Analysis of Individual-level Data from 2018-2020 Ebola Outbreak in Democratic Republic of the Congo

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Abstract

The 2018-2020 Ebola virus disease epidemic in Democratic Republic of the Congo (DRC) resulted in 3,481 cases (probable and confirmed) and 2,299 deaths. In this paper, we use a novel statistical method to analyze the individual-level incidence and hospitalization data on DRC Ebola victims. Our analysis suggests that an increase in the rate of quarantine and isolation that has shortened the infectiousness period by approximately one day during the epidemic's third and final wave was likely responsible for the eventual containment of the outbreak. The analysis further reveals that the total effective population size or the average number of individuals at risk for the disease exposure in three epidemic waves over the period of 24 months was around 16,000—a much smaller number than previously estimated and likely an evidence of at least partial protection of the population at risk through ring vaccination and contact tracing as well as adherence to strict quarantine and isolation policies.

Significance Statement

With the world health community largely preoccupied with the current COVID-19 pandemic, the Ebola Virus Disease (EVD) continues to lurk as a significant threat to public health, prosperity, and political stability in large regions of Africa with undiminished potential for spread to other parts of the world. Despite its vital importance for public health policy, knowledge about the effects of the recent 2018-2020 EVD response efforts in the Democratic Republic of the Congo (DRC) based on ring vaccination supplemented with isolation and quarantine has been limited by challenges with data collection and by the lack of simple methods for analyzing complex multi-wave patterns of disease incidence occurring across time and space. Within this environment, competing narratives with differing policy implications emerged around the effectiveness of vaccination strategy and the need for supporting DRC Ebola treatment centers. To address this issue, University of Kinshasa researchers collected a large number of individual records of disease histories from probable and confirmed Ebola cases during the 2018-2020 EVD outbreak in DRC. This study describes a model-based Bayesian statistical method developed to estimate the effects of ring vaccination, quarantine, and isolation in Ebola treatment centers across northwestern provinces of the country. The method accounts in particular for missing and censored data, heterogeneity of infection patterns and multiple waves of infection with different intervention strategies.

1 Introduction

We present here a quantitative analysis of the effects of public health interventions against the spread of the Ebola virus disese (EVD) during the DRC Ebola epidemic that unfolded between August 2018 and September 2020 in the northeastern provinces of DRC [1, 2], partially sharing the timeline of the better known and much larger West African epidemic [3]. The DRC 2018 epidemic, being more geographically contained and smaller, was considerably better documented, with the majority of cases' disease histories collected through the efforts of the College of Public Health at the University of Kinshasa [4]. The work of these researchers allowed in particular for tracking the time elapsed between symptom onset, hospitalization, and recovery or death for over 3000 Ebola victims, creating a unique opportunity for detailed analysis of the epidemic dynamics based on individual disease histories.

The authorization for emergency use of Merck experimental Ebola vaccine rVSV-ZEBOV-GP [5, 6] and its field deployment in 2019 has provided for better protection of those involved in monitoring efforts, as it was given to many frontline workers including doctors, nurses, and burial workers. An estimated 330,000 people living in the northern DRC provinces were vaccinated in 2019 and 2020, including frontline workers as well as ring vaccinations of the contacts of suspected and confirmed cases. This was done in part by the international nongovernmental organization Doctors Without Borders, with authorization by the Ministry of Health, concerned with the possibility of further northward spreading of the disease [1]. However, the more comprehensive vaccination efforts were complicated and significantly delayed in late 2019 and in 2020 by local distrust, political instability and the resulting lack of security both for aid workers and for vaccine supplies [7]. For those reasons, despite the apparent effectiveness of the rVSV-ZEBOV-GP Ebola vaccine, quarantine and isolation were often still the primary and most effective practical interventions for breaking the chain of transmission, especially in rural and isolated communities across northern DRC.

Early in the outbreak, a large number of health care workers working for the DRC ministry of health were brought to the villages to monitor possible EVD symptoms as the ring vaccination campaign was introduced wherever adequate vaccine supplies were procured and safe funeral practices were mandated [8]. All these factors likely limited the size of the initial outbreak and prevented the uncontrolled EVD spread into the crucial commercial centers of the region along the border towns of Goma in North Kivu and Gisenyi in Rwanda [9]. The spillover of DRC cases to Rwanda and possibly Uganda would have undoubtedly and considerably increased the geographical reach of the outbreak. Largely due to successful public health monitoring efforts, EVD spread occurred mainly via symptomatic individuals in relatively isolated villages, which contributed to better protection of neighbors and other household members of EVD victims and the lack of transmission in the treatment centers and among health care workers. This simplified transmission chain allowed us, in turn, to implement a relatively simple mathematical model of infection spread based on an individual-level stochastic SIR (susceptible-infected-recovered) model [10].

