

# Low-threshold ultrahigh-energy neutrino search with the Askaryan Radio Array

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(Received 14 February 2022; accepted 24 May 2022; published 27 June 2022)

In the pursuit of the measurement of the still-elusive ultrahigh-energy (UHE) neutrino flux at energies of order EeV, detectors using the in-ice Askaryan radio technique have increasingly targeted lower trigger thresholds. This has led to improved trigger-level sensitivity to UHE neutrinos. Working with data collected by the Askaryan Radio Array (ARA), we search for neutrino candidates at the lowest threshold achieved to date, leading to improved analysis-level sensitivities. A neutrino search on a data set with 208.7 days of livetime from the reduced-threshold fifth ARA station is performed, achieving a 68% analysis efficiency

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over all energies on a simulated mixed-composition neutrino flux with an expected background of  $0.10^{+0.06}_{-0.04}$  events passing the analysis. We observe one event passing our analysis and proceed to set a neutrino flux limit using a Feldman-Cousins construction. We show that the improved trigger-level sensitivity can be carried through an analysis, motivating the phased array triggering technique for use in future radio-detection experiments. We also include a projection using all available data from this detector. Finally, we find that future analyses will benefit from studies of events near the surface to fully understand the background expected for a large-scale detector.

DOI: [10.1103/PhysRevD.105.122006](https://doi.org/10.1103/PhysRevD.105.122006)

## I. INTRODUCTION

Neutrinos are a powerful tool for understanding the Universe at the highest energies. While other messenger particles such as cosmic rays and gamma rays are either deflected or absorbed on the way to Earth after being created by their astrophysical sources, neutrinos point back to their sources and rarely interact, making them unique messengers for understanding distant or dense astrophysical sources. Additionally, we expect cosmogenic neutrinos, created via interactions between cosmic rays and the cosmic microwave background [1]; measuring the cosmogenic neutrino flux will help answer fundamental questions about cosmic ray composition at the highest energies. The IceCube experiment has measured an astrophysical neutrino flux up to 10 PeV [2,3] and has early hints of a potential first source [4,5]. However, because the neutrino flux falls as energy increases, experiments searching for neutrinos above 10 PeV have needed to build larger detectors that observe many cubic kilometers of ice to increase the chances of a detection.

One such experiment, the Askaryan Radio Array (ARA), takes advantage of the Askaryan effect, first proposed in 1962 by G. Askaryan [6] and which influences the design of many neutrino experiments at high energies [7–9]. When a neutrino interacts in matter, a particle shower occurs, which develops a negative charge excess of  $\mathcal{O}(20\%)$  due to scattering with the electrons in the medium, and positrons in the shower annihilating with electrons in the matter. This negative charge excess causes two types of radiation to occur: bremsstrahlunglike radiation, caused by the transient nature of the net charge, and Cerenkov-like radiation, caused by the net charge moving faster than the speed of light in the interaction media. For wavelengths greater than the apparent lateral width of the shower (determined by the Molière radius of the material and the viewing angle), the radiation is coherent [10].

Ice is one medium in which Askaryan radiation can be observed, due to its transparency to radio-frequency radiation [11]; it has also been observed in the lab in sand, rock salt, and polyethylene, as well as in the atmosphere [12–15]. In ice, the Molière radius is  $\approx 10$  cm, which leads to coherent radiation and consequently an increase in power at radio wavelengths. As an additional benefit, Antarctic ice has a radio attenuation length of  $\mathcal{O}(1$  km) [16], which

allows detectors to survey many cubic kilometers of ice with sparse instrumentation.

In this paper, we report on the ARA Station 5 (A5) instrument, including the new Phased Array detector (also called NuPhase [17]), and we present the first neutrino search of data triggered by the Phased Array. Demonstrating that low-threshold events can pass selection in a neutrino search is the crucial next step in demonstrating the improvement in effective volumes brought about by the phased array, and in motivating the design of future Phased Array triggers on other experiments [9,18–20].

## II. EXPERIMENTAL APPARATUS AND DATASET

### A. The ARA detector

The ARA instrument (Fig. 1) consists of five independent stations, arranged in a triangular grid with neighboring stations separated by two kilometers and all deployed near South Pole Station in Antarctica. Each station consists of sixteen antennas installed in holes drilled in the ice to a maximum depth of 200 m. Both vertically polarized (VPol) and horizontally polarized (HPol) antennas are used so that polarization of the incoming signal can be measured. ARA is sensitive to electromagnetic radiation of the frequency range 150–850 MHz [21].

The newest station, A5, was built in 2018 and has two separate but connected detectors, as seen in Fig. 1: one, the typical ARA station design described above, hereafter referred to as the baseline instrument; and two, an additional central antenna string with its own triggering instrument called the Phased Array [17]. Unlike the baseline design, which has antennas deployed in pairs of VPol and HPol antennas separated by a vertical distance between 20–30 m, the Phased Array instrument consists of seven VPol antennas and two HPol antennas, deployed with compact 1–2 m separation [22]. While the Phased Array and the baseline system are connected, they are mostly separate instruments, each with their own data acquisition (DAQ) system.

The baseline A5 trigger requires three antennas of the same polarization to record their integrated power over a 25 ns time window as greater than five times the ambient thermal noise level, within a coincidence of approximately 170 ns. The baseline A5 instrument records this type of

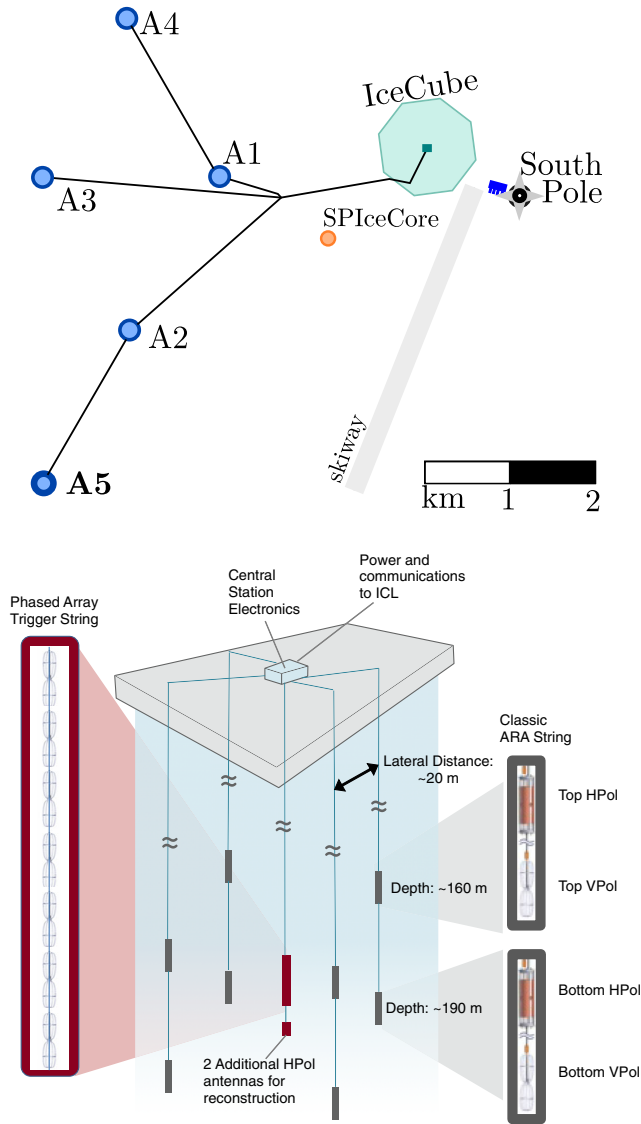


FIG. 1. Top: bird's eye view of the ARA instrument relative to South Pole Station. Black lines indicate cable connections for power and network. This work focuses on ARA Station 5 (A5), the only station with an additional phased array trigger. Bottom: a schematic of the A5 detector. Gray antennas are the baseline ARA antennas while the red antennas are the Phased Array antennas.

trigger at a rate of  $\sim 6$  Hz, with an additional software trigger at a rate of 1 Hz. More details on the ARA electronics can be found in [23].

