdmin}, \text{BuildAdmin}\}$,
 $UG = \{G_1, G_2, G_3, G_5\}$,
 $UGH = \{(G_1, G_1), (G_2, G_2), (G_1, G_2), (G_3, G_3), (G_5, G_5)\}$
 $\text{SCOPE}_{\text{college}} = \{\text{COS}, \text{COE}, \text{BUS}\}$,
 $\text{SCOPE}_{\text{roomAcc}} = \{1.2, 2.03, 2.04, 3.02, 3.05\}$,
 $\text{SCOPE}_{\text{skills}} = \{c, c++, \text{python}, \text{matlab}\}$
 δ (Transition Function)

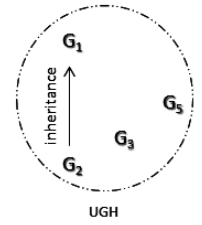


Fig. 4: Input Starting State ($\gamma_0 \in \Gamma$)

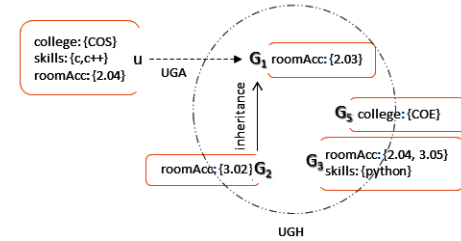


Fig. 5: Initial State for $\text{RP}_{=}$ in $[\text{rGURA}_{G_1+} - \bar{N}]$

check extra values and value 1.2 for attribute roomAcc is added to the user and requests is appended to the plan. Second rule allows to add COE for attribute college, but the preconditions are not satisfied by user. We try to add group G_3 but it also adds extra values which are not required in query. It can be noticed that after all the administrative rules are checked, the query cannot be satisfied and hence the algorithm returns false.

Plan Generation for $\text{RP}_{=}$ in $[\text{rGURA}_{G_1+} - \bar{D}, \text{SR}_d]$: Figure 6 shows user and group attributes along with user to group direct membership. Table 8 defines the set of administrative rules allowed in the scheme and three reachability queries. It should be noted that the rules in Ψ have negation conjuncts and single precondition with direct attributes or group memberships for each attribute value pair or user group. We will start with Algorithm 2 to assign new groups to the user. Once groups are assigned, attributes will be added to user or its newly computed effective groups. If Algorithm 2 doesn't add new groups, the computation will still be done by Algorithm 3 with old effective groups.

Algorithm 2 creates group assignment plan (defined as plan_{ug}) to assign new groups to user. Two administrative rules exists in canAssign relation. Since G_3 is not directly assigned to user u , precondition is satisfied and G_3 has value python for skill attribute, which is required in query q_1 , algorithm adds G_3 to the set of vertices V_{ug} . Similarly group G_5 is also added to V_{ug} . There are no more canAssign rules, hence the algorithm starts adding edges to the graph. For $(G_3, G_5) \in V_{ug}$, since G_3 is a negation conjunct in precondition to add G_5 , therefore, directed edge is drawn from G_5 to G_3 . As there are no other relevant canAssign rules and vertices pair, it breaks the loop and creates a topological sort of the graph. Sort will have $\{G_5, G_3\}$ order and the corresponding plan $\text{plan}_{ug} := \text{assign}(\text{DeptAdmin}, u, G_5), \text{assign}(\text{DeptAdmin}, u, G_3)$ is returned. Before proceeding to Algorithm 3, the request in plan_{ug} must be executed to get new effective groups of the user. Algorithm 3 is used to assign attributes to user and newly computed effective groups (which will now have group G_5 and G_3 along with G_1 and G_2). It first checks if the query (q_1) is satisfied in the current state (line 2) which has new direct groups assigned using algorithm 2. Clearly query q_1 is satisfied with new group assignments only, hence the

TABLE 8: Example Problem Instance for $RP_{=}$ in $[rGURA_{G_1+} - \bar{D}, SR_d]$

Input: problem instance $I = \langle \gamma_0, q \rangle$ **Output:** *plan* or false

$\psi \in \Psi$:

