

SpaceQ – Direct Detection of Ultralight Dark Matter with Space Quantum Sensors

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(Dated: December 16, 2021)

Recent advances in quantum sensors, including atomic clocks, enable searches for a broad range of dark matter candidates. The question of the dark matter distribution in the Solar system critically affects the reach of dark matter direct detection experiments. Partly motivated by the NASA Deep Space Atomic Clock (DSAC), we show that space quantum sensors present new opportunities for ultralight dark matter searches, especially for dark matter states bound to the Sun. We show that space quantum sensors can probe unexplored parameter space of ultralight dark matter, covering theoretical relaxation targets motivated by naturalness and Higgs mixing. If an atomic clock were able to make measurements on the interior of the solar system, it could probe this highly sensitive region directly and set very strong constraints on the existence of such a bound-state halo in our solar system. We present sensitivity projections for space-based probes of ultralight dark matter which couples to electron, photon, and gluon fields, based on current and future atomic, molecular, and nuclear clocks.

I. INTRODUCTION

In addition to explaining the dark matter (DM) of the universe, ultralight dark matter (ULDM) can be motivated by naturalness [1, 2], string theory [3–6], and dark energy [7–14]. The “fuzzy”, wavelike nature of such particles can also affect structure formation [15–17]. An important probe of ultralight dark matter arises in precision tests using atomic clocks and other quantum technologies [18–28], which are complementary to interesting astrophysical [29–35], cosmological [36–40], planetary and space probes [41–44].

Space quantum technologies are known to have important practical applications, including the auto-navigation of spacecrafts, relativistic geodesy [45], linking Earth optical clocks [46], secure quantum communications [47], and others. The NASA Deep Space Atomic Clock (DSAC) mission has recently demonstrated a factor of 10 improvement over previous space-based clocks [48], and similar or better sensitivity has been achieved by the other atomic clocks in space [49]. We aim to demonstrate a new window of opportunity to study ultralight dark matter with such technologies, taking advantage of these and upcoming space missions to study DM in environments that are drastically different from that of the Earth.

In this paper, we study an exciting new avenue of probing ultralight dark matter with future high-precision

atomic, molecular, and nuclear clocks¹ in space. The oscillations of the ultralight dark matter field can induce a time-varying contribution to fundamental constants, including the electron mass and fine-structure constant [50, 51]. Exceptional enhancements of DM density that can be enabled by the bound halos present an opportunity for direct DM detection with clocks [52, 53].

We propose a clock-comparison satellite mission with two clocks onboard, to the inner reaches of the solar system to search for the dark matter halo bound to the Sun, probe natural relaxation parameter space, and look for the spatial variation of the fundamental constants associated with a change in the gravitation potential. We show that the projected sensitivity of space-based clocks for detection of Sun-bound dark matter halo exceeds the reach of Earth-based clocks by orders of magnitude. We consider both the projected bounds for the clocks that were already demonstrated, and the novel nuclear and molecular clocks under development. This proposal of a clock-comparison experiment in a variable-gravity environment can test the potential spatial variations of fundamental constants under the change in the gravitational potential [54, 55]. We show that using space-based quantum clocks, one can improve the precision by two orders of magnitudes for this measurement in comparison to similar tests on Earth or near-Earth orbits. We also discuss other new physics searches enabled by clock-comparison experiments in space.

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¹ We sometimes refer to them as *quantum clocks* for simplicity.

Unless otherwise specified, we use the convention of natural units ($\hbar = c = 1$) in this work.

II. QUANTUM CLOCK SEARCHES FOR ULDM

ULDM scalar field couplings to the Standard Model can induce oscillations of fundamental constants, including masses and couplings. Consider the following interaction Lagrangian for a DM scalar field ϕ :

$$\mathcal{L} \supset \kappa \phi \left(d_{m_e} m_e \bar{e} e + \frac{d_\alpha}{4} F_{\mu\nu} F^{\mu\nu} + \frac{d_g \beta_3}{2g_s} G_{\mu\nu}^A G^{A\mu\nu} \right), \quad (1)$$

where e is the electron field, $F^{\mu\nu}$ ($G^{A\mu\nu}$) is the electromagnetic (QCD) field strength, g_s and β_3 are the strong interaction coupling constant and beta function (respectively), and $\kappa = \sqrt{4\pi}/M_P$ with $M_P = 1.2 \times 10^{19}$ GeV. In a DM background field of amplitude $\phi = \phi_0$, the couplings in Eq. (1) induce modification of the electron mass m_e , fine-structure constant α , and strong coupling $\alpha_s \equiv g_s^2/4\pi$, respectively. However, the fundamental oscillatory nature of the ULDM field implies that the contribution to these parameters is oscillatory as well, oscillating at the DM Compton frequency $\omega = m_\phi c^2/\hbar$.

Atomic physics experiments, including atomic clock-comparison tests, have shown great promise to probe these signals. The very low fractional uncertainty in frequency that has been achieved corresponds to similar sensitivity to the oscillatory signals of the form

$$\begin{aligned} \mu(\phi) &\simeq \mu_0 (1 + d_{m_e} \kappa \phi), & \alpha(\phi) &\simeq \alpha_0 (1 - d_\alpha \kappa \phi) \\ \alpha_s(\phi) &\simeq \alpha_{s,0} \left(1 - \frac{2d_g \beta_3}{g_s} \kappa \phi \right), \end{aligned} \quad (2)$$

where $\mu = m_e/m_p$ is the electron-proton mass ratio, and the subscript “0” denotes the central (time-independent) value of μ , α , and α_s . Variation of the strong coupling α_s gives rise to variation of the dimensionless ratio [56, 57]

$$\left(\frac{m_q}{\Lambda_{\text{QCD}}} \right) (\phi) \simeq \left(\frac{m_q}{\Lambda_{\text{QCD}}} \right)_0 (1 - d_g \kappa \phi). \quad (3)$$

where Λ_{QCD} is the QCD scale and m_q is the averaged light quark mass. There are now many dedicated experiments searching for these types of signals [51, 58–64].