The Phased Array instrument, described in detail in [17], is designed with a beamforming trigger, a technique used often by radio telescope experiments [24]. Incoming radio waves arrive at the antennas of the one-dimensional Phased Array in a specific order depending on the incoming zenith angle of the signal; thus, for distant, plane-wavelike signals, the time difference between the pulses on each channel are directly related to the arrival angle of the incoming signal. By defining 15 pre-determined directions (often called

“beams”) based on the expected time delays seen at the antennas, signals are delayed appropriately and then summed together prior to the trigger. The power in each beam is monitored in 10 ns interleaved time intervals, with the trigger threshold continuously adjusted to meet a 0.75 Hz rate for each of the 15 beams for a global trigger rate of 11 Hz. Impulsive signals add coherently for the beam that they are associated with, while noise on average do not, lowering the trigger threshold compared to a baseline ARA station. The 50% trigger efficiency point for the Phased Array instrument occurs at a single-antenna voltage-based signal-to-noise ratio (SNR) of 2.0, compared to an SNR of 3.7 for the baseline ARA trigger; the full definition of SNR can be found in [17].

If the Phased Array triggers on an event, it externally triggers the baseline ARA system at A5. The baseline system may or may not have independently triggered on the event due to the baseline system having a higher trigger threshold. In normal operations, up to 98% of Phased Array triggered events have a matching baseline event. If the baseline system triggers on an event, it does not externally trigger the Phased Array instrument.

This analysis only considers events triggered by the Phased Array instrument. As of the 2018–2019 deployment season, the output of one of the baseline ARA channels was split and connected to both the baseline ARA DAQ and the Phased Array DAQ. Because of this common channel, the timing of events that occur in both instruments can be synchronized and all available channels at A5 can be used to reconstruct the events. However, because not all Phased Array events have matching events in the baseline ARA system, the baseline instrument is primarily used for calibration and reconstruction of candidate events, not as a principal analysis tool.

## B. Livetime

A5 was installed in the 2017–2018 deployment season and has been operational since that time. For this report, we only analyze data taken throughout the 2019 calendar year, to take advantage of the common channel described above.

Within this dataset, approximately 3.5 months are not usable due to the Phased Array instrument overheating when operated in the warmest months. This overheating can be solved in future versions of a Phased Array system by adding additional heat-sinking measures or designing a system that consumes less power [9]. Additionally, starting in October 2019 the baseline ARA system suffered a USB failure on its triggering and readout interface board, causing a loss in livetime of approximately 2 months. This leaves 208.7 days of total livetime in which both the Phased Array and the baseline system were taking data at the same time during 2019. The deadtime of the Phased Array system is estimated to be 0.12% and has a negligible impact on the livetime.

We blind the data using the data prescaling method discussed by Klein and Roodman [25], unblinding 10% of the full data set to select passing event criteria and extrapolate background estimates. The events comprising this 10% data set are selected from all events by ordering events by their trigger time, breaking the data into groups of 10 events, and selecting one event at random from each group. We also unblind all data taken during one full 24-hour period to monitor any short-term cyclical behavior. The 10% training sample is not included in the final result.

While the analysis focuses on events triggered by the Phased Array, the baseline A5 instrument is used in three ways. First, the baseline instrument was used to calibrate the location of the Phased Array relative to the other landmarks at the South Pole [26]. Second, the common channel that was connected to both the Phased Array and the baseline instrument was used in the analysis. Third, the baseline instrument was used to point surface events both in the 10% training sample and in the unblinded sample.

### C. Simulation

A modified version of the AraSim simulation package is used to simulate the entire A5 instrument, including both the baseline ARA channels and the Phased Array trigger string [27]. The trigger is implemented in the simulation following the methodology laid out in [17]. First, the SNR and the incoming angle at the antenna array are calculated for each event. Second, each event is assigned a probability of passing the trigger based on two *in-situ* measurements: the trigger efficiency as a function of SNR, and the efficiency as a function of how “on-beam” or “off-beam” the incoming direction is with respect to the 15 beam directions of the trigger system discussed in Sec. II A. For each event, a random number is generated between 0 and 1, and the event passes if its assigned probability is greater than the random number. The resulting simulated trigger matches the *in-situ* measurements of trigger efficiency observed in the Phased Array instrument. A comparison is shown in Fig. 2 between the effective volume for this analysis, calculated using the same Monte Carlo counting methods described in [23], and the effective volume calculated in the Phased Array instrument paper [17].

Event selection in data analysis is optimized using simulated data sets, in which realistic simulation of the neutrino flux traversing the detector is crucial. We chose to simulate neutrinos using a flux based on a mixed composition of galactic cosmic rays and an optimistic model of source evolution [28]. This simulation set includes neutrinos at all energies and is used to calculate analysis efficiency at each analysis stage. Separate data sets are simulated for different neutrino energies in half-decade energy bins from  $10^{16}$  eV to  $10^{21}$  eV to determine the analysis efficiency as a function of energy.

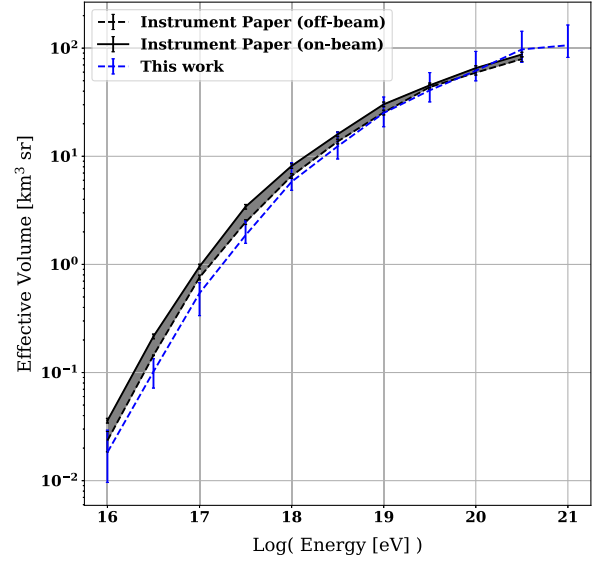


FIG. 2. A comparison of the effective volume of the simulated Phased Array trigger, compared to the previously published effective volume [17]. The uncertainties for the blue curve include systematic uncertainties, which are described in Sec. VIB.

### III. ICE MODELING AND $R$ - $z$ PLANE MAPPING

The index of refraction of the ice changes as a function of depth due to the compacting of ice layers over time [29], leading to radio waves traveling in nonstraight paths through the ice. This effect is largest in the upper few hundred meters of ice, the region called the firm. We estimate a model for the changing index of refraction by combining calibration data taken from both the local pulser, approximately 50 m away from the Phased Array and  $-170$  m deep, and a pulser dropped in the SPiceCore borehole, approximately four kilometers away and between 900–1450 m in depth. The best fitting index of refraction model for the firm is found to be

$$n(z) = 1.780 - 0.454 \exp \left[ -0.0202 \times \frac{z}{1 \text{ m}} \right] \quad (1)$$

where  $z$  is the depth in meters. This is determined by starting with an existing internal ice model and modifying only the parameter in the exponent, using least squares regression to compare the predicted time delays from the model to the measured time delays between channels of the Phased Array. The ice model is specifically tuned to match only direct pulses from the SPiceCore calibration pulser, and did not fit for refracted pulses. This means the ice model likely describes deep ice most accurately. Using this model, the possible paths for a radio signal can be calculated for any source following Fermat’s principle. For in-ice sources, this includes direct paths between the



