Impact of gas spin and Lyman–Werner flux on black hole seed formation in cosmological simulations: implications for direct collapse

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ABSTRACT
Direct collapse black holes (BHs) are promising candidates for producing massive $z \gtrsim 6$ quasars, but their formation requires fine-tuned conditions. In this work, we use cosmological zoom simulations to study systematically the impact of requiring: (1) low gas angular momentum (spin), and (2) a minimum incident Lyman–Werner (LW) flux in order to form BH seeds. We probe the formation of seeds (with initial masses of $M_{\rm seed} \sim 10^4$–$10^6\,{\rm M_\odot}\,h^{-1}$) in haloes with a total mass $>3000 \times M_{\rm seed}$ and a dense, metal-poor gas mass $>5 \times M_{\rm seed}$. Within this framework, we find that the seed-forming haloes have a prior history of star formation and metal enrichment, but they also contain pockets of dense, metal-poor gas. When seeding is further restricted to haloes with low gas spins, the number of seeds formed is suppressed by factors of ~ 6 compared to the baseline model, regardless of the seed mass. Seed formation is much more strongly impacted if the dense, metal-poor gas is required to have a critical LW flux ($J_{\rm crit}$). Even for $J_{\rm crit}$ values as low as $50 J_{21}$, no $8 \times 10^5\,{\rm M_\odot}\,h^{-1}$ seeds are formed. While lower mass (1.25×10^4, $1 \times 10^5\,{\rm M_\odot}\,h^{-1}$) seeds do form, they are strongly suppressed (by factors of ~ 10–100) compared to the baseline model at gas mass resolutions of $\sim 10^4\,{\rm M_\odot}\,h^{-1}$ (with even stronger suppression at higher resolutions). As a result, BH merger rates are also similarly suppressed. Since early BH growth is dominated by mergers in our models, none of the seeds are able to grow to the supermassive regime ($\gtrsim 10^6\,{\rm M_\odot}\,h^{-1}$) by $z = 7$. Our results hint that producing the bulk of the $z \gtrsim 6$ supermassive BH population may require alternate seeding scenarios that do not depend on the LW flux, early BH growth dominated by rapid or super-Eddington accretion, or a combination of these possibilities.

Key words: black hole physics – galaxies: high-redshift – galaxies: nuclei.

1 INTRODUCTION

Supermassive black holes (SMBHs) are now believed to be central components of galaxy formation and evolution. Almost every massive galaxy in the local Universe harbours a SMBH (Kormendy & Richstone 1992; Harms et al. 1994; Miyoshi et al. 1995). Evidence for SMBHs is also seen at higher redshifts ($z \gtrsim 1$), where they are primarily observed as active galactic nuclei (AGN). The most luminous AGN (also known as quasars) have now been observed to redshifts of $z \sim 7.5$ (Fan et al. 2001; Mortlock et al. 2011; Wu et al. 2015; Bañados et al. 2018). However, these quasars likely represent a very tiny and highly biased portion of the underlying SMBH population at $z \gtrsim 7$; this population is going to be unveiled by upcoming facilities such as *James Webb Space Telescope* (*JWST*; Gardner et al. 2006), the *Nancy Graham Roman Space telescope* (*NGRST*, formerly *WFIRST*; Spergel et al. 2015), the Lynx X-ray Observatory (The Lynx Team 2018), and the Laser Interferometer

Space Antenna (LISA; Baker et al. 2019). The overall $z \gtrsim 7$ SMBH population (including the observed brightest quasars) potentially contains imprints of the earliest seeds of SMBHs, which is currently a major theoretical gap in contemporary galaxy formation models.

A popular candidate for SMBH seeds is the remnant of a first generation (Population III or Pop III) star (e.g. Madau & Rees 2001; Bromm, Coppi & Larson 2002; Volonteri, Madau & Haardt 2003; Banik, Tan & Monaco 2018; Smith et al. 2018; see also review by Inayoshi, Visbal & Haiman 2020 and references therein). This is a very promising channel for potentially explaining a substantial fraction of SMBHs, largely because they almost certainly exist as an inevitable consequence of the collapse of such massive stars (~ 10–$1000\,{\rm M_\odot}$). Seeds formed via this channel are predicted to have masses $\sim 100\,{\rm M_\odot}$ (Fryer, Woosley & Heger 2001). However, the inferred masses of the $z > 7$ quasars ($\sim 10^9\,{\rm M_\odot}\,h^{-1}$) pose a huge challenge to Pop III seeds, since they require sustained accretion of gas at the Eddington limit to grow by ~ 7 orders of magnitude by $z \sim 7$. Alternatively, a higher initial seed mass ($\sim 10^4$–$10^6\,{\rm M_\odot}\,h^{-1}$) makes it substantially easier for black hole (BH) seeds to grow to $\gtrsim 10^9\,{\rm M_\odot}\,h^{-1}$ by $z \sim 7$. For this reason, BHs formed from direct

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collapse of pristine gas (also known as 'direct collapse black holes' or 'DCBHs') have become popular candidates for $z > 7$ quasar progenitors, particularly because this channel can potentially form very massive seeds within $\sim 10^4$–10^6 M$_\odot$ h^{-1} (e.g. Bromm & Loeb 2003; Begelman, Volonteri & Rees 2006; Regan, Johansson & Wise 2014; Latif, Schleicher & Hartwig 2016; Becerra et al. 2018; Luo et al. 2018; Wise et al. 2019; Luo et al. 2020).

In order to form $\sim 10^4$–10^6 M$_\odot$ h^{-1} DCBHs, gas needs to undergo a nearly isothermal collapse at temperatures $\gtrsim 10^4$ K. Additionally, large inflow rates ($\gtrsim 0.1$ M$_\odot$yr^{-1} at a few tens of pc scales sustained for $\sim$10 Myr) are needed to form a massive compact object (e.g. Begelman 2010; Hosokawa, Omukai & Yorke 2012; Hosokawa et al. 2013; Schleicher et al. 2013; Regan et al. 2020a; Haemmerlé et al. 2021). To sustain the gas at $\gtrsim 10^4$ K and make it eventually collapse, metal-line cooling and molecular hydrogen cooling channels need to be suppressed until the host halo assembles at least enough mass to cross the virial temperature $T_{\rm vir} \sim 10^4$ K (known as the atomic cooling threshold, corresponding to halo masses $\sim 10^7$ M$_\odot$). Primordial gas is devoid of metals, so molecular hydrogen is the only agent that can cool below $\sim 10^4$ K and fragment the gas into forming the first generation of Pop III stars. Once star formation begins, subsequent stellar evolution will pollute the gas with metals, and that region will longer be able to form DCBHs.

Molecular hydrogen formation can be suppressed if the gas is exposed to a sufficient amount of UV radiation in the Lyman–Werner (LW) band (11.2–13.5 eV). The minimum amount of LW flux ($J_{\rm crit}$) required to suppress fragmentation depends crucially on the source radiation spectrum (Latif et al. 2014), self sheilding of H_2 (Wolcott-Green, Haiman & Bryan 2011), and the modelling of gas chemistry (Glover 2015). At the mini-halo stage, this could be achieved with low values of $J_{\rm crit} \sim 10^{-4}$–$1 J_{21}$ (where $J_{21} = 10^{-21}$erg s^{-1} cm^{-2} Hz^{-1} sr^{-1}) that can be supplied by the mean LW background (Visbal, Haiman & Bryan 2014). However, $J_{\rm crit}$ steeply increases with halo mass; by the time haloes cross the atomic cooling threshold, $J_{\rm crit}$ values are high enough that H_2 can only be dissociated if there is a nearby starburst of young Population II (Pop II) and Pop III stars. Estimated values of $J_{\rm crit}$ in this regime are typically $\gtrsim 1000 J_{21}$ based on radiation hydrodynamic simulations (Shang, Bryan & Haiman 2010) as well as one-zone chemistry models (Sugimura, Omukai & Inoue 2014; Wolcott-Green, Haiman & Bryan 2017). That being said, some recent works have also found that dynamical heating in haloes (triggered by periods of rapid growth) can significantly contribute to the suppression of cooling, thereby further decreasing $J_{\rm crit}$ to $\sim 3 J_{21}$ (Wise et al. 2019; Regan et al. 2020b).

Another potential impediment for DCBH formation is the angular momentum (spin) of the gas. In addition to the suppression of molecular hydrogen cooling, having low gas spin may also be necessary to achieve inflow rates $\gtrsim 0.1$ M$_\odot$yr^{-1}. In other words, haloes with high gas spin can provide rotational support to the pre-galactic gas disc and prevent the gas from achieving such high inflow rates.

While DCBHs are a promising alternative to alleviate the stringent growth time-scales of lower mass ($\lesssim 10^3$ M$_\odot$) seeds, the previous considerations make it clear that their formation requires a number of fairly restrictive conditions to be simultaneously satisfied. This raises a couple of broad questions: (1) How (un)common are DCBH-forming gas environments within a given large-scale structure? (2) What portion of the observable SMBH population originates from DCBH seeds?

Several aspects of these questions have been investigated in previous works; a vast majority of them use semi-empirical mod-

els (Lodato & Natarajan 2006, 2007; Dijkstra et al. 2008; Natarajan & Volonteri 2012; Dijkstra, Ferrara & Mesinger 2014; Ricarte & Natarajan 2018; DeGraf & Sijacki 2020). Lodato & Natarajan (2006) found that only ~ 5 per cent of dark matter haloes ($\sim 10^7$ M$_\odot$) have spins that are low enough to form DCBHs ($\sim 10^5$ M$_\odot$). Dijkstra et al. (2008) found that a very small fraction (10^{-8}–10^{-6}) of atomic cooling haloes have a close star-forming neighbour ($\lesssim 10$ kpc) that provides LW fluxes ($\gtrsim 10^3$ J_{21}) necessary to prevent fragmentation. Additionally, a halo may also need to be 'synchronized' with a nearby star-forming halo, i.e. both haloes need to cross the atomic cooling threshold within a few ~ 5 Myr apart from each other (Visbal et al. 2014; Regan et al. 2017; Lupi, Haiman & Volonteri 2021). Overall, these results indicate that DCBH formation sites may be rare. While they could potentially explain the rarest, brightest tip of the observed high-z SMBH population, accounting for the 'typical' (lower masses and luminosities, yet to be observed) SMBHs at these redshifts but may be a lot more difficult.

Recently, cosmological hydrodynamic simulations (see Vogelsberger et al. 2020, for a recent review) have been used to probe the large-scale structure for DCBH formation sites (Habouzit et al. 2016; Tremmel et al. 2017; Dunn et al. 2018; Luo et al. 2020; Chon, Hosokawa & Omukai 2021). While they are considerably more expensive than semi-empirical models, they have the unique advantage of being able to self-consistently track the dynamics of gas that is a crucial ingredient for governing seed formation. This makes them an ideal tool to systematically assess the importance of different seeding criteria on DCBH formation. For example, Habouzit et al. (2016, hereafter H16) studied the impact of varying $J_{\rm crit}$ using simulations spanning a wide range of volumes and resolutions. Dunn et al. (2018) performed a similar study, seeding DCBHs using only the local gas properties instead of those averaged over the entire host halo. In principle, the use of local gas properties is more physically consistent than halo averaged gas properties (as done in Bhowmick et al. 2021 where the seeding is based on the total mass and star-forming, metal-poor gas mass of a halo); this is particularly true for modelling seeding conditions such as high densities and low metallicities. However, the actual length scales that are referred to as 'local' are determined by the spatial resolution of the simulation. Achieving resolution convergence may be more challenging when the seeding is only based on properties of a single 'local' gas cell. Moreover, seeding conditions based on properties such as gas angular momentum inevitably require information beyond the local environment. Consequently, Dunn et al. (2018) decided not to explore the impact of gas angular momentum on seed formation. At the same time, H16 also decided to focus only on the LW flux criterion. It is important to note that Dunn et al. (2018) does not resolve mini-haloes, which can form stars and get polluted with metals before crossing the atomic cooling threshold; this will tend to overestimate the number of potential DCBH forming haloes.

In this work, we use a suite of cosmological hydrodynamic zoom simulations to systematically characterize the impact of both LW flux and gas angular momentum based seeding criteria on the SMBH population at $z > 7$. We specifically investigate how seeds of different birth masses grow in the presence of these seeding criteria. Because of the fine-tuned nature of DCBH seeding conditions, probing the rare conditions of metal-poor gas irradiated by LW fluxes $\gtrsim 1000 J_{21}$ would require simulating a large cosmological volume. We find that our zoom region is only able to probe $J_{\rm crit}$ values up to $100 J_{21}$. We are not able to directly probe much higher values $\gtrsim 1000 J_{21}$ that are more likely to represent actual DCBH formation; nevertheless, our results will still enable us to assess the feasibility of the DCBH channel to explain different parts of the underlying mass function of z

> 7 SMBHs. In a follow-up paper (Bhowmick et al., in preparation), we are probing the formation of the brightest $z > 6$ quasars in much more extreme regions where higher LW fluxes are expected.

We also note that, similar to Dunn et al. (2018), we do not resolve star formation in mini-haloes; as a result, we do not intend to probe the typical DCBH formation scenario wherein haloes just crossing the atomic cooling threshold are exposed to supercritical LW fluxes. Instead, we will focus on possible formation of seeds in haloes that have grown significantly (by factors of $\gtrsim$ 4–10 depending on the seed mass) beyond the atomic cooling threshold by the time they are exposed to supercritical LW fluxes. A majority of these haloes have already initiated star formation but they do not get instantaneously metal enriched; as a result, some haloes may have pockets of metal-poor gas that can potentially be exposed to supercritical fluxes from nearby star-forming regions. As it turns out, our model ends up producing seeds in these metal-poor pockets of dense gas. Therefore, it is this scenario that is the focus of this study.

This work is also part of a larger effort (started with Bhowmick et al. 2021) to build a family of gas based seeding prescriptions for the next generation of cosmological simulations. Our prescriptions are generally agnostic about which theoretical seed formation channels they may represent (e.g. Pop III, DCBH, or something else), such that we can tune our parameters to emulate a specific model. To that end, we use zoom simulations to characterize the impact of various aspects of galaxy evolution on the formation of seeds and their subsequent growth.

This paper is organized as follows. Section 2 presents the basic methodology, which includes the simulation suite, and the implementation and gas angular momentum and LW flux based seeding. Section 3 describes the results of our work, followed by our main conclusions in Section 4.

2 METHODS

Our simulations were run using the AREPO code (Springel 2010; Pakmor, Bauer & Springel 2011; Pakmor et al. 2016; Weinberger, Springel & Pakmor 2020) that solves for gravity coupled with magnetohydrodynamics (MHD). The gravity sector involves an N-body solver using PM-Tree method (Barnes & Hut 1986). The MHD sector uses a quasi-Lagrangian description of the gas fluid with an unstructured grid constructed via a Voronoi tessellation of the domain. AREPO has been used to run a variety of cosmological simulations that include uniform volumes such as Illustris (Genel et al. 2014; Vogelsberger et al. 2014a,b; Nelson et al. 2015; Sijacki et al. 2015), IllustrisTNG (Marinacci et al. 2018; Naiman et al. 2018; Nelson et al. 2018; Pillepich et al. 2018b, 2019; Springel et al. 2018; Nelson et al. 2019a,b), and zoom volumes such as AURIGA (Grand et al. 2017) and HESTIA (Libeskind et al. 2020).

AREPO contains several distinct sets of galaxy formation models. As in Bhowmick et al. (2021), we use the IllustrisTNG model (Weinberger et al. 2017; Pillepich et al. 2018a) in this work as our baseline (except for the BH seed model). The key features of the IllustrisTNG model include: star formation in the dense interstellar medium, where stars form stochastically from gas cells (with an associated time-scale of 2.2 Gyr) when their densities exceed a threshold of $\rho_{SF} = 0.13$ cm^{-3}, and the ISM itself is modelled by an effective equation of state (Springel & Hernquist 2003; Vogelsberger et al. 2013). In doing so, our model assumes that each gas cell with density >0.13 cm^{-3} has an unresolved cold dense component that can form stars; in regions where the gas is pristine, this cold dense component is presumably formed via molecular (H_2) cooling that is otherwise not explicitly included in the model.