Atomic clock accuracy has improved immensely over the past decade, and so too has their ability to test variation of fundamental constants; we review recent work in this field in Section IV. Other probes of ultralight scalar fields include equivalence principle (EP) tests, which do not need to assume anything about the DM density in the vicinity of the experiment, as they search for virtual exchange of ϕ particles that appear as a “fifth force” not proportional to $1/r^2$ (see e.g. [25, 65, 66]). Historically, EP tests have outperformed atomic physics probes across a wide range of ULDM mass parameters, with the exception of very light particles $m_\phi \lesssim 10^{-17}$ eV [62], at least

for generic couplings and under the usual assumption of $\rho_{\text{DM}} = 0.4$ GeV/cm³ for the local density of dark matter. On the other hand, atomic physics probes couple directly to the DM density and, therefore, allow for direct detection. Furthermore, such experiments have the ability to probe bound-state DM in our solar system, as we will explain below, and a space-based clock allows one to probe novel parameter space as well. Future development of the nuclear clock, expected to be $10^4 - 10^5$ times more sensitive to variations of α than all operating atomic clocks, will drastically increase the discovery reach of such experiments. In addition, the nuclear clock has strong sensitivity to m_q/Λ_{QCD} ; for further details, see Section IV.

III. SOLAR SYSTEM HALOS

The local DM density ρ_{DM} is a key parameter dictating experimental sensitivity; on the basis of halo modeling and (weak) local constraints (see below, as well as Appendix A), its value is typically assumed to be $\rho_{\text{DM}} = 0.4$ GeV/cm³. For ultralight particles, the field oscillates coherently on a timescale dictated by the virial velocity $v_{\text{DM}} \simeq 10^{-3}c$, given by $\tau_{\text{coh}} \approx 2\pi(m_\phi v_{\text{DM}}^2/\hbar c^2)^{-1} \simeq 2\pi \times 10^6 \hbar/m_\phi$. However, the possibility that a large density of such fields could become bound to objects in the solar system has been considered, which would give rise to unique signals and strongly modified values for the local DM density and timescale of coherent DM oscillations [52, 53, 67]. Here we focus on the specific case of a bound ULDM halo around the Sun, known as a *solar halo* (SH).²

There are intriguing hints that some density of ULDM would become bound to the Sun. One piece of suggestive evidence arises in numerical simulations of galaxy formation in ULDM with $m_\phi \sim 10^{-22}$ eV, which have recently included the presence of (fixed) baryonic gravitational potential [70]. The simulation suggests that the same relaxation processes that form boson stars in DM-only case can instead form a halo-like configuration, akin to a gravitational atom (analogous to a hydrogen atom ground state with a gravitational potential), in the presence of a baryonic potential. If this holds also at larger m_ϕ , as we will consider below, it implies a plausible formation mechanism for ULDM to become bound to the Sun. It has also been suggested that a SH could form from adiabatic contraction during star formation [67]. In this work, we analyze the consequences of the existence of a SH on atomic clock searches for ULDM, with a focus on possibilities for future missions in space; previous work has focused instead on terrestrial searches (e.g. [52]).

² Note that a SH shares similarities to (though distinct from) a stellar DM basin [68, 69], which is generally formed from heavier particles.

A SH can be thought of as similar to a boson star [71–74], but supported by the external gravitational effect of the host body (the Sun) rather than self-gravity. The radius of a SH takes the form [52]

$$R_\star \simeq \frac{M_P^2}{M_{\text{ext}} m_\phi^2}, \quad (4)$$

where $M_{\text{ext}} = M_\odot$ is the mass of the external host body; note that R_\star is independent of the total mass in the halo M_\star . For ULDM masses of $m_\phi \sim \text{few} \times 10^{-14}$ eV, the radius of a SH is roughly 1 AU (the average orbital radius of the Earth), and R_\star grows as $\propto m_\phi^{-2}$ as m_ϕ mass decreases. Therefore, terrestrial atomic probes are sensitive only to a lower mass range fixed by the requirement $R_\star \gtrsim 1$ AU.

Note that a bound halo around the Earth would modify signals in the higher mass range 10^{-12} eV $\lesssim m_\phi \lesssim 10^{-7}$ eV; we discuss the resulting effects on atomic clocks in orbit around the Earth in Appendix B.

Space-based atomic clocks are notably different from terrestrial ones regarding sensitivity to ULDM probes. Firstly, a space clock would provide a novel method to probe a SH at larger m_ϕ , when the radius of the SH in Eq. (4) is smaller than 1 AU. Secondly, and perhaps more strikingly, the constraints on an SH with a small radius are very weak; if an atomic clock were able to make measurements on the interior region of the solar system, it could probe this highly sensitive range directly and set very strong constraints on the existence of such a halo in our solar system. Current constraints on a SH in our solar system arise from measurements of solar system ephemerides, especially from Mercury, Mars, and Saturn, which are known with very high precision [41]. The resulting maximum mass of a SH, following [52], is of order $10^{-12} M_\odot$ at $m_\phi \simeq 10^{-14}$ eV, and weaker elsewhere; in what follows, we use the full range of gravitational constraints, and we always enforce that $M_\star < M_\odot/2$ as a naive requirement on the total mass in our solar system. See Appendix A for further details.

We also note that the effective coherence time of the oscillations of the bound ULDM field τ_\star is generically larger than that of the virialized DM scenario [52, 53], where $\tau_{\text{DM}} \simeq 10^6/m_\phi$. In a narrow range around $m_\phi \simeq 10^{-13}$ eV, however, $\tau_\star < \tau_{\text{DM}}$ by a factor of few, possibly reducing the sensitivity reach of atomic clock probes by as much as an order of magnitude; we discuss this further in Appendix A.

IV. ATOMIC, MOLECULAR, AND NUCLEAR CLOCKS

To detect ultralight dark matter with high-precision clocks, one measures a frequency ratio of two clocks with different sensitivities to the variation of fundamental constants over a period of time [50]. The discrete Fourier transform of the resulting time series then allows the extraction of a peak at the dark matter Compton frequency,

with an asymmetric lineshape [50, 75, 76]. The lack of such a signal allows one to establish bounds on the DM parameter space. It is also possible to carry out such a measurement with a single clock by comparing the frequency of atoms to the frequency of the local oscillator (i.e., cavity) [62, 77].

The present proposal calls for a two-clock or clock-cavity setup onboard a satellite. It does not require a comparison to Earth-bound clocks. There are several factors one has to consider while selecting clocks for a proposed mission: (1) variation of which fundamental constants do we want to probe and what are the corresponding sensitivity factors; (2) what are the clock stabilities and systematic uncertainties; and (3) the difficulty of making these clocks space-ready.

