

Measurement of the Sixth-Order Cumulant of Net-Proton Multiplicity Distributions in Au + Au Collisions at $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV at RHIC

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According to first-principle lattice QCD calculations, the transition from quark-gluon plasma to hadronic matter is a smooth crossover in the region $\mu_B \leq T_c$. In this range the ratio, C_6/C_2 , of net-baryon distributions are predicted to be negative. In this Letter, we report the first measurement of the midrapidity net-proton C_6/C_2 from 27, 54.4, and 200 GeV Au + Au collisions at the Relativistic Heavy Ion Collider (RHIC). The dependence on collision centrality and kinematic acceptance in (p_T, y) are analyzed. While for 27 and 54.4 GeV collisions the C_6/C_2 values are close to zero within uncertainties, it is observed that for 200 GeV collisions, the C_6/C_2 ratio becomes progressively negative from peripheral to central collisions. Transport model calculations without critical dynamics predict mostly positive values except for the most central collisions within uncertainties. These observations seem to favor a smooth crossover in the high-energy nuclear collisions at top RHIC energy.

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One of the main goals of high-energy nuclear physics is to understand the phase diagram of the strongly interacting matter predicted by quantum chromodynamics (QCD), with respect to temperature (T) and baryon chemical potential (μ_B). At high T and/or μ_B , the strongly interacting matter called quark-gluon plasma (QGP) is predicted to exist, while the hadronic matter appears at low T [1–3]. The phase transition between QGP and hadronic matter at $\mu_B \approx 0$ was shown to be a smooth crossover, based on first-principle lattice QCD calculations [4]. At finite μ_B , on the other hand, the phase transition is predicted to be of the first order [5]. If this is true, a critical end point may also exist, which is the connecting point between crossover and the first-order phase transition [6].

Experimentally, the QCD phase diagram can be explored by measuring heavy-ion collisions at various collision energies. The beam energy scan (BES) program was carried out at the Relativistic Heavy-Ion Collider (RHIC), and datasets for Au + Au collisions at $\sqrt{s_{NN}} = 7.7, 11.5, 14.5, 19.6, 27, 39, 54.4, 62.4$, and 200 GeV were collected by the STAR experiment. The r th-order cumulants (C_r) and their ratios up to the fourth order of net-charge, net-proton, and net-kaon multiplicity distributions have been measured to search for the critical point [7–12]. In particular, the ratio C_4/C_2 of the net-proton multiplicity distributions with an extended p_T coverage shows a nonmonotonic beam energy dependence in Au + Au central collisions [9]. This is qualitatively consistent with a theoretical model prediction which incorporates a critical point [13,14]. Since the results are dominated by large statistical uncertainties at low collision energies, the beam energy scan phase II (BES-II) and the fixed-target programs are being performed to detect more definitive signatures of the critical point [15]. New findings on the QCD phase structure at large

μ_B are thus expected in the near future from the BES-II program.

There is no direct experimental evidence of a smooth crossover at $\mu_B \approx 0$ MeV as predicted by the lattice QCD calculations. This can be studied by measuring the ratio of the sixth to second-order cumulant (C_6/C_2) of net-baryon and net-charge multiplicity distributions. According to the QCD model calculations, the C_6/C_2 values of net-baryon distributions become negative at $\sqrt{s_{NN}} \geq 60$ GeV if the freeze-out, where ratios of particle yields are fixed, occurs near the chiral crossover temperature [16], whereas the hadron resonance gas model calculations yield a positive sign for C_6/C_2 [17]. Recent model studies predict a negative sign of C_6/C_2 at $\sqrt{s_{NN}} \geq 7.7$ GeV within large uncertainties [18]. Furthermore, recent lattice QCD calculations also show a negative sign of the ratio of the sixth-order to the second-order baryon number susceptibilities, χ_6^B/χ_2^B , at the transition temperature for $\sqrt{s_{NN}} \geq 39$ GeV [17,19]. The susceptibility ratio can be compared to a corresponding ratio of experimentally measured cumulants.

