



# Determining water content and bulk density: The heat-pulse method outperforms the thermo-TDR method in high-salinity soils

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## ABSTRACT

Heat-pulse (HP) and thermo-time domain reflectometry (thermo-TDR) methods have been used to determine soil thermal properties, water content ( $\theta$ ) and bulk density ( $\rho_b$ ) simultaneously. Their performances on salt-affected soils, however, remain unknown. This study investigated the effect of salinity on HP signals and thermo-TDR measured electromagnetic waveforms, and the derived  $\theta$  and thermal property values of packed soil columns with various textures, saturations and bulk electrical conductivities ( $\sigma_a$ ). The thermo-TDR and HP-based methods for estimating  $\rho_b$  values were also evaluated. The results showed that: (1) at  $\sigma_a$  values lower than  $1.0 \text{ dS m}^{-1}$ , the TDR method provided reliable  $\theta$  with relative errors within 5%; salt effects became apparent at  $\sigma_a$  values greater than  $1.0 \text{ dS m}^{-1}$  due to the distortion of TDR waveforms; the TDR method failed to estimate  $\theta$  at  $\sigma_a > 2.71 \text{ dS m}^{-1}$  because the 2nd reflection point on the waveform was undetectable; (2) salinity had negligible effects on soil thermal property values in the studied range ( $\sigma_a < 7.59 \text{ dS m}^{-1}$ ), and the HP-based approach was able to derive  $\theta$  and  $\rho_b$  values from thermal property measurements, with root mean square errors within  $0.02 \text{ m}^3 \text{ m}^{-3}$  for  $\theta$  and within  $0.12 \text{ Mg m}^{-3}$  for  $\rho_b$ . Thus, the HP-based approach outperformed the thermo-TDR approach for determining  $\theta$  and  $\rho_b$  values in soils with  $\sigma_a > 1.0 \text{ dS m}^{-1}$ .

## 1. Introduction

Quantitative determination of soil water content ( $\theta$ ), thermal property values, electrical conductivity ( $\sigma_a$ ) and bulk density ( $\rho_b$ ) are required to characterize the physical state and transfer processes in salt-affected soils (Nassar et al., 1997; Nassar and Horton, 1999; Hamamoto et al., 2010). In saline soils, coupled transport processes of water and heat are accompanied by salt dissolution and precipitation which often lead to porosity variations (Olivella et al., 1996). Therefore, it is important to determine soil thermal property values,  $\theta$ ,  $\sigma_a$ , and  $\rho_b$  simultaneously to study coupled processes in salt-affected soils.

The heat-pulse (HP) method is widely used to determine soil thermal properties, i.e., soil heat capacity ( $C$ ) and thermal conductivity ( $\lambda$ ). A thermo-TDR sensor, which integrates HP and time domain reflectometry (TDR) functions, can measure in situ values of  $C$ ,  $\lambda$ ,  $\theta$ , and  $\sigma_a$  (Ren et al., 1999). Thermo-TDR and HP techniques can also determine in situ  $\rho_b$  based on  $C$  and  $\lambda$  models that express soil thermal property dependence on  $\theta$  and  $\rho_b$  (Ren et al., 2003a; Ren et al., 2003b; Liu et al., 2008; Lu et al., 2016; Lu et al., 2018). Therefore, with sensor determined  $C$ ,  $\lambda$  and  $\theta$  values,  $\rho_b$  can be derived from either a  $C$  model or a  $\lambda$  model (de Vries,

1963; Lu et al., 2014; Tian et al., 2016). Thermo-TDR and HP methods have been reported to provide in situ, non-destructive measurements of  $\rho_b$  in laboratory and field soils (Liu et al., 2008; Tian et al., 2018; Fu et al., 2019).

In saline soils, salts have influence on both dielectric and thermal properties of soil. The TDR technique measures the travel time of electromagnetic waves and determines the apparent dielectric constant ( $K_a$ ) of a soil based on the travel time. Then  $\theta_{\text{TDR}}$  can be derived from an empirical  $\theta$ - $K_a$  equation such as the Topp et al. (1980) equation. A soil complex dielectric constant is composed of a real component (i.e.,  $K_a$ ) and an imaginary component, which represents the ionic conductivity losses and relates to  $\sigma_a$  (Nigara et al., 2015; Kargas and Soulis, 2019). Therefore, the TDR waveforms from saline soils can be used to estimate  $\sigma_a$  (Muñoz-Carpena et al., 2005). The presence of salt mainly affects the imaginary component of a soil complex dielectric constant (Nigara et al., 2015). The effect of salt on  $K_a$  values is not clear.

For the TDR technique,  $\theta_{\text{TDR}}$  and  $\sigma_a$  measurements are both based on the propagation/reflection of voltage signals along parallel waveguides (Noborio, 2001; Robinson et al., 2003; Jones et al., 2002; Wang et al., 2021). However, in soils with high electrical conductivity, it is

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challenging to measure  $\theta_{\text{TDR}}$  and  $\sigma_a$  due to the fact that salts alter the propagation speed and attenuate the energy of voltage signals significantly (Dalton, 1992; Sun et al., 2000; Nichol et al., 2002; Jones and Or, 2004; Schwartz et al., 2014). It is unlikely to determine  $\theta_{\text{TDR}}$  accurately with high  $\sigma_a$  values in saline soils because salt affects the measurement of  $K_a$  (Regalado et al., 2007). It was reported that  $\theta_{\text{TDR}}$  and  $K_a$  values were overestimated in soils with  $\sigma_a$  larger than 2 dS m<sup>-1</sup> (Wyseure et al., 1997). Therefore, the errors in  $\theta_{\text{TDR}}$  might cause errors in  $\rho_b$  and  $\theta$  determination when applying the thermo-TDR method in salt-affected soils.

