# Hybrid Magnonics for Short-Wavelength Spin Waves Facilitated by a Magnetic Heterostructure

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Recent research on hybrid magnonics has been restricted by the long magnon wavelengths of the ferromagnetic resonance modes. We present an experiment on the hybridization of 250-nm-wavelength magnons with microwave photons in a multimode magnonic system consisting of a planar cavity and a magnetic bilayer. The coupling between magnon modes in the two magnetic layers, i.e., the uniform mode in Permalloy and the perpendicular standing spin waves (PSSWs) in yttrium iron garnet, serves as an effective means for exciting short-wavelength PSSWs, which is further hybridized with the photon mode of the microwave resonator. The demonstrated magnon-photon coupling approaches the superstrong coupling regime, and can even be achieved near zero bias field.

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# I. INTRODUCTION

Owing to their unique tunability and compatibility, magnons (as elementary excitations of spin waves) are considered advantageous carriers to bridge different quantum systems [1–6]. This is especially relevant if one uses yttrium iron garnet (YIG),  $Y_3Fe_5O_{12}$ , due the material's low damping rate and high spin density [7]. In particular, in the context of developing hybrid quantum systems, the coherent coupling between YIG magnons and microwave photons has exhibited excellent properties such as the ability to enter the strong coupling regime, opening opportunities for a wide range of useful applications such as nonreciprocal microwave devices [8–13] and dark matter detection [14–16].

Nevertheless, most of the works so far on magnonmicrowave photon hybridization have been done in the context of a macroscopic microwave cavity coupled to the uniform magnon mode, i.e., ferromagnetic resonance (FMR) of YIG spheres, with only a few examples of using microscale circuit-based resonators and coupling with relatively low-order magnon modes [1,17–19]. It is well known that magnons have a rich dispersion and can exist in many different mode forms; therefore, it is straightforward to extend such mode hybridization to other types of magnons to take advantage of their unique properties. In particular, when the magnon wavelength is reduced to the nanometer scale, exchange interactions start to set in as the underlying mechanisms for magnon excitation, which will lead to useful physics and applications. However, the inefficient cavity excitation of spin waves due to their weak coupling to microwave photons severely limits such explorations.

Recently, it has been demonstrated that the magnonmagnon coupling in magnetic heterostructures provides an efficient route towards exciting short-wavelength magnons by microwave signals [20-24]. Due to the interfacial exchange torque, high-order magnon modes can be effectively excited by other magnons, whose footprints are then governed by the magnons' dispersion and are not limited by the conventional electromagnetic wave excitations. Leveraging this approach, here we present an experimental demonstration of a hybrid magnonic system with a magnon wavelength as short as approximately 250 nm. Figure 1 illustrates our multimode cavity magnonic system comprised of a bus waveguide coupled to a resonator that is further coupled to a YIG/permalloy (Py) hybrid magnonic system. In our experimental realization, as shown in Fig. 2(a), the resonator is a planar split-ring resonator (SRR) coupled to a bus waveguide (feedline),

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FIG. 1. Schematic of the multimode cavity magnonic system consisting of a linearly coupled magnon-magnon system:  $m_{Py} \rightleftharpoons m_{YIG}$ . Here g,  $\kappa_{Py}$ , and  $\kappa_{YIG}$  are the coupling strength and dissipation rates of the respective magnon subsystems. The hybridized magnon modes further couple to a resonator with a dissipation rate  $\kappa_p$ , via a magnon-photon coupling  $g_p$ . The resonator is coupled to a waveguide bus (feedline), via  $\kappa_e$ .