The dimensionless sensitivity factors K of a pair of clocks translate the fractional accuracy of the ratio of frequencies ν to the fractional accuracy in the variation of the fundamental constant. For example, for the fine-structure constant

$$\frac{\partial}{\partial t} \ln \frac{\nu_2}{\nu_1} = (K_2 - K_1) \frac{1}{\alpha} \frac{\partial \alpha}{\partial t}, \quad (5)$$

where indices 1 and 2 refer to clocks 1 and 2, respectively. If the frequency ratio is measured with relative 10^{-18} precision and $\Delta K \equiv K_2 - K_1 = 1$, then such an experiment will be able to measure the fractional change in α with 10^{-18} precision. If $\Delta K = 10^4$ then the 10^{-18} accuracy of the frequency ratio allows one to detect a change in α at the 10^{-22} level. The sensitivity factors K to α -variation for all atomic clocks can be computed from first principles with high precision [78]. They increase for atoms with heavy nuclei and depend on the electronic configurations of the clock states.

At present, all operating atomic clocks are either based on transitions between the hyperfine substates of the ground state of the atom (microwave clocks: H, DSAC Hg⁺, Rb, Cs) or transitions between different electronic levels (optical clocks: Al⁺, Ca⁺, Sr, Sr⁺, Yb, Yb⁺, and others) [79]. The typical frequencies of the optical clock transitions are $0.4 - 1.1 \times 10^{15}$ Hz, while the frequencies of the microwave clocks are several orders of magnitude smaller, a few GHz. The optical clock frequency is only sensitive to the variation of α , with varying sensitivity factors K . Microwave clocks are sensitive to variation of α and $\mu = m_e/m_p$ ratio (with a sensitivity factor of $K = 1$), and there is also a small sensitivity of microwave clocks to m_q/Λ_{QCD} . The sensitivity to the variation of α of most currently operating atomic clocks are small: $K(\text{Al}^+) = 0.01$, $K(\text{Ca}^+) = 0.1$, $K(\text{Sr}) = 0.06$, $K(\text{Sr}^+) = 0.4$, $K(\text{Yb}) = 0.3$, $K(\text{Yb}^+ \text{ E2}) = 1$, with a notable exception of Yb⁺ clock based on the octuple transition with $K = -6$ [78]. For the microwave Cs clock, $K = 2.83$. The most recent limits on the slow drifts of α and μ are given in [80]. Comparing any optical clock to cavity gives $\Delta K = 1 + K_{\text{clock}}$, where K_{clock} is given above.

There are two characteristics to consider when evaluating the state-of-the-art clocks: stability and uncertainty

[79, 81]. *Stability* is the precision with which we can measure a quantity. It is usually determined as a function of averaging time, since noise is reduced through averaging for many noise processes, and the precision increases with repeated measurements. Probing the resonance using the Ramsey method of separated fields³ in the regime where the stability is limited by fundamental quantum projection noise, a clock instability is limited by [79, 81]

$$\sigma(\tau) \approx \frac{1}{2\pi\nu_0\sqrt{NT_m\min(\tau, \tau_*)}}, \quad (6)$$

where ν_0 is the clock transition frequency, N is the number of atoms or ions used in a single measurement, $T_m \sim 2\pi\delta\nu$ is the maximum possible time of a single measurement cycle (i.e., the free-precession time where $\delta\nu$ is the spectroscopic linewidth of the clock transition), and τ is the averaging period [79, 81]. Generally, T_m is still limited by the clock laser coherence rather than the natural linewidth, which represents a fundamental limit. This formula demonstrates the advantages of the optical clocks over the microwave clocks due to five orders of magnitude increase in the clock transition frequency ν_0 . Note that per Eq. (6), the clock stability is diminished when $\tau < \tau_*$, which becomes relevant at large values of m_ϕ , e.g. $\tau_* \lesssim 1$ day for $m_\phi \gtrsim 10^{-13}$ eV; we explain this in greater detail in Appendix A.

The absolute *uncertainty* of an atomic clock describes how well we understand the physical processes that shift the measured frequency from its unperturbed natural value. Several optical clocks have reached uncertainty at the 10^{-18} level [82–84], while microwave clocks are at the 10^{-16} level [85], which is at the achievable technical limit. There is no apparent technical limit to significant further improvement of the optical clocks [86]. Portable high-precision optical clocks were also demonstrated [87, 88].

We now consider all parameters in Eq. (6) in the context of dark matter detection. All present optical clocks are based on either neutral atoms or singly-charged ions. To achieve high precision, the atoms/ions that serve as the frequency standards have to be trapped, leading to significant differences in atom and ion clock design due to different trapping technologies. Neutral atom clocks are sometimes referred to as “lattice clocks”, as atoms are held in optical lattices, i.e., light potentials created by counterpropagating laser beams. While ions trap technology design is simpler than that of lattice clocks, all of the ion clocks are operating with a single ion, i.e., $N = 1$, leading to lower stability compared to the optical lattice clocks that have $N \sim 1000$. Much larger values of N were recently demonstrated for lattice clocks [86]. Development of multi-ion clocks is in progress [87, 89].

The range of dark matter masses for which the DM frequency signal can be extracted without sensitivity loss depends on parameters of the clock operation T_m and τ and DM coherence time [76]. Generally, one needs to have at least one DM oscillation during the total measurement time τ , losing the sensitivity beyond this point. For high frequencies, one eventually will have multiple dark matter oscillations during free precession (probe) time T_m , leading to a loss of sensitivity. This is particularly significant for this proposal, as the characteristic probe time of $T_m = 1$ sec corresponds to DM mass of 4×10^{-15} eV. This problem can be partially remedied by either reducing T_m (leading to reduced short-term stability) or applying additional “dynamical decoupling” (DD) series of π laser pulses during the clock probe time [60]. DD scheme allows to coherently add the DM signal contribution over the probe time and, therefore, to extract the DM signal that oscillates on a faster timescale than the clock measurement cycle. The DD sequence can be optimized to probe the 10^{-13} eV mass range of specific interest to this work. Here, we assume an ideal case where the clock probes are continuous; realistically, clocks have a “dead time” required to prepare the system, which can be 50% of the entire clock measurement cycle or more. A zero-dead-time clock has been demonstrated with two atomic ensembles [90].

