

# Clustering Object Trajectories for Intersection Traffic Analysis

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**Abstract:** Vehicle and pedestrian traffic at a traffic intersection provide crucial information about the performance of the intersection for safety and throughput. It is possible to discover patterns and outliers on this data by applying data analytics. In this paper, we present a novel clustering algorithm for trajectories that use a new distance measure and a two-level hierarchical clustering approach based on geometric properties of the trajectories and spectral clustering. Trajectory data is augmented with signal phasing and timing information, which gives new insights to the trajectory data. We demonstrate the procedure on a real-life intersection where the prominent patterns for traffic movement are found, and the anomalous trajectories are extracted.

## 1 INTRODUCTION

Traditionally, most intersections have induction loop detectors installed underneath the road. These detectors detect vehicles passing over them and may be used to monitor the vehicle throughput at an intersection. However, these detectors incur high costs for deployment as well as maintenance and may not sense pedestrians or scooters. Additionally, even for the vehicles that can be detected, the loop detectors cannot precisely tell the class of the vehicle passing over it. To address these limitations, many intersections are now being equipped with other types of sensors, such as video cameras and radars. The use of videos has tremendous potential as it provides rich information in addition to counting the vehicles. Examples of this include tracking the type of object passing through an intersection, tracing the trajectories of objects, and detecting anomalous traffic behaviors. These additional information can be used to improve safety and performance of an intersection.

An object moving through an intersection is captured by the video camera installed at the intersection, and it is possible to generate the coordinates using video processing algorithms such as (Huang et al., 2018) and (Huang et al., 2020) where the coordinates of the path are annotated with the timestamp, and the height and width of a bounding box enclosing the object. A trajectory is defined as a path traced by a moving object and is represented by a time series of spatial coordinates of the object. A triplet representation of the object  $((x_1, y_1, t_1), (x_2, y_2, t_2) \cdots (x_n, y_n, t_n))$  provides the location of the object at different time

instants. We leverage the trajectories generated using video processing and fuse it with SPaT (Signal Performance and Timing) data to determine vehicle and pedestrians on the intersection for different signal phases.

Broadly, we develop a novel end-to-end workflow for analyzing vehicular and pedestrian traffic at an intersection, beginning with ingesting video data and controller logs, followed by data storage and processing to generate dominant and anomalous behavior at the intersection, which helps in various applications such as near-miss detection. The key contributions of our paper are as follows:

1. We develop a new distance measure for computing distances between trajectories. Using this distance measure, we develop an offline, two-level hierarchical clustering scheme. At the first level, the trajectories are clustered based on their direction of movement. At the second level, spectral clustering is applied. Clustering helps us to detect the outliers automatically.
2. We show how new insights and perspectives into the trajectory data are possible by joining the trajectory database with the SPaT data. For example, the combined data can be used to detect signal violations, to count the number of vehicles entering the intersection on a yellow light, and several other useful behavior patterns.

Extensive results are provided on video and SPaT data collected at an intersection. These results demonstrate that video and signal timing information is useful in quantifying

1. Safety of pedestrians and bicyclists by studying the nature of the anomalous vehicle trajectories and also the statistics of occurrence of these anomalies (counts of anomalies depending upon the hour and day of the week)
2. Effective tuning of signal timing based on demand profiles. It also helps us compare the new technologies such as video-based monitoring and existing technologies such as induction loops.

The approach presented in this paper can be used to develop a system that uses edge-based video-stream processing to convert video data into space-time trajectories of individual vehicles and pedestrians. These trajectories are transmitted and stored to a centralized system for intersection level and city wide processing.

The rest of the paper is organized as follows. We present existing work on trajectory analysis in Section 2. The background information for our application may be found in Section 3, while the methodology developed as part of this paper is presented in Section 4, which includes computing distance measures and clustering trajectories along with case-studies for some intersections. The conclusions are presented in Section 6.