The classical SIR model for epidemic dynamics was introduced in early 20th century for malaria and cholera and led to the so-called ecological models of infections usually described by ordinary differential equations (ODEs) [11]. Such models typically represent an epidemic as a process of transferring individuals between disease-related states (or compartments) and describe it in terms of the temporal changes in the compartment sizes. For the purpose of our analysis, we consider a version of that classical model, which focuses on the fate of a single individual (or agent), making our approach similar to the modern agent-based model (ABM) approach to disease modeling [12]. Although other more complex ecological models have been used for studying Ebola transmission (most notably including "funeral" and "exposed" compartments, see [13]), it appears that for 2018 DRC Ebola data our stochastic SIR model is both

sufficiently flexible to incorporate the heterogeneity of individual disease histories and simple enough to require only a small set of population-level parameters. This allows us to estimate the key quantities of interest in the DRC outbreak, such as the rates of disease reproduction and quarantine/isolation (or hospitalization) and the size of the subpopulation at risk of infection though contact with EVD cases. The model also accounts for observed seasonality and spatial variation in the number of cases (e.g., see [14]) by allowing for the three independent sets of parameters to govern the three waves of infections observed over the course of the outbreak. For the purpose of our analysis we have determined, similarly as in [7], the first wave to end in late February 2019 and the second one to end around late May 2020. See Table 1 below for more details. Our approach may be also viewed as an alternative to the complicated multi-phase longitudinal analysis proposed recently for the DRC outbreak data in [15].

2 Materials and Methods

2.1 Ebola Dataset

The 2018-2020 DRC EVD outbreak lasted over 24 months and spread over 3 distinct spatial and temporal waves. Between the emergency declaration of the EVD outbreak in northern DRC on August 1, 2018 and the outbreak's official end on June 25, 2020, the DRC Ministry of Health has reported a total of 3,481 cases (including confirmed and probable), 1,162 recoveries, and 2,299 deaths [16] in the provinces of Northern Kivu, Southern Kivu, and Ituri. The dataset considered here is a large subset of the entire EVD database compiled by the University of Kinshasa School of Public Health, which comprises 3,117 total case records (confirmed and probable) recorded between May 3, 2018, and September 12, 2019. The data included partially de-identified but still detailed patient information, such as each person's location, date of symptom onset and hospitalization, as well as discharge due to recovery or death. These individual records came from the Ebola treatment centers in 24 different health zones, spread out among the three DRC provinces of Northern Kivu, Southern Kivu, and Ituri.

Of the 24 health zones, 77.1% of all cases were from only 6: Beni, Butembo, Katwa, Kalunguta, Mabalako, and Mandima. Only 9.7% of cases were under the age of 18. There is also a slightly larger proportion of females contracting the disease, comprising 57.0% of the cases. Approximately 5% of the cases were health care workers. About one-third of the EVD fatalities were not identified until patient's death and thus not effectively isolated from the time of infection. Although over 170,000 contacts of confirmed and probable Ebola cases had been monitored across all affected health zones for 21 days after their last known exposure by the end of the epidemic, some of the contact tracing was incomplete due to insecurity that prevented public health response teams from entering some communities. The overall case density map is presented in panel (A) of Figure 1 with the animated version of the map presented in the appendix in Figure A.1. Notice that the high-density areas, particularly Butembo, Katwa, and Beni, are all spatially small health zones corresponding to cities or towns with larger populations.

2.1.1 Case Alerts and Definitions

Since early August, 2018, the DRC Ministry of Health has been collaborating with several international partners to support and enhance EVD response activities through its emergency operations center in Goma. To the extent possible given regional security considerations [19], the response teams were deployed to interview patients and their suspected contacts using a standardized case investigation form classifying cases as suspected, probable, or confirmed. A suspected case (whether surviving or not) was defined



Figure 1: **DRC Ebola Dataset.** (A) The spatial distribution of 3,481 EVD cases across the northern DRC health zones during Ebola 2018-2020 outbreak. (B) The flowchart of personal records available up to September 12, 2019 available for the current analysis. The total number of available individual disease records was 3,080. Map created using open software R [17] with geospatial data obtained from [18].

as one with the acute onset of fever (over 100°F) and at least three Ebola-compatible clinical signs or symptoms (headache, vomiting, anorexia, diarrhea, lethargy, stomach pain, muscle or joint aches, difficulty swallowing or breathing, hiccups, unexplained bleeding, or any sudden, unexplained death) in a North Kivu, South Kivu, or Ituri resident or any person who had traveled to these provinces during this period and reported the signs or symptoms defined above. A patient who met the suspected case definition and died but from whom no specimens were available was considered a probable case. A confirmed Ebola case was defined as a suspected case with at least one positive test for Ebola virus using reverse transcription polymerase chain reaction (RT-PCR) [20] testing. Patients with suspected Ebola were isolated and transported to an Ebola treatment center for confirmatory testing and treatment [2].