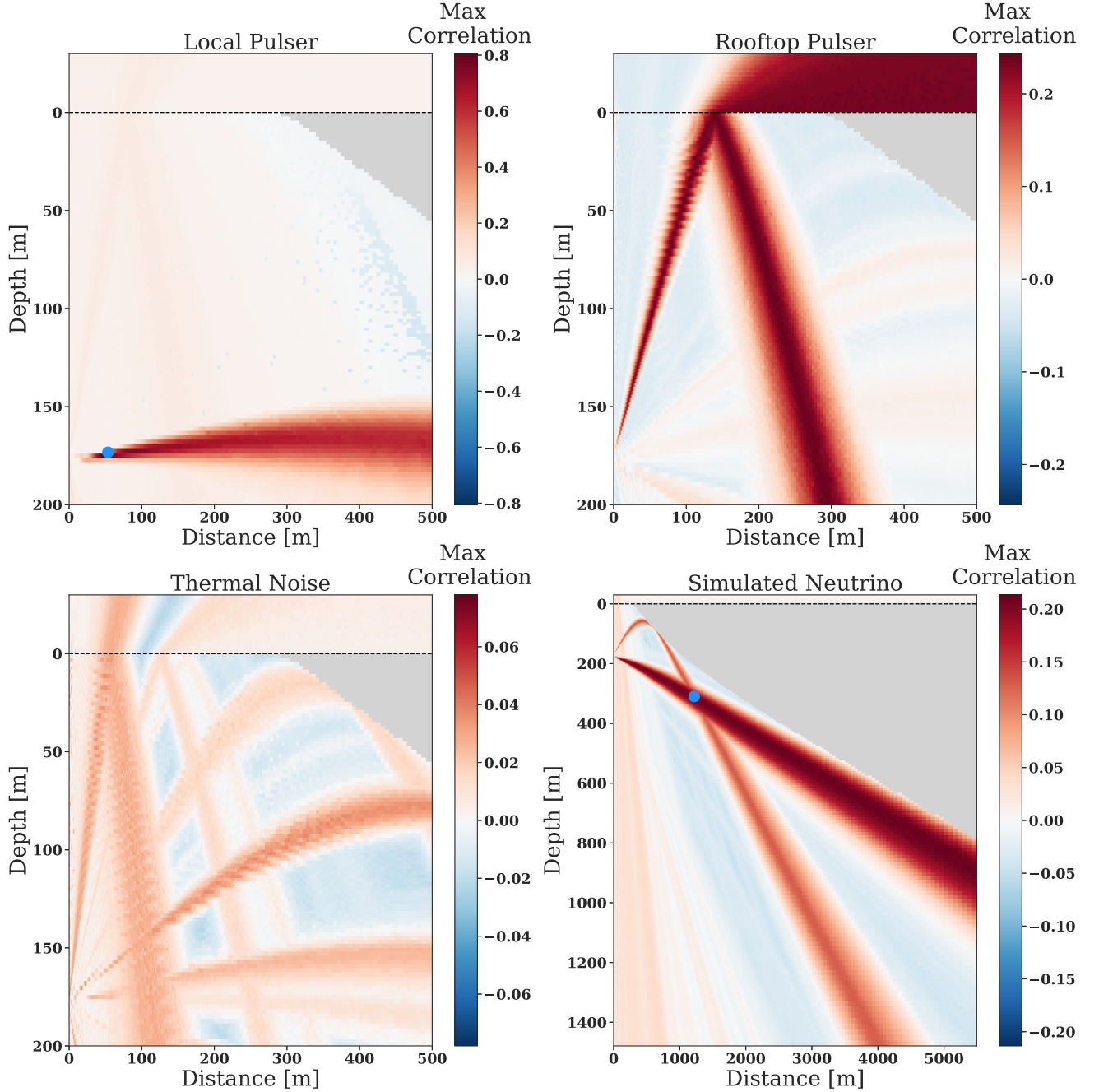


FIG. 3. Four example correlation maps created using only the antennas from the Phased Array instrument, centered at a depth of 170 m. The blue dots indicate the true location of the source, where applicable; the rooftop pulser location is out of frame, about 4 km away. The gray area is disallowed based on ray optics using the exponential firm model. The color map indicates the maximum value of  $C(R, z)$  between the direct and refracted solutions, and is scaled differently for each map to match the maximum correlation value for that event. The Phased Array alone has  $\pm 0.3^\circ$  pointing resolution in zenith; with the full ARA5 instrument, we improve by an order of magnitude.

interaction and the detector, and refracted paths, in which the signal path curves above the detector before curving back down, made possible by the changing index of refraction. By comparing the different path lengths for each antenna, expected time delays  $\tau(R, z)$  between pulses on different channels can also be calculated for any given

source as a function of the radial distance  $R$  and the depth  $z$  of that source. These expected time delays are characteristics of the environment, defined by the locations of the antennas relative to each other and the ice model.

For a given event, each antenna records a measure of voltage as a function of time, called a waveform. The cross

correlation between the waveform of the  $i$ th antenna and the waveform of the  $j$ th antenna is calculated as a function of time delay  $\tau$  using the correlation function

$$\text{Corr}_{i,j}(\tau) = \sum_{t=0}^{N-1} \frac{V_i(t)V_j(t+\tau)}{\sigma_i\sigma_j}, \quad (2)$$

where  $V_i(t)$  and  $V_j(t+\tau)$  are the waveforms and  $\sigma_i$  and  $\sigma_j$  are the variances of the waveforms of the  $i$ th and  $j$ th channels, respectively. The location of the maximum of  $\text{Corr}_{i,j}(\tau)$  corresponds to the time delay that best aligns the signals. A map can be created describing the average correlation at every  $(R, z)$ , described by

$$C(R, z) = \frac{\sum_{i=1}^{n_{\text{ant}}-1} \sum_{j=i+1}^{n_{\text{ant}}} \text{Corr}_{i,j}[\tau(R, z)]}{\binom{n_{\text{ant}}}{2}}, \quad (3)$$

where, for the Phased Array,  $n_{\text{ant}} = 7$  is the number of antennas and  $\binom{n_{\text{ant}}}{2}$  is the binomial coefficient. For each event, three correlation maps are created, corresponding to the  $\tau(R, z)$  that describe the direct path,  $\tau(R, z)$  for the refracted path, and the average between the two. For the plots in Fig. 3, the maximum between the direct and refracted maps is plotted.

While typically a correlation map describes potential source locations in three dimensions, the Phased Array instrument records no azimuthal information due to the cylindrical symmetry around its  $z$ -axis. Instead,  $R$ - $z$  correlation maps are generated, from which many pairs of  $(R, z)$  can be identified as potential source locations. Due to the tight packing and small baselines of the phased array

antennas, these maps generally do not have significant discerning power for the exact location of either  $R$  or  $z$  except for extremely bright and/or nearby signals such as the local calibration pulser. One exception to this is events which contain both direct and refracted pulses; an example of the correlation map for a simulated event with two pulses is shown in Fig. 3. The additional A5 baseline channels are used to reconstruct the azimuthal direction for candidate events but are not used in the primary analysis. Similarly, the HPol antennas on the Phased Array string are used only for candidate events, as they are most useful for reconstructing the incoming neutrino direction.

For each map, at the location where the correlation value is largest, the corresponding time delays can be used to add the signals together with appropriate time delays to generate a single waveform, called the coherently summed waveform (CSW). From the CSW, analysis variables such as SNR, peak power, and impulsivity are computed which are used in the analysis to distinguish neutrinelike signals from noise. An example CSW from simulation is shown in Fig. 4. One such analysis variable, the impulsivity  $I$ , is calculated using the same method as [30], where the CDF of the power of the waveform is generated starting from the location of the peak power and integrated to either end of the waveform. For a noise event, this CDF should be nearly linear, as the power is distributed evenly throughout the CSW; for an impulsive event, the CDF should be steeply rising at the beginning and nearly flat toward the end. The impulsivity  $I$  is defined as  $2A - 1$ , where  $A$  is the average of the CDF. Example CSWs and CDFs are shown later in Fig. 8.