## 2 RELATED WORK

The general advancement of location acquisition technologies has made it feasible to generate a massive database of trajectories for different kinds of entities, such as vehicles, hurricanes, migratory animals. It requires data mining techniques to gain insight into this massive dataset. Feng et al. (Feng and Zhu, 2016), Mazimpaka et al. (Mazimpaka and Timpf, 2016), and Banerjee et al. (Banerjee et al., 2019) describe the fact that a complete trajectory data mining application involves components for data collection, data preprocessing, management and storage, query processing, data mining, and privacy protection. Most of the existing work on trajectory data mining focuses on trajectories at a macro level, such as those through cities, states, countries, or continents, where trajectory data is collected using satellites or an appropriate satellite-based radio navigation system. Examples are vehicle positioning data, or data from hurricanes or animal movement (Lee et al., 2008), activities in and around a city (Loecher and Jebara, ). Unlike this work, the focus of this paper is on the analysis of object trajectories at signalized intersections using trajectory clustering to find patterns and anomalies of traffic behavior with reference to the signaling

phase of the intersection as well as the spatial constraints. The trajectory data is collected from videos installed at the intersections, and the trajectory data is fused with SPaT data from the intersections. SPaT data may be obtained either from high-resolution controller data or from DSRC (Dedicated Short-Range Communications) RSU (Roadside Unit). In the following we briefly describe some of the related work in this area.

Trajectory clustering algorithms may be divided into three groups, namely, supervised, semi-supervised, and unsupervised algorithms. This distinction arises if labeled data is used to aid in the clustering where the labels uniquely identify the clusters (Bian et al., 2018). We use unsupervised clustering in this work, and the user can just invoke the algorithm without having to input any labeled data. Model-based unsupervised clustering strategies use probabilistic models for clustering trajectories (Morris and Trivedi, 2011). Gaussian Mixture models and hidden Markov models are used in (Morris and Trivedi, 2011), to model the trajectory coordinates and the trajectory dynamics, respectively. Another existing unsupervised clustering strategy is iterative (Lloyd, 1982), where the cluster centers are found and updated iteratively. In our work, we use a hierarchical clustering scheme where the trajectories are first clustered based on their general direction of movement using geometrical properties of the trajectories. Then spectral clustering is applied on each trajectory cluster to identify the typical pattern of movement and associated anomalies.

Clustering a given set of objects involves computing the pairwise distance between them so that the closest objects may be clustered together. Thus, the concept of a distance measure is essential for clustering trajectories. A trajectory is a time-series and one of the existing distance measures used in literature for a time-series is the longest common subsequence (LCSS (Vlachos et al., 2002), edit distance with real penalty (ERP) (Chen and Ng, 2004), dynamic time warping (DTW) (Kruskal and Liberman, 1983) and FastDTW (Salvador and Chan, 2004). Applying DTW or FastDTW directly to the trajectories at an intersection collected in real-time using video processing is not effective, because location coordinates are often dropped due to artifacts of video processing and occlusion. Partial trajectories results in a very high distance value for two otherwise similar trajectories (Figure 2). We have developed a new distance measure that is more effective for these type of trajectories. The distance measure is based on the warp path of two trajectories. The warp path is obtained by applying FastDTW, and using the warp path, we de-

termine the area between the trajectories and divide the area by the length of the two trajectories to get the average perpendicular distance between the trajectories.

### 3 BACKGROUND

The background information required for analyzing the trajectories is presented in this section. Section 3.1 describes the trajectory generation in brief while Section 3.2 describes the recording of the current signal state of an intersection. Finally, Section 3.3 presents a detailed comparison of the candidate distance measures.

#### 3.1 Trajectory Generation

A video processing software processes object locations frame by frame from a video and outputs the location coordinates along with the corresponding timestamp. The video is captured by a camera installed at an intersection. To accurately locate the coordinates of an object, the video processing software must account for the different types of distortions that creep into the system. For example, for a fisheye lens, there would be a significant amount of radial distortion. After taking into account the intrinsic and extrinsic properties of the camera, a mapping is created, which is used by the video processing software to map observed coordinates to modified coordinates that are nearly free of any distortion. To represent the location of a 3D object using a dimensionless point, one looks to find the center of mass of the object. A bounding box is drawn enclosing the object. The center of the box is approximated to be the center of mass of the object. After generating timestamped coordinates of a trajectory, the software computes other properties such as speed, the direction of movement.