The absence of an explicit modelling for H_2 cooling will artificially suppress star formation and metal enrichment in mini-haloes (with virial temperature $T_{vir} < 10^4$ K). While we do not resolve minihalos below $\lesssim 10^6$ M$_\odot$ h^{-1}, this can also overestimate the number of metal-poor haloes crossing the atomic cooling threshold. As we shall see, with a minimum halo mass criterion and an LW-flux-based seeding criterion ($J_{crit} \geq 50J_{21}$), our simulation ends up largely forming seeds in $10^8 \lesssim M_h \lesssim 10^{10}$ M$_\odot$ h^{-1} haloes; these haloes have grown significantly since crossing the atomic cooling threshold. We again emphasize that the existence of metal-poor pockets of gas within these star-forming haloes allows seeding to occur even after the onset of star formation in a given halo. Owing to this, and because our galaxy formation model is well calibrated for these haloes, the lack of explicit H_2 cooling model should not have a serious impact on our results. Note also that the exclusion of an explicit H_2 cooling model is a feature of many large volume cosmological simulations (for e.g. Vogelsberger et al. 2014a; Khandai et al. 2015; Schaye et al. 2015; H16; Nelson et al. 2018), and coincides with the choice not to resolve the cold, dense phase of the interstellar medium. We plan to explore this issue further in future work.

Stellar evolution and metal enrichment assumes a Chabrier (2003) initial mass function for the underlying single stellar populations (SSPs) represented by the star particles. Metal cooling is implemented in the presence of a spatially uniform and time-dependent ultraviolet background (UVB) radiation field (including the self-shielding of dense gas). A uniform seed magnetic field (10^{-14} comoving Gauss) is added at an arbitrary orientation, and its subsequent evolution is governed by MHD.

The modelling of BH seeding is discussed in detail in the following section. Here, we summarize the other aspects of the BH modelling that have been kept the same as IllustrisTNG. Once seeded, BHs can grow either via gas accretion or mergers with other BHs. BH accretion follows the Eddington limited Bondi–Hoyle formula and is given by

$$\dot{M}_{BH} = \min(\dot{M}_{Bondi}, \dot{M}_{Edd}), \tag{1}$$

$$\dot{M}_{Bondi} = \frac{4\pi G^2 M_{BH}^2 \rho}{c_s^3}, \tag{2}$$

$$\dot{M}_{Edd} = \frac{4\pi G M_{BH} m_p}{\epsilon_r \sigma_T} c, \tag{3}$$

where G is the gravitational constant, M_{BH} is the mass of the BH, ρ is the local gas density, c_s is the local sound speed of the gas, m_p is the mass of the proton, ϵ_r is the radiative efficiency and σ_T is the Thompson scattering cross-section. The resulting bolometric luminosity is given by

$$L = \epsilon_r \dot{M}_{BH} c^2, \tag{4}$$

where $\epsilon_r = 0.2$. Accreting BHs inject energy into the surrounding gas as active galactic nuclei (AGN) feedback; this is implemented in two modes. For Eddington ratios ($\eta \equiv \dot{M}_{bh}/\dot{M}_{Edd}$) higher than a critical threshold of $\eta_{crit} = \min[0.002(M_{BH}/10^8 \text{ M}_\odot)^2, 0.1]$, thermal energy is injected into the neighbouring gas at a rate given by $\epsilon_{f,high}\epsilon_r \dot{M}_{BH} c^2$, where $\epsilon_{f,high}\epsilon_r = 0.02$; $\epsilon_{f,high}$ is referred to as the 'high accretion state' coupling efficiency. For Eddington ratio values lower than the critical threshold, kinetic energy is injected into the gas surrounding the BH, in a time pulsated fashion, as a directed 'wind' oriented along a randomly chosen direction; the energy injection rate ($\dot{E}_{kin}$) is given by

$$\dot{E}_{kin} = \epsilon_{f,kin} \dot{M}_{BH} c^2, \tag{5}$$

$$\epsilon_{f,\text{kin}} = \min\left(\frac{\rho}{\rho_{\text{SF}}}, 0.2\right). \tag{6}$$

The merging of BH pairs occurs when their separations fall below the smoothing length of the BHs; this is the minimum radius of a sphere that encloses a specified number of neighbouring gas cells weighted over a smoothing kernel. Due to the limited resolution, the small-scale dynamics of BHs cannot be determined self-consistently; this is particularly true when the BH mass is smaller than the mass of the DM particles. To avoid spurious forces, the BHs are therefore re-positioned to the location of the closest potential minimum.

2.1 Modelling of BH seeds

Our seed models are based on the gas properties of haloes and are designed to emulate conditions for DCBH seed formation. We first apply a set of seeding criteria to restrict the seeding to haloes with gas that is metal-poor and has a density above the minimum threshold for star formation; we hereafter refer to this as 'dense, metal-poor gas'. In particular, seeds of mass M_{seed} are allowed to form only in haloes that satisfy the following:

(i) A minimum threshold for dense, metal-poor gas mass, denoted by $\tilde{M}_{\text{sf,mp}}$. As in Bhowmick et al. (2021), the tilde indicates that the mass threshold is a dimensionless quantity normalized to the seed mass: $\tilde{M}_{\text{sf,mp}} \equiv M_{\text{sf,mp}}/M_{\text{seed}}$. 'Metal-poor' gas cells refer to those with metallicities less than 10^{-4} Z$_\odot$. Note however that our results are not significantly sensitive to the choice of this threshold from 10^{-5} to 10^{-2} Z$_\odot$.

(ii) A minimum threshold for the total mass, denoted by $\tilde{M}_{\text{h}}$ (this is also a dimensionless quantity normalized to the seed mass: $\tilde{M}_{\text{h}} \equiv M_{\text{h}}/M_{\text{seed}}$).

A range of models with the above seeding criteria (in the parameter space of $\tilde{M}_{\text{sf,mp}}$, $\tilde{M}_{\text{h}}$, and M_{seed}) has been explored in Bhowmick et al. (2021), where we found that both $\tilde{M}_{\text{sf,mp}}$ and $\tilde{M}_{\text{h}}$ leave strong and distinct imprints on the merger rates, and therefore also the BH masses. More specifically, a factor of 10 increase in $\tilde{M}_{\text{h}}$ causes $\sim$100 times suppression of merger rates at $z > 15$; $\tilde{M}_{\text{sf,mp}}$ has greater impact at lower redshifts ($z \sim 7$–15), where it can suppress the merger rates by factors of $\sim$8 when increased from 5 to 150.

In this work, we fix $\tilde{M}_{\text{h}} = 3000$, $\tilde{M}_{\text{sf,mp}} = 5$ and explore seed masses of $M_{\text{seed}} = 1.25 \times 10^4$, 1×10^5, 8×10^5 M$_\odot$ h^{-1}; this is motivated by a number of considerations. First, the seed masses and the corresponding halo masses for their formation ($\sim 10^7$–10^9 M$_\odot$ h^{-1} haloes) are consistent with theoretical predictions for where DCBHs are expected to form (Bromm & Loeb 2003; Koushiappas, Bullock & Dekel 2004). Secondly, the choice of $\tilde{M}_{\text{h}} = 3000$, $\tilde{M}_{\text{sf,mp}} = 5$ provides reasonably well-converged results with respect to increasing resolution (Bhowmick et al. 2021). Thirdly, this model also produces a sufficient number of BHs within our zoom volume (to be described in Section 2.2), so that we can put in additional criteria to further restrict the seeding and investigate their impact. Hereafter, we shall refer to the above criterion as the *baseline seeding criteria*.

Having applied the baseline seeding criteria, we then explore the impact of further restricting the seeding based on the gas angular momentum and LW flux as described in the following subsections.

2.1.1 Gas spin criterion

Here, we restrict the seeding to haloes with low gas angular momentum. For each halo, we compute the net angular momentum

of all gas cells with respect to their centre of mass, which we hereafter refer to as 'gas spin' ($\boldsymbol{J}_{\text{spin}}$), as

$$\boldsymbol{J}_{\text{spin}} = \sum_{i}^{\text{gas cells}} \left[\boldsymbol{r}_i \times \boldsymbol{p}_i - \boldsymbol{r}_{\text{com}} \times \boldsymbol{p}_{\text{com}} \right], \tag{7}$$

where the summation is over all gas cells around the halo potential minimum up to the halo virial radius R_{vir}; $\boldsymbol{r}_i$ and $\boldsymbol{p}_i$ are the position and momentum of the ith gas cell. $\boldsymbol{r}_{\text{com}}$ and $\boldsymbol{p}_{\text{com}}$ are the position and momentum of the centre of mass of gas cells within the virial radius. We define the dimensionless gas spin parameter of the halo as

$$\lambda = \frac{|\boldsymbol{J}_{\text{spin}}|}{\sqrt{2} M_{\text{gas}} R_{\text{vir}} V_{\text{vir}}}, \tag{8}$$

where M_{gas} is total gas mass within the halo virial radius, and $V_{\text{vir}} = \sqrt{G M_{\text{vir}}/R_{\text{vir}}}$ is the circular velocity.

Our gas spin criterion is motivated by the results of Lodato & Natarajan (2006) on the stability analysis of pre-galactic gas discs in high-redshift haloes (as also adopted by Natarajan & Volonteri 2012 and DeGraf & Sijacki 2020). They derive a maximum gas spin λ_{max}, above which the gas disc is gravitationally stable. At lower gas spins, the disc becomes prone to gravitational collapse, potentially resulting in a massive DCBH seed. This maximum gas spin is given by

$$\lambda_{\text{max}} = \frac{m_{\text{d}}^2 Q_{\text{c}}}{8 j_{\text{d}}} (T_{\text{vir}}/T_{\text{gas}})^{1/2}, \tag{9}$$

where m_{d} and j_{d} are the fractions of the mass and angular momentum, respectively, of the halo that forms the disc. Q_{c} is the Toomre instability parameter. T_{vir} is the virial temperature of the halo and T_{gas} is the mean gas temperature. When $\lambda < \lambda_{\text{max}}$, the fraction of the disc mass that falls towards the centre (providing fuel for BH seed formation) is $\sqrt{1 - \lambda/\lambda_{\text{max}}}$.

We now focus on the implications of the foregoing physical arguments on our seed models. For a given seed mass M_{seed} to form, haloes must have (1) a gravitationally unstable disc and (2) a sufficient amount of gas mass ($> M_{\text{seed}}$) collapsing to the centre as a consequence. This corresponds to the following seeding criteria:

$$\lambda < \lambda_{\text{max}} \tag{10}$$

and

$$M_{\text{h}} > \frac{M_{\text{seed}}}{m_{\text{d}} \sqrt{1 - \lambda/\lambda_{\text{max}}}}, \tag{11}$$

where M_{h} is the halo mass. Equation (11) is essentially derived by inverting equation (1) from Natarajan & Volonteri (2012); as it turns out, it corresponds to halo mass thresholds that typically lie between $\sim$100 and $500 M_{\text{seed}}$, which is much smaller than our baseline criteria for halo mass ($\tilde{M}_{\text{h}} = 3000$). Therefore, it is only equation (10) that impacts our seeding.

To determine λ_{max}, we compute T_{vir} and T_{gas} for every halo on the fly during the simulation. The parameters m_{d}, j_{d}, and Q_{c} can depend on the structure of discs, which may not be well resolved for all of our simulations, particularly in low-mass haloes at early epochs. Computing these quantities on the fly would also be computationally demanding. For these reasons we instead simplify our model by assuming $m_{\text{d}} = j_{\text{d}} = 0.05$ and $Q_{\text{c}} = 2$, as also done in Natarajan & Volonteri 2012 and DeGraf & Sijacki (2020). We test the choices for m_{d} and j_{d} using one of our highest resolution simulations (gas mass resolutions $\sim 10^3$ M$_\odot$ h^{-1}), where we compute them in post-processing for our seed forming haloes using a kinematic decomposition of gas cells (as done in Huang et al. 2018); the values tend to lie between

0.01 and 0.1, broadly consistent with our assumed value of 0.05. Hereafter, we shall refer to equation (10) as the *gas spin criterion*.

2.1.2 *LW flux criterion*

We also examine the impact of restricting the seeding to haloes exposed to an LW flux above a critical threshold. We first describe our methodology to compute the LW flux over the entire simulation box. Note that our simulations do not include direct radiative transfer. Therefore, we adopt an empirical prescription to compute the LW flux on the fly. In principle, the LW flux at a given location consists of a background component (originating from distant stars not necessarily within the simulation volume) and a spatially varying component (originating from nearby stars). The background component depends on the global star formation rate (SFR) density, and is estimated to be $0.01 J_{21}$ at $z \sim 25$–$1 J_{21}$ at $z \sim 7$–10 (Johnson, Dalla Vecchia & Khochfar 2013). The spatially varying component can however be much higher than the background component, particularly at the sites of potential seed formation. Moreover, the flux thresholds we plan to consider are also ~ 10–300 times higher. Therefore, we neglect the background component and include only the spatially varying component in our calculation (as also done in H16).

The spatially varying components for both Pop III and Pop II LW fluxes (adopted from Dijkstra et al. 2014 and Lupi et al. 2021) are given by

$$J_{\rm LW} = \sum_i \frac{\langle h\nu \rangle}{\Delta \nu} \frac{f_{\rm esc} Q_{\rm LW}}{16\pi^2 r_i^2} m_{*,i}, \tag{12}$$

where $m_{*,i}$ is the mass of each resolution element comprised of young stars, r_i is the corresponding distance. $\nu = 2.99 \times 10^{15}$ Hz and $\Delta \nu = 7.79 \times 10^{14}$ Hz are mean frequency and band width, respectively, of the LW band (11.2–13.6 eV). $f_{\rm esc}$ is the escape fraction of LW photons, which is assumed to be 1 as done in both Dijkstra et al. (2014) and Lupi et al. (2021). This assumption may not necessarily be true, in which case our calculated LW fluxes, and therefore the number of seeds formed, would only correspond to upper limits. $Q_{\rm LW}$ is the photon production rate (adopted from Schaerer 2003) and is given by

$$Q_{\rm LW} = Q_0 \left(1 + \frac{t_{\rm LW}}{4 \, {\rm Myr}} \right)^{3/2} \exp\left(-\frac{t_{\rm LW}}{300 \, {\rm Myr}} \right), \tag{13}$$

where $t_{\rm LW}$ is the time elapsed after a star-burst and $Q_0 = 10^{47}$ s^{-1}M$_\odot^{-1}$. We include contributions only from star formation within the previous 5 Myr (consistent with Agarwal et al. 2012, 2014; DeGraf & Sijacki 2020), since most LW photons are emitted within this time interval due to the shorter lifetimes of the most massive Pop II and Pop III stars. Therefore, $m_{*,i}$ in equation (12) is assumed to be the total stellar mass formed in the last 5 Myr within the ith star-forming gas cell, given by

$$m_{*,i} = {\rm SFR}_i \times 5 \, {\rm Myr}, \tag{14}$$

where ${\rm SFR}_i$ is the instantaneous star formation rate of the gas cell at a given time-step. In other words, each star-forming gas cell is assumed to contain an SSP characterized by its age and metallicity. We only include gas cells representing Pop III and Pop II SSPs, which are classified by metallicities of $Z < 0.001 \, Z_\odot$ and $0.001 < Z < 0.1 \, Z_\odot$, respectively. Star-forming gas with $Z > 0.1 \, Z_\odot$ (Pop I stars) does not contribute to our LW flux calculation since (1) they have redder spectra, and (2) they form a very small fraction (~ 5 per cent at $z \sim 11$ and $\lesssim 1$ per cent at $z \gtrsim 16$) of the total stellar content in our zoom

volume at such high redshifts. Lastly, note that our simulation time resolution is not high enough to resolve the detailed star formation history of each gas cell within 5-Myr interval; therefore, we simply assume that the entire stellar mass $m_{*,i}$ has an age of 5 Myr, and assign $t_{\rm LW} = 5$ Myr in equation (13).