Because the CDF is generally linear in the case of a noise event, other metrics can also be calculated from the CDF. A

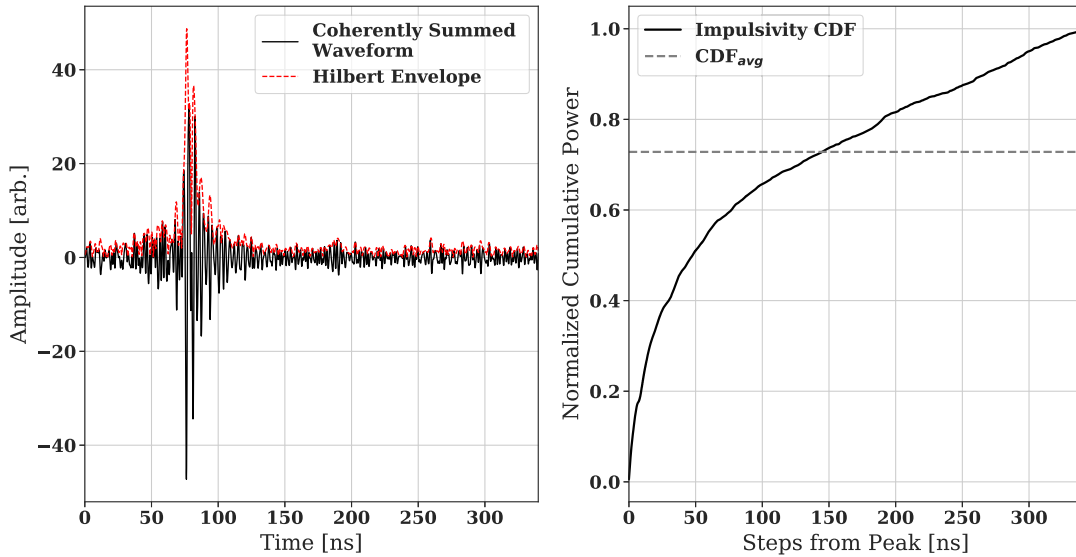


FIG. 4. Left: an example CSW for a simulated neutrino event, along with its Hilbert envelope. Some analysis variables are calculated directly from this plot, including PowerSpot (the location of the peak power, approx. 76 ns) and Hilbert peak (the maximum value of the Hilbert envelope). Right: the impulsivity CDF for the simulated CSW. A noise event would have an approximately linear CDF due to power being evenly spread throughout the waveform. Impulsivity is defined as  $I = 2 * \text{CDF}_{\text{avg}} - 1$ .

least-squares fitting method is used to calculate a linear fit for the CDF, and the slope, intercept, and the correlation coefficient are used as analysis variables. Additionally, a K-S test statistic is calculated as the largest distance between the linear fit and the CDF. We describe calculations of these variables and others in a later section.

#### IV. EVENT SELECTION

##### A. Defining a deep region

In addition to thermal noise fluctuations, which make up the vast majority of background, there are backgrounds that share characteristics with the expected neutrino signal. The most challenging backgrounds to remove are anthropogenic backgrounds and cosmic ray interactions, which can both look impulsive, isolated in time, and have strong peaks in their correlation maps.

The biggest difference between these backgrounds and neutrino candidates is the incoming direction: anthropogenic backgrounds and cosmic ray interactions both occur at or near the surface, while the neutrinos we expect to see mostly interact in deep ice. We define a phase space in which cosmic and anthropogenic backgrounds associated with surface locations are well separated from the neutrino-induced events, referred to as the signal region or the deep region. Two variables were used to define this deep region: zenith angle reconstructed at the antenna array, and the surface correlation ratio, the ratio of the maximum correlation value within 10 m of the surface to the global maximum correlation value, each retrieved from the values in the  $R$ - $z$  correlation map. Events with a high surface correlation ratio value are more likely to be caused by emission near the surface, which in turn makes them potential anthropogenic or cosmic ray backgrounds. By

plotting the 10% training sample using these coordinates, the highly correlating events that are likely a combination of anthropogenic and cosmic ray backgrounds cluster at high surface correlation ratio and low zenith angle, as shown in Fig. 5.

The boundary of the deep region in reconstructed zenith angle is chosen to be 57 degrees, calculated using Snell's law to find the arrival zenith angle for a signal that experienced a total internal reflection at 20 m below the surface. This boundary is chosen to exclude cosmic rays, which are expected to emit radio waves at a depth of less than 10 m [31]. The boundary in the surface correlation ratio is chosen to be 0.5, so that only events correlating twice as well below 10 m were kept in the signal region. All other events were sorted into the surface region, which is not part of the signal region. The requirement for events to be located in the signal region removed 21% of simulated neutrinos, most of which were neutrinos that interacted deep in the ice, yet their signals traveled on a refracted path up near the surface before curving back down to the detector. It is possible that a future analysis could recover some of these simulated events by fully utilizing the baseline ARA antennas.

##### B. Nonthermal background removal and data cleaning

While the vast majority of events recorded by the Phased Array are expected to be thermal fluctuations produced by the ice, there are additional backgrounds that must be removed from the sample before characterizing the thermal noise distribution. Those backgrounds are

###### 1. Calibration pulser events

During a typical Phased Array data run, the local calibration pulser transmits a VPol pulse at a rate of

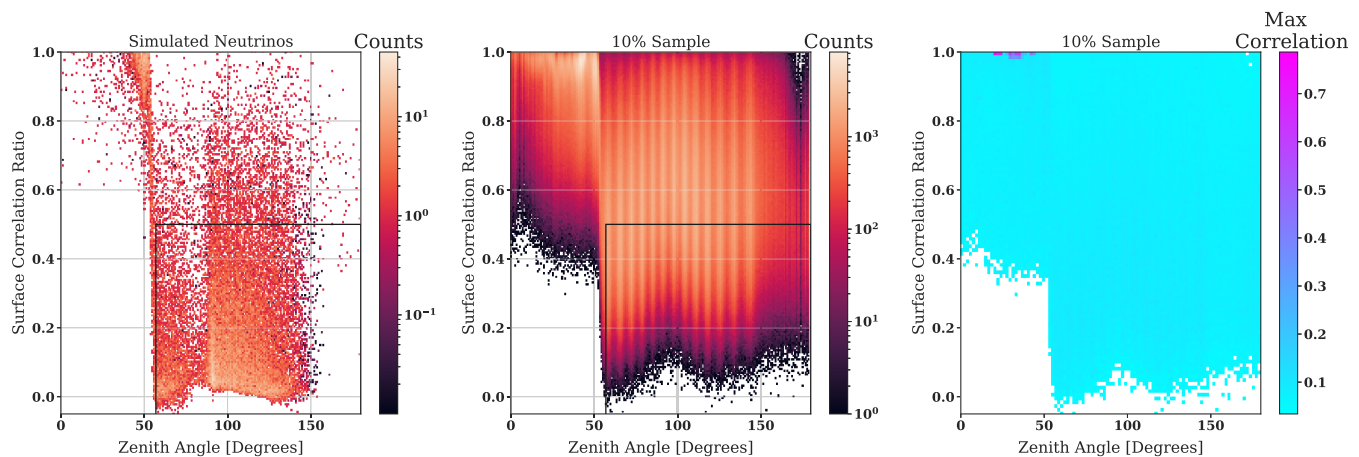


FIG. 5. The distribution of the reconstructed zenith angle at the Phased Array vs the surface correlation ratio for the simulated neutrino sample (left) and the 10% training sample (middle). The black box designates the signal region. The population in the upper left hand corner of simulated neutrinos corresponds to deep neutrinos whose paths curves near the surface. The vertical band structure in the 10% training sample correspond to the discrete trigger beam directions. Right: the full 10% training sample with the color axis referring to the maximum value of the maximum correlation for that bin. The events with high correlation are clustered in the top left hand corner. These are likely a combination of anthropogenic and cosmic ray backgrounds.

1 Hz on the second as determined by GPS. These events are removed from the sample based on their trigger time, which only removes 0.016% of simulated neutrinos. While all calibration pulses in the 10% training sample are successfully removed based on their trigger time alone, analyses of other stations showed that 1 out of 10,000 calibration pulses did not occur within the expected time window. As a precaution, events reconstructing within a box defined as between 45–55 m radially from the antenna array and between 171–175.5 m deep are also removed from the analysis. The 90% upper limit of expected calibration pulser events occurring outside of the defined box for the full livetime is calculated to be 21 events; with the geometry-based metric, 99.8% of calibration pulser events were expected to be removed, resulting in a 90% upper limit on the background estimate of 0.009 and a simulation efficiency of 99.64%. After unblinding, we find that all calibration pulser events are removed by the timing requirement, suggesting that future analyses for this station may not need the added geometry requirement.