#### 3.2 Signalling Status

An intersection almost always has traffic lights to control the flow of traffic safely. The changes in signals from green to yellow to red are events that are captured in controller logs by advanced controllers and also sometimes broadcast by DSRC RSUs, and the corresponding data are called Signal Phase and Timing (SPaT) data. To specify a particular signal and in a more general sense the direction of movement, the traffic engineers define a standard that assigns phases 2 and 6 to the two opposite directions of the major street and 4 and 8 to those of the minor street. Fig-

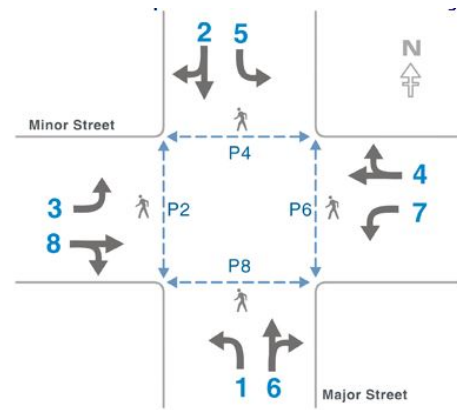


Figure 1: Phase Diagram showing vehicular and pedestrian movement at four way intersections. The solid gray arrows show vehicle movements while the blue dotted arrows show pedestrian movements. (US Department of Transportation, 2008).

ure 1 shows these phase numbers as well as the phase numbers for the turning vehicles and pedestrians.

In our application, we store the current signal phase in a compact 6-digit hexadecimal encoding. To explain the formatting, let us consider the corresponding 24-bit binary equivalent. The bits 1-8 are programmed so that they are 1 if the corresponding phase is green, and 0 otherwise. Similarly, the bits 9-16 and bits 17-24 are reserved for programming the yellow and red status for the eight-vehicle phases, respectively. For example, green on phases 2 and 6 at an intersection, would have a binary encoding of 0100 0100 for the first 8 bits, the next eight bits would be 0000 0000 for yellow, and the last set of 8 bits for red would be one where the second and sixth bits are 0 represented as 1011 1011. Thus, the overall 24-bit binary representation of the current signalling state is 0100 0100 0000 0000 1011 1011, or 4400bb.

#### 3.3 Comparing Trajectories

The first step toward clustering a set of trajectories is applying a good distance measure that will, for any two trajectories, tell how close the trajectories are to each other in space and time. There are two potential candidates for distance measures of the intersection trajectories: Euclidean Distance (ED), and Dynamic Time Warping (DTW). Among these, ED is the square root of the sum of the squared length of vertical or horizontal hatched lines. The disadvantage of using ED is that for trajectories of different length, it cannot calculate their distance reliably.

DTW can compute distances between trajectories when they vary in time, or speed, or path length. Although DTW utilizes a dynamic programming ap-

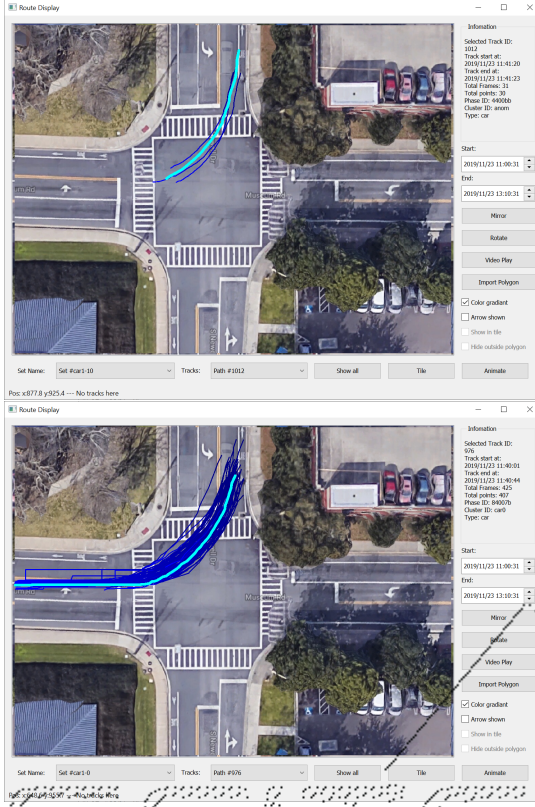


Figure 2: An example where two similar trajectories as highlighted in the top and the bottom images, have high distance value when DTW/FastDTW is directly used to compute distance. This is potentially due to differential tracking of vehicles due to potential occlusion.