2.1.2 Onset and Removal

In our analysis of the DRC dataset, we focused on dates of symptom onset and removal, with removal defined as either a death/recovery at home or transfer to an Ebola treatment center (ETC). It was assumed that, once in the treatment center, the probability of further infection spread by an isolated individual was very small due to the strict safety protocols—and later due also to vaccination of healthcare personnel and family members who were in contact with the suspected Ebola case. As summarized in panel (B) of Figure 1, we were able to access 3,117 out of 3,481 individual records of confirmed and probable Ebola cases. Of these 3,117 records, 37 were missing both the onset and recovery dates and were removed from further analysis. In about 30% of the remaining records, either their dates of onset or removal were missing. A detailed flow diagram summarizing the amount of missing data and data processing leading to the final dataset is presented in panel (B) of Figure 1. The distribution of the original and the partially



Figure 2: Daily Incidence and Removal Rates. Daily incidence (grey bars) and removal counts (red dots) during DRC Ebola 2018-2020 outbreak between August 15, 2018 and September 12, 2020 along with their respective trendlines (loess smoothers). The blue trendline above the plot represents daily effective reproduction number \mathcal{R}_t defined as the ratio of daily number of new infections to new removals. The vertical lines indicate cut-off dates for data collection in each wave as listed in Table 1.

imputed records across the three waves of infection is provided for further reference in Table 1.

2.1.3 Spatial and Temporal Patterns

Throughout the pandemic, the incidence rates exhibited strong spatial and temporal patterns that can be summarized as three distinct waves of infections with approximate boundaries marked by vertical lines in Figure 1. The distribution of weekly reported cases across the most affected health zones listed in Table 1 is provided in the bar plot and in the corresponding animation in the appendix (see Figure A.1). As seen from the bar chart and the animated plot, the epidemic was initially driven largely by infections in the health zones of Beni, Mandima and Mabalako. After several months, the incidence of new cases in these zones subsided, but the epidemic moved south to the health zones of Katwa and Butembo, where the majority of new infections was registered between weeks 22 to 45 of the epidemic (see Panel (A) in Figure A.1 in the Appendix). In the final spatial shift, around week 49, the epidemic returned to the health zones of Beni, Mandima, and Mabalako, where it was mostly extinguished around week 60 (September 2019). Isolated Ebola incidences occurred sporadically across northern DRC until end of the outbreak was officially declared in June 2020.

The empirical patterns of incidence and removal for EVD cases are summarized in Figure 2 with the bar and the dot plots representing the daily numbers of new infections and removals, respectively. As seen from the plot, these daily counts closely follow a three-wave temporal pattern in Table 1. This is further evident from the black and red trendlines representing the loess smoothers (see [21]). The daily ratio of new cases and removals may be interpreted as a crude estimate of the *effective reproduction* number \mathcal{R}_t defined more formally in (2) in Section 2.2 below. In particular, the blue trendline for \mathcal{R}_t

Table 1: **Observed Cases by EVD Wave.** The observed cases aggregated by 3 infection waves and the corresponding cutoff date for data collection. The number of cases observed in wave 3 by September 12 was 1,113 with a combined total of 3,117 cases across all three waves (see Figures 1).

| | Wave 1 | Wave 2 | Wave 3 | Total |
|-------------------------------|-------------------|--------------------------------------|----------------------------|-------|
| Cut-off Dates | February 27, 2019 | May 27, 2019 | September 12, 2019 | |
| No. Cases | 907 | 1104 | 1477 | 3481 |
| Most Affected Health Zones | Beni, Katwa | Butembo, Katwa, Mabalako, Mandima | Beni, Kalunguta Mandima | |

indicates that towards the end of the observed time period, the number of removals outpaced the number of new infections ($\mathcal{R}_t < 1$). The ability to sustain this pattern for a sufficiently long time period, mostly by increasing the rate of quarantine and ETC transfers along with ring vaccination of case contacts was largely credited with the end of EVD epidemic in mid-2020. The quantification of this public health intervention effect in 2018-2020 DRC outbreak is one of the main motivations for our model-based analysis. Although the precise cut-off dates for the three waves of 2018-2020 Ebola infections are difficult to establish, the incidence data along with simple statistical analysis (see Section 2.3) indicate that the first wave lasted approximately until the end of February 2019, whereas the second wave ended around the end of May 2019. For the purpose of the data analysis below, the specific break dates used were February 27, 2019 and May 27, 2019 as marked by vertical lines in Figure 2. September 12, 2019 was the cutoff date for the individual records data available from the University of Kinshasa (see Table 1).