## 2. Software triggered events

The Phased Array generates internal software triggers by randomly sampling the noise environment at a rate of 1 Hz, to check that the system is operating normally. These events are used to measure the average root-mean-square of the noise for each channel over all events in each run, which is used in calculations of analysis variables such as the SNR. The software triggered events are tagged by the data acquisition software and removed from the analysis.

## 3. Continuous wave (CW) backgrounds

CW contamination in our data is caused by anthropogenic sources visible to A5 and is identifiable in triggered events as a peak in the measured spectra. The most prevalent CW source is from radio communications among station personnel, which is transmitted at a frequency of 450 MHz, near the center of the Phased Array’s frequency band. To remove this, our instrument is equipped with a notch filter at the hardware level. There are two additional sources of CW that are more sporadic and must be removed in analysis. The first source is weather balloons, which are launched twice per day and communicate back to South Pole Station at a frequency of 405 MHz. The second source is satellites with downlink frequencies around 137 MHz; although this is technically outside of the Phased Array’s band, it does cause the trigger rates, and therefore thresholds, of the trigger beams to cycle up and down as satellites come into and out of view. Both of these frequencies are targeted with a sine subtraction filter developed by ANITA [30], where a frequency was filtered if removing the frequency decreased the power by at least 4%, a threshold chosen for this analysis based on CW-contaminated events within the 24-hour unblinded sample. While no other CW sources were visible in the 10% training sample, an

additional sine subtraction filter was applied to all events over the entire frequency range with a power threshold of 10%, in case other transient CW sources, such as satellites at other frequencies, appeared in the full data sample.

## 4. Additional livetime cuts

Several time periods were eliminated due to station configuration changes or known station activity, totaling 57 hours. Of this, 18 hours were removed due to multiple surface events occurring within a single run, common during known station activity, including remote configuration changes. Additionally, 39 hours of data were removed due to the calibration pulser rate dropping; this is most common when the calibration pulser is switched from one mode to another, e.g., VPol pulsing to HPol, or GPS-tied pulses to continuous noise. During these mode switches, spurious signals are possible, which would be challenging to remove in analysis. In total, this removed 2.3 days of livetime, leaving 206.4 days of data that can be used in analysis.

## C. Fisher discriminant

After applying the quality cuts, the distributions of the analysis variables of the remaining 10% unblinded sample shares the characteristics expected of thermal-noise-triggered events. To distinguish between this thermal-noiselike sample and expected neutrino signals, a Fisher discriminant [32] was trained on the remaining 10% training sample and simulated neutrinos. The input variables for the Fisher discriminant are listed in Table I, and the resulting distributions of data and simulation are seen in Fig. 6. The peaks in the simulation distribution are likely caused by slight asymmetries in variable distributions caused by some of the key variables in the Fisher discriminant, including A5 *Correlation* and *Impulsivity*.

The Fisher discriminant cut was chosen by optimizing for the best sensitivity, defined as the mean 90% upper limit using the Feldman-Cousins method [33] divided by the analysis efficiency. This optimization was carried out including uncertainties using the following method. First, the tail of the 10% training sample was fit to an exponential function  $f(x)$ , with uncertainties on each fit parameter calculated using the covariance matrix. The resulting fit can be seen in Fig. 6. Next, a background distribution for each potential cut value was populated by running 100,000 Monte-Carlo psuedoexperiments, with fit parameters varied by sampling from Gaussian distributions defined by the fit parameters and their uncertainties. For each set of sampled parameters, the background  $b$  was calculated as

$$b = \frac{t_{\text{up}}}{w} \int_{\text{cut}}^{\infty} f(x) dx + b_0 \quad (4)$$

where  $t_{\text{up}} = 9$  is the scale-up factor to account for the additional livetime in the full burn sample,  $w$  is the width of



TABLE I. Table of analysis variables used in the Fisher discriminant, along with their definitions and expected ranges where applicable. The top five variables with the highest weights are, from greatest to smallest:  $R^2$ , Hilbert peak, impulsivity, maximum correlation, and SNR. For more complete descriptions, please see the Appendix.

Variable name	Variable description	Variable range
Maximum correlation	Maximum value on the $R-z$ correlation map	$[-1.0, 1.0]$
Best R	Location of the maximum correlation (lateral distance, m)	$[10 \text{ m}, 5500 \text{ m}]$
Best Z	Location of the maximum correlation (depth, m)	$[-1500 \text{ m}, 0 \text{ m}]$
Hilbert peak	Magnitude of the peak of the coherently summed waveform (CSW)	$[0, 63]$
Surface correlation ratio	Maximum correlation within 10 m of the surface	$[-1.0, 1.0]$
Surface Z	Location of surface cor (depth, m)	$[-10 \text{ m}, 0 \text{ m}]$
Surface R	Location of surface cor (lateral distance, m)	$[10 \text{ m}, 5500 \text{ m}]$
Close surface	Maximum value of correlation map above the surface	$[-1.0, 1.0]$
Zenith angle	Best reconstructed zenith angle, calculated at the antenna array	$[0, 180.0]$
Windowed zenith	Best reconstructed zenith angle, windowed around the trigger	$[0, 180.0]$
Coherent SNR	SNR of the CSW	Not constrained
Avg SNR	Average of the SNR of each individual VPol waveform	Not constrained
Impulsivity	Average of the cumulative distribution function (CDF) around the peak of the CSW	$[0, 1.0]$
$R^2$	Correlation coefficient for the linear fit to impulsivity CDF	$[0, 1.0]$
Slope	Slope of linear fit to impulsivity CDF	Not constrained
Intercept	Intercept of linear fit to impulsivity CDF	Not constrained
Power spot	Location of peak power along the CSW	$[0, 340 \text{ ns}]$
A5 correlation	Maximum correlation between phased array CSW and A5 channel	$[-1.0, 1.0]$
K-S	The Kolmogorov-Smirnov (K-S) test, comparing the impulsivity CDF to a linear hypothesis	Not constrained

the binning used, and  $b_0$  is the background from earlier cuts, namely the geometric calibration pulser cut. The median value of this background distribution was used to calculate the mean Feldman-Cousins upper limit of 500 psuedoexperiments assuming Poisson statistics. In this way, the expected sensitivity, as well as the expected background distribution, can be determined for all possible

cuts on the Fisher discriminant. The background that optimizes the expected sensitivity for the 90% sample is  $0.09^{+0.06}_{-0.04}$  with a cut value of 1.0698 and an efficiency of 68.16%; because the distribution of the mean number of background events is asymmetric, the median, 16th percentile, and 84th percentile are reported. In the 10% training sample, 0 events passed all cuts in the deep region.

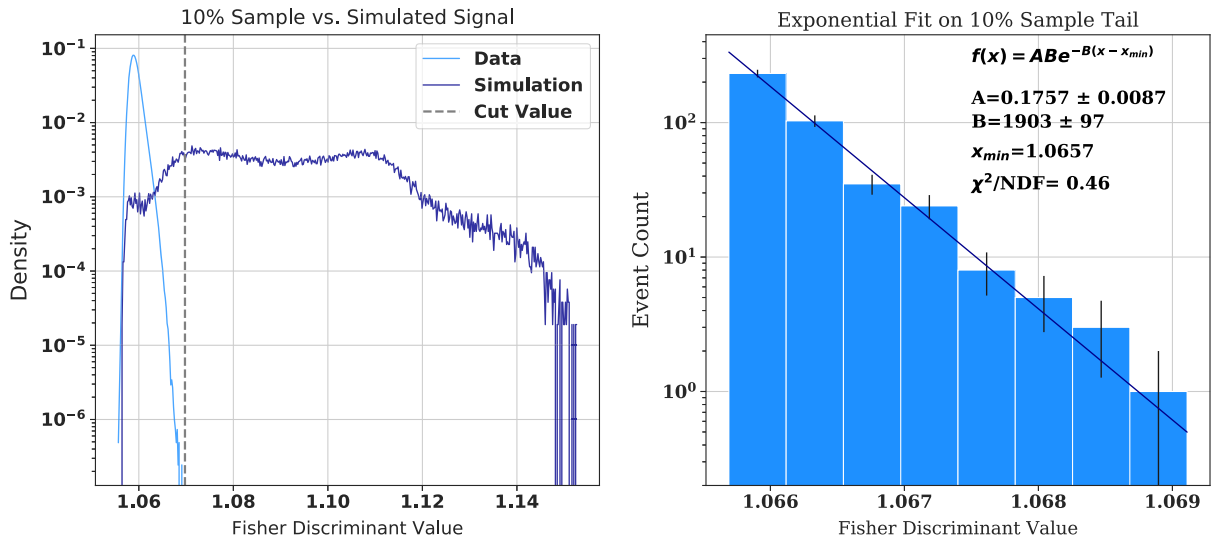


FIG. 6. Left: a comparison between the 10% training sample distribution and the simulated neutrino flux, with the optimized threshold marked with a vertical line. Right: the tail of the 10% training sample, with the exponential fit overlaid. The value of  $x_{\min}$  is defined as the minimum value of the Fisher discriminant in the tail of the 10% training sample.

