

# **Stress transmission coefficient is a reliable and robust parameter for quantifying powder plasticity**

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# 1    **1    Introduction**

2            Many processes in pharmaceutical manufacturing are highly influenced by material  
3    plasticity. For example, high plasticity can render the milling process inefficient at reducing  
4    particle size due to a lower propensity of fragmentation [1]. Plastic deformation also promotes  
5    interparticulate bonding area formation during tablet manufacturing, which is necessary to achieve  
6    adequate tableting strength [2]. Thus, plasticity is an essential material property for designing high-  
7    quality pharmaceutical tablet products. As such, modulating the plasticity of active pharmaceutical  
8    ingredients (**API**) through crystal and particle engineering is important in product development [2–  
9    10].

10           Currently, methods to quantify powder plasticity in facilitating tablet compression  
11    invariably require the value of the compact porosity ( $\varepsilon$ ). In one approach, pressure ( $P$ ) –  $\varepsilon$  data are  
12    analyzed using a suitable mathematical model, such as the Heckel [11,12], Kawakita [13], Kuentz  
13    and Leuenberger (KL) [14], and Walker [15] equations. In the macroindentation approach, the  
14    hardness of compressed tablets ( $H$ ) is measured, and  $H$  at zero porosity ( $H_0$ ) is obtained by  
15    extrapolating  $H - \varepsilon$  data using an exponential relationship [16]. Established plasticity parameters  
16    include  $P_{y,o}$  from the out-of-die Heckel analysis,  $I/C$  from the KL analysis, and  $H_0$  from the  
17    macroindentation experiments.

18           Accurate determination of  $\varepsilon$  is essential for accurately determining the plasticity of a  
19    powder using these approaches, as small errors in  $\varepsilon$  can lead to significant errors in plasticity  
20    parameters because of the sensitivity of these analyses to  $\varepsilon$  [17]. Thus, the accurate determination  
21    of powder plasticity using any of these methods requires accurate measurements of both compact  
22    density ( $\rho$ ) and the true density of the material ( $\rho_i$ ), which are used to calculate  $\varepsilon$  according to  
23    Equation 1.

$$\varepsilon = 1 - \frac{\rho}{\rho_t} \quad (1)$$

Unfortunately, the accurate out-of-die  $\rho$  is not always possible to obtain due to several issues with accurately determining tablet volume, including 1) complex tablet geometry [18], 2) inability to form an intact tablet due to capping, lamination [19], punch sticking [20,21], 3) internal tablet defects [22], and 4) tablet flashing [23]. Additionally, even for materials free from these issues, the out-of-die approach for determining  $\rho$  requires a significant amount of material. Typically at least 5–10 g are required to prepare an appropriate set of tablets for data collection to assure accurate determination of the plasticity parameter. Additionally, it takes a few hours even for a skilled researcher to collect each set of data. Therefore, adopting the out-of-die approach to guide efficient formulation design and development is not appealing in the early drug development stages.

These issues associated with  $\rho$  measurements can be avoided with an analysis of in-die data obtained during compression with a modern compaction simulator, i.e.,  $\rho$  as a function of force. Subsequently,  $P - \varepsilon$  data throughout a compression cycle can be derived from  $\rho$  and force, if the cross-sectional area of the punch and  $\rho_t$  are known. We have shown that the mean yield pressure obtained from the in-die Heckel analysis,  $P_{y,i}$ , is a reliable measure of material plasticity [24]. Hence, it is suitable for quantifying powder plasticity early in drug development. However, an accurate in-die Heckel analysis still requires an accurate  $\rho_t$ . Methods for determining  $\rho_t$  include 1) calculation from the solved crystal structure [25], 2) helium pycnometry [26], and 3) fitting out-of-die  $\rho - P$  data using the Sun approach [27]. However, none of these methods is broadly applicable for obtaining an accurate  $\rho_t$  for all pharmaceutical powders. Since pharmaceutical solids are not always perfectly crystalline, calculated  $\rho_t$  values from crystal structures tend to be over-estimated. Due to crystal thermal expansion, errors are larger when the crystal structures are solved

from data collected at sub-ambient temperatures, which is a common practice to reduce thermally induced disorders for a better structure model. Helium pycnometry cannot yield accurate  $\rho_t$  of powders that contain sealed pores or volatile components, e.g., water [17,28]. The Sun analysis allows for the determination of  $\rho_t$  for water-containing materials [28], but suffers from the same issues that impact the out-of-die  $\rho$  measurements mentioned above. Since there are no methods that can be used to measure an accurate  $\rho_t$  for all pharmaceutical powders at the present, the in-die Heckel analysis still cannot yield accurate plasticity parameters for all powders.