$canAddU_{roomAcc} = \{ \langle BuildAdmin, c++ \in skills(u) \wedge \neg(2.04 \in roomAcc(u)), 1.2 \rangle \}$,

$canAddU_{skills} = \{ \langle DeptAdmin, c \in skills(u), python \rangle \}$,

$canAddU_{college} = \{ \langle BuildAdmin, matlab \in skills(u), BUS \rangle \}$,

$canAddU_{skills} = \{ \langle DeptAdmin, c \in skills(u) \wedge COS \in college(u), matlab \rangle \}$

$canAddUG_{college} = \{ \langle BuildAdmin, python \in skills(ug) \wedge \neg(2.04 \in roomAcc(ug)), COE \rangle \}$,

$canAssign = \{ \langle DeptAdmin, G_1 \in directUg(u), G_3 \rangle, \langle DeptAdmin, \neg(G_3 \in directUg(u)), G_5 \rangle \}$

Queries:

$q_1 \in Q = \{ e_{roomAcc}(u) = \{2.04, 2.03, 3.02\}, e_{skills}(u) = \{c, c++, python\}, e_{college}(u) = \{COS, COE\} \}$

$q_2 \in Q = \{ e_{roomAcc}(u) = \{2.04, 2.03, 3.02, 1.2\}, e_{skills}(u) = \{c, c++, python\}, e_{college}(u) = \{COS, COE\} \}$

$q_3 \in Q = \{ e_{roomAcc}(u) = \{2.04, 2.03, 3.02\}, e_{skills}(u) = \{c, c++, python, matlab\}, e_{college}(u) = \{COS, COE, BUS\} \}$

reachability plan for group assignments $plan_{ug}$ is returned.

For queries q_2 and q_3 , group assignment plan $plan_{ug}$ is created similarly as above. Therefore, we will follow Algorithm 3 with user's effective groups as G_1, G_2, G_3 and G_5 . For q_2 , current state do not have value 1.2 for roomAcc attribute. The algorithm first computes *toadd*, which is the set of attribute value pair in q_2 :

$toadd = \{ \langle roomAcc, 2.04 \rangle, \langle roomAcc, 2.03 \rangle, \langle roomAcc, 3.02 \rangle, \langle roomAcc, 1.2 \rangle, \langle skills, c \rangle, \langle skills, c++ \rangle, \langle skills, python \rangle, \langle college, COS \rangle, \langle college, COE \rangle \}$

It then calculates the current attribute value pair for user and its effective groups (Line 4-5):

$cur_u = \{ \langle roomAcc, 2.04 \rangle, \langle skills, c \rangle, \langle skills, c++ \rangle, \langle college, COS \rangle \}$

$cur_{G_1} = \{ \langle roomAcc, 2.03 \rangle \}$ $cur_{G_2} = \{ \langle roomAcc, 3.02 \rangle \}$

$cur_{G_3} = \{ \langle roomAcc, 2.04 \rangle, \langle skills, python \rangle \}$

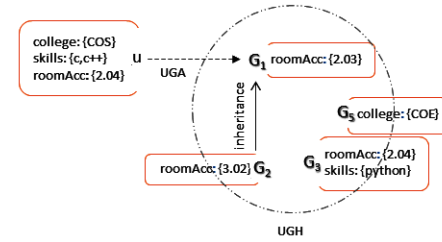
$cur_{G_5} = \{ \langle college, COE \rangle \}$

The algorithm checks if the current attributes of user and its effective groups are not extra than the values required in the query. Clearly, for query q_2 , no extra values are present in current state. The algorithm next computes the positive conjuncts in the preconditions required to add the values in *toadd*. It first calculates for each attribute value pair in *toadd* and then recalculates for each positive preconditions attribute value pair also. For example, positive conjunct for user to add $\langle roomAcc, 1.2 \rangle$ in *toadd* is $\langle skills, c++ \rangle$ and for $\langle skills, python \rangle$ in *toadd* is $\langle skills, c \rangle$. Therefore (using line 9), $ppre'_u := \{ \langle skills, c++ \rangle, \langle skills, c \rangle \}$. It then recomputes $ppre_u$ by combining its values with newly computed $ppre'_u$ after removing values already present in $ppre_u$ or cur_u . In this case, no new value is added in $ppre_u$, as both the values in $ppre'_u$ are already present in cur_u . Similarly, the positive preconditions are calculated for each effective groups.