and the magnonic system is an exchange-coupled YIG/Py bilayer. In the Py-biased YIG thin film, the magnons  $(m_{\rm YIG}^n)$  form a series of perpendicular standing spin waves (PSSWs), with wavelengths that can reach the mesoscale regime, at frequencies  $\omega_{\text{YIG}}^n$  with a magnon dissipation rate  $\kappa_{\rm YIG}$ , where *n* is the mode order. These modes couple to the uniform mode of Py  $m_{Py}$  (at frequency  $\omega_{Py}$  with a magnon dissipation rate  $\kappa_{Py}$ ), and the coupling strength is  $g_m$ . Such hybridized magnon modes further couple to the SRR, with a photon dissipation  $\kappa_p$ . The magnon-photon coupling between the hybridized magnon modes and the resonator is  $g_p$ . Finally, the resonator has a coupling coefficient  $\kappa_e$  to the bus waveguide. The square SRR has an outer dimension of  $6.5 \times 6.5 \text{ mm}^2$  and an inner dimension of  $3.5 \times 3.5$  mm<sup>2</sup>. The gap width and distance to the bus waveguide are both 0.2 mm [see Fig. 2(a)]. The SRR resonates at a photon frequency  $\omega_p/2\pi = 2.912$  GHz [Fig. 2(b)] and the dissipation rate is  $\kappa_p/2\pi = 17.6$  MHz, yielding a photon quality (Q) factor of approximately 83.

## **II. SAMPLE AND MEASUREMENT**

The YIG/Py sample is in the shape of a  $2.5 \times 2$ -mm<sup>2</sup> slab, and consists of a sputtered Py layer (30-nm thick) on top of a 3- $\mu$ m-thick, single-sided, commercial single-crystal YIG film grown on double-side-polished

 $Gd_3Ga_5O_{12}$  substrate using liquid-phase epitaxy. Following our earlier recipes for ensuring a good YIG/Py interfacial exchange coupling [24], we used *in situ* argon gas rf-bias cleaning for 3 min in a vacuum chamber, to clean the YIG surface before depositing the 30-nm Py layer.

During the measurement, the samples are mounted in the flip-chip configuration (Py side facing down) on top of the board for broadband microwave excitation. Two testing configurations are used with the YIG/Py sample placed at two different positions: (1) inside the SRR and (2) on top of the bus waveguide (feedline, along x), as shown in Fig. 2(a). An external bias field, H, can be applied at an angle  $\phi$  with respect to the normal axis (z) using an electromagnet, where  $\phi = 90^{\circ}$  corresponds to the field in the plane (along y). To achieve the best signal quality, we use the field-modulated FMR technique (as opposed to conventional vector-network analyzer measurement) with a modulation frequency of  $\Omega/2\pi = 81.57$  Hz (supplied by a lock-in amplifier and provided by a pair of modulation coils) and a modulation field of about 1.1 Oe. This modulation level has been tested and chosen not only to be insensitive to the Py resonance profile, but also to give the optimal signal strength of the hybridized magnon modes due to the sharp YIG PSSW profile. The microwave signal is delivered from a signal generator (10 dBm) to one port of the board. The field-modulated FMR signal is measured from the other port by the lock-in amplifier in the form of a dc voltage, V, by using a sensitive rf diode. We sweep the bias field H and at each incremental frequency f to construct the V[f, H] dispersion contour plots.

#### **III. RESULTS AND DISCUSSION**

We first perform a rough scan (f step size of 10 MHz) at larger field range ( $\pm 1$  kOe) for the sample placed at the respective (1) and (2) positions with the purpose of identifying the nature of the coupling by characterizing the YIG resonance. Figure 2(c) shows the V[f, H] contour plot for the YIG/Py placed inside the SRR [position (1)] and at a bias field angle  $\phi = 45^{\circ}$ . This configuration corresponds to the conventional magnon-photon coupling scenario except that we are using a planar resonator instead of a three-dimensional cavity. Accordingly, a standard avoided crossing is observed in the spectra, at  $H \sim 600$ Oe, when the YIG uniform mode crosses the SRR's photon mode.

Interestingly, a series of additional spin-wave modes are also observed, at the lower fields ( $\pm 200$  Oe) and even persisting down to H = 0 Oe, indicating an almost zerofield excitation. These modes, which are much farther away from the YIG's uniform mode, are identified as the hybrid magnon modes caused by the magnon-magnon coupling between the Py uniform mode and the YIG's PSSW modes. In other words, the Py FMR serves as an effective exciter for the PSSWs under its broad resonance envelope



FIG. 2. (a) Schematic of the experimental setup, showing the SRR and the YIG/Py bilayer sample. The YIG/Py can be positioned at location (1) or (2). The dimensions and relative positions between the sample and the SRR are also illustrated. The magnetic field H can be applied at an angle  $\phi$  with respect to the *z* axis. (b) The photon mode of the SRR, characterized using a vector-network analyzer. The SRR resonates at a photon frequency  $\omega_p/2\pi = 2.912$  GHz. A rough scan of the two-dimensional (2D) dispersion contour plot V[f, H] for the two testing positions in (a): either inside the SRR (c) or on top of the waveguide (d). The frequency step size is 10 MHz.