proach for an optimal distance and has a time complexity  $O(N^2)$ , where  $N$  is the number of coordinates in the two trajectories, there are approximate approaches such as FastDTW that realize a near-optimal solution and has a space and time complexity of  $O(N)$ . FastDTW is based on a multilevel iterative approach. FastDTW returns a distance and a list of pairs of points, also known as the warp path. A pair of points consists of coordinates on the first and second trajectories and represents the best match between the points after the trajectories are warped. The distance returned by FastDTW is the sum of the distances between each pair of points on the path. Quite naturally, the distance is small if the trajectories occur in the same geographical coordinates and are traversed at similar speeds.

DTW and FastDTW work well for trajectories that are entirely captured by the sensor system. In reality, the sensor system and the processing software may not capture the trajectory in its entirety. In that case, distance returned by the dynamic time warping algorithm is not representative of the actual dis-

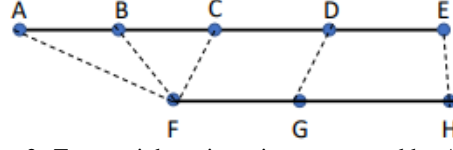


Figure 3: Two straight trajectories represented by ABCDE and FGH. The dashed lines show the point correspondence (warp path) obtained using FastDTW. The trajectory FGH is shorter as the beginning part of the trajectory was not captured.

tance. Figure 2 highlights two example trajectories for which DTW returns a high value for distance suggesting the tracks are dissimilar. For example, for two tracks going straight, if the starting portion of one of the tracks get truncated due to a processing error, as shown in Figure 3, the distance between the tracks will be  $\sqrt{AF^2 + BF^2 + CF^2 + DG^2 + EH^2}$ . Thus, the distance computed results in a high value, which often falls in the range of distance between two unrelated trajectories. Hence, we developed a new distance measure by utilizing the warp path returned by the FastDTW.

## 4 CLUSTERING

We describe our trajectory clustering method in this section. There are two main components to clustering, the first is to use an efficient distance measure for the trajectories to be clustered and the second is to use a clustering algorithm that uses the distance measure to create clusters of trajectories that behave in a similar manner. We describe the novel distance measure developed as part of this work in Section 4.1 and present our clustering algorithm in Section 4.2

### 4.1 Distance Measure

The new distance measure developed in this section, applies to trajectories captured using real-time video processing. The first step in the computation of the distance measure is to obtain the warp path using a time warping algorithm, e.g. FastDTW. Triangles are constructed using the warp path as shown in Figure 3, where the triangles are  $\triangle ABF$ ,  $\triangle BCF$ ,  $\triangle CDF$ ,  $\triangle DFG$ ,  $\triangle DEG$ , and  $\triangle EGH$ . Since the coordinates of the vertices ( $A, B, C, D, E, F, G$ , and  $H$ ) are known, the area of each may be computed using the following formula from coordinate geometry.

$$Area = \left| \frac{a_x(b_y - c_y) + b_x(c_y - a_y) + c_x(a_y - b_y)}{2} \right| \quad (1)$$



where the vertices of the triangle have coordinates:  $(a_x, a_y)$ ,  $(b_x, b_y)$ , and  $(c_x, c_y)$ . The sum of area of all triangles is computed and finally the distance,  $D_{ij}$ , between two trajectories  $T_i$  and  $T_j$ , is computed as:

$$D_{ij} = \left( \sum_{k=1}^n Area_k \right) / \bar{L}_{ij} \quad (2)$$

where  $Area_k$  is the area of the  $k^{th}$  triangle and  $\bar{L}_{ij}$  is the average length of the two trajectories,  $T_i$  and  $T_j$ , and  $n$  is the total number of triangles. If there is no warping, and the number of matched pairs is  $m$ , then  $n = 2m$ , by construction. However, if there is warping, then  $n < 2m$ .  $D_{ij}$  is the average perpendicular distance between the trajectories, which intuitively is the average height of the triangles.