The presence of salt might affect soil thermal property values. There are contradictory reports about salt effects on soil  $\lambda$ . Researchers reported no apparent effects of solution concentrations of CaCl<sub>2</sub> up to 0.18 mol kg<sup>-1</sup>, or with NaCl up to 0.34 mol kg<sup>-1</sup> on  $\lambda$  of quartz sands (e.g., Van Rooyen and Winterkorn, 1959). However, Noborio and McInnes (1993) observed a reduction in soil  $\lambda$  with increasing soil solution concentrations (CaCl<sub>2</sub>, MgCl<sub>2</sub>, NaCl, or Na<sub>2</sub>SO<sub>4</sub>) from 0.10 mol kg<sup>-1</sup> to solubility limits, because the increasing soil solution concentrations decreased the  $\lambda$  of soil solution, and chemical interactions between the soil solution and mineral particles, which could lead to the decrease of soil  $\lambda$ . Abu-Hamdeh and Reeder (2000) also found that soil  $\lambda$  decreased with increased concentrations of CaCl<sub>2</sub> and NaCl. Mochizuki et al. (2008) reported soil dependent-effects of salts on  $\lambda$ . For sand and non-swelling clay,  $\lambda$  remained stable or decreased with increasing NaCl concentration, while the  $\lambda$  of a swelling clay was unaffected by increasing NaCl concentrations. A complex mechanism involving many factors such as water content, salt content, and the differences in free water and salt solution affected the soil  $\lambda$  (Mochizuki et al., 2008). Also, little is known on the effect of salts on soil  $C$  values. So, it remains uncertain on how salts affect the determination of soil thermal properties and  $\theta_{\text{TDR}}$ , as well as the consequences on  $\rho_b$  and porosity values derived from HP or thermo-TDR measurements. There is a need to determine the accuracy of HP and thermo-TDR methods to estimate soil property values in salt-affected soils.

In this study, a thermo-TDR sensor is used to determine  $\theta$ , soil thermal property values and  $\rho_b$  in salt-affected soils. Our specific objectives are (1) to analyze the trends of electromagnetic waveforms as affected by soil salinity and its consequences on  $\theta_{\text{TDR}}$  determination; (2) to examine the effect of salts on  $C$  and  $\lambda$ , and to determine the accuracy of  $\rho_b$  and  $\theta$  values derived from thermo-TDR measurements as well as from HP measurements in salt-affected soils.

## 2. Theories

### 2.1. Determination of soil thermal property values, $\theta_{\text{TDR}}$ and $\sigma_a$ with a thermo-TDR technique

A thermo-TDR sensor measures the HP signals (temperature rise with time data) and electromagnetic waveforms. To estimate soil thermal property values accurately, we used the theory of cylindrical-perfect-conductors to analyze the HP signals, which accounted for the finite probe radius and finite probe heat capacity (Knight et al., 2012; Peng et al., 2021). To determine  $\theta_{\text{TDR}}$  and  $\sigma_a$ , the tangent line/second-order bounded mean oscillation model was used to analyze the electromagnetic waveforms and determine the reflection points and  $K_a$  values accurately (Wang et al., 2014, 2016). Then  $\theta_{\text{TDR}}$  was determined from  $K_a$  with the Topp et al. (1980) equation.

For the derivation of  $\sigma_a$ , Heimovaara et al. (1995) provided the following equation,

$$\sigma_a = \frac{K_p}{R_{\text{total}} - R_c} f_T \quad (1)$$

where  $K_p$  is the cell constant of the probe (8.77 m<sup>-1</sup>) which is calibrated with different KCl solutions (Heimovaara et al., 1995).  $R_{\text{total}}$  is the total resistance of the cable tester, coaxial cable, and probes, and it can be

calculated from the amplitude of the TDR waveforms at very long times. Refer to the first section of the Supplemental Material for the calculation of  $R_{\text{total}}$  using Eq. (S1).  $R_c$  is the combined series resistance of the cable, connectors, and cable tester. Earlier studies reported that  $R_c$  was only a small fraction of the  $R_{\text{total}}$  (Huisman et al., 2008). Thus, in this study, we neglected  $R_c$ , and only used  $K_p$  and variable  $R_{\text{total}}$  to calculate  $\sigma_a$ .

The  $\sigma_a$  needs to be corrected with a temperature factor  $f_T$  (Heimovaara et al., 1995),

$$f_T = \frac{1}{1 + \mu(T - 25)} \quad (2)$$

in which  $\mu$  is the temperature coefficient of the soil sample at the reference temperature of 25°C (0.0191°C<sup>-1</sup>, Heimovaara et al., 1995), and  $T$  (°C) is the soil sample temperature at the measurement time.

### 2.2. Estimation of $\rho_b$ values with the thermo-TDR and HP based methods

Based on quantitative relationships between values of  $C$ ,  $\lambda$  and  $\theta_{\text{TDR}}$ , thermo-TDR and HP based methods can be used to determine  $\theta$  and  $\rho_b$  of salt-affected soils.

#### 2.2.1. Thermo-TDR method to estimate $\rho_b$ values

The de Vries (1963)  $C$  model, describing the linear relationship between  $C$  and  $\theta$ , provides a way to determine in situ  $\rho_b$  (hereafter called the  $C$ -based thermo-TDR method, Ochsner et al., 2001; Ren et al., 2003a; Ren et al., 2003b),

$$\rho_b = \frac{C - \theta c_w}{c_s} \quad (3)$$

in which  $c_s$  (0.742 kJ kg<sup>-1</sup> K<sup>-1</sup>, Wang et al., 2019) is the specific heat capacity of soil solids, and  $c_w$  (4.18 kJ kg<sup>-1</sup> K<sup>-1</sup>, Campbell et al., 1991) is taken as the specific heat capacity of free water. With the Eq. (3), the  $\rho_b$  values are estimated directly with the thermo-TDR measured  $C$  and  $\theta$  values.