TABLE II. Table of cuts, background estimates, and analysis efficiencies from the 10% training sample in the deep region. For the Fisher discriminant, the median background is reported, as are the 16th and 84th percentiles. The final row represents the cumulative background (summed across all cuts) and the cumulative efficiency (multiplied across all cuts).

Cut name	Events remaining	Background estimate	Signal efficiency
None	18,651,857	N/A	100%
Deep region boundary	6,005,122	N/A	79.03%
Cal pulser gate flag	4,423,436	N/A	99.98%
Cal pulser geometry cut	4,411,686	0.009	99.64%
Software trigger cut	4,014,776	N/A	100%
Fisher discriminant	0	$0.09^{+0.06}_{-0.04}$	86.58%
Total	0	$0.10^{+0.06}_{-0.04}$	68.16%

## V. RESULTS

### A. Deep region results

The final cuts and background estimate for the deep region are shown in Table II. Additionally, in Fig. 7 we report the analysis efficiency as a function of neutrino energy and as a function of SNR. For comparison, our efficiency is compared against the most recent published ARA result, ARA Station 2, as the baseline ARA5 data is not within the scope of this paper and will instead be analyzed in a future work. The sideband region just outside the deep signal region (52–57 degrees in zenith) was unblinded first as a validation of our background estimate and was not part of the signal region. In this region, we observe zero events passing all cuts. After unblinding the deep region only, we observe one event on a background of  $0.10^{+0.06}_{-0.04}$ . This event was triggered separately by both the baseline ARA trigger and the Phased Array trigger; the

SNR measured by the classic ARA5 instrument was measured to be 6.5 and 3.5 for VPol and HPol, respectively. The p-value of the event is calculated to be 0.11 using Poisson statistics. The event is included in the limit set in Fig. 10 and is shown in detail in Figs. 8 and 9.

Various hypotheses for the origin of the single passing event have been investigated. As discussed in [34], high wind speeds can cause a noticeable radio background; the wind speed at the time of this event was 2 m/s, well below the average of 6 m/s at the station location. The event occurred during the austral winter and, using the baseline A5 antennas, reconstructs in a direction pointing away from South Pole Station. This makes anthropogenic backgrounds unlikely but not impossible. Because the baseline A5 trigger also saw this event, we can rule out a glitch event internal to the Phased Array DAQ.

Neutrinos simulated using the ice model from Eq. (1) with similar arrival angles are almost exclusively refracted

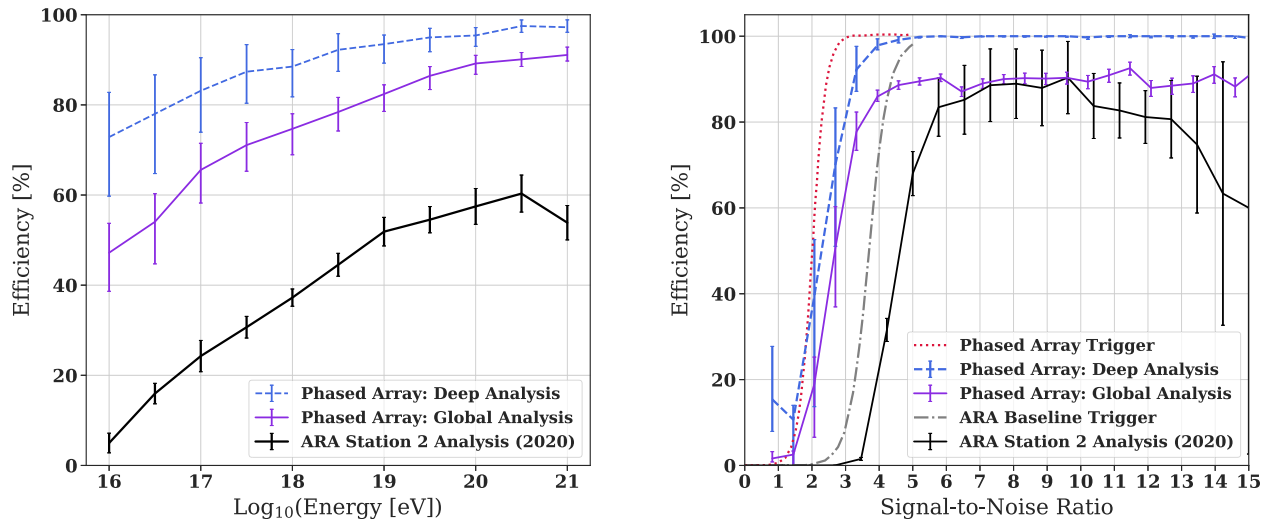


FIG. 7. Analysis efficiency of this work compared to the most recent ARA Station 2 analysis efficiency [23]. The blue curve is the efficiency on neutrinos in the deep region; the purple curve includes the efficiency loss from removing the surface region which results in a 21% loss in efficiency averaged over all energies. The analysis efficiency shown in the plot on the left is generated for each energy bin separately. The analysis efficiency shown in the plot on the right is generated based on a cosmogenic flux [28]. The trigger efficiency versus SNR is from [17], while the analysis efficiency from ARA Station 2 is adapted from [23].