This Letter reports C_6/C_2 of event-by-event net-proton multiplicity ($N_p - N_{\bar{p}} = \Delta N_p$) distributions for Au + Au collisions at $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV. These three collision energies correspond to $\mu_B = 144, 83$, and 28 MeV, respectively, for the most central collisions [20]. The datasets for $\sqrt{s_{NN}} = 54.4$ and 27 GeV were taken in 2017 and 2018. The data for 200 GeV were collected in 2010 and 2011. The numbers of events analyzed for 0%–80% centrality at $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV are around 280, 520, and 900×10^6 , respectively. All data were taken with a minimum bias trigger, except for 0%–10% centrality of 200 GeV data in 2010, which was taken with a special trigger with enhanced

event samples for central collisions. All data were taken with the time projection chamber (TPC) and the time of flight (TOF) detector at the solenoid tracker at RHIC (STAR). Events occurring within $|\Delta Z| < 30$ cm from the center of the TPC along the beam line (Z direction) are selected. The transverse positions of the collisions are required to be within $|\Delta R| < 2$ cm to reject interactions between the beam and the beam pipe [20]. Events from pileup, which is defined as the superposition of several single-collision events occurring within a small space and time interval, are rejected by cutting on the correlation between the charged particle multiplicity measured by the TPC and extrapolated tracks from the TPC to the hit positions in the TOF.

The collision centrality is defined using the charged particle multiplicities measured by the TPC in $|\eta| < 1.0$. Protons and antiprotons are excluded from the above centrality definition in order to minimize self-correlation effects [21]. Event-by-event numbers of protons and antiprotons are measured at midrapidity $|\eta| < 0.5$ for the transverse momentum range $0.4 < p_T(\text{GeV}/c) < 2.0$. Protons and antiprotons at $0.4 < p_T(\text{GeV}/c) < 0.8$ are identified using ionization energy loss distributions measured by the TPC (dE/dx), while at $0.8 < p_T(\text{GeV}/c) < 2.0$ they are identified using the mass squared (m^2) distributions measured by the TOF as well. The lower limit of the p_T range is chosen to reject the secondary protons produced by interactions with the beam pipe. Requiring the distance of closest approach to be less than 1 cm with respect to the collision vertex suppresses the effect from the contribution of weak decay daughter protons. Weak decay protons which passed this cut are all included in the analysis. Up to the fourth order, the effect of the decay is found to be small [22]. The purity of protons and antiprotons in the analyzed acceptance is higher than 95% for $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV.

Event-by-event net-proton number (ΔN_p) distributions for Au + Au collisions at $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV for 0%–10% and 30%–40% centralities are shown in Fig. 1. The plotted distributions are normalized by the corresponding total number of events and are not corrected for detector efficiencies. The distributions for 0%–10% are broader than for 30%–40% as more protons and antiprotons are produced in central collisions. The shape of the distribution is characterized by various orders of cumulants [23]. Definitions and formulas for cumulant calculations can be found in Supplemental Material [24]. Cumulants are extensive variables proportional to the volume of the collision system [23]. This undesired volume effect is canceled by taking the ratio of different order cumulants. Then the C_6/C_2 value can be compared with the ratio of baryon number susceptibilities (χ_6^B/χ_2^B) from lattice QCD calculations, keeping in mind the difference between net baryon from theory calculations and net proton from the data within the limited experimental acceptance. When

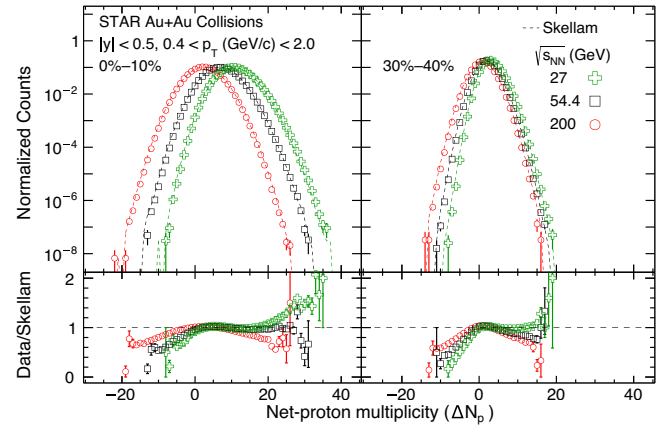


FIG. 1. Event by event net-proton multiplicity ΔN_p distributions for Au + Au collisions at $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV in 0%–10% (left) and 30%–40% (right) centralities at midrapidity ($|\eta| < 0.5$) for the transverse momentum range of $0.4 < p_T(\text{GeV}/c) < 2.0$. These distributions are normalized by the corresponding numbers of events and are not corrected for detector efficiencies. Statistical uncertainties are shown as vertical lines. The dashed lines show the Skellam distributions for each collision energy and centrality. The bottom panels show the ratio of the data to the Skellam expectations.