To get a more accurate local distance measure, we segment the trajectories and compute the distance of the starting and the finishing segments. Let  $SD_{ij}$  and  $FD_{ij}$  be the distances of the starting and the finishing segments, respectively. Then,  $SD_{ij}$  is the distance between the first pair of matching points that are not warped ( $CF$  and  $DG$  in Figure 3) and correspondingly,  $FD_{ij}$  is the distance between the last pair of matching points that are not warped ( $DG$  and  $EF$  in Figure 3).  $SD_{ij}$  may be computed as the average height of triangles  $\triangle CFG$  and  $\triangle CDG$ , and  $FD_{ij}$  as that of triangles  $\triangle DGH$  and  $\triangle DEH$ . Thus, we use triplets of  $(D_{ij}, SD_{ij}, FD_{ij})$  to represent the distance between two trajectories. These three portions of the distance measure can be suitably weighed for computing a scalar distance if required.

**Computation of Similarity Matrix.** The similarity matrix,  $S$ , is computed from the distance measures by setting up empirical thresholds for the magnitude of the distance between two trajectories. For example, given two trajectories  $T_i$  and  $T_j$ , if their average distance  $D_{ij}$  of Equation 2 is less than  $x$  and the start section distance,  $SD_{ij}$  is less than  $y$  and the last section distance,  $FD_{ij}$  is less than  $z$ , then  $T_i$  and  $T_j$  are considered similar. The corresponding entry in the similarity matrix, in that case, would be  $S_{ij} = S_{ji} = 1$ . If any distance value exceeds the thresholds -  $x$ ,  $y$ , and  $z$ , then the trajectories would be considered dissimilar and in that case,  $S_{ij} = S_{ji} = 0$ . In this manner, the similarity matrix is computed and is ready to be used in spectral clustering.

## 4.2 Hierarchical Clustering

Clustering a large set of  $N$  trajectories is a  $O(N^2)$  operation since pairwise distance needs to be computed to prepare a distance matrix. A two-level hierarchical clustering scheme is proposed here to address the

```
phase2 WB
SN (562, 880), (560, 149)
NS (560, 149), (562, 880)
WE (84, 536), (962, 547)
EW (962, 547), (84, 536)
phase2stopbar (815, 153), (819, 707)
phase4stopbar (244, 739), (825, 750)
phase6stopbar (330, 155), (287, 726)
phase8stopbar (287, 240), (804, 231)
```

Figure 4: Snippet of a configuration file that shows the user inputs needed for an intersection. The coordinates may be obtained using a visualization tool (Chen et al., 2020).

quadratic complexity. Clustering at the first level partitions the set of trajectories into homogeneous clusters based on their direction of the movement. Then spectral clustering is applied to cluster the trajectories for each phase separately and to detect anomalies. The clustering scheme is explained in detail in this section.

### 4.2.1 Partitioning Trajectories based on Movement Phase

Any object at an intersection must obey the traffic rules, and hence its trajectory is necessarily constrained both in time and space. One of the goals of the software is to detect traffic violations and the underlying causes to make the intersection safer ultimately. These violations may appear as spatial outliers or as timing violations. Figure 1 shows the phases for pedestrian and vehicular movements. A given set of trajectories is partitioned into eight bins aligned respectively with the eight phases and to four additional bins corresponding to the right turns for phases 2, 4, 6, and 8.

Since the trajectories are essentially a series of coordinates, it is possible to use basic vector algebra and trigonometry to get their general direction. For example, the spatial coordinates of a track  $T_i$  is given as  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ . Let  $\vec{A} = [x_1, y_1]$  and  $\vec{B} = [x_n, y_n]$  be two vectors connecting the origin to the start and end points respectively, of  $T_i$ , with their direction away from the origin. Let  $\vec{AB}$  be a vector connecting the start and the end points, with its head at the end point,  $(x_n, y_n)$ . Then, using the rules of vector addition,  $\vec{A} + \vec{AB} = \vec{B}$ , which implies  $\vec{AB} = \vec{B} - \vec{A}$ . Thus,  $\vec{AB} = [x_n - x_1, y_n - y_1]$ .