For seeding BHs based on the calculated LW fluxes, we assume a threshold LW flux (Pop II + Pop III contribution) required for seeding, denoted by $J_{\rm crit}$. The seeding criterion then requires that the dense, metal-poor gas must also be illuminated by LW intensities $> J_{\rm crit}$ (hereafter referred to as 'LW-illuminated'). This can then be expressed as

$$M_{\rm sf,mp,LW} > \tilde{M}_{\rm sf,mp} \, M_{\rm seed} = 5 M_{\rm seed}, \tag{15}$$

where $M_{\rm sf, mp, LW}$ is the total mass of dense, metal-poor gas cells within a given halo that are also exposed to LW fluxes greater than $J_{\rm crit}$. Lastly, we also make sure that star formation is switched off within these dense, metal-poor, LW-illuminated gas cells. We hereafter refer to this as the *LW flux criterion*. Note that we continue to use the subscript 'sf' (which stands for 'star-forming') to be consistent with the notation in Bhowmick et al. (2021); however, when the LW flux criterion is applied, 'sf' corresponds gas with densities exceeding the star formation threshold but *does not* actually form stars.

2.2 Simulation suite

Our simulation suite consists of a series of zoom simulations of a universe with an underlying cosmology adopted from Planck Collaboration XIII (2016; $\Omega_\Lambda = 0.6911$, $\Omega_{\rm m} = 0.3089$, $\Omega_{\rm b} = 0.0486$, $H_0 = 67.74$ km s^{-1}Mpc^{-1}, $\sigma_8 = 0.8159$, $n_{\rm s} = 0.9667$). The initial conditions (ICs) are generated using MUSIC (Hahn & Abel 2011) within a parent box with $(25 \, {\rm Mpc} \, h^{-1})^3$ comoving volume.

Our density field realization and the zoom-in region of interest is the same as that of Bhowmick et al. (2021). Here we briefly summarize the main features and refer the interested reader to Bhowmick et al. (2021) for more details. We first ran a uniform volume simulation with 128^3 particles and selected a target halo of mass 3.5×10^{11} M$_\odot$ h^{-1} (corresponding to a peak height $\nu = 3.3$) at $z = 5$ to resimulate at higher resolutions. DM particles comprising that halo were traced to $z = 127$, wherein a cuboidal region enclosing these particles is selected for the zoom runs; this region was referred to as ZOOM_REGION_z5 in Bhowmick et al. (2021). However, note that for this work, we increased the dimensions of the initial ($z = 127$) cuboidal zoom region by 50 per cent to allow for higher number of seeds to form in regions free of contamination from low-resolution DM and gas particles. Therefore, our baseline model in this work produces approximately two to three times higher number of seeds compared to that of Bhowmick et al. (2021).

For our zoom-in ICs, the resolution of the zoom region is characterized by the parameter $L_{\rm max}$, corresponding to a uniform box with $2^{L_{\rm max}}$ DM particles per side. Table 1 summarizes the mass and spatial resolutions in our zoom region for different values of $L_{\rm max}$. The background grid is always kept at $L_{\rm min} = 7$, while for the zoom region, we explored $L_{\rm max} = 10, 11$, and 12. In Bhowmick et al. (2021), we found that for our baseline seeding model, the results were reasonably well converged by $L_{\rm max} = 11$. Additionally, $L_{\rm max} = 11$ also runs in reasonable enough time to be able to explore wide range of seeding parameters; therefore, we primarily use $L_{\rm max} = 11$ for this study. However, we do find that the additional seeding criteria (particularly the LW flux criterion) can impact resolution convergence; we discuss this in more detail in Section 3.3.1 and Appendix A.

Table 1. Spatial and mass resolutions within the zoom region of our simulations for various values of L_{max} (see Section 2.2 for the definition).

L_{max}	M_{dm} (M$_\odot$ h^{-1})	M_{gas} (M$_\odot$ h^{-1})	ϵ (kpc h^{-1})	M_{seed} (M$_\odot$ h^{-1}) values explored
10	1×10^6	$\sim 10^5$	0.5	8×10^5, 1×10^5
11	1.3×10^5	$\sim 10^4$	0.25	8×10^5, 1×10^5, 1.25×10^4
12	1.6×10^4	$\sim 10^3$	0.125	8×10^5, 1×10^5, 1.25×10^4

Notes. M_{dm} is the mass of a dark matter particle, M_{gas} is the typical mass of a gas cell (note that gas cells can refine and de-refine depending on the local density), and ϵ is the gravitational smoothing length. The fourth column corresponds to the seed masses allowed at each L_{max}, which is limited by the gas mass resolution.

2.2.1 BH seed models explored

Here we summarize the gas based seed models explored in this work. The key parameters of interest in our modelling are $\tilde{M}_h$, $\tilde{M}_{sf,mp}$, M_{seed}, and J_{crit}. In addition, we have the gas spin criterion that can be switched on or off. As discussed in Section 2.1, $\tilde{M}_h$ and $\tilde{M}_{sf,mp}$ (which were explored in Bhowmick et al. 2021) are kept fixed at 3000 and 5, respectively.

When exploring models with the LW flux criterion, we consider J_{crit} values 10, 50, and $100J_{21}$. While these are substantially below current theoretical predictions for J_{crit} from hydrodynamic simulations and one-zone chemistry models ($\gtrsim 1000J_{21}$), it is clear from our results that such high values of J_{crit} would not produce any seeds in our simulation volume. Therefore, we systematically explore several lower values of J_{crit} and use the results to understand potential implications for DCBH formation. In future work, we plan to explore higher J_{crit} values in larger, more overdense haloes. The M_{seed} values explored in this work are 1.25×10^4, 1×10^5, and 8×10^5 M$_\odot$ h^{-1}, which broadly span the masses up to which DCBHs are expected to form via runaway infall of gas in haloes with virial temperatures $T_{vir} \gtrsim 10^4$ K (Begelman et al. 2006).

We use the following nomenclature to refer to our models for the remainder of this work. If a particular model only applies the baseline seeding criteria, we label it is 'BASELINE'. When the gas spin criteria is included, we label it as 'LOWSPIN'. When the LW flux criterion is included, then we include 'LW∗', where '∗' is replaced by the J_{crit} flux value. For example, $J_{crit} = 50J_{21}$ would correspond to 'LW50'.

3 RESULTS

3.1 Build-up of seed formation sites

Fig. 1 visualizes the evolution of the key properties of the gas distribution of the zoom region that drive the formation of seeds, which proceeds as follows. As time progresses (Fig. 1 shows $z = 13$ to 7), gravitational collapse and gas cooling leads to regions with densities high enough to trigger star formation (Fig. 1: first row). Subsequent stellar evolution processes lead to a significant amount of metal enrichment (Fig. 1: second row). These earliest stages of star formation and metal enrichment regions are primarily comprised of young Pop III and Pop II stellar populations, which bombard nearby gas with LW radiation.

The LW fluxes from Pop II and Pop III stars are shown in the third and fourth rows of Fig. 1. The BH seeds start forming in regions illuminated by LW flux. However, these regions soon become metal-enriched due to their close proximity to star-forming gas; this stops the formation of new seeds. The dispersion of metals as well as LW photons are two competing processes that are simultaneously

driven by star formation; as a result, the window for seed formation is relatively narrow.

It is instructive to compare the impact of young Pop II versus Pop III stars (age < 5 Myr) on seed formation in our models. Fig. 2 shows the total amount of young stellar content in the form of Pop II and Pop III stars, as a function of redshift. At $z \sim 16$–20, the young stellar content is dominated by Pop III stars; this is because at this relatively early stage of star formation, a majority of the star-forming regions have not yet been enriched by metals. However, by $z \sim 7$–15, the gas is sufficiently enriched and Pop II stars start to dominate the young stellar population.

Fig. 3 compares the contributions from Pop III versus Pop II stars to the LW fluxes on the surrounding gas. We first look at LW fluxes for all gas cells (dotted lines in Fig. 3); we find that at $z = 7$, 11, 15, the LW flux is predominantly contributed by Pop II stars for all flux values between ~ 1 and $\sim 10\,000$; this is expected from the results of Fig. 2 where Pop II stars dominate the total stellar content at $z \sim 7$–15. Notably, even at $z \sim 19$ where Pop III stars are more abundant overall, LW fluxes from Pop II stars still dominate at the highest values ($\gtrsim 50J_{21}$) relevant for BH formation. This is because the highest LW fluxes naturally occur in the densest regions, where metal enrichment (and therefore, Pop II star formation) is expected to be more prevalent compared to other locations.

Next, we look at the LW fluxes in gas cells that are simultaneously dense and metal-poor (solid lines in Fig. 3). The first thing to note is that the LW flux contributed by Pop II stars is substantially smaller in dense, metal-poor gas cells compared to all gas cells (solid versus dotted blue lines in Fig. 3). In contrast, the incident PopIII LW flux is similar for all gas and for the subset of dense, metal-poor gas cells, at least for LW fluxes $\gtrsim 50J_{21}$ (solid versus dotted green lines in Fig. 3). These results are not unexpected since Pop II stars are likely to be somewhat further away from metal-poor regions by construction (recall that 'metal-poor' implies $Z < 10^{-4}$ Z$_\odot$, whereas Pop II stars have $10^{-3} < Z < 10^{-1}$ Z$_\odot$). As a result, in dense, metal-poor regions the difference between LW fluxes for Pop II versus Pop III stars is not drastically different, and both populations play an equally important role in seed formation. Lastly, the maximum LW fluxes in dense, metal-poor regions are only up to a few times $\sim 100J_{21}$; this already indicates that a seeding criterion of $J_{crit} \gtrsim 1000$ would not produce any seeds within ZOOM_REGION_z5. Therefore, the remainder of the paper will largely focus on significantly lower values of $J_{crit} = 10$–$100J_{21}$ and their impact on seed formation.

3.2 Characterizing halo properties relevant for seed formation

In this section, we look at the $z \gtrsim 7$ halo population in the zoom region and characterize it in terms of properties that are relevant for seed formation. In particular, we consider the total mass, dense, and metal-poor gas mass, gas spin, and LW fluxes of haloes in Fig. 4. Note here
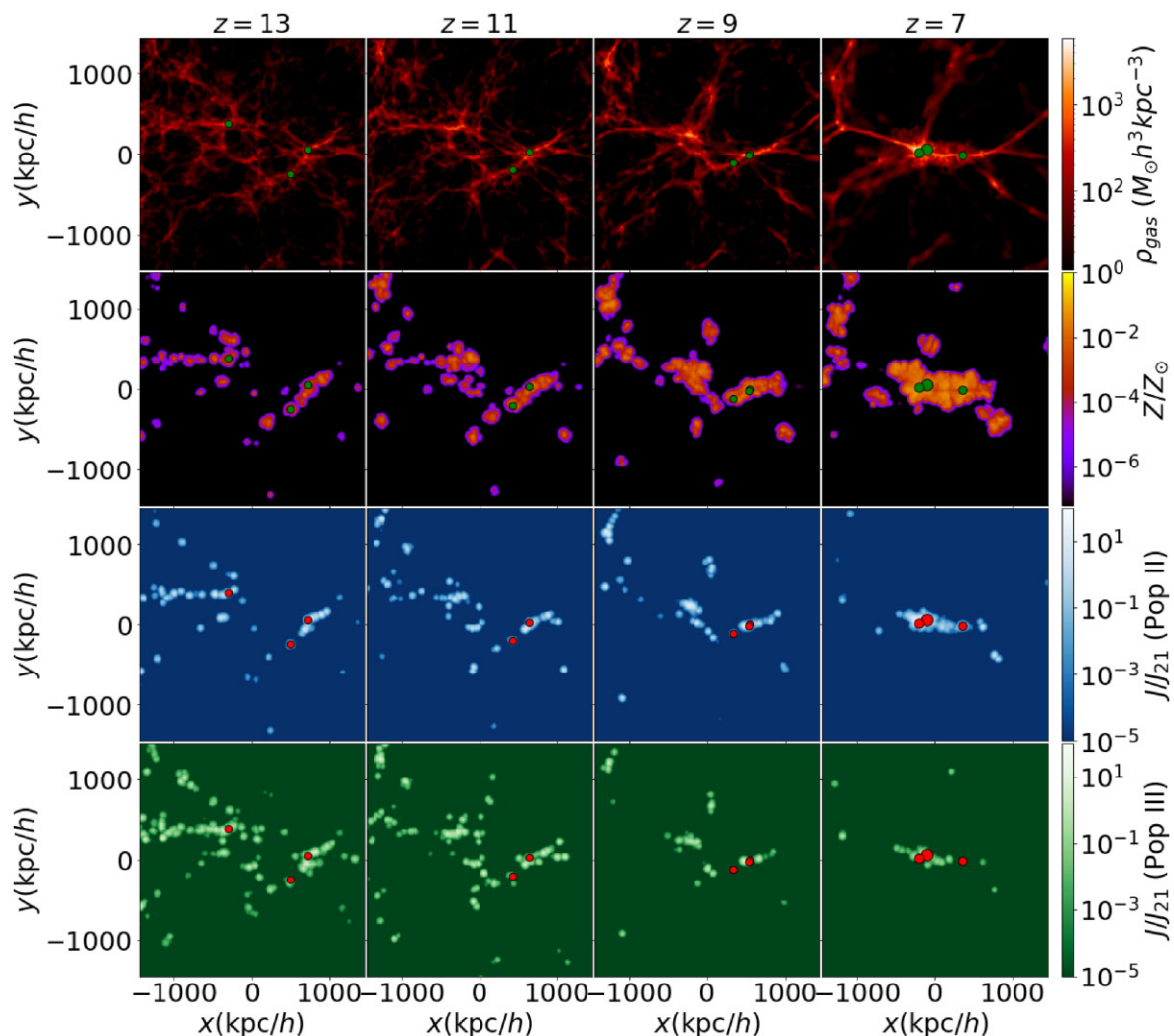
Figure 1. 2D projected colour maps of the gas density (first row), gas metallicity (second row), and LW fluxes from Pop II (third row) and Pop III (fourth row) stars in our zoom region. The left- to right-hand panels show the redshift evolution from $z = 13$ to 7. The green and red circles represent BHs seeded at $1 \times 10^5 \, \mathrm{M_\odot} \, h^{-1}$ in haloes with $\tilde{M}_\mathrm{h} = 3000$, $\tilde{M}_\mathrm{sf,mp} = 5$, and $J_\mathrm{crit} = 50 J_{21}$. As time evolves, the star-forming and metal-enriched regions appear throughout our zoom volume. These regions are sources of LW photons. Seed BHs are formed in metal-poor regions where gas densities exceed the star formation threshold (hereafter referred as 'dense gas, metal-poor gas'), but the star formation itself is suppressed by the LW flux.

that we only show haloes where $\lesssim 1$ per cent of the total mass is contaminated by low resolution DM particles.

We first focus on how these different halo properties correlate with the halo mass for the overall population. The first row in Fig. 4 shows that the dense, metal-poor gas mass positively correlates with the halo mass, particularly at $z \gtrsim 11$ (at $z = 7$, there are too few metal-poor haloes in our volume to make definitive conclusions). This is not unexpected, given that more massive haloes also have higher gas content overall and typically have higher gas densities at their potential minima. That being said, metal enrichment will also be more prevalent in more massive haloes (due to the onset of star formation and evolution), thereby weakening the correlation; we can clearly see this happening for the most massive haloes at $z \gtrsim 11$. But despite the metal enrichment in these most massive star-forming haloes ($\sim 10^8$–$10^{10} \, \mathrm{M_\odot} \, h^{-1}$), we still find that they have enough dense, metal-poor gas mass to be potential sites of seed formation. As we shall see in Section 3.2.1, the metal-poor gas typically resides in pockets embedded within surrounding star-forming and metal-enriched ($\gtrsim 10^{-4} \, \mathrm{Z_\odot}$) regions.