multiplicities of protons and antiprotons follow Poisson distributions, the resulting net-proton distribution is called a Skellam distribution. The odd-order and even-order cumulants of the Skellam distribution are expressed by the difference and sum of the mean values (C_1) of the Poisson distributions, respectively. Hence, $C_6/C_2 = 1$ for the Skellam distribution. The Skellam distributions determined from C_1 of protons and antiprotons for each collision energy and centrality are shown by dashed lines in Fig. 1. According to the ratio of data to the Skellam expectations, shown in the lower part of Fig. 1, deviations from the Skellam distributions are seen especially at the tails of the distribution.

It is known that the statistical uncertainties on higher-order cumulants become larger for broader distributions [21]. A model study indicates that higher-order cumulants suffer from larger statistical uncertainties. The effect increases with increasing order of the cumulant [25]. Statistical uncertainties also depend on the detector efficiencies. A lower efficiency gives larger statistical errors for cumulants after efficiency corrections.

A centrality bin width correction is applied for each centrality bin to suppress the effect from the initial volume fluctuations [21,26,27]. Statistical uncertainties are calculated using a bootstrap method [21,28].

All results of C_6/C_2 presented in this Letter are corrected for the detector efficiency assuming that the detector efficiencies follow the binomial distribution [25,29–35]. Nonbinomial efficiencies [36] are also studied through detector simulations in the STAR environment. Cumulants are corrected for nonbinomial efficiencies using the

unfolding and moment expansion approaches [37,38]. Results up to the sixth-order cumulant for Au + Au central collisions at $\sqrt{s_{NN}} = 200$ GeV are presented in Supplemental Material [24]. It is concluded that the results corrected for nonbinomial efficiencies are consistent with the results from the binomial efficiency correction within statistical uncertainties.

Systematic uncertainties are estimated by changing the following variables used to select protons and antiprotons: the distance of closest approach to the primary collision vertex and number of hits in the TPC to reconstruct tracks for the track quality cut, dE/dx , and m^2 selections for (anti) proton identification criteria. A Barlow check is done to remove the statistical effects from being counted as part of systematic uncertainties [39]. The contribution from track quality cuts is dominant for central collisions. The systematic uncertainties from each source go down below 10% in peripheral collisions. The uncertainties for each source are then added in quadrature. The total systematic uncertainties are 87%, 70%, and 37% at 27, 54.4, and 200 GeV, respectively, for 0%–10% central collisions, and the corresponding totals decrease down to a few percent in peripheral collisions.

Figure 2 shows the net proton C_6/C_2 for Au + Au collisions for 0%–10% and 30%–40% centralities at $\sqrt{s_{NN}} = 27$, 54.4, and 200 GeV as a function of rapidity and p_T acceptance. The values of C_6/C_2 approach the Skellam expectation, $C_6/C_2 = 1$, with narrow acceptance

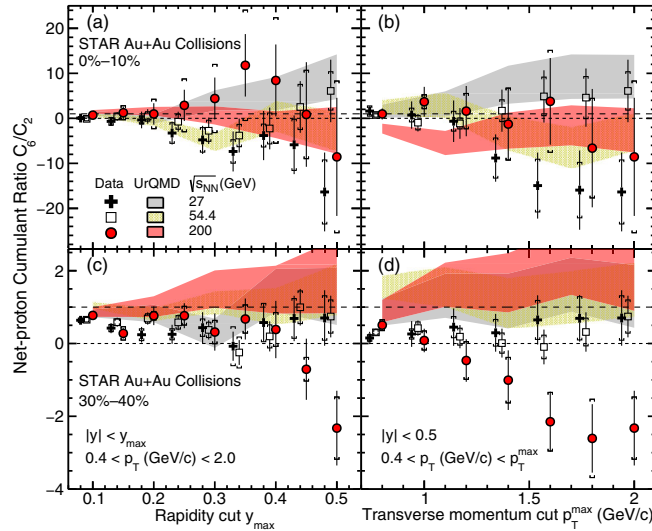


FIG. 2. Net-proton C_6/C_2 as a function of rapidity (left) and transverse momentum acceptance (right) from $\sqrt{s_{NN}} = 27$ (crosses), 54.4 (open squares), and 200 GeV (filled circles) Au + Au collisions. The upper and lower plots are for 0%–10% and 30%–40% centralities, respectively. The error bars are statistical and caps are systematic errors. Points for different beam energies are staggered horizontally to improve clarity. UrQMD transport model results are shown as shaded and hatched bands. The Skellam expectation ($C_6/C_2 = 1$) is shown as long-dashed lines.