Once constructed, a trajectory vector may be compared with a reference vector to obtain the direction of the trajectory. The start and endpoints of these reference vectors may be obtained using CAD tools supported by visualization software, and the coordinates of the start and endpoints are specified in a configuration file.

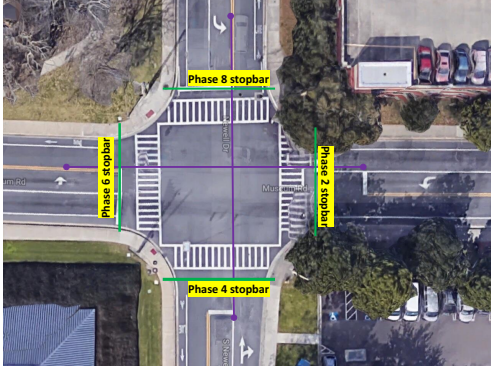


Figure 5: Pictorial representation of information in configuration file.

The cosine of the acute angle between a trajectory vector  $\vec{u}$ , and a reference vector  $\vec{v}$  is given by.

$$\cos \theta = \frac{|\vec{u} \cdot \vec{v}|}{\|\vec{u}\| \|\vec{v}\|} \quad (3)$$

When the directions are nearly matching, the value of the cosine is close to 1.0.

A snippet of a configuration file used to specify the reference vectors is shown in Figure 4. The user can specify the direction of the phase 2 movement using the `phase2` parameter of this file, which has a value WB (West Bound) in this example. The other phases, as described in Figure 1 may be derived with reference to the phase 2 direction. The parameters SN, NS, WE, EW, are used to specify the start and endpoints of reference vectors for through lanes along South-North, North-South, West-East and East-West directions respectively. Figure 5 shows the corresponding reference vectors. The start and endpoint coordinates of the stop bars are also needed to differentiate left and right turn movements that otherwise align with each other. An example of this is given later in this section.

Given a trajectory, the cosine value in Equation 3 may be computed for the trajectory vector and the reference vectors, and if the value computed is close to 1 for any of these vectors, the trajectory may be assigned the corresponding through phase (one of 2, 4, 6 or 8).

For any intersection, the coordinates of the reference vectors have to be determined once, and the configuration file may be reused over time until the geometry of the intersection is changed.

#### 4.2.2 Clustering Trajectories in a Partition

The next step in the hierarchical clustering scheme is to cluster the trajectories that have the same direction of movement. The spectral clustering algorithm

is applied in this step. Prior experimentation with a simple KMeans clustering approach for this problem highlights the benefits of using spectral clustering instead. A pure KMeans algorithm requires user input for the number of possible clusters, which is impossible for the user to know in advance. Spectral clustering, through its smart use of standard linear algebra methods, gives the user objective feedback about the number of possible clusters and further accentuates the features of the trajectories to make the separation of clusters easier.

The inputs to a spectral clustering algorithm are a set of trajectories, say,  $tr_1, tr_2, \dots, tr_n$ , and a similarity matrix  $S$ , where any element  $s_{ij}$  of the matrix  $S$  denotes the similarity between trajectories  $tr_i$  and  $tr_j$ . It is to be noted that we consider  $s_{ij} = s_{ji} \geq 0$ , where  $s_{ij} = 0$  if  $tr_i$  and  $tr_j$  are not similar. Given these two inputs, spectral clustering creates clusters of trajectories such that all trajectories in the same cluster are similar to each other. In contrast, two trajectories belonging to different clusters are not so similar to each other. For example, for the given set of trajectories, spectral clustering creates separate clusters for trajectories following different lanes or those that change lane at the intersection. As a result, spectral clustering also helps identify the outliers, which are anomalous trajectories that are not similar to any of the other trajectories in the set. The two inputs to a spectral clustering algorithm may be represented as a graph  $G = (V, E)$ , where vertex  $v_i$  in this graph represents a trajectory  $tr_i$ . Two vertices are connected if the similarity  $s_{ij}$  between the corresponding trajectories  $tr_i$  and  $tr_j$  is greater than a certain threshold  $\epsilon$ , and the edge is weighted by  $s_{ij}$ . Thus, the clustering problem may be recast as finding connected components in the graph such that the sum of the weights of edges between different components is small. Hence, by obtaining the number of connected components we know the number of clusters and then get the clusters by applying a KMeans algorithm.