In addition to presently operating clocks, a number of new clocks are being developed, bases on molecules and molecular ions [95, 96], highly-charged ions (HCIs) [97], and ^{229}Th nucleus [98]. A lattice clock based on the $4f^{14}6s6p^3P_0 - 4f^{13}6s^25dJ = 2$ transition in neutral Yb was proposed with $K = 15$ [99]. Molecular clocks are projected to reach 10^{-18} uncertainties [96]. Highly-charged ion clocks and a nuclear clock are estimated to achieve 10^{-19} uncertainties and have much higher sensitivities to α , $K \sim 100$ for HCIs and $K = -(0.82 \pm 0.25) \times 10^4$ [92] for a nuclear clock, with actual sensitivity to be determined with aid of future measurements of nuclear properties. HCI clocks have to operate in a cryogenic 4K environment, complicating space deployment. Nuclear clocks can be operated as a trapped ion or a solid state clock. Molecular clocks provide sensitivity to m_e/m_p variation and a nuclear clock is highly sensitive to hadronic sector, with possible $K = 10^4$ sensitivity to the variation of m_q/Λ_{QCD} [92, 100].

In summary, a wide variety of clocks can be selected for a pair of co-located mission clocks. A very attractive possibility is to use Yb^+ that has two clock transitions in the same ion giving $\Delta K = 7$ [80] (the probe sequence will alternate between two transitions). Such a scheme removes uncertainty due to gravitational potential and temperature differences between clock locations. Development of a two-transition Yb lattice clock proposed in [99] would have the same benefits and provide high stability enabled by thousands of trapped neutral atoms combined with high sensitivity $\Delta K = 15$. Comparing Sr clock [86] to a ultra-stable cavity [62] ($\Delta K = 1$) would utilize extraordinary clock stability but increasing cavity

³ Ramsey scheme involves applying two $\pi/2$ laser pulses with a wait (free precession) time in-between. The $\pi/2$ laser pulse creates a superposition of two clock states.

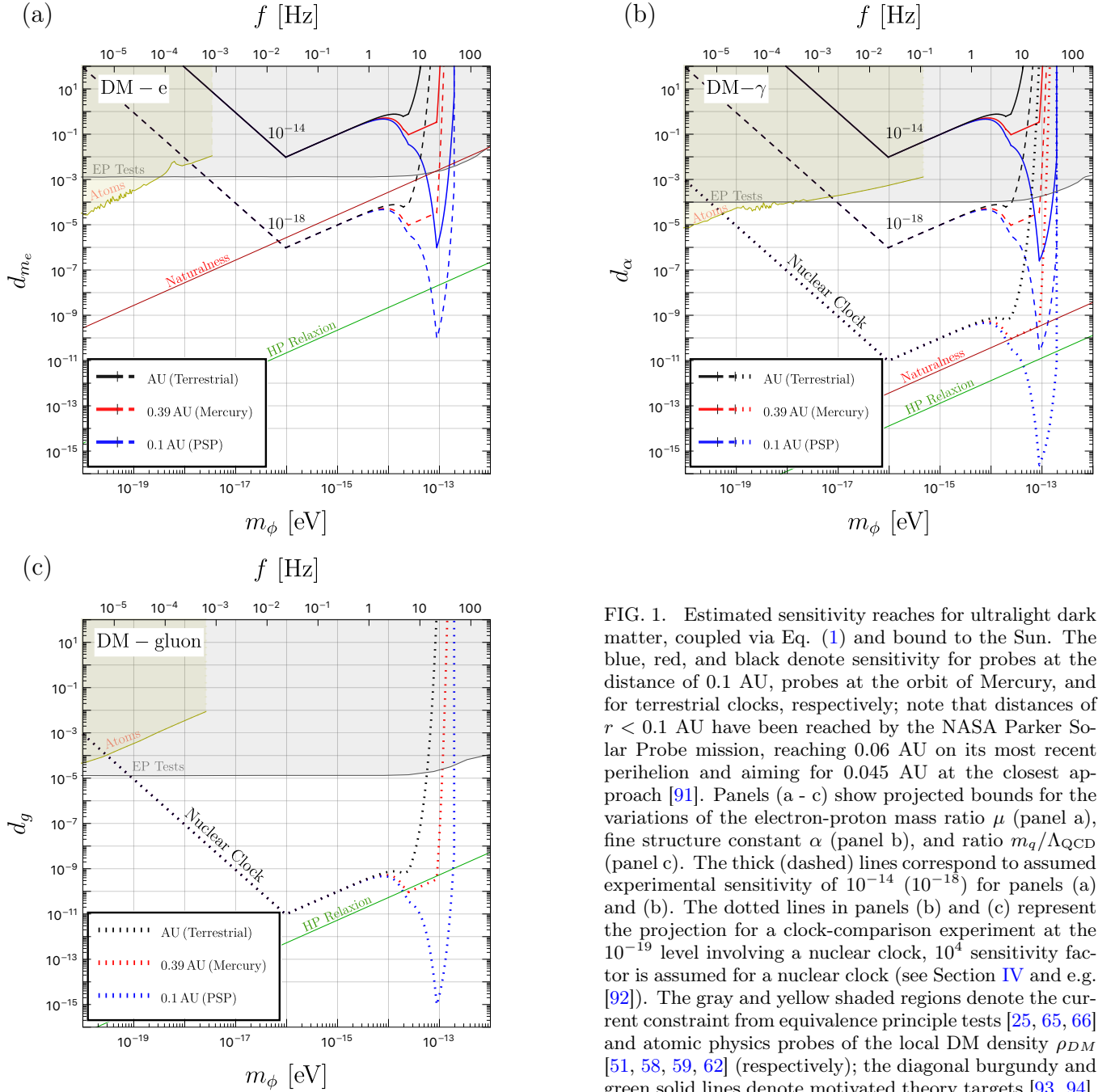


FIG. 1. Estimated sensitivity reaches for ultralight dark matter, coupled via Eq. (1) and bound to the Sun. The blue, red, and black denote sensitivity for probes at the distance of 0.1 AU, probes at the orbit of Mercury, and for terrestrial clocks, respectively; note that distances of $r < 0.1$ AU have been reached by the NASA Parker Solar Probe mission, reaching 0.06 AU on its most recent perihelion and aiming for 0.045 AU at the closest approach [91]. Panels (a - c) show projected bounds for the variations of the electron-proton mass ratio μ (panel a), fine structure constant α (panel b), and ratio m_q/Λ_{QCD} (panel c). The thick (dashed) lines correspond to assumed experimental sensitivity of 10^{-14} (10^{-18}) for panels (a) and (b). The dotted lines in panels (b) and (c) represent the projection for a clock-comparison experiment at the 10^{-19} level involving a nuclear clock, 10^4 sensitivity factor is assumed for a nuclear clock (see Section IV and e.g. [92]). The gray and yellow shaded regions denote the current constraint from equivalence principle tests [25, 65, 66] and atomic physics probes of the local DM density ρ_{DM} [51, 58, 59, 62] (respectively); the diagonal burgundy and green solid lines denote motivated theory targets [93, 94].

performance will require a cryogenic setup. Future development of a high-precision nuclear clock will enable an ultimate experiment with the highest potential discovery reach.