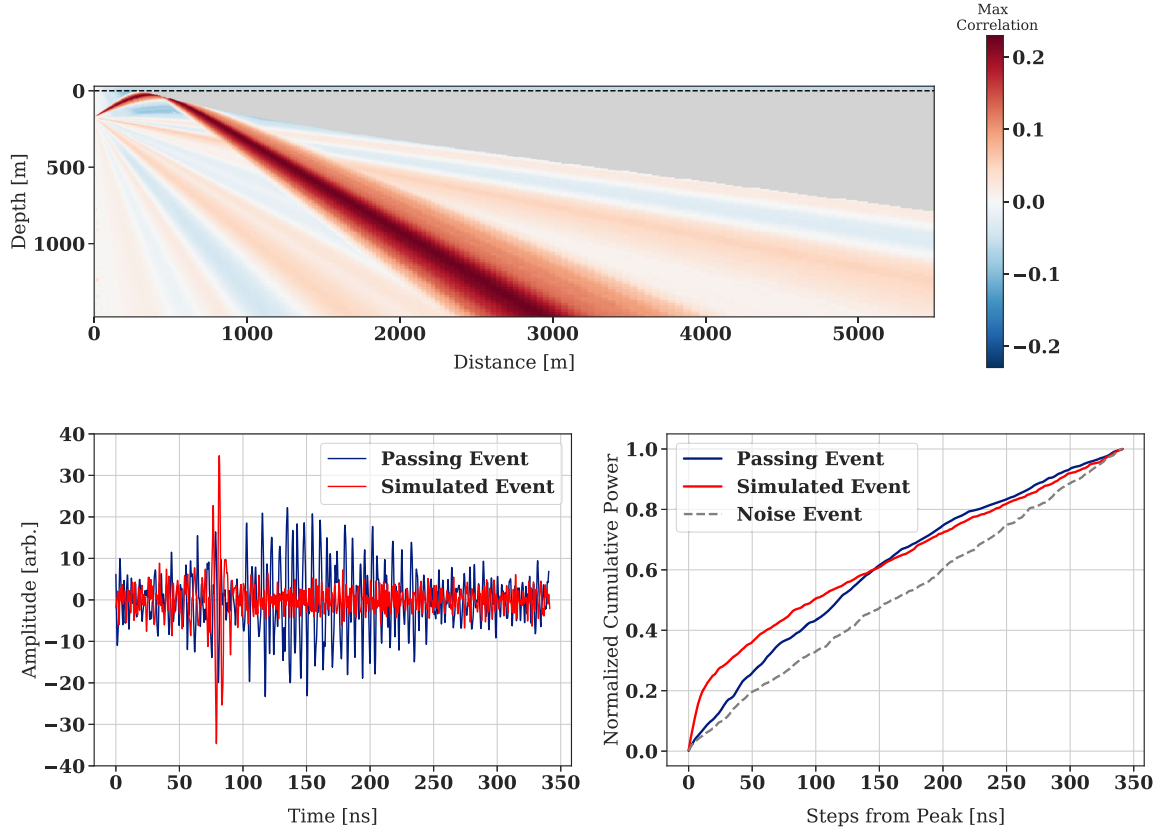


FIG. 8. Top: the correlation map of the passing event. Bottom left: the coherently summed waveform of the passing event, compared to a simulated event at the same incoming angle. The noise in the simulated waveform is normalized to have the same root-mean-square as the average from data. Bottom right: the impulsivity CDF for the passing event and the simulated event, with a noise event plotted for comparison.

neutrino events, in which the radio signal originates deep in the ice but curves near the surface before hitting the detector. The passing event is a longer, brighter signal than most simulated neutrino events, as seen in Fig. 8.

### B. Surface region analysis

The surface region was not included in the neutrino search in the analysis, due to an expected background of cosmic ray showers and anthropogenic noise. After completing the neutrino analysis, the surface region was unblinded and the same cuts were applied to this region. A total of 46 events passed the cuts. Of those events, 7 were not impulsive and reconstructed poorly; additionally, 3 events were time-clustered and likely anthropogenic. The remaining 36 were uniformly distributed in time, reconstructed to the surface well, and were generally impulsive, suggesting the sample likely contains cosmic ray candidates. By using the full A5 instrument to calculate azimuth angle, there was no excess of events that pointed toward South Pole Station. As discussed in [31], we expect multiple types of cosmic ray signals, including both in-air showers and impacting ice core events. More study and

discussion of potential cosmic ray candidates will be done in future publications.

## VI. DISCUSSION

### A. Limit on the diffuse neutrino flux and projected expected sensitivity

Using the signal region as defined above, with 1 event found in the 90% sample on a background of  $0.10^{+0.06}_{-0.04}$ , the 90% upper limit was calculated using the method laid out in [23] and is shown in Fig. 10. The key pieces of this calculation are: (1) the Feldman-Cousins upper limit; (2) the livetime; (3) the effective area, calculated from the effective volume and the interaction length of a neutrino interacting in the Earth; and (4) the analysis efficiency. This limit is the most sensitive published limit from the ARA collaboration at the lowest end of ARA's targeted energy range, even as the livetime of this analysis is lower by a factor of 14 compared to previous analyses. This improvement is a function of both a more sensitive trigger, leading to a higher effective volume, and improved analysis techniques made possible by the simplicity of the phased array geometry,

leading to better zenith angle reconstruction and a larger signal region.

While the lower trigger threshold afforded by the phased-array technique is well established, there has been an open question about whether the lower-amplitude events afforded by this technique would be efficiently separated from background. In this work we show that they can be and that the lower trigger threshold does indeed result in improved neutrino sensitivity at the analysis level. This is an optimistic finding for the other experiments planning to capitalize on a Phased Array trigger design to improve effective volumes [9,18,19,35].

As we scale up to larger experiments with longer livetimes and larger effective volumes, it is imperative to reduce backgrounds even further, and it will be important to understand the origin of the single passing event from this analysis, which is unlikely to be thermal noise. Additionally, if the single passing event were a neutrino signal, the flux would be approximately 100 times greater than the IceCube limit at energies above 10 PeV, considering the small area of ice surveyed, the small livetime included, and the higher energy threshold of the Phased Array compared with IceCube. This suggests a new type of background that was not modeled in this analysis and should be studied further. One potential explanation is a cosmic ray impacting core event penetrating the ice deeper than expected, or traveling through a poorly modeled region of ice near the surface. This hypothesis is helped by the fact that the trajectory intersects the “shadow” region close to the surface [36]. Better modeling of the ice near the shadow region, as well as ARA-specific cosmic ray simulations, would both help us understand the origin of this event, and help recover a larger fraction of the surface region to be used in a neutrino search.

Although this analysis focused on data taken in 2019, the Phased Array currently has just under 1000 days of total

livetime available, with more data taken every year. However, future analyses that take advantage of this data set will need to make some assumptions about the passing event. The projection in Fig. 10 takes the pessimistic assumption that only events reconstructing below 90 degrees are usable; the efficiency as a function of zenith angle is included in the Appendix in Fig. 11 for reference. In practice, an analysis on this full data could take advantage of a combination of characteristics that make this event an anomaly: its high SNR with relatively low correlation, its unusually long waveform, or its zenith angle near the edge of the signal region. Even considering the pessimistic option, the Phased Array alone could likely achieve the greatest sensitivity for the ARA experiment thus far across much of the energy range. Additional benefits can come from analyzing the data from the baseline ARA instrument, as well as the data taken from the other four ARA stations.

The high analysis efficiency in the deep region in particular is also encouraging. While the surface region was not included as part of the signal region in this analysis, the methods used in the deep region can be applied to the surface as well, provided that the types of expected backgrounds in the surface region are understood. Alternatively,

Variable Name	Passing Event	Simulated Event
Phased Array VPol SNR	8.59	6.49
Maximum Correlation	0.23	0.28
Fisher Score	1.0769	1.0999
Zenith Angle	60.54	60.18
Surface Correlation Ratio	0.13	0.04
Impulsivity	0.22	0.27
Event Time (UTC)	2019-05-13 03:22:37	N/A

FIG. 9. A table showing some of the values of analysis variables for the passing event, compared to the simulated neutrino events shown in Fig. 8.

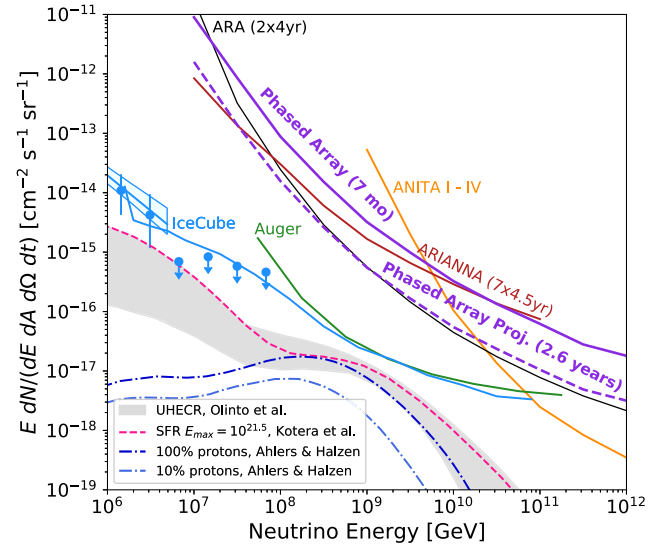


FIG. 10. The all-flavor limit from this Phased Array analysis, using one station and six months of livetime, along with the projected sensitivity from the entire available livetime of 2.6 years. The expected sensitivity is calculated by directly scaling the livetime and expected backgrounds, selecting the median expected background, and calculating the 90% upper limit. We also include a more conservative surface cut in the expected sensitivity, requiring a zenith angle of greater than 90°. Plotted for comparison are the previous published results from ARA (two stations, each with 4.0 station-years), along with results from ANITA [8], ARIANNA (seven stations, each with 4.5 station-years) [7], Auger [37] and IceCube [2,3]. Additionally, theoretical production models of cosmogenic neutrinos are plotted [38–40].