The  $\lambda$ -based thermo-TDR method to determine  $\rho_b$  was developed with the purpose of eliminating the possibility of probe-deflection errors in  $C$  measurements (Lu et al., 2016; Tian et al., 2018). The empirical  $\lambda$  model from Lu et al. (2016) was adopted,

$$\begin{cases} \lambda = \lambda_{\text{dry}} + \exp(\beta - \theta^{-\alpha}) \\ \alpha = 0.67f_{\text{cl}} + 0.24 \\ \beta = 1.97f_{\text{sa}} + 1.87\rho_b - 1.36f_{\text{sa}}\rho_b - 0.95 \\ \lambda_{\text{dry}} = -0.56(1 - \rho_b/2.65) + 0.51 \end{cases} \quad (4)$$

where  $\lambda_{\text{dry}}$  (W m<sup>-1</sup> K<sup>-1</sup>) is the thermal conductivity of dry soil;  $\alpha$  and  $\beta$  are shape factors determined by soil particle sizes and  $\rho_b$ , and  $f_{\text{sa}}$  and  $f_{\text{cl}}$  are the mass fractions of sand and clay particles under the USDA soil texture classification system. There is no explicit solution for  $\rho_b$  from Eq. (4), so after assigning an initial  $\rho_b$  of 1.0 Mg m<sup>-3</sup>, an iterative approach is used to solve for  $\rho_b$  values using the nonlinear equation solver ( $f_{\text{solve}}$ ) in MATLAB (Mathworks, Inc.) (Lu et al., 2017).

In this study, following Peng et al. (2019), a combination of the  $C$ -based and  $\lambda$ -based thermo-TDR approaches was used, i.e., the  $C$ -based approach was used when  $\theta$  was less than 0.10 m<sup>3</sup> m<sup>-3</sup>, and the  $\lambda$ -based approach was used when  $\theta$  was greater than 0.10 m<sup>3</sup> m<sup>-3</sup>. Both the  $C$ -based and the  $\lambda$ -based thermo-TDR approaches required a  $\theta_{\text{TDR}}$  value to estimate  $\rho_b$ .

#### 2.2.2. The HP-based approach to estimate $\theta_{\text{HP}}$ and $\rho_b$ values

We also applied a HP-based method to estimate  $\rho_b$  values based solely on measured  $C$  and  $\lambda$  values without requiring a  $\theta_{\text{TDR}}$  value (Lu et al., 2018). The HP-based method followed a three-step procedure to obtain  $\theta_{\text{HP}}$  and  $\rho_b$  values (Lu et al., 2018). Step 1 included the rough estimation of  $\theta_{\text{HP}}$  from a measured  $C$  value,

$$\theta_{HP} = \frac{C - \rho_b c_s}{c_w} \quad (5)$$

in which  $\rho_b$  ( $\text{Mg m}^{-3}$ ) is an initial value assumed to be  $1.5 \text{ Mg m}^{-3}$  for coarse-textured soil with  $f_{sa}$  greater than 0.40 and a value of  $1.0 \text{ Mg m}^{-3}$  for fine-textured soils with  $f_{sa}$  less than 0.40 (Lu et al., 2018). In the second step, the approximate  $\theta_{HP}$  value in Step 1 and the measured  $\lambda$  value were used to estimate the  $\rho_b$  value iteratively with Eq. (4). In step 3, the final  $\theta_{HP}$  value was re-calculated with Eq. (5) by using the updated  $\rho_b$  value obtained in Step 2.

### 3. Materials and methods

To evaluate the performance of HP-based and thermo-TDR-based methods in salt-affected soils, a thermo-TDR sensor was used to measure HP signals and electromagnetic waveforms on soil samples moistened with various concentrations of KCl solutions.

#### 3.1. Thermo-TDR sensor configuration

The Peng et al. (2019) thermo-TDR sensor was selected for this study because its heating probe rigidity, sharpened probe tips and thin sensing probes minimized soil disturbance and changes in probe spacing during sensor insertion. The thermo-TDR sensor has three parallel stainless-steel probes: one heater probe and two sensing probes with pointed tips that are mounted in a casting epoxy resin head. The probes are 70 mm long, and the heater probe and sensing probe have outer diameters of 2.38 mm and 2.00 mm, respectively. The spacing between the heater probe and each sensing probe is about 10 mm. Each sensing probe contains three thermocouples, positioned at 20, 35, and 50 mm away from the epoxy resin base. The inner conductor and the shield of the coaxial cable are soldered to the ends of the heater probe and the sensing probes, respectively.

#### 3.2. Thermo-TDR sensor calibration

Prior to making measurements of soil thermal properties,  $\theta_{TDR}$  and  $\sigma_a$ , the probe spacing, apparent probe length, and  $K_p$  of the thermo-TDR sensor were calibrated. The probe spacing was calibrated in agar-immobilized water ( $5 \text{ g L}^{-1}$ ) at  $20^\circ\text{C}$  by taking heat capacity of agar-immobilized water as  $4.18 \text{ MJ m}^{-3} \text{ K}^{-1}$ , which assumed that heat capacity of water was not affected by the addition of agar (Campbell et al., 1991). A nonlinear regression method was used to fit the HP signals to inversely estimate probe spacing. The apparent probe length of the thermo-TDR sensor was calibrated by analyzing a TDR waveform in distilled water with apparent dielectric constant of water as 80.1 at  $20^\circ\text{C}$  (Haynes and Lide, 2010).

The  $K_p$  value was determined following the procedures of Heimo-vaara et al. (1995). TDR waveforms were collected after immersing the sensor in KCl solutions with the following concentrations: 0.0001, 0.0005, 0.001, 0.005, 0.01, 0.02, 0.1, and  $1.0 \text{ mol L}^{-1}$  (Fig. S2 in Supplemental material). Because  $R_{total}$  values could vary with KCl solution concentrations, TDR waveforms were used to calculate the variable  $R_{total}$  values. The electrical conductivity values for KCl solutions were measured with a conductivity meter (model DDS-307A, Shanghai INESA Scientific Instrument Co., China). Then  $K_p$  value of the thermo-TDR sensor was calculated by using regression analysis of electrical conductivity values vs.  $R_{total}$  (Ren et al., 1999).

#### 3.3. Thermo-TDR measurements in salt-affected soils

Thermo-TDR measurements were made on three soils with varying textures (Table 1). Soil particle-size distributions of the studied soils were measured with the pipette method (Gee and Or, 2002). Soil samples were air-dried, crushed, and sieved through a 2-mm screen. Two different experimental methodologies: individual and continuous

**Table 1**

Texture, particle size distribution and bulk density ( $\rho_b$ ) of the repacked soils used in this study.