V. SENSITIVITY REACH

We estimate the sensitivity of a space-based quantum clock to the oscillation of fundamental constants, originating in ULDM fields of mass m_ϕ bound to the Sun. In Fig. 1, we estimate the reach for oscillations of μ , α ,

and m_q/Λ_{QCD} (through the couplings in Eq. (1)) in panels (a), (b), and (c), respectively. As input, we take the possible distances from the Sun of $r = 1$ AU (terrestrial searches), $r = 0.39$ AU (the orbital radius of Mercury), and the far-future potential for a probe at $r = 0.1$ AU; this latter distance is used as a demonstration, and we note that NASA Parker Solar Probe (PSP) has already reached this inner orbit and in fact even nearer to the Sun, reaching 0.06 AU on its most recent perihelion and aiming for 0.045 AU at the closest approach [91]. The NASA Parker Solar Probe instruments are designed to study particles and electromagnetic fields for its scien-

tific missions. Operating atomic clocks in an extreme environment within the Mercury orbits is a subject for future investigation. We note that the Mercury Laser Altimeter Instrument demonstrated a successful laser operation for the MESSENGER mission [101].

We observe that for probes in this inner region of the solar system, there is a clear “peak” in the sensitivity reach around $m_\phi \simeq 10^{-13}$ eV, which roughly corresponds to the point where $R_\star \simeq 0.1$ AU; at larger m_ϕ , the exponential cutoff of the SH density function rapidly diminishes the sensitivity (see Eq. (A1)).

In Fig. 1 (a) and (b), we assume a space-based clock-comparison with accuracy at the level of 10^{-14} (thick lines) or 10^{-18} (dashed lines); the former represents only a factor \sim few improvement compared to what has already been demonstrated in DSAC [102], and the latter is already achievable for the variation of α in terrestrial optical clock-comparison experiments (see Section IV, and e.g. [82–84]). Future molecular and molecular ions clocks are projected to reach 10^{-18} sensitivity to the variation of μ [96]. We observe that even a sensitivity of 10^{-14} to these oscillations allows one to probe interesting model space in a narrow range around $m_\phi \sim 10^{-13}$ eV, and space clocks at the 10^{-18} level could exceed EP probes over a wide range 3×10^{-17} eV $\lesssim m_\phi \lesssim 2 \times 10^{-13}$ eV, for a bound SH.

In Fig. 1 (b) and (c), we include a projection for a clock-comparison experiment at the 10^{-19} level involving a nuclear clock (dotted lines), assuming $\Delta K \simeq 10^4$, which is in line with future projections outlined in Section IV [92].

In these estimations, we fix M_\star by the maximal bound-state mass allowed by current constraints, though our projection can be easily rescaled to less optimistic input values using $d^{\text{limit}} \propto \phi^{-1} \propto \rho^{-1/2} \propto M_\star^{-1/2}$. The diagonal burgundy and green lines represent model targets: a naive naturalness requirement on the coupling with cut-off scale $\Lambda = 3$ TeV, and the boundary of physically-realized Higgs Portal models utilizing a relaxion, respectively [93, 94]. We observe that the relaxion benchmark is reachable by future space-based clocks for any of the three couplings we consider in this work, whereas terrestrial clocks may require much greater increases in sensitivity reach to achieve the same for a certain mass range.

A space probe with a nuclear clock would allow one to probe a vastly larger parameter space, reaching for the first time physically-motivated model space for Higgs-relaxion mixing (below the green line) for both photon and QCD couplings.

VI. SPATIAL VARIATION OF FUNDAMENTAL CONSTANTS

With our proposal of a space mission with a clock-comparison experiment in an inner solar orbit, one can also test the variations of fundamental constants due to the change in the gravitational potential during the satel-

lite transit to its orbit. Such new physics is usually parameterized as [54, 55]

$$k_X \equiv c^2 \frac{\delta X}{X \delta U}. \quad (7)$$

We quantify the change in gravitational potential as δU between the positions of two clock measurements, and $X = \alpha, \mu$, or m_q/Λ_{QCD} . There are essentially differential redshift experiments, referred to as “null” experiments in [103]. Monitoring ratio of clocks as the satellite moves deeper in the solar system can set strong constraints on the parameters k_X , as $(k_X)_{\text{exp}} = (\delta X/X)_{\text{exp}} c^2/\delta U$.

Previous studies utilize the seasonal variation in Earth’s orbital distance to the Sun, which gives rise to a difference of $\delta U/c^2 \simeq 3.3 \times 10^{-10}$, which is used to constraint k_X [55]. For a probe at 0.1 AU, as we have considered in this proposal, one can expect the change of the potential in comparison with 1 AU of $\delta U/c^2 \sim 9 \times 10^{-8}$, about 300 times larger than that of the Earth’s annual modulation. If the same uncertainty on measuring $\delta X/X$ can be reached in space as on Earth, one can therefore achieve constraints on k_X that are a factor of ~ 300 stronger, barring systematic uncertainties due to the space mission.

Our present proposal does not require an optical link enabling comparing the satellite and Earth-based clocks. If such a link can be achieved, one can also directly test general relativity and provide a direct bound on the anomalous gravitational redshift exceeding present bounds by orders of magnitude [103–105].

VII. OTHER APPLICATIONS AND OUTLOOK

We present an exciting opportunity to study ultralight dark matter in unexplored and theoretically motivated regions with atomic, molecular, and nuclear clocks in space. Such clocks can probe a very large parameter space for ULDM bound to the Sun, with the possibility in the near future of reaching well-motivated theory targets. Additionally, a clock in near approach to the Sun can significantly improve limits on spatial variation of fundamental constants.

Below, we briefly discuss some natural extensions of our ideas, as well as other well-motivated physics topics that space and quantum technologies can probe.