We used the *linalg* library provided by NumPy and to perform the linear algebra operations in spectral clustering. Once the number  $k$  of connected components is known, a KMeans algorithm is run on the first  $k$  eigenvectors to come up with the clustering results. The function *KMeans* is a standard KMeans clustering algorithm from the Python *sklearn.cluster* library.

The clusters generated by spectral clustering for all the left turn trajectories are shown in Figure 6. The clusters for straight and right turn trajectories are omitted here due to space constraints.



Figure 6: Second level of the two-level hierarchical clustering scheme where spectral clustering is applied on trajectories with the same direction of motion. The clusters of some left-turn trajectories are presented in this figure.

### 4.2.3 Finding Representative Trajectory

After the trajectories are clustered, we identify a trajectory in each cluster that is representative of that cluster. The representative for each cluster is computed as the trajectory  $t$  belonging to the cluster that has the least average distance from all the other trajectories.

## 5 ANOMALOUS BEHAVIOR

Detecting anomalous traffic behavior is one of the top goals for clustering trajectories. An anomalous trajectory may be one that violates the spatial or temporal constraints at an intersection. The spatial constraints amount to the restrictions a vehicle must follow at an intersection, such as never go in the wrong way. Temporal constraints, on the other hand, are the restrictions imposed by the signaling system at an intersection. We consider these two types of anomalous behavior in the rest of this section.

**Signal Timing Violations.** The fusion of video and SPaT data allows us to detect the validity of the trajectories with reference to the current signaling phase of the intersection. The video clock and the SPaT clock are sometimes off by a few seconds. The clocks may be treated as synchronous by adding an offset to the trajectories. This offset may be computed manually by comparing the time a signal in the video transitions to green and the time in the SPaT when there

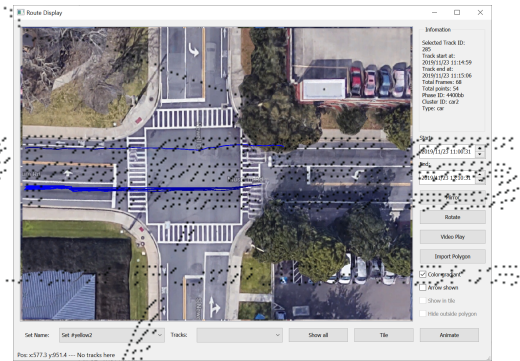


Figure 7: Collection of tracks representing vehicles that enter the intersection on a yellow light.

is a “Phase Begin Green” event for the corresponding phase. It is also possible to compute the offset automatically in software by checking the timestamp of the first trajectory that crosses, say, the phase2 stop bar, (Figure 5) and the timestamp in SPaT when phase 2 signal becomes green and then adding a 2.5 seconds of driver reaction time to the signal transition timestamp. Figure 7 shows the trajectories that happen during a yellow light.

**Trajectory Shape Violation.** Figure 8 shows the anomalous trajectories. In all the cases here, the trajectories are turn movements. Sometimes these trajectories take a very wide turn. At other times the trajectories turn left from a through lane, and at still other times, the trajectories start taking a turn much before the actual stop bar, causing wrong-way access to the adjacent lane.





Figure 8: Collection of tracks that represent vehicles that have anomalous behavior because of their shape.

## 6 CONCLUSIONS

We presented a novel method for analyzing vehicle and pedestrian trajectories at intersections and applying data mining techniques to find patterns and anomalies. We developed a new distance measure specifically for two trajectories at a traffic intersection. We applied a hierarchical clustering algorithm based on geometric properties of the trajectories and spectral clustering. We demonstrated our workflow on a real-life intersection. We augment trajectory data with SPaT data and show an example of how this is useful in detecting vehicles that crossed an intersection on a yellow light, and also potentially detecting signal violations. This application may be leveraged to implement useful applications to determine turn movement counts, to monitor demand and throughput of an intersection, to detect and manage incidents at an intersection.

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