The dimensionless gas spin (shown in the second and third rows of Fig. 4) does not strongly correlate with halo mass. The gas spins are similar to those of the underlying dark matter spins, with mean values close to ~ 0.03–0.05 at all halo masses and redshifts. These results are consistent with previous work using *N*-body simulations (Bullock et al. 2001; Macciò et al. 2007; Bett et al. 2007, 2010) as well as hydrodynamic simulations (Danovich et al. 2015; Zjupa & Springel 2017; DeGraf & Sijacki 2020). In addition, the lack of halo mass versus spin correlation is also a natural prediction from tidal torque theory (see review by Schäfer 2009).

The last row of Fig. 4 shows that more massive haloes are exposed to higher LW fluxes within their dense, metal-poor gas. This is because more massive haloes typically have higher amounts of star formation overall, and most of the LW radiation is coming from star-forming regions within the same halo. As it turns out (see Section 3.2.1 for more detail), these haloes contain pockets of dense, metal-poor gas embedded within the star-forming regions that provide the LW flux. Additionally, for haloes at fixed mass, the LW flux typically decreases with time. This is simply due to Hubble
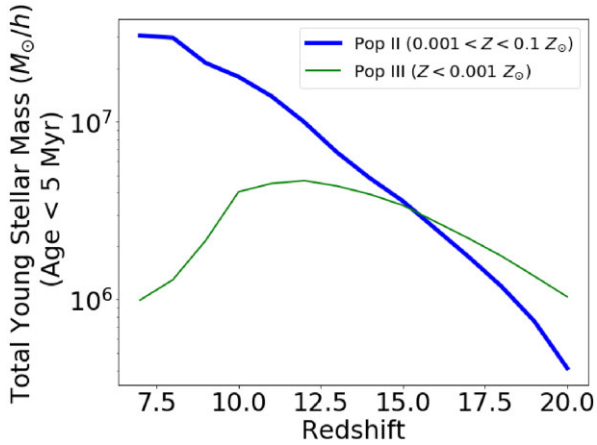
Figure 2. Total mass of young stars (age < 5 Myr) in the zoom region for Pop III ($Z < 0.001\ Z_\odot$; green curve) and Pop II ($0.001 < Z < 0.1\ Z_\odot$; blue curve) components. We find that between these components, Pop III stars dominate at $z \gtrsim 15$ and Pop II stars dominate at $z \sim 7\text{--}15$.

expansion, which causes a star-forming halo of a fixed mass to be less compact (in physical coordinates) at lower redshifts, thereby leading to smaller distances between the star-forming gas and the dense, metal-poor pockets. Therefore, the formation of seeds in the presence of an LW flux criterion will be driven by two competing effects: (1) formation of more massive haloes and proliferation of star-forming regions with time, which will tend to increase the LW flux and form more seeds as redshift decreases, (2) and Hubble expansion, which will tend to decrease the LW flux (at fixed halo mass) and suppress the formation of seeds as redshift decreases. Recall also that these competing effects are in addition to two other pre-existing effects originating from the baseline criterion: namely, the formation of dense gas (which tries to increase the number of seeds at lower redshifts), and metal enrichment (which tries to decrease the number of seeds at lower redshifts).

We now focus on the halo subsamples that satisfy different combinations of seeding criteria described in Section 2.1. The middle rows of Fig. 4 show that most haloes satisfying the baseline seeding criteria do not satisfy the gas spin criterion (filled red versus open green circles). At $z = 11$, for instance, only ~ 13 per cent of haloes satisfying the baseline seeding criteria also satisfy the gas spin criterion. This implies that gas angular momentum should have a significant impact on seed formation. Next, we see in the bottom row of Fig. 4 that an even smaller fraction of haloes satisfying the baseline criterion, also satisfy the LW flux criterion (filled blue versus open green circles) with $J_{\rm crit} = 50J_{21}$. This suggests that the LW flux criterion may be even more stringent than the gas spin criterion. Note also that amongst the $z = 7$, 11, 15, and 19 snapshots shown, the $z = 11$ snapshot has the highest number of haloes satisfying either the baseline criterion or the gas spin criterion; but when the LW flux requirement is imposed, the peak epoch is at $z = 15$. This suggests that the LW flux criterion will push the peak of seed formation to higher redshifts compared to the baseline criterion. While Fig. 4 shows the results for $M_{\rm seed} = 1 \times 10^5\ {\rm M}_\odot\ h^{-1}$, the same inferences hold for all seed masses considered in this work.

3.2.1 Sites of seed formation in haloes: dense, metal-poor, LW-illuminated pockets

Fig. 5 shows visualizations of two different seed forming regions (at our fiducial resolution $L_{\rm max} = 11$) as projected 2D colour plots of the

SFR, density, metallicity, and LW fluxes from Pop II and Pop III stars. We can see that these regions have undergone substantial amounts of star formation and metal-enrichment, which is not surprising since they are significantly above the atomic cooling threshold. However, both haloes contain small pockets ($\sim 3\text{--}5$ kpc h^{-1}; marked by red crosses) wherein the gas is still metal-poor ($Z < 10^{-4}\ Z_\odot$). Additionally, the surrounding star-forming regions provide LW flux to these pockets to completely suppress star formation, thereby creating an ideal site for seed formation. Note that the metal-poor, LW-illuminated pockets are not located at the halo centres. Therefore, the seed formation in these haloes will occur significantly away from the halo centre. In our simulations, these seeds eventually end up at the halo centre due to the BH repositioning scheme. However, recent simulations with more realistic treatment of BH dynamics have found that a substantial fraction of BHs may have difficulty in sinking to the halo centres, thereby leading to a population of off-centre BHs even at low redshifts (Bellovary et al. 2021; Ma et al. 2021; Ricarte et al. 2021). We shall investigate this in our simulations in future work.

We also note that at higher resolutions ($L_{\rm max} = 12$), the regions shown in Fig. 5 no longer contain dense, metal pockets. This is because metal enrichment is not fully converged at $L_{\rm max} = 11$; in particular, $L_{\rm max} = 12$ has relatively earlier onset of metal enrichment (see fig. 19 of Bhowmick et al. 2021). But never the less, dense metal-poor pockets do also form at higher resolutions, as shown in Fig. 6 for $L_{\rm max} = 12$. Resolution convergence of the LW flux criterion is discussed further in Section 3.3.1 and Appendix A.

Next, we examine the formation of dense metal-poor pockets in more detail for the full population of seed forming haloes from $z \sim 7$ to 20. In the left-hand panel of Fig. 7, we show the metallicities at the halo centres (more specifically the densest gas cell) of all seed forming haloes (for $J_{\rm crit} = 50J_{21}$) identified within snapshots from $z = 7$ to 20. We find that for a significant majority of the seed forming haloes within $\sim 10^8\text{--}10^{10}\ {\rm M}_\odot\ h^{-1}$, the halo centres have metallicities of $\gtrsim 10^{-2}\ Z_\odot$. For these haloes, the seed formation sites are not at the halo centres, and are located within dense, metal-poor, LW-illuminated pockets at distances that are mostly $\lesssim 20$ kpc h^{-1}, but can be up to ~ 130 kpc h^{-1} from the halo centre (right-hand panel of Fig. 7). These pockets have gas masses ranging from $\sim 10^5\text{--}10^6\ {\rm M}_\odot\ h^{-1}$. Overall, this implies that in the presence of an LW flux criterion ($J_{\rm crit} = 50J_{21}$ or greater), the majority of seeds in our simulation are formed in the peripheral regions of $\sim 10^8\text{--}10^{10}\ {\rm M}_\odot\ h^{-1}$ haloes, instead of forming at the halo centres. These haloes have a prior history of star formation and metal enrichment and for most of them, the dominant fraction ($\gtrsim 90$ per cent) of the LW radiation is contributed from their own star-forming gas, and not from neighbouring haloes. Notably, we also see that for seed formation sites in the most massive $\sim 10^{10}\ {\rm M}_\odot\ h^{-1}$ haloes, there is relatively higher contribution ($\sim 20\text{--}30$ per cent) of LW radiation coming from neighbouring haloes. This is likely because in these haloes, seed formation sites are farthest ($\gtrsim 100$ kpc h^{-1}) from the central region of their host haloes (revisit the middle panel of Fig. 7), thereby increasing their relative exposure to LW radiation from neighbouring haloes.

The build-up of seed formation sites in our simulations has some noteworthy distinctions compared to various models in the recent literature. For example (as also mentioned in Section 1), Regan et al. (2017), Lupi et al. (2021), and Visbal et al. (2014) consider the formation of DCBHs via a pair of synchronized haloes that cross the atomic cooling threshold within a few Myr; the first halo to cross the threshold becomes star forming and provides LW radiation to another nearby halo. In this scenario, seeds would inevitably form
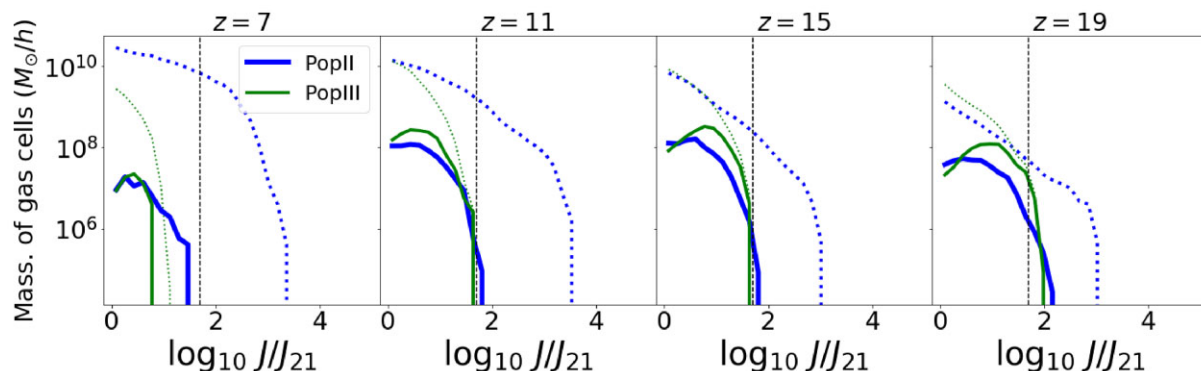
Figure 3. Total mass of gas cells illuminated by LW photons originating from Pop II (blue) and Pop III (green) stars within bins of various flux values shown in the x-axis. Dotted lines correspond to all gas cells and solid lines correspond to dense, metal-poor gas cells. Black vertical lines correspond to flux thresholds of $J_{crit} = 50J_{21}$. We find that across all gas cells, Pop II stars are the dominant contributors to the LW radiation, with fluxes reaching up to a few $\times\ 10^3 J_{21}$. However, when we specifically look at only the dense, metal-poor gas cells, the contribution from Pop II stars is substantially smaller and becomes comparable to that of Pop III stars at $z \gtrsim 11$. Within dense, metal-poor regions, flux values reach only up to $\sim 100 J_{21}$.

in haloes very close to the atomic cooling threshold with no prior history of star formation. Due to our model limitations (lack of explicit H_2 cooling), we do not attempt to place seeds in haloes very close to the atomic cooling threshold. Instead, we enforce a halo mass threshold for seeding ($\tilde{M}_h = 3000$), which forces seeds to form in haloes that have grown significantly since crossing the atomic cooling threshold ($1.25 \times 10^4\ M_\odot\ h^{-1}$ seeds in $> 3.7 \times 10^7\ M_\odot\ h^{-1}$ haloes and $1 \times 10^5\ M_\odot\ h^{-1}$ seeds in $> 3 \times 10^8\ M_\odot\ h^{-1}$ haloes).

Additionally, the LW flux criterion with $J_{crit}/J_{21} = 50$ and 100 further enforces seed formation to largely occur at $\sim 10^8$–$10^{10}\ M_\odot\ h^{-1}$ haloes (revisit fourth row in Fig. 4). Our simulations reveal that despite a prior history of star formation and metal enrichment in these haloes, seeds can still form because the metals are not able to fully pollute the halo; this creates pockets of metal-poor gas. If these pockets have dense gas that are also subjected to supercritical LW radiation from the surrounding star-forming regions of the halo, they become sites of seed formation. This distinct DCBH formation scenario revealed by our simulations indicates that DCBHs may be slightly less rare and can be probed in somewhat smaller cosmological volumes than previously thought, while they still need to be significantly larger than our zoom volume (particularly because of the high LW flux requirement i.e. $J_{LW}/J_{21} \gtrsim 1000$). Lastly, it is also noteworthy that despite the differences in seed formation scenario, there is one common implication between our models and those in the existing literature i.e. seeds are likely to end up in satellites of star-forming protogalaxies (see also Agarwal et al. 2014; Natarajan et al. 2017).

3.3 Impact of gas spin and LW flux on BH seeding

Here, we quantify the impact of gas spin and LW flux criteria on the frequency of BH seeding. Fig. 8 shows the number of seeds formed versus redshift, comparing the baseline model with the models in which a gas spin and/or LW flux criterion is added. Let us first focus on the gas spin criterion (solid versus dashed lines of same colour in upper panels of Fig. 8). At the highest redshifts ($z \gtrsim 20$), adding the gas spin criterion does not lead to any significant suppression in the number of seeds compared to the baseline seeding criteria; this is likely because at these early epochs, there has not been enough build-up of angular momentum in the gas to prevent seeding. As we approach lower redshifts, the suppression due to gas spin criterion becomes stronger. Additionally, we see that despite the

suppression, the gas spin criterion does not change the peak epoch of seed formation i.e. $z \sim 11$–12, compared to the baseline criteria; as also noted in Bhowmick et al. (2021), this peak occurs because metal pollution halts the formation of new seeds at $z \lesssim 11$. At $z \sim 11$–12, the gas spin criterion suppresses the number of seeds by factors of ~ 6. Lastly, the suppression is similar for all seed masses between 1.25×10^4–$8 \times 10^5\ M_\odot\ h^{-1}$; this is due to the lack of any significant correlation between halo mass versus gas spin seen in Section 3.2.

Comparing the foregoing results to previous work, Lodato & Natarajan (2006) used their empirical model to predict that ~ 5 per cent of haloes with $\sim 10^7\ M_\odot$ have low enough spins to form $\sim 10^5 M_\odot$ seed BHs (this percentage increases with halo mass). In our model, an overall suppression by factors of ~ 6 implies that about 16 per cent of haloes satisfying the baseline criteria will actually be seeded with BHs once the gas spin criterion is applied. However, the threshold halo masses in our baseline model ($> 3 \times 10^8\ M_\odot\ h^{-1}$ for $\sim 10^5\ M_\odot$) are significantly higher than that in Lodato & Natarajan (2006) ($10^7\ M_\odot\ h^{-1}$). If we reduce the halo mass threshold to $10^7 M_\odot$, ~ 6 per cent of our haloes satisfy the gas spin criterion, in good agreement with this previous work.

Next, we look at the suppression of seeding caused by the LW flux criterion (see Fig. 8: lower panels). Similar to the redshift trend seen with the gas spin criterion, seeding is more heavily suppressed by a lack of sufficient LW flux at $z \sim 7$–15 compared to $z \gtrsim 20$, despite the fact that LW radiation sources are more prevalent at lower redshifts. As noted in Section 3.2, this is driven by the reduction in LW flux (at fixed halo mass) with decreasing redshifts due to Hubble expansion. For the same reason, the LW flux criterion pushes the peak epoch of seed formation to higher redshifts compared to the baseline criterion (unlike the gas spin criterion). For $J_{crit} = 50J_{21}$ and $100J_{21}$, the majority of the seeds are formed around $z \sim 15$ and ~ 19, respectively. Therefore, a high LW flux criterion becomes a limiting factor for seed formation earlier than metal enrichment. We also find that the LW flux criterion has a larger impact at lower halo mass thresholds (corresponding to lower seed masses). This is most noticeable for $J_{crit} = 100J_{21}$ and is a consequence of the positive correlation between halo mass and LW flux.