The stress transmission between applied axial stress ( $\sigma_a$ ) and radial stress ( $\sigma_r$ ), can be viewed as a measure of the ability of the compressed material to flow under pressure [29]. The inverse correlation observed between crystal hardness and stress transmission indicates a potential correlation between stress transmission and powder plasticity [30,31]. It was also observed that materials exhibiting a good conversion of axial pressure to radial pressure tend to form better tablets, [29,32] due to a larger degree of plastic deformation [33]. Thus, it is reasonable to expect a correlation between the stress transmission coefficient (STC), i.e., the slope of  $\sigma_r$  versus  $\sigma_a$  after a solid plug has been formed during compression, and powder plasticity. Importantly, the STC can be experimentally determined without using  $\rho_t$  and  $\rho$  information. However, aside from these indirect pieces of evidence that associate stress transmission and plasticity, such a correlation has not been firmly established. Here, using a large set of powders exhibiting a wide range of mechanical properties, we show that the STC is indeed a reliable measure of powder plasticity suitable for adoption in an early stage of drug development.

## **2 Materials and Methods**

### **2.1 Materials**

Microcrystalline cellulose (MCC; Avicel PH102, FMC Biopolymer, Philadelphia, PA), lactose monohydrate (LM; #316 Fastflo<sup>®</sup> NF, Foremost Farms, Clayton, WI), mannitol 200SD (Mann; Pearlitol<sup>®</sup> 200SD, Roquette America Inc., Keokuk, IA), dicalcium phosphate anhydrate (DCPA; Anhydrous Emcompress<sup>®</sup>, JRS Pharma, Patterson, NY), dicalcium phosphate dihydrate (DCPD; Emcompress<sup>®</sup>, JRS Pharma, Patterson, NY), ibuprofen (IBN; Sigma Aldrich, St. Louis, MO), celecoxib (CEL; Aarti Drugs Pvt Ltd., Mumbai, India), hydroxypropyl cellulose (HPC; Klucel EF-PHARM, Ashland, Wilmington DE), and magnesium stearate (MgSt; non-bovine, HyQual<sup>™</sup>, Mallinckrodt, St. Louis, MO) were used as received.

### **2.2 Mixing and tableting**

LM, Mann, and DCPA were studied both individually and as mixtures in 25% increments with MCC. An additional mixture of 90% DCPA with 10% MCC and two mixtures of 20% IBN or CEL with 80% MCC were also prepared. All mixtures were blended for 10 min at 49 rpm in a blender (Turbula, Glen Mills, Clifton, NJ). Pure MCC and HPC were compressed without further treatment. All other powders were mixed with 1% (w/w) MgSt in the blender for 2 min at 49 rpm. The MgSt was used as an internal lubricant to reduce frictional forces between the tablet and die wall during compression.

Tablets were prepared using a compaction simulator (Styl'One Evolution; MedelPharm, Beynost, France) with a round instrumented die (11.28 mm in diameter) using a symmetrical, force-controlled, single compression cycle at 2% speed, composed of a 2 s compression (1 s rise and a 1 s fall without holding at the maximum force) followed by 3 s relaxation and a 2 s ejection step. The calibration of the instrumented die was verified before data collection using a stack of

rubber discs per the instructions in the instrument manual. Round, flat-faced punches were used to compress tablets.

The middle of the tablet was set at 6 mm below the surface of the instrumented die, and the minimum thickness of the tablets was set to 3.2 mm for all materials to ensure consistent STC measurements. Due to the 200 MPa limit for  $\sigma_r$  that can be measured by the instrumented die without risking damage to the die, the target  $\sigma_a$  was around 200 MPa by using an appropriate amount of each material.