Texture	Particle size distribution			$\rho_b$
	2–0.05 mm	0.05–0.002 mm	<0.002 mm	
	%			$\text{Mg m}^{-3}$
Sand	94	1	5	1.50–1.60
Loam	48	38	14	1.24–1.40
Silt Loam	27	50	23	1.30

measurements were performed to explore the effects of salt on thermo-TDR measurements. For Soils 1 (sand) and 2 (loam) with individual measurements, disturbed samples were mixed thoroughly with either distilled water or KCl solutions of various concentrations and repacked uniformly into PVC columns (with a height of 80 mm and a diameter of 70 mm). The dry and wet packing procedures in Oliveira et al. (1996) were used as a reference to pack soil columns uniformly. Prior to packing a soil column, a soil sample was divided into four equal parts. One of the parts was poured into a cylinder to form a 2-cm thick layer. A 6-cm diameter cylindrical wooden rod was used to press the soil layer to a desired density, and the surface of the soil layer was lightly scratched to prevent stratification within the soil column. The packing steps were repeated with the other soil parts until the cylinder was filled. This produced a series of soil columns with  $\sigma_a$  ranging from 0.07 to  $7.59 \text{ dS m}^{-1}$  and  $\theta$  values of 0.08, 0.15, 0.20 and  $0.25 \text{ m}^3 \text{ m}^{-3}$ . The relatively small  $\rho_b$  ranges of the soil columns were  $1.55 \pm 0.05 \text{ Mg m}^{-3}$  for Soil 1 and  $1.35 \pm 0.05 \text{ Mg m}^{-3}$  for Soil 2, respectively, which was a result of careful packing. The soil columns were allowed to equilibrate at room temperature ( $20^\circ\text{C}$ ) before thermo-TDR measurements. Five repeated measurements were made on each column before the soil columns were oven dried at  $105^\circ\text{C}$  for 24 h to determine the actual  $\theta$  and  $\rho_b$  values.

For Soil 3 (silt loam), continuous measurements in time were used to determine the dynamic  $\theta$  and  $\sigma_a$  values. The sample was packed to a  $\rho_b$  of  $1.30 \text{ Mg m}^{-3}$  and was saturated from bottom to top with a  $0.1 \text{ mol L}^{-1}$  KCl solution. Two thermo-TDR sensors were inserted into the soil column horizontally at the depths of 20 mm and 60 mm. The saturated column was allowed to dry gradually with one end open to the atmosphere. During the evaporation process, a balance recorded the water loss hourly and a series of HP and TDR measurements were obtained over a 10-day period until the soil column mass approached a relatively constant value. The  $\sigma_a$  and  $\theta$  values for the whole column were taken as the average of the readings from the two sensors.

To make a HP measurement, a current of 0.23 A was applied to the central heater probe with a direct current supply for 25 s to release heat energy, and temperature changes with time at the sensing probes were recorded for 480 s at a 1-s interval. The TDR measurements were made by using a TDR200 reflectometer (Campbell Scientific Inc., Logan, UT). The HP signals and TDR waveforms were recorded with a datalogger (model CR3000, Campbell Scientific Inc., Logan, UT). Based on the previously stated theories, soil thermal property,  $\theta$  and  $\sigma_a$  data were derived from the HP signals and TDR waveforms, respectively. In this study, the average  $C$  and  $\lambda$  values were derived from measured HP datasets with the six thermocouples.

#### 3.4. Error analysis

Soil thermal property values determined with the thermo-TDR measurements were compared to values obtained from the soil thermal property models, i.e. de Vries (1963)  $C$  model and Lu et al. (2014)  $\lambda$  model. The  $\theta_{TDR}$ ,  $\theta_{HP}$  and  $\rho_b$  were compared to values obtained with the oven-dry method. Root mean square error (RMSE) and bias were used to evaluate the performances of the thermo-TDR and HP methods in salt-affected soils,

$$RMSE = \sqrt{\frac{\sum (x_e - x_m)^2}{n}} \quad (6)$$

$$\text{bias} = \frac{\sum (x_e - x_m)}{n} \quad (7)$$

where  $x_e$  represents the soil thermal property values,  $\theta_{TDR}$ ,  $\theta_{HP}$  or  $\rho_b$  derived from thermo-TDR and HP methods,  $x_m$  represents thermal property values estimated with soil thermal property models or determined gravimetrically (i.e., oven-dried  $\theta$  and  $\rho_b$ ),  $n$  is the number of the values.

#### 4. Results and discussion

In this section, we presented the analysis of the effects of salts on thermo-TDR sensor measured electromagnetic waveforms and on derived  $\theta_{TDR}$  values. An approximate  $\sigma_a$  threshold value was determined for estimating  $\theta_{TDR}$  with the TDR technique. Additionally, we evaluated the effects of salts on  $C$  and  $\lambda$  measurements, and the performances of thermo-TDR and HP-based methods to determine  $\theta$  and  $\rho_b$  values in salt-affected soils.

##### 4.1. Salt effects on thermo-TDR waveforms for determining $\theta_{TDR}$ values

Fig. 1 shows the recorded TDR waveforms from the thermo-TDR sensor on Soils 1, 2 and 3. For Soils 1 and 2,  $\theta$  was in the range of 0.08–0.25  $\text{m}^3 \text{m}^{-3}$ , and  $\sigma_a$  varied from 0.09 to 2.88  $\text{dS m}^{-1}$  on the sand soil and from 0.07 to 6.02  $\text{dS m}^{-1}$  on the loam soil (Fig. 1a–1b). For Soil 3,  $\theta_{HP}$  values decreased from 0.37 to 0.20  $\text{m}^3 \text{m}^{-3}$  and  $\sigma_a$  decreased from 2.71 to 1.08  $\text{dS m}^{-1}$  during the 10-day monitoring period (Fig. 1c). It is apparent that the first reflection position  $L_1$  remained constant (i.e.,  $L_1$  was unaffected by  $\theta$  and  $\sigma_a$ ), while the second reflection position  $L_2$  varied significantly with  $\theta$  and  $\sigma_a$ . Larger  $L_2$  values were obtained at larger  $\theta$  values, and  $L_2$  became less identifiable as  $\sigma_a$  increased. This was attributed to the fact that for soil samples with high  $\sigma_a$  values, the electromagnetic signals were partially dissipated in the soils, which led to vagueness in the reflected TDR waveforms.