We now quantify the impact of LW flux criterion by comparing it to the baseline model. For $J_{crit} = 50$ and $100\ J_{21}$, the suppression is by factors of ~ 40 and ~ 300, respectively, for halo mass thresholds corresponding to $M_{seed} = 1.25 \times 10^4\ M_\odot\ h^{-1}$. For halo mass thresholds corresponding to $M_{seed} = 1 \times 10^5\ M_\odot\ h^{-1}$, seeds are
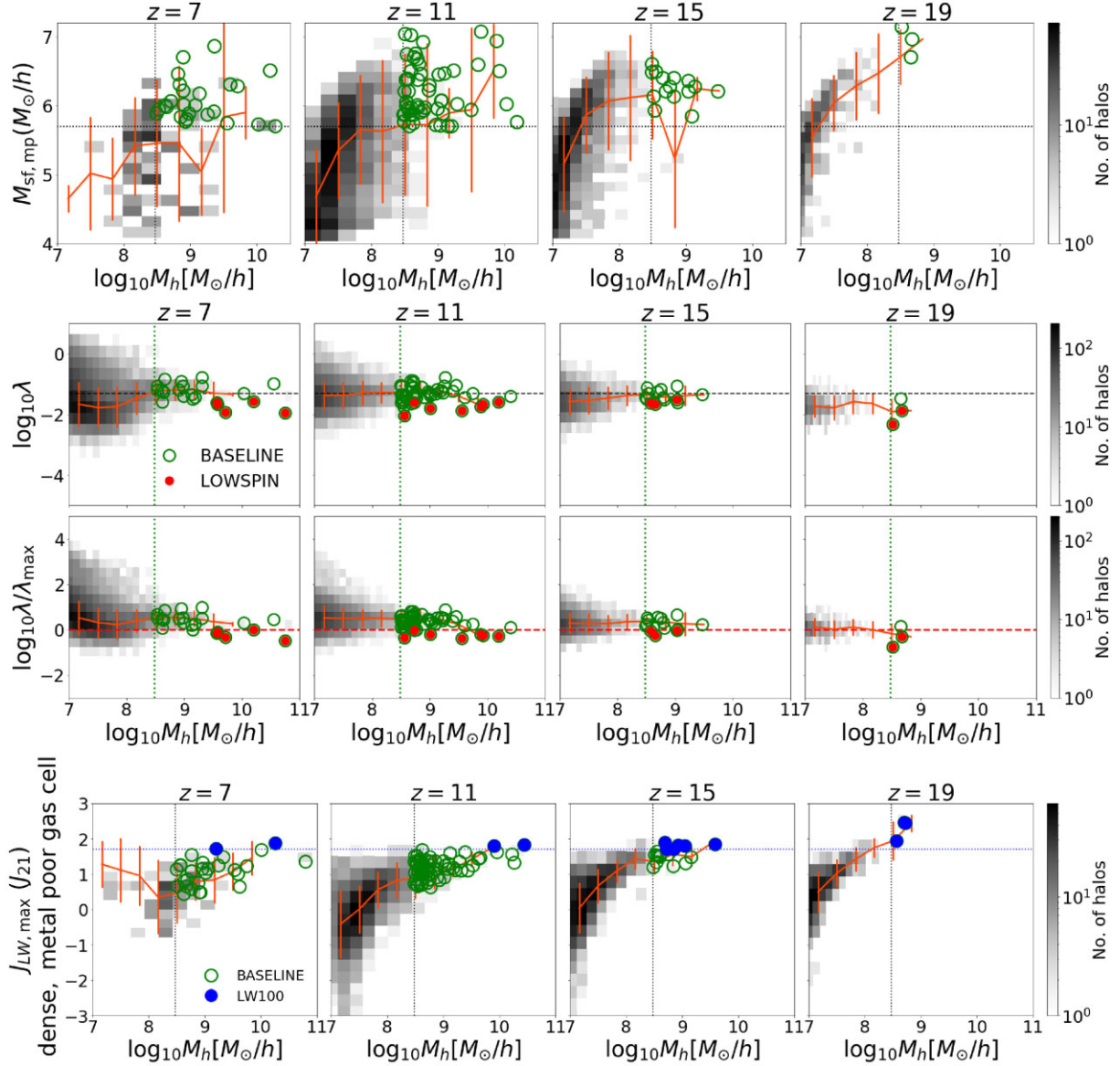
Figure 4. The relationships between the various halo properties that determine the formation of DCBHs at different redshifts from $z = 7$ to 19. We show only haloes that have contamination from low-resolution dark matter particles. The first row shows halo mass versus star-forming, metal-poor gas mass. The second row shows the halo mass (M_h) versus dimensionless gas spin (λ). In the third row, the dimensionless spins from the second row are normalized with respect to the maximum value (λ_{max}) allowed for seeding to occur. The fourth row shows the halo mass versus the maximum LW flux amongst all dense, metal-poor gas cells of the halo. The vertical lines are the minimum halo mass for seeding ($\tilde{M}_h = 3000$). The horizontal line in the first row is the minimum dense, metal-poor gas mass for seeding ($\tilde{M}_{sf,mp} = 5$). In the third row, the horizontal line is the maximum gas spin (λ_{max}) that is allowed for seeding. In the fourth row, the horizontal line corresponds to $J_{LW} = 50J_{21}$. Green open circles are haloes that satisfy the baseline seeding criteria ($\tilde{M}_h = 3000$, $\tilde{M}_{sf,mp} = 5$). The red filled circles are haloes that satisfy the baseline criteria as well as the gas spin criterion ($\lambda < \lambda_{max}$). The blue filled circles are haloes that satisfy the baseline criteria as well as the LW flux criterion ($M_{sf,mp,LW} > 5M_{seed}$; $J_{crit} = 50J_{21}$). We find that only a small fraction of haloes that satisfy the baseline seeding criteria also satisfy the gas spin and LW flux criterion.

suppressed by $\sim$20 and $\sim$100 for $J_{crit} = 50$ and 100 J_{21}, respectively. For even higher halo mass thresholds corresponding to $M_{seed} = 8 \times 10^5\ M_\odot\,h^{-1}$, there are no seeds formed for $J_{crit} = 50$ and 100J_{21}. For these highest seed masses, by the time haloes are able to accumulate a dense, LW-illuminated gas mass of $5 \times M_{seed}$, they have already become significantly metal enriched.

We can compare the results on the impact of J_{crit} to previous literature. When J_{crit} is increased from $10J_{21}$ to $100J_{21}$ (blue versus green lines in lower panels of Fig. 8), the number of seeds is suppressed by factors up to $\sim$100 for $1.25 \times 10^4\ M_\odot\,h^{-1}$ seeds,

and by factors up to $\sim$80 for $1 \times 10^5\ M_\odot\,h^{-1}$ seeds (note however that statistical uncertainties are large for $J_{crit} = 100J_{21}$). We compare this to predictions from hydrodynamic simulations of H16; notably, they are able to probe somewhat larger values of J_{crit} (30–300J_{21}) due to their larger volume (142 Mpc h^{-1} box size). H16 find an $\sim$100 times decrease in the number densities of haloes with critical LW fluxes varying from 30 to 300J_{21}. This is broadly consistent with our results, though we note that their resolution is significantly lower than ours for the (142 Mpc h^{-1})^3 box. Our simulations are similar in resolution to those of Dunn et al. (2018), but we predict a
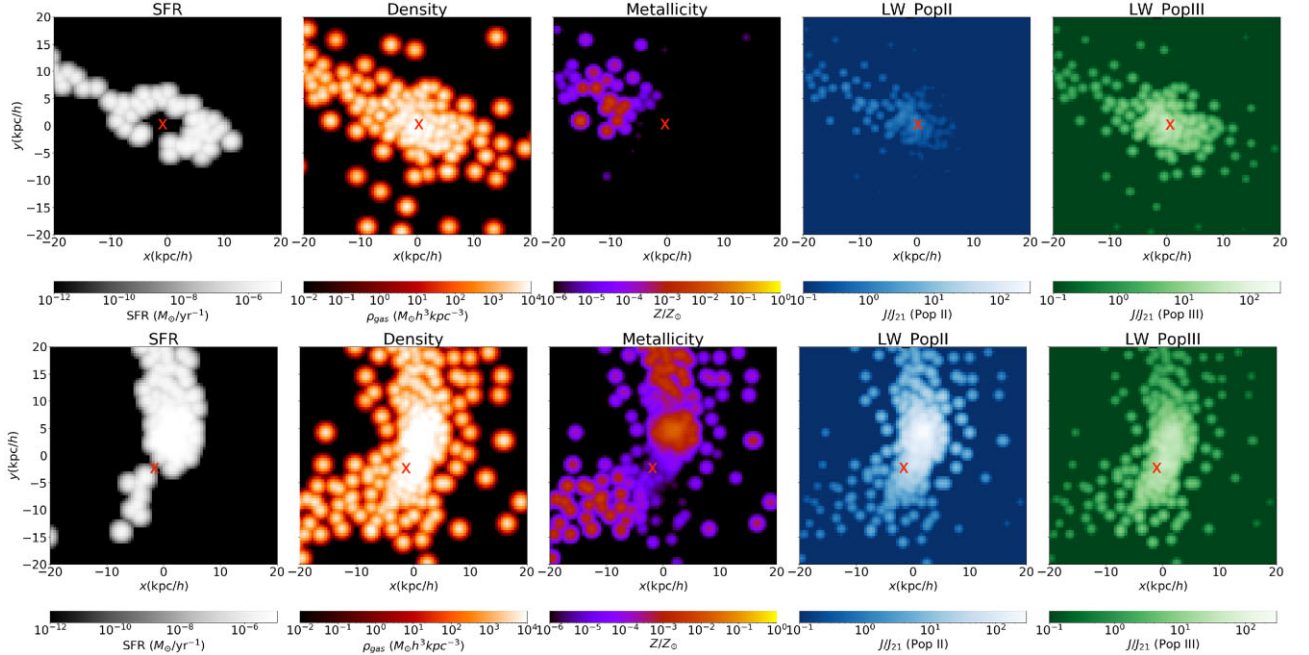
Figure 5. Top and bottom panels are visualizations (2D projected plots) of two different sites for BH seed formation that typically reside within haloes of mass $\sim 10^8$–10^{10} M$_\odot$ h^{-1} i.e. a metal-poor pocket (see the red cross) where the gas density exceeds the star formation threshold but the star formation is suppressed by LW radiation. The thickness of the slices along the line of sight is 5 kpc h^{-1}. At each pixel, the average value of the field is computed, followed by smoothening using a Gaussian filter of a fixed width at all locations. These are simulated at $L_{\max} = 11$. From the left- to right-hand side, we show the SFR, gas density, gas metallicity, and LW fluxes from Pop III and Pop II stars. In this case, star formation in metal-poor pockets is suppressed by LW fluxes greater than $50J_{21}$.

Figure 6. Similar to the previous figure, the top and bottom panels here also show visualizations of two different sites of seed formation, but for $L_{\max} = 12$ resolution. Dense, metal-poor pockets also form at higher resolutions despite the higher rates of metal enrichment.

stronger impact of J_{crit} compared to their results. More specifically, they find that the number of seeds is only suppressed by factors of ~ 7 when J_{crit} is increased from 30 to $300J_{21}$. There are some differences between our modelling and theirs that could potentially explain this. First, their seeding criteria are based on the local properties

of individual gas cells; therefore, they can form seeds even if one gas element satisfies the density, metallicity, and LW flux criteria. In contrast, our models require that a minimum total mass of gas cells (amounting to a mass of $5M_{\mathrm{seed}}$) *simultaneously* satisfies the density, metallicity, and LW flux criteria. Second, their models allow
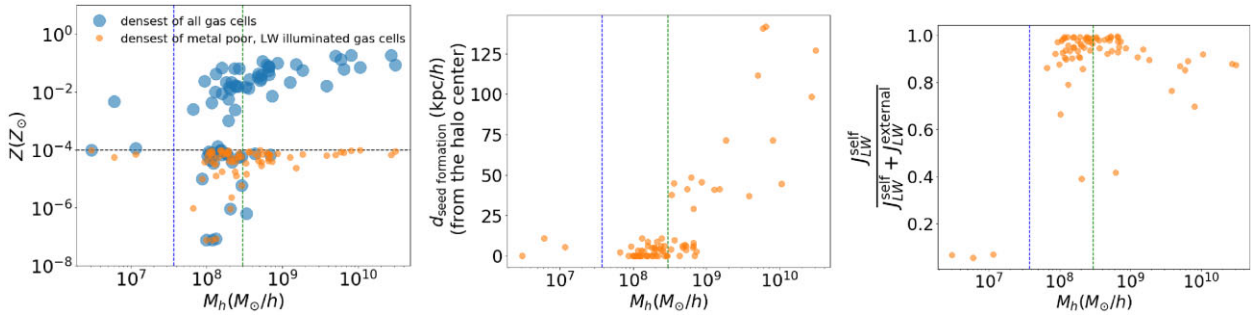
Figure 7. The scatter plots show key quantities for all haloes that contain a non-zero amount of dense, metal-poor, LW-illuminated gas for all snapshots from $z = 7$ to 20. Left-hnad panel: gas-phase metallicity versus halo mass. Blue circles show the metallicity of the densest gas cell in a halo. Orange circles show the metallicity of the densest metal-poor, LW-illuminated gas cell in a halo. Blue and green dashed vertical lines correspond to halo mass thresholds for forming 1.25×10^4 and 1×10^5 $M_\odot\,h^{-1}$ seeds, respectively. The black horizontal dashed line is the metallicity ceiling for seed formation. Most seeds form at $\sim 10^8$–10^{10} $M_\odot\,h^{-1}$ haloes wherein the densest metal-poor gas cell is not at the halo centre (blue circles are significantly above orange circles); therefore, seed formation does not occur at the centre of the halo. Middle panel: off-centre distance of seed formation site versus halo mass. $d_{\text{seed formation}}$ is defined to be the distance between the site of seed formation (densest metal-poor, LW-illuminated gas cell) from the halo centre. For seed formation occurs increasingly further away from the halo centre for increasingly massive haloes. Seed formation can occur at distances up to ~ 130 kpc h^{-1} from the halo centre, but most seeds in our simulation form within 20 kpc h^{-1} of the halo centre. Right-hand panel: the ratio between the LW flux contributed by star-forming gas present within the halo ($J_{\text{LW}}^{\text{self}}$) versus the total LW flux that also includes star-forming gas from outside the halo ($J_{\text{LW}}^{\text{self}} + J_{\text{LW}}^{\text{external}}$). Majority of the seed formation sites receive most ($\gtrsim 90$ per cent) of the LW radiation from within the same halo.
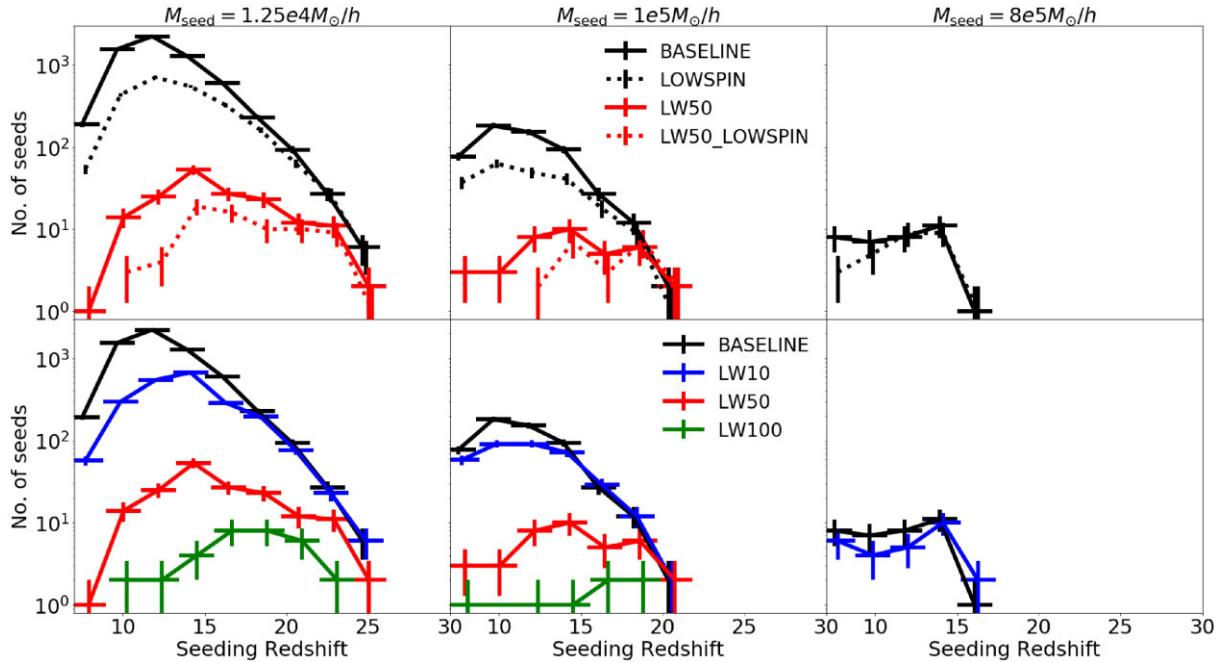

