

# Combining morphological and biomechanical factors for optimal carotid plaque progression prediction: An MRI-based follow-up study using 3D thin-layer models

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## ABSTRACT

Plaque progression prediction is of fundamental significance to cardiovascular research and disease diagnosis, prevention, and treatment. Magnetic resonance image (MRI) data of carotid atherosclerotic plaques were acquired from 20 patients with consent obtained. 3D thin-layer models were constructed to calculate plaque stress and strain. Data for ten morphological and biomechanical risk factors were extracted for analysis. Wall thickness increase (WTI), plaque burden increase (PBI) and plaque area increase (PAI) were chosen as three measures for plaque progression. Generalized linear mixed models (GLMM) with 5-fold cross-validation strategy were used to calculate prediction accuracy and identify optimal predictor. The optimal predictor for PBI was the combination of lumen area (LA), plaque area (PA), lipid percent (LP), wall thickness (WT), maximum plaque wall stress (MPWS) and maximum plaque wall strain (MPWSn) with prediction accuracy = 1.4146 (area under the receiver operating characteristic curve (AUC) value is 0.7158), while PA, plaque burden (PB), WT, LP, minimum cap thickness, MPWS and MPWSn was the best for WTI (accuracy = 1.3140, AUC = 0.6552), and a combination of PA, PB, WT, MPWS, MPWSn and average plaque wall strain (APWSn) was the best for PAI with prediction accuracy = 1.3025 (AUC = 0.6657). The combinational predictors improved prediction accuracy by 9.95%, 4.01% and 1.96% over the best single predictors for PAI, PBI and WTI (AUC values improved by 9.78%, 9.45%, and 2.14%), respectively. This suggests that combining both morphological and biomechanical risk factors could lead to better patient screening strategies.

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**Abbreviations:** AUC, Area under of the ROC curve; APWSn, Average plaque wall strain; APWS, Average plaque wall stress; ECA, External carotid artery; GLMM, Generalized linear mixed models; ICA, Internal carotid artery; LP, Lipid percent; LA, Lumen area; MRI, Magnetic resonance image; MPWSn, Maximum plaque wall strain; MPWS, Maximum plaque wall stress; MinCT, Minimum cap thickness; PA, Plaque area; PAI, Plaque area increase; PB, Plaque burden; PBI, Plaque burden increase; PWSn, Plaque wall strain; PWS, Plaque wall stress; ROC curve, Receiver operating characteristic curve; WT, Wall thickness; WTI, Wall thickness increase.

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## 1. Introduction

Cardiovascular diseases are the major cause of unnatural death in the world [1]. Most major cardiovascular clinical events such as heart attack and stroke are linked closely to atherosclerotic vulnerable plaque progression and rupture [2]. Clinical guidelines recommend carotid endarterectomy (CEA) for patients with 60–99% diameter asymptomatic carotid stenosis (ACS) with low perioperative risk [3–5]. However, the average annual risk of any territory stroke in these asymptomatic patients is ≤1.6% [6–9]. Up to 98% of all CEA and carotid artery stenting procedures in asymptomatic patients in the United States (US) may be unnecessary, generating needless healthcare costs of \$2 billion annually [7,10]. On the other hand, in a survey of 2226 symptomatic subjects, 61% of the subjects had carotid artery stenosis <50% [11]. It is necessary that methods to predict plaque progression and rupture are developed so

that appropriate treatment methods could be applied in time to prevent actual drastic clinical events from happening.

The progression and rupture of atherosclerotic plaques involve complex processes including biology, biochemistry, biomechanics and pathology, etc. [12–16]. Some research teams have made great effort to explore possible indicators to predict the plaque development with in vivo images. Stone GW et al. showed that nonculprit lesions associated with recurrent events were more likely than those not associated with recurrent events to be characterized by a plaque burden of 70% or greater, or a minimal luminal area of 4.0 mm<sup>2</sup> or less, or to be classified on the basis of radiofrequency intravascular ultrasonography as thin-cap fibroatheromas [17]. Based on in vivo magnetic resonance imaging (MRI) data, Cai et al. introduced a human carotid plaques classification system [18]. Image-based computational plaque models were introduced and used by several groups to investigate associations between biomechanical risk factors and plaque development behaviors [19–26] and to assess clinical significance [27–30]. It was reported that plaque wall stress (PWS) was associated to plaque progression [14,19,31,32]. Direct associations between flow shear stress and advanced carotid plaques were found [33]. Some groups combined biomechanical and morphological risk factors to assess plaque vulnerability for carotid and coronary arteries [28,34–38].