Space Quantum Clock Networks (SQCN) – A network of clocks in space and on Earth can study many fundamental physics topics, including transient topological dark matter [106, 107], and multimessenger signatures of exotic particles [108]. In our consideration, if a signal were to be present, the comparison of ground- and space-based clocks could help to map the density of DM in the vicinity of Earth to further constrain the bound DM scenario. One could set up a network of atomic and nuclear clocks on Earth and in space for this purpose. A high-precision clock in space with an optical link to Earth will also enable us to compare optical clocks in any place on

Earth [109], without the need for a fiber-link connection [46].

Screening – An additional motivation for a space-based atomic clock arises when the ULDM scalar field possesses quadratic couplings to SM fields. For example, in the presence of a coupling of the form $\mathcal{L} \supset g_2 \frac{\phi^2}{M_P^2} m_i \bar{\psi}_i \psi_i$, (where ψ_i are SM fields of mass m_i) with a positive coefficient, there is a screening⁴ of the field value in the vicinity of the Earth, due to a backreaction of the large number density $\bar{\psi}\psi$ of, e.g., electrons or neutrons in the Earth, rapidly reducing the sensitivity of terrestrial experiments [66]; the effect is even more severe for transients. A space-based probe considered in this work would not be subject to this Earth screening effect.

ACKNOWLEDGEMENT

We thank Kevork Abazajian, Asantha Cooray, ChunChia Chen, Jonathan Feng, Manoj Kaplinghat, Hyungjin Kim, David Leibbrandt, Gilad Perez, Stefano Profumo, and Tim Tait for useful discussions.

A part of this work was performed at the Aspen Center

for Physics, which is supported by the National Science Foundation grant PHY-1607611. JE thanks the Galileo Galilei Institute for Theoretical Physics for the hospitality and the INFN for partial support during the completion of this work. The work of Y-DT is supported in part by U.S. National Science Foundation Grant No. PHY-1915005. A part of this document was prepared by Y-DT using the resources of the Fermi National Accelerator Laboratory (Fermilab), a U.S. Department of Energy, Office of Science, HEP User Facility. Fermilab is managed by Fermi Research Alliance, LLC (FRA), acting under Contract No. DE-AC02-07CH11359. The work of JE was supported by the World Premier International Research Center Initiative (WPI), MEXT, Japan, and by the JSPS KAKENHI Grant Numbers 21H05451 and 21K20366. This work is supported in part by US NSF Grants No. PHY-2012068 and OMA-2016244. This work is a part of the “Thorium Nuclear Clock” project that has received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation program (Grant Agreement No. 856415).

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Appendix A: Properties of a Bound Solar Halo

Under the usual assumptions, DM exists in a virialized configuration with roughly constant density $\rho_{DM} = 0.4$ GeV/cm³ in our solar neighborhood. The strongest local constraints arise from the orbital dynamics of planets in the solar system, i.e., solar system ephemerides; observations constrain the density of DM at the orbital radius of Mercury, Venus, Earth, Mars, Jupiter, and Saturn at the level of $\rho \lesssim 10^3 - 10^5$ GeV/cm³ [41], which are shown by the black dots in Fig. 2.

We have been considering the scenario in which ULDM fields become bound to objects in the solar system, in which case the density and coherence properties will be modified in ways that are relevant to experimental searches [52, 53]. A bound solar halo is essentially similar to a gravitational atom, with the Sun playing the role of the nucleus; therefore the solar halo density function can be approximated as an exponential

$$\rho(r) \simeq \rho_\star \exp(-2r/R_\star) \quad (\text{A1})$$

as long as $r \gg R_\star \gg R_\odot$, in precise analogy to the ground state of a hydrogen atom. As explained in the main text, the radius R_\star is fully determined by its host mass M_{ext} (in the case under consideration, $M_{\text{ext}} = M_\odot$) and the ULDM particle mass m_ϕ ; see Eq. (4). Therefore density function $\rho(r)$ for a SH is fully calculable, given input values of scalar mass m_ϕ , radius r , and overall density normalization ρ_\star . For a density that saturates the limits of Ref. [41], we show the resulting density function $\rho(r)$, relative to ρ_{DM} , for a few relevant choices of m_ϕ , in Fig. 2.

Given the above discussion of solar halo properties, we can translate the constraints on the local DM density from Ref. [41] into a constraint on ρ_\star as a function of m_ϕ . This is what is shown in the upper panel of Fig. 3: we have illustrated the resulting limits on solar halo density ρ_\star at a distance 1 AU from the sun (relevant for Earth-based probes, black line), a distance of 0.39 AU (average radius of Mercury's orbit, red line), and for a distance of 0.1 AU (blue line). In the lower panel, we illustrate the same maximum density at 0.1 AU, but including contours to show the density for different choices of M_\star/M_\odot . Note that for consistency, we enforce $M_\star < M_\odot/2$ over the full range of parameters. It is evident from the Figure that the constraint on the local density of DM bound to the Sun becomes very weak when measured inside the orbit of Mercury. In the lower panel, we observe that even a very small bound mass, of order $10^{-16} M_\odot$, can give rise to a 10^4 increase in the density of DM at 0.1 AU for $m_\phi \simeq 10^{-13}$ eV.

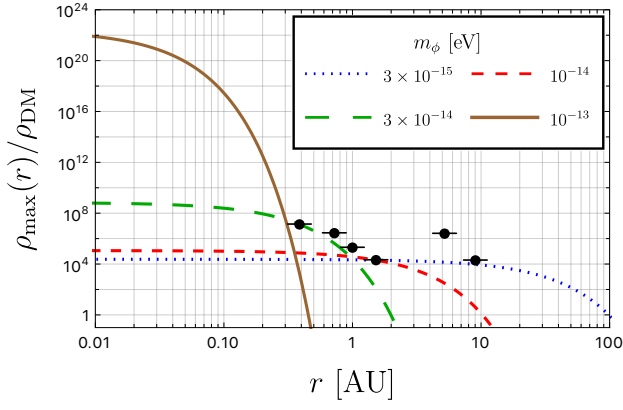


FIG. 2. The maximum allowed density $\rho_{\max}(r)$ relative to background DM density ρ_{DM} as a function of distance from the Sun r . The blue dotted, red dashed, green long-dashed, and brown solid lines correspond to ULDM particle masses of $m_\phi = 3 \times 10^{-15}$ eV, 10^{-14} eV, 3×10^{-14} eV, and 10^{-13} eV, respectively. The black points denote the constraints at the orbital radii of Mercury, Venus, Earth, Mars, Jupiter, and Saturn (left to right in the Figure) [41].