Figure 8. Distribution of seeding times for different seed models at fixed M_{seed}. Dashed versus solid lines (of the same colour) in the upper panels correspond to models with versus without the gas spin criterion, respectively. The suppression due to the gas spin criterion is by factors of $\sim$6 for all seed masses at $z \sim$ 11–12 (when most seeds form). Coloured versus black lines in the lower panels compare models with versus without an LW flux criterion respectively. When an LW flux criterion with $J_{\text{crit}} = 50$ and $100J_{21}$ is applied, 1.25×10^4 $M_\odot\,h^{-1}$ seeds are suppressed by factors of ~ 40 and 300, respectively; 1×10^5 $M_\odot\,h^{-1}$ seeds are suppressed by factors of ~ 20 and 100, respectively; 8×10^5 $M_\odot\,h^{-1}$ seeds are completely suppressed.

for multiple BH seeds to form in the same halo at a given time instant, whereas our model only allows one seed per halo. Overall, these could lead to significantly fewer seeds formed in our model compared to Dunn et al. (2018), particularly for higher values of J_{crit}. Semi-analytic models (Agarwal et al. 2012, 2014; Dijkstra et al. 2014), on the other hand, exhibit a much stronger impact compared to our simulations as well as H16 and Dunn et al. (2018), with factors of $\sim 10^4$ decrease in the number density of DCBH forming haloes when LW flux is increased from 30 to $300J_{21}$ (see fig. 4

of H16). As demonstrated in H16, the differences in predictions between hydrodynamic simulations and semi-analytic models may be attributed to differences in the modelling of star formation, metal enrichment, and LW radiation. Despite these differences, all the models (including this work) commonly predict a strong impact of LW radiation on BH seeding.

The impact of the LW flux criterion versus the gas spin criterion on BH seeding can be summarized as follows. First, the LW flux criterion is overall substantially more restrictive than the gas spin
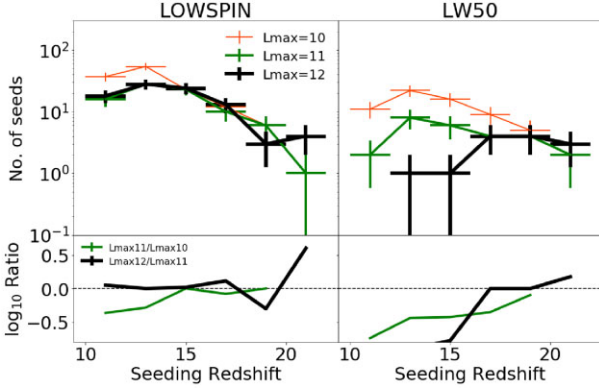
Figure 9. Resolution convergence of the distribution of seeding times for $M_{\rm seed} = 10^5 \, {\rm M}_\odot \, h^{-1}$, $\tilde{M}_{\rm h} = 3000$, and $\tilde{M}_{\rm sf,mp} = 5$. Red, green, and black lines in the upper panels correspond to $L_{\rm max} = 10, 11,$ and 12, respectively. The left-hand panel corresponds to the baseline + gas spin criterion; the right-hand panel corresponds to baseline + LW flux criterion for $J_{\rm crit} = 50 J_{21}$. Green and black lines in the lower panels show the ratios between $L_{\rm max} = 11$ versus 10 and $L_{\rm max} = 12$ versus 11, respectively. When the gas spin criterion is applied, the simulations are reasonably well converged at $L_{\rm max} \geq 11$. When the LW flux criterion is applied, there is reasonable convergence at $z \sim 18$–20. However, at $z \lesssim 17$, the seeding is significantly more suppressed at $L_{\rm max} = 12$ compared to $L_{\rm max} = 11$; this is due to relatively stronger metal enrichment at $z \lesssim 17$ for $L_{\rm max} = 12$, which was also seen in fig. 19 of Bhowmick et al. (2021).

criterion. Secondly, the gas spin criterion does not impact the peak epoch of seed formation, but the LW flux criterion pushes the peak epoch of seed formation to higher redshifts. Thirdly, the LW flux criterion preferentially suppresses seeding in lower mass haloes (at fixed redshift), whereas the impact of the gas spin criterion is broadly similar for all halo masses. This is primarily because halo mass does not have a significant correlation with gas spin, but it has a positive correlation with LW flux.

Due to the lack of correlation between halo mass and gas spin, the gas spin and LW flux criteria tend to impact seeding independently of each other. As an example, the gas spin criterion suppresses seeding by factors of $\sim$6 *regardless* of whether an LW flux criterion is applied. This can be seen by comparing the solid and dashed lines in the upper panels of Fig. 8. Therefore, when both the gas spin and LW flux criteria are applied and compared against the baseline model, the suppression of seeds is a simple product of the contributions from each of two criteria, which amounts to factors of $\sim$240 and $\sim$120 for seed masses of 1.25×10^4 and $1 \times 10^5 \, {\rm M}_\odot \, h^{-1}$, respectively.

3.3.1 Seeding at higher resolution zooms

We have thus far largely focused on $L_{\rm max} = 11$ simulations. In Bhowmick et al. (2021), we had shown that that the $L_{\rm max} = 11$ results are well converged for the baseline seeding model. However, we had also seen that making the seeding criteria more restrictive (for e.g. increasing $\tilde{M}_{\rm sf,mp}$) can reduce the rate of convergence. It is therefore instructive to also look at how the gas spin and LW flux criteria impact our resolution convergence; this is shown in Fig. 9 for $M_{\rm seed} = 10^5 \, {\rm M}_\odot \, h^{-1}$. We first note that adding the gas spin criteria does not significantly impact the resolution convergence; the results are convergent to within factors of $\sim$1.5. However, when an LW flux criterion is added with $J_{\rm crit} = 50 J_{21}$, the resolution convergence is significantly impacted at all but the highest redshifts. At $z \sim 17$–20, the $L_{\rm max} = 11$ and 12 results for the number of seeds are reasonably

well converged; however, at $z \lesssim 17$, seeds are much more strongly suppressed for $L_{\rm max} = 12$ compared to $L_{\rm max} = 11$.

We also look at the resolution convergence of the LW flux distributions in Appendix A. There, we find that the LW fluxes converge significantly more slowly within dense, metal-poor gas cells, as compared to a general gas cell (particularly for $\gtrsim 50 J_{21}$). Nevertheless, we still find that the LW fluxes do approach convergence; therefore, we expect the seeding rates to continue converging for even higher resolutions (albeit slowly compared to the baseline seed model).

To explain the slower convergence rates of models with an LW flux criterion at $z \lesssim 17$, we recall that Bhowmick et al. (2021) (see fig. 19) found that the resolution convergence of metal enrichment at $z \lesssim 17$ is slower than that of star formation. More specifically, they had found that while the total amount dense gas mass is well converged to within ~ 20 per cent, the total dense, metal-poor gas mass was approximately two to three times smaller in $L_{\rm max} = 12$ compared to $L_{\rm max} = 11$. Due to the faster metal enrichment in $L_{\rm max} = 12$, a significantly larger fraction of LW-illuminated gas cells ($\gtrsim 50 J_{21}$) become metal enriched in $L_{\rm max} = 12$, compared to $L_{\rm max} = 11$. Therefore, applying an LW flux criterion with $J_{\rm crit} \gtrsim 50 J_{21}$ tends to push seed formation to occur in regions that are metal-poor at $L_{\rm max} = 11$, but metal enriched at $L_{\rm max} = 12$. This overall leads to a significant slow-down of resolution convergence. Pushing to higher resolutions would require a tremendous amount of computing time, memory, and storage. Therefore, we continue exploring the trends in BH seeding within the LW flux criterion for $L_{\rm max} = 11$ simulations, but we carefully account for the resolution dependence of our results when drawing conclusions. As we shall see, our main conclusions drawn from the $L_{\rm max} = 11$ runs remain unchanged for $L_{\rm max} = 12$.

3.4 Varying SMBH seed masses

We finally look at the implications of the foregoing results on the predictions of merger rates, BH masses, and luminosities of $z > 7$ BHs at different seed masses (forming in haloes with different total masses and dense, metal-poor gas masses).

Fig. 10 shows the number of seeds formed in haloes of different masses for 1.25×10^4, 1×10^5, and $8 \times 10^5 \, {\rm M}_\odot \, h^{-1}$ seeds. When only the baseline criteria (upper left-hand panel of Fig. 10) are applied, the distributions are very steep, and the vast majority of the seeds are forming very close to our selected halo mass threshold ($\tilde{M}_{\rm h} = 3000$). This continues to be true even when the gas spin criterion is added (upper right-hand panel of Fig. 10), due to the weak correlation between halo mass and gas spin. However, when the LW flux criterion is added with $J_{\rm crit}/J_{21} = 50$ and 100 (lower and middle panels of Fig. 10), we can clearly see that the slopes of the distributions become significantly flatter. In other words, seed formation is enhanced in higher mass haloes and suppressed in lower mass haloes. This is because the correlation between halo mass and LW flux requires haloes to accumulate a higher mass before seeding a BH. This essentially explains why the $1.25 \times 10^4 \, {\rm M}_\odot \, h^{-1}$ seeds have a somewhat stronger suppression than $1 \times 10^5 \, {\rm M}_\odot \, h^{-1}$, when compared to the baseline seed model. As a result, the relative excess of $1.25 \times 10^4 \, {\rm M}_\odot \, h^{-1}$ seeds compared to $1 \times 10^5 \, {\rm M}_\odot \, h^{-1}$ seeds is only by factors of $\sim$5 for $J_{\rm crit}/J_{21} = 50$ and 100, in contrast to factors of $\sim$20 enhancement for low-mass seeds in the baseline seed model.

The above trends are reflected in the BH merger rates for different seed masses shown in Fig. 11. In the presence of only the baseline criteria and gas spin criterion (upper panels of Fig. 11), merger rates of $1.25 \times 10^4 \, {\rm M}_\odot \, h^{-1}$ seeds are $\sim$10 and $\sim$100 times higher

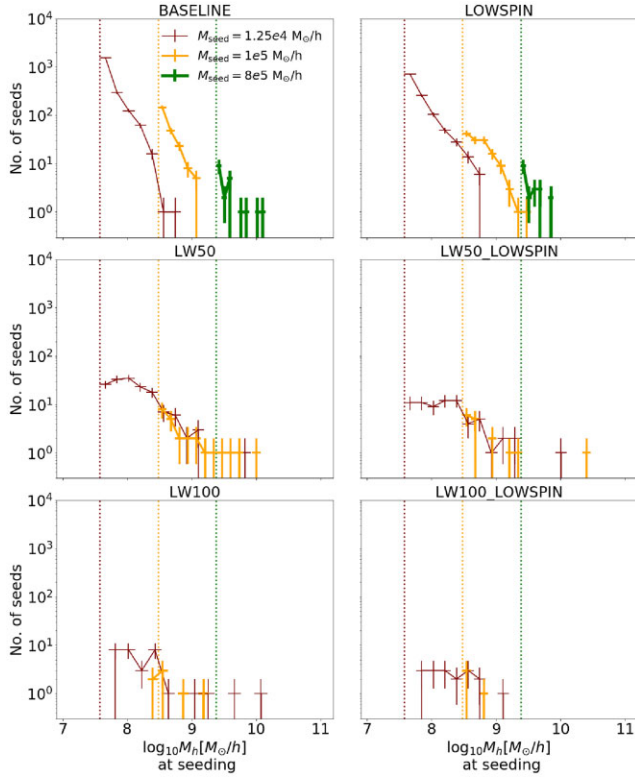**Figure 10.** Number of seeding events in various bins of host halo masses for models with $M_{\text{seed}} = 1.25 \times 10^4$, 1×10^5, 8×10^5 $\text{M}_\odot\,h^{-1}$. The vertical dotted lines show the minimum halo mass for seeding ($\tilde{M}_{\text{h}} \times M_{\text{seed}}$). In the upper left-hand panel, we apply only the baseline criteria for halo mass ($\tilde{M}_{\text{h}} = 3000$) and star-forming, metal-poor gas mass ($\tilde{M}_{\text{sf,mp}} = 5$). In the upper right-hand panel, we additionally apply the gas spin criterion. In the middle and lower left-hand panels, we additionally apply the LW flux criterion with $J_{\text{crit}} = 50$ and $100J_{21}$, respectively. Lastly, the middle and lower right-hand panels apply both the gas spin and LW flux criteria with $J_{\text{crit}} = 50$ and $100J_{21}$, respectively. When only the baseline criteria and gas spin criterion are applied, the distributions are very steep, and the majority of seeds form in haloes close to the minimum mass threshold. When the LW flux criterion is added, the distributions become significantly more flat, i.e. the seeding is strongly suppressed in lower mass haloes ($\lesssim 5 \times 10^8$ $\text{M}_\odot\,h^{-1}$) and enhanced in higher mass haloes ($\gtrsim 5 \times 10^8$ $\text{M}_\odot\,h^{-1}$) compared to the baseline criterion. Due to the positive correlation between LW flux and halo mass, adding an LW flux criterion pushes seed formation to happen in more massive haloes. As a result, formation of the lowest mass (1.25×10^4 $\text{M}_\odot\,h^{-1}$) seeds is more strongly suppressed than 1×10^5 $\text{M}_\odot\,h^{-1}$ seeds.

compared to the merger rates for 1×10^5 and 8×10^5 $\text{M}_\odot\,h^{-1}$ seeds, respectively. When the LW flux criterion with $J_{\text{crit}} = 50J_{21}$ is added (middle panels of Fig. 11), merger rates are generally suppressed by factors of ~60–100 compared to the baseline criterion. Additionally, because the LW flux criterion preferentially suppresses low-mass seed formation, we find that while 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds still have the highest merger rates, they are only a factor of ~4 higher than those of 1×10^5 $\text{M}_\odot\,h^{-1}$ seeds.