$ppre_u = \{ \}$, $ppre_{G_1} = ppre_{G_2} = ppre_{G_5} = \{ \langle skills, python \rangle \}$
 $ppre_{G_3} = \{ \}$

Next, in line 18, the algorithm checks if rules exists for values required in *toadd* and positive preconditions excluding the current values. Clearly, rule exists for $\langle roomAcc, 1.2 \rangle$ pair and all other values are already present in user or its effective groups. It then calculates negative conjuncts for user and its effective groups in preconditions to add values in *toadd* and positive preconditions excluding current state. For user, $\langle roomAcc, 1.2 \rangle$ has negation conjunct $\langle roomAcc, 2.04 \rangle$ in $canAddU_{roomAcc}$. Remaining negation conjuncts are as follows:

$npre_u = \{ \langle roomAcc, 2.04 \rangle \}$

Fig. 6: Initial State for $RP_{=}$ in $[rGURA_{G_1+} - \bar{D}, SR_d]$

$npre_{G_1} = npre_{G_2} = npre_{G_3} = \{ \langle roomAcc, 2.04 \rangle \}$
 $npre_{G_5} = \{ \}$

Line 21 checks if the negation conjuncts exists in current values of either user or its effective groups. User has $\{ \langle roomAcc, 2.04 \rangle \}$ pair in cur_u , therefore, roomAcc attribute cannot get value 1.2 required in q_2 since only single rule exists for user or groups. Hence, the algorithm returns false for query q_2 . For query q_3 , *toadd* values are:

$toadd = \{ \langle roomAcc, 2.04 \rangle, \langle roomAcc, 2.03 \rangle, \langle roomAcc, 3.02 \rangle, \langle skills, c \rangle, \langle skills, c++ \rangle, \langle skills, python \rangle, \langle skills, matlab \rangle, \langle college, COS \rangle, \langle college, COE \rangle, \langle college, BUS \rangle \}$

The current values are still the same as defined in query q_2 . The algorithm calculates the positive conjuncts in preconditions as:

$ppre_u = \{ \langle skills, matlab \rangle \}$
 $ppre_{G_1} = ppre_{G_2} = ppre_{G_5} = \{ \langle skills, python \rangle \}$
 $ppre_{G_3} = \{ \}$

The negation conjuncts are calculated as:

$npre_u = \{ \}$, $npre_{G_1} = npre_{G_2} = npre_{G_3} = \{ \langle roomAcc, 2.04 \rangle \}$
 $npre_{G_5} = \{ \}$

These negation values are not present in user or all of its effective groups. Therefore, the algorithm creates directed graph (line 22-30) with vertices $V := \{ \langle skills, matlab \rangle, \langle college, BUS \rangle \}$. Edge in E is drawn from $\{ \langle skills, matlab \rangle \}$ to $\{ \langle college, BUS \rangle \}$ as $\{ \langle skills, matlab \rangle \}$ is a precondition conjunct in rule to add $\{ \langle college, BUS \rangle \}$. Line 31 calculates *valset* which in this case is same as V . Since no cycle exists in the graph, topological sort is created. The final reachability plan to satisfy the query q_3 is *plan* := assign(DeptAdmin, u, G_5), assign(DeptAdmin, u, G_3), add(DeptAdmin, u, skills, matlab), add(BuildAdmin, u, college, BUS). The administrative requests must be executed as ordered in the reachability plan.