To estimate the experimental reach of an atomic clock to probe a SH, we saturate the constraint on SH density at a given radius r (the upper panel of Fig. 3). This translates into a field amplitude $\phi_\star = \sqrt{2\rho_\star/m_\phi}$, which we substitute in Eq. (2). Then, we fix a value for the fractional accuracy in the variation of the fundamental constants (e.g. 10^{-14}) motivated by current and near-future experiments (see Section IV), and derive the resulting sensitivity reach using

$$d_{m_e}^{\text{limit}} \simeq \frac{1}{\kappa\phi_\star(r)} \left(\frac{\delta\mu}{\mu} \right)_{\text{exp}}, \quad (\text{A2})$$

$$d_\alpha^{\text{limit}} \simeq \frac{1}{\kappa\phi_\star(r)} \left(\frac{\delta\alpha}{\alpha} \right)_{\text{exp}}, \quad (\text{A3})$$

$$d_g^{\text{limit}} \simeq \frac{1}{\kappa\phi_\star(r)} \left(\frac{\delta(m_q/\Lambda_{\text{QCD}})}{(m_q/\Lambda_{\text{QCD}})} \right)_{\text{exp}}. \quad (\text{A4})$$

The results are indicated by the black, red, and blue lines in Fig. 1.

The coherence timescale for ULDM oscillations is typically much longer in a solar halo than it would be for virial DM τ_{DM} . This is because the bound ULDM particles must be colder, i.e. have lower velocity dispersion, to remain bound to the Sun. The velocity dispersion v_\star , and therefore the coherence timescale τ_\star , of a SH is essentially dictated by its radius R_\star and particle mass m_ϕ via the relation [53]

$$\begin{aligned} \tau_\star &\simeq (m_\phi v_\star^2)^{-1} \simeq m_\phi R_\star^2 \\ &\simeq 10^3 \text{ sec} \times \begin{cases} 1, & m_\phi \gtrsim 2 \times 10^{-13} \text{ eV} \\ \left(\frac{2 \times 10^{-13} \text{ eV}}{m_\phi} \right)^3, & m_\phi \lesssim 2 \times 10^{-13} \text{ eV}. \end{cases} \end{aligned} \quad (\text{A5})$$

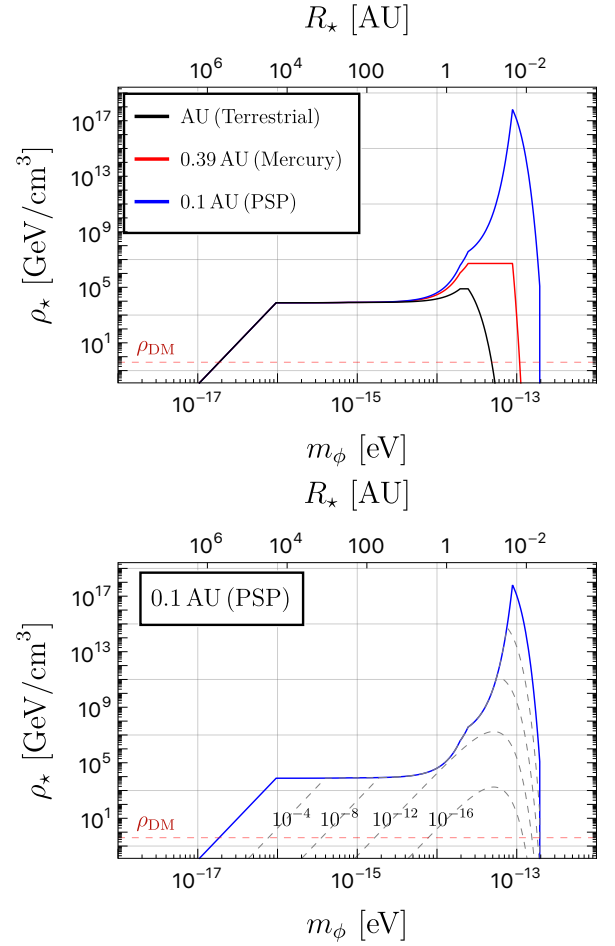


FIG. 3. The allowed solar halo density ρ_\star as a function of ULDM particle mass m_ϕ . Upper panel: Maximum density ρ_\star at different probe radii: AU (radius of Earth's orbit, black line), 0.39 AU (radius of Mercury's orbit, red line), and 0.1 AU (blue line). Burgundy dashed line is the local density of virialized DM. Lower panel: Maximum density at 0.1 AU (blue line), along with contours of fixed M_\star/M_\odot as labeled.

This relation is illustrated in Fig. 4. When τ_\star is much longer than the averaging period τ of an atomic clock DM search (see discussion around Eq. (6)), the full stability of the clock can be leveraged; on the other hand, when $\tau_\star < \tau$, the sensitivity to ULDM signals is diminished by the factor $\sqrt{\tau_\star/\tau}$. For searches that are shorter than $\tau \simeq 1$ day, the resulting reduction in sensitivity is about one order of magnitude at worst, when $m_\phi \gtrsim 2 \times 10^{-13}$ eV.

Appendix B: Clocks in Earth Orbits and An Earth-bound Halo

It has been proposed to put atomic clocks in orbit around the Earth [104, 105] and on the moon (see e.g. [110]). For completeness, we note here that depending on the details of the clock, such probes could be sensitive

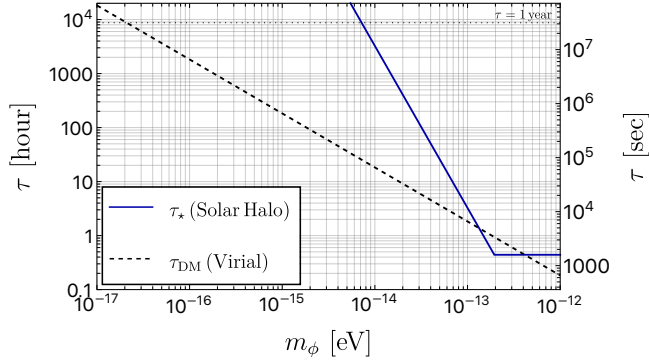


FIG. 4. The coherence timescale for a solar halo (blue) and for virialized DM (black dashed), as a function of ULDM particle mass m_ϕ .

to ULDM bound halos around the Earth. Because of the dependence of the halo radius on m_ϕ (see Eq. (4)), such probes would be restricted to a mass window of larger m_ϕ , with peak sensitivity around 10^{-11} eV and 10^{-8} eV. Atomic spectroscopy searches in this range are rapidly progressing [60, 61, 63], and molecular spectroscopy experiments are able to achieve sensitivity at the level of 10^{-15} [64]. We also note that in a scenario with a large quadratic coupling to matter and resulting screening of the ULDM field in the vicinity of the Earth [66], a probe in orbit may be advantageous in evading this screening. It is worthwhile to consider the possible sensitivity of these probes as well.