### 2.3 STC analysis fitting and data analysis

Mean  $\sigma_a$  and  $\sigma_r$  values for each cycle exported from the compaction simulator were plotted. To avoid data corresponding to the compression phase before a solid plug is formed, the terminal linear region (typically >100 MPa in  $\sigma_a$ ) of the loading curve was used for linear regression using the `curve_fit` function in SciPy's optimize package. The slope of the fitted line is taken as the STC. For the plot of STC versus other plasticity parameters ( $P_{y,i}$ ,  $P_{y,o}$ ,  $I/C$ , and  $H_0$ ), fitting was performed using SciPy's orthogonal distance regression (ODR) package (SciPy version 1.6.2, Python version 3.8.2) using ordinary least squares (job=2), unless otherwise specified.

## 3 Results and Discussion

### 3.1 Correlation between STC and established plasticity parameters

The STC values of the powders studied in this work varied over a wide range, 0.506 – 0.959, with that of HPC (0.959) being the highest. The nearly 100% transmission of stress from the punches to the die wall suggests highly efficient stress transmission by HPC. This qualitatively correlates with the high plasticity of HPC [16,24,34]. In contrast, the STC of DCPA was only 0.506, suggesting its inefficiency in transmitting stress from the axial to the radial direction, which

is consistent with the low plasticity of DCPA [16,35]. Overall, STC strongly correlates with all plasticity parameters explored in this work, including  $P_{y,i}$  ( $R^2=0.956$ ),  $P_{y,o}$  ( $R^2=0.886$ ),  $1/C$  ( $R^2=0.988$ ), and  $H_0$  ( $R^2=0.916$ ). All four plasticity parameters ranged over two orders of magnitude, and a power-law relationship adequately describes all these correlations (Figure 1). Numerical values of all parameters used in Figure 1 are summarized in Table 1.

The good correlations between STC and other plasticity parameters suggest that STC can be used to quantify material plasticity with similar authority as these traditional plasticity parameters. A key advantage of the STC is that it can be obtained to measure material plasticity without using tablet density and true density.

### 3.2 Robustness of STC measurements

Radial stress transmission has been previously characterized for a number of APIs [37–39], excipients [39–42], and mixtures [43]. However, a comparison of results in the previous studies must be made with caution because accurate die wall stress measurements require appropriate calibration, and they may be affected by compaction conditions [44], which differed among the various studies. Appropriate calibration of the instrumented die entails simulating a hydrostatic environment using hydraulic fluids or a pseudo-hydrostatic environment using natural or synthetic rubbers [44]. Die wall stress calibration constants may differ when rubbers with different mechanical properties are used. In this study, the calibration of the instrumented die was performed using rubber discs over a range of thicknesses according to the manufacturer's specifications. Although this calibration can theoretically minimize or eliminate the effects of tablet thicknesses and compression depths on measured  $\sigma_r$  [44,45], the measured STC decreases slightly with increasing tablet thickness for rubber (Figure 2). This is attributed to the fact that the

calibration was performed under a static stress condition, but the STC was measured dynamically. Hence, we have not given any physical meaning to the slight deviation (<5%) of STC values of rubber from unity across the thickness range examined in this work.

During dynamic powder compression, frictional force between the powder bed and the die wall dampens the stress transmission, which reduces measured STC. Hence, thinner tablets are more efficient in transmitting stress, corresponding to a higher STC. This is generally observed for all four materials (Figure 2). To minimize this effect, tablet thickness was fixed at a user-set thickness of 3.2 mm (Figure 2a), which corresponds to the actual minimum tablet thickness of ~4 mm after correcting for machine deformation (Figure 2b). Reproducibility was further improved by fixing the middle point of the tablet at the middle of the strain gauges, which is located 6 mm below the surface of the die. This fixation of tablet thickness and compression location resulted in highly reproducible STC measurements for all materials studied (Figure 3 and Table 1).

It should be noted that the variation in STC caused by different tablet thicknesses over a wide range, e.g., 2 – 4 mm, is much smaller than the differences among rubber, HPC, MCC, and DPCA (Figure 2). Therefore, STC can be used to rank order materials accurately according to their plasticity even when the user-set minimum tablet thickness is allowed to slightly vary.