Further increasing J_{crit} to $100J_{21}$ (lower panels of Fig. 11) causes the merger rates to be very low overall; there are only a handful of $z \gtrsim 7$ mergers for 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds, and no mergers amongst 1×10^5 $\text{M}_\odot\,h^{-1}$ seeds. Given that the inferred values of J_{crit} for DCBHs are much higher ($\gtrsim 1000J_{21}$) in the literature, our results imply that mergers of DCBHs would be rare and challenging for LISA to detect. Lastly, note that at these redshifts, mergers are
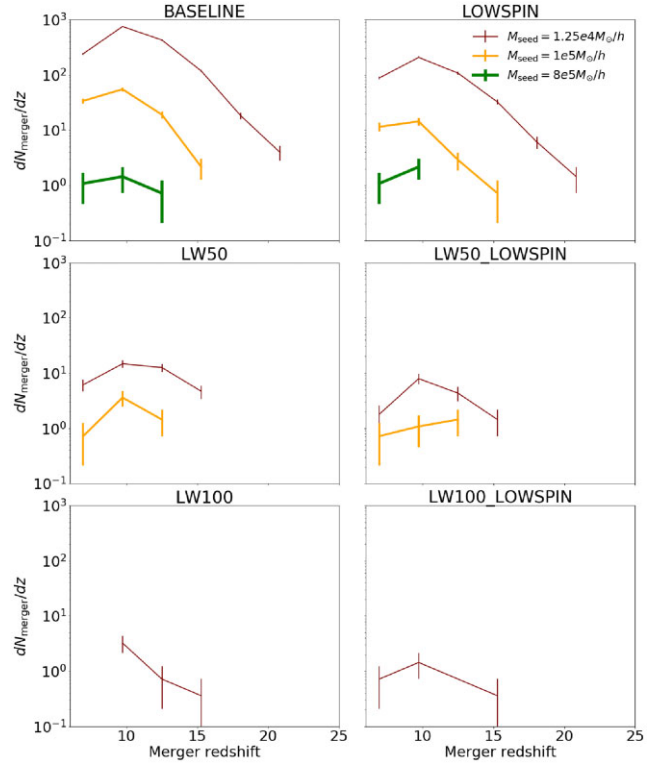
Figure 11. Comparison between BH merger rates in different seeding models, in the same format as Fig. 10. When the gas spin criterion is applied, merger rates are overall suppressed by factors ~6, and 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds merge ~10 (~100) times more frequently than 1×10^5 $\text{M}_\odot\,h^{-1}$ (8×10^5 $\text{M}_\odot\,h^{-1}$) seeds. When an LW flux criterion with $J_{\text{crit}} = 50J_{21}$ is applied, merger rates are overall suppressed by factors of ~60–100. Because lower mass seed formation is preferentially suppressed by the LW flux criterion, the merger rates for 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds are still higher than the merger rates for larger seeds, but only by factors of ~4. When $J_{\text{crit}} = 100J_{21}$, it leads to only a handful of mergers for 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds, and no mergers for 1×10^5 $\text{M}_\odot\,h^{-1}$ seeds.

the primary channel for BH growth in our models (see Bhowmick et al. 2021 or more details); this is largely because the accretion rate scales as M_{bh}^2, which makes it difficult for low-mass BHs to grow efficiently. Therefore, it is the merger rates that primarily determine the resulting final BH masses produced by the different seeds.

The final BH masses at $z = 7$, 11, and 14 produced by 1.25×10^4, 1×10^5, and 8×10^5 $\text{M}_\odot\,h^{-1}$ seeds are shown in Fig. 12 for our models with different combinations of baseline seeding criteria, gas spin criterion, and LW flux criterion. When only the baseline seeding criteria are applied (first row of Fig. 12), we find that seed masses of 1.25×10^4, 1×10^5, and 8×10^5 $\text{M}_\odot\,h^{-1}$ grow via mergers to produce BH masses up to 10^7 $\text{M}_\odot\,h^{-1}$ at $z \sim 7$–11, reiterating the results from Bhowmick et al. (2021). This continues to be true when the gas spin criteria are added (second row of Fig. 12), and directly follows from the results of Figs 10 and 11. When the LW flux criterion is added (third, fourth, and fifth rows of Fig. 12), the merger-driven growth is suppressed so much that even for $J_{\text{crit}} = 50J_{21}$, neither 1.25×10^4 nor 1×10^5 $\text{M}_\odot\,h^{-1}$ seeds are able to form SMBHs of masses $\gtrsim 10^6$ $\text{M}_\odot\,h^{-1}$ by $z = 7$ in our simulation volume. Lastly, due to the stronger suppression of seed formation and merger rates of lower mass seeds for $J_{\text{crit}}/J_{21} = 50$ and 100, we see that the lowest mass 1.25×10^4 $\text{M}_\odot\,h^{-1}$ seeds end up producing slightly smaller final BH masses (by factors of ~2–4) compared to 1×10^5 $\text{M}_\odot\,h^{-1}$

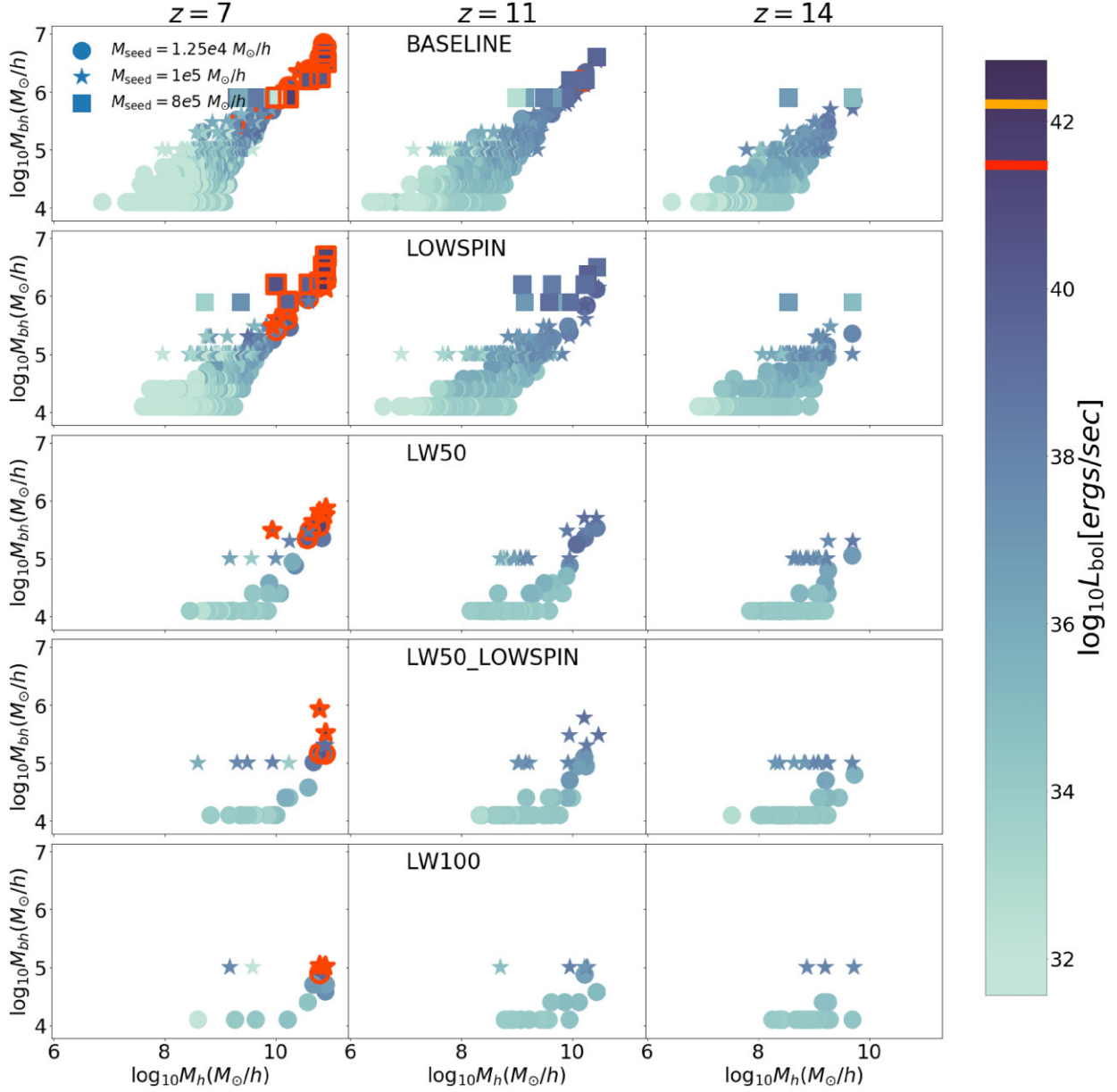**Figure 12.** Halo mass versus total BH mass relation for $M_{\rm seed} = 1.25 \times 10^4,\ 1 \times 10^5,\ 8 \times 10^5\ {\rm M_\odot}\ h^{-1}$. The data points are colour coded by the BH luminosity. Only those haloes are shown where <1 per cent of the total mass is contaminated by low resolution DM particles. The left- to right-hND panels correspond to different redshift snapshots. In the first row, we only apply the baseline criteria for halo mass ($\tilde{M}_{\rm h} = 3000$) and star-forming, metal-poor gas mass ($\tilde{M}_{\rm sf,mp} = 5$). In the second row, we additionally apply the gas spin criterion. In the third row, we apply the LW flux criterion with $J_{\rm crit} = 50 J_{21}$, and we include both the LW flux and the gas spin criteria in the fourth row. In the fifth row, we apply the LW flux criterion with $J_{\rm crit} = 100 J_{21}$. The red and orange markers on the colour bar correspond to the detection limit of Lynx at $z = 7$ and 11, respectively; this is assumed to be 1×10^{-19} erg cm^{-2} s^{-1} in the 2–10 keV band for a survey area of 360 arcmin^2 (Griffin et al. 2020). The required bolometric correction is adopted from Vasudevan & Fabian (2007). The points that are highlighted in red correspond to objects that surpass the Lynx detection limit. When the baseline and gas spin criteria are applied, BHs grow to $10^7\ {\rm M_\odot}\ h^{-1}$ for all the seed masses. When the LW flux criterion is added, $8 \times 10^5\ {\rm M_\odot}\ h^{-1}$ are absent, and the $1.25 \times 10^4,\ 1 \times 10^5\ {\rm M_\odot}\ h^{-1}$ seeds cannot grow to the supermassive regime ($\gtrsim 10^6\ {\rm M_\odot}\ h^{-1}$) due to the absence of mergers.

seeds at $z \sim 7$–11 (although statistics are limited). Recall that $8 \times 10^5\ {\rm M_\odot}\ h^{-1}$ seeds are completely absent for $J_{\rm crit}/J_{21} = 50$ and 100.

Finally, we look at the BH luminosities produced by $1.25 \times 10^4,\ 1 \times 10^5,$ and $8 \times 10^5\ {\rm M_\odot}\ h^{-1}$ seeds (colour coded in the data points of Fig. 12). These luminosities were estimated from the BH accretion rates using equation (4). For models with only the baseline seeding criteria and gas spin criteria, all three seed masses produce BHs reaching luminosities of up to $\sim 10^{42}$ and $\sim 10^{43}$ erg s^{-1}

at $z = 11$ and 7, respectively. When the LW flux criteria with $J_{\rm crit} = 50$ and $100 J_{21}$ are applied, the luminosities (at fixed halo mass) drop by a factor of ~ 10 and 100, respectively, compared to the baseline criterion (due to the drop in BH masses). We also compare these luminosities to the detection limit of Lynx, which is 1×10^{-19} erg cm^{-2} s^{-1} in the 2–10 keV band for a survey area of 360 arcmin^2 (marked in the colour-bar of Fig. 12 for $z = 7$, 11). Note that our results here are subject to theoretical uncertainties

in our BH accretion model as well as the bolometric corrections, which are adopted from Vasudevan & Fabian ([2007](#)). At $z \geq 11$, even for the baseline criterion, there are no BHs above the Lynx detection limit. At $z = 7$, where somewhat lower luminosities can be detected, we do have detectable BHs; but in the presence of LW flux criterion with $J_{crit}/J_{21} = 50$ and 100, their number reduces to only a handful. Given the much higher J_{crit} values of $\gtrsim 1000 J_{21}$ inferred in the literature, our results suggest that Lynx will not find any detectable DCBHs within regions with overdensities similar to or lower than ZOOM_REGION_z5. In future work, we plan to explore the detectability of DCBHs in more extreme cosmological regions.

The key takeaway is that even for relative low values of J_{crit} ($\gtrsim 50 J_{21}$), our simulations with LW flux criteria fail to produce BHs in the supermassive regime ($\gtrsim 10^6$ M$_\odot$ h^{-1}) by $z \sim 7$. Seeds with 8×10^5 M$_\odot$ h^{-1} completely fail to form; 1.25×10^4 and 1×10^5 M$_\odot$ h^{-1} seeds do form but are not able to grow to the supermassive regime. The growth is further suppressed at higher resolutions, where even fewer seeds form. We again emphasize that the foregoing results are specific to our underlying assumptions, including Bondi accretion, which struggles to grow low-mass BHs at early times due to the $\sim M_{bh}^2$ scaling of the accretion rate. Accretion rates are decreased further due to the fact that for these early protogalaxies, the halo centres (where BHs are repositioned to) may be offset from the densest gas within the halo by distances up to ~ 10 kpc h^{-1}. Additionally, our conclusions do not necessarily apply to the regime of the observed $z \gtrsim 7$ quasars with BH masses up to $\sim 10^9$ M$_\odot$ h^{-1}. This is because high-z quasars are expected to reside in much more extreme regions than our zoom volume, where accretion will have a more significant (and potentially dominant) contribution. This means that our conclusions may change when our models are applied to these extreme regions, and do not yet rule out DCBH seeds as progenitors of $z \gtrsim 7$ quasars; we are exploring this in an ongoing work.

4 SUMMARY AND DISCUSSION

In this work, we quantify the impact of gas spin and LW flux-based seeding conditions on the $z \geq 7$ SMBH populations using cosmological hydrodynamical zoom simulations, and we assess the implications of our results for DCBH seed formation.

The zoom region was selected to produce a target halo of mass 3.5×10^{11} M$_\odot$ h^{-1} at $z = 5$ (corresponding to a peak height of $\nu = 3.3$). We then start with a set of baseline seeding criteria as outlined in Bhowmick et al. ([2021](#)) to ensure that seeds are formed only in pristine haloes with *dense gas* i.e exceeding the star formation threshold of 0.1 cm^{-3}: BH seeding sites are required to have a minimum threshold of total halo mass ($3000 M_{seed}$) and dense, metal-poor gas mass ($5 M_{seed}$). The baseline criteria enforces seeding to take place only in haloes that have grown significantly (by factors of $\gtrsim 4$–10, depending on the seed mass) since crossing the atomic cooling threshold ($\sim 10^7$ M$_\odot$ h^{-1}). These haloes have a prior history of star formation and metal enrichment. However, metals fail to pollute the entire halo, leaving behind pockets of dense, metal-poor gas embedded within star-forming regions. These dense, metal-poor, LW-illuminated pockets have gas masses ranging from $\sim 10^5$–10^6 M$_\odot$ h^{-1}.

We then add the gas spin and LW flux criteria, and focus on their impact on seed formation and the resulting $z \gtrsim 7$ SMBH populations. These are described as follows:

(i) *Gas spin criterion*: The dimensionless spin angular momentum (λ) of the gas in the host halo must be less than the minimum value (λ_{max}) required for the gas disc to be gravitationally stable.

(ii) *LW flux criterion*: The minimum threshold ($5 M_{seed}$) for dense, metal-poor gas mass within host haloes must also be illuminated by LW intensities greater than a critical flux J_{crit}. Star formation is suppressed within all gas cells exposed to the supercritical LW flux.

We explored a wide range of models with the gas spin criterion and LW flux criterion ($J_{crit}/J_{21} = 10, 50,$ and 100) using seed masses of 1.25×10^4, 1×10^5, and 8×10^5 M$_\odot$ h^{-1}. This exploration was carried out at gas mass resolutions of $\sim 10^4$ M$_\odot$ h^{-1} within our zoom region. Our key findings are as follows:

(i) When seeding is limited to haloes with low gas spin ($\lambda < \lambda_{max}$), the overall rates of seed formation are suppressed by factors of ~ 6 for all seed masses, particularly at $z \sim 11$–12 when most seeds form. The suppression is similar for all seed masses / halo masses, because the correlation between halo mass and gas spin is weak. Additionally, the gas spin criterion has a weaker effect at higher redshifts and is negligible at $z \gtrsim 20$.

(ii) The LW flux criterion has a substantially stronger impact (compared to the gas spin criterion) on seed formation rates, even for relatively low values of J_{crit}/J_{21} such as 50 & 100; this restricts seed formation to occur only in haloes (typically $\gtrsim 10^8$ M$_\odot$ h^{-1}) that have enough LW sources to provide the necessary fluxes to halt star formation within dense, metal-poor pockets of gas. For $J_{crit} = 50 J_{21}$, the formation of 8×10^5 M$_\odot$ h^{-1} seeds is completely suppressed, while 1.25×10^4 and 1×10^5 M$_\odot$ h^{-1} seeds are suppressed by factors of ~ 40 and ~ 20, respectively. The formation of lower mass seeds in lower mass haloes is preferentially suppressed, because higher mass haloes have more star-forming gas and are therefore more likely to provide the critical LW flux to the metal-poor pockets.