For a halo bound to the Earth, the situation is similar to that of the SH in Appendix A, with the substitution $M_{\text{ext}} = M_\oplus$ and the relevant mass range is at larger $m_\phi \gtrsim$

10^{-13} eV based on Eq. (4). The strongest constraints on this scenario arise from comparison of orbital dynamics of low-orbit satellites (e.g. LAGEOS) and the moon [111]. See [52] for a more complete treatment of this case.

In Fig. 5 we illustrate the sensitivity of an atomic clock to the presence of a ULDM halo around the Earth. The style of the lines is identical to that of Fig. 1, except that the red and blue lines correspond to probes at a distance equal to the orbit of the LAGEOS Satellite, $1.9R_\oplus$ [111], and that of the moon, $59.6R_\oplus$. We have assumed a sensitivity of 10^{-14} (thick lines) or 10^{-18} (dashed) to the oscillating signal, as in Fig. 1. We found that a terrestrial clock is sufficient in probing the Earth-bound halo. Placing clocks in LAGEOS orbit or on the Moon results in reduced sensitivities for the Earth-bound halo, assuming there are no ULDM-SM quadratic couplings and the associated Earth-screening effects.

As we have noted throughout the paper, the sensitivity to the bound halo scenario is *diminished* when the probe is sent far from the center of the halo, due to the halo profile and the constraints on the halo density. In the main text, we discussed the possibility of a probe being sent towards the Sun, which would allow one to probe weaker couplings, and larger masses m_ϕ , of particles in the bound SH. An analogous case for an EH would suggest a mission to send an atomic clock being down into the Earth as deeply as possible. The largest depth ever probed by humankind is only of order 10 km below the surface, where the increase in sensitivity would be invisible at the scale of Fig. 5. One would require a clock with 10^{-18} accuracy poised a distance 2000 km below the surface (in the mantle of the Earth) to probe bound scalar ULDM up to masses as high as 10^{-7} eV, which is clearly not viable.

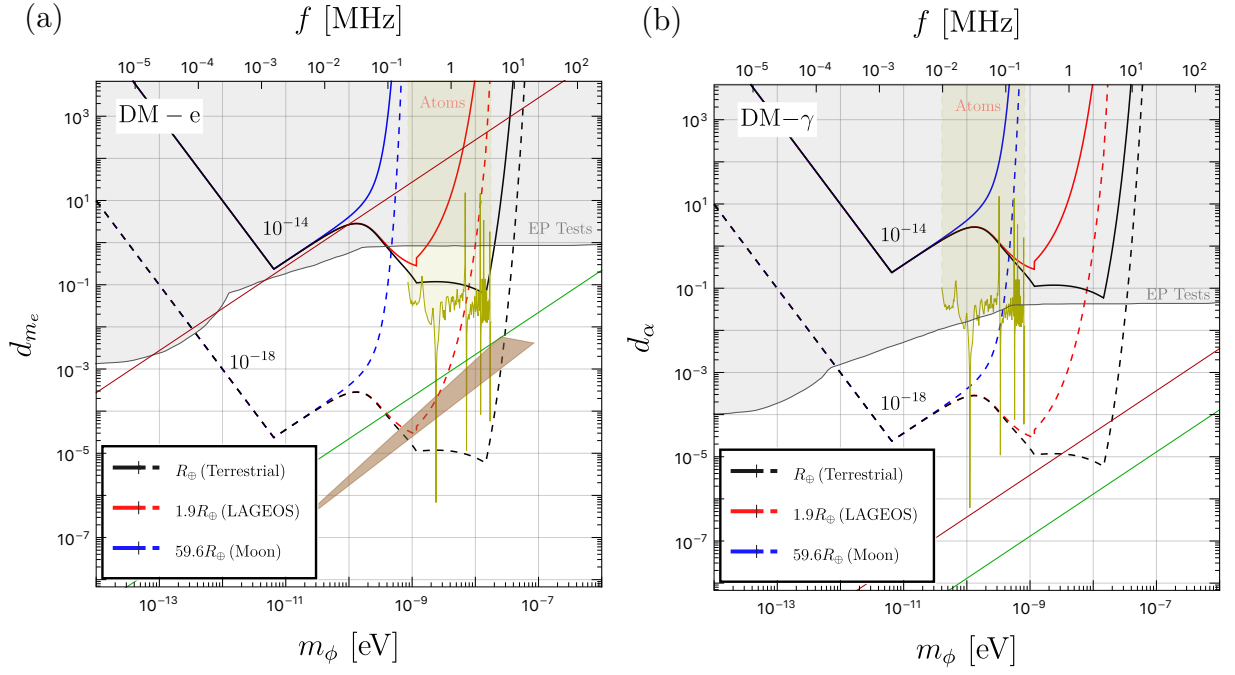


FIG. 5. Estimated sensitivity reach for ultralight dark matter, coupled via Eq. (1) and bound to the Earth; for the bound Earth halo density, we assume the maximum allowed by gravitational constraints following [52]. The blue, red, and black denote sensitivity for those at distances explored by the Moon, the LAGEOS Satellite, and terrestrial clocks, respectively. The thick and dashed lines correspond to assumed sensitivity at the level of 10^{-14} and 10^{-18} (respectively) to variations of (a) $(\delta\mu/\mu)$ or (b) fine structure constant $(\delta\alpha/\alpha)$. The gray and yellow regions denote the current constraint from equivalence principle tests [25, 65] and atomic physics probes of an Earth Halo [63] (respectively); the diagonal burgundy and green lines denote motivated theory targets, as in Fig. 1 [93, 94]. The brown shaded region is a target for probing coherent relaxation dark matter [2].