### 3.3 Applications of STC

Given the strong correlation between STC and a number of established plasticity parameters examined in this work using materials exhibiting plasticity over at least two orders of magnitude, STC can be used as an excellent alternative parameter for characterizing the plasticity of pharmaceutical powders. The independence of STC from true density or tablet density, the high

reproducibility, and the *in situ* data collection by a computer collectively make it a reliable and objective parameter. Hence, STC data among laboratories can be compared with confidence, provided the calibration of the instrumented die is properly performed.

Potential applications of STC include 1) rapid characterization of plasticity of different solid forms of an API, e.g., cocrystals, salts, and hydrates, to inform the solid form selection; 2) better understanding of the effects of particle size, crystal habit, blend composition, and excipient grade on powder plasticity; 3) evaluation of different compaction conditions, e.g., tableting speed, on the extent of plastic deformation of a formulation to guide scale-up of a tablet manufacturing process.

#### **4 Conclusion**

The STC is strongly correlated with four traditional plasticity parameters,  $P_{y,i}$ ,  $P_{y,o}$ ,  $I/C$ , and  $H_0$ , indicating that it can be used as a reliable powder plasticity parameter. The independence of the STC from tablet porosity renders it immune to unavoidable errors with tablet and true density encountered by other existing methods for quantifying powder plasticity. Thus, the STC is a highly expedited and material-sparing method for characterizing material plasticity, making it an excellent alternative to traditional methods of evaluating powder plasticity for adoption in the early stages of drug development.

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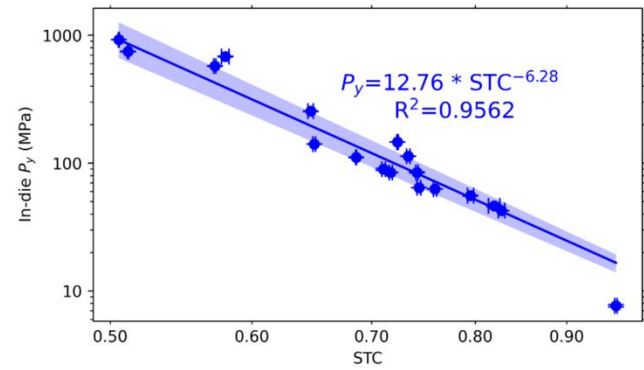
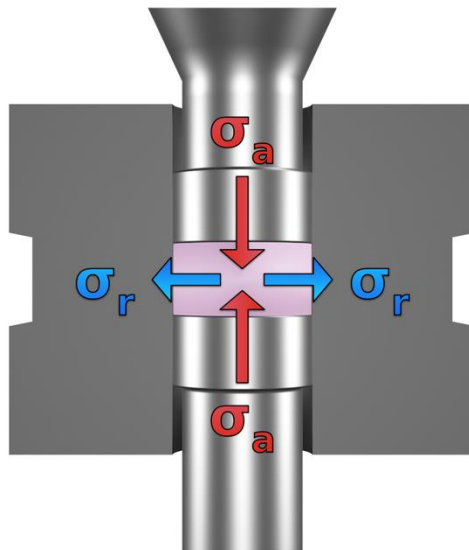
## Figure Legends

**Figure 1:** (a)  $P_{y,i}$ , (b)  $P_{y,o}$ , (c)  $I/C$ , and (d)  $H_0$  versus STC for a variety of pharmaceutical powders. The shaded regions correspond to  $\pm 1$  standard error on the fitted lines. All markers have error bars in both x and y directions, but some are hidden by the symbols.

**Figure 2:** Effects of (a) user-set minimum tablet thickness and (b) machine-deformation corrected minimum tablet thickness on the STC of rubber, HPC, MCC, and DCPD.

**Figure 3:**  $\sigma_r$  versus  $\sigma_a$  curves for (a) MCC, (b) LM mixtures with MCC, (c) Mann mixtures with MCC, (d) DCPA mixtures with MCC, and (e) DCPD, IBN and CEL mixtures with MCC, and HPC. The black dotted line indicates perfect hydrostaticity. The dashed line is the average of 3 linear regressions from 3 separate compressions. The solid line indicates the region in which linear regression was applied.