in p_T and rapidity. The reason is that multiplicity distributions of protons and antiprotons are close to the Poisson distribution because of lower particle multiplicity and thus less correlations, and therefore the observed C_6/C_2 is dominated by statistical fluctuations. The fraction of measured protons to total protons integrated in whole p_T region is 33% for $0.4 < p_T(\text{GeV}/c) < 0.8$ and 86% for $0.4 < p_T(\text{GeV}/c) < 2.0$ at 200 GeV. Although the C_6/C_2 values at the smallest acceptance of $|y| < 0.1$ or $0.4 < p_T(\text{GeV}/c) < 0.8$ in Fig. 2 are still smaller than unity, we have checked that the results are consistent with unity with further narrowed acceptance. The C_6/C_2 values for 0%–10% centrality decrease as the acceptance is increased at 27 GeV, while C_6/C_2 is nearly constant for 54.4 and 200 GeV within uncertainties. On the other hand, the results for 30%–40% centrality show a strong decrease with increasing acceptance at 200 GeV and are almost flat for 27 and 54.4 GeV. Results from the transport model UrQMD [40], in which hadronic interactions are dominant and there is no phase transition implemented, are shown by shaded and hatched bands in Fig. 2. The event statistics used in the UrQMD calculations are 215 , 100 , and 95×10^6 for 27, 54.4, and 200 GeV minimum bias Au + Au collisions, respectively. All experimental cuts in terms of the collision centrality, rapidity, and transverse momentum acceptance are applied in the calculations. The C_6/C_2 values from UrQMD are flat as a function of rapidity and p_T acceptance at 27 and 200 GeV, while the sign changes for central collisions at 54.4 GeV albeit with large uncertainties. Note that the thermal blurring in rapidity for conserved charges is discussed in Ref. [41]. More studies are necessary in order to understand the rapidity dependence as a function of collision energies.

In Fig. 3, the centrality dependence of the net-proton C_6/C_2 at midrapidity is shown for all three collision energies. The data with the largest number of participant nucleons (N_{part}) correspond to the top 0%–10% central collisions and the rest of the points are for 10%–20%, 20%–30%, 30%–40%, ..., and 70%–80% centralities. For 200 GeV collisions (filled circles), C_6/C_2 values are approaching the Skellam expectation ($C_6/C_2 = 1$) from central to peripheral collisions. The C_6/C_2 values then start to be negative from 50%–60% centrality, and stay negative systematically in central collisions within large uncertainties. Most C_6/C_2 measurements at 27 and 54.4 GeV are consistent with zero within uncertainties. We find that the C_6/C_2 values are negative within 1.7 sigma at 200 GeV 30%–40% centrality with statistical and systematic uncertainties added in quadrature.

QCD-inspired model calculations [16] show that at vanishing baryon chemical potential, the crossover transition from the QGP to hadronic phase and its remnants will affect higher-order cumulant ratios. The model further suggests that the value of C_6/C_2 of the net-baryon distribution should be positive and negative for the