The final voltage amplitude of electromagnetic signals gradually decreased with increasing  $\sigma_a$  and were close to zero at  $\sigma_a$  of 22.5  $\text{dS m}^{-1}$  (refer to Fig. S2 in the Supplemental material). The uncertainties in  $L_2$  values at the higher salt concentrations usually led to relatively large errors in  $K_a$  and  $\theta_{TDR}$  values (Dalton, 1992; Nichol et al., 2002). In this study, compared with the gravimetric  $\theta$  values, the  $RMSE$  of  $\theta_{TDR}$  values was 0.06  $\text{m}^3 \text{m}^{-3}$  for the sand and loam soils, and 0.09  $\text{m}^3 \text{m}^{-3}$  for the silt loam soil. A 0.01 m change in  $L_2$  caused a  $\theta_{TDR}$  error up to 0.02  $\text{m}^3 \text{m}^{-3}$ . In addition, the relative error in  $\theta_{TDR}$  estimates was  $\sigma_a$  dependent. It was within 5% when  $\sigma_a$  was less than 1.0  $\text{dS m}^{-1}$ , and when  $\sigma_a$  values were larger than 1.0  $\text{dS m}^{-1}$ , it reached 16% as  $\sigma_a$  increased. These results generally agreed with those from reports on other saturated and unsaturated saline soils (Wyseure et al., 1997; Sun et al., 2000; Topp et al., 2000). Besides, the effects of salt on the relationship of  $\theta$  and  $K_a$  could not be neglected (Wyseure et al., 1997; Tan et al., 2018). Later, the  $\theta$ - $K_a$  equation in Topp et al. (1980) should be revisited for its accuracy to estimate  $\theta$  in saline soils.

The attenuation of electromagnetic signals was influenced by several factors such as  $\theta$ , soil texture, salinity, cable length and probe geometry (Jones et al., 2002). For TDR sensors, the waveform reflections (e.g.,  $L_2$ ) necessary for  $K_a$  measurements could be totally attenuated in soils with high  $\sigma_a$  values. It was reported that the negative effect of electrical conductivity on the amplitude of electromagnetic signals was reduced as the probe became shorter (Noborio et al., 2001; Nichol et al., 2002). Ren et al. (1999) gave a threshold value of 6.06  $\text{dS m}^{-1}$  for a sensor with probe length of 40 mm. A much lower threshold value of 2  $\text{dS m}^{-1}$  was reported for a sensor with a probe length of 160 mm (Nichol et al., 2002). For the thermo-TDR sensor used in this study, the  $L_2$  values could