[24]. These modes are only pronounced in a small frequency range, from approximately 2.8 to 3.0 GHz, around the photon resonance.

We further quantify these hybridized modes by calculating their dispersion relations. Due to the large difference in the magnetization of YIG and Py, the observed PSSW modes that are actively coupled to the Py uniform mode are of a higher index,  $n \sim 20-25$ , which corresponds to spinwave wavelengths in the range of  $\lambda \sim 240-300$  nm. Compared with previous demonstrations that are mostly limited to FMR magnons or low-order magnetostatic magnon modes, our demonstration brings the hybrid magnonic systems into the short-wavelength regime.

Figure 2(d) shows the V[f, H] contour plot for the YIG/Py placed at the other position, i.e., on top of the bus waveguide [position (2)] and at the same field angle  $\phi = 45^{\circ}$ . Similarly, the series of hybrid PSSW modes are observed for bias field strength below 200 Oe. In addition, due to the influence from the traveling wave excitation, such low-field hybrid modes can be detected in a much broader frequency regime as compared with Fig. 2(c). These modes are again attributed to the uniform mode of the Py exciter coupling to the YIG's PSSWs. We

also perform such measurements at other magnetic field angles,  $\phi = 1^{\circ}, 15^{\circ}, 30^{\circ}, 60^{\circ}, 75^{\circ}, 90^{\circ}$ , for both positions (1) and (2), and the results are included in the Supplemental Material [25]. We can observe such magnon excitation and hybridization at almost all angles. The magnetic field orientation also provides a nice way of tuning the field spacing in the spectrum between different adjacent PSSW modes.

To further analyze the hybrid magnon modes and their magnon-photon coupling with the photon mode, we then perform a fine scan (f step size of 1 MHz) in a smaller field range ( $\pm 400$  Oe) for the sample placed again at the respective (1) and (2) positions. The bias magnetic field is again applied at the field angle  $\phi = 45^{\circ}$ . Figure 3 summarizes the results for the sample located inside the SRR [position (1)]. Figures 3(a)–3(c) display example signal traces at three selective frequencies, at: 2.985 GHz, above and away from the photon mode [Fig. 3(a)]; 2.935 GHz, immediately after the photon mode [Fig. 3(c)]. At least five hybrid magnon modes can be clearly observed near the photon resonance frequency [see Figs. 3(b) and 3(c)]. The signal amplitude decreases rapidly as the frequency



FIG. 3. The fine-scan datasets at the low-field regime (focusing on the hybridized magnon modes) for testing position (1): inside the SRR. The signal traces at selective frequencies of (a) 2.985, (b) 2.935, and (c) 2.905 GHz, and (d) the corresponding 2D contour plot. The frequency step size is 1 MHz. In (d), we also overlay the frequencies of the hybrid modes (dots) extracted from our theoretical calculation using Eq. (1) on the experimental measurement results.

shifts away from the photon mode. For example, the signal at f = 2.985 GHz is almost negligible.

In addition, we note that both the phase and amplitude of the magnon modes are center-symmetric with respect to the field H = 0 Oe, which agrees with the theory of cavity photon-magnon hybridization. Such fieldsymmetric magnon dispersion can be also evidenced from the scanned two-dimensional (2D) contour plot V[f, H][see Fig. 3(d)]. Finally, these hybridized magnon modes show an avoided crossing as their spin-wave dispersion passes through the photon mode. In other words, we herein observe the magnon-photon hybridization using magnon-magnon hybridized modes, with a significantly reduced magnon wavelength as compared with previous demonstrations.

The hybridization of the PSSW modes in YIG with the FMR mode in Py modifies their intrinsic properties. Previously, these modes could not be directly read out in the cavity transmission signal because of the weak interaction between the long-wavelength microwave photons and the short-wavelength PSSW magnons. Upon hybridization with the Py FMR mode, the modified PSSW modes have much stronger coupling with the photon mode. On the other hand, the FMR mode of Py is also modified by its interaction with the PSSW modes. However, since (1) the Py FMR mode is very lossy and (2) our field-modulation strength is only approximately 1 Oe, our lock-in measurement is much less sensitive to the broad Py FMR envelope. As a result, we can ignore it to simplify our analysis in the following, and we can treat our device as a coupled

magnon-photon system, with the magnon mode being the modified PSSW modes in YIG.