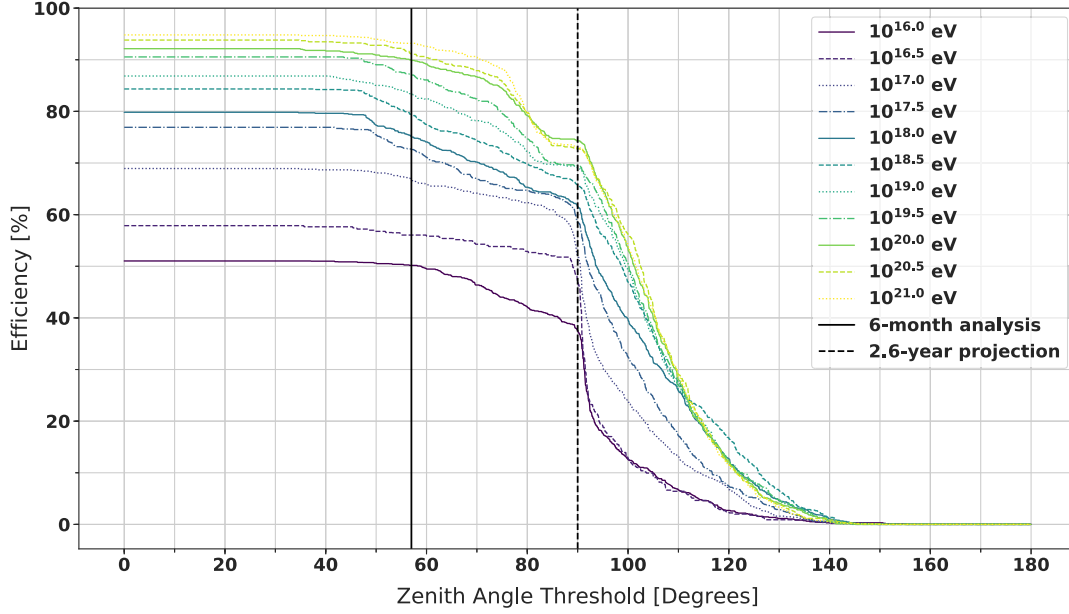


FIG. 11. The efficiency of the analysis as a function of zenith angle and half-decade energy bin. The solid black line shows where the zenith cut was applied for this analysis; the dashed black line is used for the projection in Fig. 10.

the size of the deep region could be increased by taking advantage of additional information provided by the baseline ARA instrument.

### B. Systematic uncertainties

The limit calculation includes uncertainties using the method described in [41]. In particular, we consider the uncertainties on the effective volume calculation and the analysis efficiency.

The uncertainties on the effective volume are introduced by the AraSim simulation package and are plotted in Fig. 2. Uncertainties in the neutrino cross section, the Askaryan emission model, and the attenuation length of ice are explicitly laid out in [23], which uses the same simulation code as we do in this work, allowing the uncertainties to directly carry over.

The key differences between the simulation used in [23] and this work are the ice model, the signal chain, and the trigger efficiency. The ice model is parametrized in the form  $n(z) = A - Be^{Cz}$ , with the parameters found to have the following uncertainties:  $A = 1.780 \pm 0.005$ ,  $B = 0.454 \pm 0.084$ ,  $C = -0.0202 \pm 0.0004 \text{ m}^{-1}$ . While the model is different than the model used in previous ARA analyses [23], two of the three parameters are within one standard deviation across the models, with the third being better constrained in the model used here due to the short baselines of the Phased Array. We estimate that the uncertainty in our ice model introduces a 5% uncertainty in the effective volume. Even though the ice model was fit using calibration pulses from deep ice, all surface calibration events were successfully pointed back at the sources using the new ice model.

The signal chain uncertainty is dominated by the uncertainties in the antenna response, described in [42] and estimated as a 10% effect in total. The Phased Array signal chain uncertainty independent of the antennas is measured in the lab as  $<5\%$ . From these measurements, we estimate that with the antennas included, the total signal chain uncertainty for the Phased Array instrument is also 10%. From [23], this adds a 3% uncertainty in the effective volume.

The Phased Array trigger is simulated separately from the typical ARA trigger, and has its own uncertainties. Unlike the previous analysis, the output of the Phased Array simulation was tuned to perfectly match the trigger efficiency as a function of SNR. In [17], we estimate that the error on the location of the 50% trigger point used in the simulation is  $1.8 \pm 0.2$  in SNR. This translates to a total trigger uncertainty of approximately  $\pm 5\%$  for events with SNR below 3; this corresponds to a  $\pm 2.5\%$  impact on effective volume at  $10^{16}$  eV and decreases to  $\pm 1\%$  or less at energies above  $10^{18.5}$  eV.

Finally, we consider the uncertainties related to the analysis, introduced by the Fisher discriminant. By calculating the efficiency on simulated neutrinos for the expected background range, the total simulation efficiency and its uncertainty are  $68_{-3}^{+5}\%$ . Events with the lowest calculated SNRs are most impacted by this, as they are more likely to be assigned Fisher discriminant values similar to noise.

## VII. CONCLUSION

The results presented here represent the most efficient analysis conducted with the ARA instrument, and the

lowest threshold analysis ever conducted out of all radio-detection neutrino experiments. We show that the gains made possible by a more efficient trigger are gains that can be carried through the analysis, motivating the design of future Phased Array triggers for in-ice neutrino detectors. Finally, further modeling of the backgrounds in the surface region, as well as investigations into the origins of the passing event, may lead to additional gains in analysis efficiency.

### ACKNOWLEDGMENTS

K. H. was the main author of this manuscript and led the analysis discussed. The ARA Collaboration designed, constructed, and now operates the ARA detectors. We would like to thank IceCube and specifically the winter-overs for the support in operating the detector. Data processing and calibration, Monte Carlo simulations of the detector and of theoretical models and data analyses were performed by a large number of collaboration members, who also discussed and approved the scientific results presented here. We are thankful to the Raytheon Polar Services Corporation, Lockheed Martin, and the Antarctic Support Contractor for field support and enabling our work on the harshest continent. We are thankful to the National Science Foundation (NSF) Office of Polar Programs and Physics Division for funding support. We further thank the Taiwan National Science Councils Vanguard Program NSC 92-2628-M-002-09 and the Belgian F. R. S.-FNRS Grant No. 4.4508.01. K. H. thanks the NSF for support through the Graduate Research Fellowship Program Grant No. DGE-1746045. B. A. C. thanks the NSF for support through the Astronomy and Astrophysics Postdoctoral Fellowship under Grant No. 1903885, as well as the Institute for Cyber-Enabled Research at Michigan State University. A. C. thanks the

NSF for Grant No. 1806923 and also acknowledges the Ohio Supercomputer Center. S. A. W. thanks the NSF for support through CAREER Grant No. 2033500. D. B. acknowledges support from National Research Nuclear University MEPhI (Moscow Engineering Physics Institute). A. V. thanks the Sloan Foundation and the Research Corporation for Science Advancement, the Research Computing Center and the Kavli Institute for Cosmological Physics at the University of Chicago for the resources they provided. R. N. thanks the Leverhulme Trust for their support. K. D.dV. is supported by European Research Council under the European Unions Horizon research and innovation program (Grant agreement 763 No. 805486). D. B., I. K., and D. S. thank the NSF for support through the IceCube EPSCoR Initiative (Award No. 2019597).

### APPENDIX: EFFECT OF ZENITH CUT ON EFFICIENCY

Because this analysis includes a passing event at a zenith angle of  $60.5^\circ$ , future analyses may want to consider how such an event could be removed. Possibly the simplest solution is a requiring all events to reconstruct at an angle greater than  $60.5^\circ$ , although likely a more targeted approach would be more efficient.

The projected limit in Fig. 10 takes a pessimistic approach and includes the efficiency hit if a zenith threshold at  $90^\circ$  is applied in the analysis. Other options could include a zenith threshold at  $79^\circ$ , corresponding to the most pessimistic zenith angle used in previous ARA analyses [23], or a zenith threshold at  $61^\circ$ , just greater than the zenith angle of the passing event. For the convenience of the reader, the efficiency of all zenith angle thresholds as a function of energy is included in Fig. 11.

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