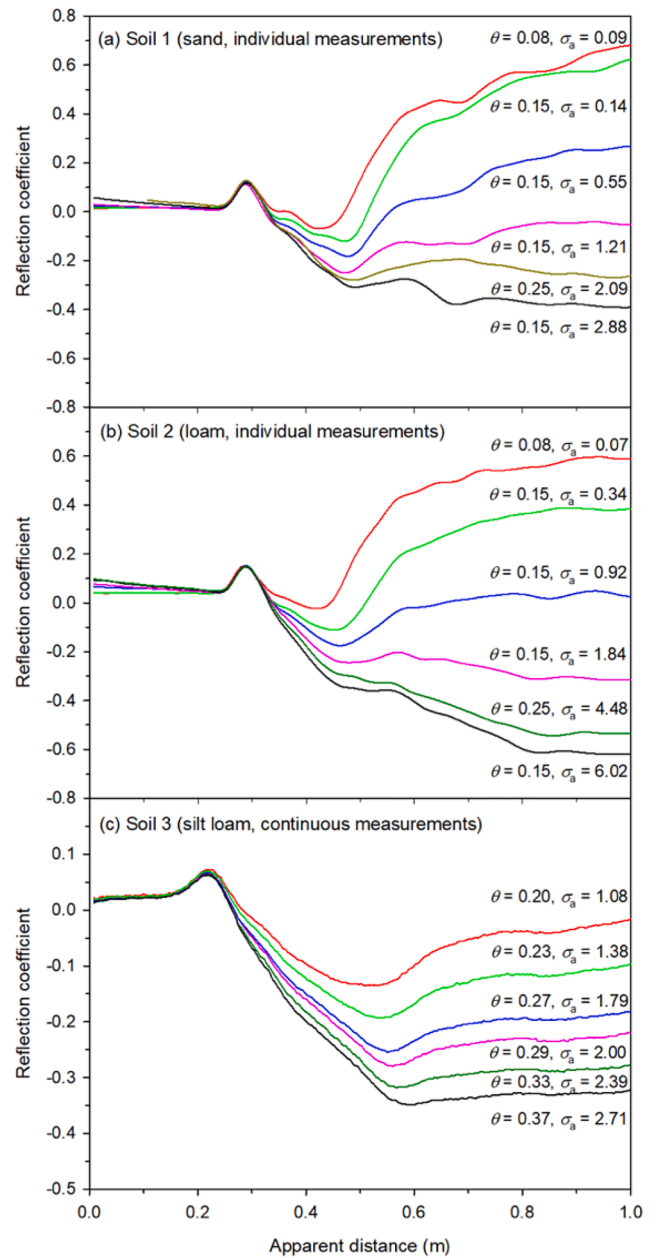


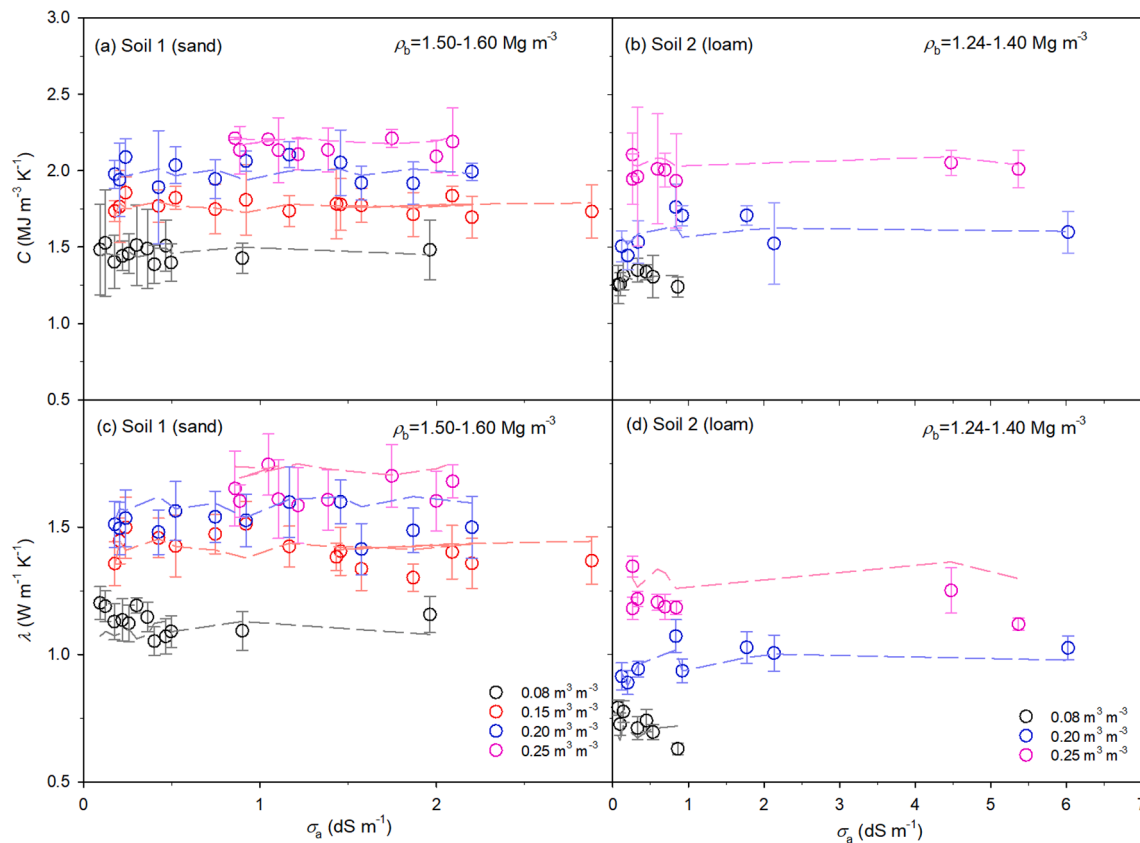
Fig. 1. Time domain reflectometry waveforms measured by thermo-TDR sensors for Soils 1–3 at specified water content values ( $\theta$ ,  $\text{m}^3 \text{m}^{-3}$ ) and bulk soil electrical conductivity values ( $\sigma_a$ ,  $\text{dS m}^{-1}$ ).

not be clearly distinguished, and thus, they were unusable for  $\theta_{TDR}$  estimations when  $\sigma_a$  was greater than 2.88  $\text{dS m}^{-1}$  in the sand soil, 4.48  $\text{dS m}^{-1}$  in the loam soil, and 2.71  $\text{dS m}^{-1}$  in the silt loam soil (Fig. 1).

##### 4.2. Salt effects on thermo-TDR measured soil $C$ and $\lambda$ values

Fig. 2 presents measured and modeled  $C$  and  $\lambda$  values as a function of  $\sigma_a$  and  $\theta$  for the sand and loam soils. The dashed curves represent the  $C$  values estimated with the de Vries (1963) model (Eq. (3)) and the  $\lambda$  values estimated with the Lu et al. (2014) model (Eq. (4)). The thermo-TDR measured  $C$  and  $\lambda$  results agreed well with the model estimates. For the conditions of this experiment, soil  $C$  and  $\lambda$  values varied significantly with  $\theta$ , while not much changes in  $C$  and  $\lambda$  were observed with increasing  $\sigma_a$ . The strong variations in the measured  $C$  values might have resulted from probe spacing changes due to repeated insertion of the sensors into the soil samples (Fig. 2a–2b).





**Fig. 2.** Thermo-TDR sensor measured soil heat capacity ( $C$ ) and thermal conductivity ( $\lambda$ ) as a function of soil bulk electrical conductivity ( $\sigma_a$ ) on the sand and loam soils at various water content and bulk density ( $\rho_b$ ) values. The dashed curves are  $C$  or  $\lambda$  values estimated with the de Vries (1963)  $C$  model or the Lu et al. (2014)  $\lambda$  model. Each value represents the mean of five repeated measurements. The error bars indicate the standard deviations.

Controversial reports existed in the literature about salinity effects on soil thermal property values. In a quartz sand, Van Rooyen and Winterkorn (1959) reported no noticeable  $\lambda$  changes when  $\text{CaCl}_2$  solution concentration was up to  $0.18 \text{ mol kg}^{-1}$  or  $\text{NaCl}$  solution concentration was up to  $0.34 \text{ mol kg}^{-1}$ , which agreed with our results that salts had negligible effects on  $C$  and  $\lambda$  measurements. However, Mochizuki et al. (2008) reported that increasing  $\text{NaCl}$  concentration (from 0 to  $3 \text{ mol kg}^{-1}$ ) decreased the  $\lambda$  values of a sand and a non-swelling clay, but increased the  $\lambda$  values of glass beads in the middle to high  $\theta$  range. Besides, we only performed experiments on soils with  $\text{KCl}$  solutions. Other salts such as  $\text{NaCl}$ ,  $\text{CaCl}_2$  and  $\text{MgCl}_2$ , differ in their interactions with clay particles, and might cause flocculation and aggregation in saline soils, which could lead to changes in soil  $\lambda$  (Abu-Hamdeh and Reeder, 2000). Thus, further research is needed to investigate the integrative effects of various salts, soil water, clay minerals, organic matter, as well as the structure (e.g., aggregation) on thermal properties of salt-affected soils.

