

Measurement of the photon polarization in $\Lambda_b^0 \rightarrow \Lambda \gamma$ decays

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The photon polarization in $b \rightarrow s \gamma$ transitions is measured for the first time in radiative b -baryon decays exploiting the unique spin structure of $\Lambda_b^0 \rightarrow \Lambda \gamma$ decays. A data sample corresponding to an integrated luminosity of 6 fb^{-1} collected by the LHCb experiment in pp collisions at a center-of-mass energy of 13 TeV is used. The photon polarization is measured to be $\alpha_\gamma = 0.82_{-0.26-0.13}^{+0.17+0.04}$, where the first uncertainty is statistical and the second systematic. This result is in agreement with the Standard Model prediction and previous measurements in b -meson decays. Charge-parity breaking effects are studied for the first time in this observable and found to be consistent with CP symmetry.

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Rare decays of hadrons containing b -quarks mediated by flavor-changing neutral currents (FCNC) are suppressed in the Standard Model (SM) since they occur only at higher order in the perturbative expansion. They are sensitive to physics beyond the SM (BSM) which can give additional contributions and alter the decay properties. Radiative decays of the type $b \rightarrow s \gamma$ are FCNC, mediated by electroweak-loop transitions which produce a final state photon. In the SM, due to the chirality of the electroweak interaction, the emitted photons are polarized. The photon polarization is defined as the normalized difference between the number of left-handed (γ_L) and right-handed (γ_R) photons produced in radiative decays,

$$\alpha_\gamma \equiv \frac{\gamma_L - \gamma_R}{\gamma_L + \gamma_R}, \quad (1)$$

with photons emitted in b decays being predominantly left handed. Right-handed contributions arise only due to chirality flips in the outgoing s -quark line of the Feynman diagram, which are suppressed by the ratio of the s and b quark masses. At leading order in the SM, the photon polarization is predicted to be $\alpha_\gamma = (1 - |r|^2)/(1 + |r|^2)$, with $|r| \approx m_s/m_b$ [1–3]. Effects arising at next-to-leading order are estimated to be at the percent level [2]. Therefore, a larger right-handed polarization, which would lower the value of α_γ , could be a clear indication of BSM physics [1,4].

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The photon polarization in $b \rightarrow s \gamma$ transitions has been indirectly probed by the BaBar, Belle, and LHCb experiments through the measurement of mixing-induced charge-parity (CP) asymmetries in B^0 and B_s^0 decays [5–7] and through the angular analysis of $B^0 \rightarrow K^{*0} e^+ e^-$ decays at very low dielectron mass [8], with the latter providing the strongest constraints on right-handed currents. Radiative decays of b baryons offer a unique opportunity for a direct measurement of the photon polarization due to the nonzero spin of the initial- and final-state particles [9]. The $\Lambda_b^0 \rightarrow \Lambda \gamma$ decay¹ is of special interest due to the weak decay of the Λ baryon, which probes the helicity structure of the $b \rightarrow s \gamma$ transition through the measurement of the Λ helicity [2,10]. The $\Lambda_b^0 \rightarrow \Lambda \gamma$ decay was first observed in data recorded by LHCb during 2016 [11]. The photon-polarization sensitivity using this decay was estimated in Ref. [12].

The angular distribution of $\Lambda_b^0 \rightarrow \Lambda \gamma$ decays, where the Λ baryon decays into a proton and a pion, is given by the differential width [3]

$$\frac{d\Gamma}{d(\cos \theta_p)} \propto 1 - \alpha_\gamma \alpha_\Lambda \cos \theta_p, \quad (2)$$

where α_Λ is the Λ weak-decay parameter, which describes the interference between the parity-violating s -wave and parity-conserving p -wave of the $\Lambda \rightarrow p \pi^-$ decay [13], and θ_p is the angle between the proton momentum and the negative Λ_b^0 momentum in the Λ rest frame. The photon direction is integrated over in this study since the distribution in this variable is flat for unpolarized Λ_b^0 baryons, as produced at the LHC [14,15].