We hypothesized that combining morphological and biomechanical factors would lead to better prediction results of plaque progression. In this paper, MRI data of carotid atherosclerotic plaques were acquired from 20 patients with consent obtained and 3D thin-layer models were constructed to obtain 10 morphological and mechanical risk factor values for analysis. The 10 factors included wall thickness (WT), lipid percent (LP), minimum cap thickness (MinCT), plaque area (PA), plaque burden (PB), lumen area (LA), maximum plaque wall stress (MPWS), maximum plaque wall strain (MPWSn), average plaque wall stress (APWS), and average plaque wall strain (APWSn). Wall thickness increase (WTI), plaque burden increase (PBI) and plaque area increase (PAI) were chosen as three measures for plaque progression. Generalized linear mixed models (GLMM) with 5-fold cross-validation strategy were used to calculate prediction accuracy for each predictor and identify the optimal predictor. Details are given below.

## 2. Methods

### 2.1. MR images acquisition and data processing

MRI sequence data of carotid plaques from 20 patients (all male; age: 58–84, mean = 72.8) were acquired with consent obtained at the University of Washington (UW), Seattle by the Vascular Imaging Laboratory (VIL) using protocols approved by the UW Institutional Review Board. For each patient, carotid bifurcation position and plaque characteristics (lipid core, calcifications, etc.) were used to match the MRI slices at baseline time and follow-up time (marked as T1 and T2, scan time intervals: 18 months). Slice distance was kept the same at both scans. The axial distance between the non-bifurcation slice position and the bifurcation position slice was used to match the MRI slices from baseline time and follow-up time. For each slice, the geometries (mainly the centroid of their lumen) of external carotid artery (ECA) and internal carotid artery (ICA) were used to match ICA slices circumferentially at baseline and follow-up. Patient-specific cuff systolic and diastolic arm pressures were collected and used for plaque mechanical model. The procedures of data acquisition and image segmentation are detailed in our previous published articles and are omitted here [39]. Fig. 1 gave one example of matched MR images and the corresponding image segmentation contour plots at baseline and follow-up.

### 2.2. Computational models and solution methods

A 3D thin-layer modeling approach was used to obtain plaque stress and strain conditions. For every slice, 3D thin-layer model was made by adding a slice thickness of 0.5 mm [38]. The pre-shrink-stretch process was used on the construction of 3D thin-layer model and the component-fitting mesh generation technique were used the same as it was done in regular 3D full vessel models [33]. The hyperelastic, homogeneous, incompressible, isotropic vascular hypothesis was adopted for carotid artery [38]. The nonlinear modified Mooney-Rivlin (M-R) model was selected as the material model for carotid vessel and plaque components [40]. The strain energy function of modified M-R model was given by:

$$W = c_1(I_1 - 3) + c_2(I_2 - 3) + D_1[\exp(D_2(I_1 - 3)) - 1] \quad (1)$$

$$I_1 = \sum C_{ij}, I_2 = 0.5(I_1^2 - C_{ij}C_{ji}), i, j = 1, 2, 3 \quad (2)$$

where  $\mathbf{C} = [C_{ij}] = \mathbf{X}^T \mathbf{X}$  is the right Cauchy-Green deformation tensor.  $I_1$  is the first strain invariant and  $I_2$  is the second strain invariants of  $\mathbf{C}$ ,  $\mathbf{X} = [X_{ij}] = [\partial x_i / \partial a_j]$ , where  $a_j$  is the original location and  $x_i$  is the current location. The values of  $c_1$ ,  $c_2$ ,  $D_1$ , and  $D_2$  constitute the material parameter set. M-R model was chosen because it could be consistent with the carotid vessel material properties measured by uniaxial and biaxial mechanical testing data [41]. The following material parameters were used in our models on the current literature and our own previous publications [39,41]: vessel and fibrous cap:  $c_1 = 36.8$  kPa,  $D_1 = 14.4$  kPa,  $D_2 = 2$ ; lipid core/hemorrhage:  $c_1 = 2$  kPa,  $D_1 = 2$  kPa,  $D_2 = 1.5$ ; loose matrix:  $c_1 = 18.4$  kPa,  $D_1 = 7.2$  kPa;  $D_2 = 1.5$ ; calcification:  $c_1 = 368$  kPa,  $D_1 = 144$  kPa,  $D_2 = 2.0$ .  $c_2 = 0$  for all materials. The patient-specific 3D thin-layer models were solved by ADINA (Adina R & D, Watertown, MA) following procedures in [40].

### 2.3. Morphological and biomechanical risk factors

Two hundred and one (201) matched slices from 20 patients were usable for our study. For each matched slice, 100 evenly-spaced points from the lumen were selected and values of the 10 morphological and biomechanical risk factors were obtained for statistical analysis. Each slice was divided into 4 quarters with each quarter containing 25 evenly-spaced nodal points on the lumen, each lumen nodal point was connected to a corresponding point on vessel outer-boundary using a Piecewise Equal-Step method to deal with irregular non-circular plaque morphologies (see Fig. 2) [26]. The wall thickness (WT) was defined as the distance between each nodal point on the lumen and corresponding point on the out-boundary. Cap thickness was defined as the length of the line connecting the lipid point and lumen point (use wall thickness if there is no lipid core in the slice). The minimum cap thickness (MinCT) is the minimum value of cap thickness of a slice. Fig. 2 shows the definitions of these morphological features. Lumen area (LA) is the area inside the lumen contour. Plaque area (PA) is the area bounded by the lumen contour and out-boundary. The area of a lipid core was defined as lipid area. Plaque burden (PB) and lipid percent (LP) was defined by:

$$PB = PA / (PA + LA) \quad (3)$$

$$LP = \text{Lipid Area} / PA \quad (4)$$

The maximum principal stress and strain were defined as plaque wall stress (PWS) and strain (PWSn) at 100 nodal points on the lumen. Maximum plaque wall stress (MPWS) was the maximum value of PWS among 100 nodal points on the lumen. Average plaque wall stress (APWS) was the mean value of PWS at 100 nodal points on the lumen. Maximum plaque wall strain (MPWSn) and average plaque wall strain (APWSn) have similar definitions to MPWS and APWS of each slice.

### 2.4. Measurement of plaque progression

Vessel plaque burden increase (PBI), plaque area increase (PAI) and wall thickness increase (WTI) from baseline to follow-up were three commonly used measures and defined by:

$$WTI = WT_{\text{follow-up}} - WT_{\text{baseline}} \quad (5)$$

$$PBI = PB_{\text{follow-up}} - PB_{\text{baseline}} \quad (6)$$

$$PAI = PA_{\text{follow-up}} - PA_{\text{baseline}} \quad (7)$$

### 2.5. Prediction model and strategy

Generalized linear mixed models (GLMM) were used as the prediction model. The binary responses for the measures of plaque progression (PBI, PAI, or WTI) were adopted to find the best predictor(s) [37]. PBI was taken as an example to illustrate the training and testing process of our GLMM model. The same process was also applied to WTI and PAI. For a selected slice, we set  $PBI = 1$  if  $PBI > 0$  or  $PBI = 0$  if  $PBI \leq 0$ . The GLMM model is defined as [37,42]:

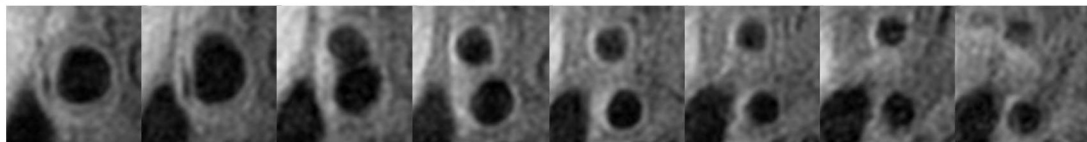
$$y_{ij} = E(y_{ij}|b_j) + \varepsilon_{ij} \quad (8)$$

$$\text{logit}(E(y_{ij}|b_j)) = \beta_0 + \beta_1 x_{1ij} + \beta_2 x_{2ij} + \dots + b_j \quad (9)$$

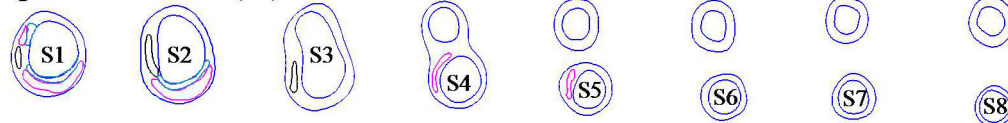
where  $y_{ij}$  is the binary response of PBI and  $E(y_{ij}|b_j) = P(y_{ij} = 1|b_j)$  is the probability on the  $i$ th slice of the  $j$ th patient.  $\text{logit}(x) = \log(x/(1-x))$  is the binomial link function.  $x_{1ij}$ ,  $x_{2ij}$ , etc. are the risk factors, which were used to predict plaque progression.  $\beta_0$ ,  $\beta_1$ , etc. are the fixed-effect coefficients,  $b_j$  and  $\varepsilon_{ij}$  are the random effect terms and the random error terms of GLMM. R function glmmPQL was used to estimate the term values by fitting GLMM [43].

A 5-fold cross-validation strategy was adopted to calculate prediction accuracy for each single predictor and identify the optimal predictor [37]. All 201 MRI slices

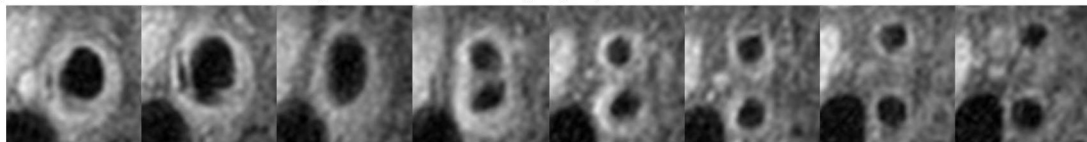
## (a) In Vivo MR Images from baseline (T1)



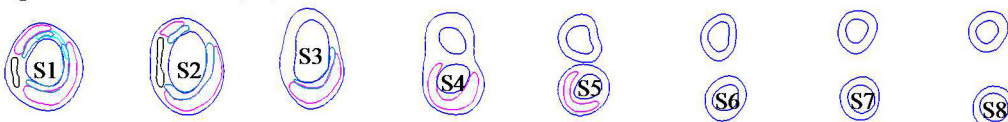
## (b) Segmented contours (T1)



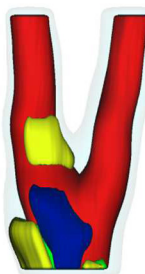
## (c) Matched In Vivo MR Images from follow-up (T2)



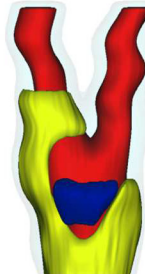
## (d) Segmented contours (T2)



## (e) 3D Geometry, Time 1 (T1)



## (f) 3D Geometry, Time 2 (T2)



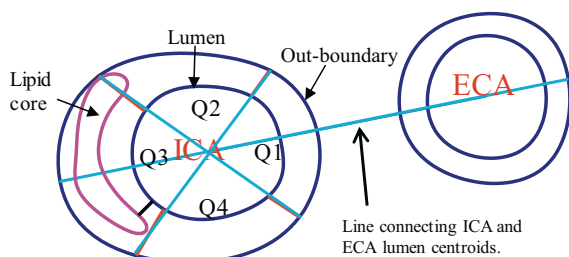
Core(magenta),  
Loose Matrix (cyan),  
Calcification(black)  
Fibrous( in dark cyan)