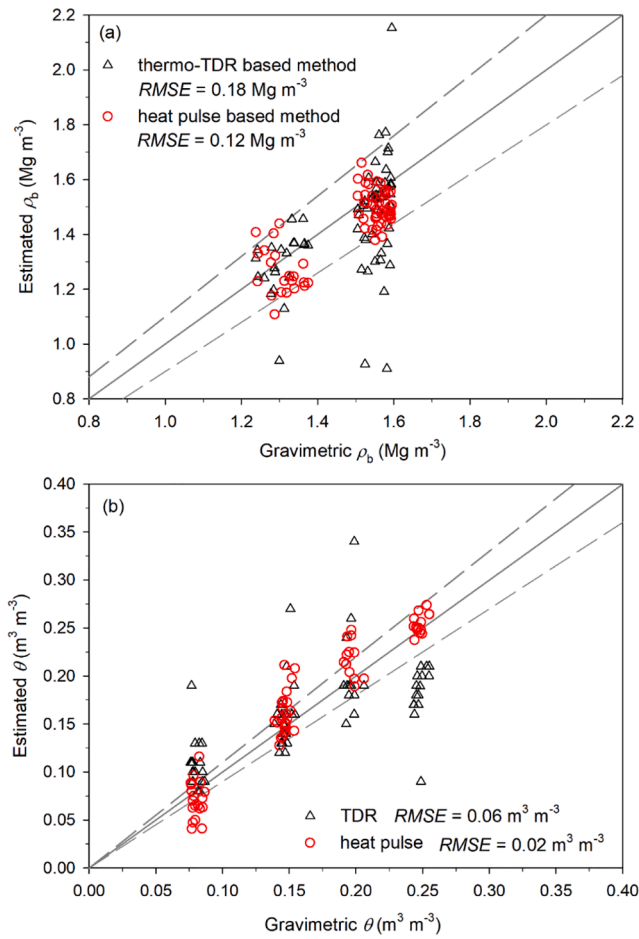
#### 4.3. Determination of $\rho_b$ and $\theta$ values of salt-affected soils with the HP and thermo-TDR based methods

The determination of  $\rho_b$  and  $\theta$  can be achieved with either HP-based or thermo-TDR based methods. Fig. 3 compares the derived  $\rho_b$  and  $\theta$  estimates with the HP-based or thermo-TDR based methods to the directly measured mass determined values for soil cores with  $\sigma_a$  ranging from  $0.07$  to  $7.59 \text{ dS m}^{-1}$ . Compared to the directly measured mass determined  $\rho_b$  and  $\theta$  values, the  $RMSEs$  were  $0.18 \text{ Mg m}^{-3}$  and  $0.06 \text{ m}^3 \text{ m}^{-3}$  for the thermo-TDR estimated  $\rho_b$  and  $\theta_{TDR}$  values, respectively (Fig. 3). As stated earlier, the  $\theta_{TDR}$  errors were mainly caused by uncertain  $L_2$  values, which limited the accuracy of  $\theta_{TDR}$  and  $\rho_b$  estimates, resulting in several thermo-TDR estimated  $\rho_b$  and  $\theta_{TDR}$  values to deviate from the 1:1 line. The application of the Topp et al. (1980) equation in

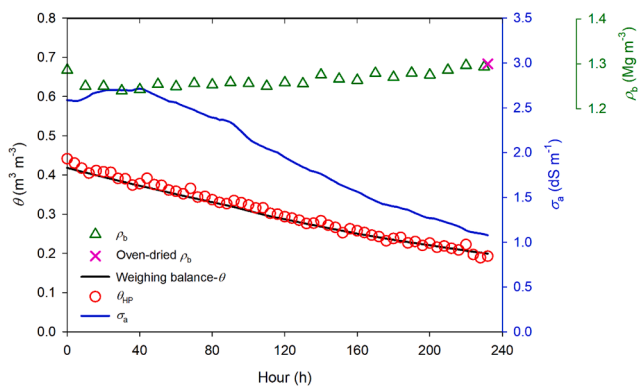
saline soil might be another source of the  $\theta_{TDR}$  errors. When  $\sigma_a$  values were less than  $1 \text{ dS m}^{-1}$ , the  $RMSEs$  of thermo-TDR estimated  $\rho_b$  and  $\theta_{TDR}$  values were  $0.12 \text{ Mg m}^{-3}$  and  $0.03 \text{ m}^3 \text{ m}^{-3}$ , respectively.

In contrast, the HP-based approach provided relatively accurate  $\rho_b$  and  $\theta_{HP}$  values on these salt-affected soils (Fig. 3). The  $\rho_b$  and  $\theta$  estimates generally agreed well with the directly measured mass determined values, as indicated by the even distribution of the data points around the 1:1 line. Error analysis showed that for the sand and loam soils, the  $\rho_b$  estimates had an average  $RMSE$  of  $0.12 \text{ Mg m}^{-3}$  and an average bias of  $-0.054 \text{ Mg m}^{-3}$  (Fig. 3a), and the  $\theta_{HP}$  estimates had a  $RMSE$  value of  $0.02 \text{ m}^3 \text{ m}^{-3}$  and a bias of  $0.008 \text{ m}^3 \text{ m}^{-3}$  (Fig. 3b). Some scattered outliers for HP determined  $\theta$  values in Fig. 3b were observed, possibly due to the fact that HP determined  $\theta$  values were prone to probe deflection errors, because they were directly derived from  $C$  values (Liu et al., 2020; Zhang et al., 2020). This type of error was insignificant for the in situ continuous measurements for Soil 3 (Fig. 4). Besides, it was found that there was a decrease in  $c_w$  with the addition of salt, and the specific heat capacity values of brine solutions decreased with increasing concentration and temperature (Sharqawy et al., 2010; Ramalingam and Arumugam, 2012). We determined that a  $0.10 \text{ kJ kg}^{-1} \text{ K}^{-1}$  change in  $c_w$  caused a  $\rho_b$  error up to  $0.34 \text{ Mg m}^{-3}$  and a  $\theta_{HP}$  error up to  $0.01 \text{ m}^3 \text{ m}^{-3}$ . Thus, it is necessary to further investigate the appropriate  $c_w$  values used in Eqs. (3) and (5) for more accurate estimations of  $\rho_b$  and  $\theta_{HP}$  values in salty soils.