2.2 Model for Data Analysis

The analysis of the individual-level epidemic data is based on the standard ecological model known as the SIR (susceptible-infected-removed) model and developed for the purpose of analyzing average behavior of a large population with a homogenous pattern of interactions [22, 11]. Although there are many variants of SIR models in the literature [23], our current analysis considers the classical Kermack-McKendrick SIR model that assumes the proportions of population categorized as susceptibles (s), infected (ι) , or removed (r) to evolve according to the differential equations

$$\begin{aligned} \dot{s}_t &= -\beta s_t \iota_t, \\ \dot{\iota}_t &= \beta s_t \iota_t - \gamma \iota_t, \\ \dot{r}_t &= \gamma \iota_t, \end{aligned} \tag{1}$$

with $s_0 = 1, \iota_0 = \rho > 0$ and $r_t = 0$ where $\beta > 0$ is the rate of infection, $\gamma > 0$ is the rate of recovery and $\rho > 0$ is the initial amount of infection. In particular, the model implies the existence of the basic reproduction number \mathcal{R}_0 (R-naught), which determines the average speed of disease spread [11] and is given by the formula

$$\mathcal{R}_0 = \beta / \gamma.$$

If $\mathcal{R}_0 > 1$, the proportion of infected initially rises and then subsides, with the final proposition of surviving susceptibles given by $s_{\infty} = 1 - \tau > 0$ where τ is know as the epidemic's *final size*. In typical statistical analysis, an estimate of \mathcal{R}_0 is obtained by separately estimating the parameters β and γ . Another important quantity related to (1) is the *effective reproduction number*, which is typically defined as

$$\mathcal{R}_t = \mathcal{R}_0 s_t. \tag{2}$$

Although equation (1) is typically considered in the context of an average behavior of a large population, for our purposes we interpret it as defining the individual histories of infection and recovery, according to the idea of the dynamic survival analysis (DSA) discussed recently in [10] and [24] and also briefly summarized in the Appendix. With the DSA approach, we interpret equation (1) as the so-called stochastic master equation [25] describing the change in probability of a randomly selected individual being at time t either susceptible, infected, or removed. These respective probabilities are represented by the scaled proportions $s_t/(1+\rho)$, $\iota_t/(1+\rho)$, and $r_t/(1+\rho)$ and evolve according to (1). As outlined in [10], the DSA-based interpretation of the classical SIR equations has a number of advantages that make it particularly convenient for analyzing epidemic data consisting of individual histories of infection onsets and removals, which is exactly the type of data available in the DRC Ebola dataset. The fact that the model is individual-based implies also that we can vary the parameters $\theta = (\beta, \gamma, \rho)$ to account for individual covariates and changes in the parameter values over time, as different waves of infection sweep through the population. Finally, for the purpose of our analysis, it is also important to note that the DSA model does not require any knowledge of the size of the susceptible population subjected to the epidemic pressure. For the DRC dataset, that assumption would be difficult to justify due to spatial and temporal heterogeneity of the epidemic and the frequent movements of local populations driven by political conflicts and insecurity. Another element complicating the determination of the size of susceptible population was the ring vaccination campaign that has been conducted since 2019 wherever possible in the northern DRC during periods of relative stability, despite local mistrust and supply issues. This campaign ultimately resulted in over 250,000 vaccinations.

Note that, because $s_0 = 1$, the values of \mathcal{R}_0 and \mathcal{R}_t coincide for t = 0. Moreover, $s_t = \exp\left(-\mathcal{R}_0 \int_0^t r_u du\right)$ is a decreasing function of time and therefore, so is \mathcal{R}_t . However, in practice, this implication is problematic. Rewriting $\mathcal{R}_t = -\dot{s}_t/\dot{r}_t$ suggests that a crude but sensible way to estimate \mathcal{R}_t empirically is to take the ratio of daily number of new infections to new removals. The empirical \mathcal{R}_t thus estimated will not be necessarily monotonically decreasing. In the light of possibly changing parameters and the effective population size, we have adopted this approach to estimating the daily effective reproduction number \mathcal{R}_t in Figure 2.

2.3 Parameter Estimation

We assume that, for each of the three waves of the epidemic, we have a separate and independent set of parameters θ and that, in each wave, we observe n_T histories (records) of infection. The *i*-th individual history may be represented either by the times of disease onset and removal (t_i, T_i) or by t_i or T_i times alone (t_i, \circ) or (\circ, T_i) (\circ denoting missing value). We assume that among the available n_T histories we have n complete records (t_i, T_i) , n_1 incomplete ones (t_i, \circ) and n_2 incomplete ones (\circ, T_i) . The wave-specific DSA likelihood function for n complete data records is (see Appendix)

$$\mathcal{L}_{C}(\theta|t_{1}...,t_{n},T_{1},...,T_{n},T) = (s_{T}-1)^{-n} \prod_{i=1}^{n} \dot{s}_{t_{i}} \gamma^{w_{i}} e^{-\gamma(T_{i} \wedge T - t_{i})}$$
(3)

where T is the available time horizon and w_i is the binary variable indicating whether T_i is right-censored (that is, $T_i \wedge T = T$) in which case $w_i = 0$ and otherwise $w_i = 1$. For the remaining $n_1 + n_2$ records that are partially incomplete, the wave-specific DSA likelihood function is