**Fig. 1.** Matched MR images and segmented contour plots of sliced from baseline scan and follow-up scan. (a) 8 in vivo MR images from baseline; (b) segmented contours for 8 MRI slices from baseline; (c) matched 8 in vivo MR images from follow-up; (d) segmented contours for 8 MRI slices from baseline; (e) 3D plaque geometry from baseline (Yellow: lipid; blue: calcification; light blue: outer wall; red: lumen.); (f) 3D plaque geometry from follow-up (Yellow: lipid; blue: calcification; light blue: outer wall; red: lumen).

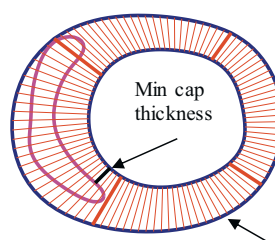
were randomly divided into 4 training subgroups and 1 verification subgroup. The training subgroups were used for model fitting, and the verification subgroup was used to estimate the model. Sensitivity is the probability of detecting a PBI = 1

slice in the PBI = 1 class of validation subgroup. Specificity is the probability of detecting a PBI = 0 slice in the PBI = 0 class of validation subgroup. All combinations of 10 risk factors were feed to GLMM and the prediction accuracy of each predictor

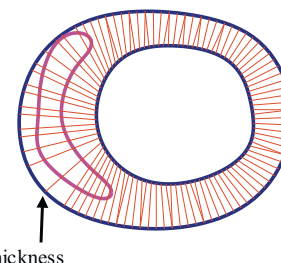
## (a) Sketch of the Quarter-Dividing Method.



## (b) Piecewise Equal-Step Method



## (c) Shortest Distance Method



**Fig. 2.** Schematic drawing demonstrating the Piecewise Equal-Step method for vessel wall thickness and the quarter-dividing method. (a) Sketch of the quarter-dividing method. A line connecting the centroids of ICA and ECA lumen area was determined first. Then Q1 was determined so that the intersection of the lumen and the centerline was chosen as a data point and Q1 contains 12 data points on each side of the center line; (b) Piecewise equal-step method; (c) Shortest distance method: for every selected data point on lumen, a point on the out-boundary with the shortest distance was chosen as the matching point. This method leads to un-even representation of the out-boundary. Colour used: magenta: lipid; blue: outer wall and lumen; red: wall thickness; black: Min cap thickness.

**Table 1**

Prediction sensitivity and specificity, AUC value of PBI, PAI and WTI using one single risk factor and optimal predictor among all combinations.