## Graphical abstract



**Stress transmission coefficient (STC)**

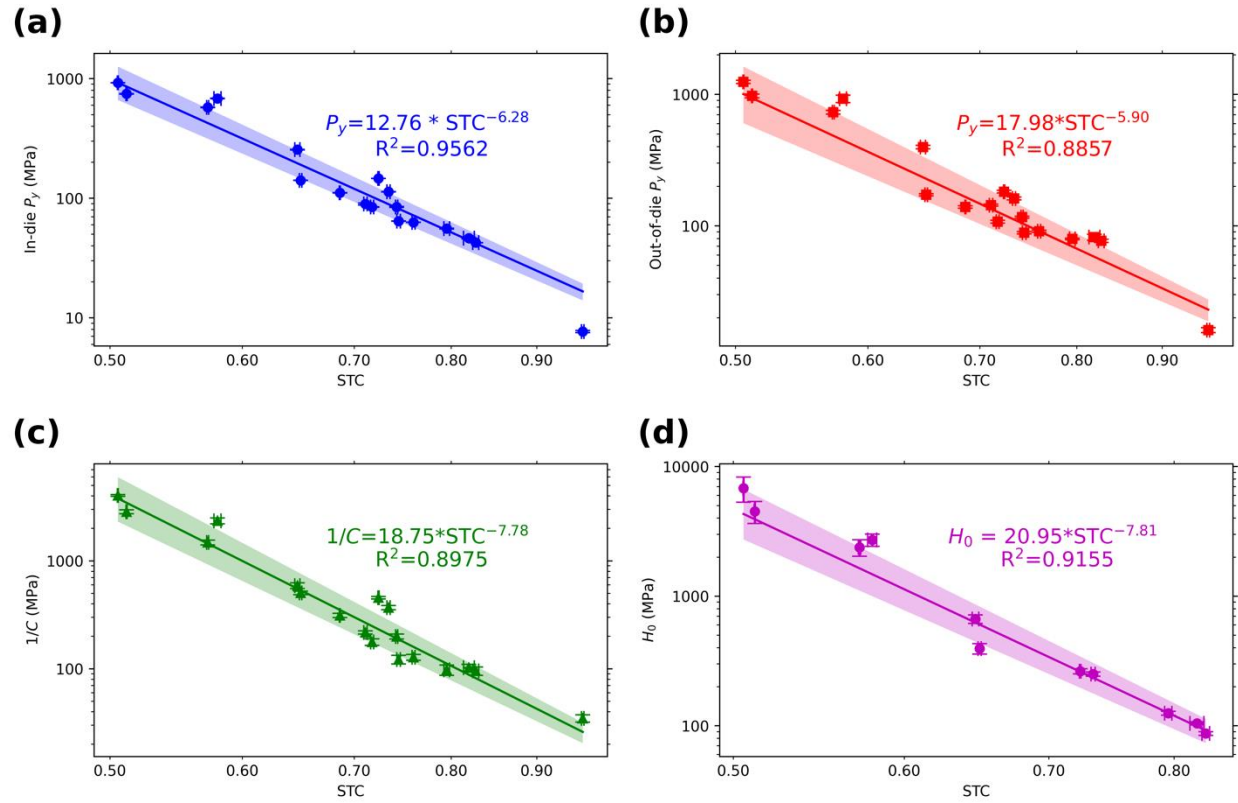
**Abstract**

Powder plasticity parameters derived by existing methods are sensitive to errors in porosity measurements resulting from inaccurate measurements of compact density, true density, or both. Using a number of materials exhibiting plasticity over a range of more than two orders of magnitude, the post-powder densification stress transmission coefficient (STC) strongly correlates with all four existing in-die and out-of-die plasticity parameters. Since the STC determination requires only axial and radial stress measurements, it is free from errors in the determination of tablet porosity suffered by other existing methods. Additionally, STC is immune from user error, because data can be collected by a computer using a compaction simulator with an instrumented die. Overall, the STC is an excellent alternative to traditional powder plasticity parameters for guiding the tablet formulation design in early stages of drug development.