Under this simplified condition, the rf signal transmission, T, through the device (before the lock-in detection) can be expressed as [26]

$$T = \left| 1 - \frac{2\kappa_e}{i(\omega_p - \omega) + \kappa_p + \sum_n \frac{g_n^2}{i(\omega_n - \omega) + \kappa_n}} \right|^2, \quad (1)$$

where  $\omega$  is the frequency of the rf signal used in the measurement. It is worth noting that there exist multiple PSSW modes that can interact with the photon mode, which are accounted for by the summation over the mode order *n*. Here,  $\omega_n$ ,  $\kappa_n$ , and  $g_n$  are the frequency, dissipation rate, and coupling strength (with the photon mode) of the *n*-th modified PSSW mode, respectively.

In our measurements, the rf signal transmission is not directly measured, but instead the device output is first sent through a diode envelope detector and then measured by a lock-in amplifier. In our lock-in measurement scheme, the periodically varying bias magnetic field introduces a modulation to the magnon frequency  $\omega_n$ , which can be simplified as  $\omega'_n = \omega_n [1 + d \sin(\Omega t)]$ , where the modulation depth *d* is of the order of 1%. The magnonic response of our device is then extracted by detecting the  $\Omega$  frequency components in the transmitted rf signals.

By far-detuning the magnons from the cavity mode, we can determine the frequency and linewidth of each mode by Lorentzian fitting, and the coupling strength is



FIG. 4. The theoretically calculated magnon-photon spectra (2D contour plot) in the low-field regime using Eq. (1). The frequencies of the hybrid modes (dots) are extracted and overlaid on the spectrum.

determined through theoretical fitting and calculation. The lock-in signal spectrum calculated based on parameters extracted from our measurements ( $\kappa_p/2\pi = 17.6$  MHz,  $\kappa_n/2\pi = 5.5$  MHz,  $g_n/2\pi = 22.4$  MHz, PSSW spacing of 35.2 Oe) is plotted in Fig. 4, which well reproduces the measurement results shown in Fig. 3(d). To compare our experiment with the theory, we extract the frequencies of the hybrid modes from our theoretical calculation and overlay them on the experimental measurement results in Fig. 3(d), which show a good agreement with the measured hybrid mode traces. Further, it is worth noting that the coupling strength  $g_n$  is of the same order as the free spectral range (FSR/ $2\pi$  = 112.6 MHz) of the PSSW modes, indicating that our system is near the superstrong coupling regime, which has been attracting much research interest recently because of its great potential for intriguing physical properties [27,28]. Finally, we also measure the fine-scan spectra for the sample located on top of the feedline [position (2)] at several selected field orientations. Similar observations are found and the comprehensive dataset is included in the Supplemental Material [25].

## **IV. CONCLUSION**

In summary, we report an experiment involving a multimode cavity magnonic system comprising a planar resonator-feedline coupled to a YIG/Py bilayer. The magnon-magnon coupling in the YIG/Py bilayer serves as an effective means for exciting short-wavelength PSSW modes. Such short-wavelength modes can further hybridize with the photon mode of the resonator. The demonstrated magnon-photon coupling approaches the superstrong coupling regime, and can even be achieved near zero bias field. Compared with previous demonstrations that are mostly limited to FMR magnons or low-order magnetostatic magnon modes, our demonstration brings the hybrid magnonic systems into the short-wavelength regime (towards exchange magnons) and opens opportunities for on-chip integration. In addition, such a spin-wave excitation by magnon-magnon coupling to Py is very close to zero bias field, which renders it practically interesting for potentially "field-free" related applications [29–31] or experiments that are sensitive to and/or incompatible with large external magnetic fields such as superconducting circuits. Finally, we note that the same system may also be of interest in studying other topics in the field of hybrid magnonics such as dissipative coupling and level attraction [32], surface spin-wave hybridization [33], nonlinear control of magnon polaritons [34], and coupling-induced transparency [35].

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