(iii) When both the gas-spin and LW flux criteria ($J_{crit} = 50 J_{21}$) are imposed (in addition to the baseline model), seed formation is even more strongly suppressed. Relative to the baseline model, seeding events are suppressed by factors of ~ 240 and ~ 120 for seed masses of 1.25×10^4 and 1×10^5, respectively.

(iv) Merger rates for all seed masses are suppressed by factors of ~ 6 when seeding is only limited by the gas spin criterion and not limited by an LW flux criterion. In this case, lower mass (1.25×10^4 M$_\odot$ h^{-1}) seeds merge ~ 10 (~ 100) times more frequently than 1×10^5 M$_\odot$ h^{-1} (8×10^5 M$_\odot$ h^{-1}) seeds. In contrast, when the seeds are limited to haloes with LW fluxes $J > J_{crit} = 50 J_{21}$, the merger rates are suppressed by factors of ~ 60–100 compared to the baseline criterion. 1.25×10^4 M$_\odot$ h^{-1} seeds are suppressed somewhat more strongly, but still merge approximately four times more frequently than 1×10^5 M$_\odot$ h^{-1} seeds. With a higher J_{crit} value of $100 J_{21}$, there are only a handful of mergers for 1.25×10^4 M$_\odot$ h^{-1} seeds and none for 1×10^5 and 8×10^5 M$_\odot$ h^{-1} seeds.

(v) When only the baseline seeding criteria and gas spin criterion are applied, all seed masses (1.25×10^4, 1×10^5, and 8×10^5 M$_\odot$ h^{-1}) form SMBHs up to masses of $\sim 10^7$ M$_\odot$ h^{-1} at $z \sim 7$–11. With the addition of an LW flux criterion, due to the absence of 8×10^5 M$_\odot$ h^{-1} seeds and lack of mergers among 1.25×10^4 and 1×10^5 M$_\odot$ h^{-1} seeds, none of the BHs reach the supermassive regime ($\gtrsim 10^6$ M$_\odot$ h^{-1}) by $z \sim 7$ in our simulations.

Our results for the gas spin criterion are reasonably well converged at the fiducial gas mass resolutions of $\sim 10^4$ M$_\odot$ h^{-1}. However, when the LW flux criterion ($J_{crit} \geq 50 J_{21}$) is added, the resolution convergence is substantially slower. More specifically, at higher resolutions (gas mass resolutions of $\sim 10^3$ M$_\odot$ h^{-1}), the LW flux

criterion produces an even stronger suppression of seeding at $z \lesssim 17$. This is primarily driven by more rapid metal enrichment at higher resolutions. Never the less, we expect our results to continue to converge at even higher resolutions. Lastly, we also note that despite the slower resolution convergence, the main qualitative conclusions drawn at the fiducial resolution remain unchanged at higher resolutions. These are summarized in the following paragraph.

Overall, we find that both the gas spin and LW flux criteria significantly impact BH seed formation. The LW flux criterion tends to have a much stronger impact. Even for critical fluxes as low as $50J_{21}$, we see a complete absence of 8×10^5 $M_\odot\,h^{-1}$ seeds and a drastic suppression in 10^4–10^5 $M_\odot\,h^{-1}$ seeds; as a result, no BHs grow to the supermassive ($\gtrsim 10^6$ $M_\odot\,h^{-1}$) regime by $z \sim 7$. Recall again that for realistic galaxy spectra at these redshifts, the inferred values of $J_{\rm crit}$ are much higher ($\sim 1000J_{21}$) compared to the values adopted in this work. It is clear from our results that for such high $J_{\rm crit}$, a larger or more highly biased cosmological volume would be required to model seed formation. Therefore, our findings agree with the general consensus that conditions for DCBH seed formation are very restrictive (e.g. Inayoshi et al. 2020, and references therein). Without a more significant contribution to BH growth from gas accretion, it would be challenging to explain a sizable majority of $z > 7$ SMBHs solely using DCBH channels.

Our findings are quantitatively consistent with some of the previous works, but have differences compared to others. For instance, the impact of gas spin predicted by our model is similar to that of Lodato & Natarajan (2006). In terms of the LW flux criterion, we predict a similar impact as the hydrodynamic simulations of H16. Note however that due to a relatively small zoom volume, our results are not as statistically robust for the highest fluxes ($\gtrsim 100J_{21}$) compared to the largest volume of H16 (142 Mpc h^{-1} per side). We however predict a somewhat stronger impact compared to Dunn et al. (2018). This may be because our seeding criteria becomes significantly more strict for higher $J_{\rm crit}$ since we require a much larger minimum mass of dense, metal-poor, LW-illuminated gas to insert seeds; in contrast, Dunn et al. (2018) impose a similar criteria but only for one individual gas particle at mass resolutions similar to ours. Semi-analytic models (Agarwal et al. 2012, 2014; Dijkstra et al. 2014) predict a substantially stronger impact of LW flux compared to hydrodynamic simulations; this can be attributed to differences in the modelling of star formation, metal enrichment, and LW radiation (as demonstrated by H16). Regardless of the quantitative differences, all of these works agree that both gas spin and LW flux can have a substantial impact on seed formation. Our work additionally demonstrates that the LW flux criterion tends to be more restrictive compared to the gas spin criterion.

Our results have several potential implications for upcoming observational facilities. The fact that the LW flux criterion pushes seed formation to higher mass haloes may have two important observational consequences. First, higher mass haloes are more rare, so the resulting merger rates are very low; this implies that LISA may find it much more challenging to detect mergers originating from DCBH channels, compared to other channels (e.g. Pop III). Secondly, for the events that are detected by LISA, follow-up electromagnetic observations of their host galaxies using JWST may be useful for constraining their seeding origins. Electromagnetic observations may also be able to distinguish other signatures of the DCBH seeding models presented here.

The AGN luminosities drop by factors of ~ 10 and ~ 100 for $J_{\rm crit} = 50$ and $100J_{21}$, respectively, compared to the baseline criterion. As a result, for $J_{\rm crit} = 50$ and $100J_{21}$, our zoom volume produces very few objects that would be detectable with Lynx. We expect the

suppression in luminosities to be even higher for larger values of $J_{\rm crit}$. Larger uniform volume simulations will be required to constrain the high-redshift AGN luminosity function resulting from our seed models, which we will explore in future work. Overall, our results suggest that if DCBHs indeed form only in the presence of very high LW fluxes ($\gtrsim 1000J_{21}$), future electromagnetic observational facilities will find it challenging to detect DCBHs.

Our results are strongly influenced by the fact that at these early epochs, BH growth is dominated by mergers, and there is very little growth due to gas accretion. This is a well-known issue in simulating the growth of low-mass BH seeds, which owes in large part to the $M_{\rm BH}^2$ scaling of the Bondi–Hoyle accretion model. A variety of alternate accretion models exist in the literature (Pelupessy, Di Matteo & Ciardi 2007; Booth & Schaye 2009; Tremmel et al. 2017; Zhu et al. 2020), but the $M_{\rm BH}^2$ scaling is generic to all models in which the gas capture radius is assumed to scale with BH mass.

Alternate accretion models exist that can have much smaller scaling exponents for the accretion rate versus BH mass (e.g. $\propto M_{\rm bh}^{1/6}$ for accretion driven by stellar gravitational torques; Hopkins & Quataert 2011; Anglés-Alcázar et al. 2017; Davé et al. 2019). If such a model can be reliably applied in the high-redshift regime, this might significantly boost early growth. Additionally, we note that both accretion rates and merger rates are likely to be influenced by the BH repositioning scheme, which causes the BHs to rapidly sink to the halo centres. Recent work incorporating more realistic subgrid prescriptions for modelling unresolved dynamical friction has been shown to increase merger times and decrease accretion rates (Tremmel et al. 2017; Bellovary et al. 2021). We plan to explore the impact of BH dynamics on early seed growth in future work.

BH accretion rates can also be impacted by the modelling of BH dynamics. Recall that the BHs are repositioned to the halo centre (minimum potential). But in these early proto-galaxies, the halo centre does not always coincide with the densest gas cell. This makes the BHs wander around (up to distances ~ 10 kpc h^{-1}) the regions with highest gas density, which further reduces the accretion rates. At the same time, recent works (Tremmel et al. 2018; Chen et al. 2021; Ma et al. 2021; Ni et al. 2021; Ricarte et al. 2021) that implement more realistic BH dynamics models find that BHs may be offset from the halo centre for a substantial amount of time, particularly for clumpy high-z galaxies. This would also lead to reduction or delays in BH mergers and slow down the merger-driven BH growth.

We again emphasize that molecular (H_2) cooling, which is a crucial component for DCBH formation, is not explicitly included in our model. This artificially suppresses star formation in mini-haloes ($M_{\rm h} \sim 10^5$–10^6 $M_\odot$); since mini-haloes are progenitors of atomic cooling haloes ($T_{\rm vir} \gtrsim 10^4$ K or $M_{\rm h} \gtrsim 10^7$ $M_\odot$), this could lead to an artificially higher number of metal-poor haloes that cross the atomic cooling threshold and potentially overestimate the number of seeds formed. However, note that our seeds are largely forming in $\sim 10^8$–10^{10} $M_\odot\,h^{-1}$ haloes wherein a significant amount of time has passed since they crossed the atomic cooling threshold and had their first burst of star formation. Yet, we see that they do not get completely polluted with metals, which creates the opportunity for seed formation to occur within dense, metal-poor pockets. For these haloes, our underlying galaxy formation model (Springel & Hernquist 2003) is well calibrated to account for the delay in star formation caused at the mini-halo stage. That being said, we do note that a further reduction in the seed mass or the halo mass threshold could cause seeds to form closer to the atomic cooling threshold; in this case, the lack of star formation in mini haloes would be a more serious issue. In the future, we plan to assess this in more

detail in future work with galaxy formation models that do include H_2 cooling.

Related to the above, our seed formation scenario is somewhat distinct from what has been explored in previous works. For example, a commonly considered scenario ('synchronized pair scenario') is that a halo with no prior star formation history forms a DCBH as soon as it crosses the atomic cooling threshold, if it receives LW radiation from a nearby star-forming halo that has also crossed the threshold within the last ~5 Myr (Visbal et al. 2014; Regan et al. 2017; Lupi et al. 2021). In contrast, our simulations probe DCBH forming conditions in haloes that have grown well past the atomic cooling threshold; these haloes have a prior star formation and metal enrichment history but still contain pockets of dense, metal-poor gas. These pockets form seeds upon receiving LW radiation from surrounding star-forming regions within the same halo. This additional scenario also indicates that DCBHs may be slightly less rare than previously thought. Future works with explicit molecular cooling recipes will enable us to also probe DCBH formation in haloes close to the atomic cooling threshold via the synchronized pair scenario.

We also emphasize that the results of this work should not be extrapolated to the regime of observed high-redshift quasars, since they are likely a tiny fraction of the overall SMBH population forming in regions much more overdense than our zoom volume. In such extreme regions, we can expect gas accretion to have an increasingly significant (and potentially dominant) role in the BH growth. In future work, we plan to explore more extreme overdense regions, which could probe much higher J_{crit} values ($\gtrsim 1000 J_{21}$) that are representative of actual DCBH formation conditions based on radiation hydrodynamic simulations and one-zone chemistry models (Shang et al. 2010; Sugimura et al. 2014; Wolcott-Green et al. 2017).

Lastly, while this work is largely motivated by the DCBH seeding channel, it is part of a continued series of studies on the underlying seeding prescriptions, agnostic about the physical channels they may represent. Between this work and Bhowmick et al. (2021), we have now expanded our seeding models to encompass most of the physical properties commonly associated with theoretical gas-dependent BH seed formation channels. These works will serve as a basis for continued development of seeding prescriptions, particularly in the context of large volume uniform simulations.

DATA AVAILABILITY

The underlying data used in this work shall be made available upon reasonable request to the corresponding author.

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APPENDIX A: RESOLUTION CONVERGENCE OF LW INTENSITY CALCULATION

In Section 3.3.1, we found that the resolution convergence of the BH seeding rates between $L_{max} = 11$ and 12 is significantly worse at $z \gtrsim 17$ in the presence of an LW flux criterion with $J_{crit} = 50J_{21}$. Given that the baseline models of Bhowmick et al. (2021) were reasonably well converged for $L_{max} \geq 11$, we find it instructive to look at the resolution convergence of our calculated LW fluxes. Fig. A1 shows the distributions of LW flux values amongst all gas cells (dotted lines) and dense, metal-poor gas cells (solid lines). The LW flux distributions among all gas cells are reasonably well converged between $L_{max} = 11$ and 12. But the convergence of seeding rates depends only on the LW fluxes among dense, metal-poor gas cells. The LW flux distributions among dense, metal-poor gas cells do converge, but significantly more slowly than than the LW flux distributions among all gas cells (solid lines versus dashed lines in Fig. A1); this is particularly true for LW fluxes $\gtrsim 50J_{21}$.

The reason for the slower resolution convergence of LW fluxes among dense, metal-poor gas cells is that metal enrichment at $z \lesssim 17$ occurs faster at $L_{max} = 12$ compared to $L_{max} = 11$. As a result, a significant fraction of the gas that is metal-poor and LW-irradiated in $L_{max} = 11$ simulations has, at the same epoch, already become metal enriched in the $L_{max} = 12$ simulations. Overall, this explains why resolution convergence between $L_{max} = 11$ and 12 of BH seeding is substantially slow in the presence of an LW flux criterion with $J_{crit} = 50J_{21}$; never the less, the convergence of the LW fluxes in Fig. A1 hints that we can expect the seeding rates to continue converging at even higher resolutions ($L_{max} \geq 13$).
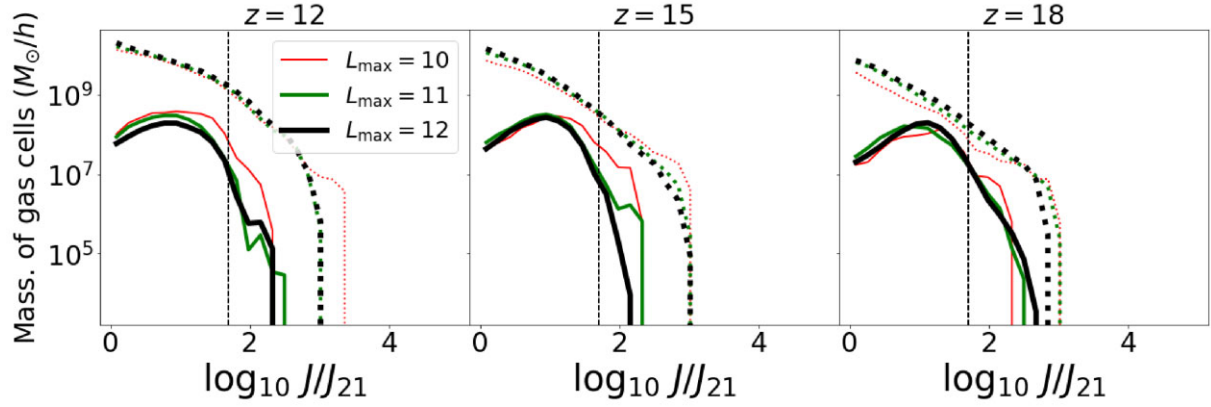
Figure A1. Resolution convergence of the distribution of LW flux values amongst all gas cells (dashed lines) and dense, metal-poor gas cells (solid lines). Red, green, and black lines in the upper panels correspond to $L_{max} = 10, 11,$ and 12, respectively. The flux distributions among all gas cells (dashed lines) are reasonably well converged between $L_{max} = 11$ and 12. The flux distributions among dense, metal-poor gas cells do converge, but at substantially slower rate for $\gtrsim 50 J_{21}$. Since BHs are seeded based on LW fluxes within dense, metal-poor gas cells, resolution convergence of seeding rates at $z \lesssim 17$ is significantly slower.

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