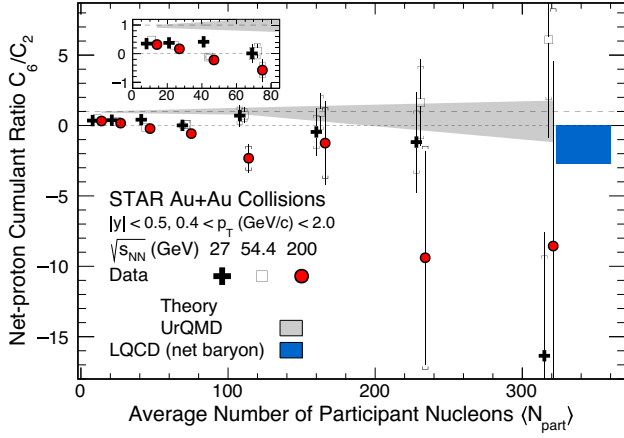


FIG. 3. Collision centrality dependence of net-proton C_6/C_2 in Au + Au collisions for $\sqrt{s_{NN}} = 27, 54.4$, and 200 GeV within $|y| < 0.5$ and $0.4 < p_T(\text{GeV}/c) < 2.0$. The error bars are statistical and caps are systematic errors. Points for different beam energies are staggered horizontally to improve clarity. A shaded band shows the results from UrQMD model calculations. UrQMD calculations from the above three collision energies are consistent among them so they are merged in order to reduce statistical fluctuations. Details on these calculations can be found in Supplemental Material [24]. The lattice QCD calculations on net-baryon number fluctuations [17,19] for $T = 160$ MeV and $\mu_B < 110$ MeV are shown as a blue band at $\langle N_{\text{part}} \rangle \approx 340$. The inset shows the expanded region of 40%–80% centrality.

emerging medium from hadronic and QGP phases, respectively. All of the results from the UrQMD calculations are consistent with the Skellam expectation ($C_6/C_2 = 1$) within large statistical fluctuations toward more central collisions. Overall, the UrQMD calculations of the net-proton C_6/C_2 reproduce, within errors, the measured centrality dependence for 27 and 54.4 GeV Au + Au collisions. Experimental results for 200 GeV are below UrQMD calculations systematically from peripheral to central collisions.

First-principle lattice QCD calculations offer accurate information on the properties of a thermalized system with zero baryon chemical potential. For example, see Ref. [4]. By a Taylor expansion at small μ_B , one could extend the predictions to finite values of the baryon chemical potential. The lattice calculations with a temperature of 160 MeV and baryon chemical potential up to $\mu_B \sim 110$ MeV are shown as the blue band in Fig. 3 [17,19]. Lattice calculations also indicate that in the region of $\mu_B/T < 1$, the transition from QGP to hadronic matter is a smooth crossover [17]. The μ_B/T ratios are approximately 0.17, 0.55, and 0.93 for central Au + Au collisions at $\sqrt{s_{NN}} = 200, 54$, and 27 GeV, respectively. Please note there are caveats when comparing experimental data with lattice calculations. While the current experimental data are midrapidity net-proton distributions from the kinematic region of $|y| < 0.5$ and $0.4 < p_T(\text{GeV}/c) < 2.0$, the lattice results are for net baryons and do not incorporate any of the

experimental kinematic cuts [29]. It is also known that the cumulants are affected by both baryon number conservation and baryon stopping [42–45] which are expected to be more significant toward lower collision energies [46,47]. Both effects are present in the results presented here. In addition, the lattice simulates a thermalized system but without other dynamics such as collective expansion in high-energy nuclear collisions. These differences between experiments and lattice calculations need to be carefully handled in the future for a quantitative comparison. With these caveats in mind, the trend observed in Au + Au collisions at 200 GeV that C_6/C_2 becomes negative with increasing centrality is potentially consistent with the smooth crossover scenario. Higher statistics datasets are necessary in order to establish a trend in the finite μ_B range.

In summary, we report the first measurements of the net-proton higher-order cumulant ratio C_6/C_2 from 27, 54.4, and 200 GeV Au + Au collisions measured by the STAR detector at RHIC. The data are taken from the kinematic region [$|y| < 0.5$ and $0.4 < p_T(\text{GeV}/c) < 2.0$]. Data from 200 GeV collisions are found to be negative progressively in more central collisions within the maximum acceptance, while the ratios from 27 and 54.4 GeV collisions are found to be close to zero within uncertainties. Without critical dynamics, the transport model UrQMD calculations predict the ratio C_6/C_2 around a statistical baseline in all cases. Lattice QCD calculations, with $T = 160$ MeV and $\mu_B = 0$ –110 MeV, predict the negative value of $C_6/C_2 \sim -1.5$, which is qualitatively consistent with the experimental results of central Au + Au collisions at top RHIC energies. These new measurements are statistics limited and seem to favor a smooth crossover for the QGP-hadronic matter transition. Future measurements with high statistics will provide more detailed information about the phase structure at the low baryon density region.

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