$$\mathcal{L}_{I}(\theta|t_{1}\dots,t_{n_{1}},T_{1},\dots,T_{n_{2}},T) = (s_{T}-1)^{-(n_{1}+n_{2})}\gamma^{n_{2}}\prod_{i=1}^{n_{1}}\dot{s}_{t_{i}}\prod_{i=1}^{n_{2}}(\rho e^{-\gamma T_{i}}-\iota_{T_{i}})$$
(4)

where we assume that $T_i < T$. The overall likelihood for all n_T individual histories is obtained by multiplying (3) and (4). Note that the likelihood formulas depends on the parameter β only implicitly, through the values of the function s_t defined by (1). Note also that we assume T to be unique and exactly known although in practice this may not be true as subsequent waves of infection may be too close in time (perhaps even overlapping) to allow for a precise specification of T. In our analysis below, we solve this practical problem by considering several candidates for the values of T in each wave and then identifying ones that jointly maximize the combined posterior distribution corresponding to the wave-specific likelihoods in equation (3).

The fitting of the model parameters $\theta = (\beta, \gamma, \rho)$ by maximizing the likelihood function (3) can be conveniently integrated into the Bayesian estimation framework, which allows for a more complete propagation of uncertainty and the use of external information in the statistical model. This, in turn, allows us to produce estimates that reflect all available information and uncertainty. In our DRC data analysis, the approximate posterior densities of θ were obtained using the Hamiltonian Monte-Carlo sampler [26] implemented in the open source statistical software STAN [27] and integrated with the popular statistical analysis language R via the library Rstan [28]. For the Rstan analysis, we have assumed uniform (sometimes improper) prior distributions on the θ components as follows

$$\beta \in (0.15, \infty),$$

$$\gamma \in (0, \beta),$$

$$\rho \in (0, 1).$$
(5)

The lower bound was placed on β based on empirical information, and the upper bound was placed on γ to enforce the constraint $\mathcal{R}_0 > 1$. Given the wave-specific time horizons (*T*'s), the set of parameters for each epidemic wave was estimated independently using 2 independent chains of 3000 iterations, with a burn-in period of 1000 iterations. The chains' convergence assessed using Rubin's R statistic [28]. The analysis resulted in approximate samples from the posterior distribution of θ for each of the three waves of the epidemic (see e.g., Figure 4).

2.3.1 Ethics Statement on Human Subjects and Methods

The research was conducted in accordance with the relevant guidelines and regulations of the US law and OSU Institutional Review Board. The research activities involving human subjects discussed in the paper meet the US federal exemption criteria under 45 CFR 46 and 21 CFR 56.



Figure 3: Model Fit. Comparison of the statistical model fit (red curve) with the observed daily incidence (onset) and removal relative counts for all 3 waves of the epidemic combined. The shaded region indicates the 95% credibility bounds based on the posterior distributions of the model parameters estimated separately for each wave with values summarized in Table 2.

3 Results

The overall comparison of the parametric DSA model predictions with the empirical data in DRC dataset until September 12, 2019 is given in Figure 3, where the scaled theoretical densities of the epidemic are plotted alongside the observed relative daily counts of infection (onset) and removal shown earlier in Figure 2. As seen from the plots, the multi-wave model appears to capture well the empirically observed patterns of daily counts represented by the histogram bars. The 95% credibility bounds around the model fit (marked in blue) are calculated based on the model parameter posterior distributions estimated via the MCMC algorithm with priors described in Section 2.3. We note that, although the DSA fit curve appears quite similar to the non-parametric loess smoother presented in Figure 2, the parametric fit has an advantage of providing an explicitly interpretable set of parameters describing the outbreak dynamics. This allows, for instance, for a purely quantitative comparison of the 3 different epidemic waves.

The wave-specific results of the MCMC analysis are summarized in Table 2 with some of the posterior plots presented in Figure 4. In Table 2, the posterior mean and corresponding credibility interval for each component of $\theta = (\beta, \gamma, \rho)$ are listed for each epidemic wave along with the estimated reproduction numbers. Additionally, in the last two rows, the posterior estimates of the effective population size (N) and the outbreak size (K_{∞}) are reported (see appendix Section B for formal descriptions of these quantities). The MCMC estimation scheme that produced the numerical values listed in the table was based on the wave-specific likelihood functions in equation (3) conditioned on the observation periods (T) according to the cut-off dates in Table 1. As seen from the entries of Table 2 and from the posterior density plots in Figure 4, the parameter values for the infection rate (β) , recovery rate (γ) and the initial

| Parameter | Wave 1 | Wave 2 | Wave 3 |
|--------------------|-------------------------------------|-------------------------------|---|
| Т | 300 days | 89 days | 108 days |
| eta | $0.190\ (0.178,\ 0.204)$ | $0.217 \ (0.201, \ 0.232)$ | $0.235\ (0.218,\ 0.253)$ |
| γ | $0.169\ (0.157,\ 0.183)$ | $0.179\ (0.165,\ 0.192)$ | $0.214\ (0.199,\ 0.230)$ |
| ho | $0.00021 \ (0.00016, \ 0.00027)$ | $0.0054 \ (0.0044, \ 0.0065)$ | $0.0067 \ (0.0055, \ 0.0081)$ |
| \mathcal{R}_0 | $1.124 \ (1.108, \ 1.142)$ | $1.214 \ (1.168, \ 1.262)$ | $\scriptstyle{1.098\ (1.061, 1.135\)}$ |
| | | All Waves | |
| \hat{K}_{∞} | 3481.41 (2877.416, 4155.878) | | |
| \hat{N} | $16385.61 \ (14416.33, \ 18703.71)$ | | |

Table 2: **Parameter Estimates.** Wave-specific posterior estimates (means and 95% credibility bounds) from the parametric model in equation (3).

prevalence of infection ρ all differ considerably across waves. The most notable appears to be an average increase of 14% in the posterior β values between waves 1 and 2. This change is seen to correspond to an 8% increase in the value of the posterior mean of \mathcal{R}_0 and the subsequent increase in the number of infections in wave 2 of the EVD outbreak. Another interesting observation in Table 2 is that, while the average value of β increased moderately (about 8%) between epidemic waves 2 and 3, the corresponding average value of γ increased over twice as much (almost 20%). Recalling the plot of the empirical effective reproduction number in the top part of Figure 2, it appears that this increase was crucial in ultimately controlling epidemic growth and ending the outbreak within the next several months. We note that the increase in the removal rate γ corresponds to the decrease in the duration of the infectious period $1/\gamma$ (measured in days). Thus, the increase in the respective γ values corresponds in this case to a decrease in the average infectious period from 5.6 days to 4.7 days. This could be further compared with the average infectious period in the initial wave 1 of the epidemic, which was estimated by the model at almost 6 days (corresponding to the posterior mean $\gamma = 0.169$). These differences in the wave-specific estimates of β and $1/\gamma$ are also clearly seen in their posterior density plots in the top panels of Figure 4, and they appear to be consistent with the empirical onset and removal rates shown in Figure 2.

As already indicated, one of the advantages of the parametric DSA approach is that it does not require knowledge of the underlying susceptible population size but may instead infer that value from the incidence data and the estimated epidemic parameters (see appendix Section B). The posterior means and 95% credibility bounds for the outbreak size (K_{∞}) and the effective population size (N) are listed in the last two rows of Table 2, and their posterior densities are presented in the bottom panels of Figure 4. In the bottom-left panel (C), we compare the model-predicted size of an outbreak (represented by posterior density contour with the mean of 3,481.4) to the number of cases officially reported by DRC health officials at the end of the epidemic in June 2020 (represented by the red vertical line at 3,481). The effective population size corresponding to that value is marked by the vertical line in the posterior density plot in the bottom-right panel (D). Both vertical lines appear close to the modes of the posterior distributions indicating good agreement of the model-based estimates with empirical data. Note that the model predicted effective population size corresponding to the observed outbreak size is only around 16,000 with the posterior CI between 14,416.33 and 18,703.71, which is a much smaller number than one might expect based on demographic estimates (see also Conclusions).



Figure 4: Top Panels: Parameters in Different Waves. The posterior distributions of β and $1/\gamma$ parameters for each of the three epidemic waves. The large increase in the rate of infection between waves 1 and 2 is clearly visible in panel (A). In panel (B), the density of $1/\gamma$ represents the distribution of time from symptom onset to removal. Between wave 1 and wave 3 of the epidemic, the average time shortened from 6 to 4.6 days. Bottom Panels: Outbreak Size and Effective Population Size. (C) The posterior density of the outbreak size based on the statistical model and the actual number of observed EVD cases (vertical red line). (D) The posterior density of the effective population size for the epidemic. The vertical line corresponds to the empirical outbreak size (red line in panel (C)).

4 Conclusions

Outbreaks of Ebola in Africa are a persistent threat not only to global public health but also to economic and political stability in some of the world's poorest and most vulnerable regions. Despite early evidence of effectiveness of the ring vaccination effort, the prolonged political and armed conflict in northern DRC, where the latest public health intervention took place, has seeded mistrust towards local authorities and international partners. This has impeded effective community collaboration, complicating the vaccination campaign and the overall response strategy [19]. To evaluate the effects of public health response to EVD outbreak in DRC during 2018-2020, we used the individual-level data based on case ascertainment, vaccination records, and contact enumeration collected by researchers at the University of Kinshasa School of Public Health in collaboration with local health authorities in northern DRC from August, 2018 to September, 2019. The analysis of this dataset is crucial for informing current and future EVD intervention policies and strategies regarding vaccination, quarantine, and isolation. However, the analysis is also quite challenging due to incomplete or missing patient information as some families have resisted putting their loved ones in isolation and some individuals have absconded from Ebola treatment centers. Another challenge is the complexity of the data itself, with individual patient histories spanning multiple waves of infections across multiple seasons and spatial environments result in very heterogenous and sometimes incompatible health records.

To overcome these challenges and analyze the University of Kinshasa dataset, we employed the dynamic survival analysis (DSA) method [10], which combines an individual-level Bayesian survival model with a classical SIR epidemic modeling framework. The fusion of the two allowed us to coherently integrate multiple analyses of individual disease histories into a single analysis based on a simple parametric model. Using that model, we were able to estimate the reproduction numbers and the effective population sizes in each of the three major waves of the EVD epidemic while appropriately accounting for uncertainty due to heterogeneity, missingness, or censoring in the records of EVD patients. This Bayesian framework also allowed us to incorporate external information through informative prior distributions and to provide exact inferences for incidence and intervention effects — the information most relevant to policy makers and public health officials.

Through our study, we estimated the epidemic effective population size (the overall number of individuals at immediate risk of infection) to be around 16,000. This number is much smaller than the demography-based estimate of the susceptible population that one would usually consider in a standard epidemic model. Indeed, the combined population of North Kivu, South Kivu, and Ituri provinces exceeds 16 million and accounts for approximately 15% of the DRC population, with many large population centers (e.g., Goma) exceeding half a million inhabitants. This discrepancy between demographic estimates and the estimated effective size of the susceptible population emphasizes the individual-based nature of our analysis and reflects the effects of public health intervention efforts (in particular, ring vaccination and contact tracing) that largely prevented the wide and uncontrolled community spread of the EVD.

Our analysis also indicated that, in different epidemic waves, the average removal time was statistically different with the shortening of the removal time from wave 1 to wave 3 by an average of 1.4 days (from 6 days in wave 1 to 4.6 days in wave 3). This finding is consistent with the general view that increased isolation and vaccination efforts in late 2019 largely contributed to breaking local chains of transmission and ultimately ending the epidemic by mid-2020. Assuming similar infectivity in future outbreaks, our results suggest that, in order to limit the spread of EVD in future outbreaks, a rate of removal similar to that achieved in wave 3 will likely be required.

Although the DRC has successfully contained Ebola outbreaks in the past [6, 29] and an effective vaccine is now available, the security and political challenges in the northern DRC — especially North Kivu and Ituru provinces — continued to create problems for effective public health interventions during the 2018-2020 outbreak. As political challenges in the DRC are likely to persist in the near future, there is great need for a flexible approach in responding to future outbreaks that combines multiple pharmaceutical and non-pharmaceutical strategies. The individual-level EVD data from the 2018-2020 outbreak presented here is, to our knowledge, the first opportunity to comprehensively look at the multi-wave outbreak data and quantitatively assess the strength of non-pharmaceutical interventions while also accounting for the the effects of ring vaccination in decreasing the size of the population at risk of infection. The methodology developed and used here is also of possible relevance for analyzing other outbreaks exhibiting complicated dynamics and multiple incidence waves, including the current COVID-19 pandemic.

Author Contributions

GAR, EK and PA designed the research. HV and PA collected and analyzed the data, YP helped visualize the data, WK, EK and GAR developed the Bayesian dynamical survival methodology. HV and GAR wrote the manuscript. All authors have contributed to manuscript editing and approved its final version.

Data Availability

Deidentified dataset and the code used in MCMC analysis are publicly available via Zenodo platform at https://doi.org/10.5281/zenodo.6104188. Further data may be available upon a reasonable request to the authors.

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Conflicts of Interest

The authors declare no conflicts of interest.

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Supplementary Material: Analysis of Individual-level Data from 2018-2020 Ebola Outbreak in Democratic Republic of the Congo

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A Additional Figures



Figure A.1: Weekly Case Count in DRC. Left: Proportion of cases, aggregated by week, for each of the six most outbreak-affected health zones: Beni, Butembo, Kalunguta, Katwa, Mabalako, Mandima (top to bottom in legend). Right: temporal and spatial distribution of the DRC cases. For full animation, see https://github.com/wasiur/DSAofEbola/blob/main/drc_animate_final5.gif. The animated map was created using open software R [17] with geospatial data obtained from [18].



Figure A.2: **Daily Incidence and Removal Rates** The model fit versus actual daily data on cases incidence (onset) and removal. As described in Section 2.3, the analysis was conducted for each wave separately, leading to different sets of parameter values. To facilitate the comparison with Figure 3 the results are plotted as relative counts (density functions).

B Derivations for DSA Model

The idea of dynamic survival analysis (DSA) is to derive individual-level independent Markov processes such that their aggregation leads to the desired ecological models, see [III] and also more recently [31, 32]. In case of the SIR model, equation [1]) describes for each individual member of the population their probabilities of being in the susceptible (S), infected (I), or recovered (R) state. This can be done by interpreting the rescaled proportions s_t , ι_t , and r_t as the respective state probabilities whose evolution is described by the stochastic master equation [25] given by equation (1) with a random initial condition.

As pointed out in [10], an alternative way of deriving the DSA-based individual infection model from (1) follows from the so-called *Sellke construction* (see, e.g., [33] chapter 2.2) that can be viewed as an agent-based description of the classical, Markovian SIR model of an epidemic. According to the construction, in the population of *m* initially susceptible individuals, with additional I_0 initially infected, the probability that a randomly selected initially susceptible individual remains susceptible at time t > 0is given by the expression

$$S_t = e^{-\frac{\beta}{m} \int_0^t I_u \, du} \tag{B.1}$$

where I_u is the total number of infected at time u. For the Markovian model, i.e., when infectious period is exponentially distributed with rate parameter γ , the quantity I_u/m converges in probability to the deterministic function ι_u which satisfies (1) (see, e.g., [33] chapter 5.3). Therefore, as the approximation of (B.1) we may take

$$s_t = e^{-\beta \int_0^t \iota_u du} = e^{-\mathcal{R}_0 r_t} \tag{B.2}$$

where (s_t, ι_t, r_t) is the solution of (1). As shown in 10 it follows from the law of large numbers for Poisson

processes that s_t converges to S_t as $m \to \infty$ uniformly in probability over any finite interval [0, T]. The DSA interpretation of the SIR model leads to the derivation of the individual-level likelihood function as follows.

Likelihood. We assume that observations of new infections and recoveries are available up to some time horizon T such that $T \in [0, \infty]$. Denote

$$\tau_T = 1 - s_T. \tag{B.3}$$

Note that τ_T is non-decreasing in T and that $\tau_{\infty} = \tau < 1$, the final epidemic size. In view of (B.2) the quantity $(s_t + \tau_T - 1)/\tau_T$ may be readily interpreted as the statistical survival function [30] on [0, T]. It follows that $-\dot{s}_t/\tau_T$ may be interpreted as a density function of infection times on [0, T] for any $T \leq \infty$. Recalling that under the DSA Markov assumption the infectious period is exponentially distributed with rate parameter γ we obtain the following individual-level likelihood function for an initially susceptible individual *i* observed until time *T* with infection and recovery times t_i and T_i , respectively:

$$\mathcal{L}(\theta|t_i, T_i, T) = (-\tau_T)^{-1} \dot{s}_{t_i} \gamma^{w_i} e^{-\gamma(T_i \wedge T - t_i)}.$$
(B.4)

Here, w_i is the event indicator satisfying $w_i = 0$ if $T_i \wedge T = T$ and $w_i = 1$ otherwise. The likelihood for the set of n individuals in the population with complete records (3) is simply the product of the individual likelihoods, reflecting the assumption that the infection events are approximately independent in a large population.

Likelihood with missing data. As discussed in the main body of the paper, in about 30% of the DRC Ebola cases the individual disease records were incomplete, missing either infection (t_i) or recovery (T_i) times. Fortunately, such missingness may be handled by the DSA likelihood without any need for data imputation. In case when only t_i is observed, $(T_i \text{ is missing})$, the likelihood (B.4) reduces simply to

$$\mathcal{L}(\theta|t_i, \circ, T) = (-\tau_T)^{-1} \dot{s}_{t_i}.$$
(B.5)

On the other hand, if only T_i is observed (t_i is missing), the likelihood is obtained from the convolution formula and (1)

$$\mathcal{L}(\theta|\circ, T_i, T) = (-\tau_T)^{-1} \int_0^{T_i} \dot{s}_u \gamma e^{-\gamma(T_i - u)} du = \frac{\gamma}{\tau_T} (\iota_{T_i} - \rho e^{-\gamma T_i}).$$
(B.6)

Similarly as above, the likelihood for incomplete data (4) is obtained by taking product of (B.5) and (B.6) over all individual incomplete histories.

Effective population size and outbreak size. Since only infections and recoveries are recorded are recorded during a typical epidemic, it is often difficult to determine the size (N) of the susceptible population at risk of infection. This is known in the literature as the problem of estimating N the effective population size [10]. Under the DSA interpretation of the SIR model, this estimate may be obtained as

$$\hat{N} = \frac{k_T}{\tau_T},\tag{B.7}$$

where k_T is the count of observed infected over the time horizon T and τ_T is given by (B.3). Similarly, one may also estimate the final epidemic count K_{∞} of all already observed and future infections by

$$\hat{K}_{\infty} = \hat{N}\tau, \tag{B.8}$$

where $\tau = \lim_{T \to \infty} \tau_T$ is the final epidemic size.

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