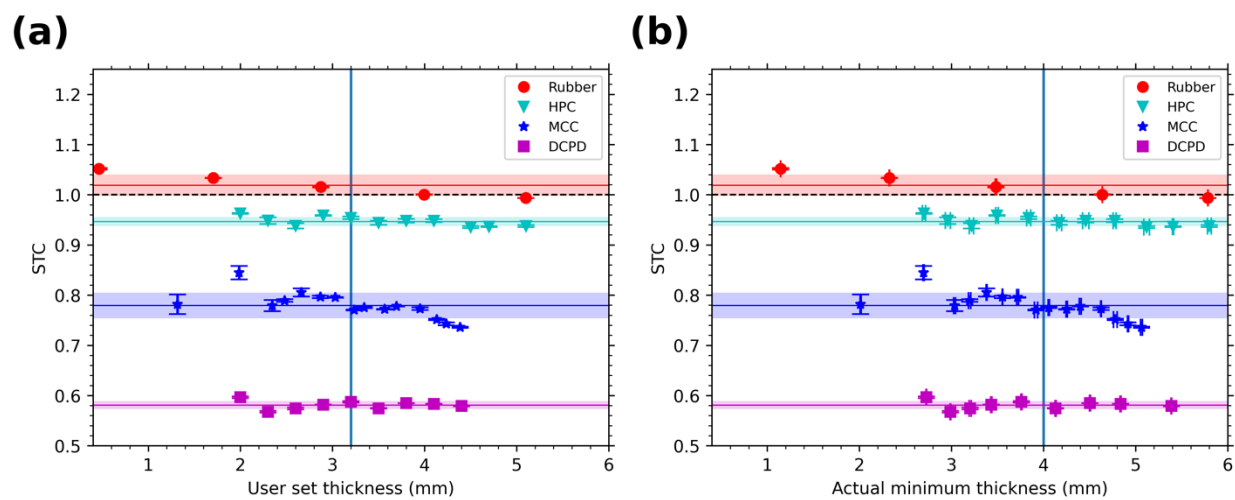
**Table 1:** STC,  $P_{y,i}$ ,  $P_{y,o}$ ,  $H_0$ , and  $I/C$  plasticity parameters used in Figure 1. Values in parenthesis indicate either the standard deviation of three measurements for STC and  $P_{y,i}$  or the standard error of regression for out-of-die measurements.