9 EXPERIMENTAL RESULTS

This section describes the performance evaluation on Algorithms 1, 2 and 3 (discussed in Section 7) after varying number of parameters and shows the analysis of the results drawn from these experiments. We measure the time it takes for a successful reachability plan to generate under different $rGURA_G$ instances once a query is requested. We implemented the algorithms in Python using PyCharm¹. We generated a random pool of attributes and their values for user and groups in the system. The initial state of the system is assigned a user, set of groups, administrative rules allowed in different schemes, group hierarchy, scope of attributes etc. where all are generated randomly. Reachability query and administrative rules are also randomly generated based on the attributes in initial state (we do not want to have the query be satisfied in the initial state itself). There are several dynamic parameters which we changed to scale the algorithms: $attr$ denotes the number of attributes, $scope$ represents the size of the range for values of attributes. $ppre$ and $npre$ represent the number of positive and negative conjuncts in a rule precondition respectively. d represents the total number of desired attribute and value pairs specified in the reachability query which are not already available in the initial state. For example, assume in initial state, $ATTR = \{College, Skill\}$ and $U = \{Bob\}$. In the initial state, $College(Bob) = \{COS\}$ and $Skill(Bob) = \{c, Python\}$. If the query requires, $College(Bob) = \{COS, COR\}$ and $Skill(Bob) = \{c, Python, c++, matlab\}$, then the value of d would be 3 as the number of attribute and value pairs that are absent in the initial state is 3. g denotes the number of user groups in the system. We generated administrative rules based on the values in d . Roughly half of the number of items in the query (for example, with $d = 30$ for Algorithm 1 results in Figure 7a) would be for $canAddUA$ and the other half $canAddUGA$ and a couple for $canAssign$. These numbers are approximate since the input and query statements are randomly generated. Therefore, the rules which are based off of those may vary as well. We vary all these parameters in Algorithms performance evaluation under different combinations as explained below. Each data reported is an average over 500 instances generated using the same parameter values. Plan generation execution time was measured on Apple MacBook Pro with a M1 processor with 16 GB of RAM.

Results for Algorithm 1: The evaluation results are in Figures 7a, 7b and 7c. We vary different parameters except $npre$ in Algorithm1 which denotes the number of negations in preconditions. These negation preconditions are not permitted in the rule conditions of Algorithm 1. Figure 7a shows the impact of d and $ppre$ on execution time. We plot the number of $ppre$ on x-axis and the execution time (in ms) on y-axis. We plot each curve for a different value of d . For these graphs we use, $attr = 10$, $scope = 40$, $g = 4$. As expected, the execution time increases with the increase of number of $ppre$ as it more takes time to check the required values for the attributes included in precondition conjuncts of administrative rules with the increasing attribute value pair required in query (denoted by d). For instance, the execution time for $attr = 10$, $scope = 40$ with $ppre = 5$ and $d = 30$ is nearly .22 ms, which is much higher than for same parameters but $d = 10$. The major reason is as the reachability query has more attribute values pair to be satisfied, it will take more time to generate a feasible plan.

1. <https://www.jetbrains.com/pycharm/>

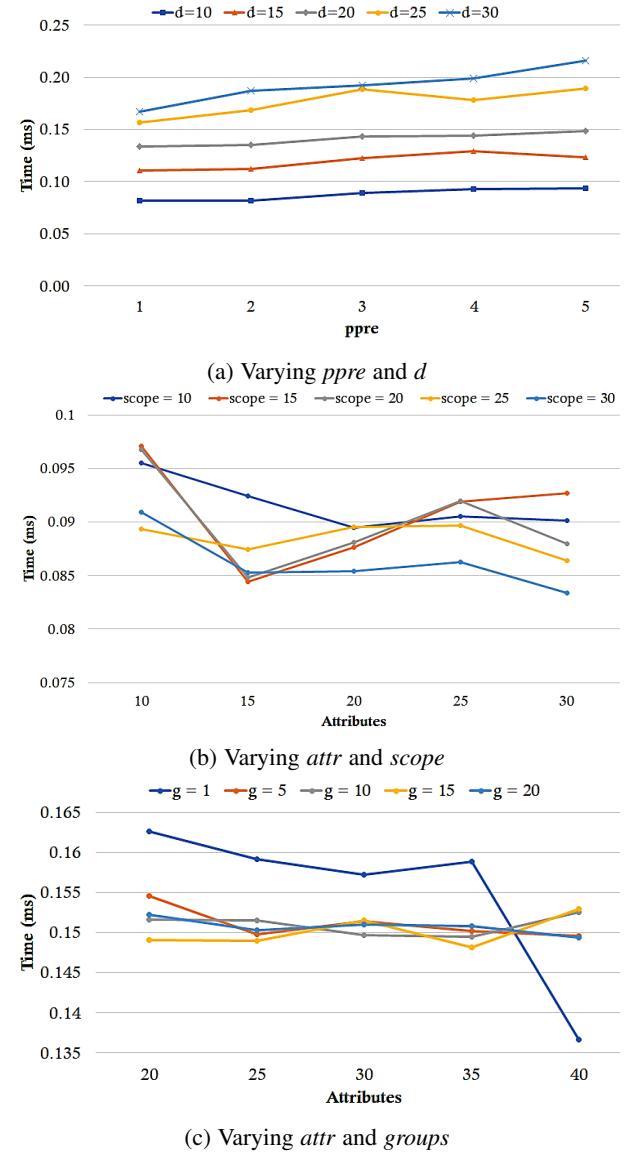


Fig. 7: Performance of Algorithm 1 with Different Parameters

Figure 7b shows the impact on execution time when we vary the $scope$ and number of attributes $attr$ (shown as Attributes). We plot the number of attributes on the x-axis and the time consumed for plan on the y-axis. In all problem instances, we ran the experiment with $d = 10$, $g = 4$ and $ppre = 5$. Our results show that there is no trend of time increase as the number of attributes increase. However, the total time to execute a query in general is less with larger scope. As we are generating the query randomly with the fixed d , the time for solving the query shall overall be small as we have larger initial state due to more attributes or scope. Similarly, as shown in Figure 7c, we vary the number of attributes and number of groups in the initial state. For all instances, we use $d = 10$, $scope = 40$, $ppre = 5$. We observe, for highest number of groups, $g = 20$, the execution time constantly remains high except for $attr = 40$. It is possible that with the large number of attributes in the initial state, the query is satisfied in early states yielding a fast plan execution. However, the dynamic generator with different queries, initial states and administrative rules, the graphs will not be able to provide a set pattern but it is fair to conjecture that overall time is still less than .30 ms with

large number of attributes, values and groups.

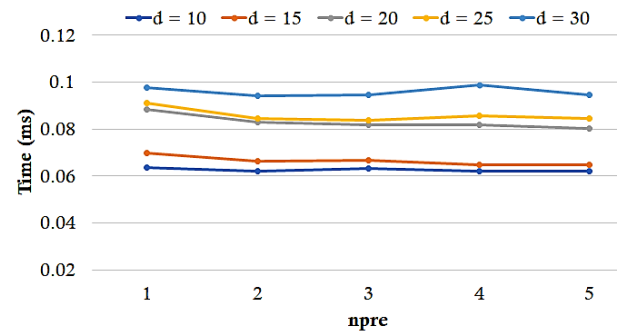
Results for Algorithms 2 & 3: The results for Algorithm 2 are shown in Figures 8a and 8b and for Algorithm 3 are illustrated in Figures 8c and 8d. We calculate the plan generation execution time based on the number of positive *ppre* and negation conjuncts (*npre*) prescribed in a rule precondition. We perform calculations for increasing numbers of *npre* followed by combined *ppre* and *npre* in equal numbers. In practical scenarios, we assume that an administrative rule will not have more than 10 conjuncts to be satisfied for a given attribute value pair or group. Figure 8a shows the impact of negative precondition conjuncts *npre* (on x-axis) and *d* on the execution time for Algorithm 2. The curve is nearly flat for the different values of *npre* with same *d*. We observe that checking attribute values that are not in the current state (due to *npre* requirement) for user does not take much time while the execution time increases with increasing number of required attribute-value pair in query that are not in the current state since more values are to be satisfied. Figure 8c captures the behaviour for Algorithm 3 with the same parameter values as for Algorithm 2. It shows similar behavior except the increase in the execution time to run Algorithm 3. This is due to the fact that Algorithm 3 is more complex and requires checking all the different pre-conditions before generating the plan.

Figure 8b and 8d evaluate the impact of changing both *npre* and *ppre* respectively for Algorithms 2 and 3. We plot the number of *ppre* and *npre* conjuncts on x-axis against execution time and observe the curves for *d* = 10 to 30. The plan generation time increases in both graphs as the required attribute values in query increase with *d*. It happens as the expected values for satisfying query in current state are higher when the value of *d* is large. The calculation time for the same parameters is higher in the graphs for Algorithm 3. For all the graphs in Figure 8, we see the increase in consumed time when we increase the value of *d*.

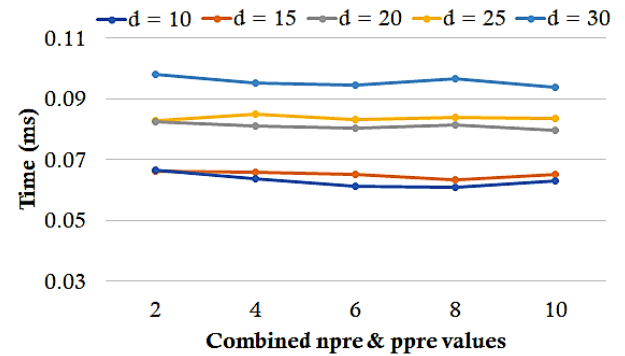
The parameters assumed in our set of experiments are realistic in practical situations, for example, we do not expect users to carry 1000s of attributes or an organization having 100s of groups or administrative rules. However, it does not limit the scalability of our algorithms and the reachability problems can be solved in very reasonable amount of time.

10 CONCLUSION AND FUTURE WORK

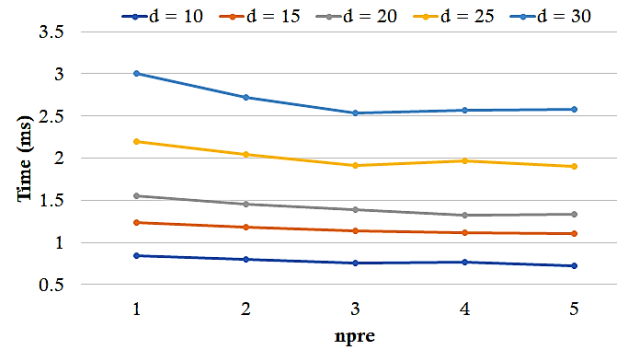
Attributes based access control defines permissions of entities based on their attributes. In this work, we presented reachability analysis for effective attributes of the user based on the direct attributes assignment to the user or its member user groups. We first stated the HGABAC model and $GURA_G$ administrative model to provide some background. We defined a restricted form of $GURA_G$, referred as $rGURA_G$ and classified three schemes $rGURA_{G_0}$, $rGURA_{G_1}$ and $rGURA_{G_1+}$ to discuss different reachability solutions. In general, we proved the reachability problem for $rGURA_G$ scheme is intractable as PSPACE-complete but with certain restrictions, polynomial time algorithms can also be achieved. We empirically evaluated the algorithms under different varying parameters to understand its practicality and use in real world scenarios. In future, we can develop more polynomial algorithms for some restricted forms and perform reachability analysis on other types of queries like effective user groups or minimum number of administrative requests to satisfy query.



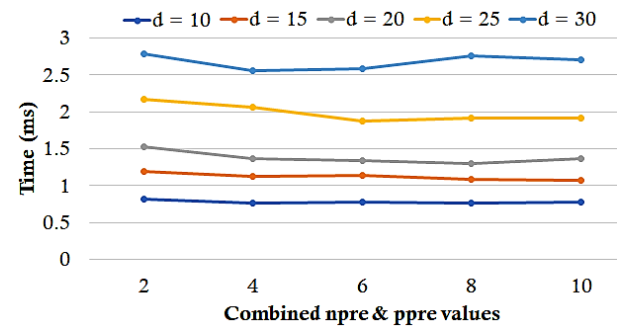
(a) Varying *npre* and *d* for Algorithm 2



(b) Varying *npre* & *ppre* with *d* for Algorithm 2



(c) Varying *npre* and *d* for Algorithm 3



(d) Varying *npre* & *ppre* with *d* for Algorithm 3

Fig. 8: Performance of Algorithms 2 & 3 with Diff. Parameters

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