¹The inclusion of charge-conjugate processes is implied throughout, except in the discussion of asymmetries.

Contrary to b decays, photons produced in $\bar{b}$ decays are expected to be predominantly right handed in the SM, resulting in a photon polarization of $\alpha_\gamma = -1$. A discrepancy in the absolute value of the photon polarization in b and $\bar{b}$ decays would be a hint of CP asymmetry in these transitions. In the SM, CP asymmetries in $b \rightarrow s\gamma$ decays are estimated to be less than $\mathcal{O}(1\%)$ [2]. However, new CP -violating BSM contributions can produce asymmetries of $\mathcal{O}(10\%)$ [2]. Experimentally, the strongest constraint on direct CP violation in $b \rightarrow s\gamma$ transitions is from $B^0 \rightarrow K^{*0}\gamma$ decays [16]. Measurements of angular asymmetries and CP -conjugated decay branching ratios can separate the CP -odd and CP -even components of both the SM and opposite chirality contributions to the $\Lambda_b^0 \rightarrow \Lambda\gamma$ decay rate [2].

This paper reports the first measurement of the photon polarization in $\Lambda_b^0 \rightarrow \Lambda\gamma$ decays, with $\Lambda \rightarrow p\pi^-$, using a data sample corresponding to an integrated luminosity of 6 fb^{-1} collected by the LHCb experiment in proton-proton (pp) collisions at a center-of-mass energy of 13 TeV during 2015–2018. Additionally, the first study of CP angular asymmetries in $b \rightarrow s\gamma$ decays is performed.

The LHCb detector [17,18] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector elements that are relevant for this analysis are; a silicon-strip vertex detector surrounding the pp interaction region that allows c and b hadrons to be identified from their characteristically long flight distance, a tracking system that provides a measurement of the momentum of charged particles, two ring-imaging Cherenkov detectors that are able to discriminate between different species of charged hadrons, a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter (ECAL) and a hadronic calorimeter that enables the reconstruction and identification of photons, electrons, and hadrons, and a muon system composed of alternating layers of iron and multiwire proportional chambers.

Charged and neutral clusters in the ECAL are separated by extrapolating reconstructed tracks to the ECAL; photons and neutral pions are distinguished by their cluster shape and energy distribution. For decays with high-energy photons in the final state, e.g., $\Lambda_b^0 \rightarrow \Lambda\gamma$, a mass resolution around 100 MeV is achieved² [19,20], dominated by the photon energy resolution. The online event selection is performed by a trigger [21], consisting of a hardware stage followed by a software stage which fully reconstructs the event. The hardware trigger requires events to have an ECAL cluster with an energy component transverse to the beam, E_T , above a threshold varying between 2.1 GeV–3.0 GeV. The software trigger first requires at least one

charged particle to have transverse momentum $p_T > 1 \text{ GeV}$ and to be inconsistent with originating from any primary pp collision vertex (PV). Subsequently, Λ candidates are formed from two tracks significantly displaced from any PV, and combined with a high- E_T photon to identify decays consistent with the signal mode. In the offline selection, trigger signals are associated with reconstructed particles and only events where the trigger was activated by the decay products of the signal candidate are kept.

Simulated events are used to model the effects of the detector geometry and the selection requirements. In the simulation, pp collisions are generated using PYTHIA [22] with a specific LHCb configuration [23]. Decays of unstable particles are described by EVTGEN [24], in which final-state radiation is generated using PHOTOS [25]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [26] as described in Ref. [27]. The signal sample is generated with unpolarized Λ_b^0 decays and only a left-handed photon contribution. The simulation is validated using the $\Lambda_b^0 \rightarrow pK^-J/\psi$ and $\Lambda_b^0 \rightarrow \Lambda J/\psi$, with $J/\psi \rightarrow \mu^+\mu^-$, control modes in the data. The $\Lambda_b^0 \rightarrow pK^-J/\psi$ mode is selected according to Ref. [28], while the $\Lambda_b^0 \rightarrow \Lambda J/\psi$ mode is selected with the strategy described for the signal mode below. The Λ_b^0 momentum distribution of all simulated samples with Λ_b^0 decays is corrected to data in two-dimensional intervals of Λ_b^0 transverse momentum and pseudorapidity, $p_T(\Lambda_b^0)$ and $\eta(\Lambda_b^0)$, using $\Lambda_b^0 \rightarrow pK^-J/\psi$ background-subtracted data and simulated candidates.

Offline signal candidates are reconstructed from the combination of a Λ baryon and a high-energy photon candidate. Opposite-charge good-quality track pairs, well separated from any PV, are combined to form Λ candidates, where one track is consistent with the proton hypothesis and the other with the pion hypothesis. Proton and pion candidates are required to have p_T larger than 800 MeV and 300 MeV, respectively. The Λ candidate must form a good-quality vertex that is well separated from the nearest PV and have a mass in the range 1110 MeV–1122 MeV. Only Λ candidates that decay in the central part of the vertex detector ($z < 270 \text{ mm}$) and have a p_T larger than 1 GeV are retained for further study. Photons, reconstructed from clusters in the ECAL, must have $E_T > 3 \text{ GeV}$ and be inconsistent with the extrapolation of reconstructed tracks to the ECAL. Since the Λ_b^0 decay vertex cannot be reconstructed in this mode, the photon is assumed to originate from the pp interaction region. The sum of the Λ p_T and the photon E_T must be larger than 5 GeV. The Λ_b^0 candidate must have a transverse momentum above 4 GeV and a mass within 900 MeV of the known Λ_b^0 mass [29]. The distance of closest approach between the Λ_b^0 and Λ trajectories is required to be small; the Λ_b^0 trajectory is assumed to originate from the PV closest to the Λ trajectory

²Natural units with $\hbar = c = 1$ are used throughout.

A boosted decision tree (BDT) [30], implementing the XGBoost algorithm [31], used within the Scikit-learn library [32], separates signal from combinatorial background, which is formed by combinations of a real Λ baryon with a random photon. The BDT classifier is trained on a signal sample of $\Lambda_b^0 \rightarrow \Lambda\gamma$ simulated events and a background sample from data candidates with a mass larger than 6.1 GeV. The same variables of Ref. [11], with the addition of the photon pseudorapidity, are used as input for the classifier. To maximize sensitivity to the photon polarization, the BDT threshold is selected to reject 99% of background and retain around 50% of signal candidates.

The mass distribution of the selected candidates is shown in Fig. 1. A fit to this mass distribution is used to determine the signal and background yields. The $\Lambda_b^0 \rightarrow \Lambda\gamma$ signal component is modeled with a Crystal Ball [33] probability density function (PDF), with power-law tails above and below the Λ_b^0 mass. The tail parameters and the width of the signal peak are fixed to values determined from simulation while the mean is allowed to vary freely in the fit to data. A comprehensive set of background contributions is investigated but only two are found to be significant [11]. The dominant contribution is from combinatorial background which is modeled by an exponential PDF with a freely varying slope. A small contamination from $\Lambda_b^0 \rightarrow \Lambda\eta$ decays with $\eta \rightarrow \gamma\gamma$, where one of the photons is not reconstructed, is also expected and is described with the shape determined from simulation. The signal and combinatorial background yields vary freely in the fit to data, while the yield of $\Lambda_b^0 \rightarrow \Lambda\eta$ is constrained to its expected value, obtained from its measured branching fraction [29] and reconstruction and selection efficiencies determined from simulation.

The signal and background yields are obtained from an extended unbinned maximum likelihood fit to data, as shown in Fig. 1 (left). In the signal region, [5387.1, 5852.1] MeV, the signal yield is 440 ± 40 , with

1460 ± 23 and 10 ± 4 combinatorial and $\Lambda_b^0 \rightarrow \Lambda\eta$ decays, respectively.

The photon polarization is measured with an unbinned maximum likelihood fit to the $\cos\theta_p$ distribution for events in the signal region, as shown in Fig. 1 (right). The signal is described by the PDF in Eq. (2) multiplied by an acceptance function, which accounts for the effect of the detector geometry, reconstruction and selection requirements. The photon polarization parameter, α_γ , is allowed to vary freely in the fit to data, whereas the physical boundary $[-1, 1]$ on this parameter is imposed later using the Feldman-Cousins technique [34]. The Λ weak decay parameter, α_Λ , is fixed to the average of the values measured by BESIII in Λ and $\bar{\Lambda}$ decays, $\alpha_\Lambda = 0.754 \pm 0.004$ [35]. The shape of the acceptance in $\cos\theta_p$ is determined from simulation and is parametrized as a fourth-order polynomial. It is dominated by the impact parameter and transverse momentum requirements on the proton and the pion. The correct description of the acceptance in simulation is validated using $\Lambda_b^0 \rightarrow \Lambda J/\psi$ decays, which are reconstructed without using information from the J/ψ vertex. This decay mode, with higher yield and purity than that of the signal mode, has the same final-state hadrons. The combinatorial and $\Lambda_b^0 \rightarrow \Lambda\eta$ components are described together by a fourth-order polynomial, with the coefficients determined from a fit to the candidates in the Λ_b^0 mass control region [4719.6, 5382.1] MeV $\cup$ [5857.1, 6519.6] MeV. The values of these coefficients are found to be consistent for candidates below and above the signal region. The ratio between signal and background decays is constrained by the yields obtained from the mass fit. The fit stability is validated with pseudoexperiments and the results were only examined after all analysis procedures had been finalized in order to avoid experimenter's bias. The result of the fit to data candidates is $\alpha_\gamma = 0.82 \pm 0.23$, where the uncertainty is obtained from the Hessian matrix.

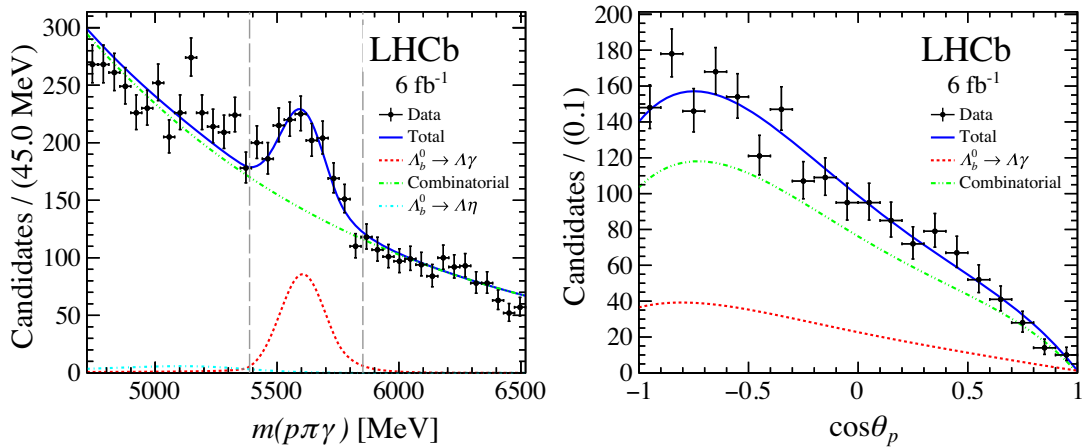


FIG. 1. Distribution of (left) mass, $m(p\pi\gamma)$, and (right) $\cos\theta_p$ for $\Lambda_b^0 \rightarrow \Lambda\gamma$ candidates. The latter shows the subset of candidates in the signal region $m(p\pi\gamma) \in [5387.1, 5852.1]$ MeV, delimited by dashed vertical lines in the former. The results of the fits are overlaid as well as the individual contributions.

The data are separated into $\Lambda_b^0 \rightarrow \Lambda\gamma$ and $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$ by the charge of the final-state pion and potential CP breaking effects on the photon polarization are studied. The photon polarization values in $\Lambda_b^0 \rightarrow \Lambda\gamma$ and $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$ decays, denoted as α_γ^- and α_γ^+ , are expected to have the same absolute value with opposite sign in the absence of CP violation. Both values are measured independently for Λ_b^0 and $\bar{\Lambda}_b^0$ decays following the same strategy as described for the combined sample. The shape of the mass distribution for Λ_b^0 and $\bar{\Lambda}_b^0$ decays is studied in simulation and is compatible, for both signal and $\Lambda_b^0 \rightarrow \Lambda\eta$ decays, therefore the shape from the combined sample is used in the fit of the two data sets. In the signal region, 233 ± 32 $\Lambda_b^0 \rightarrow \Lambda\gamma$ and 210 ± 30 $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$ decays are found. These yields are affected by production and detection asymmetries [36] and cannot be directly interpreted as a measurement of CP -violation effects. The Λ and $\bar{\Lambda}$ weak-decay parameters measured by BESIII [35], $\alpha_\Lambda^- = 0.750 \pm 0.009 \pm 0.004$ and $\alpha_\Lambda^+ = -0.758 \pm 0.010 \pm 0.007$, are used in the angular fit for $\Lambda_b^0 \rightarrow \Lambda\gamma$ and $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$, respectively. Due to the limited sample size, the acceptance and background shapes are taken from the combined sample. The fit to data candidates yields $\alpha_\gamma^- = 1.26 \pm 0.42$ and $\alpha_\gamma^+ = -0.55 \pm 0.32$, where the uncertainty is statistical only. The results of the angular fits are shown in Fig. 2. The measured value of α_γ^- is found to be affected by a 5% bias and a 13% over-coverage driven by boundary effects in this observable.

Systematic uncertainties associated with the determination of the signal and background yields in the mass fit, the modeling of the background shape and signal acceptance and the finite precision on the external parameter α_Λ are evaluated. These uncertainties are determined by fitting pseudosamples, generated by an alternative model, with the default model. The limited data size from the mass control region used to determine the background angular shape dominates this uncertainty and is evaluated by varying the background shape parameters. The systematic uncertainty

of the background parameterization is evaluated using a third- and fifth-degree polynomial. The acceptance uncertainty is evaluated by considering the limited size of the simulation, using alternative fifth- and third-degree parametrizations, and removing the Λ_b^0 kinematic corrections. The mass-fit uncertainty is determined with pseudoexperiments using an alternative model with a variable signal width. Finally, the limited precision of the Λ decay parameter introduces a small systematic uncertainty. The photon polarization, with all systematic uncertainties included, is $\alpha_\gamma = 0.82 \pm 0.23 \pm 0.13$.

For the CP asymmetry measurement, the uncertainties described above are 100% correlated and sum to 0.13 and 0.11 for α_γ^- and α_γ^+ , respectively. Additional uncertainties arise from potential differences in the background shape and signal acceptance between Λ_b^0 and $\bar{\Lambda}_b^0$ decays. Fits are performed with the default combined model to pseudo-samples generated with alternative models obtained independently for Λ_b^0 and $\bar{\Lambda}_b^0$ candidates, to estimate this effect. These uncertainties are uncorrelated and are 0.15 and 0.12 for α_γ^- and α_γ^+ , respectively, resulting in $\alpha_\gamma^- = 1.26 \pm 0.42 \pm 0.20$ and $\alpha_\gamma^+ = -0.55 \pm 0.32 \pm 0.16$.

Confidence intervals on the photon polarization are set within the physical limits of $[-1, 1]$, see Eq. (1), using the Feldman-Cousins technique, the fit result, and the relation between the true and measured values obtained from pseudoexperiments, including both statistical and systematic uncertainties. The photon polarization in $\Lambda_b^0 \rightarrow \Lambda\gamma$ decays is found to be

$$\alpha_\gamma = 0.82_{-0.26}^{+0.17} (\text{stat.})_{-0.13}^{+0.04} (\text{syst.}),$$

which is compatible with the SM prediction. This result excludes two regions allowed by previous measurements for the Wilson coefficients of the effective Hamiltonian of the $b \rightarrow s\gamma$ transition (see the Supplemental material to this paper [37] for details).

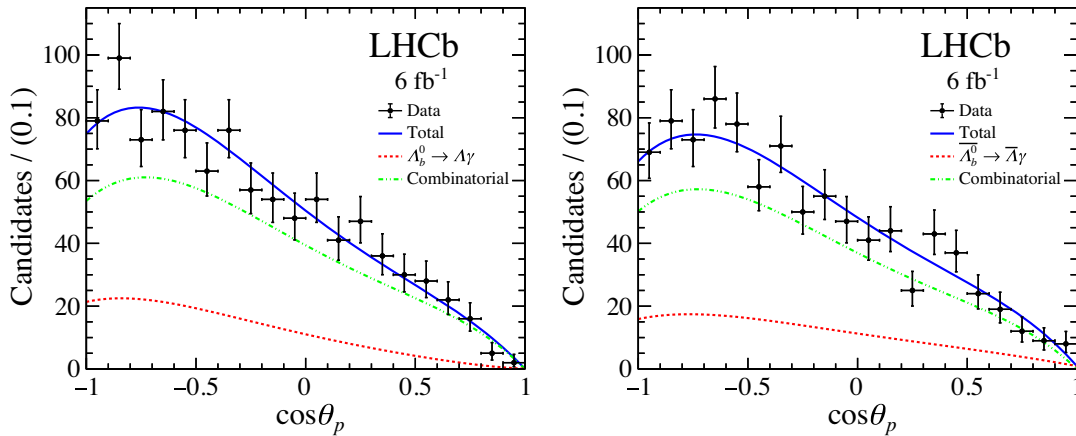


FIG. 2. Distribution of $\cos\theta_p$ for selected (left) $\Lambda_b^0 \rightarrow \Lambda\gamma$ and (right) $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$ candidates as well as the individual contributions.

The Feldman-Cousins technique is also applied to the photon polarization measurements in $\Lambda_b^0 \rightarrow \Lambda\gamma$ and $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}\gamma$ decays, which are found to be

$$\alpha_\gamma^- > 0.56 (0.44) \text{ at } 90\% (95\%) \text{ C.L.},$$

$$\alpha_\gamma^+ = -0.56_{-0.33}^{+0.36} (\text{stat.})_{-0.09}^{+0.16} (\text{syst.}),$$

consistent with CP symmetry.

To summarize, the photon polarization in $b \rightarrow s\gamma$ transitions has been measured for the first time in b -baryon decays exploiting the decay chain $\Lambda_b^0 \rightarrow \Lambda\gamma$, $\Lambda \rightarrow p\pi^-$, which enables the determination of this observable from the angular distribution of the Λ decay products. The α_γ result is compatible with the SM prediction at the level of one standard deviation and provides new constraints that are compatible with previous measurements of the photon polarization in b -meson decays [7,8]. Additionally, CP -breaking effects on this observable are studied for the first time and the results are compatible with CP -symmetry. These results can be used to place constraints on the real and imaginary contributions of right-handed currents in BSM models. The precision of the results is dominated by the statistical uncertainty; furthermore, the dominant systematic uncertainty, due to the angular shape of the background, can be reduced with more data. Consequently, future data that will be collected by the LHCb experiment during the next decade will enable significant improvements of these results.

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