| Material  | STC            | $P_{y,i}$ (MPa)          | $P_{y,o}$ (MPa)            | $H_0$ (MPa)               | $I/C$ (MPa)                 |
|-----------|----------------|--------------------------|----------------------------|---------------------------|-----------------------------|
| MCC       | 0.795 (0.003)  | 55.7 (0.4) <sup>2</sup>  | 79.4 (1.1) <sup>2</sup>    | 124.8 (4.4) <sup>1</sup>  | 97.5 (10.7) <sup>2</sup>    |
| 25% LM    | 0.744 (0.002)  | 64.3 (0.04) <sup>2</sup> | 88.5 (1.89) <sup>1</sup>   | -                         | 121.8 (11.2) <sup>1</sup>   |
| 50% LM    | 0.717 (0.001)  | 84.4 (0.3) <sup>2</sup>  | 107.5 (2.75) <sup>1</sup>  | -                         | 176.8 (12.3) <sup>1</sup>   |
| 75% LM    | 0.686 (0.0004) | 110.8 (0.5) <sup>2</sup> | 138.9 (2.95) <sup>1</sup>  | -                         | 312.1 (14.5) <sup>1</sup>   |
| 100% LM   | 0.650 (0.001)  | 141.0 (0.4) <sup>2</sup> | 172.4 (3.16) <sup>1</sup>  | 393.1 (36.1) <sup>1</sup> | 504.4 (19.2) <sup>1</sup>   |
| 25% Mann  | 0.760 (0.002)  | 62.7 (0.1) <sup>2</sup>  | 90.9 (1.7) <sup>1</sup>    | -                         | 127.8 (8.1) <sup>1</sup>    |
| 50% Mann  | 0.742 (0.001)  | 84.5 (0.6) <sup>2</sup>  | 116.3 (2.12) <sup>1</sup>  | -                         | 199.1(10.3) <sup>1</sup>    |
| 75% Mann  | 0.734 (0.002)  | 113.3 (0.4) <sup>2</sup> | 161.3 (4.09) <sup>1</sup>  | 250 (9.4) <sup>1</sup>    | 368.5 (16.3) <sup>1</sup>   |
| 100% Mann | 0.724 (0.001)  | 146.2 (0.1) <sup>2</sup> | 181.8 (4.13) <sup>1</sup>  | 263.0 (12.1) <sup>1</sup> | 455.2 (12.4) <sup>1</sup>   |
| 25% DCPA  | 0.711 (0.002)  | 89.3 (1.6) <sup>2</sup>  | 143.5 (2.5) <sup>2</sup>   | -                         | 252.6 (13.1) <sup>2</sup>   |
| 50% DCPA  | 0.647 (0.002)  | 254.5 (1.0) <sup>2</sup> | 397.3 (12.4) <sup>2</sup>  | 665.4 (49.4) <sup>1</sup> | 796.9 (62.2) <sup>2</sup>   |
| 75% DCPA  | 0.572 (0.001)  | 573.5 (2.2) <sup>2</sup> | 730.7 (24.8) <sup>2</sup>  | 2374 (346) <sup>1</sup>   | 1921.8 (103.1) <sup>2</sup> |
| 90% DCPA  | 0.512 (0.0003) | 745.5 (2.8) <sup>2</sup> | 972.7 (32) <sup>2</sup>    | 4501 (865) <sup>1</sup>   | 3686.8 (113.5) <sup>2</sup> |
| 100% DCPA | 0.506 (0.0003) | 921.3 (0.2) <sup>2</sup> | 1243.7 (35.7) <sup>2</sup> | 6790 (1494) <sup>1</sup>  | 4203.8 (77.1) <sup>2</sup>  |
| 100% DCPD | 0.580 (0.003)  | 681.4 (3.7) <sup>2</sup> | 925.2 (60) <sup>2</sup>    | 2715 (295) <sup>1</sup>   | 3573.7 (349.0) <sup>2</sup> |
| 20% IBN   | 0.828 (0.003)  | 42.4 (0.1) <sup>2</sup>  | 76.9 (2.23) <sup>1</sup>   | 87.1 (2.85) <sup>1</sup>  | 95.3 (8.3) <sup>1</sup>     |
| 20% CEL   | 0.820 (0.006)  | 46.3 (0.7) <sup>2</sup>  | 81.9 (4.26) <sup>1</sup>   | 1043 (3.01) <sup>1</sup>  | 102.0 (7.8) <sup>1</sup>    |
| HPC       | 0.959 (0.002)  | 7.7 (0.2) <sup>2</sup>   | 16.1 (0.7) <sup>2</sup>    | -                         | 34.7 (2.7) <sup>2</sup>     |