| Predictor                               | ProbCutoffs | Sensitivity | Specificity | Sensi<br>+<br>Speci | AUC    |
|-----------------------------------------|-------------|-------------|-------------|---------------------|--------|
| Prediction results for PBI              |             |             |             |                     |        |
| LA + PA + LP + WT + MPWS + MPWSn        | 0.6347      | 0.6984      | 0.7162      | 1.4146              | 0.7158 |
| LA                                      | 0.6297      | 0.7183      | 0.6419      | 1.3601              | 0.6540 |
| APWSn                                   | 0.6243      | 0.6944      | 0.6419      | 1.3363              | 0.6342 |
| MPWS                                    | 0.6355      | 0.6905      | 0.6419      | 1.3324              | 0.6576 |
| PB                                      | 0.5921      | 0.7222      | 0.5685      | 1.2907              | 0.6362 |
| LP                                      | 0.6547      | 0.6000      | 0.5850      | 1.1850              | 0.5867 |
| MinCT                                   | 0.6987      | 0.502       | 0.6419      | 1.1439              | 0.5724 |
| MPWSn                                   | 0.6102      | 0.6255      | 0.5170      | 1.1425              | 0.5568 |
| WT                                      | 0.4873      | 0.7952      | 0.2500      | 1.0452              | 0.4763 |
| APWS                                    | 0.7219      | 0.3400      | 0.6875      | 1.0275              | 0.4936 |
| PA                                      | 0.7287      | 0.3855      | 0.6370      | 1.0225              | 0.4736 |
| Prediction results for PAI              |             |             |             |                     |        |
| PA + PB + WT + MPWS + MPWSn + APWSn     | 0.4570      | 0.7917      | 0.5109      | 1.3025              | 0.6657 |
| LA                                      | 0.5811      | 0.4907      | 0.6940      | 1.1846              | 0.6064 |
| MPWSn                                   | 0.3907      | 0.8920      | 0.2912      | 1.1832              | 0.6084 |
| PA                                      | 0.6608      | 0.2710      | 0.8611      | 1.1321              | 0.5813 |
| APWS                                    | 0.4730      | 0.7383      | 0.3859      | 1.1242              | 0.5628 |
| MinCT                                   | 0.3721      | 0.9202      | 0.2099      | 1.1301              | 0.5546 |
| MPWS                                    | 0.6505      | 0.3081      | 0.8011      | 1.1092              | 0.5420 |
| APWSn                                   | 0.5789      | 0.4512      | 0.6538      | 1.1050              | 0.5246 |
| WT                                      | 0.6558      | 0.2817      | 0.7845      | 1.0662              | 0.5019 |
| PB                                      | 0.7252      | 0.1596      | 0.9000      | 1.0596              | 0.5007 |
| LP                                      | 0.4741      | 0.6916      | 0.3497      | 1.0413              | 0.4960 |
| Prediction results for WTI              |             |             |             |                     |        |
| PA + PB + WT + LP + MinCT + MPWS + MPWS | 0.6481      | 0.6025      | 0.7115      | 1.3140              | 0.6552 |
| PA                                      | 0.5479      | 0.7951      | 0.4936      | 1.2887              | 0.6415 |
| WT                                      | 0.5691      | 0.7314      | 0.5226      | 1.2540              | 0.6097 |
| APWSn                                   | 0.5721      | 0.7107      | 0.5226      | 1.2333              | 0.6362 |
| MPWS                                    | 0.6367      | 0.5643      | 0.6581      | 1.2224              | 0.6163 |
| LA                                      | 0.6462      | 0.5226      | 0.6883      | 1.2109              | 0.6176 |
| LP                                      | 0.4679      | 0.7963      | 0.4076      | 1.2039              | 0.6275 |
| MinCT                                   | 0.5696      | 0.7190      | 0.4737      | 1.1927              | 0.5828 |
| PB                                      | 0.6047      | 0.6132      | 0.5613      | 1.1745              | 0.5896 |
| MPWS                                    | 0.6374      | 0.6175      | 0.5524      | 1.1700              | 0.5654 |
| APWS                                    | 0.6387      | 0.5169      | 0.5197      | 1.0367              | 0.4978 |

was selected from the point on the ROC (receiver operating characteristic) curve with the highest sum of specificity and sensitivity. The area under the ROC curve (AUC) was used to assess the predictive power of each predictor.

### 3. Results

#### 3.1. Combination of predictors for PBI improved AUC value by 9.45% over best single predictor

A total of 1023 ( $2^{10}-1$ ) combinations of 10 risk factors at baseline were selected to determine the optimal predictor with the highest prediction accuracy. Table 1 shows the results for PBI prediction using 10 single predictors and the optimal predictor. LA was the best single predictor for PBI with the highest prediction accuracy (1.3601), and the AUC is 0.6540, followed by APWSn (1.3363) with AUC = 0.6342. The combination of LA, PA, LP, WT, MPWS, and MPWSn (marked as LA + PA + LP + WT + MPWS + MPWSn) gave the best prediction accuracy (1.4146), with AUC = 0.7158. The combinational predictor improves the AUC by 9.45%, and 4.01% in prediction accuracy compared to those given by LA, the best single predictor. The ROC curve of optimal predictor LA + PA + LP + WT + MPWS + MPWSn are given in Supplement Fig. 3.

#### 3.2. The optimal combination of predictors for PAI prediction

Similar to the prediction process of PBI, Table 1 also summarizes the prediction results for PAI using single predictors and the optimal predictor at baseline. LA was once again the best single predictor for PAI with the highest prediction accuracy (1.1846) with AUC = 0.6064, followed by MPWSn (1.1832) with AUC = 0.6084. The combination of PA, PB, WT, MPWS, MPWSn and APWSn (marked as PA + PB + WT + MPWS + MPWSn + APWSn) gave the best prediction accuracy (1.3025), and the AUC value is 0.6657. The prediction accuracy values and AUC values for PAI were lower than those for PBI. The combinational predictor improves the AUC by 9.78%, and 9.95% in prediction accuracy compared to those given by LA, the best single predictor. The ROC curve of the optimal predictor PA + PB + WT + MPWS + MPWSn + APWSn are given in Supplement Fig. 4.

#### 3.3. The optimal combination of predictors for WTI prediction

Table 1 shows that PA was the best single predictor for WTI with highest prediction accuracy (1.2887) with AUC = 0.6415, followed by WT (1.2540), with AUC = 0.6097. The combination of PA, PB, WT, LP, MinCT, MPWS and MPWS (marked as PA + PB + WT + LP + MinCT + MPWS + MPWS) was the best predictor with prediction accuracy as 1.3140, with AUC = 0.6552. The combination predictor still had better prediction accuracy and AUC value over those given by best single predictor. Supplement Fig. 5 shows the ROC curve using the optimal predictor PA + PB + WT + LP + MinCT + MPWS + MPWS at baseline for predicting WTI.

### 4. Discussion

#### 4.1. Combining morphological and biomechanical risk factors for carotid plaque progression prediction

In the prediction of plaque progression, the combinational predictors improved prediction accuracy by 9.95%, 4.01% and 1.96% over the best single predictors for PAI, PBI and WTI, respectively. When using

**Table 2**

Correlation results between plaque progression (WTI) and the risk factors (PWS, PWSn, & WT) using 3D full vessel model and 3D thin-layer model at baseline (T1) and follow up (T2). ('+' means the correlation is consistent, '-' means the correlation is inconsistent).

| Slices      | Nodes | 3D full vessel |        | 3D thin-layer |        | Agreement |
|-------------|-------|----------------|--------|---------------|--------|-----------|
|             |       | r              | p      | r             | p      |           |
| WTI vs WT   |       |                |        |               |        |           |
| 1           | 100   | −0.5286        | 0.0000 | −0.5424       | 0.0000 | +         |
| 2           | 100   | −0.7280        | 0.0000 | −0.7152       | 0.0000 | +         |
| 3           | 100   | −0.7942        | 0.0000 | −0.7946       | 0.0000 | +         |
| 4           | 100   | −0.2285        | 0.0215 | −0.2221       | 0.0256 | +         |
| 5           | 100   | −0.5171        | 0.0000 | −0.6203       | 0.0000 | +         |
| 9           | 100   | −0.1936        | 0.0524 | −0.1755       | 0.0792 | +         |
| 10          | 100   | 0.6105         | 0.0000 | 0.6792        | 0.0000 | +         |
| WTI vs PWS  |       |                |        |               |        |           |
| 1           | 100   | 0.8018         | 0.0000 | 0.8114        | 0.0000 | +         |
| 2           | 100   | 0.9112         | 0.0000 | 0.8578        | 0.0000 | +         |
| 3           | 100   | 0.4548         | 0.0000 | 0.6300        | 0.0000 | +         |
| 4           | 100   | −0.1664        | 0.0962 | −0.1090       | 0.2777 | +         |
| 5           | 100   | 0.0512         | 0.6113 | 0.2127        | 0.0327 | +         |
| 9           | 100   | 0.3242         | 0.0009 | −0.0871       | 0.3862 | −         |
| 10          | 100   | 0.2895         | 0.0033 | 0.0965        | 0.3372 | +         |
| WTI vs PWSn |       |                |        |               |        |           |
| 1           | 100   | 0.7676         | 0.0000 | 0.7890        | 0.0000 | +         |
| 2           | 100   | 0.9514         | 0.0000 | 0.8802        | 0.0000 | +         |
| 3           | 100   | 0.3323         | 0.0007 | 0.6208        | 0.0000 | +         |
| 4           | 100   | −0.2303        | 0.0205 | −0.1763       | 0.0779 | +         |
| 5           | 100   | 0.1280         | 0.2020 | 0.2160        | 0.0300 | +         |
| 9           | 100   | 0.4063         | 0.0000 | −0.1779       | 0.0750 | −         |
| 10          | 100   | 0.0807         | 0.4222 | 0.0026        | 0.9792 | +         |



the single morphological or biomechanical risk factor as the predictor, PA was the best single predictor for WTI, LA was the best single predictor for PBI and PAI. The single risk factor prediction AUC values were around 50%–60% and had little clinical significance which is consistent with the current literature [11]. Combinational predictors improved prediction AUC values to near 70% (71.58%, 66.57% and 65.52% for PBI, PAI and WTI, respectively). Those represented 9.45%, 9.78%, and 2.14% improvements in AUC values over those given by the best single predictors.

#### 4.2. PBI is more predictable measure for carotid plaque progression than WTI and PAI

PB, PA and WT are three commonly used indicators, which are often used to measure atherosclerotic plaque in human carotid and coronary artery. WTI, PBI and PAI were used to evaluate plaque progression and compare their differences. Our results show that PBI was a more predictable measure for carotid plaque progression than WTI and PAI with 10 risk factors as predictive indicators. And the combinations of LA, PA, LP, WT, MPWS and MPWSn was the best predictor with prediction accuracy 1.4146 and AUC value 0.7158. The values of sensitivity and specificity were 0.6984 and 0.7162, indicating that the predictor can better predict PB changes. No matter how the plaque size changed, at least 71% of the slices could get the correct consistency between the prediction of the plaque size change and the actual plaque size change. For the other two plaque progression measurements, the optimal prediction accuracy of WTI and PAI can only reach 1.314 and 1.3025. This suggests that we may want to use PBI to measure plaque progression in future studies.

#### 4.3. 3D thin-layer model are consistent with the 3D full vessel model correlation results

3D full vessel computational models are certainly desirable for plaque stress and strain calculations. However, 3D full vessel model construction is time consuming. 3D thin-layer modeling method was used in this paper as an approximation to full 3D models since the thin-layer model requires much less computational cost and human labor than 3D full vessel models. 3D axial stretch was still included in 3D thin-layer models, which is similar to the procedures of 3D full vessel model. That made 3D thin-layer model much better approximation to 3D full vessel model than the simple 2D models. Correlation results given in Table 2 show that results from 3D thin-layer models were consistent with those from 3D full vessel models. The agreement rate was as high as 90.48% (19 from 21, detailed in Table 2). Therefore, considering the modeling time (1 or 2 weeks) cost of 3D full vessel model, 3D thin-layer models may be used to replace 3D full vessel models to perform mechanical analysis for possible clinical implementation.

#### 4.4. Limitations

MR has a limited imaging resolution, and the thin plaque cap cannot be detected. In this study, patient-specific vessel and plaque component material properties data were lacking and unavailable. The parameter values in the material models were selected from our previous literature [24]. Acquisition of intravascular pressure data with a noninvasive manner is still a challenge. Furthermore, larger patient size studies are necessary to further improve and validate our results. Lastly, due to potential collinearity among the predictors, generalizing the prediction accuracies to a broader population requires the assumption that the collinearity patterns remain unchanged. This assumption is to be further studied upon more data are available.

## 5. Conclusion

In this study, 10 morphological and biomechanical risk factors at baseline were used to predict plaque progression. The prediction results of plaque progression supported our hypothesis that the predictor combining morphology and biomechanics risk factors was more accurate than any single risk factor. 3D thin-layer models showed good agreement with 3D full vessel models.

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## Conflict of interest

None.

## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.ijcard.2019.07.005>.

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