The performance of the thermo-TDR based method to estimate  $\theta$  and  $\rho_b$  values with  $\sigma_a$  less than  $1 \text{ dS m}^{-1}$  were similar to those for the HP-based method, however, the HP-based approach outperformed the thermo-TDR based approach for determining  $\theta$  and  $\rho_b$  in salt-affected soils with  $\sigma_a$  ranging from  $1.0$  to  $7.59 \text{ dS m}^{-1}$ . The electromagnetic signal attenuated with increasing  $\theta$  and  $\sigma_a$ , the large errors in thermo-TDR measured  $\theta$  might be due to the undetectable  $L_2$  values caused by



**Fig. 3.** Heat-pulse based (circles) and thermo-TDR based (triangles) estimates of (a) soil bulk density ( $\rho_b$ ) and (b) water content ( $\theta$ ) versus directly measured  $\rho_b$  and  $\theta$  values on the sand and loam soils. Soil bulk electrical conductivity ranged from 0.09 to 2.88  $\text{dS m}^{-1}$  for the sand soil, and from 0.07 to 7.59  $\text{dS m}^{-1}$  for the loam soil. The solid lines are the 1:1 lines, and the dashed lines are  $\pm 10\%$  error lines.



**Fig. 4.** Dynamics of soil water content ( $\theta$ ), bulk electrical conductivity ( $\sigma_a$ ), and bulk density ( $\rho_b$ ) values for Soil 3 during a drying process. The black line represents  $\theta$  determined from mass balance measurements, while the red circles and green triangles are the heat-pulse based  $\theta_{HP}$  and  $\rho_b$  estimates, respectively. The pink X represents the oven-dried  $\rho_b$  value. The blue line represents thermo-TDR measured  $\sigma_a$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

the presence of salt, causing further large  $\rho_b$  errors. Thus, it was possible to obtain more accurate  $\rho_b$  and  $\theta$  results from the HP-based approach than from the thermo-TDR approach, because salt effects on the  $C$  and  $\lambda$  measurements were negligible for the studied  $\sigma_a$  range (Fig. 2).

The HP-based  $\theta_{HP}$  and  $\rho_b$  estimates were also examined on Soil 3 (Fig. 4). The average  $\theta_{HP}$ ,  $\sigma_a$  and soil thermal property values from the two thermo-TDR sensors were used to reduce the measurement errors caused by any nonuniform water and salt distributions in soil during the evaporation process. Due to uncertainty in waveform  $L_2$  values (Fig. 1c),  $\theta_{TDR}$  was overestimated with a  $\text{RMSE}$  of  $0.09 \text{ m}^3 \text{ m}^{-3}$  (data not shown). Thus, only the HP-based results ( $\theta_{HP}$  and  $\rho_b$ ) were presented. During the evaporation process,  $\theta$  decreased gradually from saturation to about  $0.20 \text{ m}^3 \text{ m}^{-3}$ , and  $\sigma_a$  was reduced from 2.71 to  $1.08 \text{ dS m}^{-1}$  (Fig. 4). The  $\theta_{HP}$  values followed closely to the  $\theta$  trend from the mass balance measurements, with a  $\text{RMSE}$  of  $0.01 \text{ m}^3 \text{ m}^{-3}$  and a bias of  $0.001 \text{ m}^3 \text{ m}^{-3}$ . Meanwhile,  $\sigma_a$  decreased nonlinearly as  $\theta$  decreased. The relatively constant  $\rho_b$  values indicated that there were no apparent soil structure changes during the drying process, and the estimated values matched well with the directly measured value (which was determined by oven drying soil at the end of the experiment). Hence, the HP measurements obtained with the thermo-TDR sensor provided reliable  $\theta$  and  $\rho_b$  values on the salt-affected column of Soil 3. Generally, if you make measurements with a thermo-TDR sensor, both the thermo-TDR and HP-based methods can be used to estimate  $\theta$  and  $\rho_b$  in salt-affected soils, but if  $\sigma_a$  is larger than  $1.0 \text{ dS m}^{-1}$ , we recommend using the HP-based method to estimate  $\theta$  and  $\rho_b$ .

## 5. Conclusion

We evaluated the effects of salt concentration on thermo-TDR and HP-based methods to determine  $\theta$ ,  $\rho_b$ ,  $\sigma_a$  and thermal property values in salt-affected soils. The presence of salts reduced the final voltage values after multiple reflections of electromagnetic waves, which decreased with increasing  $\sigma_a$ . When the  $\sigma_a$  value was greater than  $1.0 \text{ dS m}^{-1}$ , the distortion of TDR waveforms caused errors in  $L_2$  estimations, which transferred to uncertainties in  $\theta_{TDR}$ . It became difficult to determine  $\theta_{TDR}$  values at relatively large  $\sigma_a$  values ( $>2.71 \text{ dS m}^{-1}$ ) because  $L_2$  on the waveform was undetectable. Within the studied  $\sigma_a$  range ( $<7.59 \text{ dS m}^{-1}$ ), the effects of salt on soil thermal property values ( $C$  and  $\lambda$ ) were negligible. The derived soil thermal property values could be used with the HP-based method to accurately estimate  $\theta$  and  $\rho_b$  values, with  $\text{RMSEs}$  of  $0.02 \text{ m}^3 \text{ m}^{-3}$  and  $0.12 \text{ Mg m}^{-3}$ , respectively. Generally, the thermo-TDR method could be used to determine reliable  $\theta$  and  $\rho_b$  values when  $\sigma_a$  was less than  $1.0 \text{ dS m}^{-1}$ . For soils with  $\sigma_a$  ranging from  $1.0$  to  $7.59 \text{ dS m}^{-1}$ , the HP method outperformed the thermo-TDR method at determining accurate  $\theta$  and  $\rho_b$  values. This has important implications for studies of coupled processes of water, heat and solute in soils. Future studies should focus on the performance of the HP method to determine  $\theta$  and  $\rho_b$  values under complex field conditions.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.geoderma.2021.115564>.

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