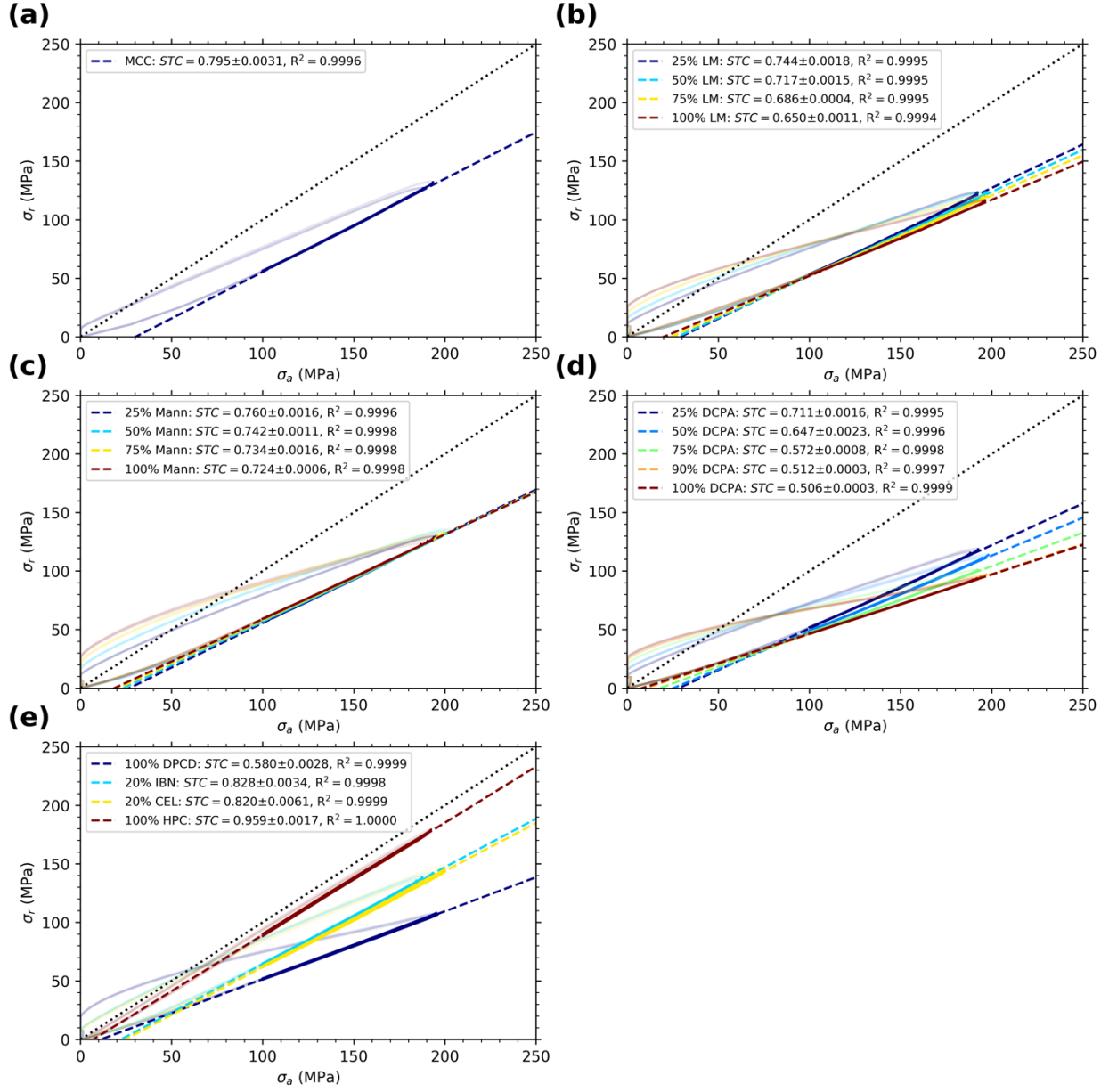
<sup>1</sup>[36], <sup>2</sup>[24]



**Figure 1:** (a)  $P_{y,i}$ , (b)  $P_{y,o}$ , (c)  $1/C$ , and (d)  $H_0$  versus STC for a variety of pharmaceutical powders. The shaded regions correspond to  $\pm 1$  standard error on the fitted lines. All markers have error bars in both x and y directions, but some are hidden by the symbols.



**Figure 2:** Effects of (a) user-set minimum tablet thickness and (b) machine-deformation corrected minimum tablet thickness on the STC of rubber, HPC, MCC, and DCPD.



**Figure 3:**  $\sigma_r$  versus  $\sigma_a$  curves for (a) MCC, (b) LM mixtures with MCC, (c) Mann mixtures with MCC, (d) DCPA mixtures with MCC, and (e) DCPD, IBN and CEL mixtures with MCC, and HPC. The black dotted line indicates perfect hydrostaticity. The dashed line is the average of 3 linear regressions from 3 separate compressions. The solid line indicates the region in which linear regression was applied.

## **Highlights**

- Stress transmission coefficient (STC) affects transmission of stress to die wall
- STC is quantified using a compaction simulator with an instrumented die
- STC correlates well with the plasticity of a large set of powders
- STC is free from errors in traditional methods for quantifying plasticity

Gerrit Vreeman: Methodology, Formal analysis, Investigation, Writing- Original draft preparation.

Changquan Calvin Sun: Supervision, Conceptualization, Writing- Reviewing and Editing, Resources, Funding acquisition

**Declaration of interests**

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

☐The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: